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# Distributed Adaptive Droop Control for DC Distribution Systems

Vahidreza Nasirian, *Student Member, IEEE*, Ali Davoudi, *Member, IEEE*, Frank L. Lewis, *Fellow, IEEE*, and Josep M. Guerrero, *Senior Member, IEEE*

**Abstract**— A distributed-adaptive droop mechanism is proposed for secondary/primary control of dc Microgrids. The conventional secondary control, that adjusts the voltage set point for the local droop mechanism, is replaced by a voltage regulator. A current regulator is also added to fine-tune the droop coefficient for different loading conditions. The voltage regulator uses an observer that processes neighbors' data to estimate the average voltage across the Microgrid. This estimation is further used to generate a voltage correction term to adjust the local voltage set point. The current regulator compares the local per-unit current of each converter with the neighbors' on a communication graph and, accordingly, provides an impedance correction term. This term is then used to update the droop coefficient and synchronize per-unit currents or, equivalently, provide proportional load sharing. The proposed controller precisely accounts for the transmission/distribution line impedances. The controller on each converter exchanges data with only its neighbor converters on a sparse communication graph spanned across the Microgrid. Global dynamic model of the Microgrid is derived, with the proposed controller engaged. A low-voltage dc Microgrid prototype is used to verify the controller performance, link-failure resiliency, and the plug-and-play capability.

**Index Terms**— Cooperative control, dc-dc converter, dc Microgrid, distributed control, droop control.

## I. INTRODUCTION

Microgrids, as small-scale power systems, are becoming popular in distribution systems [1]–[3]. The dc nature of renewable energy sources, storage elements, or emerging electronics loads favor a dc Microgrid paradigm to avoid redundant dc-ac-dc conversions [4], [5]. Moreover, dc Microgrids can overcome some disadvantages of ac systems, e.g., transformer inrush current, frequency synchronization, reactive power flow, and power quality issues [6]. Resembling the control hierarchy of the legacy grid, a hierarchical control structure is conventionally adopted for Microgrid operation

[7]–[10]. The highest level in the hierarchy (tertiary) is in charge of economical dispatch and coordination with the distribution system operator. It assigns the Microgrid voltage to carry out a prescheduled power exchange between the Microgrid and the main grid [11]–[13]. To satisfy the voltage demand of the tertiary control, the secondary control measures voltages across the Microgrid and, accordingly, updates the voltage set points for the primary controllers. The primary control, typically implemented locally on individual converters with a droop mechanism, regulates the output voltage of individual converters and handles load sharing among sources.

The secondary and tertiary controls are typically implemented in a centralized fashion [14], where a central entity communicates with converters through a highly-connected communication network. Loss of any link in such topologies can lead to the failure of the corresponding unit, overstressing other units, and potentially leading to system-level instability and cascaded failures [15]. Since future extensions add to the controller complexity, scalability is not straightforward. Distributed control has emerged as an attractive alternative as it offers improved reliability, simpler communication network, and easier scalability [16]. For example, distributed tertiary control via dc bus signaling is studied in [17], [18]. Structurally, it is desirable to extend the distributed control paradigm to the secondary/primary levels. Categorically, such a controller shall satisfy two main control objectives of dc Microgrids, namely voltage regulation [19] and proportional load sharing [20].

Proper load sharing assigns the load among participating converters in proportion to their rated powers (or, equivalently, rated currents). This approach equalizes the per-unit currents of all sources, and prevents circulating currents [20] and overstressing of any source [21]. The droop control is widely adopted for load sharing by imposing virtual output impedance on each converter [22], [23]. Static/dynamic performance and stability assessment of droop controllers are investigated in [1], [24], and [25]. Constant droop is commonly used for power reference tracking and load sharing in grid-connected and islanded modes, respectively [26], [27]. However, its load sharing performance is susceptible to transmission line impedances [28]. Generally, higher droop coefficients result in improved load sharing, however, at the cost of further degrading the voltage regulation. Thus, to achieve a desirable load sharing, the droop coefficients should vary to account for line impedances and load variations.

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Moreover, since some sources (e.g., PV-driven modules or storage devices) lack a constant rated power, dynamic adjustment of droop coefficients is required as their rated power changes [29].

A piece-wise linear droop mechanism in [28] and [30] uses two different droop gains for low and high powers. The idea is further developed in [31] and [32] where droop coefficients continuously vary in response to change in power. This approach improves voltage regulation; however, voltage drop across the Microgrid is still noticeable. This method is developed for two-agent systems and extension to a multi-converter system is not straightforward. Moreover, improved voltage regulation has compromised accurate proportional load sharing. Adaptive-droop control for power flow control in grid-connected mode is studied in [33], [34]. Droop gains are adjusted in reciprocal to power demand in [35] where communication of a synchronization signal is needed among all converters. This requirement, in turn, compromises the plug-and-play capability. Decentralized [21] and supervisory [36] adaptive-droop approaches formulate droop gains in terms of batteries' state of charges [37].

Existing droop mechanisms generally suffer from poor voltage regulation and load sharing, particularly when the distribution line impedances are not negligible [38]–[40]. Possible solutions to the aforementioned issues have been reviewed in [16]. These solutions are either structured centrally [7] or require development of a fully connected data exchange network across the Microgrid, where any two nodes are in direct contact [22], [41]–[43]. Assuming equal voltages for all converters across the Microgrid in [7] is not practical, particularly, in dc distribution systems. Point-to-point communication links are required for all sources in [44], where any link failure renders the whole Microgrid inoperable. The line impedance is taken into account in [45], where the data exchange requires a fully connected communication graph. Proper operation of the controller demands information of all nodes and, thus, any link failure impairs the whole control functionality. Scalability is another challenge; after any structural/electrical upgrade, some control settings, e.g., the number of sources, need to be updated and embedded in all converters.

The voltage regulation requirement is redefined in [46] to incorporate the line impedance effect. The average voltage across the Microgrid (and only not a specific bus voltage) should be regulated at the global voltage set point determined by the tertiary control. This is called the *global voltage regulation*, and is considered here. Tertiary control levels would involve distributed optimization techniques to implement economical dispatch and/or loss optimization, and is the subject of future work. This paper focuses on the secondary/primary control of the dc Microgrids and offers the following contributions:

- Each converter is augmented with a current regulator that compares the actual per-unit current of that converter with a weighted average of its neighbors' and, accordingly, generates an impedance correction term to adjust droop coefficient and, thus, provide proportional load sharing.

- A voltage regulator is also added. This regulator uses the estimation made by a voltage observer to adjust the local voltage set point and provide global voltage regulation.
- The voltage observer processes neighbors' data and local voltage measurement through a so-called *dynamic consensus* protocol to estimate the global average voltage.
- Cooperation of the voltage and current regulators is shown to effectively carry out both global voltage regulation and proportional load sharing, particularly, when the line impedances are not negligible.
- A sparse communication network is spanned across the Microgrid to enable limited message passing among converters; each converter only exchanges data with its neighbors. This is in direct contrast to the centralized control approaches that require communication networks with high-bandwidth communication links and a high level of connectivity.
- This adaptive droop approach expands the work of authors in [46] and achieves a faster load sharing dynamics.
- Compared to the existing techniques (e.g., [45]) the control scheme employs a truly distributed approach that does not require a priori knowledge of the global parameters such as the number of sources. Thus, it is scalable and suitable for the plug-and-play operation.
- Unlike existing methods that require fully connected graphs and may fail in case of any communication link failure, the proposed method is not susceptible to any single link failure, which leads to a more reliable control framework.

The rest of this paper is outlined as follows: Section II introduces the distributed control paradigm. The cooperative adaptive-droop control is discussed in Section III. Section IV, explains functionality of the voltage observer. Global dynamic and static models are studied in Section V. The controller performance is verified using a low-voltage dc Microgrid prototype in Section VI. Section VII concludes the paper.

## II. DISTRIBUTED COOPERATIVE CONTROL FRAMEWORK

Microgrid sources are mapped to a cyber network as shown in Fig. 1, where each node represents an active source (or, converter) and each edge represents a communication link for data exchange. The communication graph might have a different topology than the underlying physical Microgrid. This cyber connection sets the groundwork for the cooperative control paradigm, where neighbors' interactions can lead to a global consensus. Accordingly, not all agents (converters) in a large-scale dynamic system need to be in direct contact. Instead, each agent only communicates its control variables with its neighbors. Then, using the neighbors' data and its local measurements, the agent updates its control variables. The cooperative control offers global consensus of the desired variables, shall the communication graph be designed properly.

A directed graph (digraph), associated with the cyber layer in Microgrid, is highlighted in Fig. 1.

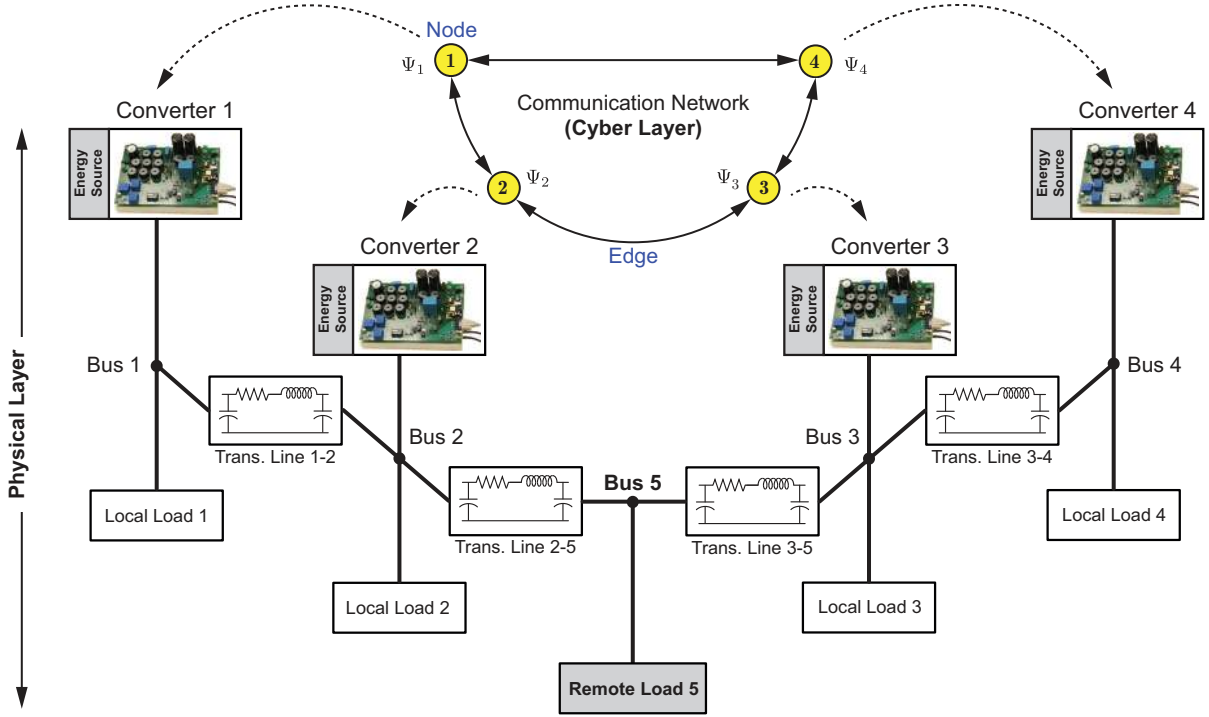


Fig. 1. General layout of a dc Microgrid including energy sources supplying the grid and the cyber network facilitating data exchange among sources.

Such a graph is usually represented as a set of nodes  $\mathbf{V}_G = \{v_1^g, v_2^g, \dots, v_N^g\}$  connected via a set of edges  $\mathbf{E}_G \subset \mathbf{V}_G \times \mathbf{V}_G$ , and an associated adjacency matrix  $\mathbf{A}_G = [a_{ij}] \in \mathbb{R}^{N \times N}$ . The Adjacency matrix  $\mathbf{A}_G$  contains communication weights, where  $a_{ij} > 0$  if  $(v_j^g, v_i^g) \in \mathbf{E}_G$  and  $a_{ij} = 0$ , otherwise.  $a_{ij}$  is the communication weight for data transfer from node  $j$  to node  $i$ . Here, a time-invariant adjacency matrix is assumed.  $N_i = \{j \mid (v_j^g, v_i^g) \in \mathbf{E}_G\}$  denotes the set of all neighbors of node  $i$ , i.e., if  $j \in N_i$ , then  $v_i^g$  receives information from  $v_j^g$ . However, in a digraph, the link is not necessarily reciprocal, i.e.,  $v_j^g$  might not receive information from  $v_i^g$ . The in-degree matrix  $\mathbf{D}_G^{\text{in}} = \text{diag}\{d_i^{\text{in}}\}$  is a diagonal matrix with  $d_i^{\text{in}} = \sum_{j \in N_i} a_{ij}$ . Similarly, the out-degree matrix is  $\mathbf{D}_G^{\text{out}} = \text{diag}\{d_i^{\text{out}}\}$ , where  $d_i^{\text{out}} = \sum_{j \in N_i} a_{ji}$ . The Laplacian matrix is then defined as  $\mathbf{L} = \mathbf{D}_G^{\text{in}} - \mathbf{A}_G$ , whose eigenvalues determine the global dynamics [47]. The Laplacian matrix is balanced if the in-degree of each node matches its out-degree, i.e.,  $\mathbf{D}_G^{\text{in}} = \mathbf{D}_G^{\text{out}}$ . Particularly, if the graph is undirected, i.e., all links are bidirectional, then the Laplacian matrix is balanced. A direct path from  $v_i^g$  to  $v_k^g$  is a sequence of edges that connects the two nodes. A digraph is said to have a spanning tree if it contains a root node, from which there exists at least a direct path to every other node.

The physical layer of the Microgrid, shown in Fig. 1, includes dispatchable sources (including the power converters), transmission lines, and loads. The cyber layer, comprised of all communication links, is spanned among the sources to facilitate data exchange. This is a sparse communication network with at least one spanning tree. In addition, the graph is chosen such that in case of any link failure the remaining network still contains at least one spanning tree. This redundancy is required to ensure link-

failure resiliency. Each converter broadcasts a data set,  $\Psi_i$ , to its neighbors. The data package transmitted by node  $i$ ,  $\Psi_i = [\bar{v}_i, i_i^{\text{pu}}]$ , consists of two elements; its estimate of the average voltage across the Microgrid,  $\bar{v}_i$ , and the measured per-unit current,  $i_i^{\text{pu}}$ . The term per-unit here refers to the current provided by the converter divided by its rated current, i.e.,  $i_i^{\text{pu}} \triangleq i_i / I_i^{\text{rated}}$ , where  $i_i$  and  $I_i^{\text{rated}}$  are the supplied and rated currents of the  $i$ -th converter, respectively. This terminology of the per-unit is used here to represent loading percentage of each converter. At the receiving ends of the communication links, each converter  $k$  receives data from all its neighbors,  $\Psi_j$ ,  $j \in N_k$ , with associated communication weights,  $a_{kj}$ . These weights are design parameters and can be considered as data transfer gains.

### III. ADAPTIVE DROOP CONTROL

The global voltage regulation and proportional load sharing are the two objectives of the secondary control, which require proper voltage set point assignment for individual converters. The proposed secondary controller is elaborated in Fig. 2(a), where local and neighbors' information are processed to adjust the local voltage set point,  $v_i^*$ . Cooperation among converters, at the secondary control level, helps to fine-tune the voltage set points,  $v_i^*$ , and mitigate the current and voltage residues.

The voltage set point for each converter is augmented with two terms provided through cooperation among converters. They are resulted from voltage and current regulators. Based on Fig. 2(a), the local voltage set point for an individual converter can be expressed as

$$v_i^* = v_i^{\text{ref}} - v_i^{\text{d}} + \delta v_i = v_i^{\text{ref}} - r_i i_i + \delta v_i, \quad (1)$$

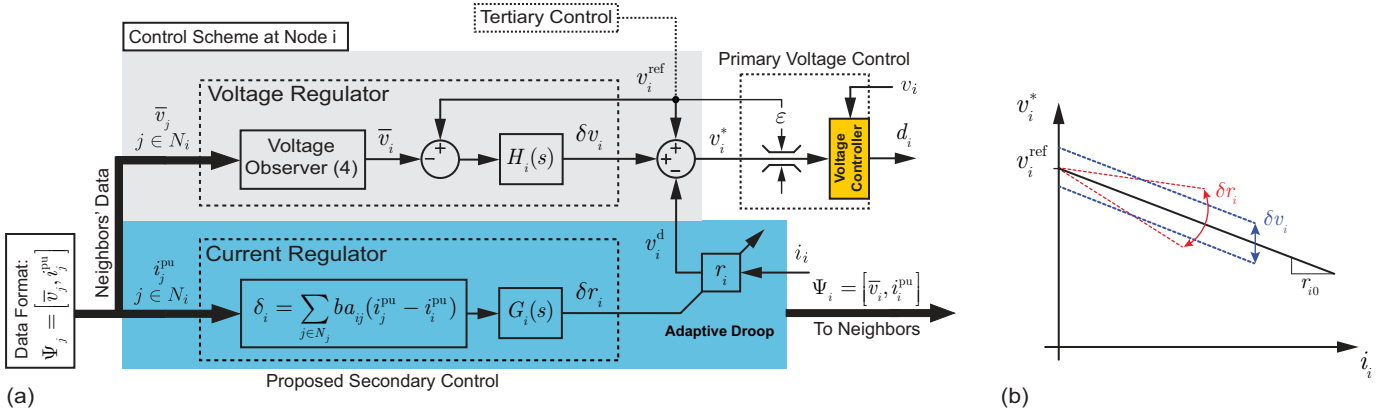


Fig. 2. Proposed distributed control policy: (a) cooperative adaptive droop control for a single agent (converter), (b) effect of adjustable voltage correction and virtual impedance on the droop characterization.

where  $v_i^{\text{ref}}$ ,  $v_i^{\text{d}}$ ,  $\delta v_i$ , and  $r_i$  are the global reference voltage, droop voltage, voltage correction term, and the virtual impedance of the  $i$ -th converter, respectively. This set point is further adjusted by a voltage limiter (see Fig. 2(a)) to maintain the bus voltages within an acceptable range. Figure 2(b) elaborates how adjustable voltage correction term,  $\delta v_i$ , and virtual impedance,  $r_i$ , can navigate operating point of the converter. The droop mechanism, which generates the term  $r_i i_i$  in (1), characterizes output impedance of the converters and helps to share load, which leads to the voltage drop across the Microgrid. The voltage correction terms,  $\delta v_i$ s, are augmented to the local reference voltages to boost the voltage across the Microgrid. Accordingly, the controller contains two modules; a voltage regulator and a current regulator.

The voltage regulator at node  $i$  consists of a voltage observer and a PI controller,  $H_i(s)$ . The voltage observer at each node estimates the averaged voltage across the Microgrid, where  $\bar{v}_i$  is the estimation at node  $i$ . This estimation is then compared with the global reference voltage,  $v_i^{\text{ref}}$ , to generate the voltage correction term,  $\delta v_i$ . In case of any mismatch between  $\bar{v}_i$  and  $v_i^{\text{ref}}$ , the controller adjusts  $\delta v_i$  to eliminate the discrepancy. In the islanded mode of operation, the global reference voltages,  $v_i^{\text{ref}}$ s, are typically identical and equal to the rated voltage of the Microgrid. However, in the grid-tied mode, the tertiary control sets a new voltage level for the Microgrid and relays the new reference values to individual converters. A cooperative observer will process the local voltage measurement and the neighbors' estimates to evaluate the average voltage across the Microgrid. Functionality of the observer is discussed in detail in Section IV.

The current regulator at node  $i$  provides the input to the droop mechanism. The droop mechanism characterizes the converter output impedance using the virtual impedance  $r_i$ . Virtual impedances are conventionally initialized in reciprocal to the converters' rated current, i.e.,  $r_{i0} = m/I_i^{\text{rated}}$ , where  $m$  is a design parameter and is identical for all converters. However, the distribution line impedances compromise performance of the droop controller. Thus, the droop gains are suggested to adapt according to the Microgrid loading

condition. To this end, a cooperative current regulator is included in the secondary control of any converter, e.g., converter  $i$ , which compares local per-unit current,  $i_i^{\text{pu}}$ , with the weighted average of the neighbors' per-unit currents and finds the current mismatch,  $\delta_i$ ,

$$\delta_i = \sum_{j \in N_i} b a_{ij} (i_j^{\text{pu}} - i_i^{\text{pu}}). \quad (2)$$

where  $b$  is the coupling gain between the voltage and current regulators. This mismatch is then fed to a PI controller,  $G_i(s)$ , to generate an impedance correction term,  $\delta r_i$ , which updates the virtual impedance,

$$r_i(t) = r_{i0} - \delta r_i(t). \quad (3)$$

If the per-unit currents of any two neighbors' differ, the current regulators of the corresponding converters respond and adjust their impedance correction terms to achieve balance.

#### IV. VOLTAGE OBSERVER

The observer is the primary stage of the voltage regulator module, as shown in Fig. 2. It uses a dynamic cooperative framework to process local and neighbors' information and estimate the average voltage across the Microgrid. Figure 3 explains the distributed cooperative policy for global averaging. The observer at node  $i$  receives its neighbors' estimates,  $\bar{v}_j$ s ( $j \in N_i$ ). Then, the observer updates its own estimate,  $\bar{v}_i$ , by processing the neighbors' estimates and the local voltage measurement,  $v_i$ ,

$$\bar{v}_i(t) = v_i(t) + \int_0^t \sum_{j \in N_i} a_{ij} (\bar{v}_j(\tau) - \bar{v}_i(\tau)) d\tau. \quad (4)$$

This updating protocol is referred to as *dynamic consensus* in the literature [48]. As seen in (4), the local measurement, i.e.,  $v_i$ , is directly fed into the estimating protocol. Thus, in case of any voltage variation at node  $i$ , the local estimate,  $\bar{v}_i$ , immediately responds. Then, the change in  $\bar{v}_i$  propagates through the communication network and affects all other estimations.

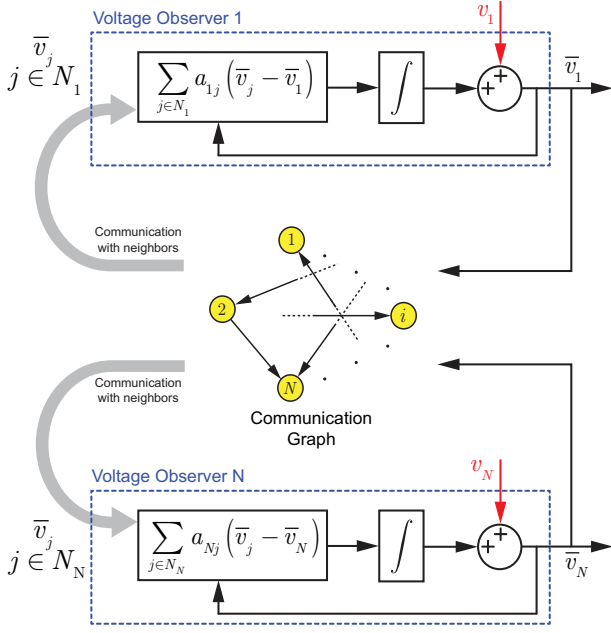


Fig. 3. Dynamic consensus protocol for averaging voltage across a Microgrid; estimating policy at each node.

By differentiating (4),

$$\dot{\bar{v}}_i = \dot{v}_i + \sum_{j \in N_i} a_{ij} (\bar{v}_j - \bar{v}_i) = \dot{v}_i + \sum_{j \in N_i} a_{ij} \bar{v}_j - d_i^{\text{in}} \bar{v}_i. \quad (5)$$

The global observer dynamic can be formulate accordingly,

$$\dot{\bar{\mathbf{v}}} = \dot{\mathbf{v}} - (\mathbf{D}_G^{\text{in}} - \mathbf{A}_G) \bar{\mathbf{v}} = \dot{\mathbf{v}} - \mathbf{L} \bar{\mathbf{v}}, \quad (6)$$

where the voltage measurement vector,  $\mathbf{v} = [v_1, v_2, \dots, v_N]^T$ , carries measured voltage of all nodes. Similarly, the voltage estimation vector,  $\bar{\mathbf{v}} = [\bar{v}_1, \bar{v}_2, \dots, \bar{v}_N]^T$ , contains the global average voltage estimated by all nodes. Equivalently, in the frequency domain,

$$s\bar{\mathbf{V}} - \bar{\mathbf{v}}(0) = s\mathbf{V} - \mathbf{v}(0) - \mathbf{L}\bar{\mathbf{V}}, \quad (7)$$

where  $\mathbf{V}$  and  $\bar{\mathbf{V}}$  are the Laplace transforms of  $\mathbf{v}$  and  $\bar{\mathbf{v}}$ , respectively. Equation (4) implies that  $\mathbf{v}(0) = \bar{\mathbf{v}}(0)$ . Therefore,

$$\bar{\mathbf{V}} = s(\mathbf{I}_N + \mathbf{L})^{-1} \mathbf{V} = \mathbf{H}_{\text{obs}} \mathbf{V}, \quad (8)$$

where  $\mathbf{I}_N \in \mathbb{R}^{N \times N}$  and  $\mathbf{H}_{\text{obs}}$  are the identity matrix and the observer transfer function, respectively. Equation (8) represents the global dynamics of the voltage observers. It is shown in [46] that if  $\mathbf{L}$  is balanced, then all entries of the voltage estimation vector,  $\bar{\mathbf{v}}$ , converge to a consensus value, which is the true average voltage, i.e., the average of all entries in  $\mathbf{v}$ . In other words,

$$\bar{\mathbf{v}}^{\text{ss}} = \mathbf{Q} \mathbf{v}^{\text{ss}} = \langle \mathbf{v}^{\text{ss}} \rangle \mathbf{1}, \quad (9)$$

where  $\mathbf{Q} \in \mathbb{R}^{N \times N}$  is the averaging matrix, whose elements are all equal to  $1/N$ .  $\mathbf{1} \in \mathbb{R}^{N \times 1}$  is a vector whose elements are all equal to one.  $\mathbf{x}^{\text{ss}}$  and  $\langle \mathbf{x} \rangle$  represent the steady-state value of the vector  $\mathbf{x} \in \mathbb{R}^{N \times 1}$  and the average of all vector elements, respectively.

## V. GLOBAL MODEL DEVELOPMENT

Global model development is essential to study how the proposed controller affects the transient response and steady-state operation of the Microgrid. This model can be used to tune the design parameters and achieve any desired dynamic.

### A. Global Dynamic Model

Switching nature of power electronic converters can potentially result in a nonlinear system. Accordingly, small-signal methods are commonplace for dynamic characterization purposes (e.g., via averaging) [49]. Such tools are suitable for relatively small disturbances, e.g., as shown in [50], [51]. Thus, small-signal modeling is considered here, where, each variable  $x$  is written as  $x = x^q + \hat{x}$ , where  $x^q$  and  $\hat{x}$  are the quiescent and small-signal perturbation parts, respectively. This representation helps to linearly express the droop voltage for the  $i$ -th converter,  $v_i^d$ , as

$$v_i^d = v_i^{\text{d},q} + \hat{v}_i^d = (r_i^q + \hat{r}_i) (i_i^q + \hat{i}_i). \quad (10)$$

By neglecting the second-order term, i.e.,  $\hat{r}_i \hat{i}_i \approx 0$ , (10) can be reduced to

$$\hat{v}_i^d = r_i^q \hat{i}_i + i_i^q \hat{r}_i. \quad (11)$$

Let  $\hat{\mathbf{v}}_{\text{ref}} = [\hat{v}_1^{\text{ref}}, \hat{v}_2^{\text{ref}}, \dots, \hat{v}_N^{\text{ref}}]^T$  and  $\hat{\mathbf{i}} = [\hat{i}_1, \hat{i}_2, \dots, \hat{i}_N]^T$  be the small-signal vectors of the rated voltages and actual supplied currents, respectively. Similarly,  $\hat{\mathbf{v}}$ ,  $\hat{\mathbf{v}}^d$ ,  $\Delta \hat{\mathbf{v}}$ ,  $\hat{\mathbf{r}}$ , and  $\hat{\mathbf{v}}^*$  are column vectors containing small-signal portions of the output voltages, droop voltages, voltage correction terms, virtual impedances, and local voltage set points, respectively.  $\mathbf{r}^q$  and  $\mathbf{i}^q$  are vectors of quiescent virtual impedances and currents, respectively.  $\mathbf{I}_{\text{rated}} = \text{diag}\{I_i^{\text{rated}}\}$  is a diagonal matrix containing rated currents of individual sources.  $\hat{\mathbf{V}}_{\text{ref}}$ ,  $\hat{\mathbf{I}}$ ,  $\hat{\mathbf{V}}$ ,  $\hat{\mathbf{V}}^d$ ,  $\Delta \hat{\mathbf{V}}$ ,  $\hat{\mathbf{R}}$ , and  $\hat{\mathbf{V}}^*$  are the Laplace transforms of  $\hat{\mathbf{v}}_{\text{ref}}$ ,  $\hat{\mathbf{i}}$ ,  $\hat{\mathbf{v}}$ ,  $\hat{\mathbf{v}}^d$ ,  $\Delta \hat{\mathbf{v}}$ ,  $\hat{\mathbf{r}}$ , and  $\hat{\mathbf{v}}^*$ , respectively. Based on Fig. 2,

$$\mathbf{H} (\hat{\mathbf{V}}_{\text{ref}} - \hat{\mathbf{V}}) = \Delta \hat{\mathbf{V}}, \quad (12)$$

where  $\mathbf{H} = \text{diag}\{H_i(s)\}$  is the voltage controller matrix. By using (3),  $\hat{r}_i = -\delta \hat{r}_i$ , thus,

$$-b\mathbf{G}\mathbf{L}\mathbf{I}_{\text{rated}}^{-1} \hat{\mathbf{I}} = -\hat{\mathbf{R}}, \quad (13)$$

where  $\mathbf{G} = \text{diag}\{G_i(s)\}$  is the current controller matrix. Substituting the observer transfer function,  $\mathbf{H}_{\text{obs}}$ , from (8) in (12) yields,

$$\Delta \hat{\mathbf{V}} = \mathbf{H} (\hat{\mathbf{V}}_{\text{ref}} - \mathbf{H}_{\text{obs}} \hat{\mathbf{V}}). \quad (14)$$

In addition, (11) can be written in the global form,

$$\hat{\mathbf{V}}^d = \mathbf{T}(\mathbf{r}^q) \hat{\mathbf{I}} + \mathbf{T}(\mathbf{i}^q) \hat{\mathbf{R}}, \quad (15)$$

where  $\mathbf{T}(\cdot): \mathbb{R}^{N \times 1} \rightarrow \mathbb{R}^{N \times N}$  is a transformation that maps a vector to a diagonal matrix,

$$\mathbf{T}([x_1, x_2, \dots, x_N]^T) \triangleq \text{diag}\{x_1, x_2, \dots, x_N\}. \quad (16)$$

The small-signal reference voltage vector,  $\hat{\mathbf{V}}^*$ , can be derived using (1) and (13)-(15),

$$\begin{aligned}
\hat{\mathbf{V}}^* &= \hat{\mathbf{V}}_{\text{ref}} - \hat{\mathbf{V}}^{\text{d}} + \Delta \hat{\mathbf{V}} \\
&= \hat{\mathbf{V}}_{\text{ref}} - \mathbf{T}(\mathbf{r}^{\text{q}}) \hat{\mathbf{I}} - \mathbf{T}(\mathbf{i}^{\text{q}}) \hat{\mathbf{R}} + \mathbf{H}(\hat{\mathbf{V}}_{\text{ref}} - \mathbf{H}_{\text{obs}} \hat{\mathbf{V}}) \\
&= (\mathbf{I}_N + \mathbf{H}) \hat{\mathbf{V}}_{\text{ref}} - (\mathbf{T}(\mathbf{r}^{\text{q}}) + b\mathbf{T}(\mathbf{i}^{\text{q}}) \mathbf{GLI}_{\text{rated}}^{-1}) \hat{\mathbf{I}} \\
&\quad - \mathbf{H}\mathbf{H}_{\text{obs}} \hat{\mathbf{V}}.
\end{aligned} \tag{17}$$

On the other hand, dynamic behavior of any converter with closed-loop voltage regulator can be expressed as

$$\hat{V}_i = G_i^c(s) \hat{V}_i^*, \tag{18}$$

where  $\hat{V}_i$  and  $\hat{V}_i^*$  are the Laplace transforms of  $\hat{v}_i$  and  $\hat{v}_i^*$ , respectively.  $G_i^c$  is the closed-loop transfer function of the  $i$ -th converter. The closed-loop transfer functions are derived in [49] for a wide variety of converters. Global small-signal dynamic of the converters can be found according to (18),

$$\hat{\mathbf{V}} = \mathbf{G}_c \hat{\mathbf{V}}^*, \tag{19}$$

where  $\mathbf{G}_c = \text{diag}\{G_i^c\}$  is the converters' transfer function matrix. By substituting (19) in (17),

$$\begin{aligned}
(\mathbf{G}_c^{-1} + \mathbf{H}\mathbf{H}_{\text{obs}}) \hat{\mathbf{V}} &= \\
(\mathbf{I}_N + \mathbf{H}) \hat{\mathbf{V}}_{\text{ref}} - (\mathbf{T}(\mathbf{r}^{\text{q}}) + b\mathbf{T}(\mathbf{i}^{\text{q}}) \mathbf{GLI}_{\text{rated}}^{-1}) \hat{\mathbf{I}}
\end{aligned} \tag{20}$$

For a dc Microgrid, it is a common practice to assume that the transmission/distribution line and load impedances are predominantly resistive [52]. Accordingly, one can use the Microgrid conductance matrix,  $\mathbf{g}_{\text{bus}}$ , to relate supplied currents to the bus voltages,

$$\mathbf{i} = \mathbf{g}_{\text{bus}} \mathbf{v}. \tag{21}$$

Small-signal perturbation expands (21),

$$(\hat{\mathbf{i}}^{\text{q}} + \hat{\mathbf{i}}) = (\mathbf{g}_{\text{bus}}^{\text{q}} + \hat{\mathbf{g}}_{\text{bus}}) (\mathbf{v}^{\text{q}} + \hat{\mathbf{v}}). \tag{22}$$

The small-signal portion of the conductance matrix,  $\hat{\mathbf{g}}_{\text{bus}}$ , models any small-signal changes in the conductance matrix,  $\mathbf{g}_{\text{bus}}$ , caused by load change or transmission network reconfiguration. Neglecting the second-order term, i.e.,  $\hat{\mathbf{g}}_{\text{bus}} \hat{\mathbf{v}} \approx \mathbf{0}$ , simplifies (22),

$$\hat{\mathbf{i}} = \mathbf{g}_{\text{bus}}^{\text{q}} \hat{\mathbf{v}} + \hat{\mathbf{g}}_{\text{bus}} \mathbf{v}^{\text{q}}. \tag{23}$$

Or, equivalently, in the frequency domain,

$$\hat{\mathbf{I}} = \mathbf{g}_{\text{bus}}^{\text{q}} \hat{\mathbf{V}} + \hat{\mathbf{G}}_{\text{bus}} \mathbf{v}^{\text{q}}. \tag{24}$$

where  $\hat{\mathbf{G}}_{\text{bus}}$  is the Laplace transform of  $\hat{\mathbf{g}}_{\text{bus}}$ . Substituting (24) in (20) provides the global dynamic model of the Microgrid with the proposed controller in effect,

$$\begin{aligned}
(\mathbf{G}_c^{-1} + \mathbf{H}\mathbf{H}_{\text{obs}} + (\mathbf{T}(\mathbf{r}^{\text{q}}) + b\mathbf{T}(\mathbf{i}^{\text{q}}) \mathbf{GLI}_{\text{rated}}^{-1}) \mathbf{g}_{\text{bus}}^{\text{q}}) \hat{\mathbf{V}} &= \\
(\mathbf{I}_N + \mathbf{H}) \hat{\mathbf{V}}_{\text{ref}} - (\mathbf{T}(\mathbf{r}^{\text{q}}) + b\mathbf{T}(\mathbf{i}^{\text{q}}) \mathbf{GLI}_{\text{rated}}^{-1}) \hat{\mathbf{G}}_{\text{bus}} \mathbf{v}^{\text{q}}.
\end{aligned} \tag{25}$$

Equation (25) implies that the Microgrid is systematically a multi-input-multi-output plant where  $\hat{\mathbf{V}}_{\text{ref}}$  and  $\hat{\mathbf{G}}_{\text{bus}}$  are the inputs and  $\hat{\mathbf{V}}$  and  $\hat{\mathbf{I}}$  are the outputs. The global dynamic model in (25) formulates the transfer functions from each input to the primary output,  $\hat{\mathbf{V}}$ .

## B. Design Approach

For a given Microgrid, the matrix of converters' closed-loop transfer functions,  $\mathbf{G}_c$ , and the current rating matrix,  $\mathbf{I}_{\text{rated}}$  are known. The communication graph needs to be a connected graph with the minimal redundancy defined in Section III, where no single link failure can compromise communication connectivity. Weights of the communication links,  $a_{ij}$ , and, thus, the Laplacian matrix,  $\mathbf{L}$ , may, then, be chosen to provide any desired dynamic response for the voltage observers by evaluating (8). It should be noted that the selection of the communication weights must satisfy a balanced Laplacian matrix.

For the given Microgrid with known transmission/distribution network, one can evaluate  $\mathbf{g}_{\text{bus}}^{\text{q}}$  assuming base loads at all consumption terminals. Accordingly, quiescent voltage and current vectors ( $\mathbf{v}^{\text{q}}$  and  $\mathbf{i}^{\text{q}}$ , respectively) can be found by iteratively solving (26)-(27),

$$\mathbf{i}^{\text{q}} = \mathbf{g}_{\text{bus}}^{\text{q}} \mathbf{v}^{\text{q}}, \tag{26}$$

$$\mathbf{i}^{\text{pu}^{\text{q}}} = \mathbf{I}_{\text{rated}}^{-1} \mathbf{i}^{\text{q}} = n \mathbf{1}, \tag{27}$$

where  $n$  is a positive real number. The designer may initialize the virtual impedances as

$$\mathbf{r}_0 = m \left[ 1/I_1^{\text{rated}}, 1/I_2^{\text{rated}}, \dots, 1/I_N^{\text{rated}} \right]^T, \tag{28}$$

where  $m$  is a positive scalar design parameter [7]. The adaptive-droop mechanism adjusts the virtual impedances to provide proportional load sharing. Due to the line impedances, this adjustment results in different values than the initial values, i.e.,  $\mathbf{r}^{\text{q}} \neq \mathbf{r}_0$ . However, empirical studies in Section VI will show that the quiescent virtual impedance vector remains almost intact for various operating conditions. Thus, one can run a steady-state numerical analysis to find  $\mathbf{r}^{\text{q}}$  for the base load condition and further use it in the design procedure.

Given the Laplacian matrix,  $\mathbf{L}$ , the observer transfer function,  $\mathbf{H}_{\text{obs}}$ , the converters' transfer function matrix,  $\mathbf{G}_c$ , and all other constant vectors in (25), one can use this equation to design the voltage and current controller matrices ( $\mathbf{H}$  and  $\mathbf{G}$ , respectively) and the coupling gain,  $b$ , to provide any desired asymptotically stable dynamic response for the entire Microgrid, where all poles of the transfer functions extracted from (25) lie on the Open Left Hand Plane (OLHP).

## C. Steady-State Analysis

Steady-state analysis of the Microgrid operation is essential to ensure that the cooperative controllers satisfy both operational requirements; the global voltage regulation and the proportional load sharing. Since the converters' rated voltages match the Microgrid rated voltage, with no loss of generality, one can assume

$$\mathbf{v}_{\text{ref}} = v_{\text{rated}} \mathbf{1}, \tag{29}$$

where  $v_{\text{rated}}$  is the Microgrid rated voltage. It is also assumed that the control parameters are properly tuned, based on the design approach in Section V-B, to stabilize voltage and current throughout the Microgrid.

Let's assume that the Microgrid voltages and currents are in the steady state for  $t \geq t_0$ . The voltage and current controller of the  $i$ -th converter can be expressed as  $H_i = H_i^P + H_i^I/s$  and  $G_i = G_i^P + G_i^I/s$ , respectively, where  $H_i^P$  and  $G_i^P$  are the proportional and  $H_i^I$  and  $G_i^I$  are the integral gains. One can show that, with stable voltages, all voltage observers converge to the true average voltage, i.e.,

$$\bar{\mathbf{v}}^{\text{ss}} = \left( \frac{1}{N} \sum_{i=1}^N v_i^{\text{ss}} \right) \mathbf{1} = \bar{v}^{\text{ss}} \mathbf{1}, \quad (30)$$

where  $x^{\text{ss}}$  represents the steady-state value of the variable  $x$ . According to Fig. 2, for  $t \geq t_0$  one can write,

$$\Delta \mathbf{v}^{\text{ss}} = \mathbf{W}_v(t_0) + \mathbf{H}_P(\mathbf{v}_{\text{ref}} - \bar{\mathbf{v}}^{\text{ss}}) + \mathbf{H}_I(\mathbf{v}_{\text{ref}} - \bar{\mathbf{v}}^{\text{ss}})(t - t_0), \quad (31)$$

where  $\mathbf{W}_v(t_0)$  is a vector that carries integrator outputs of the voltage regulators at  $t = t_0$ . Similarly,

$$\Delta \mathbf{r}^{\text{ss}} = \mathbf{W}_r(t_0) + \mathbf{G}_P(-b\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}}) + \mathbf{G}_I(-b\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}})(t - t_0), \quad (32)$$

where  $\mathbf{W}_r(t_0)$  is a vector that carries integrator outputs of the current regulators at  $t = t_0$ . In the steady state,  $\mathbf{v}^{\text{ss}} = \mathbf{v}^{\text{ss}}$ , thus, according to (1),

$$\mathbf{v}^{\text{ss}} = \mathbf{v}_{\text{ref}} - \mathbf{T}(\mathbf{r}^{\text{ss}})\mathbf{i}^{\text{ss}} + \Delta \mathbf{v}^{\text{ss}} = v_{\text{rated}} \mathbf{1} - \mathbf{T}(\mathbf{r}_0 - \Delta \mathbf{r}^{\text{ss}})\mathbf{i}^{\text{ss}} + \Delta \mathbf{v}^{\text{ss}}. \quad (33)$$

By substituting (31)-(32) in (33),

$$\mathbf{v}^{\text{ss}} = v_{\text{rated}} \mathbf{1} - \mathbf{T}(\mathbf{r}_0 + b(\mathbf{G}_P + \mathbf{G}_I(t - t_0))\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}} - \mathbf{W}_r(t_0))\mathbf{i}^{\text{ss}} + (v_{\text{rated}} - \bar{v}^{\text{ss}})(\mathbf{H}_P + \mathbf{H}_I(t - t_0))\mathbf{1} + \mathbf{W}_v(t_0). \quad (34)$$

Equation (34) holds for all  $t \geq t_0$ . Thus, the time varying term in (34) is zero. Accordingly,

$$(v_{\text{rated}} - \bar{v}^{\text{ss}})\mathbf{H}_I \mathbf{1} = \mathbf{T}(b\mathbf{G}_I\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}})\mathbf{i}^{\text{ss}}. \quad (35)$$

One can see that if  $\mathbf{G}$  is a diagonal matrix and  $b$  a real number then, for any vector  $\mathbf{x}$ ,

$$\mathbf{T}(b\mathbf{G}\mathbf{x}) = b\mathbf{G}\mathbf{T}(\mathbf{x}). \quad (36)$$

The transformation property in (36) helps to rewrite (35),

$$\mathbf{T}(\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}})\mathbf{I}_{\text{rated}}\mathbf{i}^{\text{pu}^{\text{ss}}} = (v_{\text{rated}} - \bar{v}^{\text{ss}})b^{-1}\mathbf{G}_I^{-1}\mathbf{H}_I \mathbf{1}. \quad (37)$$

Both  $\mathbf{T}(\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}})$  and  $\mathbf{I}_{\text{rated}}$  are diagonal matrices and, thus,

$$\mathbf{T}(\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}})\mathbf{I}_{\text{rated}} = \mathbf{I}_{\text{rated}}\mathbf{T}(\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}}). \quad (38)$$

Accordingly,

$$\mathbf{T}(\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}})\mathbf{i}^{\text{pu}^{\text{ss}}} = (v_{\text{rated}} - \bar{v}^{\text{ss}})b^{-1}\mathbf{I}_{\text{rated}}^{-1}\mathbf{G}_I^{-1}\mathbf{H}_I \mathbf{1} = (v_{\text{rated}} - \bar{v}^{\text{ss}})[u_1, u_2, \dots, u_N]^T. \quad (39)$$

where  $u_i = H_i^I / (bG_i^I I_i^{\text{rated}}) > 0$ . If any of the currents is zero, e.g.,  $i_j^{\text{pu}} = 0$ , then, (39) implies  $v_{\text{rated}} = \bar{v}^{\text{ss}}$ .

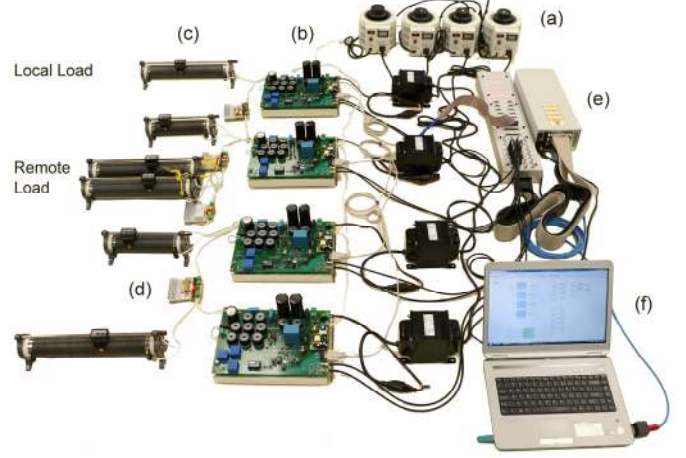


Fig. 4. DC Microgrid prototype: (a) Input ac sources, (b) Buck converters driving each source, (c) Local and remote loads, (d) distribution line, (e) dSAPCE control board (DS1103), (f) Programming/monitoring PC.

Otherwise, one can safely assume that all currents are positive (i.e.,  $i_i > 0$ ); sources only deliver power. Using (39),

$$\mathbf{L}\mathbf{i}^{\text{pu}^{\text{ss}}} = (v_{\text{rated}} - \bar{v}^{\text{ss}}) \left[ \frac{u_1}{i_1^{\text{pu}}}, \frac{u_2}{i_2^{\text{pu}}}, \dots, \frac{u_N}{i_N^{\text{pu}}} \right]^T. \quad (40)$$

with the balanced Laplacian matrix,  $\mathbf{L}$ ,

$$\underbrace{\mathbf{1}^T \mathbf{L}}_{=0} \mathbf{i}^{\text{pu}^{\text{ss}}} = (v_{\text{rated}} - \bar{v}^{\text{ss}}) \sum_{\substack{j=1 \\ >0}}^N \frac{u_j}{i_j^{\text{pu}}}. \quad (41)$$

Accordingly,

$$v_{\text{rated}} = \bar{v}^{\text{ss}}, \quad (42)$$

which, equivalently, satisfies the global voltage regulation, i.e., the controller successfully regulates the average voltage of the Microgrid,  $\bar{v}^{\text{ss}}$ , at the rated value,  $v_{\text{rated}}$ .

For any vector  $\mathbf{x}$  one can investigate that

$$\mathbf{1}^T \mathbf{T}(\mathbf{x}) = \mathbf{x}^T. \quad (43)$$

Multiplying both sides of (39) from left by  $\mathbf{1}^T$ , one can write

$$(\mathbf{i}^{\text{pu}^{\text{ss}}})^T \mathbf{L}^T \mathbf{i}^{\text{pu}^{\text{ss}}} = (v_{\text{rated}} - \bar{v}^{\text{ss}}) \sum_{j=1}^N u_j = 0, \quad (44)$$

which is a quadratic equation. It is shown in Appendix I that

$$\mathbf{i}^{\text{pu}^{\text{ss}}} = k\mathbf{1}, \quad (45)$$

is the only solution to the quadratic equation in (44), where  $k$  is a positive real number. Equation (45) ensures consensus of the per-unit currents or, equivalently, achievement of proportional load sharing.

## VI. EXPERIMENTAL VERIFICATION

A low-voltage dc Microgrid, with the structure shown in Fig. 1, is prototyped. Figure 4 shows the test bench where four adjustable isolated ac sources are used as energy sources. Each source is driven by a buck converter with an input rectifier.



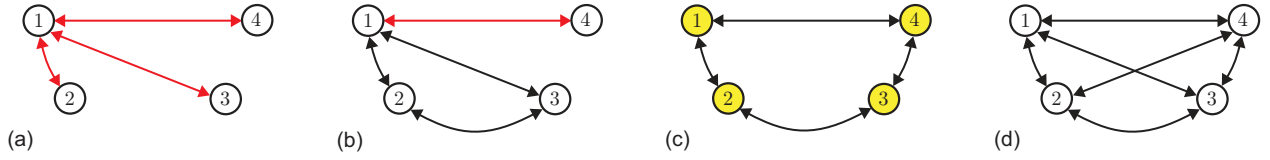


Fig. 5. Alternative communication topologies forming a connected graph with: (a) No redundant link, (b) Suboptimal link redundancy, (c) Optimal link redundancy, and (d) full connection.

The converters have similar topologies but different ratings, i.e., the rated currents of the first and the fourth converters are twice those for the other two converters. Each distribution line is built using a  $\pi$ -circuit model. The Microgrid has five consumption terminals; four to supply local loads and one to supply a remote load, as seen in Fig. 1. Although different voltage levels are possible [53], [54], a 48 V system is considered here. The typical acceptable voltage deviation is about 5% of the rated voltage [22] and, thus, the voltage limiters are set with  $\varepsilon = 2.5$  V. Electrical and control parameters of the Microgrid are provided in Appendix II.

Alternative communication topologies for a group of four agents are represented in Fig. 5, where all links are assumed bidirectional to feature a balanced Laplacian matrix. Despite carrying spanning tree, not all alternatives satisfy the communication redundancy required for the safe operation (link failure resiliency) of the proposed method. In other words, some topologies are susceptible to lose connectivity in the case of a single link failure. For example, if any of the links highlighted in red in Figs. 5(a) or 5(b) is lost, the corresponding graph loses its connectivity, which renders the whole control mechanism inoperable. However, the circular communication structure in Fig. 5(c) is the sparsest network where no single link failure can compromise the graphical connectivity. Figure 5(d) shows a fully connected graph, which provides a similar redundancy feature yet lacks sparsity. Therefore, the communication structure in Fig. 5(c) is considered for this study.

The communication channels are assumed ideal and are modeled in the dSAPCE. Wireless or fiber optic networks may be used for physical implementation of the data network. The effect of non-idealities such as noise, limited bandwidth, channel delay, packet drop, etc. is studied in [45]. Moreover, consensus protocols are tailored for non-ideal data networks in [55]–[57], whose application in the power distribution systems will be the subject of future studies.

The control approach is built in Simulink on a programming/monitoring PC which is linked to a dSPACE control board (DS1103). The PC compiles the Simulink model and, accordingly, programs the DS1103. It also generates a variable description file further used by the dSPACE monitoring software, ControlDesk 5.0, to provide a live view of any variable. When the proposed control methodology is in effect, the ControlDesk enables the designer to tune any control parameter online and monitor the system performance.

#### A. Constant Droop versus Adaptive Droop

Figure 6 comparatively studies the performance of the proposed methodology. The Microgrid is initially controlled

using the conventional droop controller, where a fixed droop impedance is used, i.e.,  $r(t) = r_0$ . As seen in Fig. 6(a), it leads to voltages less than the desired value, i.e.,  $v_{\text{rated}} = 48$  V. In addition, although the initial values of the droop gains are designed reciprocal to the converters' rated currents, the transmission line effect has clearly incapacitated the droop mechanism, resulting in a poor load sharing where converters with identical ratings supply different currents (see Fig. 6(b)). The proposed controller is engaged at  $t = 10.1$  s. Consequently, the voltages are boosted across the Microgrid and the average voltage is finely regulated at the set point, i.e.,  $v_{\text{rated}} = 48$  V. Figure 6(b) shows that the proportional load sharing is also carried out, where the first and the fourth converters carry twice the current as the other two converters. Dynamic performance of the controller can be tuned by adjusting the communication weights (or, equivalently, entries of the Adjacency matrix). In comparison with alternative solution in [46], it can be seen that the distributed adaptive droop has provided a faster load sharing; almost twice as fast as the method in [46].

The voltage observers is studied in Fig. 6(c), where a good agreement is reported between the true average voltage,  $\bar{v}$ , and the individual estimated values,  $\bar{v}_i$  s. Figure 6(d) expresses how the proposed controller sets voltage correction terms,  $\delta v_i$  s, to boost the voltage across the Microgrid and overcome the natural voltage drop caused by the droop mechanisms. Figure 6(e) shows how the current controller adjusts the virtual impedances,  $r_i$  s, to provide proportional load sharing.

#### B. Load Variation

The controller performance in case of load change is studied in Fig. 7, where the remote load at bus five,  $R_5$ , is changed in step between  $10\Omega$  and  $20\Omega$ . Tight voltage regulation and load sharing can be observed in Figs. 7(a) and 7(b). Excellent transient load sharing is also noticeable in Fig. 7(b). Estimations of the average voltage across the Microgrid are plotted in Fig 7(c) where a good agreement between the true and estimated values ( $\bar{v}$  and  $\bar{v}_i$  s, respectively) can be seen. Comparing Figs. 7(d) and 7(e), one can observe that load change mostly affects voltage correction terms,  $\delta v_i$  s, and has a negligible impact on the virtual impedances.

#### C. Plug-and-Play Capability

Figure 8 studies plug-and-play capability of the proposed method and its performance in the case of a converter failure. As seen, when the second converter fails at  $t = 7.3$  s, the controller adjusts the voltages to regain the global voltage regulation. When the Converter 2 fails, the voltage at the second bus,  $v_2$ , is no longer available.

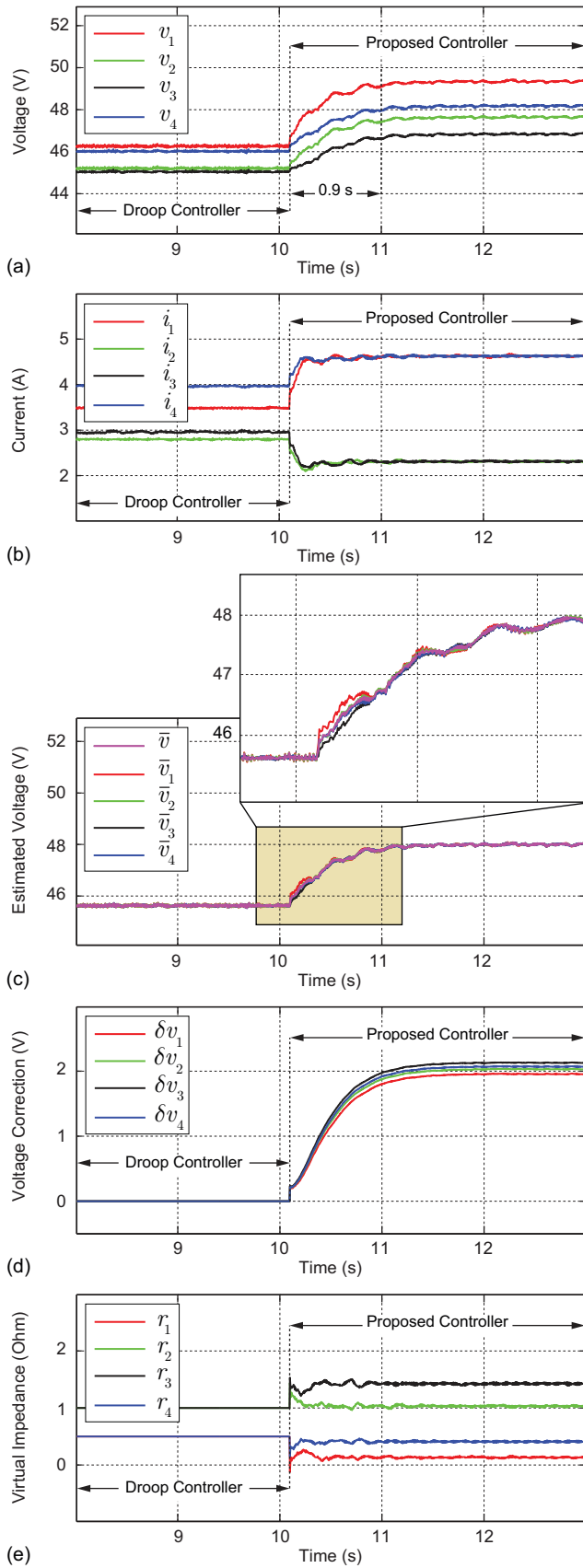


Fig. 6. Comparative studies of the conventional droop control and the distributed adaptive-droop control: (a) Terminal voltages, (b) Supplied currents, (c) Estimations of the average voltage, (d) Voltage correction terms, (e) Virtual impedances.

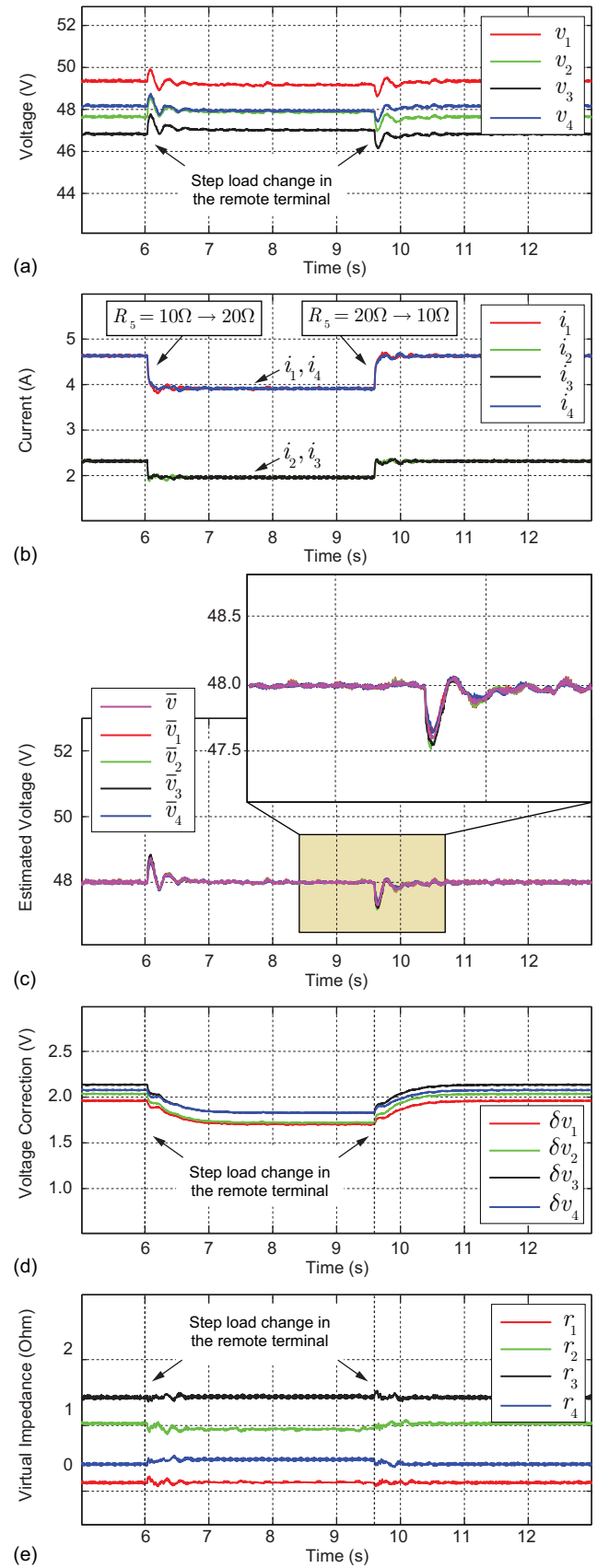


Fig. 7. Performance of the distributed adaptive-droop controller in a case of load change: (a) Terminal voltages, (b) Supplied currents, (c) Estimations of the average voltage, (d) Voltage correction terms, (e) Virtual impedances.

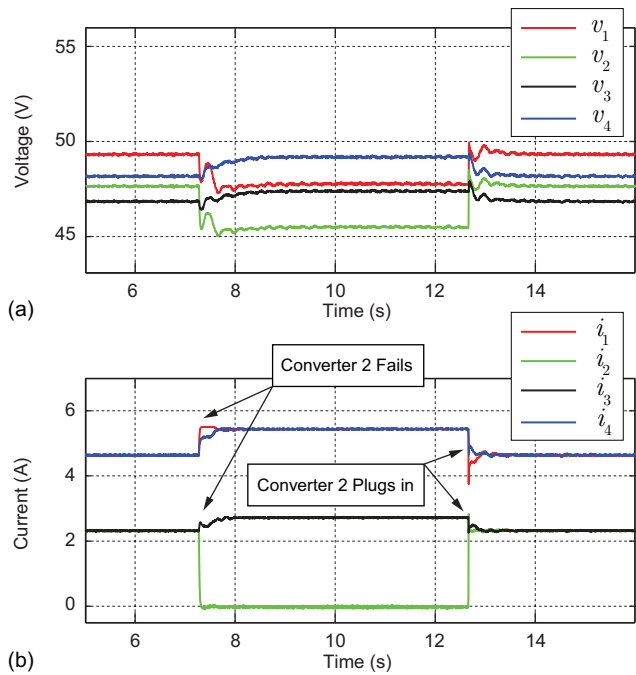


Fig. 8. Converter failure and plug-and-play studies: (a) Terminal voltages, (b) Supplied currents.

Thus, the controller averages the three remaining measurements, i.e.,  $v_1$ ,  $v_3$ , and  $v_4$ , and regulates this new average at the reference value. The controller also readjusts the load sharing among the remaining converters. It should be noted that a converter failure also implies loss of all communication links attached to that particular converter. Accordingly, failure of the second converter automatically renders the link 1-2 (between nodes 1 and 2) and link 2-3 inoperable. However, the remaining links still form a connected graph with balanced Laplacian matrix (see Fig. 1, cyber layer) and, thus, the whole control system is still functional. Then, the Converter 2 is plugged back at  $t = 12.6$  s. As seen, the controller has properly updated the load sharing and global voltage regulation, afterwards.

#### D. Link-failure Resiliency

Resiliency to a single link failure is studied next in Fig. 9. The original communication graph in Fig. 1 is designed to carry a minimal redundancy, so no single link failure can cause loss of connectivity in the graph. Thus, the control system shall remain operational. As seen in Fig. 9, the link 1-2 has failed at  $t = 4.0$  s, but it does not have any impact on voltage regulation or load sharing. Controller response to the step load change in the remote load is also studied with the failed link, where a satisfactory performance can be seen. It should be noted that the reconfiguration caused by the link failure affects the Laplacian matrix and, thus, the whole system dynamic but not the steady-state performance.

Generally, any link failure limits information flow and can slightly slow down the transient response. Similar to Fig. 7(e), Fig. 9(d) demonstrates negligible impact of load change on the virtual impedances. However, by comparison, Fig. 7(e) shows more stable impedances than those of Fig. 9(d).

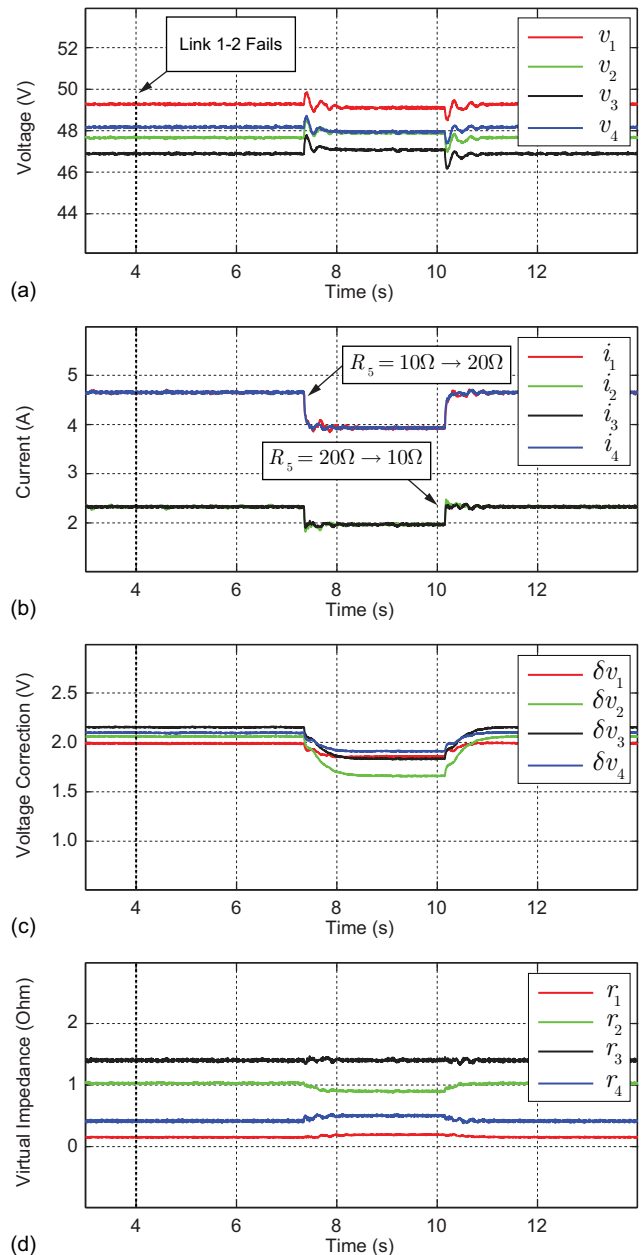


Fig. 9. Link-failure resiliency: (a) Terminal voltages, (b) Supplied currents, (c) Voltage correction terms, (d) Virtual impedances.

This observation concludes that higher graphical connectivity results in more stable droop impedances. In addition, small variations of the virtual impedance terms in Figs. 7(e) and 9(d) implies that the developed small-signal model in Section V-A is appropriate for modeling and stability analysis of the proposed adaptive droop mechanism.

## VII. CONCLUSION

An adaptive droop-based distributed secondary controller is proposed for dc Microgrids. The controller on each converter comprises two modules; the voltage regulator and the current regulator. The voltage regulator uses a cooperative voltage observer to estimate the global average voltage. This estimation is then further used to boost the local voltage set point to provide global voltage regulation. The current

regulator at each source compares local per-unit current with its neighbors' and, accordingly, adjusts the local virtual impedance to carry out proportional load sharing. This control paradigm uses a sparse communication network for data exchange among converters. Studies show that the proposed cooperative control provides precise global voltage regulation and proportional load sharing. Plug-and-play capability and link-failure resiliency of the control structure are also verified through experiments. It is also discussed that the droop coefficients show slight variations in response to load variations, which makes the small-signal modeling a viable approach for stability analysis of the proposed controller.

Future works focus on two main areas: 1) Study of alternative communication infrastructures, effects of channel non-idealities (e.g., delay or packet drop), and, consequently, to tailor consensus protocols to account for non-ideal data network; 2) Development of distributed optimization techniques for cost optimization in the tertiary control level.

#### APPENDIX I: SOLUTION TO THE QUADRATIC EQUATION

**Theorem A.1:** Assume  $\mathbf{L}$  is the Laplacian matrix of a communication graph with at least one spanning tree. If  $\mathbf{L}$  is balanced then, the only solution to the quadratic equation  $\mathbf{x}^T \mathbf{L} \mathbf{x} = 0$  is  $\mathbf{x} = k \mathbf{1}$ , where  $k$  is a real number.

**Proof:** The quadratic form,  $\mathbf{x}^T \mathbf{L} \mathbf{x}$ , is a real number. Thus,

$$\mathbf{x}^T \mathbf{L} \mathbf{x} = (\mathbf{x}^T \mathbf{L} \mathbf{x})^T = \mathbf{x}^T \mathbf{L}^T \mathbf{x} = \mathbf{x}^T \left( \frac{\mathbf{L} + \mathbf{L}^T}{2} \right) \mathbf{x}. \quad (\text{A.1})$$

Let's define the co-Laplacian matrix as  $\mathbf{L}_c \triangleq (\mathbf{L} + \mathbf{L}^T)/2$ , which is a symmetric matrix. Assume  $\mathbf{L} = [l_{ij}] \in \mathbb{R}^{N \times N}$  and  $\mathbf{L}_c = [l_{ij}^c] \in \mathbb{R}^{N \times N}$ . Then,

$$\begin{cases} l_{ii}^c = 2l_{ii} \geq 0, \\ l_{ij}^c = l_{ij} + l_{ji} = l_{ji}^c \leq 0, \quad i \neq j \end{cases} \quad (\text{A.2})$$

Since the Laplacian matrix,  $\mathbf{L}$ , is balanced,

$$l_{ii} = -\sum_{j \in N_i} l_{ij} = -\sum_{j=1(j \neq i)}^N l_{ij} = -\sum_{j=1(j \neq i)}^N l_{ji}. \quad (\text{A.3})$$

Accordingly, one can formulate diagonal elements of the co-Laplacian matrix,  $\mathbf{L}_c$ ,

$$l_{ii}^c = -\sum_{j=1(j \neq i)}^N (l_{ij} + l_{ji}) = -\sum_{j=1(j \neq i)}^N l_{ij}^c = -\sum_{j=1(j \neq i)}^N l_{ji}^c. \quad (\text{A.4})$$

The quadratic equation can be expanded using (A.4)

$$\begin{aligned} \mathbf{x}^T \mathbf{L} \mathbf{x} &= \frac{1}{2} \mathbf{x}^T \mathbf{L}_c \mathbf{x} = \frac{1}{2} \sum_{1 \leq i, j \leq N} x_i l_{ij}^c x_j \\ &= \frac{1}{2} \sum_{i=1}^N x_i^2 l_{ii}^c + \frac{1}{2} \sum_{i \neq j} x_i l_{ij}^c x_j \\ &= -\frac{1}{2} \sum_{i=1}^N \left( \sum_{j=1(j \neq i)}^N l_{ij}^c \right) x_i^2 + \frac{1}{2} \sum_{i \neq j} x_i l_{ij}^c x_j \\ &= \frac{1}{2} \sum_{i < j} (x_i l_{ij}^c x_j - x_i^2 l_{ij}^c - x_j^2 l_{ji}^c + x_j l_{ji}^c x_i) \\ &= -\frac{1}{2} \sum_{i < j} l_{ij}^c (x_i - x_j)^2 = 0 \end{aligned} \quad (\text{A.5})$$

where  $\mathbf{x} = [x_1, x_2, \dots, x_N]^T$ . All off-diagonal entries of the co-Laplacian matrix,  $\mathbf{L}_c$ , are non-positive. Thus, (A.5) holds if and only if for every two connected nodes, i.e.,  $a_{ij} > 0$ ,  $x_i = x_j$ .

The communication graph has a spanning tree and, thus, has a root node, from which there exists a path to every other node. Assume that  $v_i^g$  is the root node then, for any other node,  $v_j^g$ , one can find a sequence of nodes connecting  $v_i^g$  to  $v_j^g$ ,

$$v_i^g \rightarrow v_k^g \rightarrow \dots \rightarrow v_l^g \rightarrow v_j^g. \quad (\text{A.6})$$

Given that for every two connected nodes associated entries of the vector  $\mathbf{x}$  are equal, one can conclude

$$x_i = x_k = \dots = x_l = x_j. \quad (\text{A.7})$$

Thus, the vector  $\mathbf{x}$  has equal entries, i.e.,  $\mathbf{x} = k \mathbf{1}$ , where  $k$  is a real number. ■

#### APPENDIX II

Each of the underlying buck converters has  $L = 2640 \mu\text{H}$  and  $C = 2.2 \text{ mF}$  and operates with  $F_s = 60 \text{ kHz}$  switching frequency. Impedances of the transmission lines are  $Z_{12} = Z_{34} = Z_b$  and  $Z_{25} = Z_{35} = 2Z_b$ , where the base impedance is  $Z_b = 0.5 + (50 \mu\text{H})s$ . Impedances of the local loads are  $R_1 = 30 \Omega$  and  $R_2 = R_3 = R_4 = 20 \Omega$ . Voltages of the (rectified) input sources are  $V_{s1} = V_{s4} = 100 \text{ V}$  and  $V_{s2} = V_{s3} = 80 \text{ V}$ . The control parameters are as follow,

$$\mathbf{I}_{\text{rated}} = \text{diag}\{6, 3, 3, 6\}, \quad (\text{A.8})$$

$$b = 0.5, \quad (\text{A.9})$$

$$\mathbf{H}_p = 0.1 \times \mathbf{I}_4, \quad \mathbf{H}_1 = 2.5 \times \mathbf{I}_4, \quad (\text{A.10})$$

$$\mathbf{G}_p = 0.3 \times \mathbf{I}_4, \quad \mathbf{G}_1 = 5 \times \mathbf{I}_4, \quad (\text{A.11})$$

$$\mathbf{A}_G = \begin{bmatrix} 0 & 10 & 0 & 10 \\ 10 & 0 & 10 & 0 \\ 0 & 10 & 0 & 10 \\ 10 & 0 & 10 & 0 \end{bmatrix}, \quad \mathbf{r}_0 = \begin{bmatrix} 0.5 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0.5 \end{bmatrix}. \quad (\text{A.12})$$

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