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This is the accepted version of:

T. Dang, Z. Liu, X.W. Zhou, Y. Sun, P.G. Zhao
Dynamic Response of a Hypersonic Rocket Sled Considering Friction and Wear
Journal of Spacecraft and Rockets, Vol. 59, N. 4, 2022, p. 1289-1303
doi:10.2514/1.A35267

The final publication is available at <https://doi.org/10.2514/1.A35267>

Access to the published version may require subscription.

When citing this work, cite the original published paper.

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<http://hdl.handle.net/11311/1222876>

Dynamic Response of a Hypersonic Rocket Sled considering Friction and Wear

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The dynamic response of a hypersonic rocket sled was studied by considering the time-varying friction coefficient and the gap caused by wear between the slipper and track. A multi-body dynamic model for a hypersonic rocket sled system was established by considering the time-varying mass and moment of inertia, nonlinear aerodynamic loads, engine thrust, track irregularity, and nonlinear contact force. As for the wear calculation, the ductile and shear criteria were used as the material damage criteria, and slipper wear was determined by the number of damaged elements. A rocket sled test was also carried out, and the dynamic response of the sled was measured. The results showed that the computational sliding displacement and velocity of the third-stage sled matched well with the test values. The computational root mean square (RMS) values of the vertical acceleration of the third-stage sled front slipper considering friction and wear matched better with the test values than with the case without considering friction and wear, which underestimated the RMS value by approximately 20.1% at Mach 5. The importance of considering friction and wear and the correctness of the computational method were

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28 validated. It is also found that the kinetic friction coefficient decreased with an increase in
29 the product of the pressure and velocity. The wear height of the slipper increased almost
30 linearly with the sliding displacement. The test results showed that the vertical acceleration
31 power spectral density of the third-stage sled front slipper increased with time in the full
32 frequency band below 2000 Hz. This study will guide the design and optimisation of
33 hypersonic rocket sleds.

34 Nomenclature

35	A	=	slipper-track contact area
36	a	=	acceleration
37	b	=	directionally dependent material parameter in ductile fracture curve
38	c	=	damping constant
39	D	=	aerodynamic drag
40	$DMAX$	=	maximum penetration depth
41	e	=	exponent in L-N contact force formula
42	F_n	=	slipper-track normal contact force
43	F_t	=	slipper-track tangential contact force (frictional force)
44	f	=	material parameter in shear fracture curve
45	G	=	gravity
46	g	=	current penetration depth
47	H	=	length of the third-stage sled
48	h	=	wear height
49	J	=	moment of inertia
50	K	=	contact stiffness
51	k_s	=	material parameter in shear fracture curve
52	L	=	aerodynamic lift
53	l	=	step size of backward differentiation formula
54	M	=	mass matrix

55	m	=	mass
56	Ma	=	Mach number
57	M_p	=	aerodynamic pitch moment
58	n	=	normal unit vector
59	n_{\perp}	=	tangential unit vector
60	P	=	normal pressure
61	PV value	=	product of normal pressure and sliding velocity
62	\mathbf{q}	=	generalised coordinates
63	s	=	displacement
64	T	=	engine thrust
65	t	=	time
66	Δt	=	time step
67	t_1	=	moment when the first-stage sled separates
68	t_2	=	moment when the second-stage sled separates
69	t_{total}	=	total time
70	\mathbf{v}	=	velocity
71	w	=	wear rate
72	β	=	attitude angle
73	γ	=	second order derivative term in dynamic equations
74	ε_D	=	ductile strain
75	ε_D^{**}	=	equivalent fracture strain at ductile fracture
76	ε_S	=	shear strain
77	ε_S^{**}	=	equivalent fracture strain at shear fracture
78	$\varepsilon_S^+ / \varepsilon_S^-$	=	equivalent plastic strain in equibiaxial tension/compression at shear fracture
79	$\varepsilon_T^+ / \varepsilon_T^-$	=	equivalent plastic strain in equibiaxial tension/compression at ductile fracture
80	η	=	stress triaxiality

81	η^+ / η^-	=	stress triaxiality in equibiaxial tension/compression at ductile fracture
82	θ	=	shear stress parameter
83	θ^+ / θ^-	=	shear stress parameter for equibiaxial tension/compression
84	λ	=	Lagrange multiplier
85	μ	=	kinetic friction coefficient
86	ϕ	=	ratio of maximum shear stress to equivalent stress
87	φ	=	coefficient of backward differentiation formula
88	Φ_q	=	Jacobian matrix
89	ψ	=	coefficient of backward differentiation formula
90			
91	<i>Subscripts</i>		
92			
93	x, y, z	=	sliding direction, vertical direction, lateral direction
94			

I. Introduction

96 A hypersonic rocket sled is a large, high-precision ground-test equipment mainly used to solve a series of test
 97 problems associated with aerodynamics, structure, control, fuse, engine ignition, and damage encountered by aircraft
 98 at high speeds and in large-overload environments [1–7]. In a hypersonic rocket sled test, a solid rocket engine is
 99 used as the power source to push the rocket sled along a high-precision straight track at a hypersonic speed.
 100 Simultaneously, the performance parameters of the test products fixed on the sled are tested and analysed using
 101 various electronic equipment. Rocket sled systems are widely used in performance tests and reliability assessments
 102 of hypersonic vehicles because their carrying capacity, moving velocity, acceleration, and environment are easy to
 103 control, and it is easy to observe and collect test data.

104 A monorail rocket sled is one of the widely used forms of hypersonic rocket sleds. Compared to a duo-rail rocket
 105 sled, a monorail rocket sled has much less mass and aerodynamic drag, making it easier to accelerate. However, at
 106 the same time, the vibration acceleration of a monorail rocket sled is greater, the stability is poorer, and the
 107 mechanical environment is worse. The sled experiences track irregularities, large dynamic loads caused by
 108 continuous slipper-track collisions, powerful shock waves, and engine thrust oscillations. These factors cause severe

109 vibration of the rocket sled system and cause its moving environment to deteriorate sharply [8]. When reaching a
110 hypersonic speed, even a small excitation will cause the rocket sled to vibrate strongly and significantly affect its
111 motion stability. The instability of a rocket sled may result in the failure of the slipper or a track shear fracture and
112 lead to test failure. The dynamic response of a rocket sled directly affects the test environment of the tested product
113 and determines the accuracy and reliability of the test results. Therefore, it is necessary to establish an accurate
114 rocket sled system dynamic model and to analyse its dynamic response.

115 Some studies have been conducted on the dynamic response of rocket sleds. The earlier methods for predicting
116 the dynamic response of rocket sleds include the empirical coefficient λ method and the sled impact parameter
117 method. Thereafter, some scholars used the finite element method (FEM) to carry out structural response analysis of
118 rocket sleds [9–11]. However, these methods only studied the dynamic response of a rocket sled at a certain speed.
119 In fact, the dynamic characteristics of a rocket sled system vary with the mass, gap between the slipper and track,
120 aerodynamic loads, and thrust. For instance, the fuel consumption will result in a continuous and significant mass
121 reduction for a few seconds and induce a difference in the dynamic response of the rocket sled. Therefore, it is
122 necessary to study the dynamic response of rocket sleds over the entire test period. Generally, the multi-body
123 dynamics method is often used to study the dynamics of the entire test period. According to the initial conditions
124 and boundary conditions of a system, the dynamic differential equations of the system can be solved using this
125 method, and various nonlinear factors can be considered. For a hypersonic rocket sled, its nonlinear factors include
126 aerodynamics, boundary conditions, and slipper–track contact. First, a rocket sled runs from low to hypersonic
127 speeds. In contrast to free flight, the aerodynamic coefficient of a rocket sled changes with velocity owing to the
128 influence of the ground effect and other factors and results in the nonlinear aerodynamic characteristics of the sled.
129 Second, a rocket sled runs along a track with a time-varying gap height between the slipper and track which
130 introduces nonlinearity into the boundary condition. The height of the gap depends on the local track irregularities.
131 In addition, because there is no lubrication between the slipper and the track, it leads to a dry sliding friction
132 phenomenon. Combined with the large impact force generated at high speed and with large loads, the slipper and
133 track undergo very serious wear damage [12], thus increasing the slipper–track gap. These two reasons lead to the
134 discontinuity and nonlinearity of the boundary conditions between the slipper and the track. Third, there are
135 intermittent collisions between the slipper and track during the movement of a rocket sled that introduce nonlinearity
136 into the contact. The normal contact force is a strong nonlinear force related to deformation. In addition, the friction

137 coefficient of the material surface changes with the sliding velocity after a large number of experiments [13].
138 Therefore, the tangential contact force also exhibits nonlinear characteristics with a change in the friction coefficient
139 between the slipper and the track.

140 In summary, the dynamic response of a hypersonic rocket sled is a highly nonlinear dynamic response of a time-
141 varying system. The time-varying and nonlinear factors of the system must be considered to improve the accuracy of
142 research results. Hoose [14-15] considered track irregularity and slipper-track contact force in a study of rocket sled
143 dynamics but did not consider the aerodynamic load on the rocket sled or the influence of slipper-track friction and
144 wear. Wang [16] established a sled-track coupling dynamic model by considering the track irregularities,
145 aerodynamic load, slipper-track contact force, and time-varying characteristics. The acceleration, velocity,
146 displacement, and contact force of the rocket sled system were obtained by numerical calculations, but the influence
147 of slipper-track friction and wear was not considered. Zhang [17] established a multi-body dynamic model of a
148 rocket sled system, considered track irregularities and aerodynamic drag, and analysed the model using the co-
149 simulation method. However, the effects of aerodynamic lift, aerodynamic moment, time-varying mass, friction, and
150 wear were not considered. Gu [18] established a simplified dynamic model of a duo-rail rocket sled system and
151 solved the dynamic equations by considering track irregularities. However, they did not consider the aerodynamic
152 load, time-varying mass, or the influence of friction and wear. In summary, some nonlinear factors have been
153 considered in the study of rocket sled dynamics, but the contact nonlinearity caused by friction and the boundary
154 nonlinearity caused by wear have not been considered. Friction and wear are very important factors for accurately
155 predicting the dynamic response of rocket sleds, because the frictional force affects the prediction of the sliding
156 displacement and sliding velocity of the rocket sled, and the wear of the slipper leads to a change in the slipper-track
157 gap and significantly influences the vertical and lateral acceleration of a rocket sled [19].

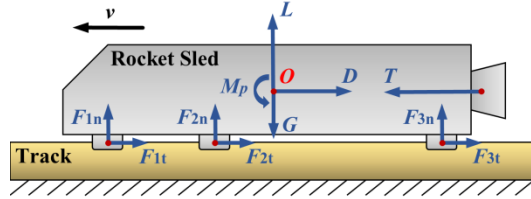
158 Therefore, the influence of slipper-track friction and wear is considered in this dynamic study. A multi-body
159 dynamics research method for a hypersonic rocket sled system combined with friction and wear analysis was
160 established, and the feasibility of the method was verified by comparing the computational results with the rocket
161 sled test results. The time-varying and nonlinear dynamic responses of the hypersonic rocket sled considering
162 friction and wear were obtained and may benefit the design of hypersonic rocket sled systems.

163

II. Theoretical method

A. Dynamic equations of rocket sled system

164 The forces and constraints of the monorail hypersonic rocket sled system are shown in Fig. 1. The gravity G ,
 165 aerodynamic lift L , aerodynamic drag D , and aerodynamic pitching moment M_p act on the centre of mass of the
 166 rocket sled when it slides along the track at velocity v . Thrust T is applied to the engine at the rear of the rocket sled.
 167 Three slippers were connected to the rocket sled shell with a fixed joint and were affected by the contact force of the
 168 track, including the normal contact force F_{jn} and the frictional force F_{jt} ($j = 1, 2, 3$). The lower surface of the track
 169 was fixed. As shown in Fig. 1, all the forces and moments on the rocket sled varied with time. Owing to fuel
 170 consumption, the mass m and the moment of inertia J of the rocket sled were also functions of time t .
 171



172

173

Fig. 1 Forces and constraints of rocket sled system

174 The Lagrange multiplier method was used to establish dynamic equations according to the force and constraint
 175 conditions of the rocket sled system. The Lagrange multiplier method is a relative coordinate method; compared
 176 with the Cartesian method, it uses fewer equations. The established dynamic equations are index-3 differential
 177 algebraic equations expressed as

$$178 \begin{pmatrix} \mathbf{M}(\mathbf{q}, t) & \Phi_q^T(\mathbf{q}, t) \\ \Phi_q(\mathbf{q}, t) & 0 \end{pmatrix} \begin{pmatrix} \ddot{\mathbf{q}} \\ \lambda \end{pmatrix} = \begin{pmatrix} \mathbf{F}(\mathbf{q}, \dot{\mathbf{q}}, t) \\ \gamma(\mathbf{q}, \dot{\mathbf{q}}, t) \end{pmatrix}, \quad (1)$$

179 where \mathbf{M} is the mass matrix, Φ_q is the Jacobian matrix of the constraint equations, $\ddot{\mathbf{q}}$ is the acceleration, $\dot{\mathbf{q}}$ is the
 180 velocity, \mathbf{q} is the generalised coordinates, λ is the Lagrange multiplier, \mathbf{F} is the applied force, and γ is the
 181 second-order derivative term in the acceleration equations.

182 The system is completely constrained, and the constraint equation is

$$183 \Phi(\mathbf{q}, t) = 0. \quad (2)$$

184 The Jacobian matrix Φ_q of the constraint equation was obtained by solving the partial differential of the
 185 constraint equation with respect to the generalised coordinates \mathbf{q} as

186
$$\Phi_q(\mathbf{q}, t) = \frac{\partial \Phi(\mathbf{q}, t)}{\partial \mathbf{q}}. \quad (3)$$

187 The velocity constraint equation was obtained by taking the total differential of Equation (2) with respect to time
188 t as

189
$$\Phi_q(\mathbf{q}, t)\dot{\mathbf{q}} + \Phi_t(\mathbf{q}, t) = 0. \quad (4)$$

190 The acceleration constraint equation was obtained by taking the total differential of Equation (4) with respect to
191 time t as

192
$$\Phi_q\ddot{\mathbf{q}} + (\Phi_q\dot{\mathbf{q}})_q\dot{\mathbf{q}} + 2\Phi_{qt}\dot{\mathbf{q}} + \Phi_{tt} = 0. \quad (5)$$

193 The expression of γ obtained from Equation (5) is

194
$$\gamma = -(\Phi_q\dot{\mathbf{q}})_q\dot{\mathbf{q}} - 2\Phi_{qt}\dot{\mathbf{q}} - \Phi_{tt}. \quad (6)$$

195 The rocket sled system was dominated by the collision contact process. The slide and collision contact between
196 the slipper and track affected each other during the movement of the rocket sled, and the contact load varied with
197 time and the attitude angle of the rocket sled. Therefore, this is a typical dynamic contact problem. Because the
198 slipper–track contact force directly affected the dynamics, friction, and wear characteristics of the rocket sled, it was
199 necessary to establish a reasonable slipper–track contact model. For the slipper–track normal contact force, the L-N
200 nonlinear contact force model was adopted [20]. Compared with the linear contact and Hertz contact models, this
201 model is more suitable for high-speed collision contact problems [21]. The L-N nonlinear contact force model
202 divides the normal contact force F_n into elastic force and damping force as

203
$$F_n = \max[Kg^e + \text{step}(g, DMAX)c\dot{g}, 0]\mathbf{n}, \quad (7)$$

204 where \mathbf{n} is the normal unit vector, K is the contact stiffness, g is the current amount of penetration, \dot{g} is the current
205 relative penetration velocity, e is the exponent, c is the damping constant, $DMAX$ is the maximum penetration depth
206 at which the damping force is scaled to $c\dot{g}$ with a cubic step function, and $\text{step}(g, DMAX)$ is a cubic step function
207 that smoothly increases the damping constant from zero to c as the penetration increases from zero to $DMAX$.

208 According to Equation (7), normal contact force is a strong nonlinear force depending on the amount of
209 penetration. In the L-N nonlinear contact force model, when the amount of penetration g reaches the maximum
210 penetration depth $DMAX$, the two components begin to separate. In a specific rocket sled dynamics computation,

211 each contact parameter can be calculated using the FEM [16]. The slipper–track tangential contact force (frictional
 212 force) \mathbf{F}_t is expressed as

$$213 \quad \mathbf{F}_t = F_n \mu \mathbf{n}_\perp, \quad (8)$$

214 where \mathbf{n}_\perp is the tangential unit vector and μ is the kinetic friction coefficient.

215 **B. Friction and wear theory**

216 The stress field of the slipper and track contact was studied in the FEM analysis of the slipper–track friction and
 217 wear. There are three main methods of study: displacement, force, and mixed methods. Among them, the
 218 displacement method has a clear relationship between the basic variables and is convenient for matrix calculations
 219 [22]. Therefore, the displacement method was chosen to study the stress field.

220 In friction and wear theory, the general parameters used to evaluate the performance of friction and wear are the
 221 wear height h , wear rate w , and PV value. The wear height h is used to reflect the wear amount, and the wear rate w
 222 is defined as the ratio of the wear height h to the sliding displacement s_x [23]. Because the slipper–track normal
 223 pressure P and the sliding velocity v_x constitute the independent variables in the calculation of friction and wear, the
 224 PV value is defined as the product of the two. The normal pressure P is the ratio of the normal contact force F_n to the
 225 slipper–track contact area A .

226 It is necessary to select the material failure criteria to determine whether the material is worn. Ductile and shear
 227 criteria can be used for fracture ductile metals. Ductile fracture is caused by the nucleation and aggregation of
 228 microstructural cavities, while shear fracture is caused by the movement of a shear zone. Because measuring
 229 fracture strain under different stress triaxialities requires many experiments, to avoid this, Hooputra [24] proposed
 230 failure models of ductile fracture and shear fracture. For ductile fracture, the relationship between the equivalent
 231 fracture strain ε_D^{**} and stress triaxiality η is

$$232 \quad \varepsilon_D^{**} = \frac{\varepsilon_T^+ \sinh[b(\eta^- - \eta)] + \varepsilon_T^- \sinh[b(\eta - \eta^+)]}{\sinh[b(\eta^- - \eta^+)]}, \quad (9)$$

233 where ε_T^+ and ε_T^- are the equivalent plastic strain in equibiaxial tension and compression at ductile fracture,
 234 respectively; η^+ and η^- are the stress triaxiality in equibiaxial tension and compression at ductile fracture,
 235 respectively; and b is the directionally dependent material parameter in the ductile fracture curve.

236 When Equation (10) is established, ductile fracture begins to occur.

$$237 \int_0^{\varepsilon_D^{**}} \frac{d\varepsilon_D}{\varepsilon_D^{**}(\eta)} = 1 \quad (10)$$

238 For shear fracture, the shear stress parameter θ is defined as

$$239 \theta = \frac{1 - k_s \eta}{\phi}, \quad (11)$$

240 where k_s is the material parameter in the shear fracture curve, and ϕ is the ratio of the maximum shear stress to
 241 the equivalent stress. Then, the relationship between the equivalent fracture strain ε_s^{**} and the shear stress
 242 parameter θ is

$$243 \varepsilon_s^{**} = \frac{\varepsilon_s^+ \sinh[f(\theta - \theta^-)] + \varepsilon_s^- \sinh[f(\theta^+ - \theta)]}{\sinh[f(\theta^+ - \theta^-)]}, \quad (12)$$

244 where ε_s^+ and ε_s^- are the equivalent plastic strain in equibiaxial tension and compression at shear fracture,
 245 respectively; f is the material parameter in the shear fracture curve; and θ^+ and θ^- are the shear stress parameters
 246 for equibiaxial tension and compression, respectively.

$$247 \begin{aligned} \theta^+ &= 2 - 4k_s \\ \theta^- &= 2 + 4k_s \end{aligned} \quad (13)$$

248 When Equation (14) is established, shear fracture begins to occur.

$$249 \int_0^{\varepsilon_s^{**}} \frac{d\varepsilon_s}{\varepsilon_s^{**}(\theta)} = 1 \quad (14)$$

250 According to the above material failure criteria, it can be determined whether the slipper material has ductile or
 251 shear fracture through the FEM calculation, and then the slipper wear can be determined.

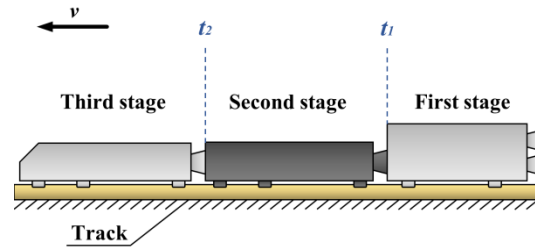
252 **III. Computational method**

253 **A. Dynamics analysis method**

254 *1. Dynamic model*

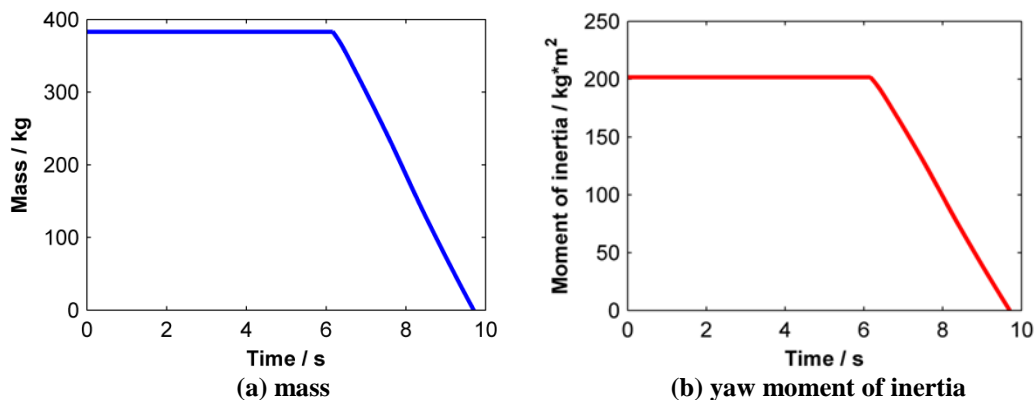
255 The first step of the multi-body dynamics computation of a rocket sled system is to establish the model of the
 256 rocket sled and track. The monorail rocket sled used in this test adopted a three-stage tandem propulsion as shown in
 257 Fig. 2. During the movement of the rocket sled, the second-stage sled engine worked at t_1 after the first-stage sled

258 engine finishes working, and then the first-stage sled separated. Similarly, the third-stage sled engine worked at t_2
 259 after the second-stage sled engine finished working, and then the second-stage sled separated. The third-stage sled
 260 finally reached hypersonic speed, which was the simulation object.

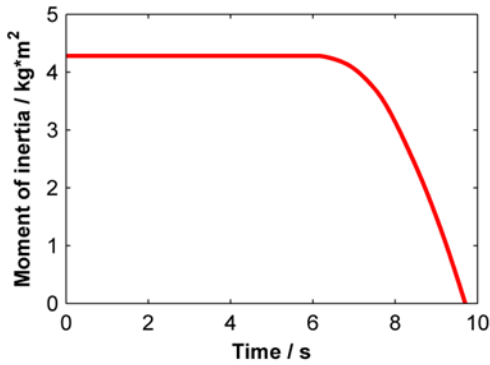


261
 262 **Fig. 2 Three-stage rocket sled**

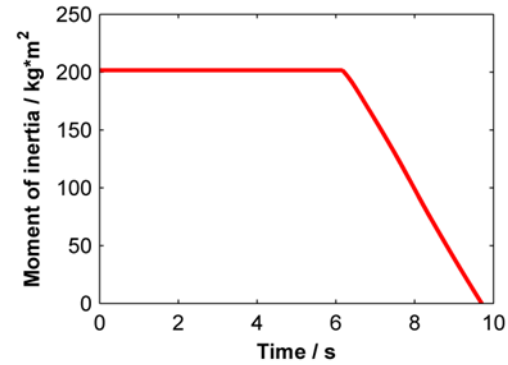
263 The third-stage sled contained a sled body and propellant. The sled body contained the shell, internal structure,
 264 test product, engine, electronic equipment, and three slippers. The test product was integrated into the third-stage
 265 sled. The initial mass of the third-stage sled was 894 kg. The time-varying curve of the mass characteristics of the
 266 third-stage sled propellant was obtained according to the factory parameters of the solid rocket engine as shown in
 267 Fig. 3. Since the propellant was of a rotating shape and burnt from the inside out, the yaw moment of inertia curve
 268 was the same as the pitch moment of inertia curve. It was found that the reduction rates of mass, yaw moment of
 269 inertia, and pitch moment of inertia remained constant after $t_2 = 6.166$ s, while the roll moment of inertia showed
 270 nonlinear time-varying characteristics. The initial propellant mass in the third-stage sled accounted for
 271 approximately 42.8% of the total mass and lost within 9.475 s, indicating that the rocket sled system had strong
 272 time-varying mass characteristics.



273
 274



(c) roll moment of inertia



(d) pitch moment of inertia

Fig. 3 Time-varying mass characteristics of propellant

275
276

277

278 Track irregularity is one of the main factors causing the vibration of a rocket sled; therefore, the vertical
279 irregularity was measured by an optical method. Considering the measurement error, the original information
280 obtained from the measurement was detrended to obtain the vertical track spectrum as shown in Fig. 4. Because the
281 computational method mainly focused on the vertical track spectrum, the lateral track spectrum was not established,
282 and the subsequent analysis was limited to the vertical direction.

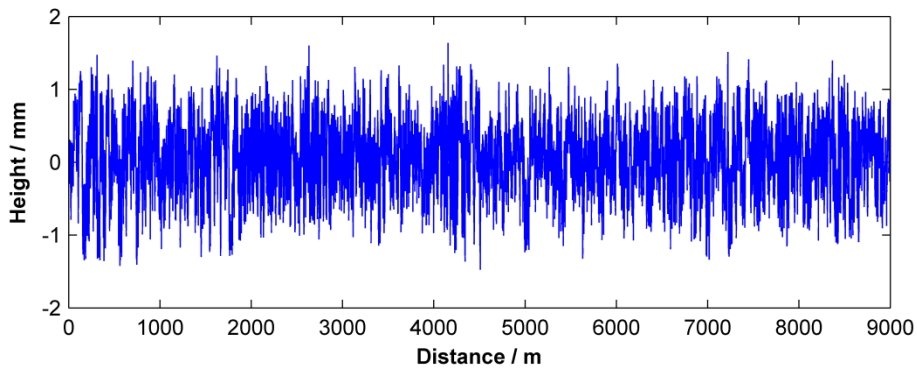
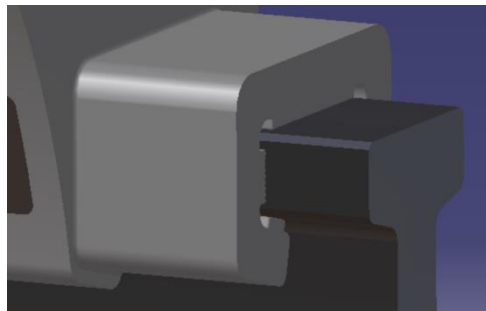


Fig. 4 Vertical track spectrum

283

284

285 According to the vertical track spectrum shown in Fig. 4, a track model with irregularities was established. The
286 third-stage sled model was assembled using the track model shown in Fig. 5. An initial 1.9-mm gap was found
287 between the slipper and the track, and the gap varied with the local track spectrum.



288

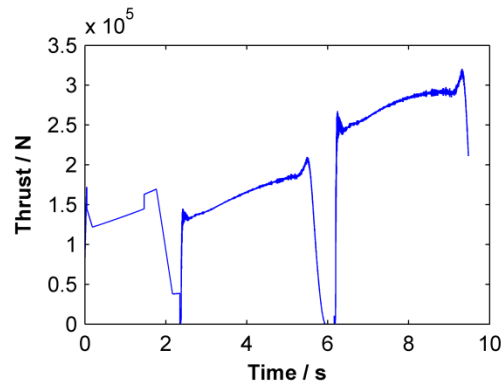
289

Fig. 5 Assembly of slipper and track

290 2. Sled loads

291 The second step of the multi-body dynamics computation of the rocket sled system was to calculate the load
292 characteristics, including the thrust for the entire period and the aerodynamic load at different velocities, and use
293 them as the input conditions for the dynamics computation. In the process of the multi-body dynamics computation
294 of the rocket sled system, the position and direction of thrust and aerodynamic loads are shown in Fig. 1. The
295 eccentricities of thrust and aerodynamic drag were not considered.

296 As for the thrust calculation, because the research object was the third-stage sled, the thrust curve after time t_2 of
297 the third-stage sled engine provided by the factory was used directly. The force of the second-stage sled on the third-
298 stage sled was used as the equivalent thrust curve before time t_2 . The calculated third-stage sled thrust curve for the
299 entire time period is shown in Fig. 6. It was found that the ignition times of the second and third stages were $t_1 =$
300 2.379 s and $t_2 = 6.166$ s, respectively, and the thrust oscillation phenomenon existed in the rocket sled engines.



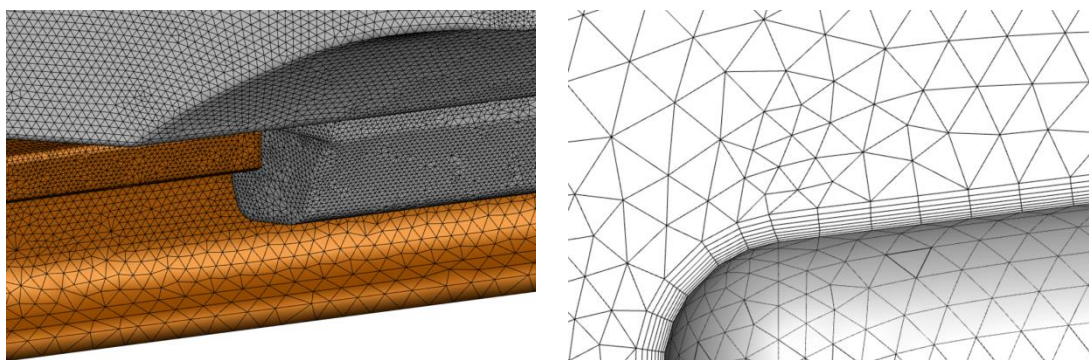
301

302

Fig. 6 Thrust curve

303 The aerodynamic loads of the third-stage sled were obtained using the computational fluid dynamics method.
304 The steady aerodynamic loads of the third-stage sled under different Ma were calculated, and the aerodynamic loads
305 at other velocities were obtained by piecewise interpolation and used as the input conditions for the multi-body
306 dynamics computation of the rocket sled system. During the dynamics analysis, the sliding velocity v_x of the third-
307 stage sled was solved at each time step to obtain the corresponding aerodynamic loads at that time step. Owing to
308 the small gap between the slipper and the track, the attitude angle β of the rocket sled was limited to a very small
309 range; therefore, the angle of attack and angle of sideslip of the rocket sled were not considered in the aerodynamic
310 calculation. Accordingly, only lift L , drag D , and pitch moment M_p were considered as aerodynamic loads.

311 For the aerodynamic calculation of the third-stage sled, steady three-dimensional compressible viscous Navier–
312 Stokes equations were adopted as the governing equations. The spatial difference format was the Roe format [25],
313 and the non-physical solution was modified using the entropy method. The Roe format is one of the most successful
314 upwind formats in practical applications because of its excellent viscous resolution and shock wave discontinuous
315 resolution. The lower-upper symmetric Gauss – Seidel (LU-SGS) implicit time stepping format [26] was used,
316 which has the characteristics of small computation requirements and good robustness. The turbulence was solved
317 using the Reynolds-averaged Navier–Stokes method, and the two-equation realised $k-\varepsilon$ turbulence model was used.
318 The length of the third-stage sled was denoted as H , and the flow field was set as a cuboid, with a length, width, and
319 height of $10H$, $5H$, and $5H$, respectively. The inlet and far field of the flow field were set as far-field boundaries.
320 The outlet was set as a supersonic outlet boundary. And the sled was set as a non-slip adiabatic wall. The track and
321 the ground were set as translational walls, whose translational speed was consistent with the incoming flow speed.
322 Considering the ground effect and symmetry of the structure, the 1/2 flow field grid model was established as shown
323 in Fig. 7.



324
325 (a) Local grid

324
325 (b) Boundary-layer grid

326 **Fig. 7 Flow field grid model**

327 The aerodynamic load curves of the third-stage sled after the calculation are shown in Fig. 8. The centre of the
328 pitch moment M_p was the centre of mass of the third-stage sled. When the pitch moment M_p was positive, it was a
329 pitch-down moment. As can be seen, the lift L , drag D , and pitch moment M_p were not proportional to Ma^2 within
330 the range of $Ma = 0-6$, indicating that the aerodynamic coefficients constantly varied with velocity, thus reflecting
331 the nonlinear aerodynamic characteristics of the rocket sled.

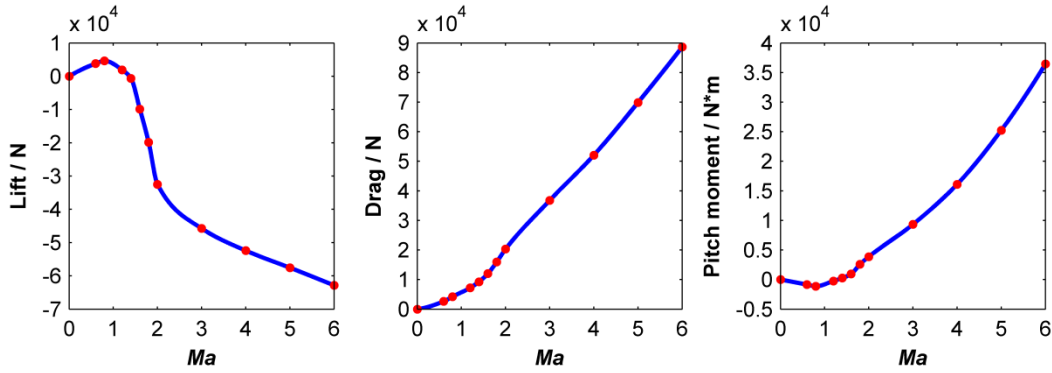
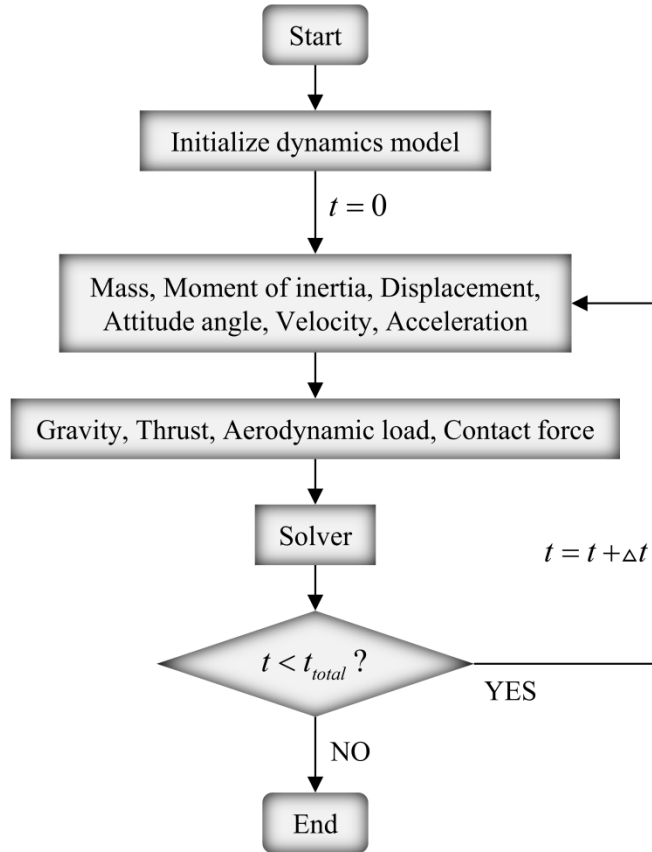


Fig. 8 Aerodynamic load curves

3. Dynamics analysis method

First, a multi-body dynamics simulation of a hypersonic rocket sled system was carried out without considering friction and wear. The computational process is illustrated in Fig. 9. The time-varying propellant mass curves, thrust curve, and aerodynamic load curves were introduced to obtain the mass matrix \mathbf{M} , engine thrust \mathbf{T} , and aerodynamic loads at different time steps when initialising the dynamic model. To solve the contact force, the local track spectrum heights and slopes of the three slippers were obtained according to the sliding displacement s_x of the third-stage sled. It was then determined whether the three slippers were in contact with the track, so the vertical displacements s_y , lateral displacements s_z , and attitude angles β of the three slippers were calculated. If there was no contact, there was no contact force at this time step; if there was contact, then the current penetration depth g was obtained. The current relative penetration velocity \dot{g} was obtained according to the local track spectrum slope, vertical velocity v_y , and lateral velocity v_z of the slipper. According to Equations (7) and (8), the slipper-track normal contact force F_n and frictional force F_t were obtained, in which the kinetic friction coefficient $\mu = 0.2$ was defined.



347 **Fig. 9 Dynamics computational process without considering friction and wear**

348 The multi-body dynamics calculation of the rocket sled system was based on the commercial software LMS
 349 Virtual.Lab Motion. To solve the dynamic equations, a sparse matrix was used to improve the operation speed. The
 350 integration algorithm used was the backward differentiation formula (BDF) [27], which is an implicit multi-step
 351 integration algorithm with variable order and variable step size. The advantage of the BDF is that it is inherently
 352 stable for stiff systems. The ordinary differential equations in multi-body dynamics are second-order, and the basic
 353 form is

$$354 \quad \ddot{\mathbf{q}} = f(\mathbf{q}, \dot{\mathbf{q}}, t). \quad (15)$$

355 The BDF method was used to iteratively solve Equation (15) so that the equation converged at each time step.
 356 The iteration format was

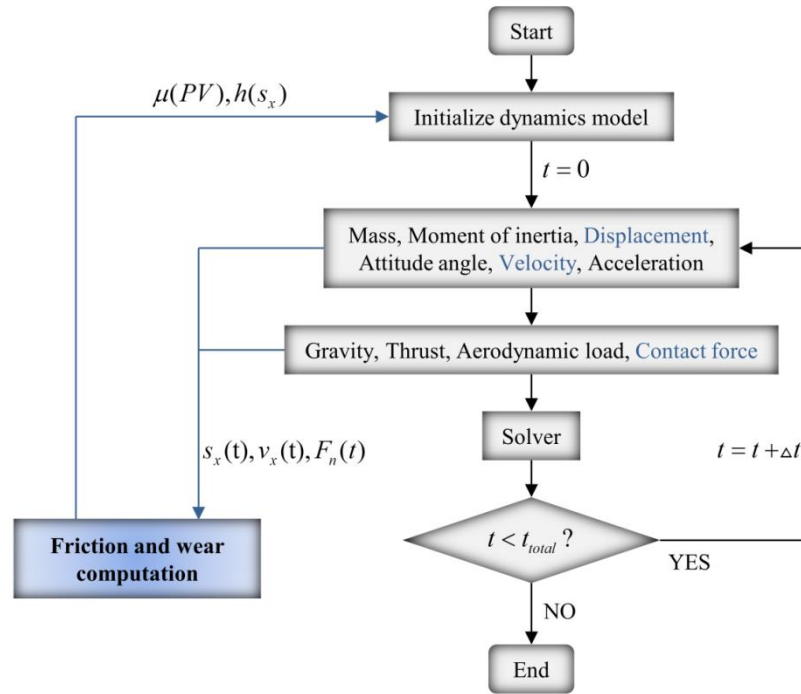
$$357 \quad \begin{cases} \mathbf{q}_{n+1} = l\varphi_k \dot{\mathbf{q}}_{n+1} + \sum_{i=1-k}^0 \psi_i \mathbf{q}_{n+i} \\ \dot{\mathbf{q}}_{n+1} = l\varphi_k f_{n+1} + \sum_{i=1-k}^0 \psi_i \dot{\mathbf{q}}_{n+i} \end{cases}, \quad (16)$$

359 where ψ_i and φ_k are the coefficients, and l is the step size. For rigid ordinary differential equations, the range of k
 360 was $1 \leq k \leq 6$, and the resolution of the k -step method was of the order k . In Equation (16), velocity and f_{n+1} must
 361 be predicted. f_{n+1} is a function of the velocity and generalised coordinate at time $n + 1$.

$$362 \quad f_{n+1} = f_{n+1}(\mathbf{q}_{n+1}, \dot{\mathbf{q}}_{n+1}) \quad (17)$$

363 For the calculation of acceleration, the matrix was simplified to a banded matrix as much as possible, and the
 364 matrix was factored to reduce the operation time. The total calculation time t_{total} was 9.475 s and defined as the
 365 maximum time of the thrust curve.

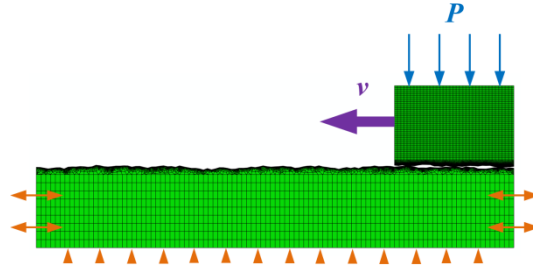
366 A multi-body dynamics simulation considering the friction and wear of the hypersonic rocket sled system was
 367 also carried out. The computational process was illustrated in Fig. 10. According to the case without considering
 368 friction and wear, the sliding displacement $s_x(t)$, sliding velocity $v_x(t)$, and slipper-track normal contact force $F_n(t)$
 369 over the entire time period were output as the input conditions for the friction and wear computation. Then, the
 370 kinetic friction coefficient $\mu(PV)$ curve and the wear height $h(s_x)$ curve were output as the input conditions for the
 371 dynamics computation considering friction and wear. The wear height h of the slipper increased with an increase in
 372 the sliding displacement s_x . However, it was unrealistic to change the shape of the slipper at each time step in the
 373 rocket sled dynamics computation. In fact, the continuous wear of the slipper was reflected in the rocket sled
 374 dynamics as the gap between the slipper and track increased. Therefore, although the shape of the slipper was not
 375 adjusted during the modelling, the shape of the track was adjusted to make the slipper-track gap at each point on the
 376 track reflect the wear height of the slipper at that point. Because the size of the gap was very small relative to the
 377 slipper and track, this equivalent method was reasonable. Therefore, the track was remodelled by combining the
 378 vertical track spectrum and the wear height $h(s_x)$ curve in the dynamic analysis considering friction and wear. In
 379 contrast to the computational process shown in Fig. 9, the kinetic friction coefficient $\mu(PV)$ curve and the worn-track
 380 model needed to be imported during the initialisation of the computational process shown in Fig. 10. To calculate
 381 the slipper-track frictional force F_t , the normal pressure P was obtained by dividing the normal contact force F_n by
 382 the contact area $A = 0.02 \text{ m}^2$. The kinetic friction coefficient μ corresponding to the normal pressure P and the
 383 sliding velocity v_x was obtained according to the kinetic friction coefficient $\mu(PV)$ curve, and the slipper-track
 384 frictional force F_t was obtained according to Equation (8).



385
386 **Fig. 10 Dynamics computation process considering friction and wear**

387 **B. Friction and wear computation**

388 The kinetic friction coefficient was computed using the method presented in Ref. [28]. First, the actual surface
 389 roughness of the slipper and track was measured, and the W-M function method [29] was used to establish a rough
 390 surface profile. The W-M function method has a clear parameter meaning and high accuracy and is widely used. A
 391 finite element model with a rough surface was created based on the rough surface profile as shown in Fig. 11. The
 392 left and right ends of the track were set as symmetric constraints to simulate an infinite-length track, and the lower
 393 surface of the track was set as a fixed constraint. According to the sliding velocity $v_x(t)$ and normal contact force
 394 $F_n(t)$ obtained from the rocket sled dynamics computation, normal pressure P was applied to the upper surface of the
 395 slipper, and the sliding velocity v_x was applied to the slipper. The contact mode between the slipper and track was
 396 set as hard contact and frictionless. The materials of the slipper and track were 18Ni(300) steel and U71Mn steel,
 397 respectively, and their material properties are listed in Table 1. Because the slipper-track collision model is a high-
 398 speed collision model, the Johnson-Cook constitutive model was used for computation.



399
400 **Fig. 11 Slipper–track finite element model with rough surface**

401
402 **Table 1 Slipper–track material properties**

403

Parameter	Slipper	Track
Density / $\text{kg}\cdot\text{m}^{-3}$	8000	7920
Elastic modulus / GPa	190	210
Poisson ratio	0.283	0.3

404
405 Because the slipper and track contact intermittently, there may be no slipper–track contact at the time of a certain
406 sliding velocity v_x ; that is, the normal pressure $P(v_x) = 0$ at that time. Therefore, the root mean square (RMS) values
407 of the non-zero normal pressure P in a small range around each sliding velocity v_x were used to calculate the kinetic
408 friction coefficient under multiple groups of PV values. The shear stress and normal stress of the contact nodes were
409 extracted from the computational results and divided by each other to obtain the kinetic friction coefficients μ under
410 multiple groups of PV values. The kinetic friction coefficient $\mu(PV)$ curve was fitted with multiple groups of data.
411 Then, the $\mu(PV)$ curve was used as the input condition for the multi-body dynamics computation of the rocket sled
412 system considering friction and wear.

413 In related studies, the friction between the slipper and track was considered to be similar to the collision of small
414 particles. Therefore, a slipper–track microscopic sub-model of the finite element was established, and a single
415 micro-convex was used to represent the roughness of the entire track as shown in Fig. 12. The slipper and track were
416 set to be deformable bodies, and they deformed plastically after contact. All the degrees of freedom at the lower
417 surface of the track were constrained, and the left and right ends of the track were set as symmetric constraints. The
418 initial velocity condition was loaded on each node of the slipper to prevent grid distortion. The subsequent velocity
419 boundary conditions were applied to the upper and right surfaces of the slipper to make the slipper deformable.
420 Because the normal pressure P corresponds to the sliding velocity v_x , the load was not applied to the upper surface
421 of the slipper. Instead, the vertical and rotational degrees of freedom on the upper surface of the slipper were set to
422 zero, and the sliding velocity v_x was used to replace the PV value to carry out multiple groups of wear computations.

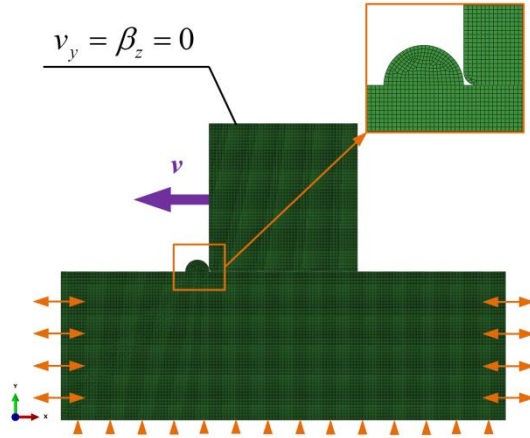
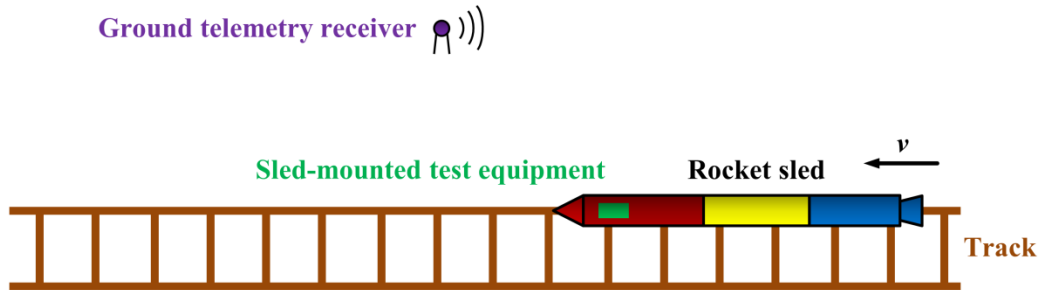


Fig. 12 Slipper-track microscopic sub-model

Both the slipper and track were worn during the wear computation. However, the track after wear did not affect the motion of the rocket sled; therefore, the wear computation only focused on the slipper. Combined with the element stress generated by computation and the failure criteria shown in Equations (9)–(14), the number of slipper failure elements at the computational sliding velocity v_x was determined. By counting the number of failure elements at each computational sliding velocity v_x , the wear rate w at each computational sliding velocity v_x was obtained. Combined with the relationship between the sliding displacement $s_x(t)$ and the sliding velocity $v_x(t)$ obtained from the rocket sled dynamics computation, the wear rate w of each computational sliding displacement s_x was obtained, and the wear rate $w(s_x)$ curve was obtained through interpolation. By integrating the wear rate $w(s_x)$ before each sliding displacement s_x , the wear height $h(s_x)$ curve of the slipper was obtained. The wear height $h(s_x)$ curve was superimposed with the vertical track spectrum, and then the track model including the track spectrum considering wear was established. The newly established track model was the input condition for the multi-body dynamics computation of the rocket sled system considering friction and wear.

IV. Hypersonic rocket sled test

A hypersonic rocket sled test was carried out to verify the computational method of the hypersonic rocket sled dynamic response considering friction and wear. The test system was mainly composed of a rocket sled, track, sled-mounted test equipment, and ground test equipment as shown in Fig. 13. The sled-mounted test equipment was installed inside the sled, including the acceleration sensor, storage system, power system, telemetry equipment, and synchronous trigger. The ground test equipment mainly included a ground telemetry receiver, velocity radar, and photoelectric theodolite.



Velocity radar

Photoelectric theodolite

Fig. 13 Rocket sled test system

444

445

446 The photoelectric theodolite is a high-precision measuring device with a tracking function that can realise
 447 automatic tracking and high-speed photography of a rocket sled. The velocity of the rocket sled was measured using
 448 velocity radar. An acceleration sensor was installed at the front slipper of the third-stage sled to collect the vibration
 449 acceleration signal. For the poor mechanical environment of a hypersonic rocket sled, a small lightweight
 450 acceleration sensor with a strong impact resistance and high temperature resistance was selected, and a static and
 451 dynamic calibration was performed to ensure test accuracy. The sensor signal was transmitted to the sled-mounted
 452 storage system via a cable, and the sled-mounted telemetry equipment transformed the electrical signal into a
 453 telemetry signal. The ground telemetry receiver received the wireless telemetry signal and transformed it into an
 454 electrical signal in a specified format for real-time display and storage. The test data was instantly transmitted
 455 through the telemetry system.

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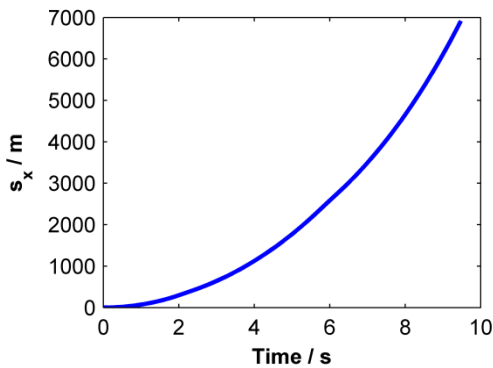
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The test used a three-stage tandem-propulsion monorail rocket sled, which was consistent with the computation. When the rocket sled was launched, the trigger signal was generated by the sled-mounted synchronous trigger because of the movement of the rocket sled. The transistor-transistor logic signal was output synchronously to the storage system and telemetry system to ensure that the time zero of each sled-mounted system was unified. When the rocket sled moved along the track, each test system collected the data. The test results revealed that the maximum Mach number of the third-stage sled was 5.2. The ground test equipment recorded the sliding displacement and sliding velocity of the third-stage sled over the entire period. The ground telemetry receiver collected the vibration acceleration data before 7.575 s, but the data after 7.575 s were not collected.

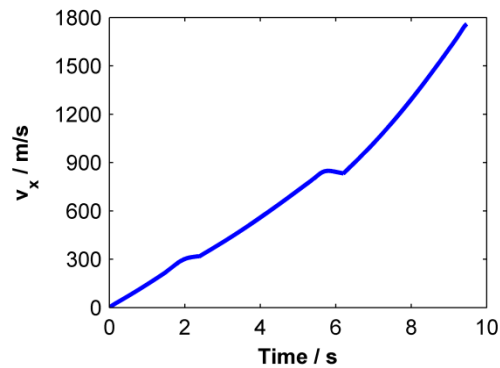
V. Results and analysis

465 A. Friction and wear analysis

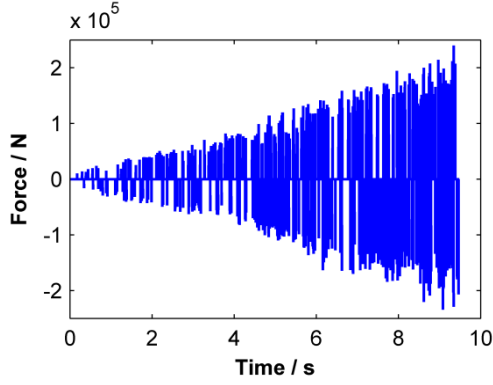
466 Based on the multi-body dynamics computation of the rocket sled system without considering friction and wear,
 467 the sliding displacement $s_x(t)$, sliding velocity $v_x(t)$, and front slipper-track normal contact force $F_n(t)$ of the third-
 468 stage sled over the entire time period were obtained. The normal pressure P under different sliding velocities was
 469 obtained by combining the front slipper-track normal contact force $F_n(t)$ and sliding velocity $v_x(t)$ as shown in Fig.
 470 14. The maximum sliding displacement of the rocket sled was 6916 m, the maximum sliding velocity of the rocket
 471 sled was 1760 m/s, and the maximum slipper-track normal contact force was 2.4×10^5 N during $t_{total} = 9.475$ s. As
 472 shown in Fig. 14(c), the slipper-track normal contact force changed dramatically over the entire period. A positive
 473 value indicates that a slipper was in contact with the upper surface of the track and thus was subjected to a vertical
 474 upward force. The negative value indicates that a slipper was in contact with the lower surface of the track and thus
 475 was subjected to a vertical downward force. The occurrence ratio of positive and negative values was 1.036
 476 according to statistics, and they appeared alternately, indicating that the slipper and track collided back and forth in
 477 the vertical direction. As shown in Fig. 14(d), the RMS value of the normal pressure P and the sliding velocity v_x
 478 showed a clear positive correlation. The RMS value of the normal pressure P reached a maximum value of 11.954
 479 MPa at Mach 5.



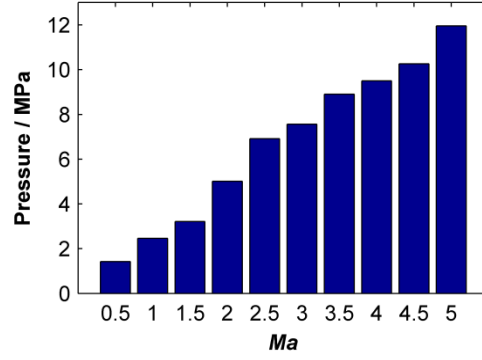
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481 (a) sliding displacement vs. time



(b) sliding velocity vs. time



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483 (c) slipper-track normal contact force vs. time

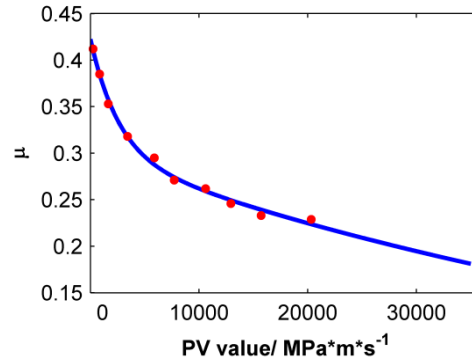


484 (d) normal pressure vs. sliding velocity

485 **Fig. 14 Input conditions for friction and wear computation**

486 Under normal pressure P and sliding velocity v_x shown in Fig. 14(d), kinetic friction coefficient computations
487 were carried out to obtain 10 groups of kinetic friction coefficient μ under PV values, which were then fitted into the
488 kinetic friction coefficient $\mu(PV)$ curve shown in Fig. 15. The fitting function was

$$\mu(PV) = 0.1231e^{-0.0003889PV} + 0.2994e^{-0.00001435PV} . \quad (18)$$



489
490 **Fig. 15 Kinetic friction coefficient curve**

491 As shown in Fig. 15 and Equation (18), the kinetic friction coefficient μ decreased with an increase in the PV
492 value, and the rate of decrease was high at the beginning and then lowered. Because the kinetic friction coefficient μ
493 changed nonlinearly with the PV value, the frictional force between the slipper and the track showed contact
494 nonlinearity. The wear was calculated at 10 different velocities as shown in Fig. 14(d). The slipper stress
495 distributions at $Ma = 1, 3,$ and 5 are shown in Fig. 16. By comparing the stress distribution at the three velocities, it
496 was found that the stress generated by the slipper increased, and the stress concentration area decreased with an
497 increase in velocity. This is because the stress became more difficult to transfer to other interior areas in a timely
498 manner as the velocity increased, resulting in a stress concentration in the contact area of the slipper and the track
499 micro-convex.

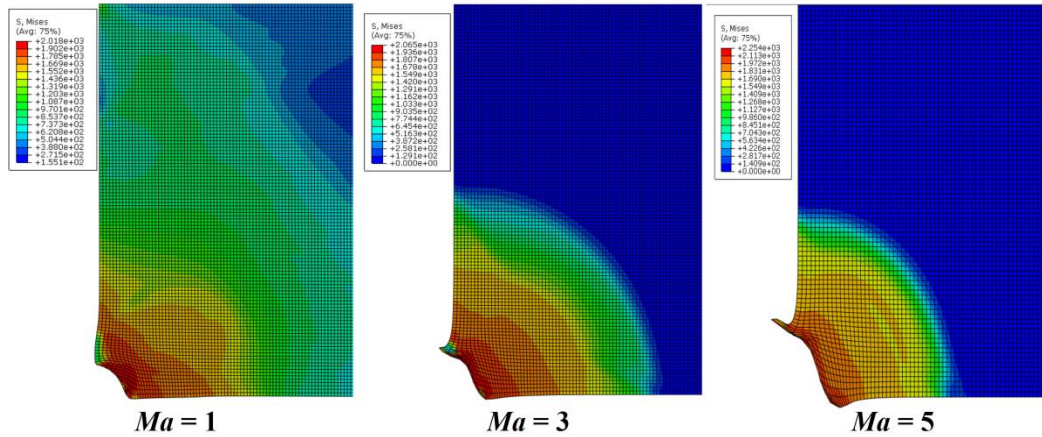


Fig. 16 Slipper stress distribution

In combination with the stress distribution of each working condition and the material failure criteria, the wear rate w of the sliding velocity v_x under each working condition was obtained as shown in Fig. 17. The wear rate w increased with an increase in sliding velocity v_x in the Mach ranges 0.5–2 and 2.5–5. However, the wear rate decreased in the Mach range 2–2.5 because the principal strain rate increased by one order of magnitude within this PV value range, leading to a decrease in the number of elements judged as failure.

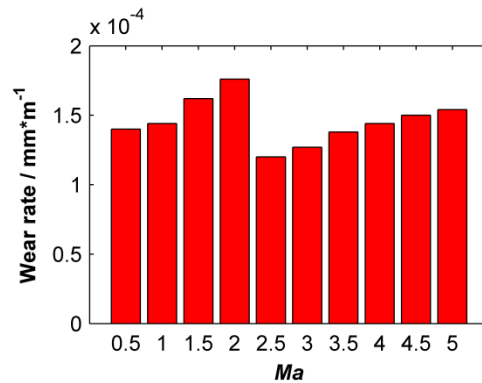
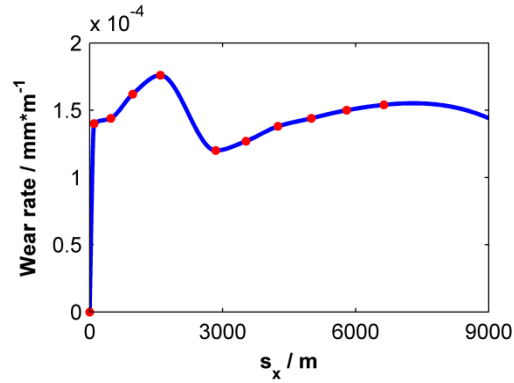


Fig. 17 Slipper wear rate vs. sliding velocity

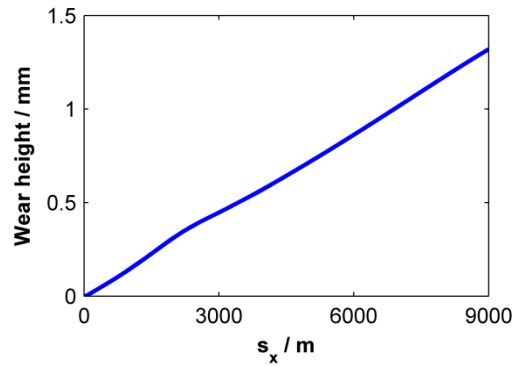
According to the wear rate $w(v_x)$ of the above sliding velocities, combined with the relationship between the sliding displacement $s_x(t)$ and the sliding velocity $v_x(t)$ in Fig. 14(a) and 14(b), the wear rate w of each computational sliding displacement s_x was obtained. The wear rate $w(s_x)$ curve was obtained through interpolation as shown in Fig. 18. The wear rate $w(s_x)$ was integrated along the sliding displacement s_x to obtain the wear height $h(s_x)$ curve of the slipper as shown in Fig. 19. The wear height h increased almost linearly with the sliding displacement s_x . The maximum sliding displacement obtained by computation was 6916 m, and the corresponding wear height was 0.9875 mm. The above wear height $h(s_x)$ curve was superimposed with the vertical track spectrum in Fig. 4 to obtain the vertical track spectrum considering wear as shown in Fig. 20, and a track model considering wear was

517 established based on the track spectrum. Because the new track model considered the irregularity and wear, the
518 boundary conditions of the rocket sled slipper at different track positions were different and demonstrated the
519 boundary nonlinearity of the hypersonic rocket sled dynamics.



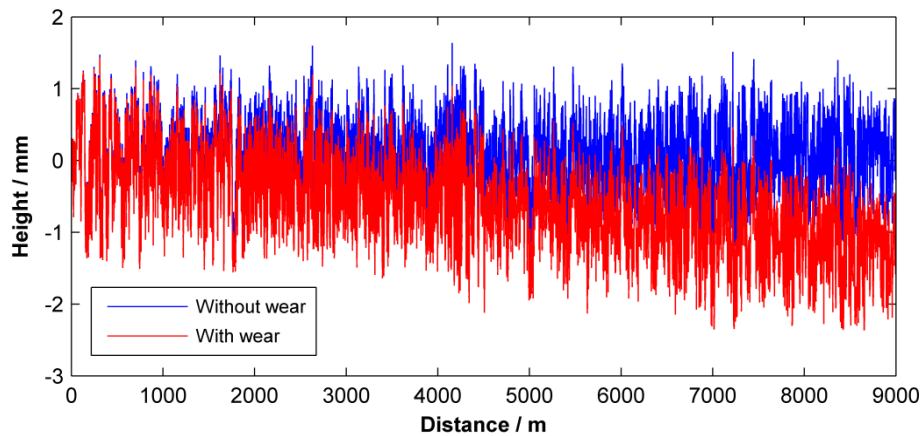
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Fig. 18 Slipper wear rate vs. sliding displacement



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Fig. 19 Slipper wear height vs. sliding displacement

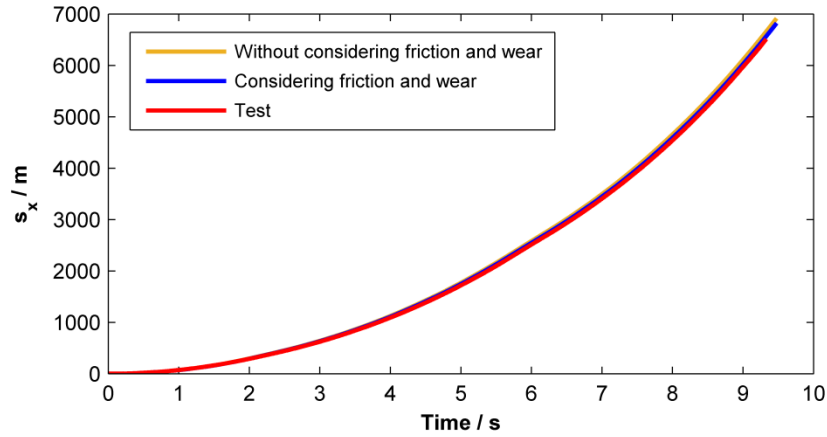


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Fig. 20 Vertical track spectrum considering wear

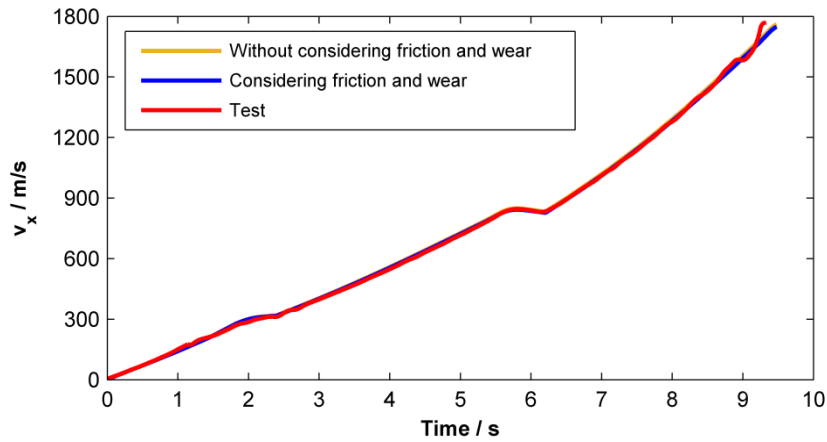
526 **B. Dynamic response analysis**

527 The sliding displacement s_x and sliding velocity v_x curves of the rocket sled over the entire computation and
528 testing period are shown in Fig. 21. The curves of sliding displacement s_x and sliding velocity v_x obtained by
529 computation matched well with the test values, which confirmed the effectiveness of the computational method in
530 the prediction of sliding displacement and velocity. The time at which the third-stage sled reached the maximum
531 sliding velocity was called the total time. After that, the rocket sled gradually slowed down without thrust until it left
532 the end of the track. The total time and maximum values of the sliding displacement and velocity are listed in Table
533 2. It can be seen from the table that the total test time was 9.328 s, while the total computation time was 9.475 s,
534 with an error of 1.6%. For the sliding displacement, the computational value was larger than the test value. The error
535 between the maximum sliding displacement of the test and the value of the dynamics computation considering
536 friction and wear was 4.7%, and the error between the maximum sliding displacement of the test and the value of the
537 dynamic computation without considering friction and wear was 6.2%. The computational value of the sliding
538 velocity was smaller than that of the test value. The error between the test maximum sliding velocity and that of the
539 dynamic computation considering friction and wear was 1.2%, and the error between the test maximum sliding
540 velocity and that of the dynamic computation without considering friction and wear was 0.6%. As shown in Fig.
541 21(b), the computation accurately predicted the velocity changes of the rocket sled during the separation of each
542 stage but failed to predict the abnormal velocity changes of the third-stage sled within a short time before the
543 maximum velocity. This abnormal change in velocity may have been caused by the abnormal combustion of the
544 propellant at this time. In addition, the sliding velocity and displacement without considering friction and wear were
545 slightly larger than those considering friction and wear. This is because in the dynamics computation without
546 considering friction and wear, the kinetic friction coefficient was defined as $\mu = 0.2$, which was smaller than the
547 kinetic friction coefficient considering friction and wear at most times. Because the frictional resistance was smaller,
548 the rocket sled moved faster and farther. However, the frictional force was too small compared with the thrust, and
549 the slipper was not in contact with the track at all times; therefore, the sliding displacement and velocity of the two
550 computations were similar. This indicates that within the acceptable error range, it is reasonable to consider dynamic
551 computational results without considering friction and wear as the input to perform friction and wear computations,
552 even if there is a small deviation between the input and the dynamic results considering friction and wear.



553
554

(a) Sliding displacement



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(b) Sliding velocity

557 **Fig. 21 Sliding displacement and velocity of test and computation**

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Table 2 Total time and maximum values of sliding displacement and velocity

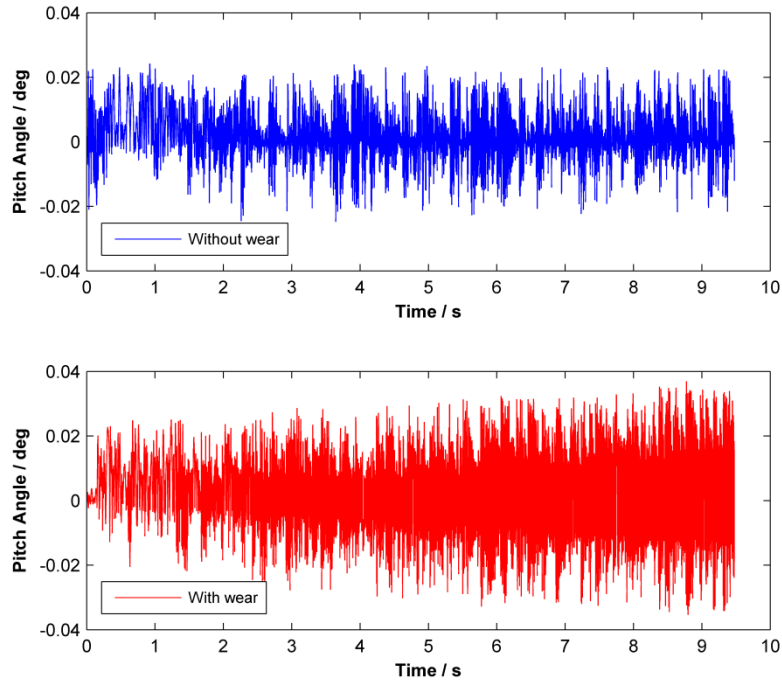
	Without considering friction and wear	Considering friction and wear	Test
Total time / s	9.475	9.475	9.328
Maximum sliding displacement / m	6916	6821	6512
Maximum sliding velocity / m*s ⁻¹	1760	1748	1770

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Figure 22 shows the curve of the third-stage sled pitch angle β_z over the entire computation period. In the previous analysis, the third-stage sled was mostly subjected to a pitch-down moment. However, Figure 22 shows that the pitch angle of the rocket sled oscillated around 0° without a clear pitch-down phenomenon, indicating that the aerodynamic moment of the third-stage sled was not sufficient to overcome the larger slipper-track contact force.

566 In the case of considering friction and wear, the amplitude of the pitch angle increased with time owing to the time-
567 varying gap between the slipper and track. In addition, the frequency of the pitch angle fluctuation was higher than
568 that without considering friction and wear. This indicates that wear had a significant influence on the attitude angle
569 of the rocket sled. However, the maximum pitch angle of the rocket sled was less than 0.04° . Therefore, it is
570 reasonable to ignore the influence of the angle of attack on the aerodynamic computation.



571
572 **Fig. 22 Pitch angle**
573 The vertical vibration acceleration a_y of the front slipper of the third-stage sled over the entire period is shown in
574 Fig. 23, in which the test data was collected before 7.575 s. The results show that the vertical vibration acceleration
575 of the front slipper was distributed almost symmetrically along the x-axis and changed dramatically. The maximum
576 value reached 360 g, indicating a poor rocket sled dynamic environment. The rocket sled was affected by track
577 irregularity, shock wave impact, oscillating engine thrust, and time-varying mass characteristics; therefore, its
578 stability was poor. Once the rocket sled was unstable, a large slipper-track collision occurred, resulting in a large
579 acceleration. As shown in Fig. 23, large vibration accelerations occur occasionally, and this phenomenon occurs
580 more often at high speeds. This indicates that the slipper-track collision frequency was higher at high speeds than at
581 low speeds, which was consistent with the slipper-track contact frequency shown in Fig. 14(c).

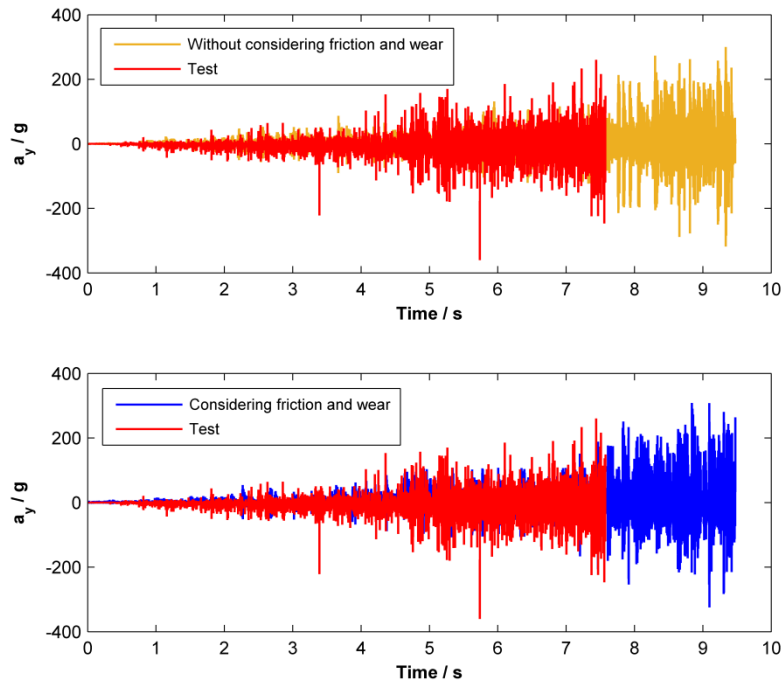


Fig. 23 Vertical acceleration

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The vertical vibration acceleration of the front slipper was analysed in the time domain. To obtain the internal relationship between the vertical acceleration a_y and the sliding velocity v_x , the RMS values of the vertical acceleration in a small range under different sliding velocities were extracted as shown in Fig. 24. It was found that the RMS value of the vertical acceleration of the front slipper increased almost linearly with the sliding velocity. Compared with the computational values without considering friction and wear, the RMS values of the vertical acceleration considering friction and wear matched better with the test values, confirming the need to consider friction and wear in the hypersonic rocket sled dynamics computation. There was no significant difference between the computational results with and without considering friction and wear at low speeds, during which only a small amount of wear was generated. However, at high speeds above 800 m/s, owing to increasing wear, the RMS values of the computational vertical acceleration without considering friction and wear were smaller and different from the test values, while the computational results considering friction and wear were closer to the test values. When the sliding velocity of the rocket sled reached 1700 m/s, the RMS value of the computational vertical acceleration considering friction and wear was 78.4 g, whereas it was only 65.3 g when friction and wear were not considered. The case without considering friction and wear underestimated the RMS value by approximately 20.1%.

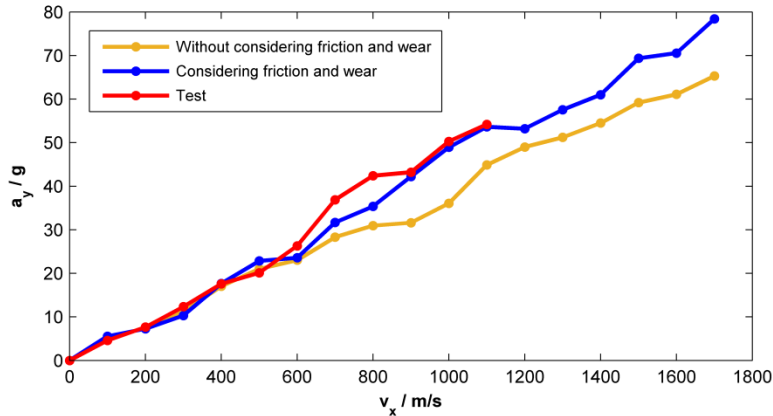


Fig. 24 RMS value of vertical acceleration vs. sliding velocity

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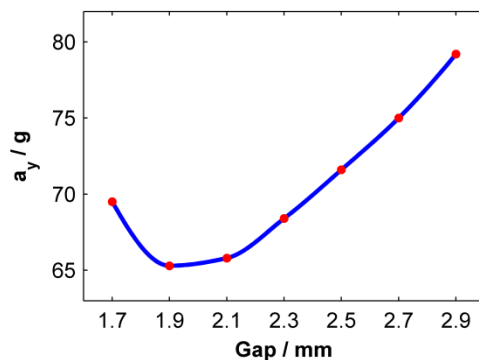
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From the above analysis, it was shown that wear had a significant influence on the vertical vibration acceleration of the front slipper. In fact, the change in the wear height in the dynamic computation of the rocket sled was reflected by the change in the slipper–track gap. Therefore, a dynamic study of the rocket sled under different slipper–track gaps was conducted. The rocket sled dynamic computational method without considering friction and wear was adopted to simulate seven working conditions, and the vertical slipper–track gap size was different under different working conditions. Figure 25 shows the RMS values of the vertical vibration acceleration of the front slipper under each working condition at Mach 5. It was found that the RMS value of the vertical vibration acceleration of the front slipper initially decreased and then increased with an increase in the slipper–track gap within the calculated range, and the acceleration reached a minimum when the slipper–track gap was 1.9 mm. The initial slipper–track gap used in the rocket sled test was 1.9 mm; therefore, the vertical acceleration of the rocket sled dynamics computation considering friction and wear was larger than that without considering friction and wear.



611

612

Fig. 25 RMS value of vertical acceleration vs. gap between slipper and track

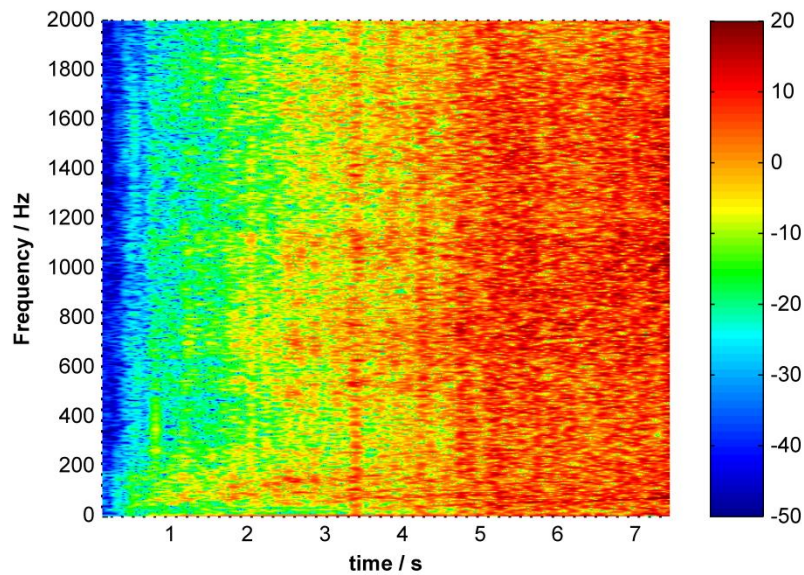
613

614

As shown in Fig. 25, the best gap height existed when the vertical acceleration of the front slipper was the smallest. On the one hand, the vertical distance that the slipper can accelerate increases with an increase in the

615 slipper–track gap; therefore, the slipper–track collision force increases and enhances vibration. On the other hand,
616 the influence of track irregularity on the movement of the slipper increases with a decrease in the slipper–track gap
617 and also enhances vibration. The above analysis provides ideas for the design and optimisation of an initial slipper–
618 track gap. There is an optimal initial slipper–track gap that can minimise the vibration magnitude of the rocket sled
619 slipper at the maximum sliding velocity after wear to reduce vibration. However, the constraint condition of the
620 optimal design is the minimum value of the initial slipper–track gap used to prevent the slipper from getting stuck on
621 the track during movement.

622 To further analyse the dynamic response of the rocket sled in the frequency domain, time–frequency analysis
623 was carried out on the vertical vibration acceleration test data of the third-stage sled front slipper. As shown in Fig.
624 26, the acceleration power spectral density (PSD) of the third-stage sled front slipper was analysed and expressed in
625 decibels. In general, the vertical acceleration PSD of the front slipper increased with time in the full frequency band.
626 Before 2.5 s, the vibration energy of the front slipper was mainly concentrated in the low-frequency range below
627 200 Hz. However, the vibration energy was distributed in the full frequency band at a high speed. This is because
628 the average slipper–track impact force is large in the high-speed stage of a rocket sled, and the impact form is a
629 high-frequency impact, resulting in large vibration acceleration in the full frequency band. However, the average
630 slipper–track impact force is small in the low-speed stage of a rocket sled, and the impact form is a low-frequency
631 impact; thus, the vibration acceleration data largely reflects the response of the third-stage sled within the first
632 several natural frequencies below 200 Hz. In addition, as shown in Fig. 26, the energy of vibration acceleration in
633 the full frequency band was large at $t = 3.4$ s and corresponded to the large slipper–track impact at $t = 3.4$ s as shown
634 in Fig. 23. Therefore, it is reasonable to infer that the vibration acceleration energy in the full frequency band below
635 2000 Hz increases when the third-stage sled front slipper is subjected to a large impact.



636
637 **Fig. 26 Time–frequency characteristics of vertical acceleration test values**

638 **VI. Conclusion**

639 In this study, considering the variation in the slipper–track kinetic friction coefficient and the variation in the
640 slipper–track gap caused by wear, a multi-body dynamic computational method for time-varying and nonlinear
641 hypersonic rocket sled system was established, and a hypersonic rocket sled test was carried out. The sliding
642 displacement and sliding velocity of a third-stage sled predicted by the above computational method matched well
643 with the test values. The computational RMS values of the vertical acceleration of the third-stage sled front slipper
644 considering friction and wear matched better with the test values than the case omitting consideration. This confirms
645 the effectiveness of the proposed computational method.

646 The friction and wear computational results showed that the kinetic friction coefficient decreased with an
647 increase in the *PV* value, and the rate of decrease was high at the beginning and then decreased. The wear height of
648 the slipper increased almost linearly with the sliding displacement of the third-stage sled. The dynamic
649 computational results show that friction and wear had a significant effect on the pitch angle of the third-stage sled.
650 The maximum vertical acceleration of the front slipper reached 360 *g*, and its RMS value increased almost linearly
651 with the sliding velocity. The test results show that the vertical acceleration PSD of the third-stage sled front slipper
652 increased with time in the full frequency band below 2000 Hz. The wear of the slipper in the dynamics computation
653 was reflected by the change in the slipper–track gap. The RMS value of the vertical acceleration of the front slipper

654 decreased initially and then increased with an increase in the slipper-track gap, which provides useful information
655 for the design and optimisation of the initial slipper-track gap of a rocket sled system.

656 In conclusion, friction and wear should be considered in the dynamic analysis of a hypersonic rocket sled
657 system. Because of the limitations of computing resources, the rocket sled system was regarded as a rigid body in
658 this study. Further studies will be carried out to discretize the rocket sled system and strike a balance between
659 excessive computation and high precision. In addition, only the mechanical wear of the slipper was considered in
660 this study; melt wear will be considered in subsequent work.

661 **Funding Sources**

662 This work was supported by the National Natural Science Foundation of China (grant numbers u20b2002),
663 Project B18040, and the K. C. Wong Education Foundation.

664 **Acknowledgments**

665 The work was supported by HPC Platform of Xi'an Jiaotong University.

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