



# CHORUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

## Dispersion of edge states and quantum confinement of electrons in graphene channels drawn on graphene fluoride

Ning Shen and Jorge O. Sofo

Phys. Rev. B **83**, 245424 — Published 24 June 2011

DOI: [10.1103/PhysRevB.83.245424](https://doi.org/10.1103/PhysRevB.83.245424)

# **Dispersion of Edge States and Quantum Confinement of Electrons in Graphene Channels Drawn on Graphene Fluoride**

Ning Shen<sup>1</sup> and Jorge O. Sofo<sup>1,2,\*</sup>

<sup>1</sup>*Department of Physics, The Pennsylvania State University, University Park, Pennsylvania 16802, USA*

<sup>2</sup>*Materials Research Institute, The Pennsylvania State University, University Park, Pennsylvania 16802, USA*

(\*) To whom correspondence and requests for materials should be addressed, email [sofo@psu.edu](mailto:sofo@psu.edu)

Graphene is an excellent conductor while graphene fluoride is a wide band gap semiconductor. We propose the formation of graphene channels embedded in graphene fluoride as a method to induce quantum confinement of charge carriers in graphene. In particular, we study the electronic structure of graphene channels drawn on the fluoride along two high-symmetry directions, the armchair and zigzag orientations. The zigzag channels are found to have dispersive one-dimensional edge bands, contrary to the case of ribbons and channels drawn on graphane, where the edge state is flat close to the Fermi level and has a very large effective mass. The effective mass of this one-dimensional edge state can be controlled by electrostatic interactions at the edge of the channel. This result indicates that the mobility of these channels can be controlled by a localized gate voltage. The armchair channel is found to be metallic or semiconducting depending on the width of the channel, in agreement with ribbons and hydrogen limited channels.

## I. INTRODUCTION

1  
2 Graphene, a single plane of carbon atoms in a honeycomb lattice, became a fascinating  
3 material after the group of Manchester unveiled it from the interior of graphite.<sup>1</sup> Among other  
4 intriguing and fascinating properties such as integer quantum hall effect at room temperature<sup>2</sup>,  
5 graphene exhibits extremely high carrier mobility exceeding  $10^7 \text{ cm}^2/(\text{V}\cdot\text{s})^3$  and ballistic  
6 transport of carriers on long distances of  $10\sim 10^2 \text{ nm}^4$  which make it a promising candidate for  
7 future graphene-based field effect transistors. However, the ability to confine carriers and open a  
8 gap in graphene is crucial to realize its practical applications. One possibility is to cut narrow  
9 stripes in the form of graphene nanoribbons (GNRs) provide one possible solution. Studies have  
10 shown that the GNRs can be made either metallic or semiconducting by controlling their width  
11 or orientation<sup>5, 6</sup>. Recent ab-initio calculations have shown that the electronic structure of the  
12 ribbons is not greatly affected by the termination of dangling bonds with hydrogen<sup>7, 8</sup>. These  
13 studies have shown that the heavy mass of the edge states in zigzag ribbons induce an instability  
14 that creates a localized magnetic moment at the edge.

15 Two approaches have been attempted to produce GNRs. One method consists of  
16 physically cutting the ribbons with either E-beam<sup>9, 10</sup> or STM<sup>11</sup> lithography of graphene.  
17 However, the reported GNRs by E-beam lithography are too wide (15-100nm) and  
18 correspondingly exhibit small band gap (10~100meV). Although STM lithography can produce  
19 ribbons with smaller width (2.5nm~10nm) and large gaps (0.5eV~0.18eV), it requires more time  
20 and dexterity. Another approach is to use solution-dispersion and sonication<sup>12, 13</sup> to break the  
21 graphene into narrow ribbons (sub 10nm) with varying widths along their lengths. Although this  
22 approach can produce many narrow GNRs much easier than the physical cutting approach, it has

Dispersion of Edge States and Quantum Confinement...

1 the disadvantages of much less control of the width of the produced ribbons and type of edge  
2 terminations.

3 Recently, an alternative approach to confine the carriers in graphene has been  
4 suggested.<sup>14</sup> The idea is to chemically modify certain regions of graphene to transform the  $sp^2$   
5 hybridized carbon atoms to  $sp^3$  hybridization. Our group predicted that hydrogenation changes  
6 highly conductive graphene into an insulator<sup>15</sup>. The structure of hydrogenated graphene, which  
7 we named “graphane”, was previously predicted as stable by Sluiter and Kawazoe.<sup>16</sup>  
8 Consequently, hydrogenation can confine the carriers in graphene by sandwiching graphene  
9 between two insulating regions. Elias et al.<sup>17</sup> hydrogenated graphene and reversibly transformed  
10 the material into an insulator, confirming the prediction. Singh et al.<sup>18</sup> studied the electronic  
11 properties of graphene channels embedded between graphane barriers and found electronic states  
12 in the channels that are similar to those of the graphene ribbons. As the channel width is  
13 increased row by row, the structures alternate between two cases that are semiconducting and  
14 one that is metallic with a total period of three. The zigzag channels possess the peculiar edge  
15 state at the Fermi level that corresponds to a one dimensional electron channel localized at the  
16 interface between graphene and graphane with a very flat dispersion relation<sup>5, 6</sup>. Similar to what  
17 is observed in the ribbons, the heavy mass of this one-dimensional electronic state induces spin  
18 polarization.

19 Compared to the newly proposed graphane, graphite fluoride is a material that has been  
20 synthesized and studied for many years.<sup>19-21</sup> Early experimental studies by Parry et al.<sup>22</sup> and  
21 Mahajan et al.<sup>23</sup> have measured the structure and electronic properties of  $(CF)_n$  and found that  
22 the lattice constants of the hexagonal unit cell is about 2.53 Å in plane and about 5.7 Å in c-axis.  
23 They also showed  $(CF)_n$  to be insulator. Charlier et al.<sup>24</sup> calculated the electronic structure of  
Dispersion of Edge States and Quantum Confinement...

1 (CF)<sub>n</sub> and found an insulator with a direct band gap of 3.5 eV at  $\Gamma$ . More recent GW calculations  
2 report a much larger band gap of 7.4 eV.<sup>25, 26</sup> There have been some experimental results  
3 suggesting possible routes to remove fluorine atoms and reduce it back to a graphene layer. For  
4 instance, the reduction of (CF)<sub>n</sub> and (C<sub>2</sub>F)<sub>n</sub> have been attained by hydrogen gas<sup>27-31</sup> or NaOH–  
5 KOH solution<sup>32, 33</sup>. Recent work by R. R. Nair et al.<sup>34</sup> and J. T. Robinson, et al.<sup>35</sup> show that  
6 fluorinated graphene can be readily patterned and has better stability and insulating properties  
7 than hydrogenated graphene.

8 In this work, we study the electronic properties of graphene channels with zigzag or  
9 armchair boundaries limited by insulating graphene fluoride barriers. We will show that the  
10 zigzag channels display the peculiar edge state at the Fermi level localized at the interface  
11 between graphene and CF, similar to the case of ribbons and channels limited by graphene.  
12 However, in the case of the channels limited by CF, the one-dimensional edge state shows a  
13 quadratic dispersion relation indicating a smaller effective mass of the carriers. With a simple  
14 tight-binding model, we show that the dispersion relation of the peculiar edge state is extremely  
15 sensitive to the site energy of the carbon atom at the edge of the graphene channel. The presence  
16 of Fluorine in the barrier region is responsible for the lower site energy of the carbon atom at the  
17 edge and of the dispersion of the edge state. This observation unveils a method to control the  
18 dispersion relation of the edge state and consequently the effective mass of the carriers in the  
19 channel with a localized gate voltage. Controlling the effective mass with a gate voltage enables  
20 switching on and off the spin polarization and modifying the electronic mobility of the  
21 structures. The armchair channel is found to be metallic or semiconducting depending on the  
22 width of the channel, which is similar to the behavior of armchair ribbons.

## 23 II. METHODS

Dispersion of Edge States and Quantum Confinement...

1 All electronic structure calculations reported in this work were done using density  
 2 functional theory (DFT) with a plane wave basis set as implemented in the Vienna Ab Initio  
 3 Simulation Package (VASP)<sup>36-39</sup>. The core electrons were treated with a frozen projector  
 4 augmented wave method<sup>40, 41</sup>. The exchange and correlation potential was treated with a  
 5 generalized gradient approximation using the Perdew-Burke-Ernzerhof (PBE) functional<sup>42, 43</sup>.  
 6 The plane wave energy cutoff determining the basis set size was set to 400 eV, and the Brillouin  
 7 zone was sampled with Monkhorst-Pack<sup>44</sup> grid of  $8 \times 1 \times 1$  (for zigzag) and  $1 \times 8 \times 1$  (for armchair).  
 8 For density of states calculation we use a k-point sampling of  $64 \times 16 \times 1$  (for zigzag) and  
 9  $16 \times 64 \times 1$  (for armchair). A vacuum of 12 Å is added in the direction normal to the GR/CF super-  
 10 lattice plane to avoid artificial interactions of the images. For the relaxed configurations in this  
 11 work, the converged atomic forces were smaller than 0.01 eV/Å.

12 We have tested the above calculation setup for graphene fluoride, which shows a band  
 13 gap of 3.1 eV at the  $\Gamma$  point and lattice constant of the hexagonal unit cell at 2.61 Å. The lattice  
 14 constant is in good agreement with the neutron scattering value of 2.61 Å recently obtained by Y.  
 15 Sato<sup>20</sup>. The lattice constant of the superlattices is approximated by a linear interpolation between  
 16 the lattice constant of graphene and CF. The lattice constant of a structure of  $M$  rows of CF (the  
 17 barrier) and  $N$  rows of graphene (the channel) is calculated as

$$18 \quad a_{\text{GR/GF}} = \frac{M}{M+N} a_{\text{GF}} + \frac{N}{M+N} a_{\text{GR}}, \quad (1)$$

19 where  $a_{\text{GF}} = 2.61$  Å and  $a_{\text{GR}} = 2.46$  Å. None of the results presented in this work are strongly  
 20 dependent on the small departures from this approximation. All the structures considered have  
 21 been optimized with respect to the atomic positions. Two representative examples are shown in  
 22 Fig. 1. In the rest of this paper, we will use a notation zz(M,N) or ac(M,N) depending if the  
 Dispersion of Edge States and Quantum Confinement...

1 orientation is zigzag or armchair respectively to refer to structures with M rows of carbon atoms  
2 in the barrier and N rows of carbon atoms in the channel. This nomenclature is graphically  
3 indicated in Fig. 1.

### 4 III. RESULTS AND DISCUSSION

5 **Zigzag channels.** The electronic structure of the zigzag channels shares its general  
6 features with their analog channels limited by graphene or with the ribbons. The features we will  
7 describe can be understood with a tight-binding model with one  $p_z$  orbital per atom and hopping  
8 to first neighbors in the channel.<sup>5, 6</sup> In Fig. 2 we show the bands close to the Fermi level of a  
9 zz(6,12) channel. They have two degenerate states at the Fermi level in the X point of the  
10 Brillouin zone that disperse along the X- $\Gamma$  direction, which is the direction corresponding to  
11 motion along the channel, forming two bands that will be the center of our discussion below. In a  
12 zigzag structure with N rows of carbon atoms in the channel, there are other  $2N-2$  bands derived  
13 from the folding of the  $\pi$  and  $\pi^*$  bands of graphene divided in two manifolds of  $N-1$  bands each,  
14 one above and one below the Fermi level. Each of these manifolds is almost degenerate at the X  
15 point at energy approximately equal to the first neighbors hopping of the  $p_z$  orbitals above and  
16 below the Fermi level. Due to the dispersion in the direction X- $\Gamma$ , these states form a gap at  
17 about 1/3 of the distance from the X point to the  $\Gamma$  point. This gap gets smaller as the channel  
18 gets wider. This intermediate point 1/3 of the distance from the X point, which is the folded  
19 location of the K point in the graphene band structure, is also important for the states at the  
20 Fermi level. They disperse together up to this point when one of them moves up in energy and  
21 the other moves down away from the Fermi level to almost join the manifolds at the  $\Gamma$  point. The  
22 charge density associated with these states is mainly localized at the edge. It is strictly localized

Dispersion of Edge States and Quantum Confinement...

1 at the edge row for the states at X and the localization length increase as the states depart from  
2 this point. The features described are also evident from the partial density of states at the barrier  
3 and at the channel region also shown in the right panel of Fig. 2. The barrier shows a big gap  
4 except for a small contribution from the edge state at the Fermi level. The density of states of the  
5 channels at the Fermi level is dominated by the edge states and the manifolds appear around it.  
6 They are still in the gap regions of the barrier indicating their localization.

7 In channels limited by graphane and in ribbons these two states remain pinned to the  
8 Fermi level until they separate at about the intermediate point  $1/3$  of the distance from the X  
9 point. For a semi-infinite plane, they will separate exactly with no gap between the manifolds at  
10 this point. However, in the channels limited by CF these two states disperse together  
11 quadratically up to this point before separating to join the manifolds. This quadratic dispersion  
12 signifies that the carriers in the channels will have a smaller effective mass with all its  
13 implications to mobility. Understanding the origin of this peculiar behavior will enable  
14 controlling the effective mass of this one dimensional channel with interesting implications for  
15 applications.

16 The origin of the dispersion of the edge state must be a property of CF affecting the  
17 interface. One important property is the large electron affinity of CF. Since fluorine is the most  
18 electronegative element of the periodic table there is an important charge transfer from the  
19 middle carbon layer to the external fluorine layers. From an electrostatic point of view, the  
20 system can be represented by two negative layers outside a central positively charged layer. All  
21 carbon atoms are sitting at a much lower potential than the vacuum level, much lower than, for  
22 example in graphane. This results in a very large electron affinity. We have estimated the  
23 electron affinity of CF as the difference between the vacuum level of the electrostatic potential  
Dispersion of Edge States and Quantum Confinement...



1 and the bottom of the conduction band to be 4.8 eV. This value is lower than the work function  
2 of graphene that we estimate using the same method to be 4.6 eV. This means that there will be  
3 an interface dipole formed at the junction between graphene and CF and the edge atoms of the  
4 channel will be sitting at a lower potential energy with respect to the center of the channel. To  
5 prove this hypothesis, we modified the tight-binding model used to describe the ribbons<sup>5, 6</sup>  
6 adding a term that lowers the site energy of the carbon  $p_z$  orbital at the edge with respect to the  
7 site energy of similar orbitals in the center of the channel. This simple modification indeed  
8 produces the desired effect. The resulting tight-binding band is plotted with continuous line in  
9 Fig. 2. The figure shows excellent agreement except for a slight deviation close to the  $\Gamma$  point  
10 where this band starts mixing more with other bands not considered in the simplified tight-  
11 binding model. This agreement was obtained for a site-energy at the edge that is 0.5 eV lower  
12 with respect to the other orbitals and a hopping integral equal to 2.3 eV. This confirms that the  
13 lowering of the site energy at the edge is a reasonable explanation for the dispersion relation of  
14 the edge states.

15 The agreement shown in Fig. 2 corresponds to a  $zz(6,12)$  structure. We found that all the  
16 structures we explored with channel widths from 8 to 12 can be fitted with the same excellent  
17 agreement using the same parameters for hopping and edge site energy. These fitting parameters  
18 are also a good value for different barrier widths. These results confirm the expectation that we  
19 are describing an effect whose origin is well localized at the interface and not affected by the  
20 presence of the other edge. It is possible that for very narrow channels both edge states influence  
21 each other. However, this is of no practical importance.

22 As a result of the lower site energy of the edge carbon atom, an evaluation of the charge  
23 distribution with the tight-binding model results in 5% more electrons occupying the edge orbital  
Dispersion of Edge States and Quantum Confinement...

1 with respect to the orbitals at the center of the channel. This result is in good agreement with  
 2 similar estimations with the DFT calculations.

3 ***Armchair channels.*** As the number of rows in the armchair channels increases, their  
 4 electronic structure around the Fermi level goes in a cycle of period three with two  
 5 semiconducting and one almost semimetallic case. This feature has been reported previously<sup>45</sup>  
 6 and is shared by the ribbons with<sup>5, 6</sup> and without<sup>7, 8</sup> hydrogen termination and with the channels  
 7 limited by graphane<sup>18</sup>. The results of our calculations are summarized in Fig. 3 where the  
 8 electronic band gap at the Fermi level is plotted as a function of the channel width for different  
 9 widths of the barrier. The Figure shows that the band gaps are almost independent of the size of  
 10 the barrier region for the rather small sizes represented here. As expected, this dependence will  
 11 disappear as the size of the barrier becomes large. The figure also shows that the band gap  
 12 obtained for each period decreases as the channel width increases due to a reduction of the  
 13 quantum confinement for wider channels. Let  $E_g(M, N)$  represent the gap, obtained by DFT, of  
 14 a structure with  $M$  rows in the barrier and  $N$  rows in the channel. The armchair channels can be  
 15 divided into three classes corresponding to  $N$  equal to  $3p$ ,  $3p+1$ , and  $3p+2$  for any natural  
 16 number  $p$ . The band gap follows the hierarchy  $E_g(M, 3p+1) > E_g(M, 3p) > E_g(M, 3p+2)$ . The  
 17  $3p$  and  $3p+1$  classes are semiconducting while the  $3p+2$  class is almost semimetallic with  
 18 bandgap on the order of few meV.

19 This hierarchy is different than the result expected from a tight binding model with  
 20 uniform hopping integrals and similar to the hierarchy obtained for hydrogenated ribbons by  
 21 Son, Cohen, and Louie.<sup>8</sup> These authors provided an interesting analysis of the origin of this  
 22 discrepancy that can be explained assuming a different hopping between the carbon atoms at the

Dispersion of Edge States and Quantum Confinement...

1 edge of the ribbon. They found expressions for the gaps of the different classes to first order in  
 2 the hopping perturbation. Their results for these gaps,  $\Delta_{3p}$ ,  $\Delta_{3p+1}$ , and  $\Delta_{3p+2}$  are provided in  
 3 Eq. (1) of their paper. The DFT results in their case can be reproduced if they assume a hopping  
 4 integral in ribbon  $t = 2.7$  eV except at the edge where the hopping integral is 12% larger. We  
 5 notice that, contrary to this observations, Muñoz and coworkers<sup>45</sup> obtain a different hierarchy for  
 6 the gaps. In view of the tight binding model, this difference can be related to the hoping integral  
 7 at the edge and possibly to difference in the relaxation geometry.

8 As can be seen in Fig. 3, although there is some variation in each class due to the  
 9 different barrier widths considered, our results for the channels limited by CF barriers can also be  
 10 described by the same model. We can reproduce the behavior of our DFT results assuming a  
 11 hopping integral  $t = 2.6$  eV except for the edge carbon atoms where the hopping integral is 9%  
 12 larger. The beauty of these expressions is that it permits a correct extrapolation to larger channel  
 13 widths, not accesible to DFT calculations but more easy to realize experimentally. This  
 14 extrapolation to large channel width,  $W_a$ , is  $\Delta_i \rightarrow a_i W_a^{-1}$ . It behaves as expected, scaling as the  
 15 inverse of the width with a coefficient for each class given by

$$\begin{aligned}
 a_{3p} &= ta(\pi - \delta 6\sqrt{3}) \approx 0.81 \text{ eV.nm} \\
 a_{3p+1} &= ta(\pi + \delta 3\sqrt{3}) \approx 1.33 \text{ eV.nm} \\
 a_{3p+2} &= ta\delta 3\sqrt{3} \approx 0.17 \text{ eV.nm}
 \end{aligned}
 \tag{2}$$

17 where  $a = 0.142$  nm is the distance between carbon atoms in graphene.

18 In addition to the interesting behavior of the gap, the electronic states close to the Fermi  
 19 level are localized in the channel. Fig. 4 shows two typical band structures for armchair channels.  
 20 The top panel corresponds to a semiconducting channel, ac(5,13) with a width of 15 Å, and the

Dispersion of Edge States and Quantum Confinement...



1 state that moves along the edge of the channel. The dispersion relation of this state, along the X-  
2  $\Gamma$ , direction determines the effective mass of this carrier. In channels limited by graphene or in  
3 ribbons, the effective mass of this carrier is very high; the state shows a flat band at the Fermi  
4 level. For the channels limited by graphene fluoride, this band shows a quadratic dispersion  
5 indicating a lower effective mass of carriers. A tight-binding analysis indicates that the quadratic  
6 dispersion can be explained by a lower site-energy of the Carbon atoms  $p_z$  orbitals at the edge  
7 of the channel. We argue that this effect is caused by the large electron affinity of CF that  
8 produces an interfacial dipole moment and lowers the electrostatic potential in this region. The  
9 extra charge accumulated in response by this change in the electrostatic potential is observed in  
10 the DFT calculations and is in good agreement with the results of the tight binding model. It is  
11 important to notice that these results are independent of the exact value of the band gap of the  
12 barrier region, a quantity that it is so far unknown with theoretical values ranging from 3.1 eV  
13 using DFT/GGA<sup>24</sup> to 7.4 eV using GW<sup>25, 26</sup>. As long as the CF region produces a negative  
14 electrostatic potential on the carbon plane, the carbon atoms at the edge will be more attractive to  
15 electrons and, as demonstrated in our work, will add dispersion to the edge states.

16 This observation suggests a method to control the effective mass of carriers in the  
17 channel by modifying the electrostatic potential around the edge. This can be done by a localized  
18 knife shaped gate potential<sup>46</sup> or by the selective absorption of ferroelectric polymers such as  
19 polyvinylfluoride<sup>47</sup> that are chemically compatible with graphene fluoride. The change in the  
20 effective mass of the carriers close to the Fermi level will induce a change on the mobility<sup>48</sup> and  
21 on the magnetic properties of the channels<sup>49</sup>. It is interesting to notice that the formation of a  
22 magnetic moment on the edge atoms of the ribbons is a consequence of a competition between  
23 the intrasite Coulomb repulsion in the  $p_z$  orbitals and the hopping between edge sites. A smaller  
Dispersion of Edge States and Quantum Confinement...

1 effective mass of the edge states corresponds to a larger hopping probability between edge sites.  
2 This larger hopping may overcome the Coulomb induced localization and remove the localized  
3 magnetization. Our group is currently working on these possibilities.

4         The armchair channels are less affected by the materials that provide the confinement and  
5 the graphene fluoride embedded structures have similar electronic structure to the graphene  
6 embedded structures or the ribbons. This is expected because, in the absence of edge states, all  
7 states in the channel have very low weight of their wave function on the carbon atoms close to  
8 the edge. A tight binding analysis shows that the main effect at the interface is given by a 9%  
9 increase of the hopping integral between carbon atoms at the edge. This assumption explains the  
10 scaling and relative values of band gaps for different width of the channels. The one-dimensional  
11 bands observed in the armchair channels of the  $3p+2$  class derive from the Dirac points of the  
12 graphene band structure and possess very interesting symmetry properties.

13         The experimental realization of these structures has already been attempted in many  
14 labs<sup>31, 35, 50</sup> and their stability depends on the diffusion of fluorine on graphene. Our current  
15 estimate for the diffusion barrier of an isolated fluorine atom on graphene is of the order of  
16 0.3 eV. Assuming a standard attempt jump frequency of  $10^{13}$  1/s, this barrier implies a diffusion  
17 coefficient of  $2 \times 10^8$  nm<sup>2</sup>/s at 300K. However, if the fluorine atom is close to other fluorine  
18 atoms on the surface of graphene, the barrier for diffusion is of the order of 1 eV and the  
19 diffusion coefficient is as low as  $3 \times 10^4$  nm<sup>2</sup>/s at the same temperature. These diffusion barriers  
20 have been estimated with the nudged elastic band method<sup>51, 52</sup> with the same setup used for all  
21 other VASP calculations in this paper. A similar result was recently reported for the case of  
22 hydrogen on graphene.<sup>53</sup> Ao and coworkers report that the barrier for hydrogen diffusion on  
23 graphene is almost 10 times larger when the hydrogen atoms are at the armchair or zigzag  
Dispersion of Edge States and Quantum Confinement...

1 interfaces. These results seem to indicate that, although isolated fluorine atoms will diffuse quite  
2 fast on the surface, once assembled in the region of the barrier, the structure will be stable at  
3 room temperature.

4 **Acknowledgments.** This work was supported by NSF MRSEC DMR-0820404, and by the  
5 Donors of the American Chemical Society Petroleum Research Fund. The authors acknowledge  
6 use of facilities at the NSF NNIN and the Penn State Materials Simulation Center.

#### 7 REFERENCES

- 8 <sup>1</sup> K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, Y. Zhang, S. V. Dubonos, I. V.  
9 Grigorieva, and A. A. Firsov, *Science* **306**, 666 (2004).
- 10 <sup>2</sup> K. S. Novoselov, et al., *Science* **315**, 1379 (2007).
- 11 <sup>3</sup> P. Neugebauer, M. Orlita, C. Faugeras, A. L. Barra, and M. Potemski, *Phys. Rev. Lett.* **103**,  
12 136403 (2009).
- 13 <sup>4</sup> W. K. Tse, E. H. Hwang, and D. S. Sarma, *Appl. Phys. Lett.* **93**, 023128 (2008).
- 14 <sup>5</sup> K. Nakada, M. Fujita, G. Dresselhaus, and M. S. Dresselhaus, *Phys. Rev. B* **54**, 17954 (1996).
- 15 <sup>6</sup> M. Fujita, K. Wakabayashi, K. Nakada, and K. Kusakabe, *J. Phys. Soc. Jpn.* **65**, 1920 (1996).
- 16 <sup>7</sup> Y. W. Son, M. L. Cohen, and S. G. Louie, *Nature* **444**, 347 (2006).
- 17 <sup>8</sup> Y. W. Son, M. L. Cohen, and S. G. Louie, *Phys. Rev. Lett.* **97**, 216803 (2006).
- 18 <sup>9</sup> M. Y. Han, B. Ozyilmaz, Y. B. Zhang, and P. Kim, *Phys. Rev. Lett.* **98**, 206805 (2007).
- 19 <sup>10</sup> Z. H. Chen, Y. M. Lin, M. J. Rooks, and P. Avouris, *Physica E* **40**, 228 (2007).
- 20 <sup>11</sup> L. Tapasztó, G. Dobrik, P. Lambin, and L. P. Biro, *Nat. Nanotechnol.* **3**, 397 (2008).
- 21 <sup>12</sup> X. L. Li, X. R. Wang, L. Zhang, S. W. Lee, and H. J. Dai, *Science* **319**, 1229 (2008).
- 22 <sup>13</sup> X. R. Wang, Y. J. Ouyang, X. L. Li, H. L. Wang, J. Guo, and H. J. Dai, *Phys. Rev. Lett.* **100**,  
23 206803 (2008).

Dispersion of Edge States and Quantum Confinement...

- 1 <sup>14</sup> R. Ruoff, *Nat. Nanotechnol.* **3**, 10 (2008).
- 2 <sup>15</sup> J. O. Sofo, A. S. Chaudhari, and G. D. Barber, *Phys. Rev. B* **75**, 153401 (2007).
- 3 <sup>16</sup> M. H. F. Sluiter and Y. Kawazoe, *Phys. Rev. B* **68**, 085410 (2003).
- 4 <sup>17</sup> D. C. Elias, et al., *Science* **323**, 610 (2009).
- 5 <sup>18</sup> A. K. Singh and B. I. Yakobson, *Nano Lett.* **9**, 1540 (2009).
- 6 <sup>19</sup> H. Touhara, et al., *J. Fluorine Chem.* **114**, 181 (2002).
- 7 <sup>20</sup> Y. Sato, K. Itoh, R. Hagiwara, T. Fukunaga, and Y. Ito, *Carbon* **42**, 2897 (2004).
- 8 <sup>21</sup> H. Touhara and F. Okino, *Carbon* **38**, 241 (2000).
- 9 <sup>22</sup> D. E. Parry, J. M. Thomas, B. Bach, and E. L. Evans, *Chem. Phys. Lett.* **29**, 128 (1974).
- 10 <sup>23</sup> V. K. Mahajan, Badachha.Rb, and J. L. Margrave, *Inorg. Nuc. Chem. Lett.* **10**, 1103 (1974).
- 11 <sup>24</sup> J. C. Charlier, X. Gonze, and J. P. Michenaud, *Phys. Rev. B* **47**, 16162 (1993).
- 12 <sup>25</sup> M. Klintonberg, S. Lebègue, M. I. Katsnelson, and O. Eriksson, *Phys. Rev. B* **81**, 085433
- 13 (2010).
- 14 <sup>26</sup> O. Leenaerts, H. Peelaers, A. D. Hernández-Nieves, B. Partoens, and F. M. Peeters, *Phys.*
- 15 *Rev. B* **82**, 195436 (2010).
- 16 <sup>27</sup> Y. Sato, R. Hagiwara, and Y. Ito, *J. Fluorine Chem.* **110**, 31 (2001).
- 17 <sup>28</sup> Y. Sato, H. Watano, R. Hagiwara, and Y. Ito, *Carbon* **44**, 664 (2006).
- 18 <sup>29</sup> Y. Sato, S. Shiraishi, H. Watano, R. Hagiwara, and Y. Ito, *Carbon* **41**, 1149 (2003).
- 19 <sup>30</sup> N. Kumagai, M. Kawamura, H. Hirohata, K. Tanno, Y. Chong, and N. Watanabe, *J. Appl.*
- 20 *Electrochem.* **25**, 869 (1995).
- 21 <sup>31</sup> S. H. Cheng, K. Zou, F. Okino, H. R. Gutierrez, A. Gupta, N. Shen, P. C. Eklund, J. O. Sofo,
- 22 and J. Zhu, *Phys. Rev. B* **81**, 205435 (2010).



- 1 <sup>32</sup> A. B. Bourlinos, V. Georgakilas, R. Zboril, D. Jancik, M. A. Karakassides, A. Stassinopoulos,  
2 D. Anglos, and E. P. Giannelis, *J. Fluorine Chem.* **129**, 720 (2008).
- 3 <sup>33</sup> J. Giraudet, M. Dubois, J. Inacio, and A. Hamwi, *Carbon* **41**, 453 (2003).
- 4 <sup>34</sup> R. R. R. Nair, W. C.; Jalil, R.; Riaz, I.; Kravets, V. G.; Britnell, L.; Blake, P.; Schedin, F.;  
5 Mayorov, A. S.; Yuan, S.; Katsnelson, M. I.; Cheng, H. M.; Strupinski, W.; Bulusheva, L. G.;  
6 Okotrub, A. V.; Novoselov, K. S.; Geim, A. K.; Grigorieva, I. V.; Grigorenko, A. N., *Small* **6**,  
7 2877 (2010).
- 8 <sup>35</sup> J. T. Robinson, et al., *Nano Lett.* (2010).
- 9 <sup>36</sup> G. Kresse and J. Hafner, *Phys. Rev. B* **47**, 558 (1993).
- 10 <sup>37</sup> G. Kresse and J. Hafner, *J. Phys.: Condens. Matter* **6**, 8245 (1994).
- 11 <sup>38</sup> G. Kresse and J. Furthmüller, *Phys. Rev. B* **54**, 11169 (1996).
- 12 <sup>39</sup> G. Kresse and J. Furthmüller, *Comput. Mater. Sci.* **6**, 15 (1996).
- 13 <sup>40</sup> P. E. Blöchl, *Phys. Rev. B* **50**, 17953 (1994).
- 14 <sup>41</sup> G. Kresse and D. Joubert, *Phys. Rev. B* **59**, 1758 (1999).
- 15 <sup>42</sup> J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **77**, 3865 (1996).
- 16 <sup>43</sup> J. P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* **78**, 1396 (1997).
- 17 <sup>44</sup> H. J. Monkhorst and J. D. Pack, *Phys. Rev. B* **13**, 5188 (1976).
- 18 <sup>45</sup> E. Muñoz, A. K. Singh, M. A. Ribas, E. S. Penev, and B. I. Yakobson, *Diamond Relat. Mater.*  
19 **19**, 368 (2010).
- 20 <sup>46</sup> S. Woo and Y. W. Son, in <http://meetings.aps.org/link/BAPS.2010.MAR.W22.4>.
- 21 <sup>47</sup> Y.-L. Lee, S. Kim, C. Park, J. Ihm, and Y.-W. Son, *ACS Nano* **4**, 1345 (2010).
- 22 <sup>48</sup> M. Q. Long, L. Tang, and D. Wang, *J. Am. Chem. Soc.* **131** 17728 (2009 ).
- 23 <sup>49</sup> L. Pisani, J. A. Chan, B. Montanari, and N. M. Harrison, *Phys. Rev. B* **75**, 064418 (2007).  
Dispersion of Edge States and Quantum Confinement...

1 <sup>50</sup> M. Baraket, S. G. Walton, E. H. Lock, J. T. Robinson, and F. K. Perkins, *Appl. Phys. Lett.* **96**,  
2 231501 (2010).

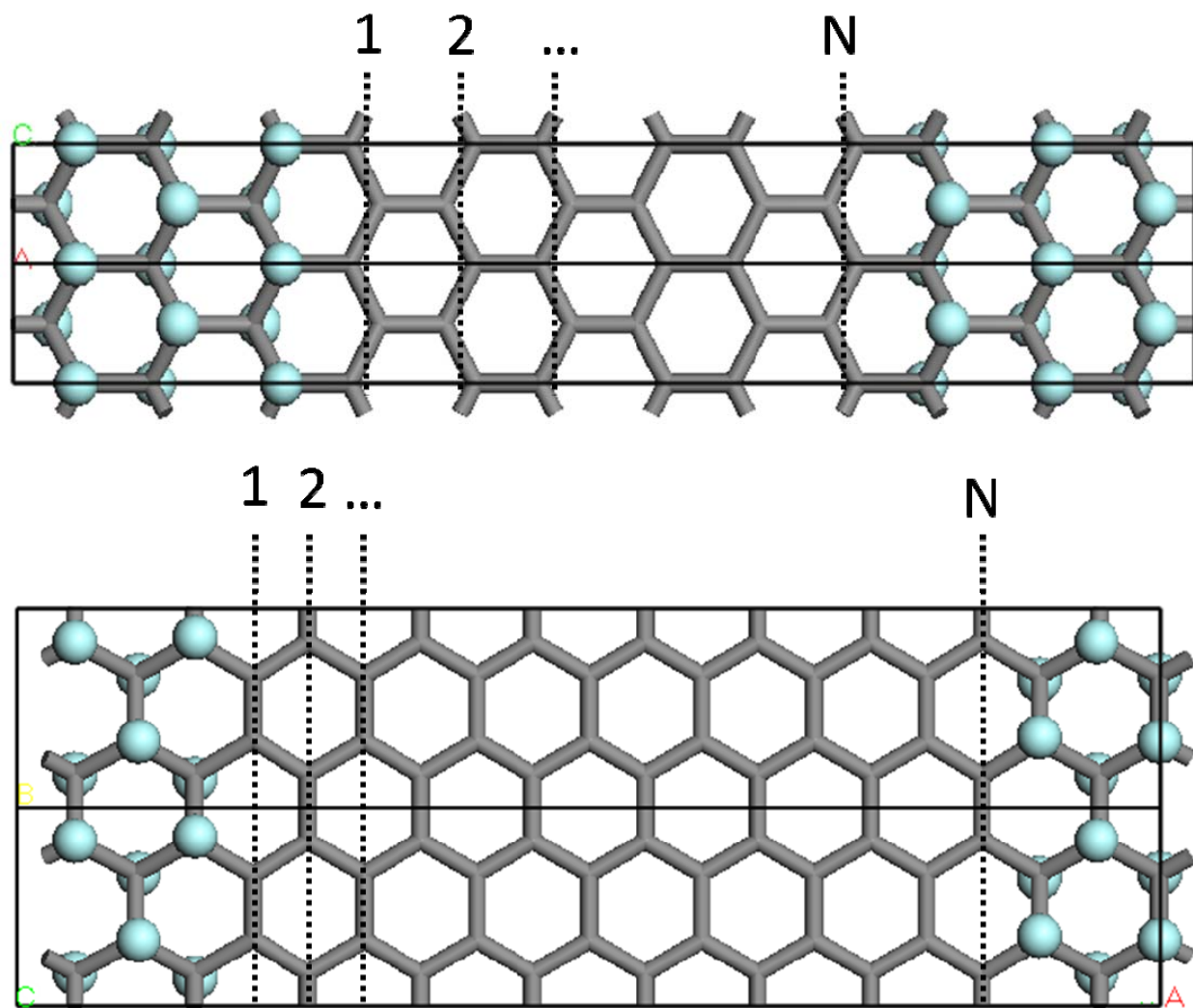
3 <sup>51</sup> G. Henkelman and H. Jonsson, *J. Chem. Phys.* **113**, 9978 (2000).

4 <sup>52</sup> D. Sheppard, R. Terrell, and G. Henkelman, *J. Chem. Phys.* **128**, 134106 (2008).

5 <sup>53</sup> Z. M. Ao, A. D. Hernandez-Nieves, F. M. Peeters, and S. Li, *Appl. Phys. Lett.* **97**, 233109  
6 (2010).

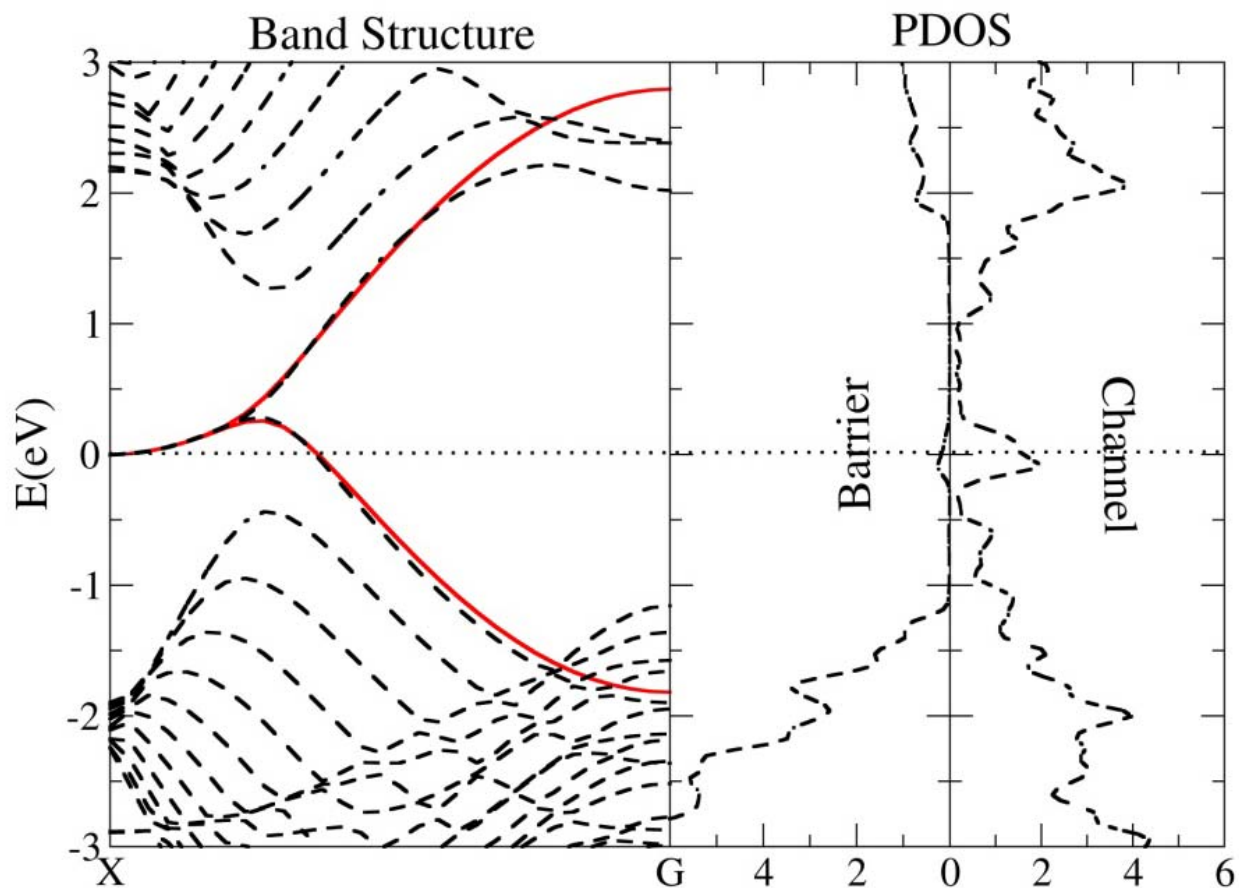
7

8



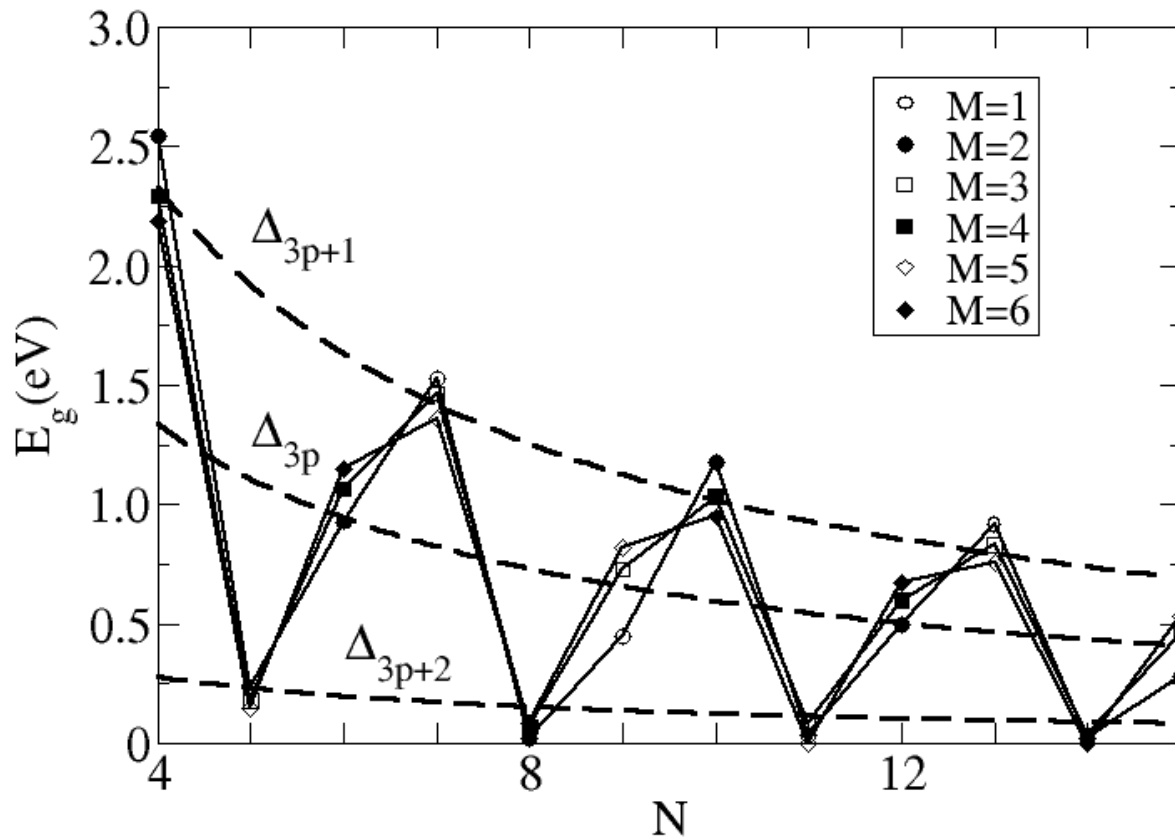
1  
 2 FIG. 1. (color online) Zigzag (top) and armchair (bottom) channels of graphene limited by a  
 3 barrier region of graphene fluoride. The carbon network is represented in gray while the fluorine  
 4 atoms are represented by light blue balls. For each geometry we indicate the convention to count  
 5 the number of rows in the channel; this is generically called  $N$  in the text. The number of rows in  
 6 the barrier region is generically called  $M$  and counted in the same way. For clarity, we present  
 7 two unit cells are presented in each case.

8



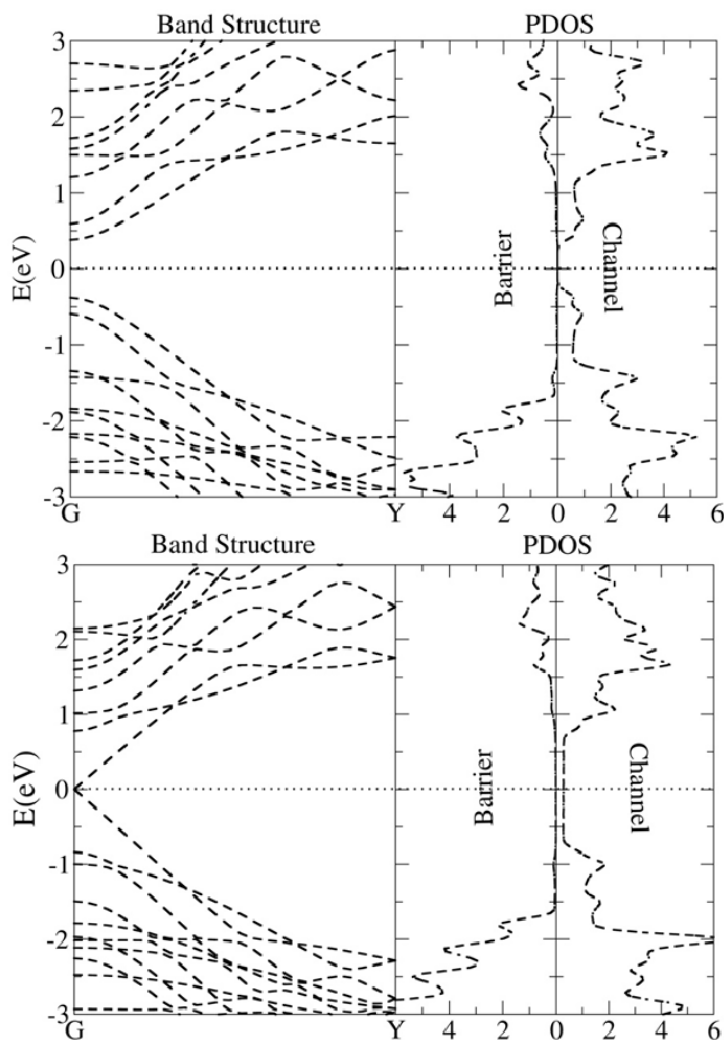
1  
 2 FIG. 2. (color online) Band structure on the left and partial density of states of barrier and  
 3 channel region of a zigzag structure  $zz(6,12)$ . The tight binding approximation of the edge state  
 4 around the Fermi level is shown with a continuous line in red. The tight binding model  
 5 demonstrates that the dispersion relation of the edge state is controlled by the site energy of the  
 6 carbon atoms at the edge.

7



1  
 2 FIG. 3. (color online) Band gap of armchair channels as a function of the number of rows in the  
 3 channel,  $N$ , for different number of rows in the barrier,  $M$ . The dashed lines correspond to the  
 4 tight-binding approximation with hopping integral equal to 2.6 eV and a 9% increase of the  
 5 hopping at the edge.

6



1  
 2 FIG. 4. (color online) Band structure and partial density of states in the barrier and channel  
 3 region of two representative armchair channels. The top panel corresponds to a semiconducting  
 4 channel,  $ac(5,13)$ , and the bottom panel to a semi-metallic channel,  $ac(6,14)$ . From the band  
 5 structure in the top panel, we see that the semiconducting armchair channel has a direct gap.  
 6 From the density of states we see that the states close to the gap are localized within the channel  
 7 because the gap in the channel is centered with respect to the gap in the barrier. For the band  
 8 structure in the bottom panel we see that the semimetallic structures have a one-dimensional  
 9 linear band, localized within the channel and producing a constant density of states.

Dispersion of Edge States and Quantum Confinement...