

CenWIT
Center for Wireless Information Technology

**Dynamic Multiuser Resource Allocation
and Adaptation for Wireless Systems**

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Hong Kong University of Science & Technology





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**The Hong Kong University of
Science & Technology**

- **The university opened in 1991**
 - Consists of four schools
 - Offers academic programs at undergraduate, master and doctoral levels
- **HKUST Academic System**
 - Credit based continuous assessment system used by North American universities
 - Faculty retention and promotion system similar to North American universities
 - Faculty is expected to perform research, teaching and service
 - English Instruction




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ECE Department: State-of-the Facilities






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ECE Faculty Background

Mostly educated in North America

- UC Berkeley 7
- Stanford 5
- Toronto 4
- U. Wash. Seattle 4
- U. Illinois, Urbana C. 3
- U. Southern California 3
- Harvard 3
- Princeton 2
- Columbia 2
- Yale 2
- Purdue 1



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Overseas Exchange Program

- Enhances students' exposure in overseas universities w/o delaying graduation (One semester in Mainland and two semesters Overseas)
- Some of our partners
 - Univ. of Pennsylvania, UCLA, USA
 - UC Berkeley, Georgia Tech, MIT, Rice, USA
 - Rice Univ., USA
 - U. of Toronto, U. of Waterloo, Canada
 - Univ. of Sydney, Australia
 - Chalmers University of Technology, Sweden
 - École des Mines de Nantes, France
 - INT, France
 - Technical U. of Denmark, Denmark
 - U. of Bath, UK
 - Chinese universities
 - Peking University, Fudan U., Tsinghua, Shanghai Jiaotong U., Nanjing U.




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ECE -International Recognition

- IEEE Grade of Fellow is one of the Institute's most prestigious honors
- Comparison between some countries in Asia-Pacific (as of 16/1/03)

Country	No. Fellows
Australia	35
Taiwan	35
Hong Kong	28
India	26
China	23
Korea	16
New Zealand	3

- ECE Department at HKUST has 11 IEEE Fellows as of December 2006



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WORLD'S TOP 50 UNIVERSITIES



(The Times of London Nov 5, 2004)

1 Harvard University (US) 1,000 pts	25 McGill University (Canada) 364.1	45 Indian Institute of Technology (India) 241.7
2 University of California, Berkeley (US) 890.2	26 Melbourne University (Australia) 353.2	46 Hong Kong University of Sci & Tech (Hong Kong) 240.6
3 Massachusetts Institute of Technology (US) 798.9	27 Cornell University (US) 348.8	47 Manchester University (UK) 238.5
4 California Institute of Technology (US) 736.9	28 University of California, San Diego (US) 331.5	48 School of Oriental and African Studies (UK) 235.8
5 Oxford University (UK) 731.8	29 Johns Hopkins University (US) 330.8	49 Massachusetts University (US) 235.7
6 Cambridge University (UK) 731.8	30 University of California, Los Angeles (US) 315.4	50 University of British Columbia (Canada) 230.4
7 Stanford University (US) 688.0	31 Ecole Polytechnique (France) 315.5	51 Heidelberg University (Germany) 228.3
8 Yale University (US) 582.8	32 Ecole Normale Supérieure (France) 303.7	52 Edinburgh University (UK) 227.6
9 Princeton University (US) 557.5	33 Kyoto University (Japan) 300.7	53 Queensland University (Australia) 223.9
10 ETH Zurich (Switzerland) 553.7	34 Ecole Normale Supérieure (France) 298.4	54 Nanjing University (China) 217.1
11 London School of Economics (UK) 484.4	35 Michigan University (US) 293.3	
12 Tokyo University (Japan) 482.0	36 Ecole Polytechnique Fédérale de Lausanne (Switzerland) 280.4	
13 University of Chicago (US) 444.0	37 Monash University (Australia) 280.0	
14 Imperial College London (UK) 443.7	38 University College London (UK) 281.2	
15 University of Texas at Austin (US) 421.5	39 Brown University (US) 281.6	
16 Australian National University (Australia) 417.7	40 New South Wales University (Australia) 275.7	
17 Beijing University (China) 391.8	41 Toronto University (Canada) 272.5	
18 National University of Singapore 385.9	42 Carnegie Mellon University (US) 259.4	
19 Columbia University (US) 384.1	43 Hong Kong University (Hong Kong) 249.5	
20 University of California, San Francisco (US) 376.5	44 Sydney University (Australia) 245.2	




Bristol University: No 91



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2006 Top Universities



HKUST among World's Best Technology Universities
HKUST has been **ranked number 17** by *The Times Higher Education Supplement (THES)* in its league table of the **World's Top 100 Technology Universities**, and **number ONE** university in **Hong Kong**.
(*The Times Higher Education Suppl* - Oct. 17, 2006)

Rank	Institution	Country
1	Massachusetts Institute of Technology	US
2	University of California, Berkeley	US
3	Indian Institutes of Technology	India
4	Imperial College London	UK
5	Stanford University	US
6	Cambridge University	UK
7	Tokyo University	Japan
8	National University of Singapore	Singapore
9	California Institute of Technology	US
10	Carnegie Mellon University	US
11	Oxford University	UK
12	ETH Zurich	Switzerland
13	Delft University of Technology	Netherlands
14	Tsing Hua University	China
15	Nanyang Technological University	Singapore
16	Melbourne University	Australia
17	Hong Kong University of Sci & Technol	Hong Kong
18	Tokyo Institute of Technology	Japan
19	New South Wales University	Australia
20	Beijing University	China

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Newsweek International Edition

Newsweek ranks HKUST at #60 globally! (Aug., 2006)

✓ **Global Top 100 Ranking** takes into account *openness and diversity*, as well as *distinction in research*.
 ✓ **UST is #1 in HK at #60**, with **HKU at #69** and **CU at #96**.
 ✓ **Youngest University** in the list of **Global Top 100**.
 ✓ **Not a single other Mainland Chinese university** made the **Global Top 100**.
 (NEWSWEEK International - Aug 13, 2005)

- Harvard University
- Stanford University
- Yale University
- California Institute of Technology
- University of California at Berkeley
- University of Cambridge
- Massachusetts Institute of Technology
- Oxford University
- University of California at San Francisco
- Columbia University
- ...
59. University of California at Santa Barbara
60. Hong Kong University of Science and Technol.
61. Wageningen University
62. Michigan State University
63. University of Munich
64. University of New South Wales
65. Boston University
66. Vanderbilt University
67. University of Rochester
68. Tohoku University
69. University of Hong Kong
- ...
96. Chinese University of Hong Kong
97. University of Newcastle
98. Innsbruck University
99. University of Massachusetts at Amherst
100. Sussex University

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Motivation and Background

Cellular mobile subscribers worldwide (Source: ITU)



1.5 billion

9.5 billion



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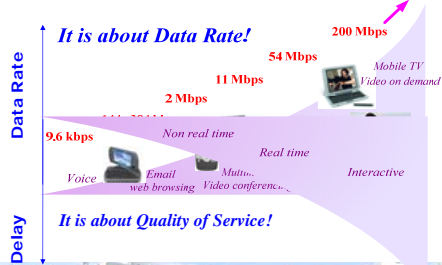
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Motivation and Background

It is not just about data rate!

It is about Data Rate!

It is about Quality of Service!



200 Mbps

54 Mbps

11 Mbps

2 Mbps

9.6 kbps

Mobile TV

Video on demand

Non real time

Real time

Voice

Email

web browsing

Multi-video conferencing

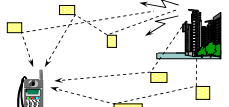
Interactive

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Challenges

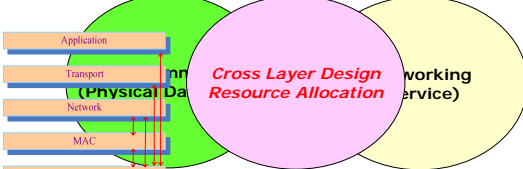
- ❑ High Data Rate, seamless and high mobility requirements
- ❑ Spectral efficiency challenge (2 – 10 b/s/Hz)
- ❑ Frequency selectivity due to large bandwidth requirements
- ❑ High System Capacity
- ❑ Seamless coverage and support across different networks, devices, and media forms
- ❑ Reliable Communications
 - Harsh wireless channel
 - Scarce radio spectrum
 - Energy constraint



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Cross-layer Optimization and Resource Allocation



Cross Layer Design Resource Allocation

- High Spectral Efficiency
- High Energy Efficiency
- Overall good performance


K. B. Letaief and Y. J. Zhang, "Dynamic Multiuser Resource Allocation and Adaptation for Wireless Systems," (Invited Paper) IEEE Wireless Commun., Aug. 2006

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Outline

- Introduction to OFDM and MIMO
- Introduction to dynamics in wireless communications systems
- Dynamic resource allocation
 - SISO-OFDM systems
 - MIMO-OFDM systems
- Cross-layer design and optimization
 - Joint MAC-PHY resource allocation
 - Joint design of PHY and networking or application layers

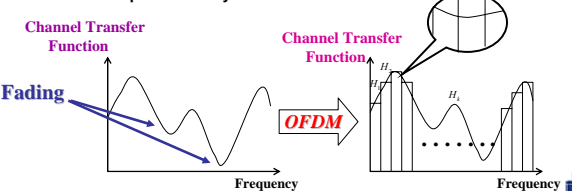


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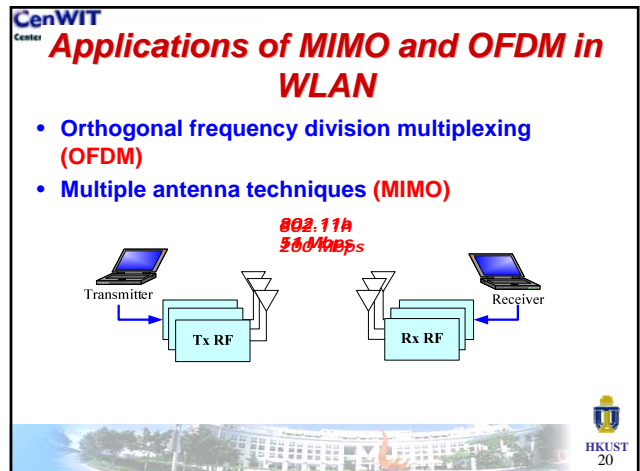
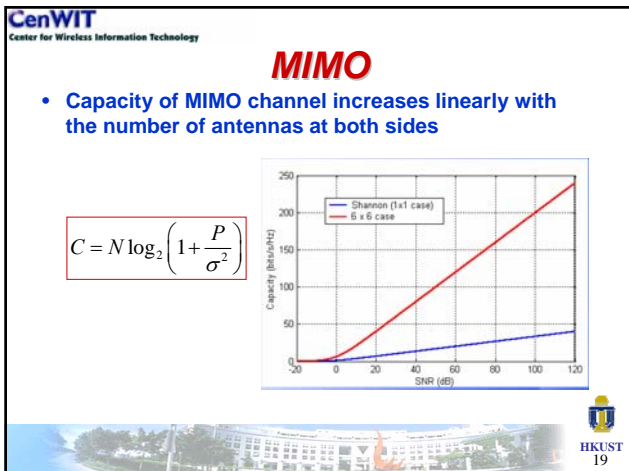
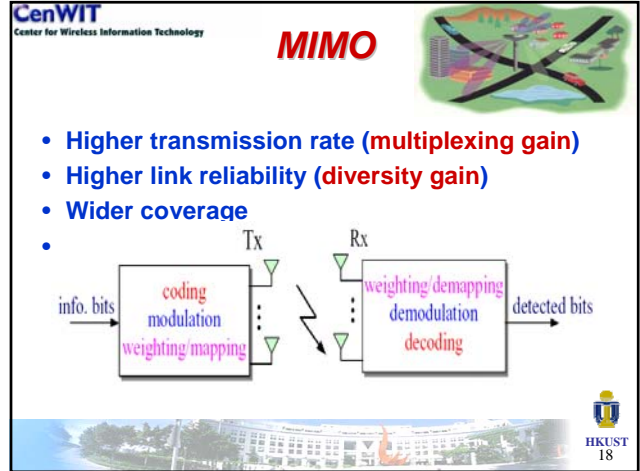
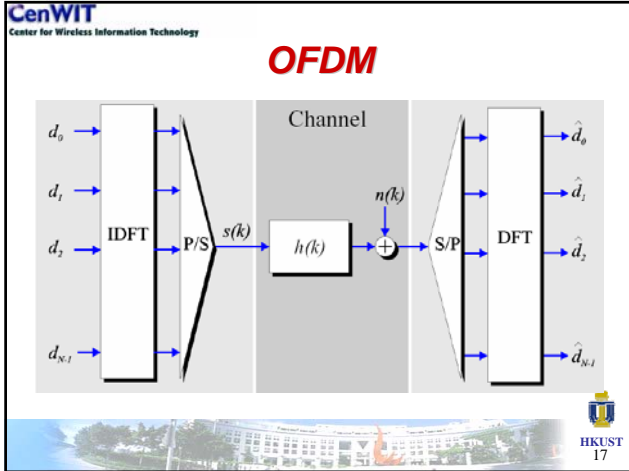
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OFDM

- OFDM: **O**rtogonal **F**requency **D**ivision **M**ultiplexing
- Converts a **wideband frequency selective fading channel** into a parallel collection of narrow band **frequency flat sub-channels**
 - Robust against fading, ISI, and narrowband interference
 - Can be implemented by discrete FFT



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Dynamics in Wireless Communications Systems – Channel Variation

- Wireless channel varies dramatically over time, frequency, and space

A 3D surface plot with 'Time/Hz' on the x-axis, 'Frequency' on the y-axis, and 'Channel Gain' on the z-axis. The surface shows a complex, multi-peaked landscape representing channel variations.

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Link Adaptation

- Adaptive modulation
 - Data rate: $\log_2(1 + \gamma_n P_n)$
 - γ_n : Effective channel gain on subchannel n
 - P_n : Transmit power on subchannel n
- Optimal power allocation: *Water filling*

Two graphs are shown. The top graph plots 'Channel Gain (dB)' vs 'Subchannel Index' (0-250), showing a fluctuating line with markers for 6, 4, 2, and 0 bps/Hz. The bottom graph is a bar chart of 'Subchannel Index' vs 'Power Allocation', showing a water-filling distribution with a constant level λ and a power constraint $P_n = \lambda - \frac{1}{\gamma_n}$.

$$P_n = \begin{cases} \lambda - \frac{1}{\gamma_n} & \lambda \geq \frac{1}{\gamma_n} \\ 0 & \text{otherwise} \end{cases}$$

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Link Adaptation

A log-log plot of 'BER error rate' vs 'Average received E_b/N_0 (dB)'. The y-axis ranges from 10^{-4} to 10^0 , and the x-axis ranges from 0 to 30. Three curves are shown for 2, 4, and 6 bps/Hz. The 'Adaptive' curves are significantly lower than the 'Non-adaptive' curves, indicating better performance.

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Dynamics in Wireless Communications Systems – Multiuser Diversity

- Channel attenuations of different users are mutually independent
- Frequency and time domain channels can be dynamically allocated to users
- Examples:
 - Dynamic subcarrier allocation
 - Opportunistic scheduling

Three diagrams show 'Channel Gain' vs 'Frequency'. The top diagram shows OFDM for User 1 with a red dashed line. The middle diagram shows OFDM for User 2 with a blue dashed line. The bottom diagram shows OFDMA with multiple users' channel gains represented by colored bars.

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Dynamics in Wireless Communications Systems

- Impact of PHY layer characteristics on the upper layers
 - Time-varying channel capacity
 - Time-varying connectivity and topology
 - User mobility

Obstacles or Opportunities?






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Resource Allocation in SISO-OFDM Systems

- **Resource:** time slots, subcarriers, power
- **Constraints:** Bit error rate, maximum transmit power, minimum data rate, ...
- **Objectives:** Maximize spectrum efficiency, power efficiency, or system utility






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Problem Formulation

- $r_{k,n}$: data rate of user k on subcarrier n
- $p_{k,n}$: transmit power of user k on subcarrier n
- $c_{k,n}$: subcarrier allocation indicator of user k on subcarrier n
- $h_{k,n}$: channel coefficient of user k on subcarrier n
- R_k : minimum data rate requirement of user k , if any

$$p_{k,n} = \frac{f_k(r_{k,n})}{|h_{k,n}|^2} \text{ for } k, n$$



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Problem Formulation


- Maximizing data rate for a given power budget and a target BER:

$$\max_{P_{k,n}, c_{k,n}, r_{k,n}} \sum_{n=1}^N \sum_{k=1}^K c_{k,n} r_{k,n}$$

Subject to:

$$\sum_{n=1}^N \sum_{k=1}^K c_{k,n} P_{k,n} \leq P_{total}$$

$$\sum_k c_{k,n} = 1 \text{ for all } n$$

$$c_{k,n} \in \{0,1\}$$


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Problem Formulation


- Minimizing total transmit power for a given data rate and BER

$$\min_{r_{k,n}, P_{k,n}, c_{k,n}} \sum_{n=1}^N \sum_{k=1}^K c_{k,n} P_{k,n}$$

Subject to:

$$\sum_{n=1}^N c_{k,n} r_{k,n} \geq R_k \text{ for all } k$$

$$\sum_k c_{k,n} = 1 \text{ for all } n$$


$$c_{k,n} \in \{0,1\}$$


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Intra- and Inter-cell Adaptation for SISO-OFDM

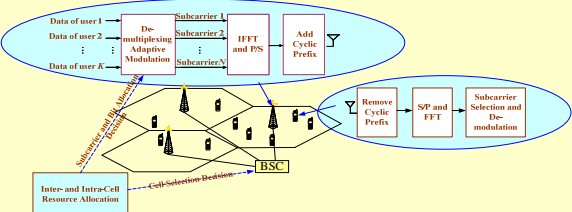
- We have considered SISO-OFDM adaptive resource allocation in a single cell
- What about a multi-cell system?
 - Adaptive cell selection

Y. J. Zhang and K. B. Letaief, "Multiuser adaptive subcarrier-and-bit allocation with adaptive cell selection for OFDM systems," *IEEE Transactions on Wireless Communications*, Sept. 2004.




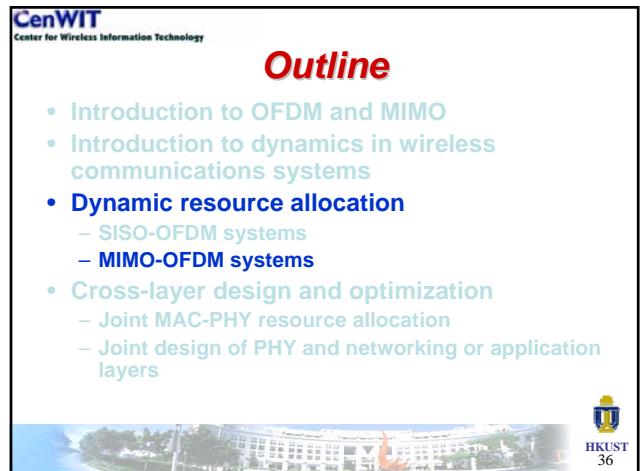
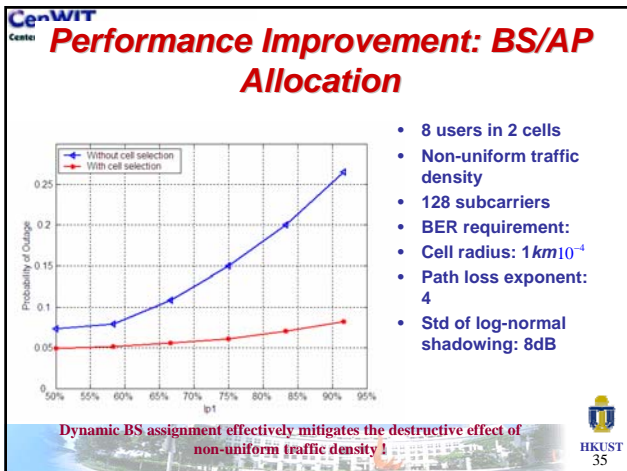
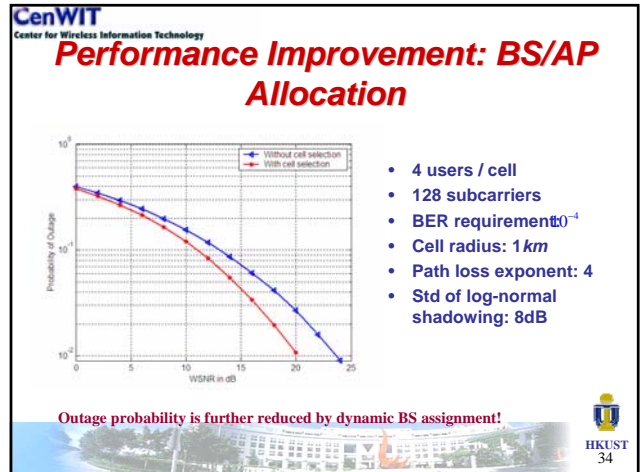
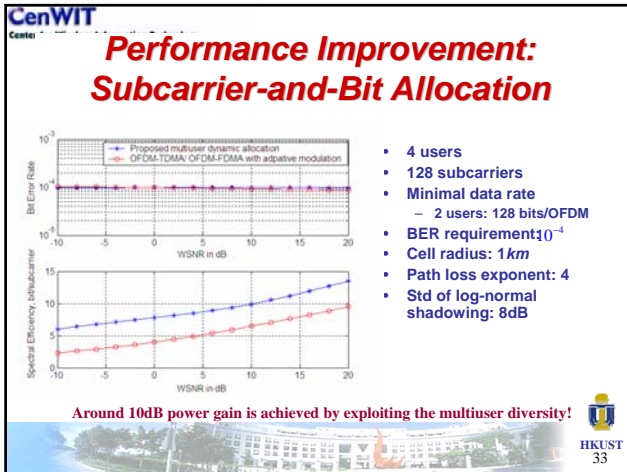
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Intra- and Inter-cell Adaptation for SISO-OFDM



- A mobile is adaptively associated to a cell based on
 - Resource availability in the candidate cells
 - Amount of resources that have already been assigned
 - Amount of resources that is necessary to satisfy the investigated user's QoS
 - Intra-cell adaptation affects the resource occupancy






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Resource Allocation for MIMO-OFDM: Challenges and Opportunities

- Co-channel interference resistance due to MIMO
- Inter-symbol interference resistance due to OFDM
- Time, frequency, and space domain freedom for adaptive resource allocation
- The optimization problem is more complex due to the presence of co-channel interference
- Users can be multiplexed in both frequency and space domains – have to decide which dimension should be occupied by which set of users



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Problem Formulation – Power Minimization

$$\arg \min_{p_{k,n}, r_{k,n}} p_{tot} = \sum_{k=1}^K \sum_{n=1}^N p_{k,n}$$

Subject to:

$$\sum_{n=1}^N r_{k,n} = R_k \quad \forall k$$

$$p_{k,n} \geq 0$$

$$r_{k,n} \geq 0$$


QoS Constraints

$$p_{k,n} = f(BER_{arg}, r_{k,n}, g_{k,n})$$

Nonlinear! Carrier to interference and noise ratio

Combinatorial! $g_{k,n} = g(\{h_{k,n}\}_{k=1,\dots,K}, \{p_{k,n}\}_{k=1,\dots,k-1,k+1,\dots,K})$

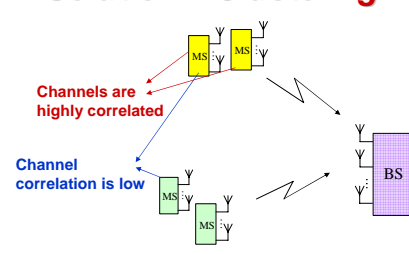
Y. J. Zhang and K. B. Letaief, "An efficient resource allocation scheme for spatial multiuser access in MIMO/OFDM systems," IEEE Transactions on Communications, Jan. 2005



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Solution – Clustering



Channels are highly correlated

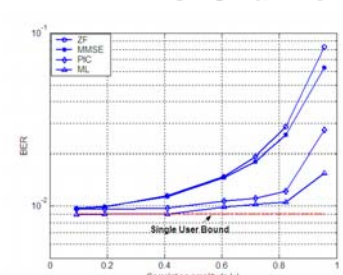
Channel correlation is low



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BER vs. Channel Correlation



- 2 users
- 64 subcarriers
- QPSK Modulation
- Eb/No: 5dB
- 2 Tx/user
- 4 Rx

- BER is affected by CCI
- BER performance degrades when the correlation increases
- When the correlation is low, the performance is similar to that of a single user system



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Solution – Clustering

- Divide users into **clusters** according to the **mutual correlations**
- **Highly correlated** users are put in one cluster
- The channel correlation between users in different clusters is **lower** than a threshold

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Solution – Clustering

- For the users with **low correlation**
 - Assume that the mutual interference is **perfectly cancelled** by **multiuser detection techniques**
 - Users can share the same channels and transmit as if there were **no co-channel users**
 - Adaptive resource allocation reduces to **single-user rate-and-power adaptation**

$$\arg \min_{P_{k,n}, r_{k,n}} \sum_{n=1}^N p_{k,n}$$

$$\sum_{n=1}^N r_{k,n} = R_k$$

$$p_{k,n} = f \left(BER_{target}, r_{k,n}, \left| \frac{h_{k,n}}{\sigma^2} \right|^2 \right)$$

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Solution – Clustering

- For the users with **high mutual correlation**
 - The assumption of **perfect CCI cancellation is not valid**
 - **CCI degrades the performance**
 - Users **DO NOT** share sub-channels to avoid CCI

$$\arg \min_{P_{k,n}, r_{k,n}, c_{k,n}} p_{tot} = \sum_{k=1}^K \sum_{n=1}^N p_{k,n} c_{k,n}$$

$$\sum_{n=1}^N r_{k,n} c_{k,n} = R_k \quad \forall k$$

if $c_{k,n} = 1$, then $c_{k',n} = 0 \quad \forall k' \neq k$ No longer combinatorial!

$$p_{k,n} = f(BER_{target}, r_{k,n}, |h_{k,n}|^2)$$

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Performance

- 2 users
- 64 subcarriers
- 128 bits/OFDM/user
- 2 Tx/user
- 4 Rx
- PIC detector
- Threshold: 0.6


- **Significant performance improvement and diversity gain**
- **No need to sacrifice antenna diversity in the presence multiple users**

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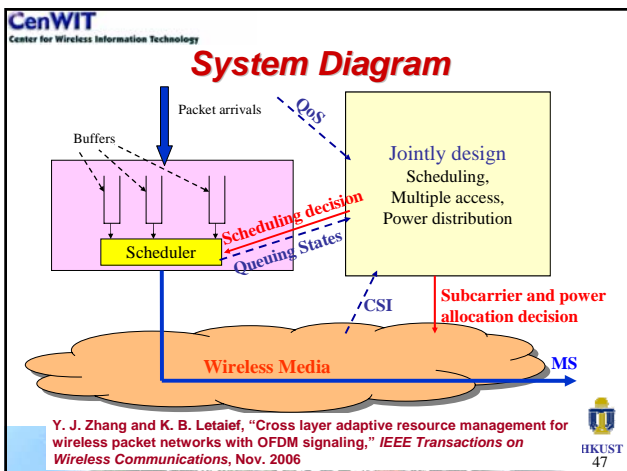
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Challenges and Opportunities

- Opportunistic resource allocation that assumes a **saturated** traffic condition is not accurate in **packet-switched** networks
 - Resource may be allocated to users that do not have enough packets to transmit
- Resource allocation affects the **effective channel capacity** seen by the upper layers, and hence has an impact on scheduling
- Multi-user diversity gain, statistical multiplexing gain, time- and frequency-domain diversity
- Key issue: joint optimization of scheduling and subcarrier-bit-power allocation in OFDM networks



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Constraints – subcarrier allocation

- Allocate subcarriers to the **packets** that are scheduled for transmission
- Allocate subcarriers in a most **power efficient** way

Exclusive subcarrier allocation: $\sum_{k=1}^K c_{k,n} \leq 1 \quad \forall n$

Number of subcarriers needed by one user: $\sum_{n=1}^N c_{k,n} = g_k \frac{L}{r} \quad \forall k$

g_k : the number of packets scheduled for user k
 L : packet size
 r : data rate on each subcarrier



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Constraints – power allocation

- To maintain a sufficiently **low error rate** at the receiver
- To **smooth** the fluctuation in the wireless channel capacity

$$\frac{|h_{k,n}|^2 p_{k,n}}{N_s B} = \gamma_k \quad \forall n, k$$

γ_k : SNR required by user k for achieving a given bit error rate



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Constraints – Scheduling

- To ensure **QoS and fairness** from the MAC's viewpoint
- **Serve packets** in a way that **approximates a fair queueing scheme** in a error-free system (i.e., a reference scheme)
- **Explicitly control the leading or lagging** of the flows compared to the reference scheme

$$|Q_k - Q_k^r| \leq \eta_k \quad \forall k$$

Q_k : queue length of user k
 Q_k^r : queue length of user k in the reference system
 η_k : maximum allowable leading or lagging



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Problem Formulation

$$\arg \min_{p_{k,n}, c_{k,n}, g_k} \sum_{k=1}^K \sum_{n=1}^N p_{k,n} c_{k,n}$$


To maintain the received SNR: $\frac{|h_{k,n}|^2 p_{k,n}}{N_s B} = \gamma_k \quad \forall n, k$

To control leading or lagging: $|Q_k - Q_k^r| \leq \eta_k \quad \forall k$

Exclusive subcarrier allocation: $\sum_{k=1}^K c_{k,n} \leq 1 \quad \forall n$

Number of subcarriers needed by a user: $\sum_{n=1}^N c_{k,n} = g_k \frac{L}{r} \quad \forall k$

Maximum number of packets transmitted during a frame: $\sum_{k=1}^K g_k = \min\left(\sum_{k=1}^K Q_k, \frac{Nr}{L}\right)$




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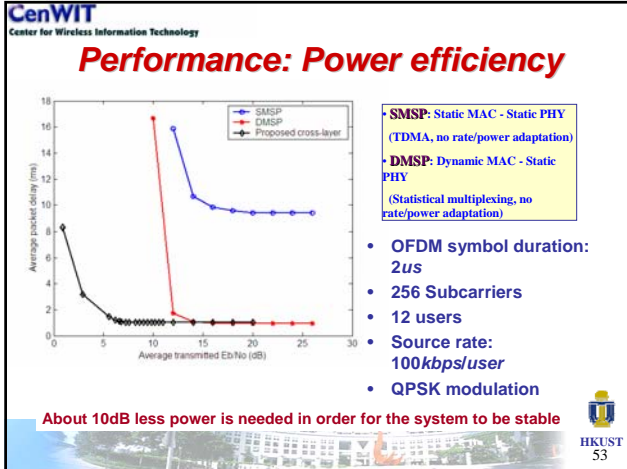
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Performance

- The proposed joint MAC-PHY resource allocation algorithm can achieve
 - **Throughput guarantee**
 - The throughput of the proposed system is **almost the same as** that of a fair queueing system with **error-free channels**
 - **Delay guarantee**
 - The **worst case delay** of the proposed system is **bounded**
 - **Fairness guarantee**
 - **Short-term and long-term fairness** is guaranteed at a similar degree as the reference system
 - **Significantly higher power efficiency**

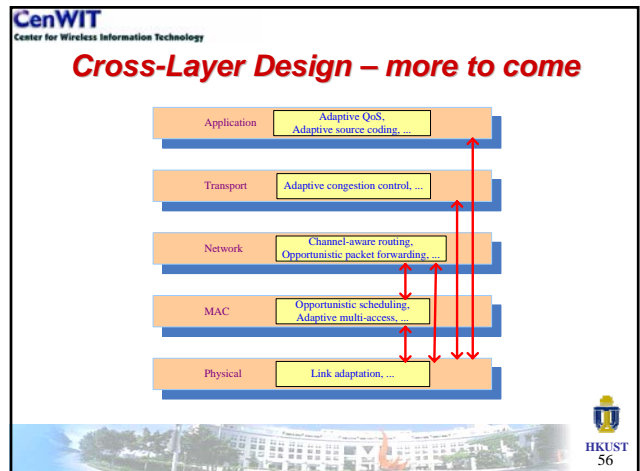


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- ### Outline
- Introduction to OFDM and MIMO
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 - MIMO-OFDM systems
 - **Cross-layer design and optimization**
 - Joint MAC-PHY resource allocation
 - Cross-layer design in wireless networking
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- ### Potential Research Topics
- Joint PHY, MAC, and Networking layer design
 - Joint TCP congestion control and per-link power adaptation
 - Joint routing, scheduling, and power control
 - Adaptive admission control
 - Joint optimization of Transport layer retransmission limit, MAC layer retransmission limit, and PHY layer adaptation
 - Joint PHY and application layer design
 - Co-design of source coding parameters and MAC-PHY layer resource allocation
- HKUST 55



Conclusion

- Dynamic resource allocation and cross-layer design are emerging technologies that are nowadays under active research throughout the world
- This talk gave an overview of dynamic multiuser resource allocation
- It discussed a broad spectrum of important topics, including
 - Issues and principles of resource allocation in single- and multi-antenna OFDM networks, with or without perfect channel state information



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