

In press at
Algebras, Groups and Geometris, Vol. 21, 2004

DISPROOFS OF RIEMANN'S HYPOTHESIS

Chun-Xuan, Jiang

P.O.Box 3924, Beijing 100854, China
and Institute for Basic Research
P.O.Box 1577, Palm Harbor, FL 34682, U.S.A.
liukxi@public3.bta.net.cn

Abstract

As it is well known, the Riemann hypothesis on the zeros of the $\zeta(s)$ function has been assumed to be true in various basic developments of the 20-th century mathematics, although it has never been proved to be correct. The need for a resolution of this open historical problem has been voiced by several distinguished mathematicians. By using preceding works, in this paper we present comprehensive disproofs of the Riemann hypothesis. Moreover, in 1994 the author discovered the arithmetic function $J_n(\omega)$ that can replace Riemann's $\zeta(s)$ function in view of its proved features: if $J_n(\omega) \neq 0$, then the function has infinitely many prime solutions; and if $J_n(\omega) = 0$, then the function has finitely many prime solutions. By using the Jiang $J_2(\omega)$ function we prove the twin prime theorem, Goldbach's theorem and the prime theorem of the form $x^2 + 1$. Due to the importance of resolving the historical open nature of the Riemann hypothesis, comments by interested colleagues are here solicited.

AMS mathematics subject classification: Primary 11M26.

1. Introduction

In 1859 Riemann defined the zeta function[1]

$$\zeta(s) = \prod_p (1 - p^{-s})^{-1} = \sum_{n=1}^{\infty} \frac{1}{n^s}, \quad (1)$$

where $s = \sigma + ti$, $i = \sqrt{-1}$, σ and t are real, p ranges over all primes. $\zeta(s)$ satisfies the functional equation [2]

$$\pi^{-\frac{s}{2}} \Gamma\left(\frac{s}{2}\right) \zeta(s) = \pi^{-\frac{(1-s)}{2}} \Gamma\left(\frac{1-s}{2}\right) \zeta(1-s). \quad (2)$$

From (2) we have

$$\zeta(ti) \neq 0. \quad (3)$$

Riemann conjectured that $\zeta(s)$ has infinitely many zeros in $0 \leq \sigma \leq 1$, called the critical strip. Riemann further made the remarkable conjecture that the zeros of $\zeta(s)$ in the critical strip all lie on the central line $\sigma = 1/2$, a conjecture called the famous **Riemann hypothesis** (RH).

It was stated by Hardy in 1914 that infinitely many zeros lie on the line; A. Selberg stated in 1942 that a positive proportion at least of all the zeros lie on the line; Levinson stated in 1974 that more than one third of the zeros lie on the line; Conrey stated in 1989 that at least two fifths of the zeros lie on the line.

The use of the RH then lead to many mathematical problems, such as the generalized Riemann conjecture, Artin's conjecture, Weil's conjecture, Langlands' program, quantum chaos, the hypothetical Riemann flow [3, 4], the zeta functions and L-functions of an algebraic variety and other studies. Similarly, it is possible to prove many theorems by using the RH.

However, the RH remains a basically unproved conjecture to this day. In fact, Hilbert properly stated in 199 that the problem of proving or disproving the RH is one of the most important problems confronting 20th century mathematicians. In 2000 Griffiths and Graham pointed out that the RH is the first challenging problem for the 21st century. The proof of the RH then become the millennium prize problem.

In 1997 we studied the tables of the Riemann zeta function [5] and reached preliminary results indicating that the RH is false [6, 7, 8]. In

this paper we present a comprehensive disproof of the RH and show that the computation of all zeros of the $\zeta(1/2 + ti)$ function done during the past 100 years is in error, as preliminarily indicated in Refs. [9, 10, 11]. Since the RH is false, all theorems and conjectures based to the same are also false.

2. Disproofs of Riemann's Hypothesis

Theorem 1. $\zeta(s)$ has no zeros in the critical strip, that is $\zeta(s) \neq 0$, where $0 \leq \sigma \leq 1$.

Proof 1. From (1) we have

$$\frac{1}{\zeta(s)} = \prod_p \left(1 - \frac{1}{p^s}\right) = Re^{\theta i}, \quad (4)$$

where

$$R = \prod_p R_p, \quad R_p = \sqrt{1 - \frac{2 \cos(t \log p)}{p^\sigma} + \frac{1}{p^{2\sigma}}}, \quad (5)$$

$$\theta = \sum_p \theta_p, \quad \theta_p = \tan^{-1} \frac{\sin(t \log p)}{p^\sigma - \cos(t \log p)}. \quad (6)$$

If $\sigma = 0$, from (5) we have $R_p = \sqrt{2} \sqrt{1 - \cos(t \log p)}$. If $\cos(t \log p) = 1$, we have $R_p = 0$ then $R = 0$. If $\sigma > 0$ from (5) we have $R_p \neq 0$. $\zeta(s) = 0$ if and only if $\text{Re } \zeta(s) = 0$ and $\text{Im } \zeta(s) = 0$, that is $R = \infty$. From (5) we have that if $\cos(t \log p) \leq 0$ then $R_p > 1$ and if $\cos(t \log p) > 0$ then $R_p < 1$. $\cos(t \log p)$ is independent of the real part σ , but may well depend on primes p and imaginary part t . We write $m_+(t)$ for the number of primes p satisfying $\cos(t \log p) > 0$, $m_-(t)$ for the number of primes p satisfying $\cos(t \log p) \leq 0$.

For $\cos(t \log p) > 0$, we have

$$1 > R_p(1 + ti) > R_p(0.5 + ti). \quad (7)$$

If $m_+(t_1)$ is much greater than $m_-(t_1)$ such that $R(0.5 + t_1 i) = \min$. From (5), (6) and (7) we have for given t_1

$$\begin{aligned} \min R(\sigma_1 + t_1 i) &> \min R(1 + t_1 i) > \min R(0.5 + t_1 i) \\ &> \min R(\sigma_2 + t_1 i) \rightarrow 0, \end{aligned}$$

(8)

$$\theta(\sigma_1 + t_1 i) = \theta(1 + t_1 i) = \theta(0.5 + t_1 i) = \theta(\sigma_2 + t_1 i) = \text{const} \quad (9)$$

where $\sigma_1 > 1$ and $0 \leq \sigma_2 < 0.5$.

Since $|\zeta(s)| = \frac{1}{R}$ from (8) we have

$$\begin{aligned} \max |\zeta(\sigma_1 + t_1 i)| &< \max |\zeta(1 + t_1 i)| \\ &< \max |\zeta(0.5 + t_1 i)| < \max |\zeta(\sigma_2 + t_1 i)| \rightarrow \infty. \end{aligned} \quad (10)$$

For $\cos(t \log p) < 0$ we have

$$1 < R_p(0.5 + ti) < R_p(0.4 + ti) < R_p(0.3 + ti). \quad (11)$$

If $m_-(t_1)$ is much greater than $m_+(t_1)$ such that $R(0.5 + t_1 i) = \max$. From (5), (6) and (11) we have for given t_1

$$\begin{aligned} \max R(\sigma_1 + t_1 i) &< \max R(0.5 + t_1 i) < \max R(0.4 + t_1 i), \\ &< \max R(0.3 + t_1 i) < \max R(\sigma_2 + t_1 i) \neq \infty, \end{aligned} \quad (12)$$

$$\begin{aligned} \theta(\sigma_1 + t_1 i) &= \theta(0.5 + t_1 i) = \theta(0.4 + t_1 i) \\ &= \theta(0.3 + t_1 i) = \theta(\sigma_2 + t_1 i) = \text{const}, \end{aligned} \quad (13)$$

where $\sigma_1 > 0.5$ and $0 \leq \sigma_2 < 0.3$.

Since $|\zeta(s)| = \frac{1}{R}$ from (12) we have

$$\begin{aligned} \min |\zeta(\sigma_1 + t_1 i)| &> \min |\zeta(0.5 + t_1 i)| > \min |\zeta(0.4 + t_1 i)| > \\ &\min |\zeta(0.3 + t_1 i)| > \min |\zeta(\sigma_2 + t_1 i)| \neq 0. \end{aligned} \quad (14)$$

Proof 2. We define the beta function

$$\beta(s) = \prod_p (1 + p^{-s})^{-1} = \sum_{n=1}^{\infty} \frac{\lambda(n)}{n^s}, \quad (15)$$

where $\lambda(1) = 1$, $\lambda(n) = (-1)^{a_1 + \dots + a_k}$ if $n = p_1^{a_1} \dots p_k^{a_k}$, $t \neq 0$.

From (15) we have

$$\frac{1}{\beta(s)} = \prod_p \left(1 + \frac{1}{p^s}\right) = \bar{R}e^{\bar{\theta}i}, \quad (16)$$

where

$$\bar{R} = \prod_p \bar{R}_p, \bar{R}_p = \sqrt{1 + \frac{2 \cos(t \log p)}{p^\sigma} + \frac{1}{p^{2\sigma}}}, \quad (17)$$

$$\bar{\theta} = \sum_p \bar{\theta}_p, \bar{\theta}_p = \tan^{-1} \frac{-\sin(t \log p)}{p^\sigma + \cos(t \log p)}. \quad (18)$$

For $\cos(t \log p) < 0$, we have

$$1 > \bar{R}_p(1 + ti) > \bar{R}_p(0.5 + ti). \quad (19)$$

If $m_-(t_1)$ is much greater than $m_+(t_1)$ such that $\bar{R}(0.5 + t_1i) = \min$. From (17), (18) and (19) we have for given t_1

$$\begin{aligned} \min \bar{R}(\sigma_1 + t_1i) &> \min \bar{R}(1 + t_1i) > \min \bar{R}(0.5 + t_1i) \\ &> \min \bar{R}(\sigma_2 + t_1i) \rightarrow 0, \end{aligned} \quad (20)$$

$$\bar{\theta}(\sigma_1 + t_1i) = \bar{\theta}(1 + t_1i) = \bar{\theta}(0.5 + t_1i) = \bar{\theta}(\sigma_2 + t_1i) = \text{const}, \quad (21)$$

where $\sigma_1 >$ and $0 \leq \sigma_2 < 0.5$.

Since $|\beta(s)| = \frac{1}{\bar{R}}$ from (20) we have

$$\begin{aligned} \max |\beta(\sigma_1 + t_1i)| &< \max |\beta(1 + t_1i)| \\ &< \max |\beta(0.5 + t_1i)| < \max |\beta(\sigma_2 + t_1i)| \rightarrow \infty. \end{aligned} \quad (22)$$

For $\cos(t \log p) > 0$ we have

$$1 < \bar{R}_p(0.5 + ti) < \bar{R}_p(0.4 + ti) < \bar{R}_p(0.3 + ti). \quad (23)$$

If $m_+(t_1)$ is much greater than $m_-(t_1)$ such that that $\bar{R}(0.5 + t_1i) = \max$. From (17), (18) and (23) we have for given t_1

$$\begin{aligned} \max \bar{R}(\sigma_1 + t_1i) &< \max \bar{R}(0.5 + t_1i) < \max \bar{R}(0.4 + t_1i) \\ &< \max \bar{R}(0.3 + t_1i) < \max \bar{R}(\sigma_2 + t_1i) \neq \infty, \end{aligned} \quad (24)$$

$$\begin{aligned}
\bar{\theta}(\sigma_1 + t_1 i) &= \bar{\theta}(0.5 + t_1 i) = \bar{\theta}(0.4 + t_1 i) \\
&= \bar{\theta}(0.3 + t_1 i) = \bar{\theta}(\sigma_2 + t_1 i) = \text{const},
\end{aligned}
\tag{25}$$

where $\sigma_1 > 0.5$ and $0 \leq \sigma_2 < 0.3$.
Since $|\beta(s)| = \frac{1}{R}$ from (24) we have

$$\begin{aligned}
\min |\beta(\sigma_1 + t_1 i)| &> \min |\beta(0.5 + t_1 i)| \\
&> \min |\beta(0.4 + t_1 i)| \\
\min |\beta(0.3 + t_1 i)| &> \min |\beta(\sigma_2 + t_1 i)| \neq 0.
\end{aligned}
\tag{26}$$

From (1) and (15) we have

$$\zeta(2s) = \zeta(s)\beta(s). \tag{27}$$

In 1896 J. Hadamard and de la Vallee Poussin proved independently $|\zeta(1 + ti)| \neq 0$. From (27) we have

$$|\zeta(1 + 2ti)| = |\zeta(\frac{1}{2} + ti)| |\beta(\frac{1}{2} + ti)| \neq 0. \tag{28}$$

From (28) we have

$$|\zeta(\frac{1}{2} + ti)| \neq 0 \quad \text{and} \quad |\beta(\frac{1}{2} + ti)| \neq 0. \tag{29}$$

$\zeta(s)$ and $\beta(s)$ are the dual functions. From (22) we have

$$|\beta(\frac{1}{2} + ti)| \neq \infty. \tag{30}$$

Therefore we have

$$|\zeta(\frac{1}{2} + ti)| \neq 0. \tag{31}$$

In the same way we have

$$|\zeta(\frac{1}{2} + 2ti)| = |\zeta(\frac{1}{4} + ti)| |\beta(\frac{1}{4} + ti)| \neq 0. \tag{32}$$

From (32) we have

$$|\zeta(\frac{1}{4} + ti)| \neq 0 \quad \text{and} \quad |\beta(\frac{1}{4} + ti)| \neq 0. \quad (33)$$

In the same way we have

$$|\zeta(\frac{1}{2^n} + ti)| \neq 0. \quad (34)$$

As $n \rightarrow \infty$ we have

$$|\zeta(ti)| \neq 0. \quad (35)$$

Proof 3. For $\sigma > 1$ we have

$$\log \zeta(s) = \sum_p \sum_{m=1}^{\infty} m^{-1} p^{-m\sigma} \exp(-itm \log p). \quad (36)$$

If $\zeta(s)$ had a zero at $\frac{1}{2} + ti$, then $\log |\zeta(\sigma + ti)|$ would tend to $-\infty$ as σ tends to $\frac{1}{2}$ from the right. From (36) we have

$$\log |\zeta(s)| = \sum_p \sum_{m=1}^{\infty} m^{-1} p^{-m\sigma} \cos(tm \log p), \quad (37)$$

with t replaced by $0, t, 2t, \dots, Ht$, it gives

$$\begin{aligned} \sum_{j=0}^{H-1} \binom{2H}{j} \log |\zeta(\sigma + (H-j)ti)| + \frac{1}{2} \binom{2H}{H} \\ \log \zeta(\sigma) = \sum_p \sum_{m=1}^{\infty} m^{-1} p^{-m\sigma} A \geq 0, \end{aligned} \quad (38)$$

where

$$\begin{aligned} A &= \sum_{j=0}^{H-1} \binom{2H}{j} \cos((H-j)tm \log p) + \frac{1}{2} \binom{2H}{H} \\ &= 2^{H-1} [1 + \cos(tm \log p)]^H \geq 0, \end{aligned} \quad (39)$$

H is an even number.

From (38) we have

$$(\zeta(\sigma))^{\frac{1}{2}} \binom{2H}{H} \prod_{j=0}^{H-1} |\zeta(\sigma + (H-j)ti)| \binom{2H}{j} \geq 1. \quad (40)$$

Since $|\zeta(\frac{1}{2} + eti)| \neq \infty$ [5], where $e = 1, 2, \dots, H$, from (40) we have $|\zeta(\frac{1}{2} + eti)| \neq 0$ for sufficiently large even number H .

Min $|\zeta(\frac{1}{2} + ti)| \approx 0$ but $\neq 0$. The computation of all zeros of $\zeta(\frac{1}{2} + ti)$ is error, which satisfies the the error RH.

From (39) we have

$$\begin{aligned} \cos 2\theta + 4 \cos \theta + 3 &= 2(1 + \cos \theta)^2, \\ \cos 4\theta + 8 \cos 3\theta + 28 \cos 2\theta + 56 \cos \theta + 35 &= 8(1 + \cos \theta)^4, \\ \cos 5\theta + 12 \cos 5\theta + 66 \cos 4\theta + 220 \cos 3\theta \\ + 495 \cos 2\theta + 792 \cos \theta + 462 &= 32(1 + \cos \theta)^6. \end{aligned}$$

3. The Arithmetic Function $J_n(\omega)$ Replacing Riemann's Hypothesis

In view of the preceding results, the RH has no value for the study of prime distributions. In 1994 the author discover the arithmetic function $J_n(\omega)$ [12, 13] that is able to take the place of Riemann's zeta-functions and L-functions because of the following properties: $J_n(\omega) \neq 0$, then the function has infinitely many prime solutions; and if $J_n(\omega) = 0$, then the function has finitely many prime solutions.

By using Jiang's $J_n(\omega)$ function we have proved numerous theorems including the twin prime theorem, Goldbach's theorem, the prime k-tuples theorem, Santilli's theory for a prime table, the theorem of finite Fermat primes, the theorem of finite Mersenne primes, the theorem of finite repunit primes, there are infinitely many triples of $n, n+1$ and $n+2$ that each is the product of k distinct primes, there are infinitely many Carmichael numbers which are product of exactly five primes, there there are finitely many Carmichael numbers which are product of exactly six primes \dots in the prime distributions [14]. We give some theorems below

Theorem 2. Twin prime theorem: $p_1 = p + 2$.

We have the arithmetic function

$$J_2(\omega) = \prod_{3 \leq p \leq p_i} (p - 2) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many primes p such that p_1 is a prime.

Theorem 3. Goldbach theorem: $N = p_1 + p_2$.

We have the arithmetic function

$$J_2(\omega) = \prod_{3 \leq p \leq p_i} (p - 2) \prod_{p|N} \frac{p - 1}{p - 2} \neq 0.$$

Since $J_2(\omega) \neq 0$, every even number N greater than 4 is the sum of two odd primes.

Theorem 4. $p_1 = (p + 1)^2 + 1$.

We have the arithmetic function

$$J_2(\omega) = \prod_{3 \leq p \leq p_i} (p - 2 - (-1)^{\frac{p-1}{2}}) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many primes p such that p_1 is a prime.

Theorem 5. $p_1 = p^2 - 2$.

We have

$$J_2(\omega) = \prod_{3 \leq p \leq p_i} (p - 2 - (\frac{2}{p})) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many primes p such that p_1 is a prime.

Theorem 6. $p_1 = p + 4$ and $p_2 = 4p + 1$.

We have

$$J_2(\omega) = 3 \prod_{7 \leq p \leq p_i} (p - 3) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many primes p such that p_1 and p_2 are primes.

Theorem 7. $p_1 = (p + 1)^2 + 1$ and $p_2 = (p + 1)^2 + 3$.

We have

$$J_2(\omega) = \prod_{5 \leq p \leq p_i} (p - 3 - (-1)^{\frac{p-1}{2}} - (\frac{-3}{p})) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many primes p such that p_1 and p_2 are primes.

Theorem 8. The prime 13-tuples theorem: $p+b$: $b = 0, 4, 6, 10, 16, 18, 24, 28, 34, 40, 46, 48, 90$.

Since $J_2(13) = 0$, there are no prime 13-tuples if $p \neq 13$.

Theorem 9. The prime 14-tuples theorem: $p+b$: $b = 0, 2, 6, 8, 12, 18, 20, 26, 30, 32, 36, 42, 48, 50$.

We have

$$J_2(\omega) = 300 \prod_{29 \leq p \leq p_i} (p - 14) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many prime 14-tuples.

Theorem 10. $p_1 = 6m + 1, p_2 = 12m + 1, p_3 = 18m + 1, p_4 = 36m + 1, p_5 = 72m + 1$.

We have

$$J_2(\omega) = 12 \prod_{13 \leq p \leq p_i} (p - 6) \neq 0.$$

Since $J_2(\omega) \neq 0$, there are infinitely many integers m such that p_1, p_2, p_3, p_4 and p_5 are primes. $n = p_1 p_2 p_3 p_4 p_5$ is the Carmichael numbers.

Theorem 11. $p_3 = p_1 + p_2 + p_1 p_2$.

We have

$$J_3(\omega) = \prod_{3 \leq p \leq p_i} (p^2 - 3p + 3) \neq 0.$$

Since $J_3(\omega) \neq 0$, there are infinitely many primes p_1 and p_2 such that p_3 is a prime.

Theorem 12. $p_3 = (p_1 + 1)^5 + p_2$.

We have

$$J_3(\omega) = \prod_{3 \leq p \leq p_i} (p^2 - 3p + 3) \neq 0.$$

Since $J_3(\omega) \neq 0$, there are infinitely many primes p_1 and p_2 such that p_3 is a prime.

Theorem 13. $p_4 = p_1(p_2 + p_3) + p_2p_3$.

We have

$$J_4(\omega) = \prod_{3 \leq p \leq p_i} \left(\frac{(p-1)^4 - 1}{p} + 1 \right) \neq 0.$$

Since $J_4(\omega) \neq 0$, there are infinitely many primes p_1, p_2 and p_3 such that p_4 is a prime.

Theorem 14. Each of $n, n+1$ and $n+2$ is the product of k distinct primes.

Suppose that each of $m_1, m_2 = m_1 + 1$ and $m_3 = m_1 + 2$ is the product of $k-1$ distinct primes. We define

$$p_1 = 2m_2m_3x + 1, \quad p_2 = 2m_1m_3x + 1, \quad p_3 = 2m_1m_2x + 1. \quad (41)$$

We have the arithmetic function

$$J_2(\omega) = \prod_{3 \leq p \leq p_i} (p - 4 - \chi(p)) \neq 0, \quad (42)$$

where $\chi(p) = -2$ if $p \mid m_1m_2m_3$; $\chi(p) = 0$ otherwise.

Since $J_2(\omega) \neq 0$, there exist infinitely many integers x such that p_1, p_2 and p_3 are primes.

From (41) we have $n = m_1p_1 = 2m_1m_2m_3x + m_1$, $n+1 = m_1p_1 + 1 = 2m_1m_2m_3x + m_1 + 1 = m_2(2m_1m_3x + 1) = m_2p_2$, $n+2 = m_1p_1 + 2 = 2m_1m_2m_3x + m_1 + 2 = m_3(2m_1m_2x + 1) = m_3p_3$. If p_1, p_2 and p_3 are primes, then each of $n, n+1$ and $n+2$ is the product of k distinct primes. For example, $n = 1727913 = 3 \times 11 \times 52361$, $n+1 = 1727914 = 2 \times 17 \times 50821$, $n+2 = 1727915 = 5 \times 7 \times 49369$.

$J_n(\omega)$ is a generalization of Euler's proof for the existence of infinitely many primes. It has a wide application in various fields.

Acknowledgements

The Author would like to express his deepest appreciation to Professors R. M. Santilli, G. Weiss, D. Zuckerman, Ke-xi Liu, Mao-xian Zuo, Zhong-dian Wang, Chang-pei Wang, and Xin-ping Tong for their helps and supports.

References

- [1] B. Riemann, "Über die Anzahl der Primzahlen unter einer gegebenen Grösse," Monatsber. Akad. Berlin. 671-680 (1859).
- [2] H. Davenport, "Multiplicative Number Theory, " Springer Verlag (1980).
- [3] N. Katz and P. Sarnak, "Zeroes of zeta functions and symmetry," Bull. AMS, 36, 1-26 (1999).
- [4] A. Connes, "Trace formula in noncommutative geometry and the zeros of the Riemann zeta function," Sel. Math., New Ser. 5, 29-106(1999).
- [5] C. B. Haslgrove, "Tables of the Riemann zeta function," Roy. Soc. Math. Tables, Vol.6, Cambridge Univ. Press, London and New York (1960).
- [6] Chun-xuan, Jiang, "The study of the Riemann Zeta function," Unpublished Oct. (1997).
- [7] Chun-xuan, Jiang, "Foundations of Santilli's isonumber theory II," Algebras Groups and Geometries, 15, 509-544 (1998).
- [8] Chun-xuan, Jiang, "Foundations of Santilli's isonumber theory." In: Fundamental open problems in sciences at the end of the millennium, T. Gill, K. Liu and E. Trel (Eds) Hadronic Press, USA, 105-139 (1999).
- [9] Richard P. Brent, "On the zeros of the Riemann zeta function in the critical strip," Math. Comp., 33, 1361-1372(1979).
- [10] J. van de Lune, H. J. J. te Riele and D. T. Winter, "On the zeros of the Riemann zeta function in the critical strip," Math. Comp. 46, 667-681 (1986).
- [11] A. M. Odlyzko, "10²⁰-th zero of the Riemann zeta function and its neighbors," Preprint (1989).

- [12] Chun-xuan, Jiang, "On the Yu-Goldbach prime theorem," Guangxi Sciences (in Chinese) 3. 9-12 (1996).
- [13] Chun-xuan, Jiang, "Foundations of Santilli's isonumber theory I,"
- [14] C.X.Jiang. Foundation of Santilli's isonumber theory with applications to new cryptograms, Fermat's theorem and Goldbach's conjecture. International Academic Press, 2002 (also available in dpf format at <http://www.i-b-r.org/docs/magneh.pdf>)

More Articles

Millennium Relativity home page