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Discrete Element Modelling of Rock Creep Behaviour using Rate Process Theory

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Complete List of Authors:	Gutiérrez-Ch, José; Univ Politecnica Madrid Senent, Salvador; Univ Politecnica Madrid Estebanez, Eduardo; Univ Politecnica Madrid Jimenez, Rafael; Univ Politecnica Madrid
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29 **1. Introduction**

30 The time-dependent (creep) behaviour of rocks is an essential factor for many
31 geotechnical projects, such as caverns and tunnels (Zhang et al. 2012; 2015),
32 rock-bolts and rock anchors (Wyllie 1999) or rock-socketed piles (Tang et al.
33 1994); as well as for other topics such as underground storage of radioactive waste
34 and geothermal energy (Dahhaoui et al. 2017) or mining and petroleum
35 engineering applications (Hamza and Stace 2018).

36 Creep is a progressive and time dependent deformation associated with a plastic
37 deformation that many geomaterials –e.g., soils, rocks, etc.– exhibit under a state
38 of constant homogeneous stress (Brantut et al. 2012; 2013; Kuhn and Mitchel
39 1992). Such time-dependent behaviour can be studied through in-situ or laboratory
40 creep tests; however, laboratory tests are often preferred because the range of
41 temperature and pressure required to reproduce field conditions is easier to
42 provide and control, so that their associated cost is often less than the cost of in-
43 situ tests (Dusseault and Fordham 1993; Roy and Rao 2015). Although some
44 standards to conduct creep tests in the laboratory have been proposed (see e.g.,
45 ISRM 2007; ASTM D7070-16 2016), the creep behaviour of rocks has been
46 studied using different types of laboratory creep tests, such as oedometric
47 compression (Mohajerani et al. 2011), direct shear (Larson and Wade 2001; Zhang
48 et al. 2011), uniaxial compression (Yang et al. 1999), or triaxial compression
49 (Zhang et al. 2012; 2015; Liu et al. 2018).

50 Laboratory creep tests reported in the literature have analyzed different rock types,
51 such as fine-grained clastic rocks (Larson and Wade 2001; Mohajerani et al. 2011;
52 Hamza and Stace 2018; Liu et al. 2018; Gent et al. 2018); sandstone (Brantut et al.
53 2014; Cao et al. 2014) and other clastic rocks (Zhang et al. 2013; 2015); slate (Min
54 et al. 2014); salt rock (Li et al. 2018); or limestone (Cogan 1976; Maranini and
55 Brignoli 1999; Brantut et al. 2014), shale (Cogan 1976), marble (Zhao et al. 2012),
56 and granite (Kranz 1980; Fujii et al. 1999; He et al. 2016;) and other crystalline
57 rocks (Damjanac and Fairhurst 2010). These investigations have emphasized on
58 different aspects of creep behavior such as microstructure state, clay content,
59 relative humidity, water content and chemistry of the pore fluid, temperature,
60 deviatoric stress and effective pressure.

61 Many theoretical frameworks have been proposed to explain and interpret the
62 creep behaviour of materials (see e.g., Dusseault and Fordham 1993). The Burger
63 model, for instance, has been commonly employed to model rock creep (see
64 Zhang et al. 2015; Hamza and Stace 2018); this model, however, cannot
65 reproduce the accelerating strains associated to tertiary creep –a phase of creep
66 behaviour in which strain rate increases rapidly and rock failure occurs, see
67 Section 2– (Xu et al. 2013; He et al. 2016). This is also true for other models, for
68 example based on the sliding wing crack (Ashby and Sammis 1990; Brantut et al.
69 2012). Methods to describe rate-dependent material failure, and to anticipate the
70 onset of failure under creep conditions, have also been proposed (Voight 1989).

71 Kuhn and Mitchel (1992,1993) demonstrated that the rate process theory of Eyring
72 (1936) –a theory that describes the sliding velocity between particles as a function

73 of their tangential-to-normal force ratio, among other factors– could be employed to
74 describe soil creep. For instance, the rate process theory has been shown to
75 successfully explain, without an explicit dependence of strain rate on time, the
76 dependence of creep strain on stress level and temperature; furthermore,
77 intrinsically time-dependent mechanisms can be observed if an assembly of
78 particles –like in a discrete element model– is considered (Kuhn and Mitchel 1992;
79 Kwok and Bolton 2010).

80 Numerical methods –such as the Finite Element Method (FEM) or the Distinct
81 Element Method (DEM)– have also gained recent attention to study the creep
82 behaviour of rocks and rock masses (Kemeny 2005; Lisjak and Grasseli 2014). In
83 particular, the DEM approach, in conjunction with the rate process theory, has
84 been shown to be particularly useful to model soil creep (Kuhn and Mitchel
85 1992;1993; Kwok and Bolton 2010; Liu et al. 2019). Similarly, Li et al. (2017; 2018)
86 have studied the creep of salt rocks employing the DEM and the Burger model.
87 However, Kuhn and Mitchel’s model has been developed and employed for sandy
88 soils, and there is still an open research question regarding its applicability for rock
89 materials subjected to creep.

90 In this work, the DEM and the rate process theory are employed to simulate rock
91 creep. To that end, the results of laboratory uniaxial compression creep tests (on
92 intact slate samples), that were available in the context of the construction project
93 for a high speed railway tunnel (Ministerio de Fomento, 2012), are used as a
94 benchmark to calibrate and validate the results of the numerical models developed
95 in this work.

96 2. Fundamentals of creep modelling using rate process theory

97 An idealized creep behaviour consists of the following main phases (see **Fig. 1**):
 98 first, an almost instantaneous elastic strain occurs as a response to a rapid load
 99 increase, until a specified stress value is reached (A→B); then, if a sufficiently high
 100 stress is maintained, the following three stages could be noted: (i) the strain
 101 increases with a strain rate that decreases with time (primary creep, B→C); (ii)
 102 then, a stage with a quasi-constant strain rate follows (secondary creep C→D); and
 103 finally, (iii) the strain accelerates and rock failure occurs (tertiary creep, D→E)
 104 (Hamza and Stace 2018).

105 **[Fig. 1 approx. here]**

106 Kuhn and Mitchel (1992; 1993) proposed that creep strain occurs due to sliding
 107 between particles, so that the sliding velocity (\dot{s}) at each contact between particles
 108 depends on its tangential-to-normal force ratio (f^t/f^n) which can change during
 109 deformation even under constant boundary stresses (Mitchell and Soga 2005). The
 110 relationship between sliding velocity and tangential-to-normal force ratio can be
 111 modelled using the rate process theory proposed by Eyring (1936). The
 112 constitutive equation of rate process theory can be written as (Kuhn and Mitchel
 113 1992):

$$\dot{s} = \lambda \frac{2kT}{h} e^{\frac{-\Delta F}{RT}} \sinh \left(\frac{1}{2kTn_1} \frac{f^t}{f^n} \right) \quad (1)$$

114
 115 where λ is the flow unit, k is Boltzmann's constant ($1.381 \times 10^{-23} \text{ J K}^{-1}$), T is the
 116 absolute temperature (K), h is Planck's constant ($6.626 \times 10^{-34} \text{ J s}$), ΔF is the

117 activation energy (kJ mol^{-1}), R is the universal gas constant ($8.314 \times 10^{-3} \text{ kJ K}^{-1}$
118 mol^{-1}), n_1 is the number of bonds per unit of normal contact force (bonds/N), and
119 f^t/f^n can be expressed as the friction coefficient at contacts between particles ($\mu =$
120 f^t/f^n).

121 The main aspects of rate process theory that affect creep behaviour of a DEM
122 model are (these explanations are mainly based on Mitchell and Soga 2005, where
123 additional details can be found):

- 124 a) The activation energy (ΔF) represents the energy that a particle needs to
125 slide with respect to another particle, so that both are in equilibrium. The
126 activation energy controls the breakage of strong bonds and depends on the
127 material: e.g., soils have an activation energy of about 40 to 400 kJ/mol ,
128 metals of around 210 kJ/mol , etc.
- 129 b) The flow unit (λ) is the separation distance between successive equilibrium
130 positions in the interparticle contact structure, so that an amount of energy Δ
131 F is needed to move the particles from one position to another. This
132 movement, of magnitude equal to λ , could cause a single bond to break, or
133 the simultaneous breakage of several bonds.
- 134 c) The number of bonds (n_1) at any contact depends on the compressive force
135 transmitted at the contact –e.g., the number of bonds is directly proportional
136 to the effective consolidation pressure for normally consolidated clays– so
137 that the macroscopic strength is directly proportional to the number of
138 bonds.

- 139 d) An increase in temperature (T) decreases the strength and the sliding
140 velocity (\dot{s}) at each contact, so that (i) creep rates increase and (ii) the
141 relaxation stresses corresponding to specific values of strain decrease.
- 142 e) The friction coefficient at contact particles ($\mu = f^t/f^n$) represents the “visco-
143 frictional” nature of interparticle sliding (Eyring 1936). A decrease in the
144 friction coefficient decreases the sliding velocity (\dot{s}) at every contact.

145 3. Fundamentals of DEM modelling with PFC

146 The Particle Flow Code (PFC) is the commercial code developed by Itasca
147 Consulting Group Inc. (2014) used in this paper. PFC employs a distinct element
148 modeling framework (Potyondy and Cundall 2004) to simulate the behaviour of
149 different materials composed by a collection of rigid and finite-sized particles with a
150 random distribution of sizes, and that can translate and rotate independently to
151 each other. These particles interact at pair-wise contacts with internal forces and
152 moments. Newton’s second law, together with a force-displacement law, are
153 employed to control the interactions between particles, to assess the contact
154 forces, and to calculate particle displacements. In particular, the system evolution
155 is computed using an explicit dynamic scheme –a time-stepping algorithm– to
156 solve Newton’s laws of motion (Itasca Consulting Group Inc. 2014).

157 To model the interactions between particles, PFC provides a Bonded-Particle
158 Model (BPM) (Potyondy 2015) with several possible bond/contact models –e.g.,
159 Linear Model (LM), Linear Parallel Bond Model (LPBM), Flat-Joint Contact Model
160 (FJCM), etc.– that can mimic the macroscopic behaviour of bonded materials (such

161 as rock). In the BPM, the LM models the behaviour of an infinitesimal interface –
162 which does not resist rotation– with linear and dashpot components (see **Fig. 2a**).
163 The linear component simulates linear elastic frictional behaviour –non-tension
164 springs with constant normal and shear stiffness–, while the dashpot reproduces
165 viscous behaviour (Itasca Consulting Group Inc. 2014). On the other hand, the
166 FJCM simulates the contact between particles using locally notional (bonded or
167 unbonded) surfaces discretized into elements (see **Fig. 2b**) (Potyondy 2012). In
168 FJCM, the behaviour of bonded interfaces is linear elastic until the bond strength is
169 reached and the bond breaks, hence making the interface unbonded (Itasca
170 Consulting Group Inc. 2014). Unbonded interfaces have a linear, elastic and
171 frictional behaviour. In the LM and the FJCM, the slip is simulated by imposing a
172 Coulomb limit on the shear force through the friction coefficient. For additional
173 details, see Potyondy (2015) and Itasca Consulting Group Inc. (2014).

174 **[Fig. 2 approx. here]**

175 Following Li et al. (2017), we simulate rock creep behaviour using a DEM model
176 with a mixture of different models of contact between particles; in particular, a
177 mixture of LM and FJCM is employed, but with a significant preponderance of the
178 FJCM with respect to the LM. FJCM is selected due to its ability to reproduce the
179 behaviour of rock under direct tension and compression tests (Potyondy 2012);
180 and, in particular, for its ability to reproduce the behaviour of intact rocks with a
181 uniaxial compressive strength to tensile strength (σ_c/σ_t) ratio of more than 10
182 (Bahaaddini et al. 2019) –which is on the order of the σ_c/σ_t ratio reported by
183 Ministerio de Fomento (2012) for rocks similar to those considered in this work–.

184 Note, however, that several LM contacts are necessary to model creep, as almost
 185 no creep occurs when they are removed from the DEM model (the selection of LM-
 186 to-FJCM contact ratio is based on a sensitivity analysis, see Section 5.2).

187 Different to the approach by Li et al. (2017) –who used the Burger and linear
 188 parallel bond models–, the rate process theory has been implemented into the
 189 DEM numerical model. To do that, Eq. (1) has been rewritten as:

$$\dot{s} = \alpha \sinh(\beta \mu) \quad (2)$$

190 Or approximately:

$$\dot{s} \approx \frac{\alpha}{2} e^{\beta \mu} \quad (3)$$

191 Where:

$$\alpha = \lambda \frac{2kT}{h} e^{\frac{-\Delta F}{RT}} \quad (4)$$

$$\beta = \frac{1}{2kTn_1} \quad (5)$$

192
 193 According to Kuhn and Mitchell (1992,1993) and using the parameters listed in
 194 **Table 1**, Eq. (3) can be simplified to Eq. (6) (see **Fig. 3**). Note that, since the main
 195 objective of this work is to validate the viability of the rate process theory to
 196 qualitatively simulate creep in rocks, the influence of rate process theory
 197 parameters are not studied; for a recent discussion on the influence of these
 198 parameters on the evolution of creep (in soils) see Liu et al. (2019).

$$\dot{s} \approx 2.727 \times 10^{-15} e^{37\mu} \quad (6)$$

199 **[Table 1 approx. here]**

200 **[Fig. 3 approx. here]**

201 Next, Eq. (6) has been implemented into the PFC model as a Visual C++ function
202 that is compiled as a Dynamic Link Library (DLL) file, hence providing a 10-100-
203 fold efficiency increase in relation to its implementation as a FISH function (Itasca
204 Consulting Group Inc. 2014). (FISH is the internal programming language in PFC
205 that enables the user to interact with PFC models, Itasca Consulting Group Inc.
206 2014). With this function, and at each time-stepping of the DEM simulation: (i) the
207 sliding velocity (\dot{s}) at each ball-ball contact –i.e., the tangential component of their
208 relative velocity– is computed; and (ii) the corresponding friction coefficient (μ) of
209 the contact model –i.e., LM or FJCM– is modified using Eq. (6) and **Fig. 3**. For
210 additional details about the DEM implementation of rate process theory, see Kuhn
211 and Mitchell (1992,1993) and Kwok and Bolton (2010).

212 **4. Laboratory tests**

213 As comparison benchmark, we employ the results of compression creep tests
214 conducted on intact slate samples available from Ministerio de Fomento (2012)
215 (Note that, since tests were conducted by others, we will not discuss the
216 experimental design in detail; rather, we will employ the available test results as a
217 comparison benchmark of our numerical tool so that, given the existing
218 experimental uncertainties, our goal is to reproduce the creep behaviour of soft
219 rock in a qualitative way only). For completeness, however, a short description of
220 the rock and tests analyzed is presented next.

221 The samples of natural slate used in this work were obtained from cylindrical cores
222 from boreholes drilled in the Nogueira Group from the Galicia-Trás-Os-Montes
223 Zone (north of Spain) during geotechnical investigations for Del Espino tunnel

224 (Ministerio de Fomento 2012). These are rocks of the Silurian Period, and samples
225 were taken at depths ranging from 41.8 m to 93.9 m. The cylindrical samples to be
226 tested were saw-cut to have a height-to-diameter ratio (H/D) of about 2.2, with
227 $D = 62.1$ mm. To identify the mineralogical composition of the rock samples, optical
228 microscopic tests were conducted. **Table 2** lists the mineral composition and its
229 corresponding grain size of the two slate samples analyzed herein.

230 **[Table 2 approx. here]**

231 There are several ways to conduct compression creep tests in the laboratory
232 (Dusseault and Fordham 1993; Maranini and Brignoli 1999): for instance, tests with
233 steps of constant stress ($\sigma = \text{constant}$), tests with constant strain rate ($\dot{\varepsilon} =$
234 constant), or relaxation or constant strain tests ($\varepsilon = \text{constant}$). In this work, we
235 employ experimental data from uniaxial compression multistage creep tests
236 (UCMCTs). In these tests, stress levels are increased in steps (or stages), so that
237 the associated strains were measured during the duration of each step. In
238 particular, such UCMCTs were conducted at room temperature on two slate
239 samples (Sample 1 and Sample 2). For each new loading step, the corresponding
240 load increment was applied first, under a loading rate of about 0.35 MPa/s; then,
241 the axial stress (σ_1) was kept constant for a specified time interval, during which
242 the axial (ε_1) and the transverse (ε_3) strains were continuously monitored using two
243 strain gauges with 2 cm length adhered to the rock sample at approximately one
244 half of its height. The results of these laboratory tests will be presented in **Fig. 8**
245 and **Fig. 9**, where the results of the numerical models will be also included. The
246 physical time of the UCMCTs on Sample 1 and Sample 2 were 94 and 71 hours,

247 respectively. Note also that the samples fail during different test stages: Sample 1
248 fails during one large load increment, whereas Sample 2 fails during creep
249 associated to a constant stress. **Fig. 4** shows the evolution, for each loading step,
250 of the elastic increments –i.e., without considering creep– of axial strain computed
251 from the elastic portions of the stress-strain curve measured in the laboratory. The
252 Young’s modulus computed for such elastic portions of the stress-strain curves are
253 almost constant for all the loading stages, except for the first ones, where the
254 behavior of the samples is more rigid. (A possible interpretation for this behaviour
255 is discussed below.)

256 **[Fig. 4 approx. here]**

257 **5. Set-up of the numerical model to simulate rock creep tests in DEM**

258 This work aims to reproduce the rock creep behaviour measured in the laboratory
259 using two-dimensional DEM numerical models that implement the rate process
260 theory. To that end, the DEM micromechanical parameters of the LM and of the
261 FJCM are calibrated against the experimental data; i.e., against the results of the
262 available uniaxial compression multistage creep tests (UCMCT). The procedure is
263 discussed next.

264 **5.1 Numerical uniaxial compression creep test**

265 To conduct the numerical UCMCT, a numerical sample composed of cylindrical
266 particles needs to be generated first. To that end, the procedure proposed by
267 Potyondy and Cundall (2004) is used. Its steps are:

268 1) *Initial particle assembly*: a container of the same height as the sample
269 (136.7 mm) and consisting of four planar frictionless walls is filled with an
270 assembly of randomly placed particles. (For illustration, see **Fig. 5a** in which
271 fewer particles are shown than those employed in the actual simulations:
272 3956 particles were employed in our simulations in Samples 1 and 2).

273 2) *Application of an isotropic initial stress*: to reduce the locked-in forces and
274 to get a better distribution of contacts, the radii of all particles are iteratively
275 changed, without still removing the boundary walls, until a specified isotropic
276 stress ($\sigma_o^c \cong 1\%$ of the uniaxial compressive strength) is reached. To do this,
277 measurement circles (e.g., three circles) are installed inside the container
278 and the isotropic stress ($\sigma_o = (\sigma_{11} + \sigma_{22})/2$) within each auxiliary circle is
279 computed for each step (see **Fig. 5b**). The process finishes when the
280 normalized difference $((\sigma_o^c - \sigma_o)/\sigma_o^c)$ is less than the isotropic stress
281 tolerance (σ_{tol}); in agreement with previous works (Bahaaddini et al. 2014;
282 Gutiérrez-Ch et al. 2018), $\sigma_{tol} = 0.5$ is used.

283 3) *Elimination of floating particles*: during the previous steps, “floating”
284 particles with less than three contacts can appear (see **Fig. 5c**). At this step,
285 the radii of floating particles are increased until all particles away from the
286 specimen boundaries have at least three contacts.

287 4) *Application of the linear and flat-joint contact model*: linear and flat-joint
288 contacts are installed depending on the gap between adjacent particles (g)
289 and the given control gap value (g_c). In DEM models, g represents the

290 distance between balls at their contact, which could be (i) greater than zero
291 or (ii) less than zero, or (iii) equal to zero, depending on the genesis of the
292 DEM specimen (see **Fig. 6**). Therefore, the control gap (g_c) is a control
293 distance employed to decide whether the LM or the FJCM are applied to
294 that contact. The decision is made depending on the value of g resulting
295 after the random generation of particles. To do that, a FISH function was
296 used to check the particle-particle gap at each contact, and to assign to it
297 the FJCM (if $g < g_c$) or LM (if $g \geq g_c$) (see **Fig. 5d**). Consequently, g_c allows
298 us to calibrate the LM-to-FJCM contact ratio, as explained in Section 5.2.
299 The micromechanical parameters of such linear and flat-joint contacts, as
300 well as the LM-to-FJCM contact ratio of each model, are listed in **Table 3**.
301 As indicated, there is a clear preponderance of FJCM with respect to the
302 LM. This differentiates our analyses from previous works on soil creep using
303 the rate process theory, in which only a cohesionless LM was employed
304 (Kuhn and Mitchel 1993; Kwok and Bolton 2010).

305 *5) Remove the lateral walls:* the sample-genesis procedure is completed by
306 (i) deleting the lateral (planar and frictionless) walls of the container and (ii)
307 stepping the DEM algorithm until static equilibrium (see **Fig. 5e**).

308 Next, the following three steps (which were added in this work to reproduce the
309 conditions of the sample in the laboratory) are applied to the generated sample:

310 *6) Initial stress:* the sample is loaded vertically up to an initial axial stress (σ_i)
311 that could represent a valid initial situation of the laboratory tests after the
312 upper platen is placed on the rock sample (see **Fig. 7a**). The initial stress

313 value has been calibrated so that, right after the application of the first
314 loading stage of the test (step 7) (i.e. without considering any creep), the
315 axial strain (ε_1) in the numerical model equals the axial strain in the
316 laboratory test. Thereby, this value of axial strain serves as a reference for
317 the rest of the test, allowing the comparison between numerical and
318 laboratory results. Consequently, the axial and transverse strains (ε_1 and ε_3 ,
319 respectively) obtained in this stage were neglected in subsequent analyses.

320 7) *Compression phase*: next, similar to Kwok and Bolton (2010), the
321 numerical sample is loaded vertically at a constant strain rate $\dot{\varepsilon}_1$ of 5 %/s –
322 i.e., a constant velocity of 0.003 m/s is applied at the top and bottom walls–
323 until the sample reaches the axial stress (σ_1) of the first stage of the
324 laboratory test (see **Fig. 7b**).

325 8) *Creep phase*: after the numerical sample has reached the specified axial
326 stress (σ_1) corresponding to the first loading stage, the rock sample is
327 allowed to creep while σ_1 is kept constant for a specified time interval. Such
328 operation can be conducted employing the servo-control mechanism of
329 PFC^{2D}, which allows one to control the translational velocity of selected
330 walls, so that a desired force can be applied or maintained on them (see
331 **Fig. 7c**). During this phase, the RPT is implemented using Eq. (6), which
332 allows one to compute the friction coefficient associated with the sliding
333 velocity (\dot{s}) between ball-ball contacts (for each time step). Then, such
334 friction coefficient is applied to the model representing each corresponding

335 ball-ball contacts: i.e., the friction coefficient of the LM or FJCM applied to
336 each ball-ball contact is modified at each time step.

337 At the first creep stage, and since the simulated time of the DEM test (t_{DEM}) is
338 different from the physical time of the laboratory test (t_{lab}), their relationship can be
339 calculated using the ε_1 reached after the first creep phase at the laboratory test as
340 a benchmark. To that end, when the ε_1 reached at the first creep phase of the DEM
341 test is equal to that obtained in the laboratory test, it is assumed that the
342 corresponding t_{DEM} is equivalent to t_{lab} , and a time scaling relationship can be
343 obtained (see **Table 3**). Such relationship (t_{DEM}/t_{lab}) allows us to compare results
344 qualitatively (as done in Figs **9** and **10**) and to define the creep time in the DEM
345 simulations of subsequent stages, as described next.

346 **[Table 3 approx. here]**

347 For multistage tests, such as the UCMCTs considered herein, steps 7 and 8 must
348 be repeated until a maximum stress value (σ_{peak}) is reached and rock failure
349 occurs. The creep time (t_{DEM}) in each loading stage –i.e., the time interval during
350 which the axial stress is kept constant–, is calculated from the corresponding
351 laboratory time (t_{lab}) interval using the t_{DEM}/t_{lab} scaling factor calculated in step 8.

352 During the UCMCT, the axial stress (σ_1) is obtained by dividing the average force
353 reaction on the top and bottom walls by the sample cross-sectional area, while the
354 axial and transverse strains (ε_1 and ε_3 , respectively) are computed using a
355 measurement circle (Itasca Consulting Group Inc. 2014) with a 2 cm diameter –i.e.,
356 equivalent to the length of the strain gauges employed during laboratory tests–

357 installed at the center of the sample (see **Fig. 7a**). (Note that the cross-section of
358 the sample changes during the test and such change is considered to compute σ_1).
359 Since the lateral walls needed to generate the sample are deleted, the change in
360 the cross section of the sample is measured by tracking the displacement of two
361 “gage particles”: i.e., one particle at the right of the model and another at the left
362 (see the blue balls in **Fig. 7**).

363 **[Fig. 5 approx. here]**

364 **[Fig. 6 approx. here]**

365 **[Fig. 7 approx. here]**

366 **5.2 Calibration of micromechanical parameters of intact materials**

367 Several procedures have been published in the literature to calibrate DEM
368 micromechanical parameters, with results of the experimental uniaxial compression
369 strength (UCS) tests being commonly used as benchmark (see e.g., Potyondy and
370 Cundall 2004; Bahaaddini et al. 2014; Castro-Filgueira et al. 2017). This is
371 probably because the UCS test of intact rocks can be estimated using relatively
372 straightforward and cost-effective techniques, hence being one of the most
373 commonly available and practical rock properties used in rock engineering (Shen
374 et al. 2014). However, in this work, UCS tests are not available for the samples
375 tested under creep, so that the calibration of the micromechanical parameters of
376 the LM and the FJCM was conducted through a variation of the methodology
377 proposed by Gutiérrez-Ch et al. (2018), in which the specific features of the
378 UCMCT were considered.

379 The calibration procedure is iterative, and it starts by matching the macroscopic
380 Young's modulus (E) of the linear (or elastic) portions of the strain-stress curves,
381 which mainly depends on the effective modulus of the particles and of the flat-joints
382 (E^* and $\overline{E^*}$); next, the cohesion (c) and tensile strength (σ_t) of the flat-joint are
383 adjusted to reproduce the maximum stress value (σ_{peak}) reached at the UCMCT. In
384 the latter adjustment, the friction angle (ϕ) is not considered, since a specific value
385 of 30° , as proposed in the tunnel Project, is employed. (For more details about the
386 calibration procedure, see Gutiérrez-Ch et al. 2018). The particle effective modulus
387 (E_{LM}^*) and normal-to-shear stiffness ratio (k_{LM}^*) for the LM were the same as those
388 employed for the FJCM. According to Kuhn and Mitchell (1992, 1993), and given
389 that the rate process theory was incorporated into the PFC^{2D} numerical model,
390 hence affecting the interactions between particles, no other damping –i.e., no other
391 dashpot component– was required to be used in the LM. As indicated, the purpose
392 of the present work is to analyse the use of DEM, in conjunction with the rate
393 process theory, to simulate rock creep. Therefore, the influence of other
394 parameters affecting a DEM model –e.g., particle size distribution, etc.–, are not
395 considered. Note also that there might be different sets of micro-parameters that
396 could reproduce a similar trend so that, it might be necessary to conduct a detailed
397 study to optimize the calibration procedure, which is however out of the scope of
398 this work.

399 Also, during the calibration procedure, a sensitivity analysis is conducted to select
400 the LM-to-FJCM contact ratio to be employed. The first loading stage on Sample 1
401 –i.e., under a constant axial stress of 3.3 MPa– is employed to illustrate this, as

402 shown in Figure 8. (To facilitate the visualization, since the laboratory test time is
403 different to the simulation time used in DEM^{2D}, test times have been normalized
404 with respect to their maximum values corresponding to the end of this loading
405 stage). Results in **Fig 8** illustrate that an almost negligible creep strain occurs when
406 a LM-to-FJCM contact ratio of 0% is used; therefore, LM-to-FJCM contact ratio
407 must be increased to reproduce the creep behavior. Using a “trial and error”
408 approach, a LM-to-FJCM contact ratio of 17.5 % is selected, as it is the one
409 producing a better fit to the macroscopic rock creep behaviour of Sample 1 (see
410 **Fig. 8**). **Table 1** lists the values employed for the rate process theory parameters.
411 **Table 4** lists the micromechanical parameters obtained after the calibration, and
412 **Table 5** compares the macroscopic UCMCTs results $-\sigma_{peak} E-$ obtained in the
413 laboratory for Samples 1 and 2 with those computed with DEM.

414 **[Fig. 8 approx. here]**

415 **[Table 3 approx. here]**

416 **[Table 4 approx. here]**

417 **6. Results**

418 **6.1 Strain evolution during creep tests**

419 Two (2) numerical uniaxial compression multistage creep tests (UCMCT) were
420 conducted with DEM to simulate, with the procedure explained in Section 5.1, the
421 creep behaviour on the slate rock described in Section 4.

422 **Fig. 9a** and **Fig. 10a** illustrate the stress “stages” employed during each UCMCT
423 conducted in the laboratory. **Fig. 9b** and **Fig. 10b** compare (i) the evolutions of

424 strain measured in the laboratory with (ii) the evolutions of strain computed with the
425 calibrated DEM models that use the rate process theory. Since the laboratory test
426 times (t_{lab}) are different from the simulated times (t_{DEM}) in DEM, t_{DEM} axes have
427 been scaled, according to the t_{DEM}/t_{lab} factors (see Section 5.1), to allow a
428 qualitative comparison between DEM and laboratory results. The DEM results,
429 except for the first 2-3 loading steps, are quite similar to the laboratory results,
430 hence suggesting that DEM models based on rate process theory, when properly
431 calibrated, can be an adequate tool to model the creep behaviour of slate rocks.
432 Furthermore, the results obtained from DEM are consistent with the results
433 reported by Zhang et al. (2011), in which a fluctuating behavior is not present,
434 demonstrating that creep strain in the numerical simulation is continuous over time.

435 The main differences between the DEM models and the laboratory tests occur
436 during the initial loading steps –when creep is still not a main aspect controlling the
437 strain behaviour of the samples–. This is expected, considering (i) the variation of
438 the sample stiffness during the loading stages shown in **Fig. 4**, and (ii) that each
439 DEM model has been calibrated employing a constant Young’s modulus. Although
440 the reason for this behavior in the laboratory tests is not completely clear, we argue
441 that this is probably because the vertical strain field in the sample is still not
442 homogenous during the initial test stages (due, for instance, to end effects).

443 **[Fig. 9 approx. here]**

444 **[Fig. 10 approx. here]**

445 Importantly (since many creep models cannot reproduce tertiary creep), **Fig. 9** and
446 **Fig. 10** also show that DEM models based on rate process theory are suitable to
447 simulate all stages (i.e., including tertiary creep) of a theoretical creep curve, such
448 as that presented in **Fig. 1**. For the lower axial stresses (σ_1) associated with the
449 initial loading stages, note (i) that only an “instantaneous” elastic strain and the
450 initial phases of creep –i.e., primary and secondary creep– are observed, and (ii)
451 that such creep strains are still minor during the initial loading stages. As an
452 example, the detail in **Fig. 9** (corresponding to the $\sigma_1 = 16.5$ MPa step) illustrates
453 the separation between primary creep (with diminishing rates of strains) and
454 secondary creep (with constant strain rate). Similarly, the DEM model can
455 reproduce the tertiary creep of the samples. This is more clearly illustrated on
456 Sample 2, as this sample fails during the creep phase associated with the last
457 loading steps of $\sigma_1 = 31.35$ MPa. (As indicated, Sample 1 fails during the load
458 increment, so that tertiary creep is not observed). Again, these numerical results
459 suggest that rate process theory and DEM are able to reproduce both types of
460 failure without any user-defined intervention: i.e., to reproduce failure during a load
461 increment; or to reproduce failure under tertiary creep for a constant load. (These
462 results are in line with those obtained for soils by Kuhn and Mitchell 1992; 1993;
463 Kwok and Bolton 2010; and Liu et al. 2019).

464 **Fig. 9** and **Fig. 10** evidence that creep is more relevant on Sample 2 than on
465 Sample 1. This could be due to its mineralogical composition (see **Table 2**), as clay
466 minerals are mostly responsible for the strength reduction and the large strains
467 associated to creep under constant load (Liu et al. 2018).

468 **Fig. 11** shows the evolution of axial strain with axial stress (corresponding to the
469 stages of constant σ_1) during DEM computations and during the laboratory tests:
470 note that creep is negligible during the first axial loading steps –i.e., for $\sigma_1 \leq 9.9$
471 MPa on Sample 1 and $\sigma_1 \leq 6.6$ MPa on Sample 2–, whereas creep is clearly
472 noticeable for subsequent loading stages, in which plastic strains also occur.
473 Additionally, results show that creep rate increases when the axial stress
474 increases, until the maximum stress (σ_{peak}) is reached and the rock sample fails.

475 **[Fig. 11 approx. here]**

476 **6.2 Creep strain rate behaviour**

477 **Fig. 12a** and **Fig. 13a** show the logarithm of axial strain rate ($\dot{\epsilon}_1$) against the DEM
478 time (t_{DEM}) during the UCMCTs conducted on Samples 1 and 2. (They also show
479 when each new loading stage is applied). As additional load is applied in each
480 loading stage, the axial strain rate increases quickly up to approximately $\dot{\epsilon}_1$ of 5
481 %/s (similar to that applied by the walls), until the axial stress specified for such
482 stage is reached; then the axial strain rate decreases gradually during primary
483 creep, until it reaches a quasi-constant value (secondary creep). The strain
484 behaviour for higher axial stress is similar to the behaviour for lower axial stress;
485 however, the strain rate at the end of each stage tends to increase for higher load
486 stages, even when their duration is equal to, or slightly shorter, than the duration of
487 earlier stages with lower axial loads. This axial strain rate behaviour qualitatively
488 agrees with the creep tests results conducted by Brantut et al. (2014, 2014) in
489 porous limestone and sandstone.

490 **Fig. 12b** and **Fig. 13b** plot the logarithm of axial strain rate ($\dot{\epsilon}_1$) against the
491 logarithm of the DEM time (t_{DEM}), showing again that DEM results agree with the
492 idealized creep behaviour in **Fig. 1**: A quasi-linear decrease of strain rate with the
493 logarithm of time (primary creep) occurs at the beginning of each loading step,
494 followed by another period of approximately constant strain rate (secondary creep).
495 This occurs, with a different relative relevance of both phenomena, in all loading
496 steps, except for the last loading step of (higher) stress in Sample 2, in which
497 tertiary creep with accelerating strains occurs, leading to rock failure.

498 **[Fig. 12 approx. here]**

499 **[Fig. 13 approx. here]**

500 **6.3 Creep failure behaviour**

501 **Fig. 14** and **Fig. 15** show the number of micro-cracks –produced in both shear and
502 tension– and the progressive failure developed during the DEM numerical
503 modeling of the UCMCTs tests conducted with Samples 1 and 2. As it can be
504 observed, the number of such micro-cracks is very small for the loading stages
505 corresponding to lower stress values; however, the number of tension cracks
506 increases rapidly with the stress applied in each loading stage, as well as with the
507 duration of such stage. In particular, a large increase of the number of micro-cracks
508 occurs (i) immediately after application of the new load and (ii) during the creep
509 stage.

510 Note also that numerical results suggest that the main failure mechanism on
511 Samples 1 and 2 is caused by long-term damage induced by accumulation of

512 micro-cracks during creep, hence reducing the strength of the rock sample with
513 time, so that its failure is not sudden and is “delayed” in time, particularly in Sample
514 2.

515 Finally, it was found that rock failure occurs when a few shear micro-cracks are
516 developed; this seems to coincide with an even faster rate of increase of the
517 number of tension cracks within the sample when failure is approached (see **Fig.**
518 **14**). These results are consistent with those of Zhao et al. (2012) who, based on
519 laboratory UCMCTs on sandstone, reported that creep failure of sandstone
520 samples occurred when micro-fissures inside the samples reached a critical value
521 producing an accelerating creep until failure. Also, this behaviour was observed by
522 Baud and Meredith (1997), who studied creep in Darley Dale sandstone.

523 **[Fig. 14 approx. here]**

524 **[Fig. 15 approx. here]**

525 **7. Conclusions**

526 Rock creep behaviour is a crucial aspect in many rock engineering applications.
527 Although many models have been proposed to reproduce rock creep, many of the
528 most common ones cannot reproduce all phases of creep and, in particular, they
529 cannot reproduce the accelerating strain rates associated to tertiary creep and
530 leading to rock failure.

531 This work demonstrates that the discrete element method (DEM) can be employed,
532 in conjunction with the rate process theory, to reproduce the creep behavior of
533 slate rock samples from the Nogueira Group in Northern Spain, when they are

534 subjected to uniaxial compression multistage creep tests (UCMCTs) conducted in
535 the laboratory. To do that, and differentiating our approach to previous works that
536 model soil creep (Kuhn and Mitchel 1992; 1993; Kwok and Bolton 2010; Liu et al.
537 2019), the DEM sample is constructed using a hybrid mixture of contact models
538 between particles, employing both the Flat Joint Contact Model and the Linear
539 Model, but with a significant preponderance of FJCM with respect to the LM. Note,
540 however, that LM contacts are necessary to model creep, as almost no creep
541 occurs when they are removed from the DEM model.

542 One significant novelty of the proposed approach with respect to other traditional
543 approaches to model rock creep (such as, e.g., Burger's model) is that it can
544 reproduce tertiary creep without having to resort to a constitutive model that
545 explicitly characterizes tertiary creep; at the same time, it can reproduce failure of
546 the sample during a load increment. (This is also the first time that rate process
547 theory is used to simulate rock creep behavior, which required us to implement it
548 into new rock specific DEM models). In particular, the rate process theory provides
549 a fundamental micromechanical relationship between the sliding velocity between
550 particles and their coefficient of friction; and it is shown that such fundamental
551 relationship is able to model all stages of creep at the macroscopic level. Results
552 also show that our DEM approach can reproduce the evolution of strain with time
553 measured in real rock samples, including samples that failed after a tertiary creep
554 stage.

555 The DEM models based on rate process theory proposed herein also provide
556 interesting information about the evolution of damage during the creep tests

557 conducted, suggesting that rock damage during such creep tests mainly occurs
558 due to tensile fractures that develop during loading and during creep; the rate of
559 tensile cracking is also very high during tertiary creep, when some shear cracks
560 develop as well.

561 Finally, the model can be calibrated, in a relatively straightforward way, with the
562 methodology provided, that uses information from the laboratory UCMCTs.
563 Together with its capability to consider aspects such as the stresses or times
564 associated to loading stages, etc.; this easy calibration makes this approach to
565 become a cost and time-effective alternative to other in-situ tests that could be
566 proposed to analyze rock creep behaviour. However, it may be more difficult to
567 incorporate into the DEM models the influence of other factors, such as the
568 mineralogical compositions of rock, and additional laboratory tests might be
569 required. The influence of mineralogy on creep behaviour, however, is considered
570 outside the scope of this research and it will be discussed in future publications.

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Draft

Table 1. Constants employed for the rate process theory (according to Kuhn and Mitchell, 1993).

Variable	Value
Boltzmann's constant, k (J/K)	1.381×10^{-23}
Planck's constant, h (J.s)	6.626×10^{-34}
Universal gas constant, R (kJ/(mol.K))	8.314×10^{-3}
Absolute temperature, T (K)	293
Flow unit, λ (m)	$3 \times 10^{-10*}$
Activation energy, ΔF (kJ/mol)	100*
Number of bonds per unit of normal contact force, n_1 (bonds/N)	1×10^9

*chosen to reproduce the experimental behavior within the range suggested by Kuhn and Mitchell (1993)

Draft

Table 2. Estimated mineral composition of the rock samples, based on optical microscopy tests.

	Sample 1		Sample 2	
	Minerals composition (%)	Grain size (mm)	Minerals composition (%)	Grain size (mm)
Quartz	19	0.008 – 0.016	20	0.008 – 0.016
Sericite	26	0.002	39	0.002
Opaque	50.5	-	31	-
Chlorite	4	0.04 – 0.16	3	0.03 – 0.12
Calcite	0.5	0.15	-	-
Others	-	-	1	-
Depth range (m)	92.7 – 93.3		43.6 – 44.2	

Draft

Table 3. Scale factor (t_{DEM}/t_{lab}) between the laboratory and DEM model.

Sample		Axial strain, ε_1 (%)	Time, t (s)	t_{DEM}/t_{lab}
1	Lab	3.6×10^{-3}	43120	1.16×10^{-6}
	DEM		0.050	
2	Lab	8.3×10^{-4}	2967.7	3.14×10^{-6}
	DEM		0.009	

Draft

Table 4. Micro-mechanical parameters fitted for the DEM employed to reproduce the UCMCTs conducted on slate rocks.

Sample	Particle micromechanical properties		FJCM micromechanical properties		Hybrid model	
1	E^* (GPa)	34.15	E^* (GPa)	34.15		
	$k^* = k_n/k_s$	1.80	k^*	1.80		
	Friction angle ϕ ($^\circ$)	30	c (MPa)	49.48	FJCM contacts	9069
	Ball density, ρ (kg/m^3)	2737	σ_t (MPa)	26.85	LM contacts	1588
	Minimum radius, R_{min} (mm)	0.60	FJ bonding ratio, c/σ_t	1.84		
	R_{max}/R_{min}	1.50	Bonded fraction, ϕ_B	1.00	LM-to-FJCM	17.5
			Gapped fraction, ϕ_G	0.00	contact ratio (%)	
			Initial gap, g_o (mm)	0.05		
			Number of elements, N_r	2	Control gap, g_c	-3.085×10^{-2}
			LM micromechanical properties		(mm)	
		E_{LM}^* (GPa)	34.15			
		k_{LM}^*	1.80			
2	E^* (GPa)	24.30	E^* (GPa)	24.30		
	$k^* = k_n/k_s$	1.80	k^*	2.70	FJCM contacts	9070
	Friction angle ϕ ($^\circ$)	30	c (MPa)	45.00	LM contacts	1587
	Ball density, ρ (kg/m^3)	2647	σ_t (MPa)	27.52		
	Minimum radius, R_{min} (mm)	0.60	FJ bonding ratio, c/σ_t	1.63	LM-to-FJCM	17.5
	R_{max}/R_{min}	1.50	Bonded fraction, ϕ_B	1.00	contact ratio (%)	
			Gapped fraction, ϕ_G	0.00		
			Initial gap, g_o (mm)	0.05	Control gap, g_c	-3.075×10^{-2}
			Number of elements, N_r	2	(mm)	
			LM micromechanical properties			
		E_{LM}^* (GPa)	24.3			
		k_{LM}^*	1.80			

Table 5. Comparison between macro-mechanical properties obtained for the UCMCTs conducted on slate rock samples, by laboratory tests and by DEM numerical tests.

Sample	Macro-properties	Lab	DEM
1	σ_{peak} (MPa)	36.30	36.10
	E (GPa)	37.23	37.19
2	σ_{peak} (MPa)	31.35	31.35
	E (GPa)	26.54	26.44

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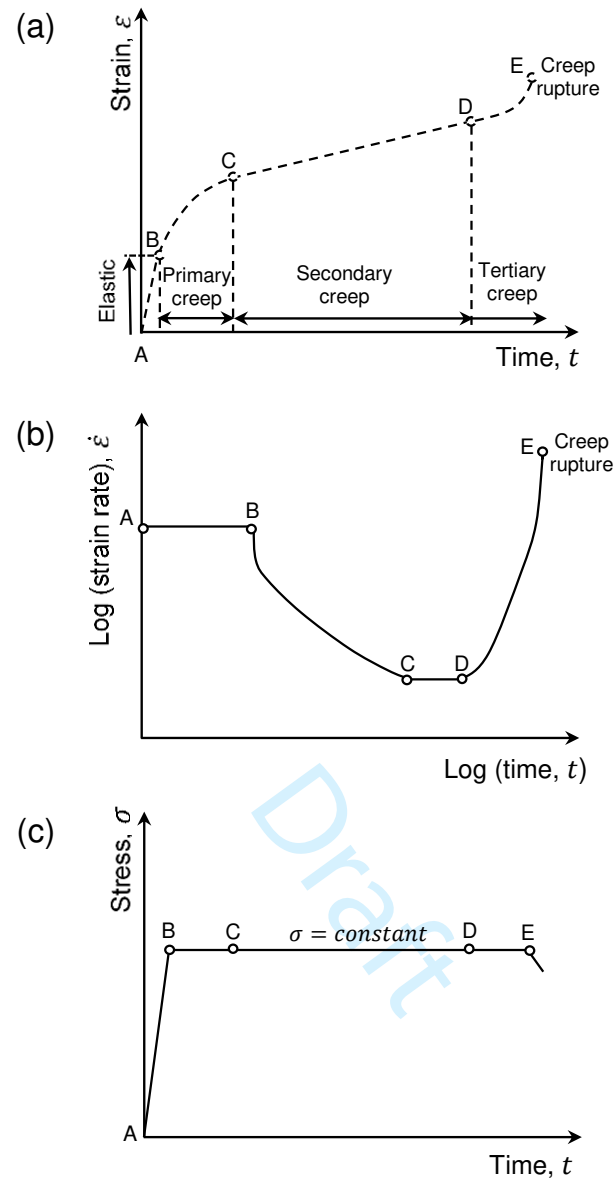


Fig. 1. Stages of creep under constant homogeneous stress: (a) strain versus time, (b) log(strain rate) versus log(time), (c) stress versus time (modified from Kwok et al. 2010)

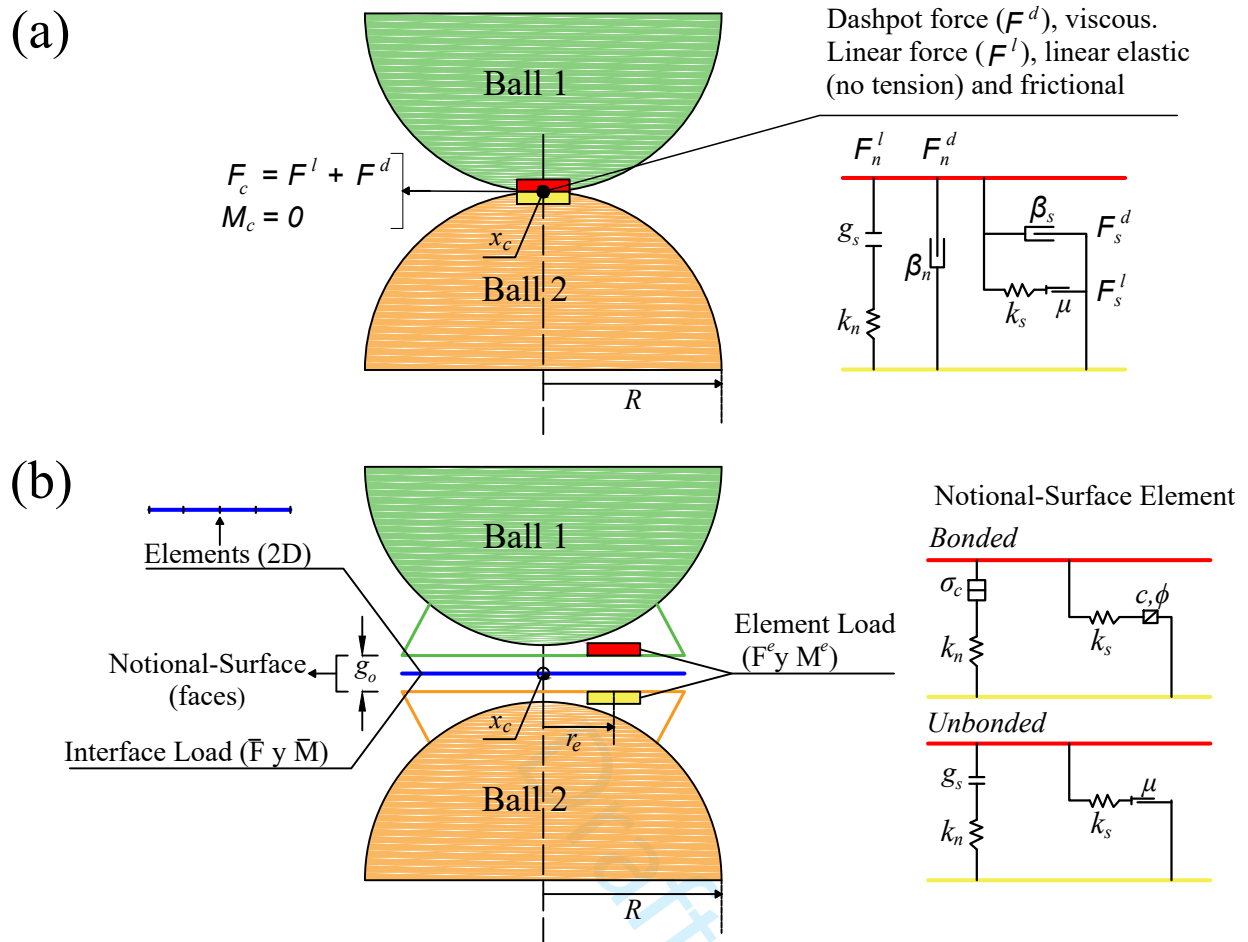


Fig. 2. Behavior and rheological components of the: (a) Linear Model (LM), (b) Flat Joint Contact Model (FJCM) (modified from Itasca Consulting Group Inc. 2014).

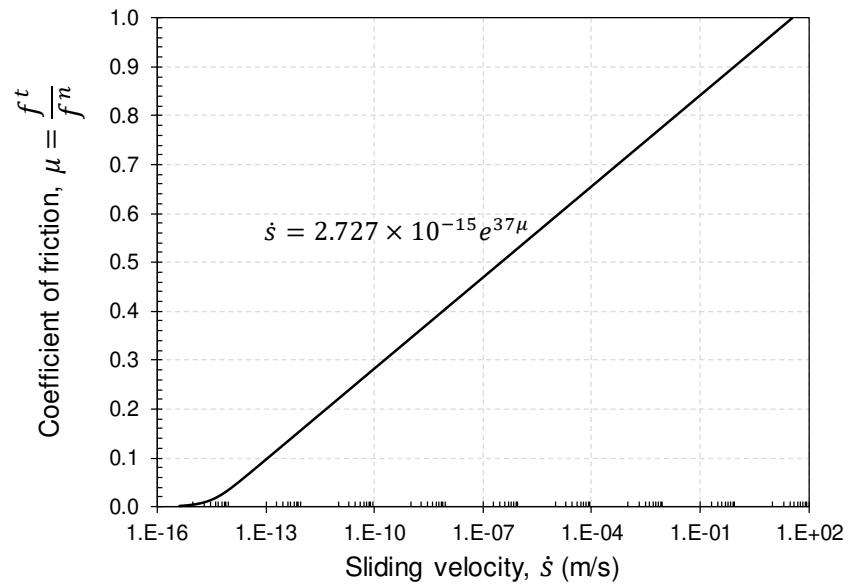


Fig. 3. Function of rate process theory employed in this work, providing a relationship between sliding velocity between particles and their corresponding coefficient of friction.

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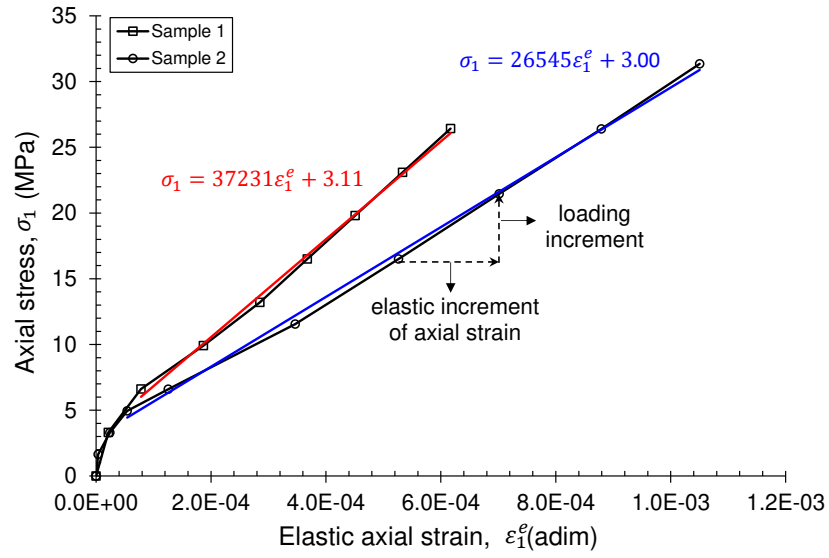


Fig. 4. Axial stress vs elastic axial strain in the laboratory tests.

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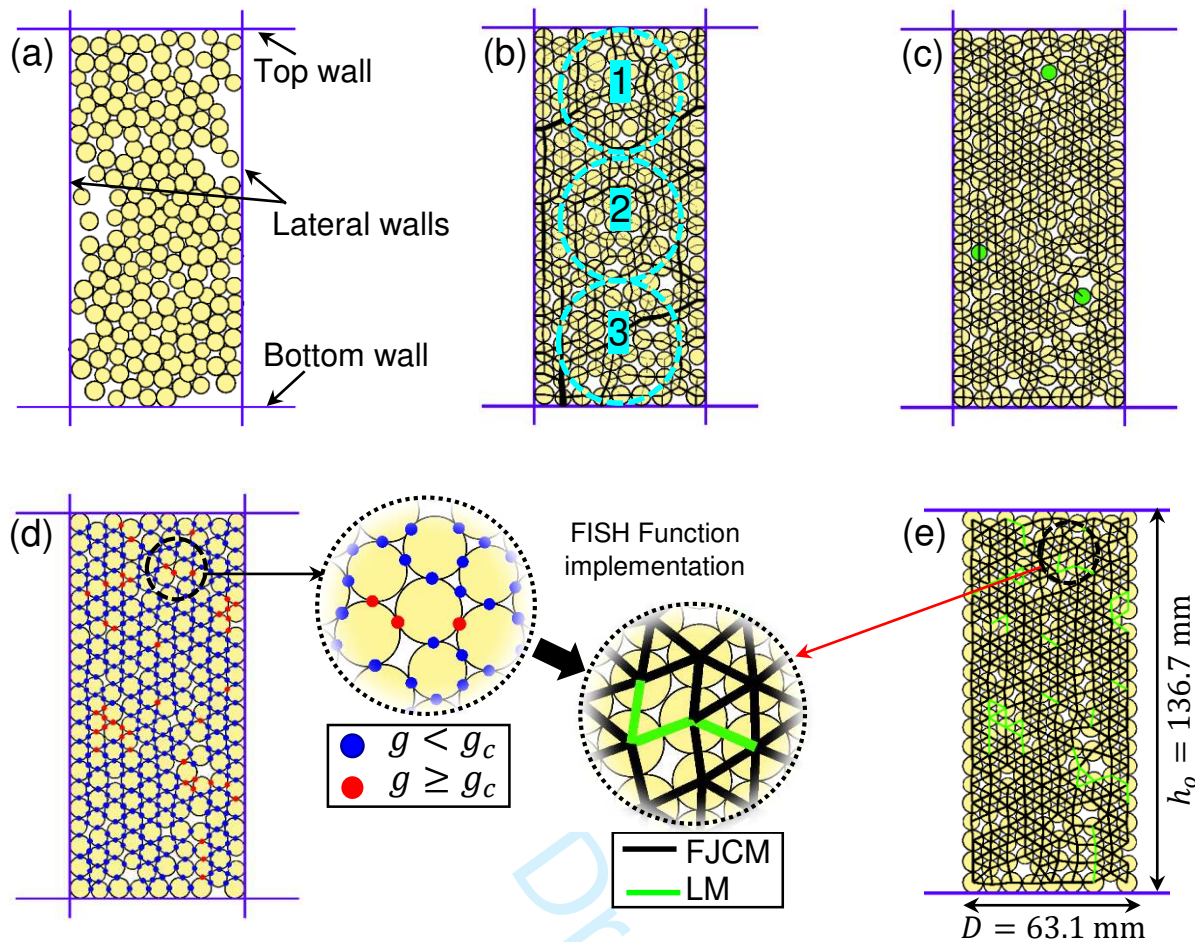


Fig. 5. Genesis of the numerical sample: (a) particle initial generation before rearrangement, (b) contact-force distribution after isotropic stress installation (black lines represent contact-force intensity and cyan lines represent the reference circles to measure stresses), (c) detection of floating particles (green balls represent floating particles), (d) application of the FJCM and LM, (e) final DEM^{2D} specimen (black and green lines represent FJCM and LM network, respectively). Note that to facilitate the visualization, fewer particles are employed herein than in actual simulations (For a color version of this figure refer to the web version of this article) (modified from Gutiérrez-Ch et al. 2018).

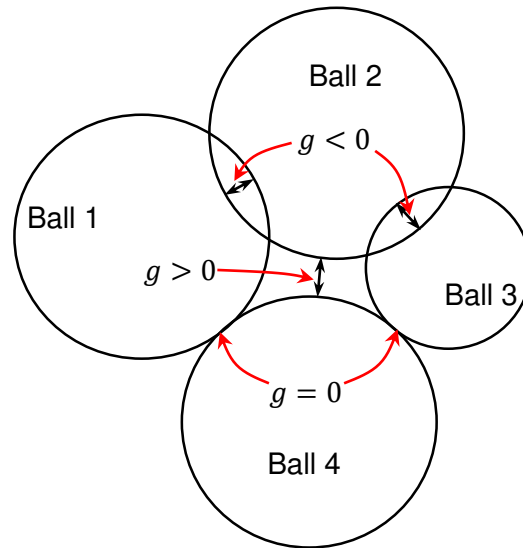


Fig. 6. Idealization of the gap (g) between particles.

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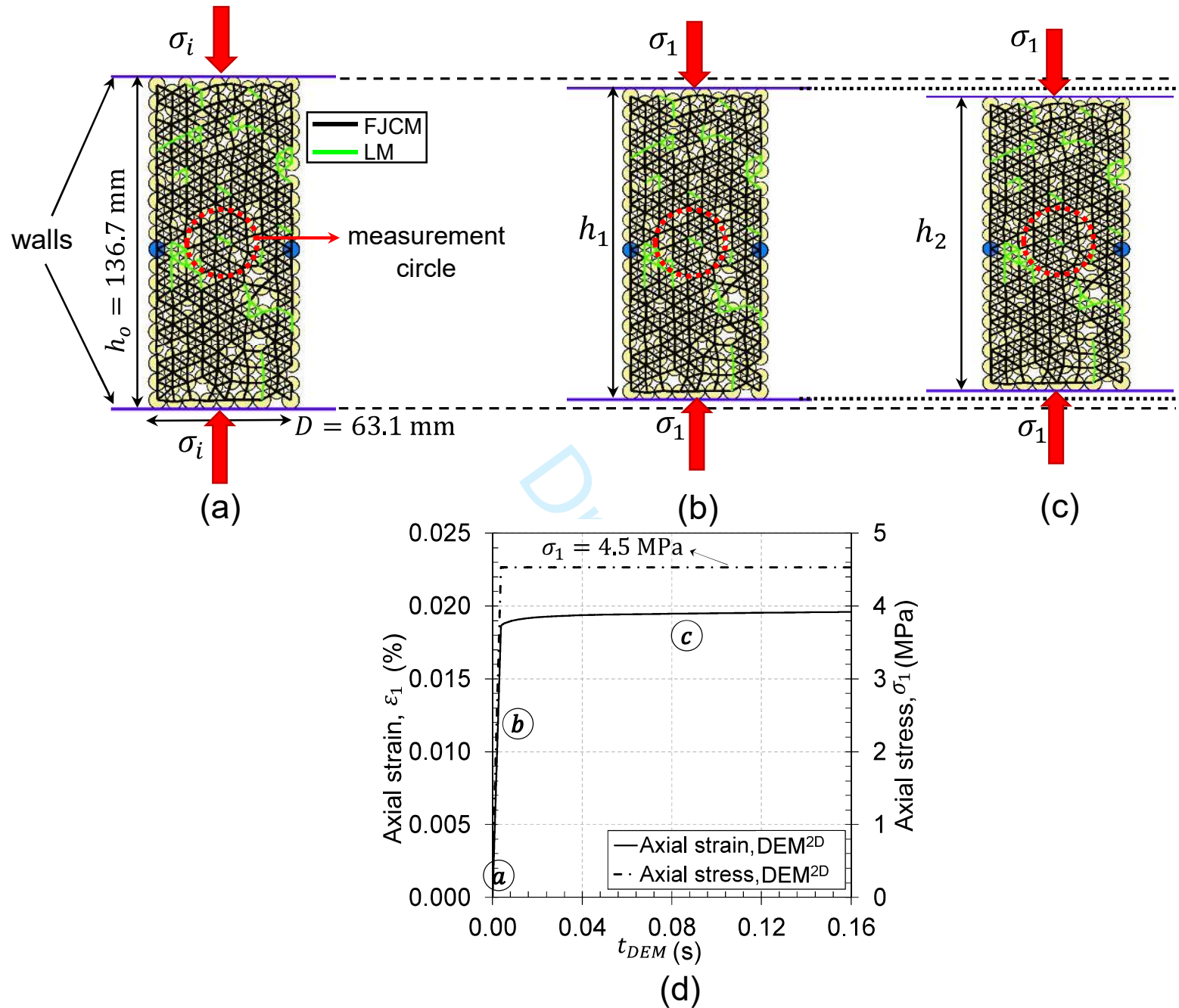


Fig. 7. Numerical uniaxial compression creep test with DEM: (a) initial stress application, (b) compression stage, (c) creep stage (black lines represent FJCM, green lines represent LM, blue balls represent the gage particles), (d) evolution of the axial strain and stress during the test. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article).

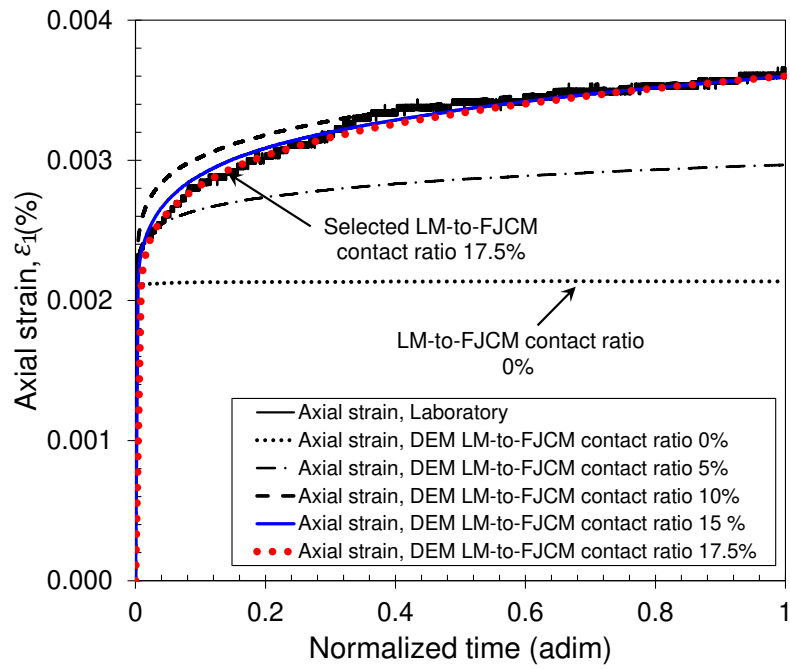


Fig. 8. Sensitivity analysis conducted on Sample 1 to select LM-to-FJCM contact ratio.

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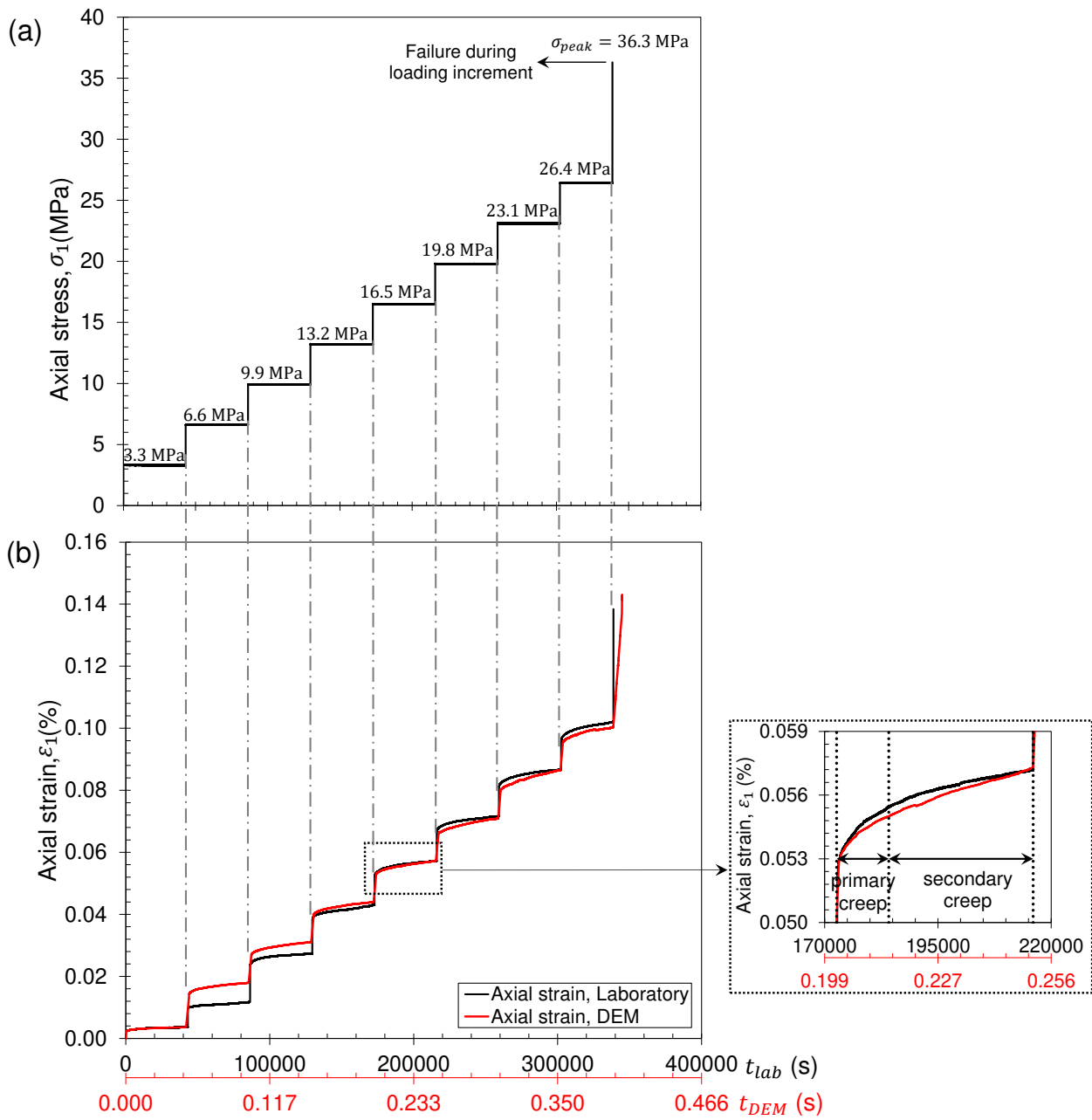


Fig. 9. Comparison between DEM and laboratory results on Sample 1: (a) axial stress (σ_1) vs laboratory time (t_{lab}), (b) creep axial strain (ϵ_1) vs laboratory time (t_{lab}) and DEM time (t_{DEM}).

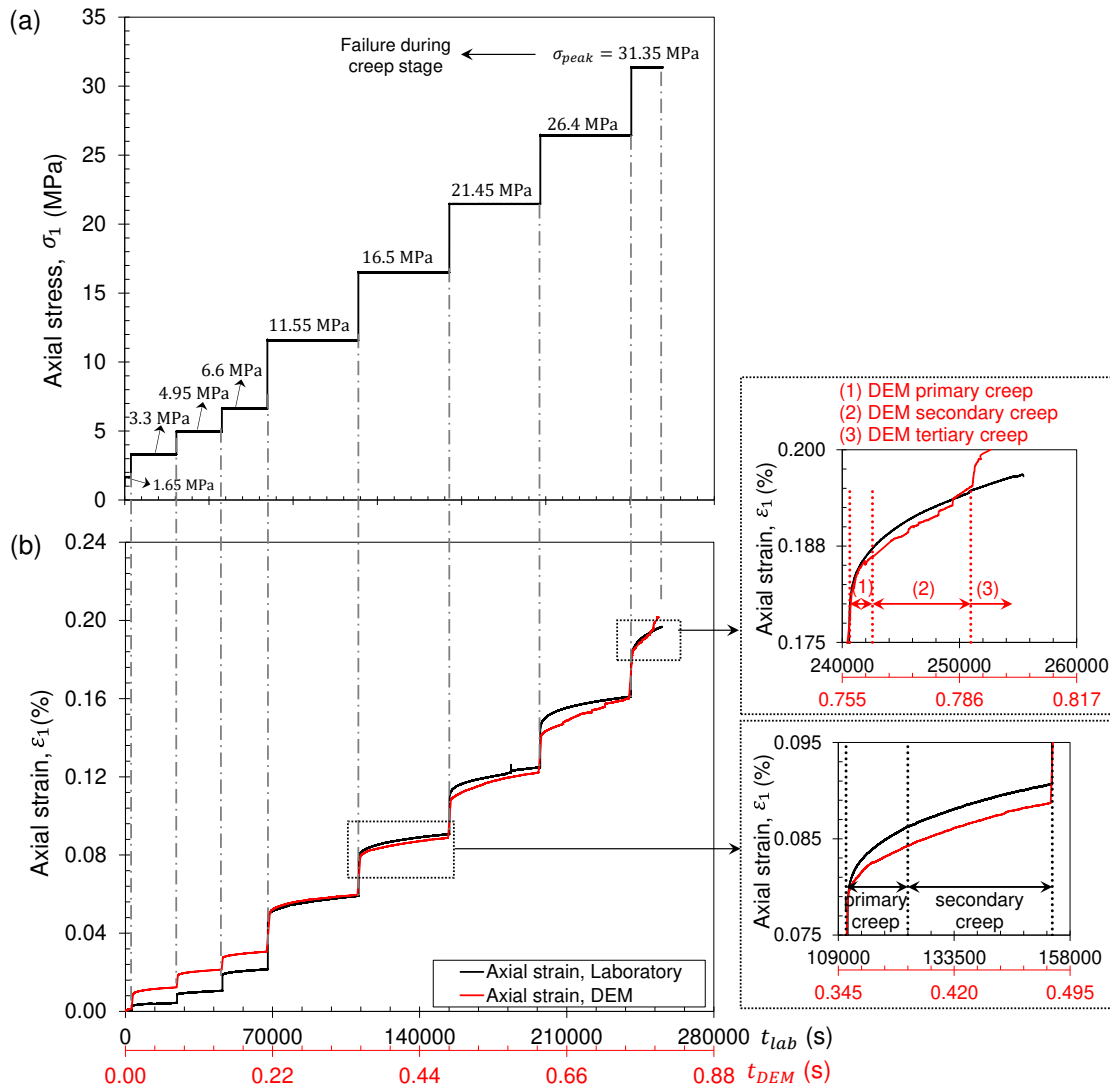


Fig. 10. Comparison between DEM and laboratory results on Sample 2: (a) axial stress (σ_1) and laboratory time (t_{lab}), (b) creep axial strain (ϵ_1) vs laboratory time (t_{lab}) and DEM time (t_{DEM}).

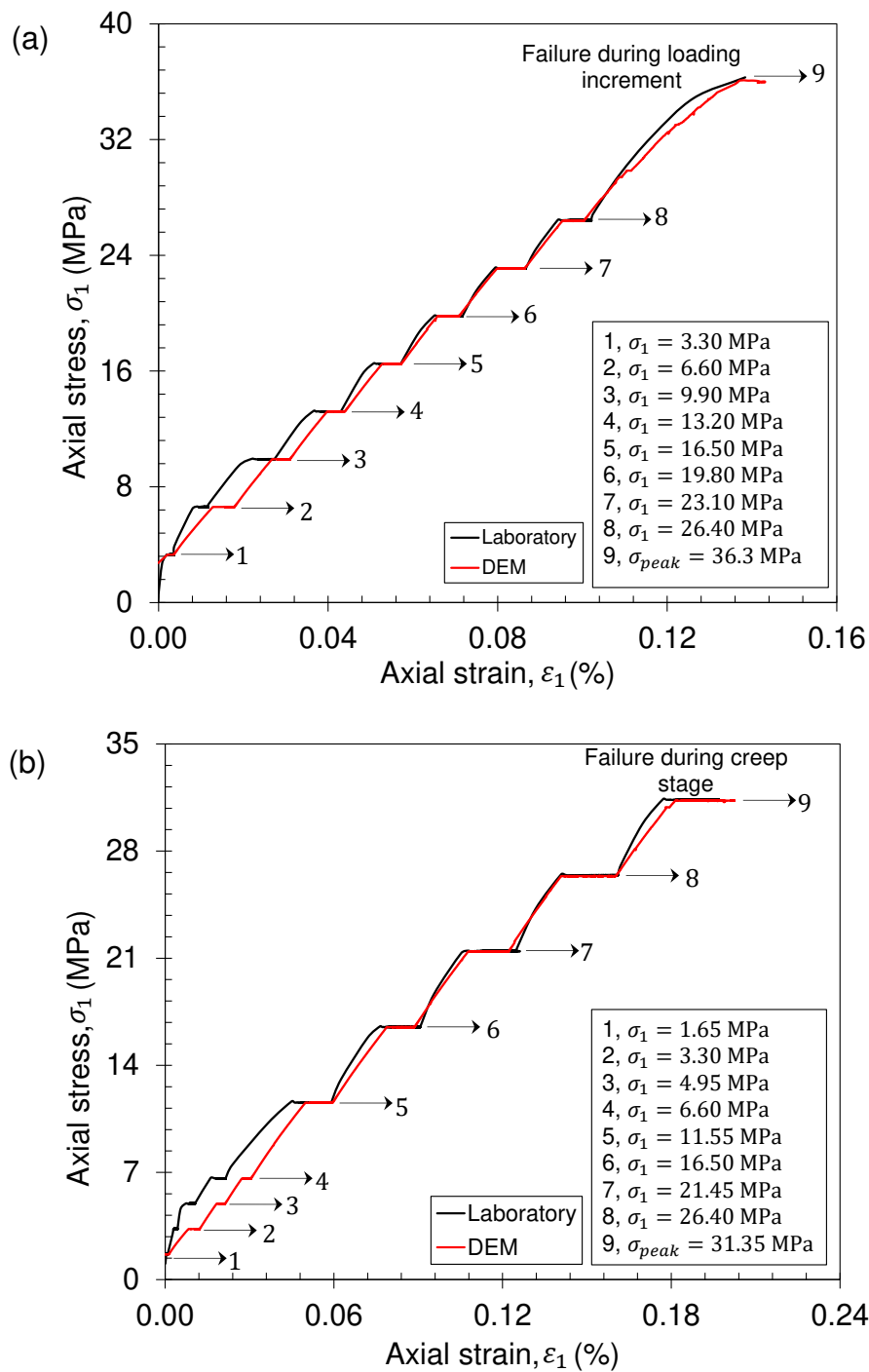


Fig. 11. Comparison between DEM and laboratory axial stress (σ_1) against axial strain (ϵ_1) during the UCMCT on: (a) Sample 1, (b) Sample 2.

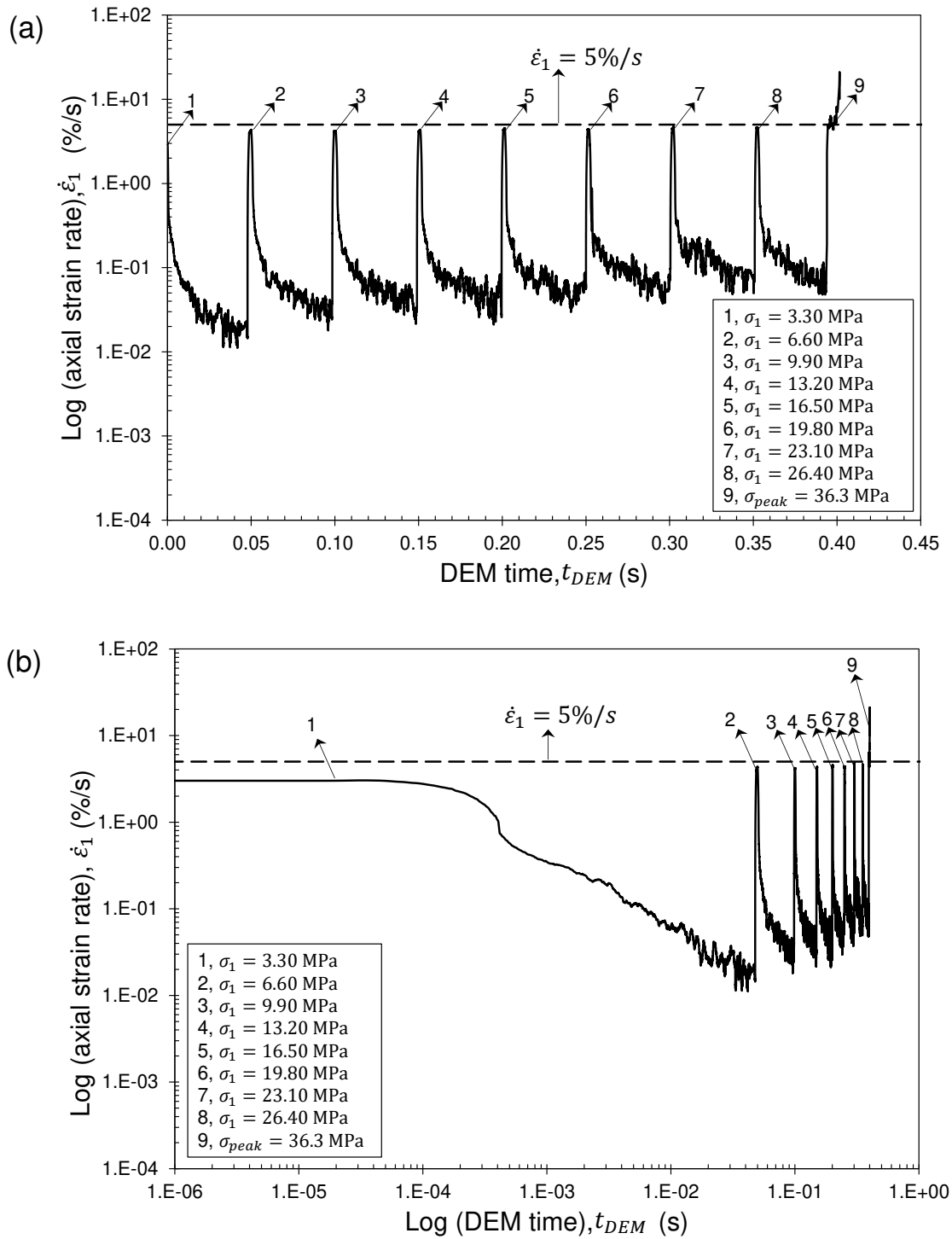


Fig. 12. Axial strain rate ($\dot{\epsilon}_1$) curve computed with DEM^{2D} during the uniaxial compression multistage creep test on Sample 1: (a) log(axial strain rate) vs DEM time, (b) log(axial strain rate) vs log(DEM time).

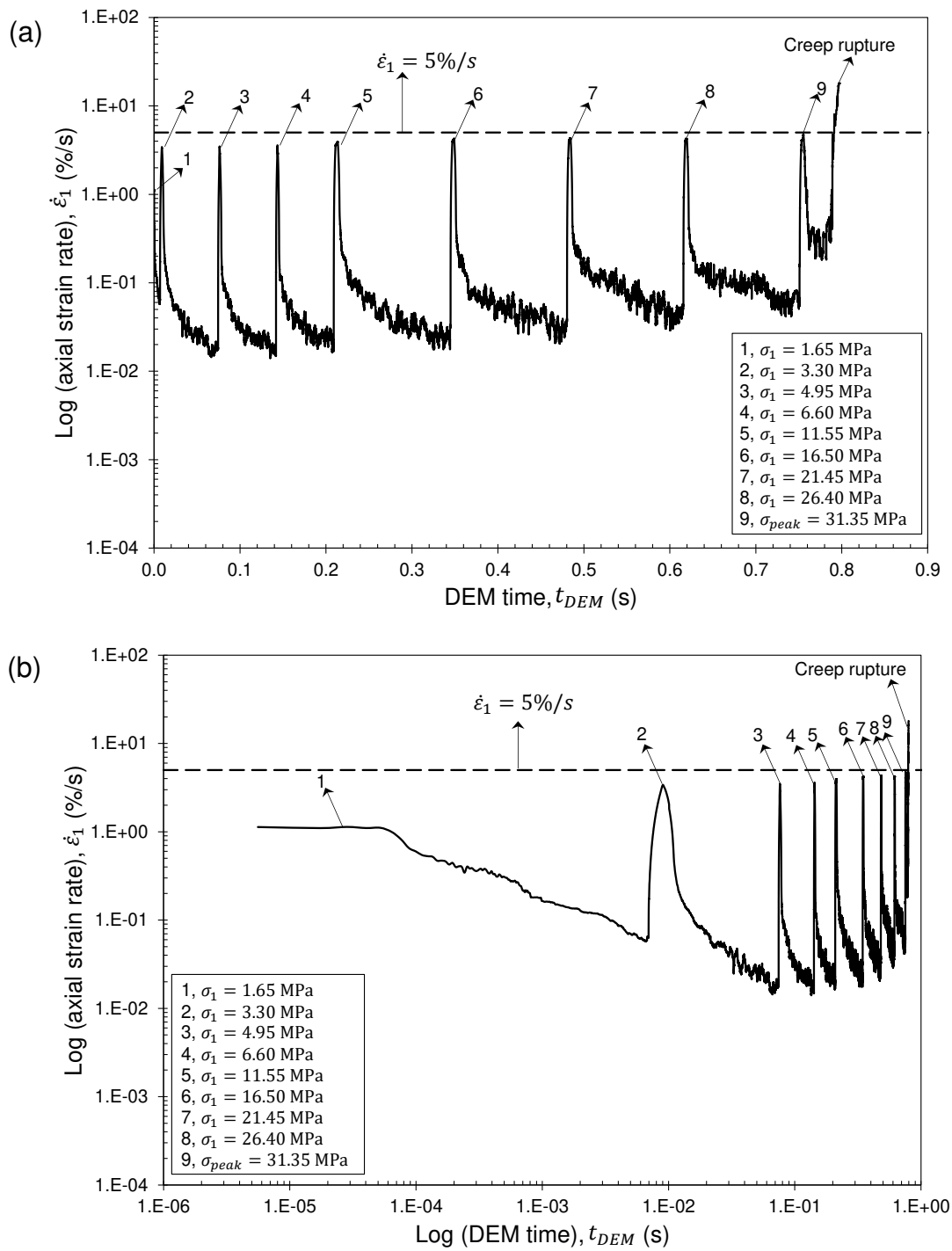


Fig. 13. Axial strain rate ($\dot{\epsilon}_1$) curve computed with DEM^{2D} during the uniaxial compression multistage creep test on Sample 2: (a) log(axial strain rate) vs DEM time, (b) log(axial strain rate) vs log(DEM time).

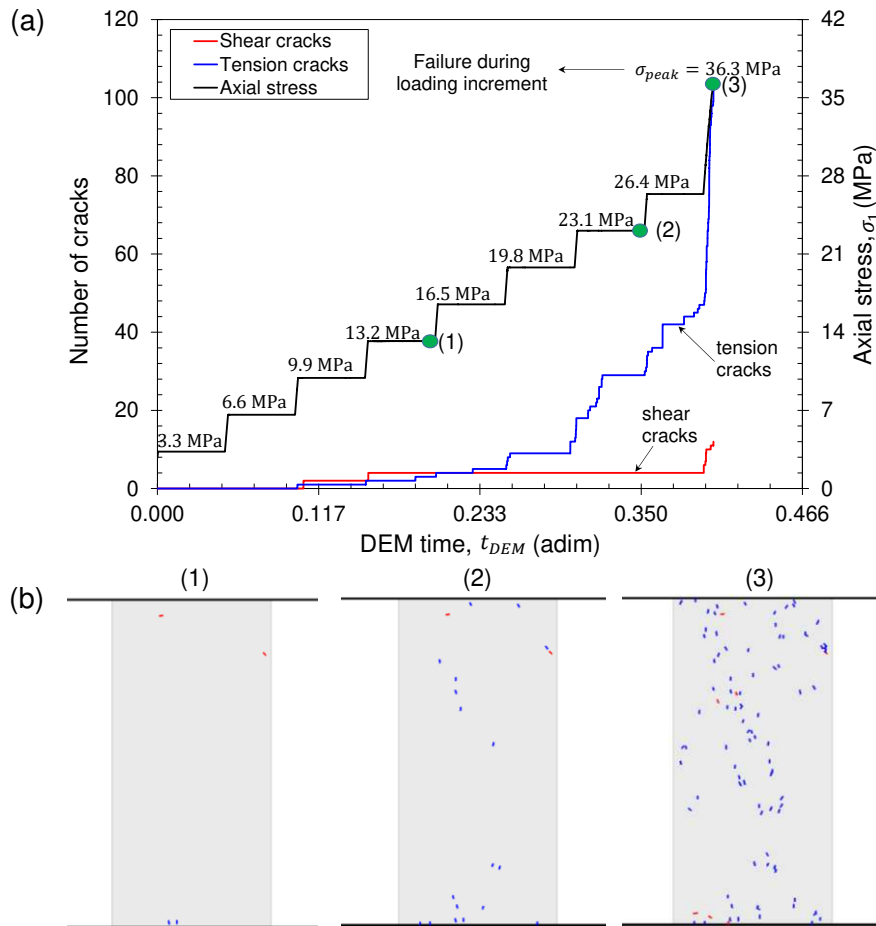


Fig.14. Sample 1: (a) number of cracks developed during the creep tests, plotted against the DEM time (t_{DEM}) computed with DEM^{2D}; (b) progressive failure (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article)

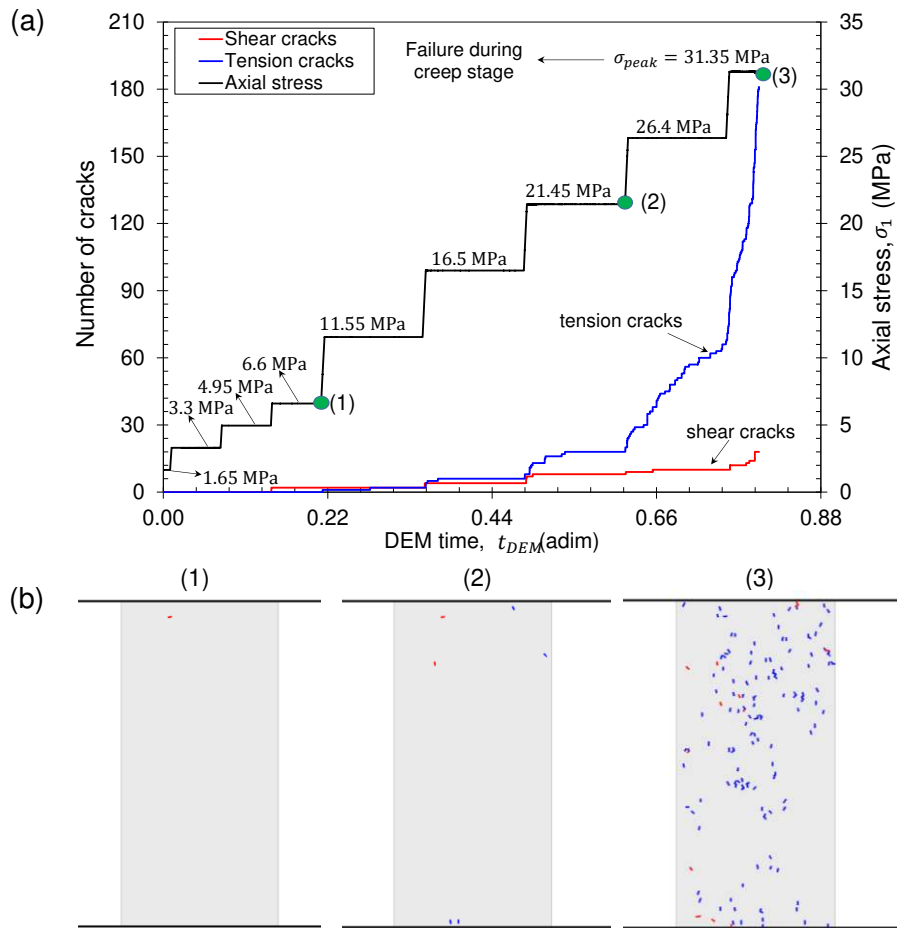


Fig.15. Sample 2: (a) number of cracks developed during the creep tests, plotted against the DEM time (t_{DEM}) computed with DEM^{2D}; (b) progressive failure (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article)