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## <sup>1</sup> Effect of Charge Regulation and Conformational Equilibria in the <sup>2</sup> Stretching Properties of Weak Polyelectrolytes

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ABSTRACT: Weak polyelectrolytes can modulate their charge in response to external perturbations, such as changes in the 9 pH, ionic strength (I), or electrostatic interactions with other charged species, a phenomenon known as charge regulation (CR). 10 On the other hand, it is well established that CR is highly coupled with the conformational degrees of freedom. In this paper, 11 the influence of CR in the stretching properties of weak polyelectrolytes is analyzed, and the possibility of CR induced by 12 mechanical stretching is explored. With this aim, we make use of a minimal model, which captures the fundamental aspects 13 14 present in the stretching of a flexible weak linear polyelectrolyte: internal angle rotation, bond stretching, bond bending, and proton binding, which is the paradigmatic mechanism of CR. The angle rotation is described by using the rotational isomeric 15 state approximation, while for protonation, the site binding model is assumed. Mechanical stretching is studied by performing 16 semi-grand canonical Monte Carlo simulations at different pH and ionic strength conditions. The simulations simultaneously 17 provide both conformational (bond state probabilities, persistence length  $l_{\rm P}$ , and chain elongation) and protonation properties 18 (degree of protonation  $\theta$  and the effective protonation constant  $K_c$ ). The obtained force–extension curves suggest that the pH 19 value and the ionic strength I have a significant effect on polyelectrolyte stretching. Three different force regimes can be 20 observed. For large forces (F > 100 pN for typical force constants), the force-extension curve is almost independent of the pH 21 and I. For low forces, the persistence length  $l_p$  is force-independent, although it strongly increases with the pH value. Under this 22 23 regime, linear and Pincus scaling behaviors are observed. Finally, in the intermediate-force regime, both rotational and protonation degrees of freedom are mechanically activated, and the picture becomes more complicated. It is found that lp 24 increases with F and, under certain conditions, a significant increase of  $\theta$  with F is observed, indicating that CR could in 25 principle be induced by means of mechanical stretching. This fact can be explained by analyzing the coupling between  $\theta$  and the 26 probability of a bond to be in the gauche state P(g). P(g) decreases with F as the bonds adopt the *trans* conformation so that the 27 electrostatic repulsion is reduced and  $\theta$  increases. Finally, the intricate interplay between short-range and long-range interactions 28 is analyzed, leading to apparently contradictory behaviors (P(g) and  $l_p$  simultaneously decrease with I), which can only be 29 30 explained by CR and the presence of complex spatial correlations.

## 31 INTRODUCTION

<sup>32</sup> In the last two decades, the development of single-molecule <sup>33</sup> force spectroscopy has led to an extraordinary expansion of the <sup>34</sup> field of mechanochemistry.<sup>1,2</sup> By applying a controlled external <sup>35</sup> force to a molecule that is chemically attached to a surface, a <sup>36</sup> wide range of mechanically induced physicochemical events <sup>37</sup> can take place. Just to mention a few examples, AFM has been <sup>38</sup> used to mechanically induce *cis*-to-*trans* isomerization of <sup>39</sup> carbon–carbon double bonds,<sup>3</sup> prolyl *cis–trans* isomerization,<sup>4,5</sup> or conformational chair—boat transitions or hydrogen 40 bond breaking in polysaccharides.<sup>6,7</sup> Some ring-opening 41 reactions, normally forbidden by orbital symmetry, become 42 possible if a tensile force is applied to the polymer chain.<sup>8,9</sup> 43 Single-molecule AFM experiments have been recently used in 44

Received: June 12, 2019 Revised: September 16, 2019 45 monitoring force-dependent enzyme catalysis<sup>10</sup> and surface 46 desorption of polypeptides;<sup>11,12</sup> the characterization of new 47 supramolecular polymers based on host-enhanced  $\pi - \pi$ 48 interaction;<sup>13</sup> or the design of mechanophores embedded in 49 macrocycles, which allows pinpointing of the mechanochem-50 ical bond rupture.<sup>14</sup> Optical tweezers have also been used in 51 the study of the elastic properties of biomacromolecules such 52 as single-stranded DNA (ss-DNA).<sup>2,15</sup>

In parallel to the experimental work, several theoretical 53 54 approaches have been developed, differing in the detail of 55 description of the macromolecular structure.<sup>1,2,16</sup> In the freely 56 jointed chain (FJC) model, the polymer chain is represented at 57 the coarse-grain level by a set of rigid links joined with fully 58 random orientations. Although able to account for the 59 stretching properties of a wide variety of synthetic polymers 60 with different structures and solvents,<sup>1</sup> this model was shown 61 to present clear deviations from the elastic response of many 62 other macromolecules of interest, such as double-stranded 63 DNA (ds-DNA). Aiming at overcoming these limitations, 64 Marko and Siggia modeled the polymer as a worm-like chain 65 (WLC), which, assuming exponential decaying correlations 66 between chain segments, accounted for the capability of the 67 chain to deform on short-length scales.<sup>17</sup> The resulting high-68 force regime matched very well with a variety of polymers for 69 which electrostatic interactions can be neglected, such as some 70 polypeptides<sup>18</sup> or ds-DNA.<sup>19</sup> Models including freely rotating 71 bonds, <sup>20</sup> bond elasticity, <sup>21</sup> or ligand–receptor equilibria<sup>22</sup> have 72 also been proposed, leading to theoretical predictions of new 73 force-extension regimes.

As an alternative to these coarse-graining approaches, 74 75 theoretical methods based on first principles, which account 76 for the detailed atomistic structure of the macromolecular 77 backbone, have also been proposed.<sup>23</sup> In most of these studies, 78 ab initio calculations are first performed in order to detect the 79 more stable conformational states of the interacting monomers 80 at different elongations of the bonds.<sup>24</sup> Once the structural 81 microscopic information is available, the necessary thermal <sup>82</sup> averages are performed by using Monte Carlo (MC) or <sup>83</sup> transfer matrix techniques.<sup>25,26</sup> The resulting scheme has been <sup>84</sup> successful in reproducing the experimental force–extension <sup>85</sup> curves of several polymers.<sup>20,27–29</sup> In particular, the stretching 86 behavior of poly(ethylene glycol) (PEG) has been analyzed in 87 detail.<sup>27,30,31</sup> In essence, this methodology can be regarded as a 88 generalization of the rotational isomeric state (RIS) model <sup>89</sup> developed mainly by Flory to study the conformational <sup>90</sup> properties of linear chains<sup>32,33</sup> in which only the rotational 91 states of minimum energy (commonly trans, gauche+, and 92 gauche-) are taken into account in the computation of the 93 thermal averages.

The methods mentioned above only account for short-range interactions and cannot thus be applied to charged macromolecules for which the long-range Coulombic forces cannot probe neglected. The presence of self-avoiding electrostatic forces produces, however, new elastic regimes, which strongly deviate prom the ideal, non-interacting FJC and WLC models.<sup>34</sup> The non resulting stretching behavior, mainly studied in single-stranded nucleic acids (ss-DNA and ss-RNA), is extremely dependent on the valence and concentration of the counterions<sup>2,15,35–39</sup> and seems to be well explained by the recently proposed well "snake chain model".<sup>40,41</sup> This model was motivated by recent MC simulations with explicit ions,<sup>42,43</sup> which suggested two los elastic regimes. At low forces, the polyelectrolyte behaves as a 107 set of swollen electrostatic blobs on a long-length scale, while at high forces, a short-length, ion-stabilized, crumpling 108 structure is detected.<sup>41-44</sup> Since ss-DNA and ss-RNA are 109 strong polyelectrolytes, in those studies, the macromolecular 110 charge is considered constant and independent of the degree of 111 stretching. 112

However, this could not be the case of weak polyelectrolytes 113 for which the charge is in general a dynamical and fluctuating 114 variable. This fact leads to the phenomenon of charge 115 regulation (CR), defined as the capability of weak polyelec- 116 trolytes to modulate their ionization state as a response to 117 some physicochemical perturbation.<sup>45,46</sup> The main aim of the 118 present work is to study the influence of CR in the stretching 119 properties of weak polyelectrolytes. The possibility of 120 mechanically induced CR will also be explored. CR is 121 ubiquitous in a wide range of processes of biological, 122 environmental, and technological interest. A few examples 123 are the stability of colloidal systems and nanoparticle 124 coatings,<sup>47,48</sup> receptor–ligand interactions in biochemical 125 systems,<sup>49</sup> and protein–protein<sup>50</sup> and protein–surface inter- 126 actions,<sup>51</sup> among many others, which can be found in ref 52 127 and references quoted therein. The paradigmatic mechanism 128 for CR is the binding of protons and other small ions present 129 in the backward medium. Although CR can take place in rigid 130 structures such as nanoparticles or surfaces, most polyelec- 131 trolytes are flexible so that alterations in the ionization state 132 induce changes in the rotational states of the bonds. 133 Sometimes, this can even produce dramatic conformational 134 transitions in the global macromolecular structure, such as the 135 helix-coil transitions of polypeptides<sup>53</sup> or the abrupt swelling 136 of poly(methacrylic acid) in a very narrow range of pH 137 values.

The mechanochemistry of weak polyelectrolytes is still a 139 fairly unexplored area from the experimental, theoretical, and 140 computational point of view. Although some AFM experi- 141 ments<sup>7,55</sup> have been performed on weak polyelectrolytes (such 142 as hyaluronic acid), they have been either focused on the 143 temperature effect<sup>7</sup> or carried out at pH conditions where CR 144 is negligible.<sup>55</sup> As a result, the effect of other environmental 145 variables such as pH or salt concentration is still unknown. In 146 this work, we introduce a minimal model that captures the 147 fundamental aspects present in the stretching of a flexible weak 148 linear polyelectrolyte: internal angle rotation, bond stretching, 149 bond bending, and proton binding. The model presented is 150 based on the site binding rotational isomeric state (SBRIS) 151 model.<sup>52,56-58</sup> The model is implemented in a Monte Carlo 152 simulation scheme in the semi-grand canonical ensemble 153 (SGCMC) widely used in computational modeling of CR 154 phenomena. <sup>51,59-66</sup> An outline of the used methodology is 155 reported in Model and Simulations, while the Results and 156 Discussion section is devoted to analyzing the behavior of both 157 the conformational (bond state probabilities, persistence 158 length, and chain extension) and protonation properties 159 (degree of protonation  $\theta$ ). 160

## MODEL AND SIMULATIONS

Minimal Site Binding Rotational Isomeric State <sup>162</sup> (SBRIS) Model of Stretched Weak Polyelectrolytes. In <sup>163</sup> this work, we will make use of a model, which, containing a <sup>164</sup> minimum number of parameters, still captures the fundamental <sup>165</sup> aspects present in the stretching of a flexible weak linear <sup>166</sup> polyelectrolyte: internal angle rotation, bond stretching, bond <sup>167</sup> bending, and proton binding. The polyelectrolyte, outlined in <sup>168</sup> Figure 1a, can be considered a simplification of a previously <sup>169</sup> fl

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Figure 1. (a) Outline of the model of a weak polyelectrolyte proposed in the present work. The monomers are represented as sites joined by flexible harmonic bonds. Only the rotational states corresponding to minimum energy (rotational isomeric state approximation), that is, trans (t), gauche+ ( $g^+$ ), and gauche- ( $g^-$ ), are taken into account. In order to minimize the number of parameters, only the bonds holding protonable sites (c bonds) are allowed to rotate, while the rest of the bonds (a and b) are forced to be in the trans state. The macromolecular chain is considered symmetric so that  $g^+$  and  $g^$ have the same energy  $\varepsilon_{r}$ . Two kinds of sites are considered: inert sites (gray) and protonating sites. The latter can adopt two possible states: protonated (dark blue) or deprotonated (cyan), with protonation constant K (site binding model). Long-range (LR) and short-range (SR) interactions are treated in a different way. LR interactions (mediated by the solvent) are described by the Debye-Hückel potential. Conversely, neighboring protonated sites linked by a c bond in the *trans* state interact with energy  $\varepsilon_{u,t}$  since SR interactions are mainly mediated by the macromolecular skeleton. Two neighboring sites linked by a c bond in the gauche state cannot be simultaneously protonated due to the huge electrostatic repulsion  $(\varepsilon_{u,g} \to \infty)$ . (b) Snapshot from a semi-grand canonical Monte Carlo (SGCMC) simulation of the stretching of a weak polyelectrolyte with pK = 9, pH = 6,  $I = 10^{-3}$  M, F = 10 pN,  $\varepsilon_{\sigma} = -\hat{1}$ ,  $\varepsilon_{u,t} = 1$ ,  $\hat{l}_0 = 1.5$  Å, and  $\alpha_0 =$ 120°. Both the extension and the degree of protonation depend on the applied force in the z axis direction.

170 proposed model for linear poly(ethylenimine) (LPEI).<sup>57</sup> A 171 similar model has been recently proposed to study the role of 172 long-range interactions in the conformational/protonation 173 coupling.<sup>52</sup> Let us assume that the chain is symmetric (i.e., 174 the chain has a plane of symmetry when it is completely 175 elongated), thus avoiding the question of tacticity, and 176 contains a protonating site situated every three chain positions. 177 In Figure 1, inert and protonating sites are depicted in gray and 178 blue, respectively. A macromolecule with *N* protonating sites 179 thus contains M = 3N - 3 bonds.

The protonation equilibria are treated using the site binding 180 The protonation equilibria are treated using the site binding 181 (SB) model for which the protonating sites can adopt two 182 possible states: protonated (dark blue) and deprotonated 183 (cyan). Within the SB approach, the ionization state of the 184 macromolecule can be characterized by a set of variables s =185 { $s_i$ }, i = 1, ..., N, with values 0 (deprotonated) or 1 186 (protonated). On the other hand, the conformational degrees 187 of freedom are treated assuming the rotational isomeric state 188 (RIS) approximation;<sup>32,33</sup> that is, only the rotational states 189 corresponding to local energy minima are taken into account, 190 typically *trans* (t), *gauche*+ ( $g^+$ ), and *gauche*- ( $g^-$ ). A 191 conformational state of the macromolecule can now be defined 213

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by a set of variables  $c = \{c_j\}, j = 1, ..., M$  where  $c_j$  is the row 192 vector with as many components as the number of states can 193 adopt the bond *j*. In our case, each  $c_j$  can only take three 194 different values:  $c_j = (1,0,0)$  if bond *j* is in *trans*, 195  $c_j = (0, 1, 0)$  if it is in *gauche+*, and  $c_j = (0, 0, 1)$  if it is in *gauche-*.

Since the chain is symmetric, gauche+ and gauche- states 197 have the same energy. For simplicity, let us also assume that 198 only the bonds with adjacent protonating sites (**c** bonds in 199 Figure 1a) are allowed to rotate, while the rest of the bonds (**a** 200 and **b**) are forced to be in the *trans* state. This approximation 201 has been previously used in the modeling of stretching 202 properties of poly(ethylene glycol) (PEG),<sup>27</sup> the neutral 203 counterpart of the model proposed here. As a result, in our 204 model, only N - 1 bonds from the total M bonds are allowed 205 to rotate. Finally, we introduce the possibility of elastic bond 206 stretching and bending. 207

Combining the SB and RIS approaches, we obtain the 208 SBRIS model, which deals with ionization and conformational 209 equilibria simultaneously.<sup>52,56,57</sup> The resulting free energy  $\mathcal{F}_{210}$  can be expressed as the sum of five contributions 211

$$\mathcal{F} = W + \mathcal{F}_{\text{length}} + \mathcal{F}_{\text{angle}} + \mathcal{F}_{\text{SR}} + \mathcal{F}_{\text{LR}} \tag{1}_{212}$$

The term

$$W = -F r \tag{2}_{214}$$

represents the mechanical work exerted by the applied force *F*, 215 which is considered to act in the *z* axis direction, as shown in 216 Figure 1, and *r* is the polyelectrolyte chain end-to-end vector. 217  $\mathcal{F}_{\text{length}}$  and  $\mathcal{F}_{\text{angle}}$  quantify the elastic deformation of the length

and the angles of the M bonds, respectively, which can be 218 important at large forces. In this work, they are represented by 219 the harmonic potentials 220

$$\mathcal{F}_{\text{length}} = \sum_{j=1}^{M} \frac{k_{\text{length},j}}{2} (l_j - l_{j,0})^2$$
(3) 221

and

$$\mathcal{F}_{ang} = \sum_{j=1}^{M-1} \frac{k_{angle,j}}{2} (\alpha_j - \alpha_{j,0})^2$$
(4) 223

where  $l_{j}$ ,  $\alpha_{j}l_{j,0}$ , and  $\alpha_{j,0}$  represent, respectively, the length, the 224 bending angle, the equilibrium length, and the equilibrium 225 bending angle of bond *j*. Finally,  $k_{\text{length}, j}$  and  $k_{\text{angle}, j}$  denote the 226 bond stretching and bending force constants. Note that the 227 geometrical parameters and the force constants in the 228 potentials (eqs 3 and 4) do not depend on the ionization 229 state of the sites. At this level of description, this is a reasonable 230 approximation, according to quantum-mechanical computa- 231 tions, which show only small variations in the bond lengths 232 (see, for instance, the results for LPEI at different degrees of 233 ionization<sup>67</sup>). On the other hand, as will be shown in the next 234 section, the bond bending and bond stretching will be 235 essentially induced by the mechanical work at high enough 236 forces rather than by electrostatic repulsions. 237

The electrostatic/conformational interaction free energy has 238 been split into short-range (SR)  $\mathcal{F}_{SR}$  and long-range (LR)  $\mathcal{F}_{LR}$  239 contributions, as depicted in Figure 1. This distinction 240 becomes necessary due to the fundamental differences in the 241 physical chemistry of SR and LR interactions. It is well 242 established that LR interactions are chemically unspecific, 243

244 mediated by the solvent, and can be reasonably approximated 245 by a simple pair-interaction continuous force field. Conversely, 246 SR interactions between neighboring sites and bonds are 247 mediated by the macromolecular skeleton so that they depend 248 on the detailed chemical environment of the site. As a result, 249 they cannot be described by simple potentials, and specific 250 interaction parameters must be used. These parameters will 251 depend on the particular rotational state of the bond 252 connecting the two protonating sites (in our case, the **c** 253 bonds).  $\mathcal{F}_{SR}$  is the result of two contributions

$$\mathcal{F}_{SR} = \mathcal{F}_{rot}(c) + \mathcal{F}_{p}(s, c), \tag{5}$$

 $\mathcal{F}_{rot}(c)$ , corresponding to the classical RIS model,<sup>32,33</sup> 256 represents the conformational energy of the bonds for a 257 given conformational state  $c = \{c_j\}$  when the polyelectrolyte is 258 uncharged. On the other hand,  $\mathcal{F}_p(s, c)$  includes the binding 259 free energy and the SR electrostatic interaction between 260 charged sites and accounts for the coupling between the 261 conformational and ionization degrees of freedom. The term

 $\mathcal{F}_{\mathrm{rot}}$  can be expressed as

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$$\frac{\beta \mathcal{F}_{rot}(c)}{\ln 10} = \sum_{j=1}^{M} \epsilon_j c_j^T + \sum_{j=1}^{M} \epsilon_j E_j c_j^T + \cdots$$
(6)

263 where  $\beta = 1/k_{\rm B}T$  is the inverse of the thermal energy,  $\epsilon_j$  is a 264 row vector whose elements are the free energies associated 265 with the rotational state of bond *j*, and *E<sub>j</sub>* is a square matrix 266 containing the interaction energies between the neighboring 267 bonds *j* and *j* + 1.  $\epsilon$  and *E* are expressed in thermal units and 268 divided by a factor ln 10 in order to be compared with the pH 269 scale. The sum in eq 6 could be extended to take into account 270 three-bond interactions, four-bond interactions, and so on. In 271 this work, however, we only considered SR interactions 272 involving the first neighbor bonds. Following Flory, <sup>32,33</sup> we 273 choose as the ground state the configuration with all the bonds 274 in the *trans* state. In this way, the rotational parameters  $\epsilon_j$  and 275  $E_i$  can be expressed as

$$\boldsymbol{\epsilon}_{j} = (0, \ \boldsymbol{\varepsilon}_{\sigma}, \ \boldsymbol{\varepsilon}_{\sigma})_{j}, \ \boldsymbol{E}_{j} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \boldsymbol{\varepsilon}_{\psi} & \boldsymbol{\varepsilon}_{\omega} \\ 0 & \boldsymbol{\varepsilon}_{\omega} & \boldsymbol{\varepsilon}_{\psi} \end{pmatrix}_{j}$$
(7)

277 where  $\varepsilon_{\sigma, j}$  is the free energy of the *gauche* states, while  $\varepsilon_{\psi, j}$  and 278  $\varepsilon_{\omega, j}$  are related to the interaction energies between two 279 consecutive *gauche* states with the same and different 280 orientation, respectively. The Boltzmann factor corresponding 281 to  $\varepsilon_{\alpha}$  is precisely  $\alpha$ , that is,  $\varepsilon_{\alpha} = -\log \alpha \ (\alpha = \sigma, \psi, \omega)$ . In 282 choosing this notation, the resulting Boltzmann factors are 283 denoted by the same symbols used in previous works, 284 which make use of the transfer matrix approach. For instance, 285 the transfer matrix corresponding to the free energy (eq 6) is 286 given by

$$\mathbf{T}_{j} = \begin{pmatrix} 1 & 1 & 1 \\ 1 & \sigma_{\psi} & \sigma_{\omega} \\ 1 & \sigma_{\omega} & \sigma_{\psi} \end{pmatrix}_{j}$$
(8)

On the other hand, the second term in eq 5,  $\mathcal{F}_{p}$ , can be 289 expressed in terms of the ionization state  $s = \{s_i\}$  by means of 290 the cluster expansion<sup>52</sup>

$$\frac{\beta \mathcal{F}_{p}(s, c)}{\ln 10} = \sum_{i=1}^{N} \mu_{i} s_{i} + \sum_{i=1}^{N-1} \epsilon_{u,i} c_{3i-1} s_{i} s_{i+1} + \cdots, \qquad (9)_{29}$$

where  $\mu_i = pH - pK_i = -\log(Ka_H)$  is the reduced chemical 292 potential of the ionizable site *i*, which depends on the proton 293 activity,  $a_H$ , and the pK values of the protonation constant of 294 site *i*,  $pK_i$ .  $\epsilon_u$  is a row vector whose components correspond to 295 the electrostatic interaction energy between the neighboring 296 charged sites *i* and *i* + 1. The intensity of the interaction is 297 determined by the rotational state of the **c** bond between the 298 two sites (bond number 3i - 1 in the chain) 299

$$\boldsymbol{\epsilon}_{u,i} = \begin{pmatrix} \varepsilon_{u,t}, & \varepsilon_{u,g}, & \varepsilon_{u,g} \end{pmatrix}_i \tag{10}_{300}$$

In eq 10, we have assumed that only the bonds of type c are 301 able to rotate. Note that in the SBRIS model, the SR 302 electrostatic interactions depend on the conformation of the 303 bond linking of the sites, which couples the ionization and the 304 conformational degrees of freedom. As in eq 6, the sum in eq 9 305 could be extended to take into account triplet interactions, 306 quadruplet interactions, and so on. In this work, however, only 307 neighboring pair SR interactions will be taken into account. 308

Finally, as in most of the previous literature,<sup>57,68</sup> LR 309 electrostatic interactions will be described by the Debye– 310 Hückel (DH) potential 311

$$\beta \mathcal{F}_{LR} = \sum_{i=1}^{N} \sum_{j=i+2}^{N} \frac{l_{B}}{d_{ij}} e^{-\kappa d_{ij}} s_{i} s_{j}$$
(11) 312

where  $l_{\rm B} \approx \simeq 0.7$  nm is the Bjerrum length in water at 298.15 313 K,  $d_{ij}$  is the distance between sites *i* and *j*, and 314  $\kappa^{-1}(nm) = 0.304/\sqrt{I(M)}$  is the Debye length for water 298.15 K at ionic strength *I*. 315

Since we are interested in a model with the minimum 316 number of parameters in order to analyze the fundamental 317 aspects of the stretching, in this work, we will restrict ourselves 318 to the special situation in which all the bonds have the same 319 length, bond angle  $(l_{j,0} = l_0 \text{ and } \alpha_{j,0} = \alpha_0)$ , and force constants 320  $(k_{\text{length}, j} = k_{\text{length}} \text{ and } k_{\text{angle}, j} = k_{\text{angle}})$ . Moreover, we consider 321 that all the protonating sites are identical  $(pK_i = pK)$  and the 322 possible end effects of the chain are neglected so that  $\epsilon_i = \epsilon_{323}$ and  $\boldsymbol{\epsilon}_{u,i} = \boldsymbol{\epsilon}_{u}$ . It is also assumed that when two neighboring 324 sites are charged, the very strong SR repulsion hinders the 325 gauche conformation of the c bond so that  $u_g = 0$  or  $\varepsilon_{u,g} \to \infty$ . 326 Since one of every two consecutive bonds is always in the trans 327 state, the interaction terms  $arepsilon_{\psi}$  and  $arepsilon_{\omega}$  become irrelevant, and 328 they can be taken as zero without loss of generality. To 329 summarize, the model presented involves the following 330 assumptions: 331

- 1. The SBRIS model is used to describe the conformational 332 and protonation equilibria on the same foot. 333
- 2. The molecule contains one protonating site every two 334 inert groups, as shown in Figure 1. 335
- 3. The ionizable sites are identical, with the same pK value, 336 and the bonds have the same length, bending angle, and 337 constant forces. 338
- 4. Only the bonds of type c are allowed to rotate, while 339 bonds of types a and b are constrained to be in the *trans* 340 state. In practice, this implies that the rotation of the 341 bonds is independent when the macromolecule is fully 342 uncharged. 343
- 5. LR interactions are described by the DH potential, 344 which accounts for screening effects so that co- and 345



**Figure 2.** Metropolis algorithm of the SMGMC simulation code. In each new MC configuration, the polyelectrolyte can change either (A) the rotational state of a bond, (B) the length or angle of a bond, (C) the ionization state of a binding site, or (D) the spatial orientation of the polyelectrolyte chain in a laboratory coordinate frame with trial probabilities of 0.88, 0.1, 0.01, and 0.01, respectively.

346	counterions intervene only in an effective way. Only
347	excluded volume effects induced by electrostatics are
348	taken into account.

6. Specific parameters are used to describe interactions
between neighboring sites. Moreover, when two
neighboring sites are simultaneously protonated, the c
bond linking the sites cannot adopt the *gauche* state.

7. As a result, the parameters involved in the model are  $\varepsilon_{\sigma}$ 353 (free energy difference between gauche and trans states), 354 interaction energy between neighboring sites  $(\varepsilon_{u,t})$ 355 when the c bonds are in the gauche state, equilibrium 356 length and equilibrium angle of the bonds  $(l_0 \text{ and } \alpha_0)$ , 357 and constant forces for the bending and bond stretching 358  $(k_{\text{length}} \text{ and } k_{\text{angle}})$ . The control variables are the reduced 359 chemical potential of the protonating sites ( $\mu = pH -$ 360 pK) and the ionic strength (I). 361

Finally, note that in the absence of LR interactions 362  $(\mathcal{F}_{LR} = 0)$ , that is, at high enough ionic strengths, the model 363 364 can be exactly solved by using the transfer matrix (TF) 365 method.<sup>52,57,58</sup> When applied to calculate stretching properties, 366 the resulting TF combine conformational energies, by means  $_{367}$  of TF of the type (eq 8), and geometrical restrictions imposed 368 by the macromolecular skeleton. In the absence of ionization 369 processes, this method has been used to study the stretching of <sup>370</sup> chains with freely rotating bonds<sup>20</sup> and the stretching <sup>371</sup> properties of POE.<sup>20,27</sup> However, in this work, we are 372 especially interested in the effect of electrostatic interactions 373 that are long ranged, and the LR term (eq 11) cannot be neglected. As a consequence, the transfer matrix approach 374 would be too restrictive since only the cases of high ionic 375 376 strength could be analyzed. For this reason, a Monte Carlo computational code has been developed in order to implement 377 378 the model, which is described in the next subsection.

Monte Carlo Simulations at Constant pH Value. The proposed SBRIS model is analyzed by means of simulations in the semi-grand canonical Monte Carlo (SGCMC); that is, the pH value is the control variable, and it is kept constant along the computation. The SGCMC code is a modification of the <sup>383</sup> one previously developed by our group to compute conforma-<sup>384</sup> tional and ionization properties of linear polyelectrolytes. <sup>52,57</sup> <sup>385</sup> In particular, it has been extended in order to include the effect <sup>386</sup> of mechanical work. As a result, bending and stretching of the <sup>387</sup> bonds have also been implemented. The resulting program is <sup>388</sup> rather general since it allows working with sites and bonds of <sup>389</sup> different *pK* values, interaction energies, conformational <sup>390</sup> energies, and so on. Excluded volume effects can also be <sup>391</sup> taken into account. Moreover, the code can deal with any <sup>392</sup> arbitrary distribution of the sites along the chain, which is <sup>393</sup> chosen by the user. However, in this paper, we restrict its use <sup>394</sup> to the assumptions detailed previously. A snapshot of one of <sup>395</sup> the SGCMC realizations is shown in Figure 1.

The Metropolis algorithm<sup>68,69</sup> generates new states at 397 constant pH in a chain with N = 50 ionizable sites (i.e., 148 398 nodes or M = 147 bonds), a number which is large enough to 399 avoid end effects and ensures the reproducibility of the 400 intensive properties of the polymer, such as bond state 401 probabilities or degree of protonation. An outline of the 402 algorithm is depicted in Figure 2. In each new MC 403 f2 configuration, the polyelectrolyte can change either (A) the 404 rotational state of a bond, (B) the length or bending angle of a 405 bond, (C) the ionization state of a binding site, or (D) the 406 spatial orientation of the polyelectrolyte chain in the laboratory 407 reference frame, with trial probabilities of 0.88, 0.1, 0.01, and 408 0.01, respectively. These values allow us to obtain a good 409 equilibration of the conformational structure for a given 410 ionization state so that the system does not get trapped in local 411 minima. Each change in the rotational state of a bond *j* implies 412 a  $\pm 120^{\circ}$  rotation of its dihedral angle and the recalculation of 413 distances among the sites situated before and after the rotating 414 bond. The changes in the stretching and bending states of 415 bond j are  $\Delta l_i = \pm 0.01$  Å and  $\Delta \alpha_i = \pm 0.5^\circ$ , respectively. 416 These variations provide an average acceptance ratio of ~20%, 417 which is an acceptable value to make proper statistics. The 418 global spatial orientation of the polymeric chain is altered by 419

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**Figure 3.** (a, b) Titration curves and (c, d) effective pK value for the polyelectrolyte depicted in Figure 1 in the absence of the pulling force. The images on the left side correspond to  $\sigma = 1$ , and those on the right side refer to  $\sigma = 10$ . The chosen ionic strengths are 1 M (green squares), 0.1 M (turquoise circles), 0.01 M (cyan upward triangles), and 0.001 M (blue downward triangles). The rest of the parameters have the same values as those in Figure 1b.

420 changing the polar angle  $\theta$  and the azimuth angle  $\phi$  of the first 421 and second bonds of the polyelectrolyte with respect to the 422 laboratory coordinate frame by amounts  $\Delta \theta = \pm 2^{\circ}$  and  $\Delta \cos$ 423 ( $\phi$ ) =  $\pm$  0.1, respectively. The latter change is important to 424 avoid preferred orientations in the space at zero force. Once 425 the free energy difference ( $\Delta F$  of eq 1) between trial and 426 current conformations is calculated, the new configuration is 427 always accepted if  $\Delta \mathcal{F} < 0$  and accepted with a probability exp( $-\beta \Delta \mathcal{F}$ ) if  $\Delta \mathcal{F} > 0$ .

The results presented represent the average over eight 428 429 different SGCMC simulations. Each simulation has been 430 equilibrated in the first  $5 \times 10^7$  configurations, and the thermal  $_{431}$  averages have been computed in the following  $4.5 \times 10^8$ 432 realizations. The simulations were performed using a parallel 433 code developed in C++ on a 126 CPU cluster. For each pH, ionic strength, and force, typical jobs were run using eight 434 435 CPUs for 1 to 2 h. The chosen parameters are pK = 9 and  $u_t =$ 436 10, similar to those corresponding to LPEI. Note, however, 437 that the reduced free energy only depends on the reduced 438 chemical potential  $\mu = pH - pK$ . This means that the results 439 and conclusions taken from the simulations are the same for 440 any pK value by choosing a suitable pH value for which the 441 difference pH - pK is the same. The simulations are 442 performed at room temperature T = 298.15 K. Free protons, 443 co-ions, and counterions are not explicit in the simulations, and 444 the screening effects are taken into account via the Debye 445 length parameter,  $\kappa^{-1}$ , in eq 11. The chosen values for the 446 parameters in the stretching and bending potentials are  $l_0 = 1.5$ 447 Å,  $\alpha_0 = 120^\circ$ ,  $k_{\text{length}} = 300 \text{ kcal mol}^{-1} \text{ Å}^{-2}$ , and  $k_{\text{angle}} = 0.01 \text{ kcal}$ 448 mol<sup>-1</sup> deg<sup>-2</sup>, which are typical values used in molecular 449 dynamics force fields for C–C bonds.<sup>7</sup>

The average degree of protonation  $(\theta)$  is computed as 450

$$\theta = \frac{\langle N_{+} \rangle}{N} \tag{12} _{451}$$

where  $\langle N_+ \rangle$  is the thermal average number of protonated sites. 452 Note that since the simulations are performed at constant pH, 453  $N_+$  is a fluctuating quantity, different in each new accepted 454 configuration. Another interesting quantity is the effective 455 protonation constant ( $K_c$ ), which provides information about 456 the average affinity of the macromolecular sites for the 457 protons.<sup>62,71,72</sup> In general,  $K_c$  depends on the charge of the 458 macromolecule, different at each pH value. It is defined as 459

$$\log K_{\rm c} = \rm{pH} + \log \left(\frac{\theta}{1-\theta}\right) \tag{13}_{460}$$

The probability of a rotating **c** bond to be in the *gauche* state,  $_{461}P(g)$ , is calculated as  $_{462}$ 

$$P(g) = \frac{\langle N_g \rangle}{N-1} \tag{14}_{463}$$

where  $\langle N_g \rangle$  is the thermal average number of rotating bonds in 464 a *gauche* state. Other quantities, such as the probability of 465 having two neighboring **c** bonds in given conformations, (e.g., 466 *tt*,  $tg^+$ ,  $g^+g^+$ , etc.) can be calculated in the same way. The 467 extension of the polyelectrolyte chain  $(L_z)$  in the direction of 468 the mechanical force, that is, the *z* axis, is obtained as 469

$$L_z = \langle z_{M+1} - z_1 \rangle \tag{15}_{470}$$

where  $z_i$  is the *z* coordinate of site *i* in the laboratory 471 coordinate frame. Finally, a very useful quantity to understand 472



**Figure 4.** (a, b) Chain elongation  $L_z$  normalized to the contour length  $L_C$  (c, d) *gauche* state probability, (e, f) persistence length, and (g, h) degree of protonation versus the applied force *F* at a constant ionic strength of 0.001 M and pH values of 4 (squares), 6 (circles), 8 (upward triangles), and 10 (downward triangles). The images on the left side correspond to  $\sigma = 1$ , and those on the right side refer to  $\sigma = 10$ . The rest of the parameters have the same values as those in Figure 1b.

<sup>473</sup> the mechanism of macromolecular stretching is the persistence <sup>474</sup> length  $l_{\rm P}$ , defined as the average sum of the projections of all <sup>475</sup> the bonds  $j \ge i$  on bond *i* in an indefinitely long chain

$$l_{\rm P}/l_0 = \sum_{j\geq i} \langle \mathbf{b}_i \cdot \mathbf{b}_j \rangle \tag{16}$$

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 $_{477}$  where **b**<sub>i</sub> are unitary vectors pointing to the direction of the  $_{478}$  bonds. It is straightforward to show that, for a long enough

chain  $(M \rightarrow \infty)$ ,  $l_{\rm P}$  is related to the average square end-to-end distance  $\langle {\bf r}^2 \rangle$  by the relationship<sup>32</sup> 480

$$l_{\rm p} = \frac{\langle \mathbf{r}^2 \rangle}{2Ml_0} + \frac{l_0}{2} = \frac{\langle (\mathbf{r}_{M+1} - \mathbf{r}_{\rm l})^2 \rangle}{2Ml_0} + \frac{l_0}{2}$$
(17) 481

where  $r_i$  is the position of site *i*. As a consequence of eq 17, the 482 Kuhn length 483 484

$$l_{\rm K} = \frac{\langle \mathbf{r}^2 \rangle}{M l_0} \tag{18}$$

485 can be directly related to the persistence length by  $l_{\rm K} = 2l_{\rm P} - l_0$ .

## 486 **RESULTS AND DISCUSSION**

487 In this section, we will discuss the effect of the pH value and 488 the ionic strength on the force-extension curves by 489 simultaneously analyzing the dependence of conformational (chain elongation, bond state probabilities, and persistence 490 491 length) and protonation properties (degree of protonation and 492 effective protonation constant). As commented above, the 493 microscopic pK value of the protonating sites will be fixed at 494 pK = 9 throughout this section without loss of generality since 495 the free energy (eq 1) depends on the pH value through the 496 reduced chemical potential  $\mu = pH - pK$ . As a result, for a 497 different pK value, all the conclusions will be the same but 498 shifting the pH value in a constant value. Concerning the 499 energy of the gauche state in the absence of charge, two cases 500 physically relevant are considered. In the first case, the 501 polyelectrolyte exhibits free rotation (i.e., gauche and trans so states have the same energy,  $\varepsilon_{\sigma} = 0$ ,  $\sigma = 1$ ). In the second case, 503 the gauche states of the c bonds are favored, for instance, 504 because of the existence of hydrogen bonding between two 505 consecutive protonating sites, which means that  $\sigma > 1$  (we take 506  $\varepsilon_{\sigma} = 1$ ,  $\sigma = 10$ ). This phenomenon has been observed in LPEI 507 and POE.<sup>57</sup> The case  $\sigma < 1$  is not much interesting since most 508 of the bonds are in the trans state so the chain is basically 509 extended even in the absence of force. Finally, the interaction 510 energy between two charged neighboring sites through a trans s11 **c** bond is fixed at  $\varepsilon_{u,t} = 1$  ( $u_t = 0.1$ ) for all the studied cases, 512 which is the order of magnitude found in a number of weak 513 polyelectrolytes by using potentiometry. These works indicate 514 that, for the same molecule, neighboring interactions are rather s15 independent of the ionic strength.<sup>56,57,</sup>

Since charge regulation is a key ingredient of the model, let 516 517 us first analyze the behavior of the degree of protonation  $\theta$ 518 when no mechanical force is applied, which will be useful in 519 the foregoing discussion. In Figure 3, the titration curves for s20 the cases  $\sigma = 1$  (a) and  $\sigma = 10$  (b) are shown at four different 521 ionic strengths (I): 1, 0.1, 0.01, and 0.001 M, from top to 522 bottom. It can be observed that in both cases, lowering the 523 ionic strength results in a decrease of the degree of protonation 524 for all of the pH values, which is explained by the increase in 525 the LR electrostatic repulsion. Note that this effect is larger in 526 the case  $\sigma$  = 10, which can be explained by the fact that *gauche* 527 states are energetically favored, which hinders the possibility of s28 having two neighboring sites charged (since  $u_g = 0$ ). The 529 effective protonation constant  $K_c$  is depicted in Figure 3c,d for 530  $\sigma$  = 1 and  $\sigma$  = 10, respectively. Clearly, K<sub>c</sub> presents two 531 asymptotic values. At high pH, the macromolecule is not  $_{532}$  charged, electrostatic interactions are absent, and the  $K_c$  value 533 corresponds to the microscopic pK value of the ionizable sites  $_{534}$  (pK = 9). However, as pH decreases, sites get ionized and the 535 work needed to protonate an empty site increases due to s36 electrostatic repulsion. This results in a decrease in  $K_{c}$ , which, 537 at low enough pH values, reaches a new asymptotic value. This 538 decrease in the affinity for the proton is especially relevant at 539 low ionic strengths for which the LR interactions are stronger 540 since screening is weaker. Finally, note that, for the same pH 541 and I values, the decrease in pK<sub>c</sub> in the case  $\sigma = 10$  is more 542 pronounced than in the case  $\sigma = 1$ . For  $\sigma = 10$ , the gauche 543 states are energetically promoted, the chain is more folded, and

the distance between charger sites is shorter, which leads to 544 larger LR interactions. 545

Effect of the pH Value on the Force–Extension 546 Curves. The force–extension curves are shown in Figure 4a,b 547 f4 for the cases  $\sigma = 1$  and  $\sigma = 10$ , respectively, for pH values 548 ranging from 4 to 10 (top to bottom). The chain extension is 549 normalized to the contour length 550

$$L_{C} = N l_{0} \cos((\pi - \alpha_{0})/2)$$
(19) 551

defined as the length of the fully extended chain (i.e., all the 552 bonds are in the trans state) with bond lengths and angles in 553 their equilibrium position. The chosen value for the ionic 554 strength is 0.001 M, a small value for which the LR 555 electrostatic interactions are maximized. In order to better 556 understand the extension curves, the gauche state probability 557 (Figure 4c,d) and persistence length (Figure 4e,f) are also 558 represented. On the other hand, the degree of protonation is 559 depicted in Figure 4g,h. The images in the left side always 560 correspond to the case  $\sigma = 1$ , while those in the right side refer 561 to the case  $\sigma = 10$ . It is important to stress that stretching, 562 conformational, and ionization properties are highly coupled, 563 so we will discuss them all at once. Owing to the lack of space, 564 in the main document of this work, we just present and discuss 565 the force-extension curves, which are more relevant for the 566 purpose of this study. However, for the lecturers interested, the 567 full casuistry, covering the complete range of pH values and 568 ionic strengths, is reported in the Supporting Information. 569

Let us first analyze the different force regimes in terms of the 570 progressive activation of the degrees of freedom of the bonds, 571 that is, rotational, bending, and stretching. First of all, note 572 that, for low enough forces and for all the pH values, both the 573 *gauche* state probability P(g) and the normalized persistence 574 length  $l_{\rm P/l_0}$  remain constant. Despite this fact, the chain is 575 considerably extended, around 10% for pH = 10 and a 576 remarkable 50% for pH = 4. This indicates the existence of a 577 low-force regime (corresponding to  $F < F_{\rm E} = k_{\rm BT/l_{\rm P\times 1}} \, {\rm pN})^{20}_{578}$  under which the chain behaves as a structureless set of 579 segments with characteristic length  $l_{\rm P}$ .

The dependence of P(g) and  $l_{\rm P}$  on the pH value is shown in 581 Figure 4. As observed in Figure 4c,d, P(g) is strongly affected 582 by the pH value at low forces. This fact can be better explained 583 by observing the behavior of the average degree of protonation 584  $\theta$  (Figure 4g,h) for  $F < F_{\rm E}$ . For  $\sigma = 1$ ,  $\theta$  increases from  $\theta \approx 0.05$  585 at pH = 10 to  $\theta \approx 0.7$  at pH = 4, while for  $\sigma = 10$ ,  $\theta$  increases 586 from  $\theta \approx 0.05$  at pH = 10 to  $\theta \approx 0.6$  at pH = 4. In both cases, 587 when the adjacent sites are simultaneously protonated, the 588 electrostatic repulsion is so strong that the gauche states are 589 forbidden ( $u_g = 0$ ). As a result, the rotational properties change 590 with the pH value, resulting in two limit behaviors. At high pH, 591 when the polymer is discharged, the bonds present free 592 rotation (when  $\sigma = 1$ ) or preference for the gauche state (when 593  $\sigma$  = 10). On the contrary, at low enough pH values, when the 594 macromolecule is almost completely charged, the restriction  $u_g$  595 = 0 forces all the bonds to adopt the *trans* conformation. The 596 increase of the number of bonds in the trans state due to 597 lowering the pH value can be clearly observed in Figure 4c,d. 598 As a result, the polymer chain gets stiffer, and the persistence 599 length increases, as can be observed in Figure 4e,f. In turn, this 600 fact leads to the increase in the chain elongation observed in 601 Figure 4a,b, which is more marked for  $\sigma = 1$  than for  $\sigma = 10$ . In 602 the latter case, the gauche state is energetically favored so that a 603

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**Figure 5.** Normalized chain extension versus force in the low-force regime for (a)  $\sigma = 1$  and (b)  $\sigma = 10$  at constant ionic strength *I* = 0.001 M but with pH values (from top to bottom) of 2, 4, 6, 8, and 10. The simulation results (markers) are compared to the linear eq 20 (dashed lines) and to the Pincus scaling law, eq 21 (continuous lines). The rest of the parameters have the same values as those in Figure 1b.

604 larger charge (i.e., a lower pH) is required to obtain the same 605 number of *trans* bonds and to increase the persistence length. 606 The elongation versus force curves in the low force regime 607 are shown in Figure 5 where the simulation values are depicted 608 as markers. As can be observed, the low-force regime can be 609 divided into two subregimes. For very low forces (F < 0.1 pN), 610 the chain behaves as an entropic spring, and the elongation 611 responds linearly to the applied force (dashed lines in the 612 figure). The relation between elongation and force is given by

$$L_z/Ml_0 = \beta \, \frac{l_{\rm K}}{3} F = \beta \, \frac{2l_{\rm P} - l_0}{3} F \tag{20}$$

614 This expression is independent of the structure of the chain 615 since it comes directly from the fluctuation-dissipation 616 theorem.<sup>73</sup> Under this subregime, the mechanical work is 617 much smaller than the thermal energy. However, for larger 618 forces (0.1 < F < 1 pN), the situation becomes more complex. 619 It is found that the extension follows the Pincus scaling law<sup>73,74</sup> 620 (continuous lines)

$$L_z \approx F^{1/\nu - 1}$$
 (21)

Note that  $\nu$  is found to range from  $\nu = 1/2$  at high pH 622 (uncharged chain and corresponding to the linear regime) to  $\nu$ 623 624 = 3/5 at low pH (at which the chain is almost fully charged). 625 The latter value was first predicted by Pincus<sup>74</sup> for strong 626 polyelectrolytes, and it can be explained as the effect of 627 electrostatic excluded volume interactions and the correspond-628 ing swelling of the macromolecule. Interestingly, both limiting 629 values are obtained with great accuracy from the simulations, 630 which nicely confirms Pincus theory. For pH values ranging 631 from 6 to 8, intermediate values of  $\nu$  are obtained, indicating 632 that a partially charged weak polyelectrolyte can be seen as an 633 intermediate situation between the neutral chain and a strong 634 polyelectrolyte. For the case  $\sigma = 10$ , the transition between the 635 two limiting cases is more gradual than for  $\sigma$  = 1 due to the fact 636 that lower pH values are necessary to fully charge the chain (see Figure 3). 637

638 So far, we have analyzed the low-force regime for which the 639 persistence length remains constant with the applied force. For 640 larger forces, however, the rotational degrees of freedom are 641 activated. This fact makes P(g) decrease with the force. In this 642 new situation, the bonds, which were initially in the *gauche* 643 state, gradually adopt the *trans* state by effect of the pulling 644 force. The stretching mechanism is no longer entropic, but it 645 depends on the free energy of the *trans/gauche* transition, and 646 the persistence length becomes force-dependent. This fact is in 647 contrast with DNA, with a much more rigid structure and for which charge regulation can be neglected.<sup>35</sup> The new 648 characteristic force  $F_{\rm R}$  for which the rotational degrees of 649 freedom are activated can be roughly estimated by equating the 650 mechanical work per monomer to the free energy of the bond 651 state transition  $\Delta F_{t \to g}$  so that 652

$$F_{\rm R}l_0 \approx \Delta F_{t \to g} \approx k_{\rm B}T\ln(2\sigma) \tag{22}$$

The  $F_{\rm R}$  resulting values are 30 and 70 pN for  $\sigma = 1$  and  $\sigma = 10$ , 654 respectively, in agreement with the observed range of forces 655 (1-100 pN) for which the variation of P(g) is more 656 pronounced. Moreover, the conformational degrees of freedom 657 are coupled with proton binding due to the term (eq 9) in the 658 reduced free energy. It is observed that, in increasing the force 659 value, the change in the rotational states from gauche to trans is 660 simultaneous with the increase in the macromolecular charge. 661 Two asymptotic behaviors are found again. At low forces, the 662 protonation state is the same as the one of the non-stretched 663 molecule. As commented above,  $\theta$  is lower for  $\sigma = 10$  than for 664  $\sigma$  = 1. At large enough forces, however, a new plateau arises, 665 and heta is the same value for both  $\sigma$  values. The gap between the 666  $\theta$  value at low and high forces is thus larger for  $\sigma$  = 10 and 667 depends on the pH value. For instance, for  $\sigma = 10$  and pH = 4, 668  $\theta$  ranges from less than 0.58 in the linear regime to 0.83 for the 669 larger forces. At large pH values, however, the change in  $\theta$  is 670 smaller in absolute terms although it can be significant in 671 relative terms. For instance, for  $\sigma = 10$  and pH = 8,  $\theta$  ranges 672 from 0.2 to 0.32, which means an increase of more than 50%. 673 Using the definition (eq 13), the effective protonation constant 674  $K_{\rm c}$  can be calculated as a function of the force. The obtained 675 effective pK value, which is not shown here but can be found in 676 the Supporting Information, slightly increases with F for both  $\sigma$  677 values. However, this effect is very weak since the pK value at 678 large forces exceeds the low force limit by, at most, 0.5 pK 679 units. However, this variation seems to be enough to cause 680 significant changes in the macromolecular charge in applying 681 an external force. This point will be discussed in more detail in 682 the next subsection for the full range of ionic strengths. 683

Finally, when the force is large enough to deform bond 684 angles and lengths, a third situation arises. The average bond 685 length  $\langle l \rangle$  (green squares) and bond angle  $\langle \alpha \rangle$  (black dots), 686 normalized by their respective equilibrium values, are shown in 687 Figure 6 as functions of the applied force. It can be observed 688 66 that the bond length and angle only start to be significantly 689 elongated for values larger than the characteristic force ( $F_S > 690$  300 pN). A rough estimation of  $F_S$  using the Hooke law also 691 confirms this value. Note that the bond angle is slightly easier 692 to deform than the bond length. Although it is not shown in 693



**Figure 6.** Average bond length  $\langle I \rangle$  (green squares) and bond angle  $\langle \alpha \rangle$  (black dots) versus applied force *F*, normalized to their equilibrium values,  $l_0$  and  $\alpha_0$ . Lines are only to guide the eyes. The simulations have been performed at pH = 6, *I* = 0.01 M, and  $\sigma = 1$ . The rest of the parameters have the same values as those in Figure 1b.

694 the figure, bond stretching and bending have been found to be 695 independent of the pH value and ionic strength. This fact 696 explains why the force–extension curves in Figure 4a,b also 697 become almost independent of the pH for forces larger than  $F_{\rm S}$ . At this point, most of the bonds are in the *trans* state. Since 698 the force constants are independent of the ionization state, the 699 response to the applied force is also the same for any degree of 700 protonation. Finally, for forces around and larger than  $F_{\rm S}$ , the 701 bending potential becomes anharmonic, finally leading to bond 702 breaking, as reported in several AFM single-molecule 703 stretching experiments.<sup>1</sup>

We conclude that, for intermediate forces and suitable pH 705 and ionic strength values, CR can be induced by an applied 706 force when the mechanism of CR is proton binding. For other 707 types of binding mechanisms, such as metal binding, the ionic 708 charge and binding constants are much larger, and the binding 709 mechanism strongly depends on the conformational state (for 710 instance, because of the presence of chelate complexes). As a 711 result, CR could be significantly enhanced. In those cases, 712 which are out of the scope of the present work, the interplay 713 between stretching and CR could be of technological interest. 714

**Effect of the lonic Strength.** Let us investigate the effect 715 of the ionic strength in the force–extension curves, which are 716 f7



**Figure 7.** (a, b) Chain elongation  $L_z$  normalized to the contour length  $L_{CI}$  (c, d) *gauche* state probability, and (e, f) persistence length versus applied force *F* at a constant pH value of pH = 6 and ionic strengths of 1 M (green squares), 0.1 M (turquoise circles), 0.01 M (cyan upward triangles), and 0.001 M (blue downward triangles). The images on the left side correspond to  $\sigma = 1$ , and those on the right side refer to  $\sigma = 10$ . The rest of the parameters have the same values as those in Figure 1b.



**Figure 8.** (a, b) Degree of protonation and (c, d) effective pK value versus applied force *F* at a constant pH value of pH = 6 and ionic strengths of 1 M (green squares), 0.1 M (turquoise circles), 0.01 M (cyan upward triangles), and 0.001 M (blue downward triangles). The images on the left side correspond to  $\sigma = 1$ , and those on the right side refer to  $\sigma = 10$ . The rest of the parameters have the same values as those in Figure 1b.

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717 represented in Figure 7a,b for ionic strengths (from bottom to 718 top) of 1, 0.1, 0.01, and 0.001 M. Now, the pH value is fixed to 719 pH = 6. For this pH value, the macromolecule is approximately 720 half charged, so it is a suitable value to discuss the influence of charge regulation. The full results for the rest of the pH values 721 (4, 8, and 10) are delivered in the Supporting Information. 722 723 The gauche state probability (Figure 7c,d), the persistence length (Figure 7e,f), degree of protonation (Figure 8a,b), and 724 effective pK value (Figure 8c,d) are also presented. Again, two 725 cases are considered,  $\sigma = 1$  and  $\sigma = 10$ , which correspond to 726 the images on the left side and on the right side, respectively. 727 First, note that the effect of the ionic strength, for the 728 interval of accessible experimental values, is overall weaker 729 than the effect of the pH value. For instance, at F = 1 pN and 730  $\sigma=1$ , the normalized chain extension varies from 0.18 at I=1731  $_{732}$  M to 0.35 at I = 0.001 M (a difference of 0.17 units), and in the case  $\sigma = 10$ , the extension ranges from 0.8 at I = 1 M to 733 0.24 at I = 0.001 M (a difference of 0.16 units). The three 734 force regimes are again observed for all the ionic strengths: the 735 736 entropic regime; the intermediate regime, for which the rotational and ionization degrees of freedom are activated; and 737 738 finally the large-force regime, corresponding to deformations in 739 the bond angle and length. However, unlike the effect of the 740 pH value, the effect of ionic strength on the conformational 741 properties is more complicated due to protonation and the complex interplay between SR and LR interactions. 742

Let us first analyze the dependence of the binding properties r44 on the applied force, depicted in Figure 8. In all the cases,  $\theta$ r45 increases with *F* for forces larger than the low-force regime *F* > r46  $F_{\rm E} \approx 1$  pN. As a general trend, the polyelectrolyte chain is on r47 average more elongated as *F* increases so that the mean r48 distance between sites increases and the LR electrostatic r49 repulsion decreases, allowing more sites to be protonated. r50 Concerning the SR interactions, note that P(g) experiences an important decrease in the interval F = 10-100 pN (see Figure 751 7c,d), which is especially dramatic in the case  $\sigma$  = 10. This fact 752 implies a drastic change in the chemical environment of the 753 ionizable sites, which become separated by trans bonds, 754 through which the repulsion is much weaker. Charge 755 regulation is clearly induced by the mechanical force. 756 Interestingly, the larger the ionic strength, the more intense 757 charge regulation is. Especially remarkable is the case I = 1 M 758 and  $\sigma = 10$  for which the charge is almost doubled at high 759 forces. This indicates that the charging process is basically a 760 local phenomenon, which is essentially driven by SR 761 interactions and the conformational state of the c bonds and 762 is rather independent of the ionic strength. Conversely, LR 763 interactions, which increase on lowering the ionic strength, 764 weaken charge regulation because they discharge the molecule 765 in all the force regimes. In the same way, the effective pK value 766 also increases with the stretching process for  $F > F_{\rm E} \approx 1$  pN, as 767 can be observed in Figure 8c,d, so that a larger affinity for the 768 protons is induced by the applied force. Again, this effect is 769 especially relevant for  $\sigma = 10$  and at high ionic strengths. 770

Concerning the dependence of the *gauche* probabilities on 771 the ionic strength, note that, as observed in Figure 7c,d, P(g) 772 seems to be in contradiction with the behavior of the 773 persistence length. On increasing the ionic strength, P(g) 774 decreases and so does the number of *gauche* bonds, and 775 apparently, the chain should be stiffer. However, for forces 776 below  $F = F_R \approx 20$  pN, the persistence length also decreases, 777 so actually the chain gets more folded. This effect can be 778 observed for the two  $\sigma$  values although it is especially relevant 779 for  $\sigma = 10$ . This apparent paradox can be explained by taking a 780 look at the degree of protonation. As commented above,  $\theta$  781 increases with the ionic strength. As a result, the probability of 782 having two charged neighboring sites increases. Since they 783 cannot be both protonated and linked by a bond in the *gauche* 784



**Figure 9.** Probability of having two neighbor bonds in given conformations  $P(c_ic_{i+1})$  versus *F* at two different ionic strengths of (a, b) I = 1 M and (c, d) I = 0.001 M at constant pH = 6. The combinations shown are both bonds in *trans* P(tt) (blue squares), one bond in *trans* and the neighbor in *gauche* P(tg) (orange circles), both bonds in *gauche* with the same orientation  $P(g^+g^+) + P(g^-g^-)$  (purple upward triangles), and both bonds in *gauche* with the opposite orientation  $P(g^+g^-)$  (green downward triangles). The images on the left side (a and c) correspond to  $\sigma = 1$ , and those on the right side (b and d) refer to  $\sigma = 10$ . The rest of the parameters have the same values as those in Figure 1b.

785 state at the same time  $(u_g = 0)$ , the number of *gauche* states 786 decreases. Note that this effect is due to action of the SR 787 interactions. However, unlike the *gauche* probability, the 788 persistence length is a "global" property, the result of the 789 simultaneous action of many bonds and sites. As a 790 consequence, LR interactions play a more important role in 791 the behavior of  $l_{\rm P}$ . The same argument can be used for the 792 chain elongation, which decreases with the ionic strength in all 793 the curves below for F < 20 pN.

For F > 20 pN, the elongation becomes almost independent 794 of I, but on examining in detail the curves, we can observe an 795 unexpected result: the extension slightly decreases with I. This 796 intriguing trend of the elongation is consistent with the 797 behavior of the persistence length: for  $F < F_{\rm R}$ , the chain gets 798 stiffer on lowering the ionic strength, but, for larger forces, it 799 gets slightly more flexible. For lower pH values, this effect is 800 more visible (as in the curves for pH = 4 shown in the 801 Supporting Information). This certainly small effect seems to 802 be apparently irrelevant but again points out the non-trivial 803 connection between SR and LR interactions. We suspect that 804 this result is related to spatial correlations of the states of 805 neighboring bonds although probably a deeper insight is 806 807 necessary.

As an example of the formation of spatial patterns, the sop probabilities of having two consecutive **c** bonds in a given succonformation  $P(c_ic_{i+1})$  as a function of *F* have been calculated succonformation in the strengths I = 1 M (Figure 9a,b) and I =succonformation M (Figure 9c,d). Again, the images on the left side and succonformation to the cases  $\sigma = 1$  and  $\sigma = 10$ ,

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respectively. Due to the polyelectrolyte symmetry, there are 814 only four different combinations of bond states: both bonds in 815 trans (with a probability P(tt)), one bond in trans and its 816 neighbor in gauche (P(tg)), both bonds in gauche with the 817 same orientation  $(P(g^+g^+) + P(g^-g^-))$ , and both bonds with 818 different orientations  $(P(g^+g^-))$ . As expected, P(tt) monotoni- 819 cally increases as the mechanical force increases and, for large 820 enough forces, P(tt) tends to 1 independent of the value of  $\sigma$ . 821 For  $\sigma = 1$  and I = 0.001 M, the preferred combination is *trans*- 822 gauche at low forces, but there is a crossover, which can be 823 observed at  $F \approx 50$  pN, curiously at the same force interval at  $_{824}$ which the change of tendency in  $l_{\rm p}$  and in the elongation is  $_{825}$ observed. For  $\sigma = 10$ , the preferred combination at low forces 826 is  $g^{\pm}g^{\pm}$ . However, the most intriguing point is the observed  $_{827}$ maximum in P(tg) at  $F \approx 50$  pN. This maximum implies the 828 existence of an intermediate situation where the mechanical 829 work contribution, which promotes the trans state, competes 830 with the energetic stabilization of the gauche states due to the 831 fact that  $\sigma > 1$ . In this force regime, the polyelectrolyte adopts 832 a highly ordered structure, which alternates bonds in the trans 833 state with bonds in the gauche state. Again, the presence of this 834 maximum coincides with the force interval for which  $l_{\rm p}$  and the 835 elongation switch their dependence on the ionic strength. We 836 would like to highlight that, even for the very simple model of 837 polyelectrolyte presented here, one finds a rather rich 838 physical-chemical behavior, which includes charge regulation, 839 complex conformational transitions, and highly correlated 840 spatial structures. 841

#### CONCLUSIONS 842

843 In this work, the influence of charge regulation, highly coupled 844 with the conformational degrees of freedom, in the stretching 845 properties of weak polyelectrolytes is studied. With this aim, 846 we propose a model, which captures the fundamental aspects 847 present in a flexible weak linear polyelectrolyte (internal angle 848 rotation, bond stretching, bond bending, and proton binding) 849 with a minimum number of parameters. The model was 850 inspired by the structure of linear poly(ethylenimine) (LPEI), 851 a symmetric weak polyelectrolyte with an ionizable site every 852 three chain positions. It is based on the site binding rotational 853 isomeric state (SBRIS) model, which allows studying 854 conformational and ionization properties on the same foot. 855 Short-range (SR) and long-range (LR) electrostatic inter-856 actions are treated separately. LR interactions are chemically 857 unspecific and can be reasonably implemented using the mean-858 field Debye-Hückel potential. Conversely, SR interactions 859 between neighboring sites and bonds are mediated by the 860 macromolecular skeleton so that they depend on the detailed chemical environment of the site. As a result, specific energetic 861 parameters are used to describe them. Bond stretching and 862 863 bending are included by means of harmonic potentials. The 864 resulting scheme is used to perform semi-grand canonical 865 Monte Carlo (SGCMC) simulations at constant pH and 866 applied force. Concerning the energy of the gauche state, two 867 situations are studied, controlled by the energy of the gauche ses state (corresponding to the Boltzmann factor  $\sigma$ ): when *trans* so and gauche states have the same energy ( $\sigma = 1$ ) and when the 870 gauche state is energetically stabilized, for instance, by s71 hydrogen bonding (we take  $\sigma = 10$ ). The influence of the 872 pH value and the ionic strength in the force-extension curves 873 is analyzed. In order to understand the different mechanisms of  $_{874}$  chain stretching, the degree of protonation  $\theta$ , bond state probabilities of the gauche state P(g), and persistence length  $l_{\rm P}$ 875 876 as functions of the force are also analyzed.

As a general trend, three force regimes are found. In the low-877 878 force regime, the persistence length is force-independent, and 879 two subregimes are identified. Up to 0.1 pN linear behavior is 880 found, as demanded by the fluctuation-dissipation theorem, 881 for all the pH values. From 0.1 to 1 pN, however, the chain 882 presents Pincus scaling behavior depending on the pH value. 883 For high pH values (i.e., neutral chain), the elongation is still 884 linear with Pincus scaling exponent  $\nu = 1/2$ , while for low pH sss values (fully charged chain),  $\nu = 3/5$ , the theoretically 886 predicted value for strong polyelectrolytes. For intermediate 887 pH values,  $\nu$  has been found to present a gradual transition 888 between the two limiting values. In the large-force regime, 889 most of the bonds are in the trans state so that the stretching 890 becomes approximately independent of the pH and the ionic 891 strength. Finally, there is an intermediate regime, between 1 892 and 100 pN, for which the rotational and protonation degrees 893 of freedom, which are highly coupled, are activated. This force 894 regime is the most interesting one since conformational 895 transitions, charge regulation, and spatial correlations are 896 observed. It is in this force regime that the pH value and the 897 ionic strength maximally influence the chain elongation. 898 Mechanically induced charge regulation is mainly driven by 899 SR interactions. When the macromolecule is elongated, the 900 trans states are promoted so that the electrostatic interaction 901 between neighboring sites decreases, favoring the affinity for 902 the protons. This effect seems to be larger at large ionic

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strengths and pH values for which the molecule is partially 903 charged. 904

The role of the pH value is relatively straightforward to 905 understand. On lowering the pH value, the macromolecule 906 gets charged, promoting trans states and larger distances 907 between sites, thus reducing the electrostatic repulsion. This 908 results in an increase in the persistence length, a reduction in 909 the number of gauche states, and an easier extension of the 910 chain. Therefore, a significant influence of the pH value on the 911 curve–extension curves is found both for  $\sigma = 1$  and  $\sigma = 10$ . 912

On the other hand, the effect of the ionic strength for a fixed 913 pH value is more complicated since it depends on the complex 914 interplay between SR phenomena (bond conformations and 915 protonation) and the LR interactions. It is found that the 916 exhibited tendency of P(g) seems to be in contradiction with 917 the behavior of the persistence length. On increasing the ionic 918 strength, P(g) decreases and so does the number of gauche 919 bonds, and apparently, the chain should be stiffer. However, 920 for forces below  $F = F_{\rm R} \approx 20$  pN, the persistence length also 921 decreases, so the chain gets more folded. This apparent 922 paradox can be solved by observing that the charge decreases 923 on increasing the ionic strength while the intensity of LR 924 interactions is enhanced. Ionization equilibria therefore play a 925 fundamental role in the stretching properties of weak 926 polyelectrolytes. Finally, it is found that in the intermediate- 927 force regime, spatial correlations are formed, which also 928 determine some subtle aspects of the stretching process. 929

We would like to highlight that, even for the very simple 930 model of polyelectrolyte presented here, one finds a rather rich 931 physical-chemical behavior, which includes charge regulation, 932 complex conformational transitions, and highly correlated 933 spatial structures. To our knowledge, this work is the first 934 attempt to study, at least by means of computational 935 simulation, the mechanical stretching of a weak polyelectrolyte 936 including the coupling of charge regulation and conformational 937 equilibria. 938

#### ASSOCIATED CONTENT

### **Supporting Information**

940 The Supporting Information is available free of charge on the 941 ACS Publications website at DOI: 10.1021/acs.macro- 942 mol.9b01160. 943

Full casuistry of chain extension, gauche state probability, 944 persistence length, degree of protonation, and binding 945 equilibrium constant as a function of the mechanical 946 force F, covering the complete range of pH values and 947 ionic strengths (PDF) 948

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