

Effect of Heat Leak and Finite Thermal Capacity on the Optimal Configuration of a Two-Heat-Reservoir Heat Engine for Another Linear Heat Transfer Law

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Abstract: Based on a model of a two-heat-reservoir heat engine with a finite high-temperature source and bypass heat leak, the optimal configuration of the cycle is found for the fixed cycle period with another linear heat transfer law $Q \propto \Delta(T^{-1})$. The finite thermal capacity source without heat leak makes the configuration of the cycle to a class of generalized Carnot cycle. The configuration of the cycle with heat leak and finite thermal capacity source is different from others.

Keywords: Finite Time Thermodynamics, Heat Engine, Optimal Configuration

Introduction

Among the important topics in thermodynamics has been the formulation of criteria for comparing the performance of real and ideal processes. For example, the Carnot cycle provides an upper bound on the efficiency of all cyclic heat engines operating between two fixed temperature heat reservoirs. The work by Clausius, Kelvin, and others carried out in this tradition identified the limits on work, heat transfer, thermodynamic efficiency, COP, energy effectiveness, and energy figure of merit of various energy conversion devices. Since Gibbs, however, the focus has been directed toward state variables rather than the process variables of heat and work. An unavoidable consequence of this shift is the emphasis on equilibrium states and reversible processes. The use of reversible processes as standards

of performance is not desirable because a reversible process must be carried out at an infinitesimal slow pace. Since power produced by a heat engine is work divided by time, a finite amount of work produced by the engine over an infinite time delivers no power. The need to develop a nontrivial amount of power in real energy conversion devices is one reason why the high performance criteria of an ideal, reversible heat engine are seldom approached.

The consequence of incorporating finite-time processes into an otherwise ideal thermodynamic cycle was demonstrated by Novikov [1](1957), Chambadal [2](1957), and Curzon and Ahlborn [3](1975) independently. They considered the case of finite rates of heat transfer to and from a Carnot heat engine. After maximizing the power output, they derived a simple expression for the efficiency that was different from the well-known Carnot efficiency. Their work is commonly referred to as finite-time thermodynamics or entropy generation minimization. Since NCCA's work, many researchers have undertaken the study of irreversible thermodynamic cycles. Some detailed literature surveys of finite time thermodynamics were given by Andresen *et al.* [4], Sieniutycz *et al.* [5, 6], Bejan [7], Hoffmann *et al.* [8], Berry *et al.* [9], Chen *et al.* [10], Wu *et al.* [11] and Salamon *et al.* [12].

Since finite time thermodynamics [1-12] was applied to the performance study of heat engines, a lot of results, which are different from those by using the classical thermodynamics, have been obtained. The performance of the cycle is affected obviously by finiteness of heat capacity of source [13-18] and heat leak [19-22]. The optimal configuration and the fundamental optimal performance of the heat engines [15-18] with a finite high-temperature source are different from those with an infinite high-temperature source [23-25]. However, heat leak changes the relations between the optimal power output and the efficiency [19-22]. For the endoreversible cycle, the research into the effects of a finite heat reservoir on the performance includes two aspects. The first is to determine the optimal performance of the finite thermal capacity cycles, such as Carnot cycle [15,18], Rankine cycle [16] and Brayton cycle [17], etc. Optimization may be carried out with fixed heat input [18] or with variable heat input [15-17]. The second is to determine the optimal configuration of these heat engines with the given conditions. For example, the optimal configuration of an endoreversible constant-temperature heat reservoir heat engine is the Curzon-Ahlborn engine [23], and the optimal configuration of Newton's law system variable-temperature heat reservoir heat engine is a generalized Carnot heat engine [13] (in which the temperature of the heat reservoirs and the working fluid change exponentially with time and the ratio of the temperatures of the working fluid and the heat reservoir is a constant). The optimal configuration of linear phenomenological law system variable-temperature heat reservoir heat engine is another generalized Carnot cycle [14] (in which the difference of reciprocal temperatures of the heat reservoirs and the working fluid is a constant). In this paper, we will investigate the latter. In general, heat transfer is not necessarily linear and also obeys other law, such as another linear heat transfer law $Q \propto \Delta(T^{-1})$, thermal radiation law $Q \propto \Delta(T^4)$, etc.. Therefore, a further discussion on the effect of heat transfer law on cycle is necessary. Some authors have assessed the effect of the heat transfer law on the performance of endoreversible and irreversible heat engines [14, 21, 26]. On the basis of these research work, a heat engine model with heat leak and finite heat capacity source is founded, and the optimal configuration of the maximum power output of a cycle is obtained under a given cycle time with another linear heat transfer law $Q \propto \Delta(T^{-1})$. From

the established model, we obtain the optimal configurations and the fundamental optimal performance of the cycle for four cases.

Physical Model

The system adopted is a working fluid alternately connected to a high-temperature heat source with finite heat capacity and to a low-temperature heat sink with infinite heat capacity. The heat engine operates in a cycle fashion with fixed time τ allotted for each cycle. There exists a direct bypass heat leak between the finite heat source and the infinite heat sink. This system to be considered in this paper is shown schematically in Fig.1. The high-temperature heat source is assumed to have constant heat capacity C , its temperature is given by $T_x(t)$, and its initial temperature is given by T_H . The low-temperature heat sink is assumed for simplicity to be infinite in size and therefore it has a fixed temperature T_L . The rate of heat leak is assumed to be proportional to the difference of reciprocal temperatures of the heat source and heat sink. The temperature of the working fluid is $T(t)$. The absorbed and released heats of the working fluid are Q_{HC} and Q_{LC} , respectively. The heat leak from high-temperature heat source to low-temperature heat sink is Q_i .

The two steps in the cycle during which the working fluid is disconnected from one reservoir and connected to the other are taken to be reversibly adiabatic. It is assumed that these steps occur instantaneously which implies that the temperature of the working fluid changes discontinuously.

We assume that the heat transfer between the reservoirs and the working fluid and the heat leak between two heat reservoirs obey another linear law [$Q \propto \Delta(T^{-1})$]

$$Q_{HC} = \int_0^\tau \alpha(t)[1/T(t) - 1/T_x(t)]dt \quad (1)$$

$$Q_{LC} = \int_0^\tau \beta(t)[1/T_L - 1/T(t)]dt \quad (2)$$

$$Q_i = \int_0^\tau \gamma(t)[1/T_L - 1/T_x(t)]dt \quad (3)$$

$$Q_H = Q_{HC} + Q_i, \quad Q_L = Q_{LC} + Q_i \quad (4)$$

where Q_H is the real heat supply, Q_L is the real heat release, Q_i is the heat leak, $\alpha(t)$ is the thermal conductivity for heat transfer between the high-temperature heat source and working fluid, $\beta(t)$ is the thermal conductivity for heat transfer between the working fluid and the low-temperature heat sink, and $\gamma(t)$ is the thermal conductivity for heat leak between the heat source and the heat sink through the heat engine plant. We shall assume that at $t=0$ the working fluid is in contact with high-temperature heat source and is separated from the low-temperature heat sink by an adiabatic boundary. At a later time t_1 ($0 < t_1 < \tau$), contact with the heat source is broken and the working fluid is placed in contact with the heat sink. The heat leak is continuous during the cycle period. Therefore, we write $\alpha(t)$, $\beta(t)$ and $\gamma(t)$ as

$$\alpha(t) = \begin{cases} \alpha & 0 \leq t \leq t_1 \\ 0 & t_1 < t \leq \tau \end{cases} \tag{5}$$

$$\beta(t) = \begin{cases} 0 & 0 \leq t \leq t_1 \\ \beta & t_1 < t \leq \tau \end{cases} \tag{6}$$

$$\gamma(t) = \begin{cases} \gamma & 0 \leq t \leq t_1 \\ \gamma & t_1 < t \leq \tau \end{cases} \tag{7}$$

where α, β and γ are constants.

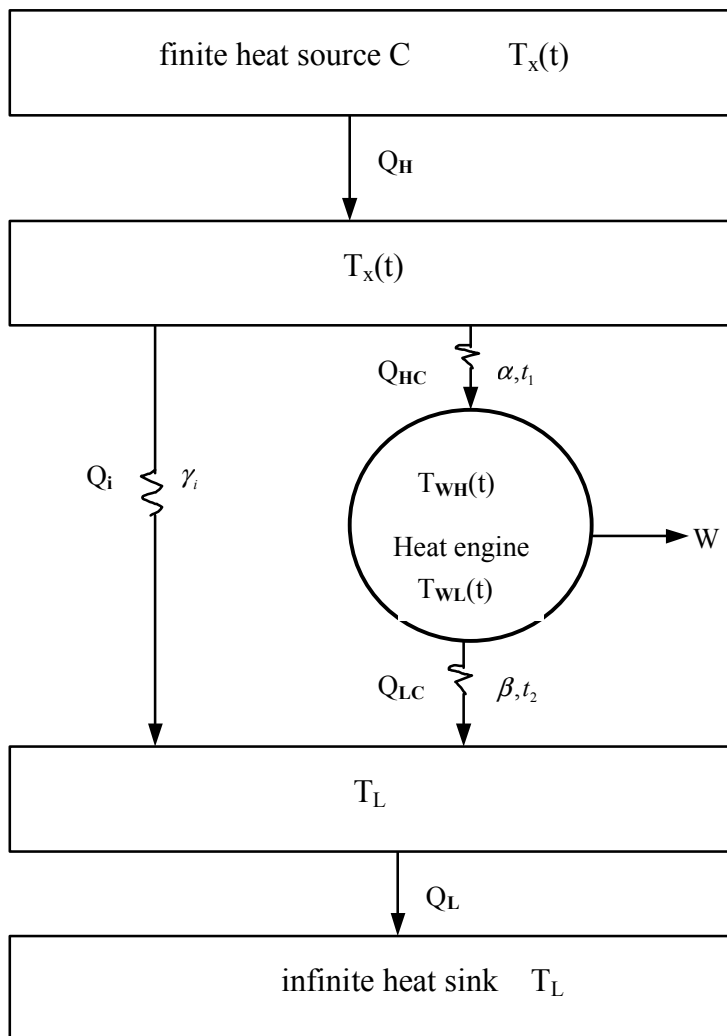


Fig1. Power cycle model

From the first law of thermodynamics and equation (4), the work output from the cycle is

$$\begin{aligned} W &= Q_H - Q_L = Q_{HC} - Q_{LC} \\ &= \int_0^\tau \{ \alpha(t)[1/T(t) - 1/T_x(t)] - \beta(t)[1/T_L - 1/T(t)] \} dt \end{aligned} \tag{8}$$

whereas from the second law of thermodynamics, the entropy change of the working fluid per cycle is

$$\begin{aligned} \Delta S &= \int_0^\tau \left[\frac{Q_{HC}}{T(t)} - \frac{Q_{LC}}{T(t)} \right] dt \\ &= \int_0^\tau \{ \alpha(t) \{ 1/T^2(t) - 1/[T_x(t)T(t)] \} - \beta(t) \{ 1/[T_L T(t)] - 1/T^2(t) \} \} dt = 0 \end{aligned} \tag{9}$$

Furthermore, since the heat capacity of the high-temperature heat source is assumed to be constant, we have

$$dQ_H = -CdT_x(t) \tag{10}$$

Combining equations (1), (3), (4) and (10), we obtain the constraint equation on the time rate of change of the temperature of the high-temperature heat source in the following equation

$$C\dot{T}_x(t) + \alpha(t)[1/T(t) - 1/T_x(t)] + \gamma(t)[1/T_L - 1/T_x(t)] = 0 \tag{11}$$

where $\dot{T}_x(t) = dT_x(t)/dt$.

Optimal Configuration

Our problem now is to determine the optimal configuration of the model cycle in which the maximum work output is obtained under a given cycle time τ . For given α , β , γ , T_H and T_L , $T(t)$ and t_1 must be determined. So using equations (8) and (11), we obtain the modified Lagrangian:

$$\begin{aligned} L &= \alpha(t)[1/T(t) - 1/T_x(t)] - \beta(t)[1/T_L - 1/T(t)] + \\ &\quad \lambda \{ \alpha(t) \{ 1/T^2(t) - 1/[T_x(t)T(t)] \} - \beta(t) \{ 1/[T_L T(t)] - 1/T^2(t) \} \} + \\ &\quad \mu(t) \{ C\dot{T}_x(t) + \alpha(t)[1/T(t) - 1/T_x(t)] + \gamma(t)[1/T_L - 1/T_x(t)] \} \end{aligned} \tag{12}$$

where λ is Lagrangian constant, $\mu(t)$ is a function of time. The path for the working fluid which results in the maximum work for a given time interval $\{0, \tau\}$ may now be obtained from the solution to the Euler-Lagrange equation. The Euler-Lagrange equations are given by

$$\frac{\partial L}{\partial T} - \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{T}} \right) = 0 \tag{13}$$

$$\frac{\partial L}{\partial T_x} - \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{T}_x} \right) = 0 \tag{14}$$

Substituting equation (12) into equations (13) and (14) yields

$$\alpha(t) + \beta(t) + \lambda \{ \alpha(t)[2/T(t) - 1/T_x(t)] + \beta(t)[2/T(t) - 1/T_L] \} + \mu(t)\alpha(t) = 0 \tag{15}$$

$$\alpha(t) + \lambda\alpha(t)/T(t) + \mu(t)[\alpha(t) + \gamma(t)] - CT_x^2(t)\dot{\mu}(t) = 0 \tag{16}$$

Substituting equations (5)-(7) into equations (15) and (16) yields

$$\alpha \{ 1 + \lambda[2/T_{WH}(t) - 1/T_x(t)] + \mu(t) \} = 0 \quad 0 \leq t \leq t_1 \tag{17}$$

$$\alpha + \lambda\alpha / T_{WH}(t) + \mu(t)(\alpha + \gamma) - CT_x^2(t)\dot{\mu}(t) = 0 \quad 0 \leq t \leq t_1 \quad (18)$$

and

$$\beta\{1 + \lambda[2 / T_{WL}(t) - 1 / T_L]\} = 0 \quad t_1 < t \leq \tau \quad (19)$$

$$\mu(t)\gamma - CT_x^2(t)\dot{\mu}(t) = 0 \quad t_1 < t \leq \tau \quad (20)$$

The optimal configuration solution may be obtained from equations (11) and (17)-(20) for the following four heat engine cycles.

When $t_1 \leq t < \tau$, $T_{WL}(t) = \text{constant}$, solving equations (11) and (19) gives

$$[T_L - T_x(t)] \exp[T_x(t) / T_L] = [T_L - T_x(t_1)] \cdot \exp\{[T_x(t_1)T_L + \gamma(t - t_1) / C] / T_L^2\} \quad (21)$$

where $T_x(t_1)$ is the temperature of high-temperature heat source at time $t = t_1$, and is determined by equations (24) discussed bellow.

Equation (21) shows that the isothermal heat transfer is executed between the low-temperature heat sink and the working fluid. Despite that the working fluid does not come into contact with high-temperature heat source, the temperature of the high-temperature heat source $T_x(t)$ decreases with time after t_1 because of the heat leak from the high-temperature heat source to the low-temperature heat sink. The temperature of the high-temperature heat source can be obtained by using Equation (21) for $t = \tau$.

When $0 \leq t < t_1$, solving equation (17) gives $\mu(t)$, and then we have

$$\dot{\mu}(t) = \lambda[2\dot{T}_{WH}(t) / T_{WH}^2(t) - \dot{T}_x(t) / T_x^2(t)] \quad (22)$$

From equation (11), we have

$$\frac{1}{T_x(t)} - \frac{1}{T_{WH}(t)} = \frac{C}{\alpha} \dot{T}_x(t) + \frac{\gamma}{\alpha} \left[\frac{1}{T_L} - \frac{1}{T_x(t)} \right] \quad (23)$$

Substituting equations (22) and (23) into equation (18) yields the differential equation about $T_x(t)$ and $T_{WH}(t)$ as following

$$\frac{2\dot{T}_{WH}(t)}{T_{WH}^2(t)} - \frac{\dot{T}_x(t)}{T_x^2(t)} = \left(1 + \frac{2\gamma}{\alpha}\right) \frac{\dot{T}_x(t)}{T_x^2(t)} - \frac{2\gamma(\alpha + \gamma)}{C\alpha} \frac{1}{T_x^3(\alpha + \gamma)} + \frac{\gamma(\alpha + 2\gamma)}{C\alpha T_L T_x^2(t)} - \frac{\gamma}{C\lambda} \frac{1}{T_x^2(t)} \quad (24)$$

The numerical solution of $T_x(t)$ and $T_{WH}(t)$ may be obtained using equations (11) and (24) with the initial condition of $T_x(0) = T_H$. Then, $T_x(t_1)$ is obtained, and $T_x(t)$ in the time interval $\{t_1, \tau\}$ is determined using $T_x(t_1)$ and equations (21). Equation (24) could include equation of all kinds of the character of heat engine cycle.

Special Cases

Case 1. Infinite high- and low- temperature reservoirs without heat leak

If the heat engine cycle is coupled with infinite reservoirs without heat leak, $\gamma = 0$ and C

approaches infinite large. Therefore the solution of equation (19) is

$$T(t) = T_{wL}(t) = \text{constant} \quad t_1 < t \leq \tau \quad (25)$$

From equation (18) we have $\mu(t) = \text{constant}$. From equation (11) we obtain $T_x(t) = \text{constant} = T_H$. Substituting $T_x(t)$ into equation (17) yields $T(t) = T_{wH}(t) = \text{constant}$, $0 \leq t \leq t_1$. The optimal cycle is composed of two isothermal and two adiabatic processes. This is an endoreversible Carnot heat cycle, i.e., NCCA cycle [1-3]. The fundamental relation between optimal power output and efficiency of the endoreversible Carnot cycle is given by [26]

$$P = \alpha \frac{(1-\eta)/T_L - 1/T_H}{[1 + \sqrt{\alpha/\beta}(1-\eta)]^2} \quad (26)$$

where $P = W/\tau$, is the power output, $\eta = 1 - W/Q_H$, is the efficiency. The power versus efficiency character is similar to a parabola, as shown in Fig.2.

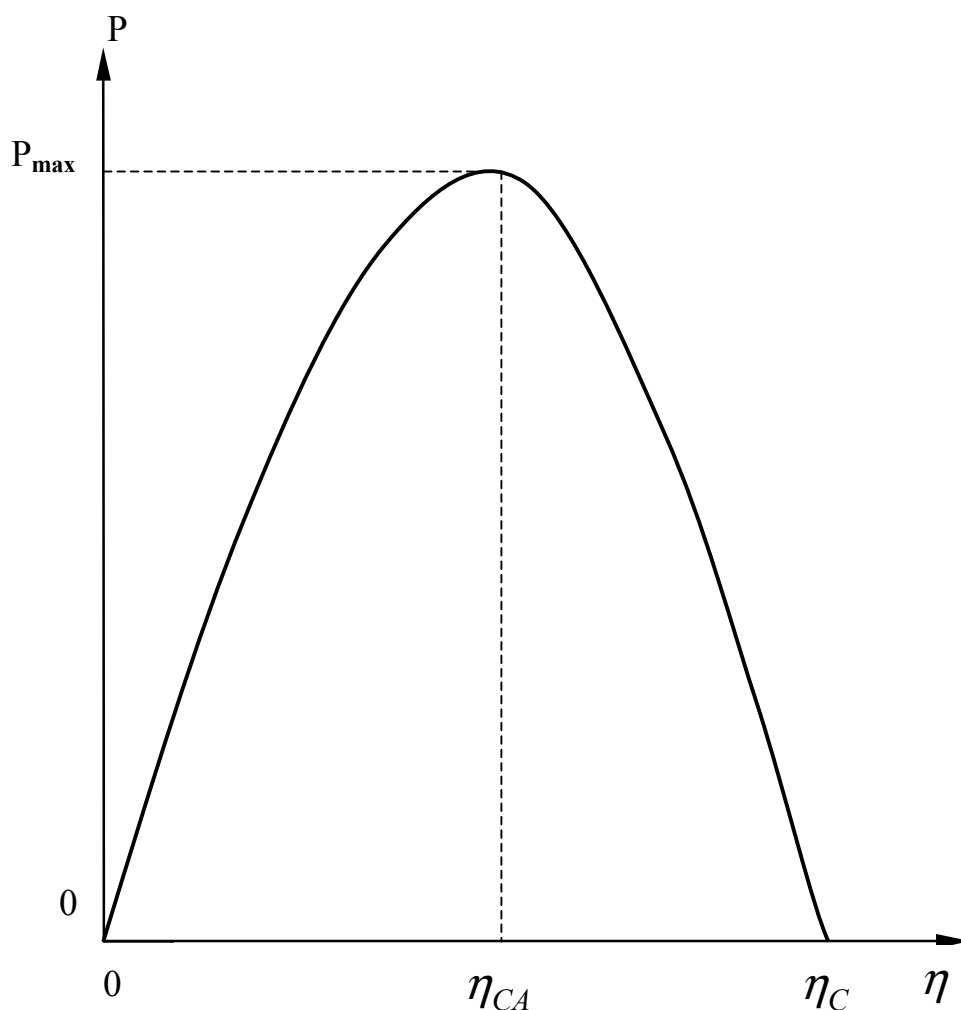


Fig. 2. Power versus efficiency characteristics of the endoreversible or generalized endoreversible Carnot engine without heat leak

Case 2. Infinite high- and low- temperature reservoirs with heat leak

This cycle model is similar to that adopted by Bejan [19] except that the cycle contacts with reservoirs alternatively instead of simultaneously. In this case, γ is finite and C approaches infinite large. The optimal configuration solution is the same as the case 1, which is an endoreversible Carnot heat engine cycle. The fundamental relation between optimal power and efficiency of an endoreversible Carnot heat engine cycle with bypass heat leak is given by [20]

$$P\eta^{-1} - Q_i = \alpha \{1/T_H - 1/T_L \{ (P\eta^{-1} - Q_i) / [P(\eta^{-1} - 1) - Q_i] \}^{-1} \} / \{ 1 + (\alpha/\beta)^{0.5} \{ [P(\eta^{-1} - 1) - Q_i] / (P\eta^{-1} - Q_i) \} \}^2 \tag{27}$$

where $Q_i = \gamma(1/T_L - 1/T_H)$. The power versus efficiency curve exhibits a loop-shaped one, i.e., there exist a maximum power output point and a maximum efficiency point, as shown in Fig.3. Despite the fact that the cycles have the same configuration, the power versus efficiency characteristics in this case is very different from that in the case 1.

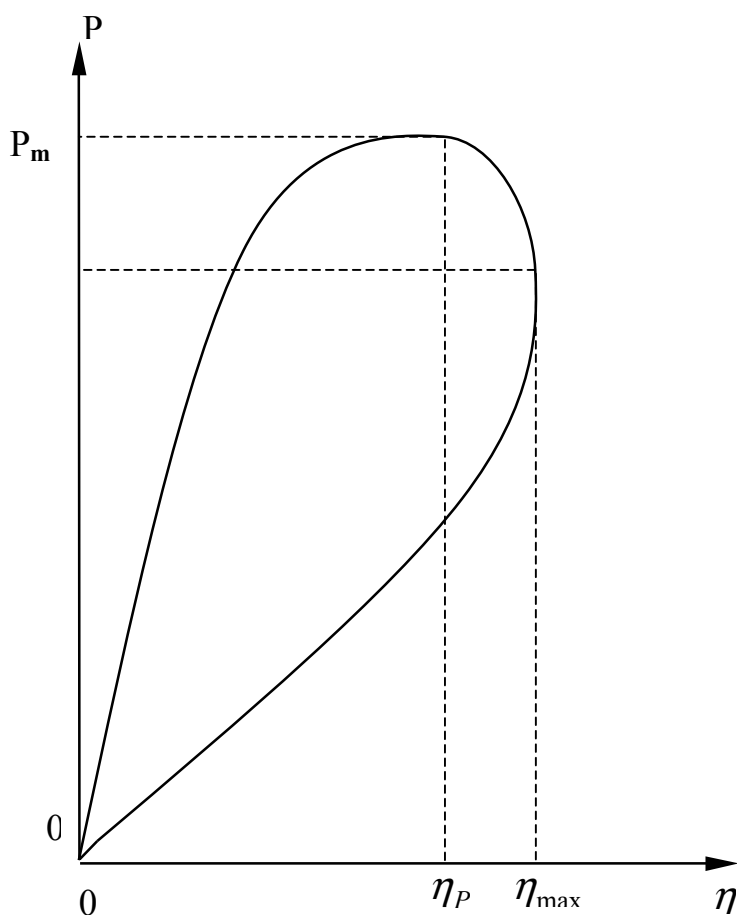


Fig.3 Power versus efficiency characteristics of the endoreversible Carnot engine with heat leak

Case 3. Finite high-temperature source and infinite low-temperature sink without heat leak

In this case, $\gamma = 0$ and C is finite. From equation (19), we obtain $T_{wL}(t) = \text{constant}$ when $t_1 < t \leq \tau$.

From equations (10), (11), (17) (18) and (19) we obtain

$$T_{wL}(t) = \text{constant} \quad t_1 < t \leq \tau \tag{28}$$

$$1/T_{wH}(t) - 1/T_x(t) = a \quad 0 \leq t \leq t_1 \tag{29}$$

$$T_x(t) = T_H - (\alpha/C)at \quad 0 \leq t \leq t_1 \tag{30}$$

From equations (28), (29), and (30) we obtain

$$T(t) = \begin{cases} \frac{T_H - (\alpha/C)at}{1 + T_H a - (\alpha/C)a^2 t} = T_{wH}(t) & 0 \leq t \leq t_1 \\ \frac{T_L}{1 - bT_L} = T_{wL}(t) = \text{const} & t_1 < t \leq \tau \end{cases} \tag{31}$$

where a and b are constants. Equations (30) and (31) indicate that the temperature of the high-temperature heat source and the working fluid is a function of time in the time interval $\{0, t_1\}$, and the temperatures of the working fluid and heat sink are constants. This configuration is the same as the heat engine configuration obtained by Yan [14] when $\alpha = \beta$ and can be called as a generalized endoreversible Carnot heat engine cycle. The fundamental optimal formula of a generalized endoreversible Carnot cycle can be derived as following [14]

$$P = \alpha \frac{(1 - \eta) / T_L - A / T_H}{[1 + \sqrt{\alpha / \beta} (1 - \eta)]^2} \tag{32}$$

where $A = -(CT_H / Q_{HC}) \ln[1 - Q_{HC} / (CT_H)]$.

Since A in equation (32) being a function of Q_{HC} , therefore the fundamental optimal formula is related to the given Q_{HC} . It is independent of Q_{HC} only if C approaches infinite. For a given Q_{HC} , the power output versus efficiency curve is similar to that shown in Fig.2.

Discussion

Comparing equation (24) with equation (29) we see that the heat leak change not only the value of $T_x(t)$ and $T_{wH}(t)$ at $t = t_1$ but also the relation between the temperatures of working fluid and the high-temperature heat source during the time interval $\{0, t_1\}$. If and only if the cycle is without heat leak, $\gamma = 0$, equation (24) becomes equation (29), and the cycle configuration is the same as that in Case 3, i.e., a generalized endoreversible Carnot heat engine cycle. The optimal cycle configuration with heat leak is as follows. When the working fluid contacts with the high-temperature heat source during the time interval $\{0, t_1\}$, the temperature of the heat sink is constant, while the temperature of

the working fluid and the high- temperature heat source decrease with time according to special law, and the relation between the temperatures of working fluid and the heat source is complex and must be determined by solving equations (11) and (24) numerically. When the working fluid contacts with the low-temperature heat sink during the time interval $\{t_1, \tau\}$, the temperatures of both the heat sink and the working fluid are constants, while the temperature of the high-temperature heat source decreases with time from $T_x(t_1)$ to $T_x(\tau)$ in the light of equation (21); At $t = t_1$ and $t = \tau$, the temperature distribution of the working fluid jumps adiabatically. Therefore, the optimal configuration is neither the endoreversible Carnot heat engine cycle nor the generalized endoreversible Carnot heat engine cycle.

Conclusion

In practice, heat reservoirs are generally of finite size with finite heat capacity and the heat leak always exists in the heat engine plant. Thus the problem of optimal configuration from which the maximum power is obtained with finite heat capacity and with heat leak is of practical. At the same time, the optimal configuration of the heat engine is of significance with another linear heat transfer law. The results include four special cases. Comparing the optimal configuration with that for an endoreversible heat engine cycle with infinite capacity without heat leak at the same transfer law $Q \propto \Delta(T^{-1})$, we know that the existence of heat leak dose not change the optimal configuration but change the power versus efficiency characteristics of the cycle with infinite heat capacity. The finite heat capacity makes the cycle without heat leak become a generalized Carnot heat engine cycle. There is a big difference of optimal configurations for the finite heat capacity cycle with heat leak and the former three cases. This paper demonstrates the importance of finite size and finite heat capacity of heat reservoirs and the heat leakage upon the maximum power, the maximum efficiency, and the nature of the optimum cycle for the heat engine plant operated in finite time. Comparing with the results of Newton's heat transfer law, we can know that heat transfer law has also different effect on the four special configurations of the cycle.

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