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# Effect of information leakage and method of splitting (rational and random) on external predictive ability and behavior of different statistical parameters of QSAR model 

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#### Abstract

Quantitative Structure-Activity Relationship not only provides guidelines regarding structural features responsible for biological activity but it can be used also for prediction of desired activity prior to synthesis of untested chemicals. Therefore, an appropriate validation of any QSAR is of utmost importance to judge its external predictive ability. Generally, internal and external validations (preferred by many) are used in the absence of a true external dataset. The model developed using external method may not be reliable as it may not capture all essential features required for the particular SAR due to omission of some compounds, especially for small datasets. In external validation, the splitting is done either rationally


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[^1]or in random manner before descriptor selection. In the present study, rational splitting of dataset was performed using a novel method and its effect on statistical parameters was analyzed. The analysis reveals that the predictive ability of a QSAR model is sensitive toward (1) the method of splitting and (2) distribution of the training and the prediction sets. In addition, purposeful selection can be used to influence the statistical parameters; therefore, external validation based on single split is insufficient to guarantee the true predictive ability of a QSAR model. Besides, it appears that the selection of descriptors prior to splitting (information leakage) has little role to play in deciding external predictivity of the model. The present study reveals that as many as possible statistical parameters should be examined along with boot-strapping instead of single external validation.

Keywords QSAR • External validation •
Statistical parameters • Splitting methods • Predictivity

## Introduction

Under the umbrella of modern drug designing, Computer Assisted Drug Designing (CADD) is the method of choice due to faster, cheaper, and result-oriented analysis (Kubinyi, 2002; Van Drie, 2007; Yuriev et al., 2011). Over the years, CADD has matured with the advent of new techniques, algorithms, and software programs. Quantitative Structure-Activity Relationship (QSAR), molecular docking, pharmacophore modeling, etc. are thriving techniques from the tenant of CADD. Of these, QSAR has gained much attention because of its applicability in risk assessment, toxicity prediction, and regulatory decisions apart from drug discovery and lead optimization. Further



Metamitron
(Sugar-beet Herbicide)
Bayer 1975
Norfloxacin
(Antibacterial agent)
Kyorin 1983
Bromobutide
(Paddy Field Herbicide)
Sumitomo 1984


Flobufen
(Long-acting Anti-inflamatory)
Kuchar et al 2000


Lomerizine
(Antimigrane, Antiglaucoma) Organon Japan-Upjohn 1999


Metconazole
(Wheat Fingicife) Kureha 1994

Fig. 1 Some of the commercial drugs developed with the aid of QSAR
application of QSAR models includes prediction of desired activity/property for a molecule before its synthesis and testing (Mahajan et al., 2012, 2013; Masand et al., 2012, 2010, 2013). In last decades, QSAR has contributed significantly in bringing many successful drugs in the market (see Fig. 1) (Selassie, 2003).

Therefore, QSAR models are routinely built to establish the statistical correlation between structural features (independent or predictor variables) that govern the biological activity or a physico-chemical property (dependent variable) (Scior et al., 2009). The four main steps involved in QSAR model building are (1) Structure drawing and geometry optimization, (2) calculation of myriad number of descriptors, (3) generation of model using least (optimal) number of descriptors, and (4) appropriate validation of mathematical model (Tropsha, 2010). The success of any QSAR model depends on various factors like accuracy of the experimental (input) data, selection of appropriate number and type of descriptors, statistical method (or algorithms), and most significantly on apposite validation of the developed model (see Fig. 2) (Huang and Fan, 2011). The utility of a QSAR model depends on its ability to predict accurately for unknown chemicals with some known degree of certainty (Roy et al., 2008). The prediction ability is a crucial aspect related to appropriate validation of the QSAR models. A QSAR model is considered appropriately statistically validated if it possesses good
internal and external predictive ability, such models are successful in predicting the activity/property of unknown chemical (Scior et al., 2009; Tropsha, 2010).

Recently, appropriate validation of QSAR model is under hot debate. For thriving QSAR models, validation must be primarily for statistical robustness, prediction abilities, and applicability domain of the models (Sahigara et al., 2012, 2010). There are two standard ways of doing this (1) internal validation (2) external validation (Hawkins et al., 2003). These are performed in five different ways: leave-one-out cross-validation, leave-many-out cross-validation, Y-randomization, bootstrapping (least known among the five), and external validation (Hawkins et al., 2003; Kiralj and Ferreira, 2009).

The widely accepted parameter $Q^{2}$ (also symbolized as $R_{\mathrm{cv}}^{2}, r_{\mathrm{cv}}^{2}, q^{2}$, and $Q_{\mathrm{LOO}}^{2}$ ) for internal validation is calculated by the formula (Consonni et al., 2010; Todeschini et al., 2004):
$\mathrm{Q}^{2}=1-\frac{\sum_{\mathrm{i}=1}^{\mathrm{n}}(\widehat{\mathrm{y}} \mathrm{i}-\mathrm{yi})^{2}}{\sum_{\mathrm{i}=1}^{\mathrm{n}}(\mathrm{yi}-\bar{y})^{2}}$.
Internal validation, a statistical method regularly performed using leave-one-out or by leave-many-out cross-validation, leads to an overestimation of predictive


Fig. 2 Flowchart diagram for the methodology used in present study
capacity in many instances. But, it is useful for verification of robustness of the model. Therefore, internal validation may not be sufficient for validation, but it is essential (Consonni et al., 2010; Golbraikh and Tropsha, 2002; Gramatica, 2013; Tropsha, 2010). It is still useful, especially, when the dataset is small or of modest size (Hawkins et al., 2003).

On the other hand, external validation involves splitting the available data into training (or learning) and test (or prediction) sets. For external validation, selection of proper size of training and prediction sets is very crucial (Kiralj and Ferreira, 2009; Roy et al., 2008). Generally, this splitting is performed using random division, but purposeful or rational splitting for selection of compounds whose chemistry covers the whole (or maximum) population, but does not introduce any bias is a good idea (Hawkins et al., 2003). Rational or purposeful splitting methods can divide datasets into training and prediction sets in an intelligent fashion (Martin et al., 2012). Different algorithms like Kennard-Stone, minimal prediction set dissimilarity, and sphere exclusion algorithms have been developed for smarter way of dividing the datasets into training and prediction sets with the aim of producing more predictive models (Chirico and Gramatica, 2012; Consonni et al., 2010; Gramatica 2013; Huang and Fan 2011; Kiralj and Ferreira 2009; Martin et al., 2012; Scior et al., 2009). Even though, earlier studies have pointed out the superiority of rational division algorithms over the simple random splitting and activity sorting methods. Yet, appropriate selection of rational division method is still unclear because of the conflicting results (Huang and Fan 2011). Recent literature survey indicates that the method/
algorithm of choice for splitting has little influence on the statistical performance of a QSAR model. Recently, Martin and co-workers reported the influence of rational selection of training and prediction sets on the model's predictivity (Martin et al., 2012). However, if the prediction set is small, unknowingly, the researcher may get a prediction set for which the developed model might show a high predictive ability (Baumann and Stiefl, 2004; Chirico and Gramatica, 2012; Consonni et al., 2009; Consonni et al., 2010; Hawkins, 2004; Huang and Fan, 2011; Martin et al., 2012; Scior et al., 2009; Todeschini et al., 2004; Tropsha, 2010).

The aim of the present study is to compare the statistical performance of different algorithms of rational selection, and to study the effect of descriptors selection prior to splitting (information leakage) on the external predictive ability of the model. In addition, the aim of the present study is to devise, evaluate, and compare a novel nonalgorithmic method for rational splitting that influences the statistical parameters of QSAR model.

## Experimental section

Datasets

For the present study, three datasets of varying size are used. The first dataset consists of forty-four N -Phenyl Ureidobenzenesulfonate Derivatives (N-PUSs) with wide variety of substituents present at different positions, as shown in Table 1, was selected from the literature (Turcotte et al., 2012). The activities of these compounds

Table 1 Substituted N-Phenyl Ureidobenzenesulfonate derivatives along with $-\log \mathrm{IC}_{50}\left(p \mathrm{IC} \mathrm{C}_{50}\right)$ and descriptor values

| S. no. | X | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\begin{aligned} & p \mathrm{IC}_{50}(\mathrm{M}) \\ & (\mathrm{HT}-29) \end{aligned}$ | $\begin{aligned} & \mathrm{F} 07 \\ & {[\mathrm{C}-\mathrm{N}]} \end{aligned}$ | $\begin{aligned} & \mathrm{F} 05 \\ & {[\mathrm{C}-\mathrm{C}]} \end{aligned}$ | Mor29e | Mor03m | RDF095v |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | O | 4-OH | 4-CEU | 5.824 | 1 | 12 | 0.728 | -3.81 | 1.503 |
| 2 | O | $2-\mathrm{Me}$ | 3-CEU | 4.481 | 2 | 13 | 0.04 | -5.025 | 5.266 |
| 3 | O | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 3-CEU | 5.367 | 2 | 14 | 0.283 | -5.342 | 3.314 |
| 4 | O | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 3-CEU | 4.824 | 2 | 16 | 0.04 | -4.293 | 5.093 |
| 5 | O | $4-\mathrm{OH}$ | 3-CEU | 3.921 | 2 | 12 | 0.408 | -4.627 | 4.138 |
| 6 | O | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 4-CEU | 4.770 | 1 | 14 | 0.246 | -2.51 | 1.679 |
| 7 | O | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 4-CEU | 5.602 | 1 | 16 | 0.249 | -4.542 | 3.791 |
| 8 | NH | 2-Me | 3-CEU | 4.149 | 2 | 13 | 0.044 | -5.776 | 5.265 |
| 9 | NH | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 3-CEU | 4.319 | 2 | 14 | 0.003 | -4.2 | 3.792 |
| 10 | NH | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 3-CEU | 4.824 | 2 | 16 | -0.015 | $-5.66$ | 6.562 |
| 11 | NH | $2-\mathrm{Me}$ | 4-CEU | 4.260 | 2 | 13 | -0.056 | -4.842 | 4.379 |
| 12 | NH | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 4-CEU | 4.398 | 2 | 14 | -0.199 | -4.036 | 3.316 |
| 13 | NH | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 4-CEU | 4.678 | 2 | 16 | -0.109 | -5.379 | 4.276 |
| 14 | O | $2-\mathrm{Me}$ | 3-CPU | 4.678 | 2 | 13 | -0.099 | -4.91 | 4.18 |
| 15 | O | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 3-CPU | 4.638 | 2 | 14 | 0.057 | -5.709 | 3.351 |
| 16 | O | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 3-CPU | 4.854 | 2 | 16 | 0.09 | -4.777 | 5.737 |
| 17 | O | $4-\mathrm{OH}$ | 3-CPU | 4.292 | 2 | 12 | 0.371 | -3.81 | 3.557 |
| 18 | O | $2-\mathrm{Me}$ | 4-CPU | 4.585 | 1 | 13 | 0.026 | -3.933 | 2.952 |
| 19 | O | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 4-CPU | 4.824 | 1 | 14 | 0.1 | -4.001 | 2.835 |
| 20 | O | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 4-CPU | 4.886 | 1 | 16 | -0.033 | -4.132 | 4.372 |
| 21 | O | $4-\mathrm{OH}$ | 4-CPU | 4.301 | 1 | 12 | 0.137 | -3.322 | 2.426 |
| 22 | NH | $2-\mathrm{Me}$ | 3-CPU | 4.377 | 2 | 13 | 0.144 | -4.557 | 4.698 |
| 23 | NH | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 3-CPU | 4.018 | 2 | 14 | $-0.233$ | -5.079 | 4.639 |
| 24 | NH | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 3-CPU | 4.824 | 2 | 16 | $-0.265$ | -5.077 | 5.298 |
| 25 | NH | 2-Me | 4-CPU | 4.194 | 2 | 13 | -0.247 | -2.874 | 2.342 |
| 26 | NH | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 4-CPU | 4.585 | 2 | 16 | -0.199 | -5.308 | 4.241 |
| 27 | O | 2-Me | 4-CEU | 5.328 | 1 | 13 | 0.182 | -4.774 | 3.14 |
| 28 | O | $2-\mathrm{Me}$ | 3-EU | 4.357 | 2 | 13 | 0.048 | -3.826 | 3.679 |
| 29 | O | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 3-EU | 4.481 | 2 | 14 | 0.123 | -3.92 | 3.658 |
| 30 | O | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 3-EU | 4.602 | 2 | 16 | 0.064 | -4.152 | 5.884 |
| 31 | O | $4-\mathrm{OH}$ | 3-EU | 4.125 | 2 | 12 | 0.245 | -3.361 | 3.747 |
| 32 | O | 2-Me | 4-EU | 4.921 | 1 | 13 | 0.226 | -3.517 | 2.458 |
| 33 | O | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 4-EU | 4.921 | 1 | 14 | 0.289 | -3.603 | 2.334 |
| 34 | O | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 4-EU | 5.620 | 1 | 16 | 0.179 | -3.78 | 3.85 |
| 35 | O | $4-\mathrm{OH}$ | 4-EU | 4.921 | 1 | 12 | 0.275 | -2.822 | 2.042 |
| 36 | O | 3-Me | 4-CEU | 5.143 | 1 | 12 | 0.179 | -5.158 | 2.729 |
| 37 | NH | $2-\mathrm{Me}$ | 3-EU | 3.991 | 2 | 13 | 0.114 | -4.003 | 5.481 |
| 38 | NH | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 3-EU | 4.824 | 2 | 14 | -0.077 | -3.948 | 3.99 |
| 39 | NH | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 3-EU | 4.387 | 2 | 16 | -0.121 | -3.772 | 4.862 |
| 40 | NH | $2-\mathrm{CH}_{2}-\mathrm{CH}_{3}$ | 4-EU | 4.066 | 2 | 14 | -0.106 | -3.638 | 2.681 |
| 41 | NH | $2-\left(\mathrm{CH}_{2}\right)_{2}-\mathrm{CH}_{3}$ | 4-EU | 4.495 | 2 | 16 | -0.179 | -3.383 | 3.517 |
| 42 | O | 4-Me | 4-CEU | 4.523 | 1 | 12 | 0.411 | -2.191 | 3.995 |
| 43 | O | 4-OMe | 4-CEU | 4.745 | 1 | 13 | 0.579 | -3.646 | 2.832 |
| 44 | O | $4-\mathrm{N}(\mathrm{Me})_{2}$ | 4-CEU | 4.409 | 2 | 14 | 0.274 | $-3.852$ | 5.562 |

$C E U$ 2-chloroethylurea, $C P U$ 3-chloropropylurea, $E U$ ethylurea
reported as $\mathrm{IC}_{50}(\mu \mathrm{M})$ against HT-29 colon carcinoma cells were converted to $p \mathrm{IC}_{50}(\mathrm{M})$. These derivatives of N-PUS, their corresponding $-\log \mathrm{IC}_{50}\left(p \mathrm{IC}_{50}\right)$ values along with the values of descriptor are presented in Table 1.

The second data consists of one hundred and twelve 4-aminoquinoline derivatives (Hwang et al., 2011) with a variety of substituents at different positions (see Table 2). The anti-malarial activity tested against chloroquine (CQ) sensitive (3D7) strain of $P$. falciparum reported as $\mathrm{EC}_{50}$ $(\mu \mathrm{M})$ values were converted to $p \mathrm{EC}_{50}(\mathrm{M})$ for smoother statistical calculations. These derivatives of 4 -aminoquinolines, their corresponding $-\operatorname{logEC}{ }_{50}\left(p \mathrm{EC}_{50}\right)$ values and values of descriptor are presented in Table 2.

The third dataset, which is a subset of the dataset 2 , comprises cytotoxicity data of one hundred 4 -aminoquinolines (Hwang et al., 2011) tested against HepG2 cell lines (see Table 3). For convenience, $\mathrm{EC}_{50}(\mu \mathrm{M})$ values were converted to $p \mathrm{EC}_{50}(\mathrm{M})$.

## Calculation and selection of descriptors

The structures were drawn using Chemsketch 12 freeware, optimized using MMFF94 force field in TINKER, and then subjected to calculation of a large number of descriptors using e-Dragon, and PowerMV. Objective feature selection was performed to eliminate highly correlated and constant variables using QSARINS v1.2 and RapidMiner 5.0. Redundant descriptors were identified and eliminated using objective feature selection (Chirico and Gramatica, 2012; Gramatica, 2013; Mahajan et al., 2013; Masand et al., 2012, 2010, 2013). The procedure reported in the literature was employed for objective feature selection (Chirico and Gramatica 2012; Gramatica, 2013; Mahajan et al., 2013; Masand et al., 2012, 2010, 2013). As a general rule, constant for $>80 \%$ molecules, low-variance and correlated ( $|R| \geq 0.6$ ) descriptors were excluded prior to modeling.

## Methodology

The general procedure of external validation involves selection of descriptor on the basis of training set after splitting. It is well established that a QSAR model well predicts for a prediction molecule that is structurally very similar to the training set molecules because the descriptor (hence, the model) has captured common features of the training set molecules and is proficient to detect them in the new molecule (Consonni et al., 2009, 2010; Huang and Fan, 2011; Schuurmann et al., 2008; Todeschini et al., 2004), reverse is true for a new molecule which has very little in common with the training set data. That is, the confidence in its prediction should be low. Recently, Roy et al. proposed a new approach to overcome this critical issue, in which they used undivided dataset for selection of
variables and performed internal validation (LOO crossvalidation) in two different ways to ensure external predictivity of the developed model (Mitra et al., 2010). In the present work, descriptor selection was performed for the whole data set prior to splitting (information leakage) to determine the effect of selection of descriptors on external predictivity and behavior of different statistical parameters of the model. Genetic Algorithm (GA) available in QSARINS v1.2 was employed for the selection of optimum number and the set of descriptors applying the default settings (Chirico and Gramatica, 2011, 2012). Though, this step contravenes the basic rule that prediction set compounds should be excluded from the model development procedure, that is, they should be unknown to the developed model. But, this ensures that the selected descriptors capture the essential features that control the biological activity. In addition, it allows determining the effect of early descriptor selection (that is, prior to splitting or information leakage) on external predictivity of the models. Ferreira and Kiralj have termed such models as 'Auxiliary models’ (Kiralj and Ferreira, 2009).

In QSARINS (Gramatica et al., 2014, 2013), CV (crossvalidation) techniques are used as the optimization parameter (fitness function) for GA-based variable selection and also to verify model robustness and to avoid naïve Q ${ }^{2}$ (Chirico and Gramatica, 2011, (2012). The novel methodology for splitting (first time reported in this work, termed as residual-based method (RBM)) begins with the creation of an original model on the basis of undivided dataset followed by splitting of dataset into training and prediction sets on the basis of sign of residuals (difference between the actual and predicted value by original model) for each sample. In short, for the whole undivided dataset, a statistically robust GA-MLR model (Original Model) was built. For some molecules, this original model resulted in positive residuals and negative for the rest. Now, for the novel methodology of splitting i.e., RBM, the whole dataset was divided rationally into training and prediction sets on the basis of sign of the residuals (obtained in the original model with the condition that the bigger set as training set). A GA-MLR QSAR model was built for the training and the prediction sets created by RBM method. For comparison purpose, the whole dataset was again divided randomly (random splitting model, termed as RSM) and rationally (using sphere exclusion model, termed a SEM method) into the training and the prediction sets with number of compounds similar to training and prediction sets as in RBM, that is, during these various splitting, the number of molecules in training and prediction set is identical in RBM, RSM, and SEM. A molecule in the training set of one method (RBM or RSM or SEM) may or may not be in the training set of other method (RBM or RSM or SEM). The identical data split with

Table 2 4-aminoquinolines used in present study along with $p \mathrm{EC}_{50}$ and descriptors

| Sr. no. | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $p \mathrm{EC}_{50}(\mathrm{M})$ | Mor13e | RDF040v | F06 [N-O] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | PhO | Furfuryl | 5.620 | -0.218 | 7.086 | 2 |
| 2 | PhO | 2-HO-3-MeO-Bn | 5.854 | $-0.81$ | 7.784 | 1 |
| 3 | PhO | Piperonyl | 5.921 | $-1.085$ | 8.62 | 1 |
| 4 | PhO | 3-F-6-MeO-Bn | 5.959 | -0.506 | 7.366 | 1 |
| 5 | 2-MeO-PhO | Furfuryl | 6.143 | -0.729 | 8.331 | 1 |
| 6 | 2-MeO-PhO | 2-HO-3-MeO-Bn | 6.152 | -1.446 | 9.537 | 1 |
| 7 | 2-MeO-PhO | Piperonyl | 6.223 | -1.455 | 9.351 | 1 |
| 8 | 2-MeO-PhO | 3-F-6-MeO-Bn | 6.236 | -0.523 | 9.875 | 1 |
| 9 | 3-MeO-PhO | Furfuryl | 6.503 | -0.319 | 7.272 | 1 |
| 10 | 3-MeO-PhO | 2-HO-3-MeO-Bn | 6.527 | -0.748 | 9.432 | 1 |
| 11 | 3-MeO-PhO | Piperonyl | 6.545 | -1.079 | 9.32 | 1 |
| 12 | 3-MeO-PhO | 3-F-6-MeO-Bn | 6.547 | -0.64 | 9.523 | 1 |
| 13 | 4-MeO-PhO | Furfuryl | 6.600 | -0.245 | 7.489 | 1 |
| 14 | 4-MeO-PhO | 2-HO-3-MeO-Bn | 6.652 | -0.838 | 9.878 | 1 |
| 15 | 4-MeO-PhO | Piperonyl | 6.682 | -1.017 | 9.645 | 1 |
| 16 | 4-MeO-PhO | 3-F-6-MeO-Bn | 6.754 | -0.392 | 9.149 | 1 |
| 17 | 4-F-PhO | Furfuryl | 6.790 | -0.428 | 6.34 | 1 |
| 18 | 4-F-PhO | 2-HO-3-MeO-Bn | 6.790 | -0.651 | 8.072 | 1 |
| 19 | 4-F-PhO | Piperonyl | 6.842 | -0.842 | 8.321 | 1 |
| 20 | 4-F-PhO | 3-F-6-MeO-Bn | 6.860 | -0.691 | 7.491 | 1 |
| 21 | 4-Cl-PhO | Furfuryl | 6.863 | -0.252 | 8.598 | 1 |
| 22 | 4-Cl-PhO | Furfuryl | 6.879 | -0.778 | 9.636 | 1 |
| 23 | 4-Cl-PhO | Piperonyl | 6.893 | -0.749 | 10.379 | 1 |
| 24 | 4-Cl-PhO | 3-F-6-MeO-Bn | 6.896 | -0.636 | 10.35 | 1 |
| 25 | 3-Me2 N-PhO | Furfuryl | 6.928 | -0.024 | 7.162 | 1 |
| 26 | 3-Me2 N-PhO | 2-HO-3-MeO-Bn | 6.936 | -0.727 | 8.607 | 1 |
| 27 | $3-\mathrm{Me} 2 \mathrm{~N}-\mathrm{PhO}$ | Piperonyl | 6.975 | -0.858 | 8.745 | 1 |
| 28 | 3-Me2 N-PhO | 3-F-6-MeO-Bn | 7.018 | -0.212 | 7.919 | 1 |
| 29 | 4-tertBu-PhO | Furfuryl | 7.036 | 0.559 | 8.276 | 1 |
| 30 | 4-tertBu-PhO | 2-HO-3-MeO-Bn | 7.046 | 1.005 | 9.795 | 1 |
| 31 | 4-tertBu-PhO | Piperonyl | 7.051 | 0.206 | 9.918 | 1 |
| 32 | 4-tertBu-PhO | 3-F-6-MeO-Bn | 7.066 | -0.375 | 10.119 | 1 |
| 33 | 4-F-Ph | Furfuryl | 7.125 | -0.585 | 5.107 | 0 |
| 34 | 4-F-Ph | 2-HO-3-MeO-Bn | 7.180 | -0.77 | 6.327 | 0 |
| 35 | 4-F-Ph | Piperonyl | 7.244 | -0.931 | 6.653 | 0 |
| 36 | 4-F-Ph | 3-F-6-MeO-Bn | 7.252 | -1.058 | 6.982 | 0 |
| 37 | 3,5-CF3-Ph | Furfuryl | 7.260 | -0.722 | 5.599 | 0 |
| 38 | 3,5-CF3-Ph | 2-HO-3-MeO-Bn | 7.268 | -0.92 | 7.079 | 0 |
| 39 | 3,5-CF3-Ph | Piperonyl | 7.268 | -1.35 | 7.336 | 0 |
| 40 | 3,5-CF3-Ph | 3-F-6-MeO-Bn | 7.268 | -0.935 | 7.85 | 0 |
| 41 | 1-Naphtyl | Furfuryl | 7.301 | -0.703 | 6.82 | 0 |
| 42 | 1-Naphtyl | 2-HO-3-MeO-Bn | 7.337 | $-0.761$ | 7.719 | 0 |
| 43 | 1-Naphtyl | Piperonyl | 7.337 | -1.118 | 8.451 | 0 |
| 44 | 1-Naphtyl | 3-F-6-MeO-Bn | 7.387 | -0.556 | 8.566 | 0 |
| 45 | 4-CF3-Ph | Furfuryl | 7.387 | -0.594 | 5.258 | 0 |
| 46 | 4-CF3-Ph | 2-HO-3-MeO-Bn | 7.398 | -0.331 | 6.622 | 0 |
| 47 | 4-CF3-Ph | Piperonyl | 7.398 | -0.877 | 7.122 | 0 |
| 48 | 4-CF3-Ph | 3-F-6-MeO-Bn | 7.398 | -0.562 | 7.114 | 0 |

Table 2 continued

| Sr. no. | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $p \mathrm{EC}_{50}(\mathrm{M})$ | Mor13e | RDF040v | F06 [N-O] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | Ph | Furfuryl | 7.398 | -0.449 | 5.193 | 0 |
| 50 | Ph | 2-HO-3-MeO-Bn | 7.409 | -0.4 | 6.467 | 0 |
| 51 | Ph | Piperonyl | 7.409 | -0.754 | 6.74 | 0 |
| 52 | Ph | 3-F-6-MeO-Bn | 7.420 | -0.588 | 6.815 | 0 |
| 53 | 4-tertBu-Ph | Furfuryl | 7.469 | -0.104 | 7.086 | 0 |
| 54 | 4-tertBu-Ph | 2-HO-3-MeO-Bn | 7.481 | 0.348 | 8.467 | 0 |
| 55 | 4-tertBu-Ph | Piperonyl | 7.495 | -0.658 | 8.7 | 0 |
| 56 | 4-tertBu-Ph | 3-F-6-MeO-Bn | 7.509 | 0.472 | 9.679 | 0 |
| 57 | Piperonyl | Furfuryl | 7.509 | 0.326 | 4.927 | 0 |
| 58 | Piperonyl | 2-HO-3-MeO-Bn | 7.509 | -0.592 | 7.546 | 0 |
| 59 | Piperonyl | Piperonyl | 7.538 | -0.501 | 7.801 | 0 |
| 60 | Piperonyl | 3-F-6-MeO-Bn | 7.538 | -0.268 | 8.098 | 0 |
| 61 | 4-MeO-Ph | Furfuryl | 7.553 | 0.539 | 6.398 | 0 |
| 62 | $4-\mathrm{MeO}-\mathrm{Ph}$ | 2-HO-3-MeO-Bn | 7.569 | -0.221 | 8.104 | 0 |
| 63 | $4-\mathrm{MeO}-\mathrm{Ph}$ | Piperonyl | 7.569 | -0.536 | 8.312 | 0 |
| 64 | 4-MeO-Ph | 3-F-6-MeO-Bn | 7.569 | -0.071 | 7.819 | 0 |
| 65 | 4-F-Bn | Furfuryl | 7.569 | 0.959 | 5.326 | 0 |
| 66 | 4-F-Bn | 2-HO-3-MeO-Bn | 7.585 | -0.233 | 8.929 | 0 |
| 67 | 4-F-Bn | Piperonyl | 7.585 | -0.067 | 10.705 | 0 |
| 68 | 4-F-Bn | 3-F-6-MeO-Bn | 7.602 | 0.219 | 8.134 | 0 |
| 69 | iso-butyl | Furfuryl | 7.602 | 1.507 | 6.712 | 0 |
| 70 | iso-butyl | 2-HO-3-MeO-Bn | 7.638 | 0.808 | 9.125 | 0 |
| 71 | iso-butyl | Piperonyl | 7.658 | 0.497 | 6.044 | 0 |
| 72 | iso-butyl | 3-F-6-MeO-Bn | 7.658 | 0.112 | 10.014 | 0 |
| 73 | cHex | Furfuryl | 7.699 | 1.544 | 7.704 | 0 |
| 74 | cHex | 2-HO-3-MeO-Bn | 7.699 | 0.438 | 11.277 | 0 |
| 75 | cHex | Piperonyl | 7.699 | 0.752 | 10.997 | 0 |
| 76 | cHex | 3-F-6-MeO-Bn | 7.699 | 0.756 | 9.319 | 0 |
| 77 | 1-Et-Pr | Furfuryl | 7.721 | 1.399 | 6.966 | 0 |
| 78 | 1-Et-Pr | 2-HO-3-MeO-Bn | 7.721 | 0.074 | 9.59 | 0 |
| 79 | 1-Et-Pr | Piperonyl | 7.745 | 0.193 | 8.59 | 0 |
| 80 | 1-Et-Pr | 3-F-6-MeO-Bn | 7.745 | 0.864 | 7.615 | 0 |
| 81 | 3-CF3-Bn | Furfuryl | 7.745 | 0.117 | 7.599 | 0 |
| 82 | 3-CF3-Bn | 2-HO-3-MeO-Bn | 7.745 | -0.196 | 9.004 | 0 |
| 83 | 3-CF3-Bn | Piperonyl | 7.770 | 0.261 | 8.227 | 0 |
| 84 | 3-CF3-Bn | 3-F-6-MeO-Bn | 7.770 | 0.413 | 8.458 | 0 |
| 85 | $4-\mathrm{CN}-\mathrm{Bn}$ | Furfuryl | 7.770 | 1.409 | 8.512 | 0 |
| 86 | 4-CN-Bn | 2-HO-3-MeO-Bn | 7.824 | -0.322 | 9.482 | 0 |
| 87 | 4-CN-Bn | Piperonyl | 7.824 | 0.399 | 9.507 | 0 |
| 88 | 4-CN-Bn | 3-F-6-MeO-Bn | 7.824 | 0.776 | 9.032 | 0 |
| 89 | Bn | Furfuryl | 7.854 | 1.122 | 8.522 | 0 |
| 90 | Bn | 2-HO-3-MeO-Bn | 7.886 | 0.25 | 10.837 | 0 |
| 91 | Bn | Piperonyl | 7.886 | -0.019 | 6.437 | 0 |
| 92 | Bn | 3-F-6-MeO-Bn | 7.886 | 0.494 | 10.293 | 0 |
| 93 | 3,5-Me-Bn | Furfuryl | 7.886 | 1.444 | 6.402 | 0 |
| 94 | 3,5-Me-Bn | 2-HO-3-MeO-Bn | 7.959 | 1.194 | 10.845 | 0 |
| 95 | 3,5-Me-Bn | Piperonyl | 7.959 | 1.419 | 11.419 | 0 |
| 96 | 3,5-Me-Bn | 3-F-6-MeO-Bn | 7.959 | 0.887 | 8.162 | 0 |

Table 2 continued

| Sr. no. | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $p \mathrm{EC}_{50}(\mathrm{M})$ | Mor13e | RDF040v | F06 [N-O] |
| :--- | :--- | :--- | :--- | :---: | ---: | :--- |
| 97 | 2-Cl-4-F-Bn | Furfuryl | 7.959 | 0.839 | 11.876 | 0 |
| 98 | 2-Cl-4-F-Bn | 2-HO-3-MeO-Bn | 7.959 | -0.479 | 9.369 | 0 |
| 99 | 2-Cl-4-F-Bn | Piperonyl | 7.959 | -0.34 | 10.094 | 0 |
| 100 | 2-Cl-4-F-Bn | 3-F-6-MeO-Bn | 8.000 | 0.067 | 9.652 | 0 |
| 101 | iso-pentyl | Furfuryl | 8.046 | 1.491 | 7.984 | 0 |
| 102 | iso-pentyl | 2-HO-3-MeO-Bn | 8.046 | 1.243 | 8.878 | 0 |
| 103 | iso-pentyl | Piperonyl | 8.046 | 0.237 | 9.109 | 0 |
| 104 | iso-pentyl | 3-F-6-MeO-Bn | 8.046 | 0.566 | 7.314 | 0 |
| 105 | cHexmethyl | Furfuryl | 8.046 | 1.37 | 8.807 | 0 |
| 106 | cHexmethyl | 2-HO-3-MeO-Bn | 8.046 | 0.976 | 10.656 | 0 |
| 107 | cHexmethyl | Piperonyl | 8.097 | 0.756 | 11.296 | 0 |
| 108 | cHexmethyl | 3-F-6-MeO-Bn | 8.155 | 1.236 | 8.876 | 0 |
| 109 | PhEt | Furfuryl | 8.398 | 0.843 | 7.842 | 0 |
| 110 | PhEt | 2-HO-3-MeO-Bn | 8.398 | 0.615 | 9.586 | 0 |
| 111 | PhEt | Piperonyl | 8.398 | 0.336 | 7.842 | 0 |
| 112 | PhEt | 3-F-6-MeO-Bn | 9.000 | 0.636 | 14.152 | 0 |

respect to number of compounds in the training and the prediction sets was used in external validation for all models of a dataset to allow better comparison between the respective statistics (Kiralj and Ferreira, 2009). GA-MLR models were built also for the RSM and SEM. Briefly, four models were generated for each dataset.

## Results and discussion

For small- and moderate-sized datasets, which is the realistic situation for a QSAR modeler, a very serious problem in developing QSAR models with reduced sets of data (splitting the sets) is the loss of considerable amount of information due to holding out of some compounds for validation purpose (Chirico and Gramatica, 2011, 2012; Consonni et al., 2009, 2010; Hawkins, 2004; Hawkins et al., 2008; Huang and Fan, 2011; Mitra et al., 2010; Roy et al., 2008; Schuurmann et al., 2008; Scior et al., 2009). Other confines associated in using small datasets include fortuitous correlation, poor regression statistics, failure of carrying out various statistical tests, and abnormal behavior in performed tests (Kiralj and Ferreira, 2009). This may lead to spurious conclusions in model interpretation and incorrect proposals for the mechanism of action of the compounds.

In the present study, the main emphasis is on various methods for splitting the dataset. For external validation, random as well as rational splitting methods were adopted to create training and prediction sets. For the rational splitting, a special method RBM was also evaluated.

Interestingly, for all the datasets, the residual-based method resulted in radical splitting with $\sim 55-60 \%$ and $\sim 40-45 \%$ compounds in the training and the prediction sets, respectively. GA-MLR models were rebuilt for training and prediction sets using the same descriptors that were used for building the original model. In addition to RBM, sphere exclusion algorithm (SEM) and random (RSM) methods were also used for creating training and prediction sets, keeping the number of compounds the same as in residual-based method in the training and prediction sets. This ensures better comparison of various statistical parameters.

The analysis of Tables S1-S3 and 4, 5, 6 indicates that (i) the training and prediction sets used in RBM, RSM, and SEM models cover the diversity of the datasets and (ii) many compounds in the training and the prediction sets are close to each other (see supplementary figure S1, S2, and S3).

The statistical results for the original model for the three datasets are presented in Table 7. The minimum acceptable statistics (or recommended threshold values of statistical parameters) (Chirico and Gramatica, 2011, 2012; Huang and Fan, 2011; Kiralj and Ferreira, 2009; Martin et al., 2012) for regression models in QSAR include following conditions: $R^{2}>Q^{2}, \quad Q^{2} \geq 0.5, \quad R_{\mathrm{tr}}^{2} \geq 0.6, \quad R_{\mathrm{ex}}^{2} \geq 0.6$, $R_{M S E}<E_{t r}<E_{c v}, \quad \Delta \mathrm{~K} \geq 0.05, \quad C C C \geq 0.85, \quad Q^{2}-$ $F^{\mathrm{n}} \geq 0.70$, and $r_{\mathrm{m}}^{2} \geq 0.6$ with $R M S E$, and $M A E$ should be close to zero. In addition, the chance correlation of a QSAR model is validated on following criteria: $R_{\text {Yrand }}^{2}>Q_{\text {Yrand }}^{2}$,

$$
Q_{Y r a n d}^{2}<0.2 \text { and } R_{Y r a n d}^{2}<0.2 \rightarrow \text { no chance correlation; }
$$

Table 3 4-aminoquinolines used in present study along with $p \mathrm{EC}_{50}$ and descriptors

| Sr. no. | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $p \mathrm{EC}_{50}$ | GATS1p | E3u | E1 m | H6u | R2e |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | PhO | 2-HO-3-MeO-Bn | 5.046 | 0.959 | 0.41 | 0.552 | 1.306 | 1.88 |
| 2 | PhO | Piperonyl | 5.886 | 1.052 | 0.383 | 0.578 | 1.446 | 2.004 |
| 3 | PhO | 3-F-6-MeO-Bn | 6.097 | 0.907 | 0.396 | 0.576 | 1.404 | 1.952 |
| 4 | 2-MeO-PhO | Furfuryl | 5.538 | 1.089 | 0.309 | 0.483 | 1.1 | 1.988 |
| 5 | 2-MeO-PhO | 2-HO-3-MeO-Bn | 4.812 | 1.011 | 0.279 | 0.572 | 1.212 | 2 |
| 6 | 2-MeO-PhO | Piperonyl | 5.215 | 1.085 | 0.288 | 0.595 | 1.355 | 2.133 |
| 7 | 2-MeO-PhO | 3-F-6-MeO-Bn | 5.076 | 0.964 | 0.353 | 0.586 | 1.485 | 2.008 |
| 8 | 3-MeO-PhO | Furfuryl | 5.086 | 1.089 | 0.447 | 0.507 | 1.073 | 1.934 |
| 9 | 3-MeO-PhO | 3-F-6-MeO-Bn | 5.161 | 0.964 | 0.316 | 0.602 | 1.42 | 1.983 |
| 10 | 4-MeO-PhO | Furfuryl | 5.553 | 1.089 | 0.45 | 0.507 | 1.07 | 1.935 |
| 11 | 4-MeO-PhO | 2-HO-3-MeO-Bn | 5.367 | 1.011 | 0.364 | 0.523 | 1.445 | 1.925 |
| 12 | 4-MeO-PhO | Piperonyl | 5.066 | 1.085 | 0.429 | 0.607 | 1.096 | 2.03 |
| 13 | 4-MeO-PhO | 3-F-6-MeO-Bn | 5.041 | 0.964 | 0.375 | 0.602 | 1.402 | 1.959 |
| 14 | 4-F-PhO | 2-HO-3-MeO-Bn | 4.857 | 0.875 | 0.435 | 0.657 | 1.331 | 1.906 |
| 15 | 4-F-PhO | 3-F-6-MeO-Bn | 5.066 | 0.845 | 0.395 | 0.683 | 1.402 | 1.974 |
| 16 | 4-Cl-PhO | Furfuryl | 4.996 | 0.974 | 0.471 | 0.686 | 1.21 | 1.89 |
| 17 | 4-Cl-PhO | Furfuryl | 5.167 | 0.901 | 0.395 | 0.771 | 1.293 | 1.88 |
| 18 | 4-Cl-PhO | Piperonyl | 5.056 | 0.986 | 0.389 | 0.786 | 1.446 | 1.997 |
| 19 | 4-Cl-PhO | 3-F-6-MeO-Bn | 5.215 | 0.858 | 0.389 | 0.798 | 1.264 | 1.899 |
| 20 | 3-Me2 N-PhO | 2-HO-3-MeO-Bn | 4.963 | 1.049 | 0.361 | 0.55 | 1.153 | 1.948 |
| 21 | 3-Me2 N-PhO | 3-F-6-MeO-Bn | 5.699 | 0.993 | 0.382 | 0.581 | 1.17 | 1.965 |
| 22 | 4-tertBu-PhO | Furfuryl | 5.409 | 1.043 | 0.446 | 0.427 | 1.59 | 1.972 |
| 23 | 4-tertBu-PhO | 2-HO-3-MeO-Bn | 5.921 | 0.949 | 0.413 | 0.482 | 1.646 | 1.957 |
| 24 | 4-tertBu-PhO | Piperonyl | 5.921 | 1.043 | 0.404 | 0.501 | 1.858 | 2.096 |
| 25 | 4-tertBu-PhO | 3-F-6-MeO-Bn | 5.056 | 0.898 | 0.389 | 0.505 | 1.617 | 1.977 |
| 26 | 4-F-Ph | Furfuryl | 5.013 | 0.84 | 0.332 | 0.592 | 0.974 | 1.888 |
| 27 | 4-F-Ph | 2-HO-3-MeO-Bn | 5.027 | 0.799 | 0.393 | 0.665 | 1.252 | 1.91 |
| 28 | 4-F-Ph | Piperonyl | 4.921 | 0.882 | 0.281 | 0.706 | 1.214 | 2.013 |
| 29 | 4-F-Ph | 3-F-6-MeO-Bn | 6 | 0.77 | 0.424 | 0.69 | 1.269 | 1.955 |
| 30 | 3,5-CF3-Ph | Furfuryl | 5.523 | 0.739 | 0.262 | 0.663 | 0.878 | 2.48 |
| 31 | 3,5-CF3-Ph | 2-HO-3-MeO-Bn | 5.921 | 0.735 | 0.353 | 0.759 | 1.538 | 2.267 |
| 32 | 3,5-CF3-Ph | Piperonyl | 5.854 | 0.765 | 0.307 | 0.762 | 1.322 | 2.519 |
| 33 | 3,5-CF3-Ph | 3-F-6-MeO-Bn | 6 | 0.73 | 0.347 | 0.783 | 1.441 | 2.283 |
| 34 | 1-Naphtyl | Furfuryl | 5.092 | 0.98 | 0.452 | 0.48 | 1.156 | 1.903 |
| 35 | 1-Naphtyl | 2-HO-3-MeO-Bn | 5.432 | 0.863 | 0.367 | 0.575 | 1.259 | 1.918 |
| 36 | 1-Naphtyl | Piperonyl | 5.161 | 0.986 | 0.4 | 0.582 | 1.469 | 2.008 |
| 37 | 4-CF3-Ph | Furfuryl | 5.167 | 0.749 | 0.34 | 0.688 | 0.919 | 2.109 |
| 38 | 4-CF3-Ph | 2-HO-3-MeO-Bn | 5.377 | 0.74 | 0.414 | 0.756 | 1.279 | 2.107 |
| 39 | 4-CF3-Ph | Piperonyl | 5.481 | 0.79 | 0.406 | 0.77 | 1.306 | 2.245 |
| 40 | 4-CF3-Ph | 3-F-6-MeO-Bn | 5.092 | 0.728 | 0.381 | 0.775 | 1.169 | 2.136 |
| 41 | Ph | Furfuryl | 5.092 | 1.012 | 0.33 | 0.51 | 0.975 | 1.854 |
| 42 | Ph | 2-HO-3-MeO-Bn | 5.409 | 0.892 | 0.354 | 0.566 | 1.181 | 1.883 |
| 43 | Ph | Piperonyl | 5.328 | 1.015 | 0.279 | 0.637 | 1.21 | 1.979 |
| 44 | Ph | 3-F-6-MeO-Bn | 5.456 | 0.835 | 0.374 | 0.603 | 1.165 | 1.919 |
| 45 | 4-tertBu-Ph | Furfuryl | 5.409 | 1.009 | 0.353 | 0.447 | 1.453 | 2.019 |
| 46 | 4-tertBu-Ph | 2-HO-3-MeO-Bn | 6.155 | 0.886 | 0.377 | 0.497 | 1.569 | 2.037 |
| 47 | 4-tertBu-Ph | Piperonyl | 5.796 | 1.011 | 0.415 | 0.528 | 1.756 | 2.163 |
| 48 | 4-tertBu-Ph | 3-F-6-MeO-Bn | 6 | 0.83 | 0.357 | 0.528 | 1.577 | 2.061 |

Table 3 continued

| Sr. no. | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $p \mathrm{EC}_{50}$ | GATS1p | E3u | E1 m | H6u | R2e |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | Piperonyl | Furfuryl | 5.076 | 1.057 | 0.255 | 0.582 | 1.033 | 2.073 |
| 50 | Piperonyl | 2-HO-3-MeO-Bn | 5.721 | 0.985 | 0.213 | 0.589 | 1.608 | 2.026 |
| 51 | Piperonyl | Piperonyl | 5.119 | 1.057 | 0.218 | 0.604 | 1.474 | 2.155 |
| 52 | Piperonyl | 3-F-6-MeO-Bn | 5.046 | 0.939 | 0.208 | 0.688 | 1.718 | 2.084 |
| 53 | $4-\mathrm{MeO}-\mathrm{Ph}$ | Furfuryl | 5.119 | 1.05 | 0.197 | 0.532 | 1.306 | 1.908 |
| 54 | $4-\mathrm{MeO}-\mathrm{Ph}$ | 2-HO-3-MeO-Bn | 5.602 | 0.956 | 0.354 | 0.504 | 1.68 | 1.96 |
| 55 | $4-\mathrm{MeO}-\mathrm{Ph}$ | Piperonyl | 5.187 | 1.049 | 0.225 | 0.502 | 1.641 | 2.051 |
| 56 | 4-MeO-Ph | 3-F-6-MeO-Bn | 5.041 | 0.905 | 0.32 | 0.497 | 1.551 | 1.963 |
| 57 | 4-F-Bn | Furfuryl | 5.215 | 0.838 | 0.35 | 0.597 | 0.765 | 1.941 |
| 58 | 4-F-Bn | 2-HO-3-MeO-Bn | 5.027 | 0.797 | 0.28 | 0.605 | 1.016 | 1.945 |
| 59 | 4-F-Bn | Piperonyl | 5.155 | 0.88 | 0.433 | 0.663 | 0.961 | 1.977 |
| 60 | 4-F-Bn | 3-F-6-MeO-Bn | 5.538 | 0.768 | 0.407 | 0.645 | 1.403 | 1.874 |
| 61 | iso-butyl | 2-HO-3-MeO-Bn | 5.409 | 0.925 | 0.286 | 0.395 | 1.138 | 2.053 |
| 62 | iso-butyl | Piperonyl | 5.569 | 1.05 | 0.423 | 0.438 | 1.042 | 2.107 |
| 63 | iso-butyl | 3-F-6-MeO-Bn | 5.444 | 0.865 | 0.303 | 0.373 | 1.305 | 2.041 |
| 64 | cHex | Furfuryl | 5.18 | 1.012 | 0.312 | 0.476 | 1.052 | 2.075 |
| 65 | cHex | 2-HO-3-MeO-Bn | 5.77 | 0.892 | 0.353 | 0.464 | 1.251 | 2.082 |
| 66 | cHex | Piperonyl | 5.268 | 1.015 | 0.256 | 0.541 | 1.231 | 2.129 |
| 67 | cHex | 3-F-6-MeO-Bn | 5.495 | 0.835 | 0.228 | 0.517 | 1.377 | 2.031 |
| 68 | 1-Et-Pr | Furfuryl | 4.987 | 1.049 | 0.299 | 0.484 | 1.331 | 1.969 |
| 69 | 1-Et-Pr | 2-HO-3-MeO-Bn | 6.959 | 0.925 | 0.361 | 0.444 | 1.619 | 2.021 |
| 70 | 1-Et-Pr | Piperonyl | 5.131 | 1.05 | 0.304 | 0.527 | 1.334 | 2.121 |
| 71 | 1-Et-Pr | 3-F-6-MeO-Bn | 5.032 | 0.863 | 0.271 | 0.584 | 1.882 | 1.973 |
| 72 | 3-CF3-Bn | Furfuryl | 5.409 | 0.746 | 0.369 | 0.722 | 1.296 | 2.168 |
| 73 | $3-\mathrm{CF} 3-\mathrm{Bn}$ | 2-HO-3-MeO-Bn | 5.678 | 0.737 | 0.356 | 0.499 | 1.701 | 2.132 |
| 74 | 3-CF3-Bn | Piperonyl | 5.602 | 0.787 | 0.337 | 0.732 | 1.565 | 2.246 |
| 75 | 3-CF3-Bn | 3-F-6-MeO-Bn | 6.398 | 0.725 | 0.311 | 0.525 | 1.738 | 2.205 |
| 76 | 4-CN-Bn | Furfuryl | 4.943 | 0.963 | 0.23 | 0.602 | 0.981 | 1.931 |
| 77 | 4-CN-Bn | 2-HO-3-MeO-Bn | 5.066 | 0.872 | 0.32 | 0.566 | 1.335 | 1.853 |
| 78 | 4-CN-Bn | Piperonyl | 5.066 | 0.983 | 0.152 | 0.578 | 1.257 | 1.97 |
| 79 | 4-CN-Bn | 3-F-6-MeO-Bn | 5.119 | 0.824 | 0.157 | 0.581 | 1.388 | 1.802 |
| 80 | Bn | 2-HO-3-MeO-Bn | 5.092 | 0.891 | 0.14 | 0.491 | 1.554 | 1.792 |
| 81 | Bn | Piperonyl | 5.086 | 1.014 | 0.436 | 0.481 | 1.119 | 2.066 |
| 82 | Bn | 3-F-6-MeO-Bn | 5.081 | 0.834 | 0.211 | 0.508 | 1.435 | 1.787 |
| 83 | 3,5-Me-Bn | Furfuryl | 5.143 | 1.009 | 0.355 | 0.494 | 1.25 | 1.983 |
| 84 | 3,5-Me-Bn | 2-HO-3-MeO-Bn | 5.602 | 0.887 | 0.176 | 0.473 | 1.993 | 1.875 |
| 85 | 3,5-Me-Bn | Piperonyl | 5.523 | 1.012 | 0.189 | 0.49 | 1.639 | 1.991 |
| 86 | 3,5-Me-Bn | 3-F-6-MeO-Bn | 6.046 | 0.831 | 0.318 | 0.499 | 1.465 | 2.046 |
| 87 | 2-Cl-4-F-Bn | Furfuryl | 5.06 | 0.789 | 0.385 | 0.674 | 1.245 | 1.82 |
| 88 | 2-Cl-4-F-Bn | 2-HO-3-MeO-Bn | 5.538 | 0.757 | 0.266 | 0.597 | 1.555 | 1.975 |
| 89 | 2-Cl-4-F-Bn | Piperonyl | 5.276 | 0.834 | 0.273 | 0.744 | 1.297 | 2.003 |
| 90 | 2-Cl-4-F-Bn | 3-F-6-MeO-Bn | 5.495 | 0.733 | 0.403 | 0.624 | 1.312 | 1.957 |
| 91 | iso-pentyl | 2-HO-3-MeO-Bn | 5.194 | 0.922 | 0.332 | 0.625 | 1.365 | 2.086 |
| 92 | iso-pentyl | Piperonyl | 5.538 | 1.047 | 0.3 | 0.689 | 1.134 | 2.228 |
| 93 | iso-pentyl | 3-F-6-MeO-Bn | 6 | 0.865 | 0.306 | 0.451 | 1.106 | 2.031 |
| 94 | cHexmethyl | Furfuryl | 5.658 | 1.011 | 0.33 | 0.478 | 1.266 | 2.051 |
| 95 | cHexmethyl | 2-HO-3-MeO-Bn | 5.921 | 0.891 | 0.278 | 0.473 | 1.733 | 2.079 |
| 96 | cHexmethyl | Piperonyl | 5.027 | 1.014 | 0.234 | 0.553 | 1.335 | 2.27 |

Table 3 continued

| Sr. no. | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $p \mathrm{EC}_{50}$ | GATS1p | E3u | E 1 m | H6u | R2e |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 97 | cHexmethyl | 3-F-6-MeO-Bn | 5.553 | 0.834 | 0.293 | 0.476 | 1.355 | 2.082 |
| 98 | PhEt | 2-HO-3-MeO-Bn | 5.119 | 0.799 | 0.278 | 0.535 | 1.744 | 1.963 |
| 99 | PhEt | Piperonyl | 5.229 | 0.832 | 0.204 | 0.554 | 1.546 | 1.854 |
| 100 | PhEt | 3-F-6-MeO-Bn | 5.252 | 1.013 | 0.317 | 0.542 | 1.794 | 1.96 |

Any $Q_{Y \text { rand }}^{2}$ and $0.2<R_{\text {Yrand }}^{2}<0.3 \rightarrow$ negligible chance correlation;
Any $Q_{\text {Yrand }}^{2}$ and $0.3<R_{\text {Yrand }}^{2}<0.4 \rightarrow$ tolerable chance correlation;
Any $Q_{\text {Yrand }}^{2}$ and $R_{\text {Yrand }}^{2}>0.4 \rightarrow$ recognized chance correlation.
$\left(1-r^{2} / r_{\mathrm{o}}^{2}\right)<0.1, \quad 0.9 \leq k \leq 1.1 \quad$ or $\quad\left(1-r^{2} / r_{\mathrm{o}}^{2}\right)<0.1$, $0.9 \leq k^{\prime} \leq 1.1$ with $\left|\overline{r_{o}^{2}}-r_{o}^{\prime 2}\right|<0.3$

Except for the dataset-3, the statistical parameters point out that the GA-MLR original models for the dataset-1 and 2 are statistically robust with statistically acceptable values of $R{ }_{\mathrm{tr}}^{2}, R_{\mathrm{adj}}^{2}, R_{\mathrm{cv}}^{2}, R_{\mathrm{LMO}}^{2}, R_{Y r a n d}^{2}, s, K x x, \Delta \mathrm{~K}, R M S E_{t r}$, $R M S E_{c v}, C C C_{t r}, C C C_{c v}, M A E_{t r}, M A E_{c v}$, and $F$. Thus, from the internal validation point of view, the original models for the dataset 1 and 2 are satisfying all the essential conditions and criteria. The positive or negative contribution of a descriptor to activity remains the same during the data split and building original model indicating self-consistency of data(Kiralj and Ferreira, 2009), which is useful for model interpretation and mechanism of action.

Since, for a dataset, the same descriptors that cover the diversity of training and prediction sets are used to build models for different types of training and prediction sets, the statistical performance of residual based, random splitting and sphere exclusion should be comparable with each other for all the datasets. But, the statistical performance of each model is different (see Tables 7, 8, 9, 10). This indicates that the method of splitting has significant effect on the behavior of statistical parameters. Additionally, since the descriptors have been selected prior to splitting, the built models have captured common features of training and prediction set molecules, therefore, the models are capable to detect them in the test molecules, also. Consequently, the external predictivity of models should be high and comparable to each other for a dataset. However, the analysis of Tables 8, 9, and 10 indicates that the external predictivity of different models is different. Thus, it appears that the selection of descriptors prior to splitting has little role to play in deciding external predictivity of model. In fact, it is the diversity of training and prediction set that decides the external predictivity of any QSAR model. In other words, if the compounds in prediction set resemble the training set compounds, high
predictive ability is observed for the developed model. Therefore, more number of model based on different training and prediction sets for a dataset must be developed, else, boot-strapping is an attractive option.

Results for the dataset-1
A comparison of various statistical parameters viz. $R_{\mathrm{tr}}^{2}$, $R_{\mathrm{adj}}^{2}, R_{\mathrm{cv}}^{2}, R_{\mathrm{LMO}}^{2}, R_{Y r a n d}^{2}, s, R_{e x}^{2}, K x x, \Delta \mathrm{~K}, R M S E_{t r}, R M S E_{c v}$, $C C C_{t r}, C C C_{c v}, M A E_{t r}, M A E_{c v}, r_{m}^{2} a v$, and $F$ reveals that the performance of RBM model is better than the other models, which suggests that the model is statistically soundful and has good predictive ability. The $r_{\mathrm{m}}^{2}$ statistic, which penalizes the model profoundly for large difference between predicted and the corresponding experimental response, is higher for residual-based model indicating good external predictivity (Mitra et al., 2010; Roy and Mitra, 2012). A plausible reason for this could be the distribution of the training and the prediction sets in the chemical space because both the sets used in RBM model covers diversity of the dataset. Though RBM model appears statistically robust but apropos of many statistical parameters, everything is not rosy-red for it.

For a good predictive ability $R M S E_{e x}$ and $M A E_{e x}$ should be as low as possible (Chirico and Gramatica, 2011), but for RBM model, the values for these parameters are higher than the rest of the models. The large difference between $R M S E_{t r}(=0.118)$ and $R M S E_{e x}(=0.441)$ as well as between $M A E_{t r}(=0.089)$ and $M A E_{\text {ex }}(=0.394)$ raises question on residual-based model's generalizability (Chirico and Gramatica, 2011, 2012). In addition, the lower values of $C C C_{e x}, Q^{2}-F^{1}, Q^{2}-F^{2}$, and $Q^{2}-F^{3}$ for RBM model than RSM and SEM models indicate low external predictivity of this model (Chirico and Gramatica 2011, 2012; Consonni et al., 2009, 2010; Schuurmann et al., 2008). Thus, the RBM model is appearing statistically soundful on the basis of many parameters, but some parameters raise doubts on its external predictivity. A possible reason could be the sensitivity of $Q^{2}-F^{1}$ and $Q^{2}-F^{2}$ toward the presence of outliers in the prediction set (Consonni et al., 2010). That is, the presence of more number of outliers in the prediction set of RBM model than the other models is responsible for its low external predictivity. Therefore, it can be stated

Table 4 Experimental and predicted $p \mathrm{IC}_{50}$ by different models for dataset-1

| ID | $p \mathrm{IC}_{50}$ | Status | Pred. $p \mathrm{IC}_{50}$ (Originalmodel) | Status | $\begin{aligned} & \text { Pred. } p \mathrm{IC}_{50} \\ & \text { RBM } \end{aligned}$ | Status | Pred. $p \mathrm{IC}_{50}$ RSM | Status | Pred. $p \mathrm{IC}_{50}$ SEM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 5.8240 | Training | 5.2945 | Prediction | 4.9468 | Training | 5.5246 | Training | 5.2338 |
| 2 | 4.4810 | Training | 4.1434 | Prediction | 4.0651 | Prediction | 4.3532 | Prediction | 4.0669 |
| 3 | 5.3670 | Training | 5.1114 | Prediction | 4.6446 | Training | 5.1312 | Prediction | 5.0960 |
| 4 | 4.8240 | Training | 4.6201 | Prediction | 4.5856 | Prediction | 4.6241 | Training | 4.7066 |
| 5 | 3.9210 | Training | 4.3456 | Training | 4.2006 | Prediction | 4.7011 | Training | 4.2484 |
| 6 | 4.7700 | Training | 4.9528 | Training | 4.8453 | Training | 4.7697 | Training | 5.0715 |
| 7 | 5.6020 | Training | 5.4692 | Prediction | 5.2327 | Training | 5.4758 | Prediction | 5.5231 |
| 8 | 4.1490 | Training | 4.4768 | Training | 4.1421 | Prediction | 4.5794 | Training | 4.3759 |
| 9 | 4.3190 | Training | 4.4971 | Training | 4.2888 | Training | 4.3606 | Prediction | 4.5313 |
| 10 | 4.8240 | Training | 4.8351 | Prediction | 4.5429 | Prediction | 4.8050 | Training | 4.8310 |
| 11 | 4.2600 | Training | 4.2126 | Prediction | 4.0629 | Prediction | 4.2534 | Prediction | 4.1652 |
| 12 | 4.3980 | Training | 4.3672 | Prediction | 4.1746 | Prediction | 4.0790 | Prediction | 4.4456 |
| 13 | 4.6780 | Training | 4.8172 | Training | 4.6643 | Prediction | 4.8165 | Prediction | 4.8690 |
| 14 | 4.6780 | Training | 4.2410 | Prediction | 4.0579 | Training | 4.2332 | Training | 4.2110 |
| 15 | 4.6380 | Training | 4.8594 | Training | 4.5173 | Training | 4.9219 | Training | 4.8445 |
| 16 | 4.8540 | Training | 4.7210 | Prediction | 4.6080 | Prediction | 4.7724 | Prediction | 4.7689 |
| 17 | 4.2920 | Training | 4.3798 | Training | 4.1487 | Training | 4.4670 | Prediction | 4.3226 |
| 18 | 4.5850 | Training | 4.6987 | Training | 4.5177 | Training | 4.6012 | Training | 4.6975 |
| 19 | 4.8240 | Training | 4.9861 | Training | 4.7799 | Training | 4.8915 | Prediction | 5.0179 |
| 20 | 4.8860 | Training | 5.0662 | Training | 4.9380 | Prediction | 4.9073 | Prediction | 5.1382 |
| 21 | 4.3010 | Training | 4.5949 | Training | 4.3935 | Training | 4.4711 | Training | 4.5774 |
| 22 | 4.3770 | Training | 4.3227 | Prediction | 4.1462 | Training | 4.4158 | Prediction | 4.2844 |
| 23 | 4.0180 | Training | 4.2580 | Training | 4.1286 | Training | 4.2083 | Training | 4.2826 |
| 24 | 4.8240 | Training | 4.5794 | Prediction | 4.4278 | Prediction | 4.4112 | Training | 4.6660 |
| 25 | 4.1940 | Training | 3.8950 | Prediction | 3.9259 | Prediction | 3.6105 | Training | 3.9953 |
| 26 | 4.5850 | Training | 4.6599 | Training | 4.5970 | Training | 4.6743 | Prediction | 4.7344 |
| 27 | 5.3280 | Training | 5.0269 | Prediction | 4.6933 | Prediction | 5.0460 | Training | 4.9675 |
| 28 | 4.3570 | Training | 4.3042 | Prediction | 4.1023 | Training | 4.1680 | Training | 4.3111 |
| 29 | 4.4810 | Training | 4.5794 | Training | 4.3587 | Prediction | 4.4580 | Prediction | 4.6178 |
| 30 | 4.6020 | Training | 4.6885 | Training | 4.5141 | Training | 4.5384 | Prediction | 4.7488 |
| 31 | 4.1250 | Training | 4.2266 | Training | 3.9974 | Prediction | 4.1417 | Training | 4.1867 |
| 32 | 4.9210 | Training | 4.9349 | Training | 4.6648 | Training | 4.8049 | Prediction | 4.9387 |
| 33 | 4.9210 | Training | 5.2090 | Training | 4.9217 | Prediction | 5.0860 | Training | 5.2472 |
| 34 | 5.6200 | Training | 5.3283 | Prediction | 5.1025 | Prediction | 5.1492 | Training | 5.4025 |
| 35 | 4.9210 | Training | 4.7116 | Prediction | 4.4781 | Prediction | 4.5533 | Prediction | 4.7109 |
| 36 | 4.9590 | Training | 4.9578 | Prediction | 4.5756 | Training | 5.0387 | Prediction | 4.8530 |
| 37 | 3.9910 | Training | 4.1116 | Training | 3.9965 | Training | 4.1346 | Training | 4.0684 |
| 38 | 4.8240 | Training | 4.3522 | Prediction | 4.1887 | Prediction | 4.1562 | Training | 4.4158 |
| 39 | 4.3870 | Training | 4.5814 | Training | 4.4422 | Training | 4.2705 | Prediction | 4.7137 |
| 40 | 4.0660 | Training | 4.3520 | Training | 4.2611 | Training | 4.1534 | Prediction | 4.4426 |
| 41 | 4.4950 | Training | 4.5532 | Training | 4.4897 | Prediction | 4.2078 | Training | 4.7186 |
| 42 | 4.5230 | Training | 4.3868 | Prediction | 4.3279 | Training | 4.3650 | Training | 4.3516 |
| 43 | 4.7450 | Training | 5.1121 | Training | 4.8920 | Training | 5.2956 | Training | 5.0681 |
| 44 | 4.4090 | Training | 4.3261 | Prediction | 4.2793 | Prediction | 4.4605 | Prediction | 4.3016 |

RBM Residual-based model, RBM Random splitting model, SEM Sphere exclusion model

Table 5 Experimental and predicted $p \mathrm{EC}_{50}$ by different models for dataset-2

| ID | $p \mathrm{EC}_{50}(\mathrm{M})$ | Status | Pred. $p \mathrm{EC}_{50}$ (Original model) | Status | Pred. $p \mathrm{EC}_{50}$ RBM | Status | Pred. $p \mathrm{EC}_{50}$ RSM | Status | Pred. $p \mathrm{EC}_{50}$ SEM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 5.620 | Training | 5.6830 | Training | 5.3535 | Prediction | 5.8460 | Training | 5.6082 |
| 2 | 5.854 | Training | 6.5075 | Training | 6.2924 | Prediction | 6.5813 | Training | 6.4897 |
| 3 | 5.921 | Training | 6.5065 | Training | 6.2847 | Training | 6.5663 | Prediction | 6.4877 |
| 4 | 5.959 | Training | 6.5481 | Training | 6.3330 | Prediction | 6.6285 | Training | 6.5248 |
| 5 | 6.143 | Training | 6.5698 | Training | 6.3449 | Prediction | 6.6337 | Training | 6.5420 |
| 6 | 6.152 | Training | 6.4911 | Training | 6.2631 | Training | 6.5357 | Prediction | 6.4734 |
| 7 | 6.223 | Training | 6.4744 | Training | 6.2494 | Training | 6.5223 | Training | 6.4594 |
| 8 | 6.236 | Training | 6.7401 | Training | 6.4880 | Prediction | 6.7765 | Prediction | 6.6853 |
| 9 | 6.503 | Training | 6.5859 | Training | 6.3683 | Training | 6.6674 | Prediction | 6.5571 |
| 10 | 6.527 | Training | 6.6512 | Training | 6.4103 | Prediction | 6.6959 | Prediction | 6.6101 |
| 11 | 6.545 | Training | 6.5626 | Training | 6.3303 | Prediction | 6.6101 | Prediction | 6.5347 |
| 12 | 6.547 | Training | 6.6844 | Training | 6.4399 | Training | 6.7272 | Prediction | 6.6382 |
| 13 | 6.600 | Training | 6.6207 | Training | 6.3983 | Training | 6.6982 | Prediction | 6.5865 |
| 14 | 6.652 | Training | 6.6644 | Training | 6.4187 | Training | 6.7015 | Prediction | 6.6207 |
| 15 | 6.682 | Training | 6.6030 | Prediction | 6.3645 | Training | 6.6446 | Prediction | 6.5687 |
| 16 | 6.754 | Training | 6.7149 | Prediction | 6.4709 | Prediction | 6.7637 | Training | 6.6648 |
| 17 | 6.790 | Training | 6.4868 | Prediction | 6.2853 | Training | 6.5849 | Training | 6.4738 |
| 18 | 6.790 | Training | 6.5683 | Prediction | 6.3457 | Training | 6.6367 | Prediction | 6.5412 |
| 19 | 6.842 | Training | 6.5417 | Prediction | 6.3193 | Training | 6.6062 | Training | 6.5182 |
| 20 | 6.860 | Training | 6.5133 | Prediction | 6.3001 | Training | 6.5919 | Prediction | 6.4950 |
| 21 | 6.863 | Training | 6.7057 | Prediction | 6.4669 | Prediction | 6.7638 | Prediction | 6.6576 |
| 22 | 6.879 | Training | 6.6599 | Prediction | 6.4166 | Prediction | 6.7011 | Prediction | 6.6172 |
| 23 | 6.893 | Training | 6.7250 | Prediction | 6.4700 | Prediction | 6.7531 | Training | 6.6718 |
| 24 | 6.896 | Training | 6.7500 | Prediction | 6.4931 | Training | 6.7783 | Training | 6.6931 |
| 25 | 6.928 | Training | 6.6484 | Prediction | 6.4264 | Prediction | 6.7312 | Prediction | 6.6106 |
| 26 | 6.936 | Training | 6.5918 | Prediction | 6.3628 | Training | 6.6509 | Training | 6.5605 |
| 27 | 6.975 | Training | 6.5710 | Prediction | 6.3426 | Training | 6.6280 | Prediction | 6.5426 |
| 28 | 7.018 | Training | 6.6622 | Prediction | 6.4328 | Training | 6.7322 | Prediction | 6.6214 |
| 29 | 7.036 | Training | 6.8761 | Prediction | 6.6254 | Prediction | 6.9378 | Training | 6.8033 |
| 30 | 7.046 | Training | 7.1023 | Training | 6.8198 | Prediction | 7.1363 | Training | 6.9942 |
| 31 | 7.051 | Training | 6.9193 | Prediction | 6.6514 | Training | 6.9531 | Prediction | 6.8380 |
| 32 | 7.066 | Training | 6.7948 | Prediction | 6.5360 | Training | 6.8266 | Prediction | 6.7317 |
| 33 | 7.125 | Training | 7.2652 | Training | 7.1980 | Training | 7.3070 | Prediction | 7.3185 |
| 34 | 7.180 | Training | 7.3159 | Training | 7.2344 | Training | 7.3368 | Prediction | 7.3602 |
| 35 | 7.244 | Training | 7.3026 | Training | 7.2195 | Prediction | 7.3181 | Prediction | 7.3484 |
| 36 | 7.252 | Training | 7.2977 | Training | 7.2123 | Prediction | 7.3078 | Training | 7.3438 |
| 37 | 7.260 | Training | 7.2706 | Training | 7.1989 | Training | 7.3042 | Training | 7.3225 |
| 38 | 7.268 | Training | 7.3385 | Training | 7.2489 | Training | 7.3466 | Training | 7.3785 |
| 39 | 7.268 | Training | 7.2549 | Prediction | 7.1703 | Training | 7.2595 | Prediction | 7.3069 |
| 40 | 7.268 | Training | 7.3952 | Training | 7.2943 | Prediction | 7.3897 | Prediction | 7.4258 |
| 41 | 7.301 | Training | 7.3706 | Training | 7.2803 | Prediction | 7.3827 | Training | 7.4062 |
| 42 | 7.337 | Training | 7.4269 | Training | 7.3244 | Training | 7.4233 | Training | 7.4530 |
| 43 | 7.337 | Training | 7.3980 | Training | 7.2920 | Prediction | 7.3824 | Prediction | 7.4275 |
| 44 | 7.387 | Training | 7.5425 | Training | 7.4232 | Prediction | 7.5236 | Prediction | 7.5505 |
| 45 | 7.387 | Training | 7.2748 | Prediction | 7.2056 | Prediction | 7.3140 | Training | 7.3265 |
| 46 | 7.398 | Training | 7.4449 | Training | 7.3498 | Prediction | 7.4595 | Prediction | 7.4697 |
| 47 | 7.398 | Training | 7.3523 | Prediction | 7.2611 | Prediction | 7.3594 | Prediction | 7.3902 |

Table 5 continued

| ID | $p \mathrm{EC}_{50}(\mathrm{M})$ | Status | Pred. $p \mathrm{EC}_{50}$ (Original model) | Status | Pred. $p \mathrm{EC}_{50}$ RBM | Status | $\begin{aligned} & \text { Pred. } p \mathrm{EC}_{50} \\ & \text { RSM } \end{aligned}$ | Status | Pred. $p \mathrm{EC}_{50}$ SEM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 48 | 7.398 | Training | 7.4276 | Training | 7.3300 | Prediction | 7.4341 | Training | 7.4544 |
| 49 | 7.398 | Training | 7.3047 | Prediction | 7.2334 | Training | 7.3447 | Training | 7.3521 |
| 50 | 7.409 | Training | 7.4161 | Training | 7.3248 | Prediction | 7.4336 | Prediction | 7.4454 |
| 51 | 7.409 | Training | 7.3521 | Prediction | 7.2640 | Training | 7.3657 | Training | 7.3905 |
| 52 | 7.420 | Training | 7.3980 | Prediction | 7.3054 | Training | 7.4098 | Prediction | 7.4295 |
| 53 | 7.469 | Training | 7.5359 | Training | 7.4292 | Prediction | 7.5418 | Training | 7.5467 |
| 54 | 7.481 | Training | 7.7528 | Training | 7.6162 | Training | 7.7333 | Prediction | 7.7299 |
| 55 | 7.495 | Training | 7.5284 | Training | 7.4092 | Training | 7.5073 | Prediction | 7.5383 |
| 56 | 7.509 | Training | 7.8774 | Training | 7.7202 | Prediction | 7.8364 | Training | 7.8346 |
| 57 | 7.509 | Training | 7.4709 | Prediction | 7.3874 | Training | 7.5136 | Training | 7.4941 |
| 58 | 7.509 | Training | 7.4541 | Prediction | 7.3507 | Training | 7.4532 | Training | 7.4765 |
| 59 | 7.538 | Training | 7.4960 | Prediction | 7.3869 | Training | 7.4903 | Prediction | 7.5118 |
| 60 | 7.538 | Training | 7.5754 | Training | 7.4571 | Training | 7.5639 | Prediction | 7.5791 |
| 61 | 7.553 | Training | 7.6372 | Training | 7.5275 | Prediction | 7.6535 | Training | 7.6340 |
| 62 | 7.569 | Training | 7.5872 | Training | 7.4678 | Prediction | 7.5755 | Training | 7.5892 |
| 63 | 7.569 | Training | 7.5275 | Prediction | 7.4115 | Training | 7.5129 | Prediction | 7.5380 |
| 64 | 7.569 | Training | 7.6011 | Training | 7.4829 | Prediction | 7.5941 | Prediction | 7.6014 |
| 65 | 7.569 | Training | 7.6547 | Training | 7.5522 | Training | 7.6888 | Prediction | 7.6503 |
| 66 | 7.585 | Training | 7.6488 | Training | 7.5174 | Training | 7.6226 | Training | 7.6406 |
| 67 | 7.585 | Training | 7.8276 | Training | 7.6663 | Prediction | 7.7699 | Training | 7.7908 |
| 68 | 7.602 | Training | 7.6956 | Training | 7.5667 | Training | 7.6824 | Training | 7.6816 |
| 69 | 7.602 | Training | 7.8951 | Training | 7.7607 | Prediction | 7.9036 | Training | 7.8535 |
| 70 | 7.638 | Training | 7.9151 | Training | 7.7593 | Prediction | 7.8830 | Training | 7.8675 |
| 71 | 7.658 | Training | 7.5994 | Prediction | 7.4958 | Prediction | 7.6221 | Training | 7.6022 |
| 72 | 7.658 | Training | 7.8168 | Training | 7.6621 | Training | 7.7707 | Prediction | 7.7825 |
| 73 | 7.699 | Training | 7.9816 | Training | 7.8316 | Training | 7.9726 | Training | 7.9259 |
| 74 | 7.699 | Training | 7.9941 | Training | 7.8138 | Training | 7.9251 | Training | 7.9320 |
| 75 | 7.699 | Training | 8.0479 | Training | 7.8653 | Prediction | 7.9831 | Training | 7.9783 |
| 76 | 7.699 | Training | 7.9178 | Training | 7.7601 | Training | 7.8823 | Training | 7.8694 |
| 77 | 7.721 | Training | 7.8890 | Training | 7.7530 | Training | 7.8932 | Training | 7.8479 |
| 78 | 7.721 | Training | 7.7745 | Training | 7.6269 | Prediction | 7.7360 | Training | 7.7469 |
| 79 | 7.745 | Training | 7.7250 | Prediction | 7.5898 | Prediction | 7.7038 | Training | 7.7061 |
| 80 | 7.745 | Training | 7.8106 | Training | 7.6761 | Prediction | 7.8049 | Training | 7.7803 |
| 81 | 7.745 | Training | 7.6292 | Prediction | 7.5104 | Training | 7.6256 | Prediction | 7.6257 |
| 82 | 7.745 | Training | 7.6636 | Prediction | 7.5303 | Training | 7.6360 | Training | 7.6531 |
| 83 | 7.770 | Training | 7.7130 | Prediction | 7.5819 | Training | 7.6980 | Prediction | 7.6963 |
| 84 | 7.770 | Training | 7.7678 | Prediction | 7.6300 | Training | 7.7483 | Prediction | 7.7427 |
| 85 | 7.770 | Training | 8.0122 | Training | 7.8530 | Training | 7.9893 | Prediction | 7.9510 |
| 86 | 7.824 | Training | 7.6705 | Prediction | 7.5327 | Prediction | 7.6349 | Training | 7.6585 |
| 87 | 7.824 | Training | 7.8463 | Training | 7.6933 | Training | 7.8085 | Training | 7.8083 |
| 88 | 7.824 | Training | 7.9001 | Training | 7.7463 | Training | 7.8697 | Training | 7.8548 |
| 89 | 7.854 | Training | 7.9437 | Training | 7.7903 | Prediction | 7.9214 | Training | 7.8926 |
| 90 | 7.886 | Training | 7.9143 | Training | 7.7445 | Training | 7.8535 | Prediction | 7.8646 |
| 91 | 7.886 | Training | 7.5056 | Prediction | 7.4069 | Prediction | 7.5227 | Training | 7.5218 |
| 92 | 7.886 | Training | 7.9307 | Training | 7.7639 | Training | 7.8788 | Prediction | 7.8792 |
| 93 | 7.886 | Training | 7.8557 | Prediction | 7.7272 | Training | 7.8698 | Training | 7.8203 |
| 94 | 7.959 | Training | 8.1426 | Training | 7.9532 | Training | 8.0793 | Training | 8.0592 |

Table 5 continued

| ID | $p \mathrm{EC}_{50}(\mathrm{M})$ | Status | Pred. $p \mathrm{EC}_{50}$ (Original model) | Status | Pred. $p \mathrm{EC}_{50}$ RBM | Status | $\begin{aligned} & \text { Pred. } p \mathrm{EC}_{50} \\ & \text { RSM } \end{aligned}$ | Status | Pred. $p \mathrm{EC}_{50}$ SEM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 95 | 7.959 | Training | 8.2417 | Training | 8.0391 | Training | 8.1678 | Prediction | 8.1430 |
| 96 | 7.959 | Training | 7.8589 | Prediction | 7.7158 | Training | 7.8435 | Training | 7.8208 |
| 97 | 7.959 | Training | 8.1376 | Training | 7.9401 | Prediction | 8.0571 | Training | 8.0536 |
| 98 | 7.959 | Training | 7.6238 | Prediction | 7.4910 | Training | 7.5906 | Training | 7.6188 |
| 99 | 7.959 | Training | 7.7140 | Prediction | 7.5675 | Prediction | 7.6677 | Prediction | 7.6948 |
| 100 | 8.000 | Training | 7.7776 | Prediction | 7.6292 | Prediction | 7.7381 | Training | 7.7496 |
| 101 | 8.046 | Training | 7.9907 | Prediction | 7.8377 | Training | 7.9769 | Training | 7.9333 |
| 102 | 8.046 | Training | 8.0007 | Prediction | 7.8395 | Prediction | 7.9719 | Training | 7.9408 |
| 103 | 8.046 | Training | 7.7762 | Prediction | 7.6324 | Prediction | 7.7457 | Training | 7.7490 |
| 104 | 8.046 | Training | 7.7153 | Prediction | 7.5914 | Prediction | 7.7155 | Training | 7.6994 |
| 105 | 8.046 | Training | 8.0258 | Prediction | 7.8630 | Training | 7.9979 | Prediction | 7.9622 |
| 106 | 8.046 | Training | 8.0753 | Training | 7.8931 | Training | 8.0159 | Training | 8.0020 |
| 107 | 8.097 | Training | 8.0722 | Prediction | 7.8851 | Prediction | 8.0021 | Training | 7.9986 |
| 108 | 8.155 | Training | 7.9989 | Prediction | 7.8379 | Prediction | 7.9701 | Prediction | 7.9392 |
| 109 | 8.398 | Training | 7.8233 | Prediction | 7.6858 | Training | 7.8136 | Prediction | 7.7908 |
| 110 | 8.398 | Training | 7.9046 | Prediction | 7.7459 | Training | 7.8649 | Training | 7.8579 |
| 111 | 8.398 | Training | 7.7010 | Prediction | 7.5740 | Prediction | 7.6926 | Prediction | 7.6866 |
| 112 | 9.000 | Training | 8.2665 | Prediction | 8.0393 | Prediction | 8.1465 | Prediction | 8.1606 |

that residual-based model possesses poor external predictivity, hence should not be adopted to create QSAR models. In addition, as many as possible parameters should be reported for a QSAR model developed using single splitting method. Because, the true predictive ability of resid-ual-based model was captured, only when many statistical parameters were calculated.

For some parameters viz. $R_{\mathrm{tr}}^{2}, R_{\mathrm{adj}}^{2}, R_{\mathrm{cv}}^{2}, R_{\mathrm{LMO}}^{2}, R_{\text {Yrand }}^{2}$, $s, K x x, \Delta \mathrm{~K}, R M S E_{t r}, R M S E_{c v}, C C C_{t r}, C C C_{c v}, M A E_{t r}$, $M A E_{c v}$, and $F$, the performance of random splitting model is either statistically satisfactory or comparable with the other models. But, for some parameters viz. $C C C_{e x}, r_{m}^{2} a v$, and $r_{m}^{2}$, the performance of the model is questionable. A large difference of 0.309 between $R_{\mathrm{tr}}^{2}(=0.674)$, and $R_{\mathrm{cv}}^{2}(=0.365)$ for sphere exclusion model reflects large inaccuracy of the model (Schuurmann et al., 2008) or overfitting (Kiralj and Ferreira, 2009). A probable reason could be either the small size of dataset-1 or size of training and prediction sets. But, the problem of large inaccuracy of model or overfitting is not visible for other models. Similarly, the very low value of $F(=7.023)$ indicates low statistical reliability of the sphere exclusion model. A very surprising and rare observation for sphere exclusion model is the higher values of $Q^{2}-F^{1}$ $(=0.706), Q^{2}-F^{2}(=0.705)$, and $Q^{2}-F^{3}(=0.828)$ than $R^{2}$ $(=0.674)$, leading to the contrasting conclusion that the model is able to predict new data better than fitting available ones (Chirico and Gramatica, 2011; 2012).

For residual-based and random splitting models, $R M S E_{t r}$ and $M A E_{t r}$ are lower than $R M S E_{e x}$ and $M A E_{e x}$,
respectively. This indicates that the samples for which the models fit very well are present in the training set. Exactly reverse is true for the sphere exclusion model, for which $R M S E_{t r}$ and $M A E_{t r}$ are higher than $R M S E_{\text {ex }}$ and $M A E_{e x}$, respectively. This observation points out one serious drawback of common practice followed in external validation, in which single split is performed to validate the model. If a researcher purposely selects training and prediction sets such that $R M S E_{t r}$ and $M A E_{t r}$ are higher than $R M S E_{e x}$ and $M A E_{e x}$, respectively then, the model will be with lower internal predictivity but with high external predictivity. In such case, many parameters will give false positive results because of the purposeful selection of training and prediction sets. Therefore, one cannot merely rely on external validation based on single split; instead, boot-strap or multiple modeling (Masand et al., 2014) must be followed to develop a good number of statistically robust QSAR models with good external predictive ability.

As the number of compounds is same in the training and the prediction sets for the three models, the difference between $R^{2}$ and $Q^{2}$ should be comparable for all the models. But, different models have different variation indicating that the method of splitting has good influence on many statistical parameters.

Results for the dataset-2

Similar to the dataset-1, different statistical parameters viz. $R_{\mathrm{tr}}^{2}, R_{\mathrm{adj}}^{2}, R_{\mathrm{cv}}^{2}, R_{\mathrm{LMO}}^{2}, R_{Y r a n d}^{2}, s, R_{e x}^{2}, K x x, \Delta \mathrm{~K}, R M S E_{t r}$,

Table 6 Experimental and predicted $p \mathrm{EC}_{50}$ by different models for dataset-3

| ID | $\begin{aligned} & p \mathrm{EC}_{50} \\ & (\mathrm{M}) \end{aligned}$ | Status | Pred. $p \mathrm{EC}_{50}$ (Original model) | Status | Pred. $p \mathrm{EC}_{50}$ RBM | Status | Pred. $p \mathrm{EC}_{50}$ RSM | Status | Pred. $p \mathrm{EC}_{50}$ SEM |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 5.0460 | Training | 5.2880 | Training | 5.0711 | Prediction | 5.2655 | Training | 5.2987 |
| 2 | 5.8860 | Training | 5.3162 | Prediction | 5.1067 | Prediction | 5.1656 | Training | 5.3758 |
| 3 | 6.0970 | Training | 5.4203 | Prediction | 5.1851 | Training | 5.4203 | Prediction | 5.4266 |
| 4 | 5.5380 | Training | 5.1536 | Prediction | 5.0015 | Prediction | 5.0639 | Training | 5.2397 |
| 5 | 4.8120 | Training | 5.1292 | Training | 4.9953 | Prediction | 5.0477 | Prediction | 5.1723 |
| 6 | 5.2150 | Training | 5.2416 | Training | 5.0927 | Prediction | 5.0486 | Training | 5.3319 |
| 7 | 5.0760 | Training | 5.3873 | Training | 5.1679 | Prediction | 5.3175 | Training | 5.4200 |
| 8 | 5.0860 | Training | 5.2170 | Training | 5.0278 | Training | 5.1048 | Prediction | 5.2875 |
| 9 | 5.1610 | Training | 5.2564 | Training | 5.0749 | Training | 5.1851 | Training | 5.2775 |
| 10 | 5.5530 | Training | 5.2207 | Prediction | 5.0306 | Training | 5.1083 | Training | 5.2915 |
| 11 | 5.3670 | Training | 5.3308 | Prediction | 5.1010 | Prediction | 5.2687 | Training | 5.3750 |
| 12 | 5.0660 | Training | 5.1657 | Training | 5.0194 | Prediction | 4.9778 | Prediction | 5.2299 |
| 13 | 5.0410 | Training | 5.2956 | Training | 5.0944 | Training | 5.2224 | Training | 5.3125 |
| 14 | 4.8570 | Training | 5.2932 | Training | 5.0920 | Training | 5.2728 | Training | 5.2583 |
| 15 | 5.0660 | Training | 5.3473 | Training | 5.1502 | Prediction | 5.3307 | Prediction | 5.3120 |
| 16 | 4.9960 | Training | 5.1086 | Training | 4.9515 | Prediction | 4.9761 | Training | 5.0904 |
| 17 | 5.1670 | Training | 4.9870 | Prediction | 4.8743 | Prediction | 4.8687 | Prediction | 4.9219 |
| 18 | 5.0560 | Training | 5.0659 | Training | 4.9428 | Prediction | 4.8331 | Training | 5.0495 |
| 19 | 5.2150 | Training | 4.9953 | Prediction | 4.8925 | Prediction | 4.9007 | Training | 4.9143 |
| 20 | 4.9630 | Training | 5.1377 | Training | 4.9818 | Training | 5.0357 | Prediction | 5.1872 |
| 21 | 5.6990 | Training | 5.2073 | Prediction | 5.0408 | Training | 5.1339 | Training | 5.2368 |
| 22 | 5.4090 | Training | 5.6696 | Training | 5.3335 | Training | 5.6231 | Training | 5.7631 |
| 23 | 5.9210 | Training | 5.6557 | Prediction | 5.3315 | Training | 5.6635 | Training | 5.7037 |
| 24 | 5.9210 | Training | 5.7666 | Prediction | 5.4245 | Training | 5.6428 | Training | 5.8705 |
| 25 | 5.0560 | Training | 5.6574 | Training | 5.3471 | Training | 5.7013 | Prediction | 5.6881 |
| 26 | 5.0130 | Training | 5.1211 | Training | 4.9909 | Prediction | 5.2146 | Prediction | 5.0824 |
| 27 | 5.0270 | Training | 5.2824 | Training | 5.1005 | Training | 5.3394 | Prediction | 5.2222 |
| 28 | 4.9210 | Training | 5.0851 | Training | 4.9867 | Training | 5.0342 | Prediction | 5.0581 |
| 29 | 6.0000 | Training | 5.3765 | Prediction | 5.1800 | Training | 5.4363 | Prediction | 5.3123 |
| 30 | 5.5230 | Training | 5.6885 | Training | 5.5625 | Prediction | 5.7878 | Training | 5.7320 |
| 31 | 5.9210 | Training | 5.7055 | Prediction | 5.4872 | Prediction | 5.7108 | Prediction | 5.6846 |
| 32 | 5.8540 | Training | 5.8074 | Prediction | 5.6322 | Training | 5.7752 | Training | 5.8473 |
| 33 | 6.0000 | Training | 5.6413 | Prediction | 5.4524 | Prediction | 5.6397 | Training | 5.6148 |
| 34 | 5.0920 | Training | 5.3899 | Training | 5.1492 | Training | 5.4014 | Training | 5.4303 |
| 35 | 5.4320 | Training | 5.3296 | Prediction | 5.1263 | Prediction | 5.3885 | Prediction | 5.3132 |
| 36 | 5.1610 | Training | 5.4215 | Training | 5.1878 | Training | 5.3298 | Prediction | 5.4626 |
| 37 | 5.1670 | Training | 5.3199 | Training | 5.2029 | Prediction | 5.4170 | Training | 5.2786 |
| 38 | 5.3770 | Training | 5.4780 | Training | 5.2955 | Training | 5.5066 | Prediction | 5.4217 |
| 39 | 5.4810 | Training | 5.5637 | Training | 5.3845 | Prediction | 5.5192 | Training | 5.5493 |
| 40 | 5.0920 | Training | 5.4044 | Training | 5.2601 | Prediction | 5.4386 | Training | 5.3439 |
| 41 | 5.0920 | Training | 5.0119 | Prediction | 4.8827 | Training | 4.9975 | Training | 5.0372 |
| 42 | 5.4090 | Training | 5.2179 | Prediction | 5.0396 | Training | 5.2640 | Prediction | 5.2032 |
| 43 | 5.3280 | Training | 4.9977 | Prediction | 4.8990 | Prediction | 4.8683 | Prediction | 5.0198 |
| 44 | 5.4560 | Training | 5.2855 | Prediction | 5.1040 | Training | 5.3574 | Prediction | 5.2528 |
| 45 | 5.4090 | Training | 5.5518 | Training | 5.2783 | Training | 5.5371 | Training | 5.6367 |
| 46 | 6.1550 | Training | 5.7172 | Prediction | 5.4084 | Training | 5.7770 | Prediction | 5.7592 |
| 47 | 5.7960 | Training | 5.8079 | Training | 5.4795 | Prediction | 5.6956 | Prediction | 5.9094 |
| 48 | 6.0000 | Training | 5.7385 | Prediction | 5.4377 | Training | 5.8305 | Training | 5.7611 |

Table 6 continued

| ID | $\begin{aligned} & p \mathrm{EC}_{50} \\ & (\mathrm{M}) \end{aligned}$ | Status | Pred. $p \mathrm{EC}_{50}$ (Original model) | Status | Pred. $p \mathrm{EC}_{50}$ <br> RBM | Status | $\begin{aligned} & \text { Pred. } p \mathrm{EC}_{50} \\ & \text { RSM } \end{aligned}$ | Status | $\begin{aligned} & \text { Pred. } p \mathrm{EC}_{50} \\ & \text { SEM } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49 | 5.0760 | Training | 5.0362 | Prediction | 4.9532 | Prediction | 4.9090 | Training | 5.1036 |
| 50 | 5.7210 | Training | 5.2562 | Prediction | 5.0786 | Prediction | 5.1665 | Prediction | 5.2963 |
| 51 | 5.1190 | Training | 5.2491 | Training | 5.1047 | Training | 5.0739 | Prediction | 5.3336 |
| 52 | 5.0460 | Training | 5.2651 | Training | 5.1029 | Training | 5.1386 | Training | 5.2798 |
| 53 | 5.1190 | Training | 4.9765 | Prediction | 4.8580 | Training | 4.8949 | Prediction | 5.0200 |
| 54 | 5.6020 | Training | 5.5567 | Prediction | 5.2637 | Training | 5.5449 | Prediction | 5.6006 |
| 55 | 5.1870 | Training | 5.3790 | Training | 5.1589 | Prediction | 5.2824 | Prediction | 5.4672 |
| 56 | 5.0410 | Training | 5.5276 | Training | 5.2577 | Training | 5.5819 | Training | 5.5568 |
| 57 | 5.2150 | Training | 5.1070 | Prediction | 5.0042 | Training | 5.2056 | Training | 5.0763 |
| 58 | 5.0270 | Training | 5.1689 | Training | 5.0449 | Training | 5.2921 | Training | 5.1264 |
| 59 | 5.1550 | Training | 5.1929 | Training | 5.0573 | Training | 5.1803 | Training | 5.1693 |
| 60 | 5.5380 | Training | 5.3921 | Prediction | 5.1635 | Prediction | 5.4864 | Prediction | 5.3224 |
| 61 | 5.4090 | Training | 5.5410 | Training | 5.3063 | Prediction | 5.6685 | Prediction | 5.6176 |
| 62 | 5.5690 | Training | 5.5278 | Prediction | 5.2954 | Training | 5.4907 | Training | 5.6434 |
| 63 | 5.4440 | Training | 5.7260 | Training | 5.4307 | Prediction | 5.9172 | Training | 5.7908 |
| 64 | 5.1800 | Training | 5.3365 | Training | 5.1632 | Training | 5.3221 | Prediction | 5.4211 |
| 65 | 5.7700 | Training | 5.6413 | Prediction | 5.3814 | Prediction | 5.7366 | Training | 5.6995 |
| 66 | 5.2680 | Training | 5.3039 | Training | 5.1497 | Training | 5.2291 | Prediction | 5.3851 |
| 67 | 5.4950 | Training | 5.4599 | Prediction | 5.2491 | Training | 5.5817 | Training | 5.4745 |
| 68 | 4.9870 | Training | 5.2660 | Training | 5.0696 | Training | 5.2030 | Prediction | 5.3385 |
| 69 | 6.9590 | Training | 5.7388 | Prediction | 5.4117 | Prediction | 5.7975 | Training | 5.8029 |
| 70 | 5.1310 | Training | 5.3843 | Training | 5.1923 | Prediction | 5.2749 | Prediction | 5.4800 |
| 71 | 5.0320 | Training | 5.5372 | Training | 5.2608 | Prediction | 5.5536 | Training | 5.5362 |
| 72 | 5.4090 | Training | 5.5461 | Training | 5.3585 | Prediction | 5.5900 | Prediction | 5.5134 |
| 73 | 5.6780 | Training | 6.0272 | Training | 5.6627 | Prediction | 6.2168 | Prediction | 6.0480 |
| 74 | 5.6020 | Training | 5.6556 | Training | 5.4393 | Training | 5.6306 | Prediction | 5.6522 |
| 75 | 6.3980 | Training | 6.0451 | Prediction | 5.6965 | Training | 6.2229 | Training | 6.0713 |
| 76 | 4.9430 | Training | 4.8893 | Prediction | 4.8292 | Training | 4.8592 | Training | 4.8908 |
| 77 | 5.0660 | Training | 5.2310 | Training | 5.0376 | Prediction | 5.2929 | Training | 5.2048 |
| 78 | 5.0660 | Training | 4.9741 | Prediction | 4.8859 | Training | 4.9271 | Training | 4.9982 |
| 79 | 5.1190 | Training | 5.0173 | Prediction | 4.8858 | Training | 5.1317 | Training | 4.9584 |
| 80 | 5.0920 | Training | 5.1228 | Training | 4.9395 | Prediction | 5.2270 | Training | 5.1068 |
| 81 | 5.0860 | Training | 5.5045 | Training | 5.2698 | Training | 5.4702 | Prediction | 5.5902 |
| 82 | 5.0810 | Training | 5.1924 | Training | 4.9968 | Prediction | 5.3423 | Prediction | 5.1544 |
| 83 | 5.1430 | Training | 5.3475 | Training | 5.1368 | Training | 5.3156 | Prediction | 5.4093 |
| 84 | 5.6020 | Training | 5.4963 | Prediction | 5.2000 | Training | 5.5783 | Training | 5.5088 |
| 85 | 5.5230 | Training | 5.3221 | Prediction | 5.1095 | Training | 5.2794 | Training | 5.3884 |
| 86 | 6.0460 | Training | 5.6648 | Prediction | 5.3883 | Training | 5.7883 | Prediction | 5.6897 |
| 87 | 5.0600 | Training | 5.1604 | Training | 4.9940 | Prediction | 5.2306 | Training | 5.0745 |
| 88 | 5.5380 | Training | 5.4862 | Prediction | 5.2545 | Training | 5.6187 | Training | 5.4473 |
| 89 | 5.2760 | Training | 5.0955 | Prediction | 4.9946 | Prediction | 5.0613 | Training | 5.0430 |
| 90 | 5.4950 | Training | 5.5162 | Training | 5.2800 | Prediction | 5.6582 | Training | 5.4595 |
| 91 | 5.1940 | Training | 5.3851 | Training | 5.1992 | Prediction | 5.3311 | Prediction | 5.4108 |
| 92 | 5.5380 | Training | 5.1659 | Prediction | 5.0812 | Prediction | 4.9477 | Training | 5.2390 |
| 93 | 6.0000 | Training | 5.5070 | Prediction | 5.2861 | Training | 5.6562 | Prediction | 5.5464 |
| 94 | 5.6580 | Training | 5.4254 | Prediction | 5.2085 | Prediction | 5.3977 | Training | 5.5069 |
| 95 | 5.9210 | Training | 5.7454 | Prediction | 5.4344 | Training | 5.8117 | Training | 5.8043 |
| 96 | 5.0270 | Training | 5.4707 | Training | 5.2993 | Training | 5.3705 | Training | 5.5809 |

Table 6 continued

| ID | $p \mathrm{EC}_{50}$ <br> $(\mathrm{M})$ | Status | Pred. $p \mathrm{EC}_{50}$ <br> (Original model) | Status | Pred. $p \mathrm{EC}_{50}$ <br> RBM | Status | Pred. $p \mathrm{EC}$ <br> RSM | Status | Pred. $p \mathrm{EC}$ <br> REM |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 97 | 5.5530 | Training | 5.6583 | Training | 5.3984 | Training | 5.8009 | Prediction | 5.6963 |
| 98 | 5.1190 | Training | 5.6214 | Training | 5.3299 | Prediction | 5.7446 | Prediction | 5.6112 |
| 99 | 5.2290 | Training | 5.2426 | Training | 5.0457 | Training | 5.3492 | Prediction | 5.2081 |
| 100 | 5.2520 | Training | 5.4367 | Training | 5.1699 | Training | 5.3379 | Training | 5.4874 |

Table 7 Comparison of statistical parameters for original model for dataset-1, 2 and 3

| Statistical Parameter | DataSet-1 | DataSet-2 | DataSet-3 |
| :--- | :---: | :---: | :---: |
| $R_{\mathrm{tr}}^{2}$ | 0.709 | 0.841 | 0.410 |
| $R_{\mathrm{adj}}^{2}$ | 0.670 | 0.837 | 0.378 |
| $R_{\mathrm{cv}}^{2}$ | 0.597 | 0.827 | 0.344 |
| $R_{\mathrm{LMO}}^{2}$ | 0.723 | 0.843 | 0.419 |
| $R_{Y \text { Yrand }}^{2}$ | 0.120 | 0.242 | 0.050 |
| $Q_{Y r a n d}^{2}$ | -0.185 | -0.488 | -0.076 |
| $s$ | 0.250 | 0.242 | 0.300 |
| $K x x$ | 0.425 | 0.245 | 0.208 |
| $\Delta K$ | 0.025 | 0.209 | 0.027 |
| $R M S E_{t r}$ | 0.233 | 0.238 | 0.291 |
| $R M S E_{c v}$ | 0.274 | 0.248 | 0.307 |
| $C C C_{t r}$ | 0.830 | 0.914 | 0.581 |
| $C C C_{c v}$ | 0.763 | 0.906 | 0.537 |
| $M A E_{t r}$ | 0.193 | 0.172 | 0.226 |
| $M A E_{c v}$ | 0.226 | 0.179 | 0.239 |
| $F$ | 18.50 | 190.388 | 13.047 |
| $r^{2}$ | 0.601 | 0.827 | 0.347 |
| $r_{o}^{2}$ | 0.429 | 0.793 | -0.574 |
| $1-\left(r^{2} / r_{o}^{2}\right)$ | 0.285 | 0.040 | 2.653 |
| $r_{o}^{2}$ | 0.597 | 0.827 | 0.344 |
| $1-\left(r^{2} / r_{o}^{\prime 2}\right)$ | 0.007 | 0.000 | 0.009 |
| $k$ | 0.996 | 0.999 | 0.997 |
| $k^{\prime}$ | 1.001 | 1.000 | 0.999 |
|  |  |  |  |

$R M S E_{c v}, C C C_{t r}, C C C_{c v}, M A E_{t r}, M A E_{c v}$, and $r_{m}^{2} a v$ indicate good predictive ability and robust statistical performance of the residual-based model than the other models. The high value of $r_{m}^{2}(=0.744)$ for residual model, though lower than sphere exclusion model $(=0.804)$, indicates good external predictivity. A very high $F(=328.459)$ value for residual-based model than the other models $(=112.835$ for random splitting and 111.362 for sphere exclusion model) indicates very high statistical significance of regression model. Similar to dataset-1, a large difference between $R M S E_{t r}(=0.143)$ and $R M S E_{e x}(=0.405)$ as well as between $M A E_{\text {tr }} \quad(=0.109)$ and $M A E_{\text {ex }}(=0.353)$ suggests low

Table 8 Comparison of statistical parameters for original, residualbased rational, random splitting, and sphere exclusion models for dataset-1

| Statistical <br> Parameter | Original model | Residualbased model | Random splitting Model | Sphere exclusion model |
| :---: | :---: | :---: | :---: | :---: |
| $R_{\text {tr }}^{2}$ | 0.709 | 0.855 | 0.801 | 0.674 |
| $R_{\text {adj }}^{2}$. | 0.670 | 0.813 | 0.743 | 0.578 |
| $R_{\text {cv }}^{2}$ | 0.597 | 0.732 | 0.640 | 0.365 |
| $R_{\text {LMO }}^{2}$ | 0.723 | 0.871 | 0.815 | 0.709 |
| $s$ | 0.250 | 0.137 | 0.241 | 0.320 |
| $R_{e x}^{2}$ | - | 0.845 | 0.418 | 0.722 |
| $R_{\text {Yrand }}^{2}$ | 0.120 | 0.223 | 0.238 | 0.231 |
| $Q_{\text {Yrand }}^{2}$ | -0.185 | -0.443 | -0.421 | $-0.433$ |
| Kxx | 0.425 | 0.457 | 0.452 | 0.446 |
| $\Delta K$ | 0.025 | 0.036 | 0.015 | 0.017 |
| $R M S E_{t r}$ | 0.233 | 0.118 | 0.207 | 0.275 |
| $R M S E_{c v}$ | 0.274 | 0.159 | 0.279 | 0.384 |
| $R M S E_{\text {ex }}$ | - | 0.441 | 0.344 | 0.200 |
| $C C C_{t r}$ | 0.830 | 0.922 | 0.890 | 0.805 |
| $C C C_{c v}$ | 0.763 | 0.859 | 0.795 | 0.621 |
| $C C C_{e x}$ | - | 0.606 | 0.611 | 0.845 |
| $M A E_{\text {tr }}$ | 0.193 | 0.089 | 0.161 | 0.238 |
| $M A E_{c v}$ | 0.226 | 0.122 | 0.220 | 0.325 |
| $M A E_{\text {ex }}$ | - | 0.394 | 0.260 | 0.169 |
| $Q^{2}-F^{1}$ | - | 0.443 | 0.266 | 0.706 |
| $Q^{2}-F^{2}$ | - | 0.097 | 0.266 | 0.705 |
| $Q^{2}-F^{3}$ | - | -1.039 | 0.451 | 0.828 |
| $r^{2} m$ | - | 0.762 | 0.290 | 0.655 |
| $r^{2} m a v$ | - | 0.678 | 0.270 | 0.612 |
| $r^{2} m d e$ | - | 0.168 | 0.040 | 0.085 |
| $F$ | 18.50 | 20.120 | 13.714 | 7.023 |
| $r^{2}$ | 0.601 | 0.845 | 0.418 | 0.722 |
| $r_{o}^{2}$ | 0.429 | 0.757 | 0.256 | 0.677 |
| 1-( $\left.r^{2} / r_{o}^{2}\right)$ | 0.285 | 0.105 | 0.386 | 0.062 |
| $r_{o}^{\prime 2}$ | 0.597 | 0.836 | 0.324 | 0.713 |
| $1-\left(r^{2} / r_{o}^{2}\right)$ | 0.007 | 0.011 | 0.223 | 0.012 |
| $k$ | 0.996 | 0.916 | 0.974 | 1.005 |
| $k^{\prime}$ | 1.001 | 1.089 | 1.021 | 0.993 |

Table 9 Comparison of statistical parameters for original, residualbased rational, random splitting, and sphere exclusion models for dataset-2

| Statistical <br> Parameter | Original model | Residualbased model | Random splitting Model | Sphere exclusion model |
| :---: | :---: | :---: | :---: | :---: |
| $R_{\text {tr }}^{2}$ | 0.841 | 0.945 | 0.856 | 0.854 |
| $R_{\text {adj. }}^{2}$. | 0.837 | 0.942 | 0.848 | 0.847 |
| $R_{\text {cv }}^{2}$ | 0.827 | 0.934 | 0.836 | 0.834 |
| $R_{\text {LMO }}^{2}$ | 0.843 | 0.947 | 0.859 | 0.855 |
| $s$ | 0.242 | 0.148 | 0.212 | 0.227 |
| $R_{\text {ex }}^{2}$ | - | 0.877 | 0.842 | 0.816 |
| $R_{\text {Yrand }}^{2}$ | 0.242 | 0.052 | 0.053 | 0.051 |
| $Q_{\text {Yrand }}^{2}$ | -0.488 | -0.087 | -0.086 | -0.089 |
| Kxx | 0.245 | 0.246 | 0.293 | 0.220 |
| $\Delta K$ | 0.209 | 0.231 | 0.201 | 0.219 |
| $R M S E_{t r}$ | 0.238 | 0.143 | 0.205 | 0.220 |
| $R M S E_{c v}$ | 0.248 | 0.157 | 0.219 | 0.234 |
| $R M S E_{\text {ex }}$ | - | 0.405 | 0.287 | 0.266 |
| $C C C_{t r}$ | 0.914 | 0.972 | 0.922 | 0.921 |
| $C C C_{c v}$ | 0.906 | 0.967 | 0.912 | 0.911 |
| $C C C_{e x}$ | - | 0.777 | 0.876 | 0.893 |
| $M A E_{\text {tr }}$ | 0.172 | 0.109 | 0.149 | 0.166 |
| $M A E_{c v}$ | 0.179 | 0.119 | 0.160 | 0.177 |
| $M A E_{\text {ex }}$ | - | 0.353 | 0.197 | 0.187 |
| $Q^{2}-F^{1}$ | - | 0.553 | 0.809 | 0.822 |
| $Q^{2}-F^{2}$ | - | 0.442 | 0.809 | 0.810 |
| $Q^{2}-F^{3}$ | - | 0.561 | 0.717 | 0.788 |
| $r^{2} m$ | - | 0.744 | 0.689 | 0.804 |
| $r^{2} m a v$ | - | 0.803 | 0.581 | 0.720 |
| $r^{2} m d e$ | - | 0.118 | 0.217 | 0.168 |
| $F$ | 190.388 | 328.459 | 112.835 | 111.362 |
| $r^{2}$ | 0.827 | 0.877 | 0.842 | 0.816 |
| $r_{o}^{2}$ | 0.793 | 0.877 | 0.649 | 0.768 |
| $1-\left(r^{2} / r_{o}^{2}\right)$ | 0.040 | 0.000 | 0.229 | 0.060 |
| $r_{o}^{\prime 2}$ | 0.827 | 0.854 | 0.809 | 0.816 |
| $1-\left(r^{2} / r^{\prime 2}\right)$ | 0.000 | 0.026 | 0.039 | 0.000 |
| $k$ | 0.999 | 0.953 | 1.000 | 0.992 |
| $k^{\prime}$ | 1.000 | 1.048 | 0.998 | 1.007 |

generalizability of the residual-based model. In addition, the lower value of $C C C_{e x}, Q^{2}-F^{1}, Q^{2}-F^{2}$, and $Q^{2}-F^{3}$ for residual-based model than random splitting model, and sphere exclusion model points out low true external predictivity of this model.

A conceivable reason for the lower values of $Q^{2}-F^{1}$, $Q^{2}-F^{2}$, and $Q^{2}-F^{3}$ could be the presence of prediction set objects near the boundary of the training set (Chirico and Gramatica, 2011, 2012; Consonni et al., 2009, 2010; Schuurmann et al., 2008). Again, these statistical

Table 10 Comparison of statistical parameters for original, residualbased rational, random splitting, and sphere exclusion models for dataset-3

| Statistical parameter | Original model | Residualbased model | Random splitting Model | Sphere exclusion model |
| :---: | :---: | :---: | :---: | :---: |
| $R_{\text {tr }}^{2}$ | 0.410 | 0.621 | 0.527 | 0.478 |
| $R_{\text {adj. }}^{2}$. | 0.378 | 0.583 | 0.478 | 0.426 |
| $R_{\text {cv }}^{2}$ | 0.344 | 0.516 | 0.430 | 0.365 |
| $R_{\text {LMO }}^{2}$ | 0.419 | 0.634 | 0.537 | 0.495 |
| $s$ | 0.300 | 0.134 | 0.279 | 0.305 |
| $R_{\text {ex }}^{2}$ | - | 0.662 | 0.237 | 0.280 |
| $R_{\text {Yrand }}^{2}$ | 0.050 | 0.093 | 0.090 | 0.092 |
| $Q_{\text {Yrand }}^{2}$ | -0.076 | -0.144 | -0.153 | -0.142 |
| Kxx | 0.208 | 0.176 | 0.232 | 0.203 |
| $\Delta K$ | 0.027 | 0.084 | 0.028 | 0.079 |
| $R M S E_{t r}$ | 0.291 | 0.127 | 0.263 | 0.288 |
| RMSE ${ }_{c v}$ | 0.307 | 0.143 | 0.289 | 0.318 |
| $R M S E_{\text {ex }}$ | - | 0.524 | 0.353 | 0.306 |
| $C C C_{t r}$ | 0.581 | 0.766 | 0.690 | 0.647 |
| $C C C_{c v}$ | 0.537 | 0.704 | 0.625 | 0.575 |
| $C C C_{e x}$ | - | 0.339 | 0.480 | 0.488 |
| $M A E_{t r}$ | 0.226 | 0.099 | 0.203 | 0.212 |
| $M A E_{c v}$ | 0.239 | 0.112 | 0.225 | 0.236 |
| $M A E_{\text {ex }}$ | - | 0.458 | 0.280 | 0.257 |
| $Q^{2}-F^{1}$ | - | 0.239 | 0.112 | 0.246 |
| $Q^{2}-F^{2}$ | - | $-0.728$ | 0.105 | 0.238 |
| $Q^{2}-F^{3}$ | - | -5.512 | 0.145 | 0.414 |
| $r^{2} m$ | - | 0.516 | 0.151 | 0.238 |
| $r^{2} m a v$ | - | 0.302 | 0.113 | 0.127 |
| $r^{2} m d e$ | - | 0.430 | 0.077 | 0.220 |
| $F$ | 13.047 | 16.382 | 10.909 | 9.158 |
| $r^{2}$ | 0.347 | 0.662 | 0.237 | 0.280 |
| $r_{o}^{2}$ | -0.574 | -0.093 | -0.235 | -0.602 |
| 1-( $\left.r^{2} / r_{o}^{2}\right)$ | 2.653 | 1.141 | 1.991 | 3.150 |
| $r_{o}^{\prime 2}$ | 0.344 | 0.614 | 0.106 | 0.257 |
| $1-\left(r^{2} / r_{o}^{\prime 2}\right)$ | 0.009 | 0.073 | 0.554 | 0.082 |
| $k$ | 0.997 | 0.916 | 0.995 | 1.006 |
| $k^{\prime}$ | 0.999 | 1.089 | 1.001 | 0.257 |

parameters are sensitive to mean of training and prediction sets, a simple analysis of Table 11 reveals that the mean of the test and the training sets of residual-based model have higher difference than the rest (Chirico and Gramatica 2011, 2012; Consonni et al., 2009, 2010; Schuurmann et al., 2008). This observation once again confirms that the distribution of the test and the training set has important impact on performance of many statistical parameters. Thus, the residual-based model is scoring high for many parameters suggesting statistical robustness of this model,

Table 11 Mean of experimental $p \mathrm{IC}_{50}$ for prediction and training sets of various models for datasets $1-3$

| DataSet | Set | Original | Residual- <br> based <br> model | Random <br> splitting <br> Model | Sphere <br> exclusion <br> model |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | Prediction | - | 4.8308 | 4.6389 | 4.6509 |
|  | Training | 4.6397 | 4.4652 | 4.6404 | 4.6295 |
| 2 | Prediction | - | 7.5342 | 7.3803 | 7.3017 |
|  | Training | 7.3867 | 7.2633 | 7.3921 | 7.4577 |
| 3 | Prediction | - | 5.6296 | 5.3598 | 5.3570 |
|  | Training | 5.3778 | 5.1799 | 5.3925 | 5.3941 |

but some parameters raise doubts on its external predictivity.

Results for the dataset-3
Various statistical parameters viz. $R_{\mathrm{tr}}^{2}, R_{\mathrm{adj}}^{2}, R_{\mathrm{cv}}^{2}, R_{\mathrm{LMO}}^{2}$, $R_{\text {Yrand }}^{2}, s, R_{e x}^{2}, K x x, \Delta \mathrm{~K}, R M S E_{t r}, R M S E_{c v}, C C C_{t r}, C C C_{c v}$, $M A E_{t r}, M A E_{c v}, r_{m}^{2} a v$, and $F$ (see Table 10) indicate low predictive ability and poor statistical performance of all the models. But, a closer inspection of various models indicates that the performance of residual-based model is better than the other models. Some of the statistical parameters like $R \underset{\mathrm{t}}{2}, R_{\mathrm{LMO}}^{2}, s, R_{e x}^{2}, R M S E_{t r}, R M S E_{c v}, M A E_{t r}$, and $M A E_{c v}$ are with acceptable values. However, the model possesses low internal and external predictivity. As stated earlier, it is not a useful model at all for the prediction and pattern recognition. The $Q^{2}-F^{2}$ and $Q^{2}-F^{3}$ are negative which indicates that the model is useless for external predictivity.

Comparison of performance of splitting methodologies and statistical behavior of statistical parameters

In the present analysis, information leakage was purposely performed for RBM. The descriptors were selected using the whole dataset, therefore, due to the information leakage, the selected descriptors must have captured the common structural features that influence the activity, and consequently, after splitting in any pattern/composition, the performance of RBM model for the all the datasets must be superior than SEM and RSM with respect to internal and external cross-validation parameters, i.e., must show high level of external predictivity with high validation score. Surprisingly, for RBM model, various validation parameters do not show expected behavior and values for all the datasets.

The random splitting models, for all the datasets, have varying performance; this could be due to the fact that during splitting the training or prediction set may not be
covering the diversity of the whole dataset or the compounds are not close to each other. Repeating the random splitting several times is a good solution to arrive at best random splitting (Huang and Fan, 2011; Kiralj and Ferreira, 2009). Yet, as pointed out in a recent study, a QSAR model with high external predictivity for one prediction set does not necessarily indicate high accuracy for another external set (Huang and Fan, 2011). Therefore, precautions must be taken in using single random splitting.

Since, the performance of the RBM, RSM, and SEM models is varying, but by luck or due to rational splitting, the researcher may arrive at the training and prediction sets that indicate high external predictive ability, such situation, though, leads to a statistically robust but a misguiding QSAR model as observed in RBM. An easy and handy solution to this problem is to develop a model using undivided dataset and compare its performance with the other models. Herein, in all the datasets, the performance of original model, though not better than residual based and sphere exclusion models, is still statistically satisfactory. It is expected that a model developed with no prediction set will be most accurate and possess the highest coverage for external evaluation set. But, a recent study reports exactly opposite results in certain situations (Martin et al., 2012). Therefore, we recommend and accentuate reporting of a statistically robust QSAR model that is developed using undivided whole dataset and same set of descriptors, which were selected and used in splitting-based model. Then, such a model tells the true effect of inclusion of compounds in the dataset. That is, it is useful in understanding the effect of increase/decrease in size of dataset as well as for capturing less privileged yet useful structural features that govern the activity.

A higher value of $R_{\mathrm{tr}}^{2}$ for residual-based model in all the datasets than the rest of the models indicates a better fitting or explanation of variance (see Tables 8-10). Similar trend for $R_{\text {ex }}^{2}$ for residual-based model for different datasets confers as if the residual based splitting is better method of splitting. Therefore, a QSAR modeler may consider the residual-based model superior than others. This apparent superiority can be attributed to the purposeful selection of the training and the prediction sets, that is, the method of splitting has significant impact on many statistical parameters. Moreover, a careful comparison of residual values for all the models (see Fig. 3) reveals that the difference between the experimental and predicted in many instances is large in case of residual-based model than the others. But, during the calculation of various statistical parameters either sum or average is used. Therefore, the statistical parameters are unable to recognize this serious pitfall. In fact, a QSAR model based on splitting method with an unusually robust training set $R_{\mathrm{tr}}^{2}$ of 0.8 or greater than $R_{\mathrm{tr}}^{2}$ of undivided set

Fig. 3 Difference between experimental and predicted $p \mathrm{IC}_{50}$ by various models for dataset-1, 2, and 3 ( $X$-axis: Compound number and $Y$-axis: $p \mathrm{IC}_{50} / p \mathrm{EC}_{50} ; X$-axis: Serial number of compound, $Y$-axis: $\mathrm{pIC}_{50}$ value)


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should be viewed with suspicion. Some parameters like $C C C_{e x}, Q^{2}-F^{1}, Q^{2}-F^{2}, Q^{2}-F^{3}$, and $r_{m}^{2}$ are more successful in identifying this crucial aspect. This can be ascribed to the method of calculation of these parameters (Chirico and Gramatica, 2011, 2012); (Consonni et al., 2009, 2010; Schuurmann et al., 2008).

$$
\begin{aligned}
& Q^{2}-F^{1}=1-\frac{\sum_{i=1}^{n_{\text {ext }}}(\widehat{y} i-y i)^{2}}{\sum_{i=1}^{n_{\text {ext }}}\left(y i-\bar{y}_{t r}\right)^{2}} \\
& Q^{2}-F^{3}=1-\frac{\sum_{i=1}^{n_{\text {ext }}}(\widehat{y} i-y i)^{2} / n_{\text {ext }}}{\sum_{i=1}^{n_{\text {tr }}}\left(y i-\bar{y}_{t r}\right)^{2} / n_{t r}} \\
& Q^{2}-F^{2}=1-\frac{\sum_{i=1}^{n_{\text {ext }}}(\widehat{y} i-y i)^{2}}{\sum_{i=1}^{n_{\text {ext }}}\left(y i-\bar{y}_{e x t}\right)^{2}} \\
& r_{m}^{2}=r^{2}\left(1-\sqrt{\left.r^{2}+r_{o}^{2}\right)}\right.
\end{aligned}
$$

Thus, $r_{m}^{2}$ considers agreement between the actual and the predicted values as an essential factor to establish the true predictivity (Mitra et al., 2010; Roy and Mitra, 2012). Thence, the statistical parameters viz. $C C C_{e x}, Q^{2}-F^{1}, Q^{2}-$ $F^{2}, Q^{2}-F^{3}$, and $r_{m}^{2}$ reflect the factual performance of model regarding true external predictivity of a QSAR model. Therefore, these parameters should be used as criteria for selection of a consensus model, as in QSARINS v1.2. In QSARINS v1.2, MAE $E_{\mathrm{tr}}, M A E_{\mathrm{ex}}, R M S E_{\mathrm{tr}}, R M S E_{\mathrm{ex}}, C C C_{\mathrm{tr}}$, $C C C_{e x}, Q^{2}-F^{1}, Q^{2}-F^{2}, Q^{2}-F^{3}$, and some other parameters are used to find a consensus model.

In agreement with the previous reports, the trend of lower CCC with higher RMSE value is true for all the datasets (Chirico and Gramatica, 2011, 2012). However, the claim that the smaller the dataset size, the better the performances of $r_{\mathrm{m}}^{2}$-EyPx and CCC compared to the other external validation measures was not observed for any of the dataset (Chirico and Gramatica, 2011, 2012). The similar values of $Q^{2}-F^{1}$ and $Q^{2}-F^{2}$ for random splitting model for dataset 1 and 2 can be attributed to the fact that these parameters depend on agreement between the mean of the training and the prediction set values (Consonni et al., 2009, 2010). For dataset 1 and 2 , the mean of test and training sets values is very close to each other (see Table 11). A good difference between the mean of the undivided set and the training set values of the residual-based model for all the datasets indicates that the prediction set was not selected properly. Such a noticeable difference is absent in case of other models. This again indicates that residual-based method of
splitting cannot be functionalised for splitting the dataset for external validation.

Since the whole dataset is involved in descriptor selection and model development, another point view toward the present approach is to consider it as a methodology to develop a model with good external predictivity using advantages of internal validation method. A model with good internal predictivity may or may not be good at external predictivity (Chirico and Gramatica, 2011, 2012; Consonni et al., 2009, 2010; Gramatica 2013, Schuurmann et al., 2008). In the present analysis, sphere exclusion model with higher values of $Q^{2}-F^{3}, C C C_{\text {ex }}$, and lower values of $R M S E_{e x}, M A E_{e x}$ indicate good external predictivity of model.

Consonni et al. argued that increasing the mean of training set values increases $Q^{2}$ artificially (Consonni et al., 2009). From Table 11, it is observed that the mean of the training set values for the random (for dataset- 1 and 2 ) and the sphere exclusion models (for dataset-1) is very close to mean of undivided set values; therefore, the value of $Q^{2}$ for these models should be close to $Q^{2}$ of the original model. However, for random splitting model, $Q^{2}=0.640$ for dataset-1, and $Q^{2}=0.836$ for dataset-2 are higher than that of the original model ( $Q^{2}=0.597$ ). In addition, lower $Q^{2}=0.365$ for sphere exclusion model for dataset-1 than $Q^{2}=0.597$ for original model conflicts the finding of Consonni et al. The mean of the training set for residual model ( $=4.4652$ ) is lower than mean of training set of undivided set ( $=4.6397$ ). Therefore, for the sphere exclusion model, $Q^{2}$ should be lower than the $Q^{2}$ for original model, but the results are exactly opposite. Therefore, further studies are required to understand the effect of mean of training set on $Q^{2}$.

## Conclusions

In conclusion, external validation based on single splitting is neither perfect nor absolutely accurate method of QSAR model validation as the statistical parameters can be influenced easily due to the biased and purposeful selection of the training and prediction sets. Moreover, the predictive ability of a QSAR model is sensitive toward the method of splitting and its manipulation is feasible. Thus, it is still insufficient to guarantee the true predictability of a QSAR model. The true external predictivity of any QSAR model cannot be decided on the basis of one or two parameters, that is, as many as possible statistical parameters should be calculated to judge the external predictivity. A good number of statistical parameters need to be calculated and presented to identify the true external predictivity of any QSAR model. We
suggest and emphasize reporting of at least one statistically robust QSAR model that is developed using undivided whole dataset with appropriate cross validation.

In the present study, we presented a novel method for splitting the dataset for external validation. The residual method, though, generates statistically robust model but with low external predictivity. Further studies are in progress for the improvement of this method.

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