

DNS OF TURBULENT CHANNEL FLOW AT VERY LOW REYNOLDS NUMBERS

Takahiro Tsukahara, Yohji Seki, Hiroshi Kawamura

Department of Mechanical Engineering,
Tokyo University of Science
Yamazaki 2641, Noda-shi, Chiba 278-8510, Japan
a7599109@rs.noda.tus.ac.jp, a7598074@rs.noda.tus.ac.jp, kawa@rs.noda.tus.ac.jp

Daisuke Tochio

Department of HTTR Project,
Oarai Research Establishment,
Japan Atomic Energy Research Institute
Oarai-machi, Higashiibaraki-gun, Ibaraki 311-1394, Japan
tochio@oarai.jaeri.go.jp

ABSTRACT

Direct numerical simulation (DNS) of a fully developed turbulent channel flow for very low Reynolds numbers has been executed with larger computational box-sizes than those of common DNS. The present Reynolds number is decreased down to $Re_\tau = 64$, where Re_τ is based on the friction velocity and the channel half width δ . For $Re_\tau=80$ with using the largest box of $51.2\delta \times 2\delta \times 22.5\delta$, the periodic weak-turbulence regions are observed. This type of locally disordered flow is similar to a turbulent puff observed in a transitional pipe flow. Various turbulence statistics such as turbulent intensities, vorticity fluctuations, Reynolds stresses are provided. Especially, their near-wall asymptotic behavior and budget terms of turbulence kinetic energy are obtained and discussed with respect to Reynolds number dependence and an influence of the computational box-size. In addition, two-point correlation coefficients, visualized instantaneous flow fields and the pre-multiplied energy spectra are presented in order to examine turbulence structures.

INTRODUCTION

A low Reynolds number flow in a channel is of practical importance with respect to a high temperature gas-cooled nuclear reactor, in which the low Reynolds number is employed to obtain a high outlet gas temperature. Direct numerical simulations (DNS, hereafter) of a fully developed turbulent channel flow have been increasingly performed for higher Reynolds numbers with an aid of recent development of computers. A DNS provides various information, such as velocity and pressure. Special attention has been paid to their near-wall asymptotic behavior and their derivatives at any time and point in the instantaneous field, which are extremely difficult to be measured in experiments.

The first DNS of the fully developed turbulent channel flow was made by Kim *et al.* (1987). Their Reynolds number was $Re_\tau=180$, which is based on the channel half width δ , the kinematic viscosity ν and the friction velocity $u_\tau = \sqrt{\tau_w/\rho}$, where τ_w is the statistically averaged wall shear stress and ρ is the density. Kuroda *et al.* (1989) carried out the DNS for a slightly lower Reynolds number of $Re_\tau=150$. The author's group (Kawamura *et al.*, 1998; Abe *et al.*, 2004a, 2004b)

Table 1: Reynolds numbers of the present DNS; i.e., $Re_\tau=u_\tau\delta/\nu$, $Re_m=u_m2\delta/\nu$, $Re_c=u_c\delta/\nu$. MB, medium box-size; SB, semi-large box-size; LB, large box-size, cf., Table 2.

Re_τ	180	150	110	80	80	70	64
Re_m	5730	4620	3290	2290	2320	2020	1860
Re_c	3360	2720	1960	1400	1430	1270	1200
Box size	MB	MB	MB	MB	LB	SB	SB

performed the DNS with respect to Reynolds number and Prandtl number dependences for $Re_\tau=180$ -1020. As for the low Reynolds number, several research groups carried out the DNS down to $Re_\tau=80$ in order to study a control of turbulence (Bewley *et al.*, 2001; Chang *et al.*, 2002; Högberg *et al.*, 2003). Iwamoto *et al.* (2002) have executed the DNS for $Re_\tau=110$ -650; their published results of $Re_\tau=110$ and 150 are also included in this paper for comparison. These studies often employed rather small computational boxes because of limited calculation resources. A great deal of effort has been conducted to experimental studies of the turbulent channel flow. Laufer (1951) first obtained the detailed turbulence statistics in the channel flow. Patel and Head (1969) measured skin friction and mean velocity profiles over the Re_m range 1,000-10,000 that includes the transition from laminar to turbulent flow, where Re_m based on the bulk mean velocity u_m and the channel width. Later, Kreplin and Eckelmann (1979) made their experiments for low Reynolds numbers of $Re_c=2,800$ -3,850, based on the centerline velocity u_c and δ . The measurements of the turbulent channel flow at $Re_c=2,850$ or 3,220 were executed by Niederschulte *et al.* (1990).

Recently, much attention is paid to a large-scale structure (LSS) in the turbulent channel flow (Jiménez, 1998; Liu *et al.*, 2001; Abe *et al.*, 2004a, 2004b). For the lower Reynolds number, the near-wall streak structure is so elongated that its length exceeds the usual computational box-size. Thus DNS of the low Reynolds number flow requires a larger box-size to capture the near-wall streak structure and the LSS.

In the present work, the DNS of fully developed turbulent channel flow has been carried out with the use of larger computational boxes than existing works. The purpose of this study is to obtain the turbulence statistics and characteristics of the turbulent channel flow at the very low Reynolds numbers.

Table 2: Computational domain size; L_i , N_i and Δi are a box length, a grid number and a spatial resolution of i -direction.

Box size	MB	SB	LB
L_x^*, L_z^*	12.8, 6.4	25.6, 12.8	51.2, 22.5
N_x, N_z	256, 256	256, 256	1024, 512
N_y	128	128	96
$\Delta x^*, \Delta z^*$	0.05, 0.025	0.10, 0.05	0.05, 0.044
$\Delta y_{\min, \max}^*$	0.0011-0.033	0.0011-0.033	0.0014-0.045

NUMERICAL PROCEDURE

The mean flow is driven by the uniform pressure gradient. It is assumed to be fully developed in streamwise (x -) and spanwise (z -) directions. The coordinates and the flow variables are normalized by u_τ , ν and δ . Periodic boundary conditions are imposed in the x - and z - directions and the non-slip is applied on the walls. The fundamental equations are the continuity and the Navier-Stokes equations. For the spatial discretization, the finite difference method is adopted. The numerical scheme with the 4th-order accuracy is employed in the streamwise and spanwise directions, while the one with the 2nd-order is applied in the wall-normal direction. Time advancement is executed by the semi-implicit scheme: the 2nd-order Crank-Nicolson for the viscous terms (wall-normal direction) and the 2nd-order Adams-Bashforth methods for the other terms.

In the present work, a series of DNS has been made for $Re_\tau=64$ -180 (see Table 1). For the lower Reynolds numbers of $Re_\tau=64$ -80, the larger boxes than those of common DNS are adopted. The computational conditions are shown in Table 2. The nonuniform meshes are applied in the wall-normal direction. Note that quantities with the superscript of * indicate those normalized by the outer variables, e.g., $y^* = y/\delta$. In the present DNS, the pressure gradient is decreased stepwisely down to an estimated level for the aimed Reynolds number. The fully developed flow field at higher Reynolds number is successively used as the initial condition for the one-step lower Reynolds number, e.g., $Re_\tau=180 \rightarrow 150$, $150 \rightarrow 110$, $110 \rightarrow 80$ and so on. Note that various statistical data are obtained after the flow has reached a statistical-steady state.

RESULTS AND DISCUSSION

Mean velocity profile

Figure 1 shows the vertical profile of the dimensionless mean velocity in wall units, where quantities with the superscript of + indicate those normalized by the wall variables, e.g., $y^+ = yu_\tau/\nu$. Statistics are denoted by a overline of $(\bar{\quad})$, that are the spatial (in the horizontal directions) and temporal averaging. The obtained data from the experiments of Patel and Head (1969) and the DNS by Iwamoto *et al.* (2002) using the spectral method are also shown for comparison. The present results for $Re_\tau=110$ -180 are in good agreement with the DNS of Iwamoto *et al.*. In these low Reynolds number flows, the mean velocity distributions do not indicate the logarithmic region clearly. For the lower Reynolds numbers of $Re_\tau \leq 110$, von Kármán constant (not shown here) does not exhibit any constant range at all. In the outer region ($y^+ > 10$), a significant Reynolds number dependence is found when normalized by the inner variables. Mean flow variables such as the bulk mean velocity \bar{u}_m^+ and the mean centerline velocity \bar{u}_c^+ are

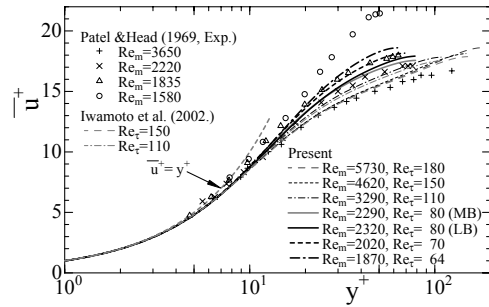


Figure 1: Mean velocity profile in viscous wall units

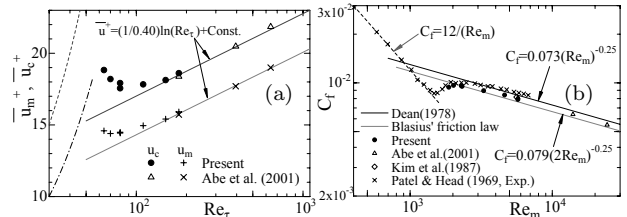


Figure 2: Reynolds number *versus* (a) centerline velocity u_c^+ and bulk mean velocity u_m^+ , (b) friction coefficient C_f . In (a), dotted lines (---, - · -) show the laminar flow relations of $u_c = Re_\tau/2$ and $u_m = Re_\tau/3$, respectively.

given in Fig. 2(a) for each Reynolds number. It is interesting to note that the values of \bar{u}_c^+ and \bar{u}_m^+ increases with decreasing Reynolds number, if $Re_\tau < 80$. The reason will be discussed later. Both \bar{u}_c^+ and \bar{u}_m^+ are expected to approach gradually to laminar values.

Although the skin friction coefficient is one of the most fundamental turbulence characteristics, the one in the transitional region of the channel flow has not been examined yet through the DNS owing to the lack of the low Reynolds number simulations. Figure 2(b) shows a variation of the skin friction coefficient $C_f = 2\tau_w/(\rho \cdot u_m^2)$ in comparison with the empirical correlations proposed by Dean (1978) for a channel flow, and by Blasius for a pipe flow. The present results are in good agreement with them for $Re_m > 3000$. It is worth noting that, for $Re_m < 3000$, C_f tends to be smaller than the empirical correlations with the decreasing Reynolds number, and it agrees well with the experimental data from Patel and Head (1969). It is found that the present Reynolds number is close to the laminarization. The lowest Reynolds number of $Re_m = 1860$ in the present DNS lays still in the transitional region. The lower limit cannot be clearly defined by the calculation up to now.

Turbulence intensity

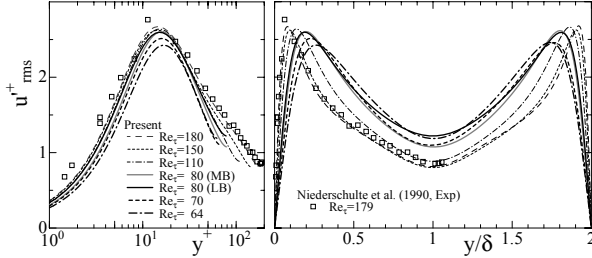
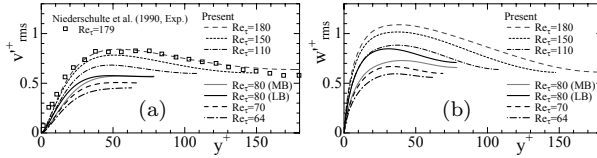
The root-mean-square (r.m.s.) of the streamwise velocity fluctuation normalized by u_τ is given in Fig. 3. If u_{rms}^+ is plotted against y/δ , it increases remarkably in the central region of the channel for $Re_\tau < 80$. The value of the local maximum near the wall decreases remarkably at $Re_\tau \leq 70$.

With respect to the computational box-size, a significant influence of the box-size upon u_{rms}^+ can be seen for $Re_\tau=80$ at the central region. With extending box size, u_{rms}^+ is enhanced, with a deviation of about 12% at the channel center. This is because the turbulence structure is confined by a short box length in the case of $Re_\tau=80$ (MB). This tendency is also

Table 3: Near-wall expansion coefficient

Re_τ	b_1	c_2	b_3	$\overline{b_1 c_2}$
180	0.360	8.70×10^{-3}	0.189	7.30×10^{-4}
180 [†]	0.356	8.5×10^{-3}	0.190	7.0×10^{-4}
150	0.354	8.60×10^{-3}	0.172	7.10×10^{-4}
110	0.336	6.75×10^{-3}	0.145	5.45×10^{-4}
80(MB)	0.302	4.55×10^{-3}	0.105	3.45×10^{-4}
80(LB)	0.333	6.85×10^{-3}	0.144	4.45×10^{-4}
70	0.291	4.65×10^{-3}	0.101	3.10×10^{-4}
64	0.268	3.90×10^{-3}	0.086	2.45×10^{-4}

[†] Antonia and Kim (1994)


 Figure 3: R.m.s. of the streamwise velocity fluctuation u'

 Figure 4: R.m.s. of the wall-normal fluctuation v' (a) and the spanwise fluctuation w' (b).

seen for spanwise fluctuations in the whole channel (Fig. 4(b)), with a deviation of 7-27%. The influence upon the wall-normal component is small (Fig. 4(a)). Moreover, the influence of the box-size on the mean flow variables and other turbulence quantities, such as $\overline{u^+}$, vorticity fluctuations (shown later), are also significant at very low Reynolds number of $Re_\tau=80$, whereas the those of the box-size on the turbulence statistics are rather small for the moderate Reynolds number of $Re_\tau=180$ -640 as shown by Abe *et al.* (2004a).

Effect of Reynolds number is significant in the u'_{rms} of both spanwise and wall-normal directions. All component values decrease with the decrease of Reynolds number. Antonia *et al.* (1992) indicated that the Reynolds number dependence of w'_{rms} is more significant compared to that of u'_{rms} and v'_{rms} . In the present work, both v'_{rms} and w'_{rms} decrease remarkably with the decreasing Re_τ . This is because the production term of u'_{rms} and redistribution for v'_{rms} and w'_{rms} are reduced with the decreasing Re_τ as discussed later.

To analyse the near-wall asymptotic behaviour, the velocity fluctuations can be expanded in Taylor series about-the-wall value as follows:

$$\begin{cases} u'^+ = b_1 y^+ + c_1 y^{+2} + \dots \\ v'^+ = c_2 y^{+2} + \dots \\ w'^+ = b_3 y^+ + c_3 y^{+2} + \dots \end{cases} \quad (1)$$

The r.m.s. values of the vorticity fluctuations are shown in Fig. 5. The streamwise and spanwise vorticity fluctuations, $\omega_x'^+ (=b_3)$ and $\omega_z'^+ (=b_1)$, decrease with decreasing

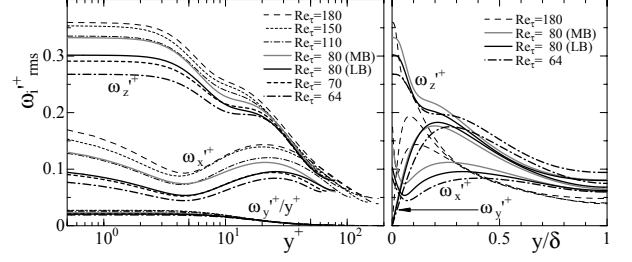


Figure 5: R.m.s. of vorticity fluctuation

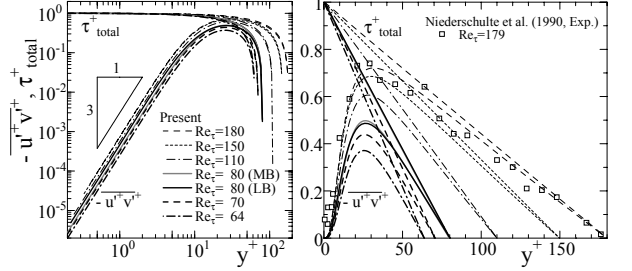


Figure 6: Reynolds shear stress and total shear distribution

Reynolds number. However, the influence of insufficient box size for $Re_\tau=110$ and 80(MB) cannot be neglected. The ratio $\omega_y'^+/y^+ (=b_{3,1})$ tends to become constant in the near-wall region as reported by Antonia and Kim (1994).

The use of Eq. (1) in the expression for the Reynolds shear stress, $-\overline{u'^+ v'^+}$, yields

$$-\overline{u'^+ v'^+} = -\overline{b_1 c_2} y^{+3} + \dots \quad (2)$$

The near-wall values of b_1 , c_2 , b_3 and $\overline{b_1 c_2}$ are extrapolated up to the wall, and are given in Table 3. The present result of $Re_\tau=180$ agrees well with that of Antonia and Kim (1994). These coefficients decrease with the decrease of Reynolds number. This is because the production rate of the turbulent kinetic energy decreases with decreasing Reynolds number as discussed later. Especially, the decrease of c_2 , b_3 and $\overline{b_1 c_2}$ is significant when the Reynolds number falls to 70; the decrease in $\overline{b_1 c_2}$ is slightly larger than that for either c_2 or b_3 . In the case of $Re_\tau \leq 80$ (MB), however, the obtained coefficients could be further influenced by the box-size.

Reynolds shear stress

Figure 6 shows the Reynolds shear stress $-\overline{u'^+ v'^+}$ and the total shear stress τ_{total} . As the Reynolds number decreases, the peak value of $-\overline{u'^+ v'^+}$ decreases and its position moves close to the wall, if scaled with the wall unit. When Re_τ is 180, the peak of $-\overline{u'^+ v'^+}$ reaches 0.72 at $y^+=32$, while, in the case of $Re_\tau=64$, it becomes 0.37 at $y^+=26$.

In the fully developed channel flow, the production term of the turbulent kinetic energy is expressed as

$$P_k = -\overline{u'^+ v'^+} \frac{\partial \overline{u^+}}{\partial y^+} = -\overline{u'^+ v'^+} \left[1 - \frac{y^+}{Re_\tau} - (-\overline{u'^+ v'^+}) \right]. \quad (3)$$

Thus the peak value of P_k can be calculated as

$$P_k = \frac{1}{4} \left[1 - \frac{y_{max}^+}{Re_\tau} \right]^2 \text{ at } \left\{ y^+ \mid -\overline{u'^+ v'^+} = \frac{\partial \overline{u^+}}{\partial y^+} \right\}. \quad (4)$$

Here, the wall-normal position of the peak of P_k is denoted as y_{max}^+ , where the Reynolds shear stress and the viscous stress

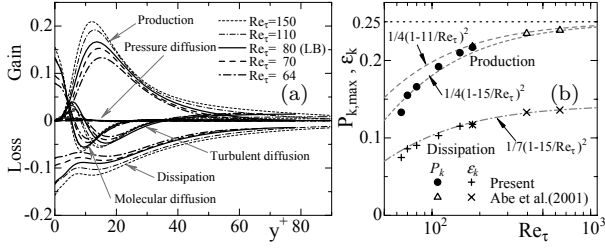


Figure 7: Budget of turbulent kinetic energy k normalized by ν/u_τ^4 ; (b) variation of the peak of production term $P_{k,\max}$ and the dissipation rate ε_k at the same height.

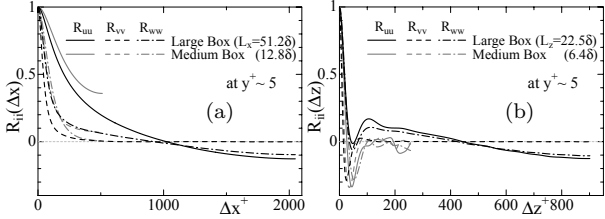


Figure 8: Two-point correlation coefficients R_{ii} of the velocity fluctuation component at $Re_\tau = 80$; (a) streamwise, (b) spanwise.

are equal to half of the total shear stress. In the present calculation, y_{\max}^+ is 11 for $Re_\tau=180$; while, decreasing Reynolds number, it moves away from the wall and reaches at $y_{\max}^+ \approx 15$ for $Re_\tau \approx 15$. In addition, this indicates that the peak value of P_k decreases with decreasing Re_τ (see Fig. 7(a)). Figure 7(b) shows the peak value of P_k and dissipation rate ε_k at y_{\max}^+ for each Reynolds number. The decrease in $P_{k,\max}$ with decreasing Re_τ is clearly more prominent than that of ε_k . This is the reason why the turbulent intensities are decreased in the near-wall region with the decreasing Re_τ , as seen in Figs. 3 and 4 and in Table 3.

Turbulence structure: instantaneous flow fields

The effect of the box size can be most clearly observed in the streamwise and spanwise two-point correlations of velocity fluctuation R_{ii} , which is shown in Fig. 8. For $Re_\tau=80(\text{MB})$, R_{uu} does not fall down to zero, indicating that the box-size is not large enough; especially, the streamwise box length is too short to contain the streak structures in the near-wall region (Fig. 8(a)). On the other hand, R_{uu} and R_{ww} fall down to negative values at the mid box-length for both stream- and the spanwise directions for the large box-size (LB), while R_{vv} falls off to almost zero. It points out that one long wavelength structure is captured with this large box (LB). In addition, a significant decrease in the magnitude of the negative maximum is found at the spanwise separation distance of $z^+ \approx 50$ which corresponds to the spanwise spacing of the near-wall streak structures (Fig. 8(b)). These suggest that there exists an influence of the LSS not only in the channel center but also in the near-wall region. The spacing of the streak structures and the LSS has been investigated with the use of the pre-multiplied energy spectra, which will be discussed later.

The streamwise and spanwise pre-multiplied energy spectra for $Re_\tau=80$ are shown in Fig. 9 with reference to Jiménez (1998). The peak position of the pre-multiplied energy spectra gives the most energetic wavelength (MEW). It is in-

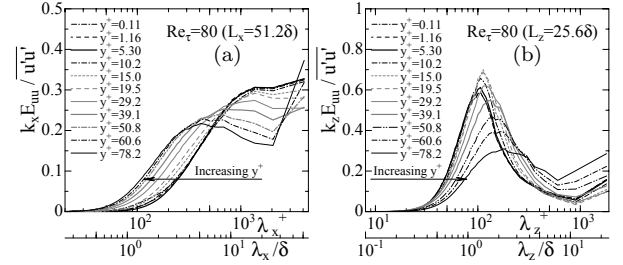


Figure 9: Pre-multiplied energy spectra for $Re_\tau = 80$; (a) $k_x E_{uu}/u'u'$, (b) $k_z E_{uu}/u'u'$.

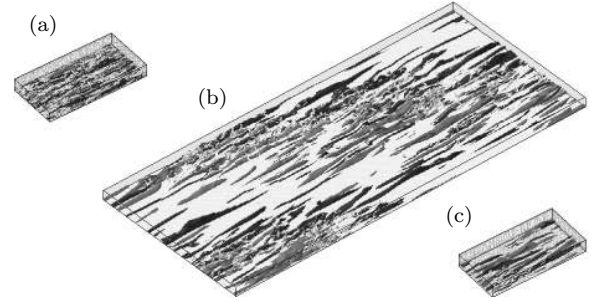


Figure 10: Instantaneous flow fields; high (gray) and low (dark-gray) speed regions of u'^+ and negative regions (light-gray) of the second invariant of deformation tensor $u'_{i,j} u'_{j,i}$. (a) $Re_\tau = 180$, (b) $Re_\tau = 80(\text{LB})$, (c) $Re_\tau = 80(\text{MB})$. All of the box-size (a)-(c) are scaled by δ . Direction of the mean flow is from bottom-left to top-right.

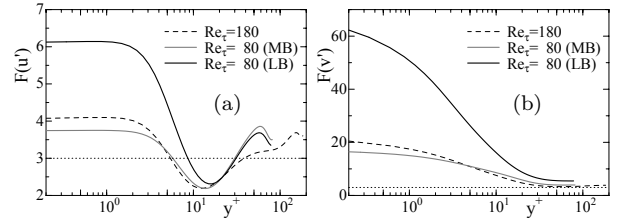


Figure 11: Flatness factor of velocity fluctuation; (a) streamwise component $F(u')$, (b) wall-normal component $F(v')$.

teresting to note that MEW in the wall vicinity stays still at about $\lambda_z^+ \approx 100$ and not much changed from that of the higher Reynolds numbers even though the Re_τ is as low as 80 (Fig. 9(b)). Moving away from the wall, the MEW shifts slightly to the longer wavelengths. In the central region, on the other hand, a peak of MEW arises at about $\lambda_z^+ = 180$. This MEW corresponds to about 2.3δ , which shows a significant deviation from $1.3-1.6\delta$ obtained for the higher Reynolds numbers, cf., Abe *et al.* (2004a). The streamwise MEW arises at $\lambda_x^+ \approx 1,000$ in the near-wall region. With increase in the distance from the wall, the streamwise MEW moves towards the shorter wavelength of $\lambda_x^+ \approx 500$ (Fig. 9(a)). On the other hand, in the both directions, another peak appears at the longest wavelength in the core region, which corresponds to long-wavelength structures in the visualized flow field (Fig. 10(b)).

Figure 10 shows the high- and low-speed regions and the second invariant of deformation tensor ($II' = \partial u'_i / \partial x_j \times \partial u'_j / \partial x_i$) at $Re_\tau=180$, 80(MB) and 80(LB). For $Re_\tau=180$, the high- and low-speed streaks are evenly distributed as seen

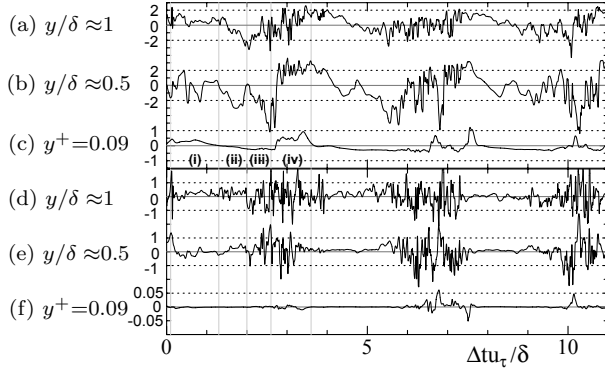


Figure 12: Typical time trace of u - and v -fluctuations at $Re_\tau=80(\text{LB})$. The measurement points are at various wall-normal locations at the same position in the (x, z) -plane. (a)-(c), the streamwise fluctuation u^+ ; (d)-(f), the wall-normal fluctuation v^+ .

in Fig. 10(a). For $Re_\tau=80(\text{LB})$, on the contrary, the near-wall streaks are unevenly distributed and the sparse region can be observed. The shape of this flow field is so similar to that of the natural turbulent spot observed in experiments of the plane channel flow in transitional region, cf., Carlson *et al.* (1982). The well-known vortex structures such as quasi-streamwise vortices are unevenly distributed near the wall. In addition, these vortices are associated closely with the crowded near-wall streaks. The long-wavelength structure of the weak-turbulent (laminar-like velocity profile) region occurs periodically. Its streamwise wavelength occupies almost the whole box-length. This is a reason why the streamwise two-point correlations R_{uu} fall down to a negative value at the middle of the box as seen in Fig. 8.

The flatness factor of the velocity fluctuation is shown in Fig. 11. For $Re_\tau=80$, comparison of the results with different box sizes indicates that the influence of box size upon the flatness factor is very significant (see 80(MB) and 80(LB)). If the box size is extended large enough to capture the highly disordered turbulent region and weak-turbulent regions, intermittency of fluctuation is enhanced. Moreover, an increase of the flatness factor with decreasing Reynolds number is found in the near-wall region.

Turbulence structure: puff-like structures

Wyganski and co-workers (1973, 1975) conducted a study of the structures and phenomena associated with transitional and turbulent *pipe flow* in the range of $1,000 < Re_m < 50,000$. They identified two transitional flow states, the type observed being dependent on Re_m . For $2,000 < Re_m < 2,700$ the transition structures were termed ‘turbulent puffs’; the second state is found at $Re_m > 3,500$ and consists of structures termed ‘turbulent slugs’. Both a puff and a slug are characterized by a distinct trailing edge over which the flow changes almost discontinuously from turbulent flow to laminar flow. In the *channel flow* of the present study, the computational results shown in Fig. 12 are strikingly similar to experimental velocity traces obtained by Wyganski and Champagne (1973) for a *pipe flow*. It is observed that the sequence of events as the structure is advected past the measurement point. It can be interpreted as: (i) laminar-like flow, (ii) a gradual reduction of u , (iii) a highly disordered turbu-

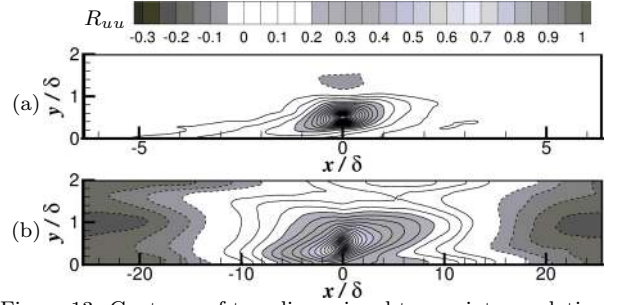


Figure 13: Contours of two-dimensional two-point correlation coefficient R_{uu} in the (x, y) -plane; the reference point is at the mid-height $y_{\text{ref}} = 0.5\delta$. The direction of the mean flow is from left to right. (a) $Re_\tau = 180$; (b) $Re_\tau = 80$ (LB). —, positive correlation; - - -, negative correlation; the line of $R_{uu} = 0$ is not shown here. Contour interval $\Delta R_{uu}: 0.05$.

lent region, (iv) a sharp interface with laminar-like flow, again return to (i) laminar-like flow. The intensities of both u' and v' are enhanced periodically with interval of $\Delta t u_\tau / \delta \approx 3.5$, so the upstream interface was observed to travel at a speed close to the bulk mean velocity $u_m^+ \approx 14.5$. With respect to the present Reynolds number, i.e. $Re_m=2320$, the obtained structures of co-existing weak-turbulent region as discussed above are consistent with and remarkably similar to the ‘turbulent puffs’ observed in a *pipe flow*.

The shape of the structures in the wall-normal direction is clearly illustrated from the two-dimensional correlation for velocity in the (x, y) -plane. While the region of negative correlation appears in the side of the other wall for $Re_\tau=180$ (Fig. 13(a)), the negative region appears in a wide region of $|\Delta x| > 13\delta$ for $Re_\tau=80(\text{LB})$. This indicates that a puff-like structure with a large streamwise wavelength of $52h$ fills the entire channel width in the case of $Re_\tau=80(\text{LB})$.

A typical well-developed structure at $Re_\tau=80(\text{LB})$ is shown in the sequence of flow visualization presented in Fig. 14. The puff-like structure Fig. 14(a) are consist of a laminar-like flow (region A) and a highly disordered turbulence (region B). Figures 14(b)-(f) indicate that the structures are equilibrium and self-sustained. Moreover, the both regions propagate with the same streamwise velocity and are inclined at an angle of 24° with respect to the streamwise direction. Therefore, the puff-like structures are spatially distributed not only in streamwise but also spanwise, while the puff of a pipe flow is homogeneous in azimuthal and intermittent only in the streamwise direction. Note that the present results, such as visualized flow fields, two-point correlation (Fig. 8) and energy spectra (Fig. 9), show signs of being constrained by the periodicity of the boundary, even when the box-size was extended to $(L_x \times L_z) = (51.2\delta \times 22.5\delta)$; and the numerical box requires to be enlarged further.

CONCLUSIONS

In the present study, we performed DNS of the turbulent channel flow with larger computational boxes down to $Re_\tau=64$ and investigated the turbulence statistics with respect to low Reynolds number effect.

- For $Re_m < 3000$ ($Re_\tau \leq 80$), C_f tends to be smaller than the empirical correlation. Reynolds number dependence of the mean velocity profile is significant in the outer region when scaled with the wall units.

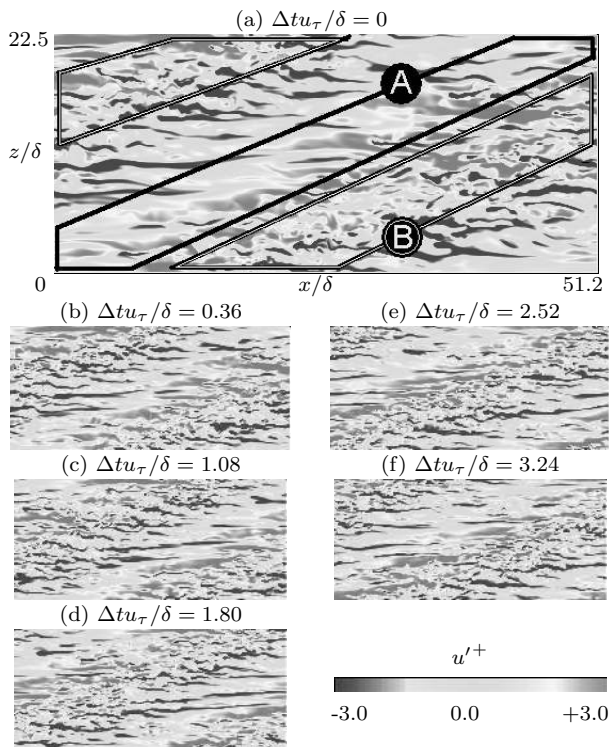


Figure 14: Contour of streamwise velocity fluctuation u'^+ for a series of consecutive times, in an (x, z) -plane at $y/\delta \approx 0.5$ for $Re_\tau = 80$ (LB). All of the contours (a)-(f) shows the whole (x, z) -plane of $L_x \times L_z = 51.2\delta \times 22.5\delta$. The direction of the mean flow is from left to right.

- For $Re_\tau=80$, the periodic weak-turbulence region with the streamwise long-wavelength is observed with using the largest box of $51.2\delta \times 2\delta \times 22.5\delta$, and is very similar to a ‘turbulent puff’ observed in a transitional pipe flow.
- The significant effects of the captured puff-like structures exist upon the turbulence statistics, such as a mean velocity and turbulence intensities.
- The equilibrium puff-like structures observed in the channel flow inclines against the streamwise direction. The propagation velocity of the puff-like structure is approximately equal to the bulk mean velocity.

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