

Digital Signal and Image Processing

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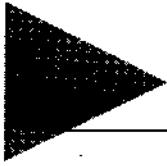
with

**Francois Meyer contributing Chapter 10 and
Mei-Qin Chen contributing the Appendix**



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Contents

►CHAPTER 1

- Fundamental Concepts 1**
 - 1.1 Signal Processing Overview 1
 - Signal Classification 2
 - A Typical DSP System 4
 - 1.2 Image Processing Basics 8
 - 2-D Signals 8
 - Overview 9
 - An Image Processing Example 12
 - 1.3 Fundamental Signals 12
 - Continuous-Time Signals 13
 - Discrete-Time Signals 16
 - Periodic Signals 19
 - Frequency in Continuous versus Discrete-Time 20
 - 1.4 Classification of Systems 21
 - Linearity 22
 - Shift-Invariance 22
 - Causal 23
 - 1.5 Characterization of LSI Systems 24
 - Difference Equations 24
 - Impulse Response 25
 - Properties of Convolution 30
 - Stability 31
 - 1.6 Implementation of Digital Filters 33
 - Filter Interconnections 34
 - FIR Filters 35
 - IIR Filters 36
 - 1.7 Basics of Random Processes 40
 - 1.8 2-D Extensions 45
 - 2-D Sequences 46
 - 2-D Systems 50
 - 1.9 Summary 53
 - 1.10 MATLAB Functions 56
 - MATLAB Help 56
 - Data Entry and Addressing 56
 - Matrix Operations 57
 - Plotting Functions 57
 - Filter Commands 58
 - Image Processing Commands 59
 - Loops and Conditions 59
 - 1.11 Problems 60
 - 1.12 Computer Experiments 70

►CHAPTER 2

- Fourier Analysis 75**
 - 2.1 Continuous-Time Fourier Analysis 76
 - Fourier Series 77
 - Continuous-Time Fourier Transform (CTFT) 80
 - 2.2 Discrete-Time Fourier Transform 83
 - DTFT Properties 87
 - Power Spectral Density 95
 - 2.3 Sampling Theory 97
 - 2.4 Decimation and Interpolation 103
 - Downsampling 103
 - Upsampling 107
 - 2.5 Discrete Fourier Transform (DFT) 110
 - Properties of the DFT 112
 - 2.6 Fast Fourier Transform 120
 - Decimation in Time FFT 120
 - Decimation in Frequency FFT 127
 - 2.7 2-D Extensions 129
 - 2-D Fourier Analysis 130
 - Computational Aspects 142
 - 2.8 Summary 147
 - 2.9 MATLAB Commands 147
 - 2.10 Problems 149
 - 2.11 Computer Projects 157

►CHAPTER 3

- Z-Transform and Digital Filters 160**
 - 3.1 Z-Transform 160
 - 3.2 Z-Transform Properties 163
 - 3.3 Inverse Z-Transform 169
 - Inverse Z-Transform Using Residues 171
 - Partial Fraction Expansion 172
 - 3.4 Causality and Stability 177
 - The Stability Triangle 178
 - 3.5 One-Sided Z-Transform 180
 - 3.6 The Linear Phase Concept 182
 - Linear Phase FIR Filters 183
 - Zero Locations of Linear Phase Filters 187
 - 3.7 State-Space Analysis 191
 - State-Space Description 191
 - Solution of the State-Space Equation 193
 - 3.8 Linear Filtering Using DFT/FFT 195
 - Overlap-Add Method 195
 - Overlap-Save Method 197

- 3.9 Computing the DFT Using Linear Filtering 197
 - The Goertzel Algorithm 198
 - The Chirp Z-Transform (CZT) 201
- 3.10 2-D Extensions 204
 - 2-D Z-Transform 205
 - Stability 208
- 3.11 Summary 215
- 3.12 MATLAB Commands 216
- 3.13 Problems 218
- 3.14 Computer Projects 225

▶CHAPTER 4

Filter Design and Implementation 228

- 4.1 FIR Filter Design 229
 - Design Using Windows 231
 - Frequency Sampling Design 239
 - Other FIR Design Methods 244
- 4.2 IIR Filter Design 245
 - Impulse Invariant Transformation 246
 - Bilinear Transformation 247
 - Analog Filter Design 250
 - Spectral Transformations 260
- 4.3 Filter Structures 265
 - FIR Structures 265
 - IIR Structures 266
 - Direct Form II_T 267
 - Lattice Structures 273
- 4.4 2-D FIR Filter Design 282
- 4.5 2-D IIR Filter Design 286
 - Shanks's Method 288
 - Iterative Design Methods 295
- 4.6 Summary 301
- 4.7 MATLAB 302
 - FIR Filter Design 302
 - IIR Filter Design 303
 - Filter Structures 304
 - 2-D Filter Design 304
- 4.8 Problems 305
- 4.9 Computer Projects 315

▶CHAPTER 5

Multirate Signal Processing 319

- 5.1 Decimation and Interpolation 320
- 5.2 Upsampling and Downsampling in the Z-Domain 321
- 5.3 FIR Filter Polyphase Structure 322
- 5.4 Filters for Decimation and Interpolation 324
- 5.5 Multistage Decimators and Interpolators 333
- 5.6 Filter Banks 337
- 5.7 Uniform DFT Filter Bank 340

- Polyphase Realization of the Uniform DFT Filter Bank 341
- 5.8 Two-Channel QMF Bank 344
 - Choices for H_0 and H_1 345
 - Perfect Reconstruction (PR) 346
 - Sufficient Condition for Alias Cancellation 347
 - Distortion 347
 - Earliest QMF 348
 - Phase and Amplitude Distortion 350
 - QMF Bank Using IIR Filters 351
- 5.9 FIR QMF Banks with PR 353
 - Half-band Filters 355
 - Design Methodology 356
- 5.10 Summary 357
- 5.11 Problems 358
- 5.12 Computer Projects 362

▶CHAPTER 6

Finite-Wordlength Effects 365

- 6.1 Number Representations 366
 - Fixed Point Numbers 366
 - Floating Point Numbers 369
- 6.2 Coefficient Quantization 371
 - Coefficient Quantization in FIR Filters 374
- 6.3 Quantization Noise Analysis 378
 - First-Order Filter 378
 - Second-Order Direct Form II 382
- 6.4 Overflow Effects in Fixed Point Digital Filters 386
- 6.5 Scaling IIR Filters to Prevent Overflow 393
 - Bounded Input 393
 - Sinusoidal Input 394
 - General Scaling Rules 395
 - Effect on SNR 398
- 6.6 Effects of Product Quantization 398
 - Rounding 398
 - Magnitude Truncation 404
 - Two's Complement Quantization 406
- 6.7 Summary 413
- 6.8 Appendix 414
- 6.9 MATLAB 415
- 6.10 Problems 416
- 6.11 Computer Projects 419

▶CHAPTER 7

Adaptive Signal Processing 422

- 7.1 The Correlation Matrix and Some Linear Algebra 426
- 7.2 The Wiener Filter 438
- 7.3 Gradient Search Algorithms 441
 - Steepest Descent Algorithm 442

- 7.4 The LMS Algorithm 445
 - Convergence 448
 - Misadjustment 450
 - Noise Cancellation 456
 - Computer Experiments 457
 - Normalized LMS Algorithm 458
 - 7.5 Frequency-Domain Adaptive Filtering 463
 - Computational Complexity 466
 - Convergence 466
 - 7.6 Block LMS Algorithm 467
 - Computational Complexity 468
 - Convergence 468
 - 7.7 Fast LMS Algorithm 470
 - Computational Complexity 472
 - 7.8 Summary 473
 - 7.9 Problems 476
 - 7.10 Computer Projects 479
- CHAPTER 8**
Least-Squares Adaptive Algorithms 483
- 8.1 The RLS Algorithm 483
 - Performance Evaluation 488
 - Channel Equalization 491
 - 8.2 EDS and Fast-EDS Algorithms 494
 - Jacobi and Gauss-Seidel Methods 494
 - The EDS Algorithm 496
 - The Fast EDS Algorithm 500
 - 8.3 ADPCM 506
 - 8.4 2-D Adaptive Algorithms 509
 - The 2-D LMS Algorithm 509
 - The 2-D FEDS Algorithm 511
 - 8.5 Image Restoration 513
 - 8.6 Summary 513
 - 8.7 Problems 515
 - 8.8 Computer Projects 515
- CHAPTER 9**
Linear Prediction 520
- 9.1 Forward Prediction 520
 - 9.2 Backward Prediction 524
 - 9.3 Levinson-Durbin Algorithm 527
 - 9.4 Properties of the Prediction Error Filter 531
 - 9.5 Joint Process Estimator 532
 - 9.6 Adaptive Lattice Filter 534
 - 9.7 Speech Coding 535
 - Waveform Coder 537
 - Transform Coder 540
 - Subband Coder 541
 - Linear Predictive Coder (LPC) 543
 - Linear Prediction Analysis-by-Synthesis (LPAS) Coder 547
 - 9.8 Summary 548
 - 9.9 Problems 549
 - 9.10 Computer Projects 550
- CHAPTER 10**
Image Processing Fundamentals 552
- 10.1 Image Enhancement 553
 - Grayscale Transformation 553
 - Contrast Stretching 554
 - Gamma Correction 555
 - Histogram Equalization 558
 - Unsharp Masking 561
 - 10.2 Image Interpolation 562
 - Linear Interpolation 566
 - Polynomial Interpolation 567
 - 10.3 Edge Detection 570
 - Definition of an Edge 572
 - Finite Differences 573
 - Roberts Edge Detector 575
 - Sobel and Prewitt Edge Detectors 575
 - Marr-Hildreth Edge Detection 578
 - Canny Edge Detector 581
 - 10.4 Image Restoration 586
 - Choices of Norms for Measuring Image Quality 586
 - Inverse Filtering and De-convolution 587
 - Removal of Additive Noise 590
 - 10.5 Color Imaging 599
 - Light and Pigments 599
 - Color Perception 599
 - Trichromacy and the Reproduction of Color 602
 - Color Models 606
 - Color Enhancement 609
 - Color Image Filtering 609
 - 10.6 Summary 612
 - 10.7 Problems 613
 - 10.8 Computer Projects 617
- CHAPTER 11**
Image Compression and Coding 623
- 11.1 Image Transforms 625
 - 1-D DFT 625
 - General Orthonormal Transform 627
 - 2-D DFT 629
 - 1-D DCT 632
 - 2-D DCT 639
 - Discrete Sine Transform 640
 - Hadamard Transform 641
 - KL Transform 644
 - 11.2 Pixel Coding 647

Huffman Coding 648
 LZW Coding 649
 11.3 DPCM of Images 651
 Simulation Results 655
 11.4 JPEG Standard 656
 JPEG Lossy Image Compression Standard 658
 JPEG Lossless Image Compression
 Standard 665
 11.5 Summary 666
 11.6 Problems 666
 11.7 Computer Projects 669

► **APPENDIX**

Concepts of Linear Algebra 672

A.1 Notations 672
 A.2 Basic Operations 673
 Transpose and Hermitian 673
 Trace of a Square Matrix 673
 Dot Product (or Inner Product) and
 Orthogonality 674
 Matrix Addition and Scalar Multiplication 674
 Matrix Multiplication 675
 Partitioned Matrices 676
 A.3 Determinant of a Square Matrix 677
 Determinant 677
 Singular and Nonsingular Matrices 678
 A.4 Linear Independence of Vectors, Basis Vectors,
 and Rank of a Matrix 678
 Linear Independence of Vectors 678
 Basis Vectors 679
 Rank of a Matrix 680
 A.5 Inverse of a Square Matrix 680
 A.6 Eigenvalues and Eigenvectors of a Square
 Matrix and Spectral Radius 682
 Eigenvalues and Eigenvectors of a Square
 Matrix 682

Spectral Radius of a Square Matrix 684
 A.7 Kronecker Product and Kronecker Sum 684
 Kronecker Product 684
 Kronecker Sum 685
 A.8 Vector Norms, Matrix Norms, and Condition
 Numbers 686
 Vector Norms 686
 Matrix Norms 686
 Condition Numbers 688
 A.9 Similarity Transformation 688
 A.10 Special Matrices and Properties 689
 Symmetric and Hermitian Matrices 689
 Normal Matrices 690
 Orthogonal and Unitary Matrices 690
 Positive Definite and Semidefinite
 Matrices 690
 Vandermonde Matrices 691
 Circulant Matrices 691
 Toeplitz Matrices 692
 Hankel Matrices 693
 Hadamard Matrices 693
 A.11 Diagonalization, Unitary Triangularization, and
 Jordan Form 694
 Diagonalization 694
 Unitary Triangularization 695
 Jordan Canonical Form 695
 A.12 Singular Values, Singular Value Decomposition,
 and Pseudo-Inverses 695
 Singular Values 695
 Singular Value Decomposition 696
 Pseudo-inverses 696
 A.13 Summary 697

 Index 698