

Effects of Chemical Reaction on Free Convection MHD Flow through Porous Medium Bounded by Vertical Surface with Slip Flow Region

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Abstract The effects of chemical reaction in two dimensional steady free convective flow of an electrically conducting viscous fluid through a porous medium bounded by vertical surface with slip flow region has been studied. A uniform magnetic field is assumed to be applied transversely in the direction of the flow. A chemically reactive species is emitted from the vertical surface into the flow field. The governing equations are developed by usual Boussinesq's approximation. The problem is solved by regular perturbation technique. The expressions for the velocity field, temperature field, species concentration, shearing stress and the coefficient of heat transfer (in terms of Nusselt number) at the walls are obtained and their nature has been discussed by means of graphs. The effects of Hartmann number, the rarefaction parameter, the porous parameter, Schmidt number and chemical reaction parameter on the flow are discussed.

Keywords MHD, Free Convective, Viscous Incompressible, Skin Friction, Nusselt Number, Chemical Reaction, Slip Flow Region

1. Introduction

The growing need for chemical reaction in industries and engineering requires the study of heat and mass transfer in the presence of different conditions and parameters with chemical reaction. There are many transfer processes governed by the combined action of buoyancy forces due to both thermal and mass diffusion in the presence of chemical reaction. It has many applications in nuclear reactor and combustion, solar collectors, drying, dehydration operations in chemical and food processing plants, polymer production etc. The effect of a chemical reaction on a moving isothermal vertical surface with suction has been considered by Muthucumaraswamy [1]. Considering this on the study of a chemical reaction, Kandasamy et al. [2] considered the chemical reaction and thermal stratification effects over a vertical stretching surface. Application of a chemical reaction to a micropolar flow over an isothermal vertical cone has been studied by El-Kabeir et al. [3]. Ibrahim et al. [4] have studied the chemical reaction and absorption effects on the unsteady mhd flow past a semi infinite vertical permeable moving

plate. Muthucumaraswamy et al. [5] have studied the mass transfer effect on isothermal vertical oscillating plate in presence of chemical reaction. Makinde et al. [6] have considered the heat and mass transfer effect on a flow with variable viscosity without chemical reaction. Recently the effect of chemical reaction on free convection flow through a porous medium bounded by a vertical surface was reported by Das et al. [7]. Ibrahim et al. [8] have studied the chemical reaction effect on mhd boundary layer flow of heat and mass transfer over a moving vertical plate with suction. Also the chemical reaction effects on heat and mass transfer flow have been considered by Pal et al. [9] and Ibrahim et al. [10]. Rushi Kumar [11] have studied the effect of heat generation and radiation on mhd boundary layer flow in porous vertical flat plate.

It is proposed to study the effects of chemical reaction on free convection mhd flow through porous medium bounded by vertical surface with slip flow region.

2. Formulation of Problem

We consider a steady flow of an incompressible viscous electrically conducting fluid through porous medium bounded by semi infinite vertical surface with slip flow region by making the following assumptions:

1. All fluid properties except the density in the buoyancy force term are constant.

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2. The magnetic dissipation term in the energy equation is negligible.

3. The Eckert number Ec is small.

4. The magnetic Reynolds Number is so small that the induced magnetic field is negligible.

5. A chemically reactive species is emitted from the vertical surface into magneto hydrodynamic flow field. It diffuses into the fluid, where it undergoes a homogenous chemical reaction. As the level of species concentration is very low, therefore heat generation due to chemical reaction is neglected.

X-axis is taken along semi vertical surface and Y'-axis is normal to it. A uniform magnetic field of strength H_0 has been applied perpendicular to the vertical surface and the magnetic permeability μ_c is constant throughout the field. T'_w and T'_∞ are the temperature and C'_w and C'_∞ are the mass concentration of surface and fluid respectively. Then by usual Boussinesq's approximation the steady flow is governed by the following equations:

$$\frac{dv'}{dy'} = 0 \tag{1}$$

$$v' \frac{du'}{dy'} = v \frac{d^2u'}{dy'^2} + g\beta(T' - T'_\infty) + g\beta_c(C' - C'_\infty) - \frac{v u'}{K'} - \frac{\sigma B_0^2 u'}{\rho} \tag{2}$$

$$v' \frac{dT'}{dy'} = \frac{k}{\rho c_p} \frac{d^2T'}{dy'^2} + \frac{v}{c_p} \left(\frac{du'}{dy'}\right)^2 \tag{3}$$

$$v' \frac{dC'}{dy'} = D \frac{d^2C'}{dy'^2} - R'(C' - C'_\infty) \tag{4}$$

with relevant boundary conditions:

$$\left. \begin{aligned} u' &= h' \frac{du'}{dy'}, T' = T'_w, C' = C'_w \text{ at } y' = 0 \\ u' &\rightarrow 0, T' \rightarrow T'_\infty, C' \rightarrow C'_\infty \text{ as } y' \rightarrow \infty \end{aligned} \right\} \tag{5}$$

By integrating equation (1), we get

$$v' = -v_0 \tag{6}$$

is the steady normal velocity suction on the surface.

Let us introduce the following non-dimensional quantities:

$$\begin{aligned} y &= \frac{v_0 y'}{h}, u = \frac{u'}{v_0}, \theta = \frac{T' - T'_\infty}{T'_w - T'_\infty}, C = \frac{C' - C'_\infty}{C'_w - C'_\infty}, Sc = \frac{v}{D}, Pr = \frac{\mu c_p}{k} \\ Gr &= \frac{v g \beta (T'_w - T'_\infty)}{v_0^3}, Gm = \frac{v g \beta_c (C'_w - C'_\infty)}{v_0^3}, E = \frac{v_0^2}{c_p (T'_w - T'_\infty)}, K = \frac{v_0^2 K'}{v^2} \end{aligned} \tag{7}$$

With corresponding boundary conditions

$$\left. \begin{aligned} u_0 &= h \frac{du_0}{dy}, u_1 = h \frac{du_1}{dy}, \theta_0 = 1, \theta_1 = 0, C_0 = 1, C_1 = 0 \text{ at } y = 0 \\ u_0 &\rightarrow 0, u_1 \rightarrow 0, \theta_0 \rightarrow 0, \theta_1 \rightarrow 0, C_0 \rightarrow 0, C_1 \rightarrow 0 \text{ as } y \rightarrow \infty \end{aligned} \right\} \tag{19}$$

By solving equations (13) – (18), using the boundary condition (19), we get the following

$$\begin{aligned} u &= (A_{13} e^{-a_{12}y} - A_{11} e^{-Pr y} - A_{12} e^{-a_{11}y}) \\ &+ E(A_{28} e^{-a_{12}y} + A_{21} e^{-Pr y} + A_{22} e^{-2 a_{12}y} + A_{23} e^{-2 Pr y} + A_{24} e^{-2 a_{11}y} - A_{25} e^{-(a_{12}+Pr)y} + A_{26} e^{-(a_{11}+Pr)y} - \\ &A_{27} e^{-a_{11}+a_{12}y} \end{aligned} \tag{19}$$

$$\begin{aligned} \theta &= e^{-Pr y} + E(A_{20} e^{-Pr y} + A_{14} e^{-2 a_{12}y} + A_{15} e^{-2 Pr y} + A_{16} e^{-2 a_{11}y} - A_{17} e^{-(a_{12}+Pr)y} + A_{18} e^{-(a_{11}+Pr)y} - A_{19} e^{-(a_{11}+a_{12})y}) \end{aligned} \tag{20}$$

$$C = e^{-a_{11}y} \tag{21}$$

where $a_{11} = \frac{Sc + \sqrt{Sc^2 + 4ScR}}{2}$, $a_{12} = \frac{1 + \sqrt{1 + 4(\frac{1}{K} + M)}}{2}$, $A_{11} = \frac{Gr}{Pr^2 + Pr - (\frac{1}{K} + M)}$, $A_{12} = \frac{Gm}{a_{11}^2 + a_{11} - (\frac{1}{K} + M)}$,

$$M = \frac{\sigma B_0^2 v}{\rho v_0^2}, \quad h = h' \frac{v_0^2}{v}, \quad R = \frac{v R'}{v_0^2}$$

where Pr is the Prandtl number, Sc is the Schmidt number, Gr is the Grashof number for heat transfer, Gm is the Grashof number for mass transfer, E is the Eckert number, K is the permeability parameter of the porous medium, R is chemical reaction parameter, h is rarefaction parameter and M is the Hartmann number. With the help of equations (6) and (7) the equations (2) to (5) reduce to

$$u'' + u' - \left(\frac{1}{K} + M\right)u = -Gr\theta - GmC \tag{8}$$

$$\theta'' + Pr\theta' = -Pr(u')^2 \tag{9}$$

$$C'' + ScC' = RScC \tag{10}$$

with the corresponding boundary conditions

$$u = h \frac{du}{dy}, \theta = 1, C = 1 \text{ at } y = 0 \tag{11}$$

$$u \rightarrow 0, \theta \rightarrow 0, C \rightarrow 0 \text{ as } y \rightarrow \infty$$

3. Method of Solution

In order to obtain solutions of coupled nonlinear system of equations (8) –(10) with boundary conditions (11) ,we expand u, θ and C in the powers of Eckert number E(assuming very small)

$$\text{Let } u = u_0 + Eu_1 + O(E^2)$$

$$\theta = \theta_0 + E\theta_1 + O(E^2)$$

$$C = C_0 + EC_1 + O(E^2) \tag{12}$$

Substituting equations (12) into equations (8) –(10) with boundary conditions, and equating the coefficients of same power of E and neglecting the higher power of E, we get the following equations.

$$u''_0 + u'_0 - \left(\frac{1}{K} + M\right)u_0 = -Gr\theta_0 - GmC_0 \tag{13}$$

$$\theta''_0 + Pr\theta'_0 = 0 \tag{14}$$

$$C''_0 + ScC'_0 - RScC_0 = 0 \tag{15}$$

$$u''_1 + u'_1 - \left(\frac{1}{K} + M\right)u_1 = -Gr\theta_1 - GmC_1 \tag{16}$$

$$\theta''_1 + Pr\theta'_1 = -Pr u_0'^2 \tag{17}$$

$$C''_1 + ScC'_1 - RScC_1 = 0 \tag{18}$$

$$\begin{aligned}
 A_{13} &= \frac{hA_{11}Pr + ha_{11}A_{12} + A_{11} + A_{12}}{1 + ha_{12}}, A_{14} = \frac{PrA_{12}^2A_{13}^2}{4a_{12}^2 - 2Pra_{12}}, A_{15} = \frac{PrA_{11}^2}{2} \\
 A_{16} &= \frac{PrA_{12}^2a_{11}^2}{4a_{11}^2 - 2Pra_{11}}, A_{17} = \frac{2Pr^2a_{12}A_{13}A_{11}}{(a_{12} + Pr)^2 - Pr(a_{12} + Pr)}, \\
 A_{18} &= \frac{2Pra_{11}A_{12}A_{13}a_{12}}{(a_{11} + Pr)^2 - Pr(a_{11} + Pr)}, A_{19} = \frac{2Pra_{11}A_{12}A_{13}a_{12}}{(a_{11} + a_{12})^2 - Pr(a_{11} + a_{12})} \\
 A_{20} &= A_{17} + A_{19} - A_{14} - A_{15} - A_{16} - A_{18} \\
 A_{21} &= \frac{A_{20}}{Pr^2 - Pr - \left(\frac{1}{K} + M\right)}, A_{22} = \frac{A_{14}}{4a_{12}^2 - 2a_{12} - \left(\frac{1}{K} + M\right)}, A_{23} = \frac{A_{15}}{4Pr^2 - 2Pr - \left(\frac{1}{K} + M\right)} \\
 A_{24} &= \frac{A_{16}}{4a_{11}^2 - 2a_{11} - \left(\frac{1}{K} + M\right)}, A_{25} = \frac{A_{17}}{(a_{12} + Pr)^2 - (a_{12} + Pr) - \left(\frac{1}{K} + M\right)} \\
 A_{26} &= \frac{A_{18}}{(a_{11} + Pr)^2 - (a_{11} + Pr) - \left(\frac{1}{K} + M\right)}, A_{27} = \frac{A_{19}}{(a_{12} + a_{11})^2 - (a_{12} + a_{11}) - \left(\frac{1}{K} + M\right)} \\
 A_{28} &= \frac{A_{27} + A_{25} - A_{26} - A_{24} - A_{23} - A_{22} - A_{21} - h \left(\begin{array}{l} prA_{21} + 2a_{12}A_{22} + 2PrA_{23} \\ + 2a_{11}A_{24} + \\ (a_{11} + Pr)A_{26} - (a_{12} + Pr)A_{25} \\ - (a_{12} + a_{11})A_{27} \end{array} \right)}{1 + ha_{12}}
 \end{aligned}$$

The non-dimensional shearing stress

$$\tau = \left(\frac{du}{dy}\right)_{y=0} = (-a_{12}A_{13} + PrA_{11} + a_{11}A_{12}) + E(-a_{12}A_{27} - PrA_{21} - 2a_{12}A_{22} - 2PrA_{23} - 2a_{11}A_{24} + a_{12} + PrA_{25} - a_{11} + PrA_{26} + a_{11} + a_{12}A_{27}) \tag{22}$$

The non-dimensional Rate of heat transfer

$$Nu = -\left(\frac{d\theta}{dy}\right)_{y=0} = (Pr + E(PrA_{20} + 2a_{12}A_{14} + 2PrA_{15} + 2a_{11}A_{16} - (a_{12} + Pr)A_{17} + (a_{11} + Pr)A_{18} - a_{11} + a_{12}A_{19})) \tag{23}$$

The non-dimensional rate of mass transfer

$$Sh = -\left(\frac{dc}{dy}\right)_{y=0} = a_{11}$$

4. Result and Discussion

In this paper we have studied the effects of Chemical Reaction on Free Convective Flow through a Porous Medium Bounded by Vertical Surface With Slip Flow Region. The effect of the parameters Gr, Gm, M, R, E, h, Pr, K and Sc on flow characteristics have been studied and shown by means of graphs. In order to have physical correlations, we choose suitable values of flow parameters. The graphs of velocity, temperature and mass concentration are taken w.r.t y. and the graphs of Nusselt number and Shearing stress are taken w.r.t h.

Velocity profiles: The velocity profiles are depicted in Figs 1-5. Figure-(1) shows the effect of the parameter E on velocity at any point of the fluid, when Gr=2, Gm=2, K=2, M=2, h=1, Pr=7, Sc=2 and R=2. It is noticed that the velocity increases with the increase of Eckert number (E).

Figure-(2) shows the effect of the parameters Gm and Gr on velocity at any point of the fluid, when K=2, M=2, h=1, Pr=7, Sc=2 and R=2. It is noticed that the velocity increases with the increase of both modified Grashoff number (Gm) and Grashoff number (Gr).

Figure-(3) shows the effect of the parameters K and M on velocity at any point of the fluid, when E=0.05, Gm=2, Pr=7, Sc=2, Gr=2 and h=1. It is noticed that the velocity

increases with the increase of permeability parameter porous medium (K) and decreases with the increase of Hartmann number (M).

Figure-(4) shows the effect of the parameters R and h on at any point of the fluid, when E=0.05, Gm=2, Gr=2, K=2, Pr=7, Sc=2 and M=2. It is noticed that the velocity increases with the increase of both Reaction parameter (R) and rarefaction parameter (h).

Figure-(5) shows the effect of the parameters Pr and Sc on at any point of the fluid, when E=0.05, Gm=2, Gr=2, K=2, h=1, R=2 and M=2. It is noticed that the velocity increases with the increase of Prandtl number (Pr) and fluctuate then decreases for the increase of Schmidt number (Sc). From all the figure of velocity the velocity reaches its maximum at a very short distance from the plate.

Temperature profile: The temperature profiles are depicted in Figs 6-9. Figure-(6) shows the effect of the parameters Gr and Gm on Temperature profile at any point of the fluid, when E=0.05, Pr=2, Sc=2, K=2, h=1, R=2 and M=2. It is noticed that the temperature rises in the increase of both modified Grashoff number (Gm) and Grashoff number (Gr).

Figure-(7) shows the effect of the parameters M, K and Pr on Temperature profile at any point of the fluid, when E=0.05, Gr=2, Sc=2, h=1, R=2 and Gm=2. It is noticed that the

temperature falls with the increase of both permeability parameter porous medium (K) and Prandtl number (Pr), where as it rises with the increase of Hartmann number (M).

Figure-(8) shows the effect of the parameter E on Temperature profile at any point of the fluid, when $E=0.05$, $Pr=2$, $Sc=2$, $K=2$, $h=1$, $R=2$ and $M=2$. It is noticed that the temperature rises in the increase of Eckert number (E).

Figure-(9) shows the effect of the parameters R and h on Temperature profile at any point of the fluid, when $E=0.05$, $Gr=2$, $Sc=2$, $K=2$, $M=2$, $Pr=2$ and $Gm=2$. It is noticed that the temperature falls with the increase both chemical reaction parameter (R) and rarefaction parameter (h).

Mass concentration profile: The mass concentration profiles are depicted in Fig -10 only. Figure-(10) shows the effect of the parameters R and Sc on mass concentration profile at any point of the fluid in the absence of other parameters. It is noticed that the mass concentration decreases with the increase of both reaction parameter (R) and Schmidt number (Sc). **Shearing stress:** The Shearing stresses of velocity are depicted in Figs 11-12. Figure-(11)

shows the effect of the parameters K,M,E and R on shearing, when $Sc=2$, $Pr=2$, $Gr=2$ and $Gm=2$. It is noticed that shearing stress at surface decreases with the increase of both Hartmann number (M) and Eckert number (E), where as increases with the increase of reaction parameter (R) and permeability parameter porous medium (K).

Figure -(12) - shows the effect of the parameters of Sc,Pr,Gr and Gm on Shearing stress when $K=2$, $M=2$, $R=2$ and $E=0.05$. It is noticed that the shearing stress of at the surface decreases with the increase of Grashoff number (Gr), where as increases with the increase of modified Grashoff number (Gm), Prandtl number (Pr) and Schmidt number (Sc).

Nusselt number: The Nusselt numbers of temperature are depicted in Figs 13-14. Figure -(13 -14) shows the effect of the parameters of heat transfer at surface, when .It is observed that the rate of heat transfer increases at surface with the increase of permeability parameter porous medium (K), reaction parameter (R), Prandtl number (Pr), whereas it decreases with the increase of Eckert number (Ec), Hartmann number (M), Grashoff number (Gr) and modified Grashoff number (Gm).

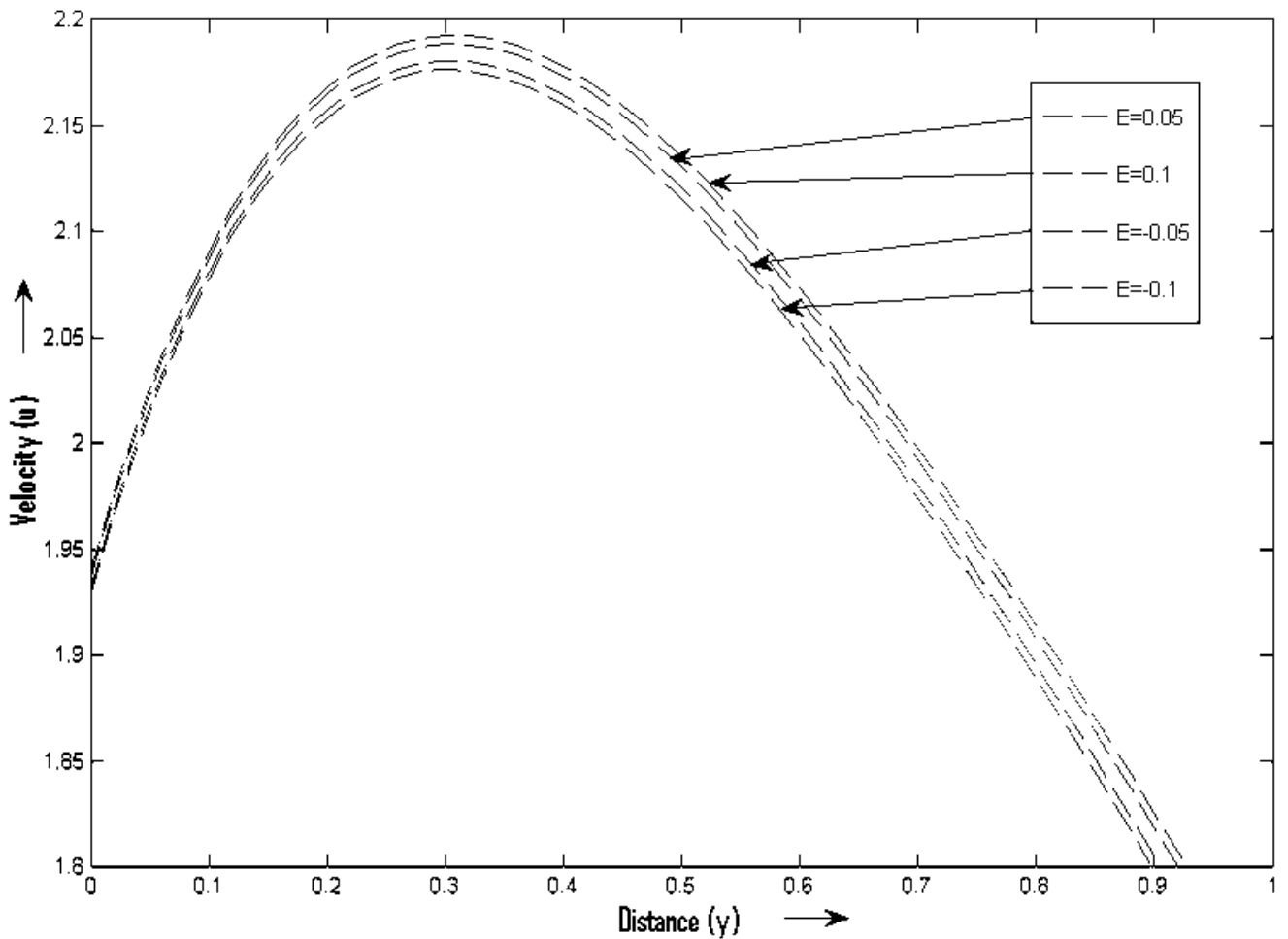


Figure 1. Effect of E on velocity profile when $Gr=2$, $Gm=2$, $K=2$, $M=2$, $h=1$, $Pr=7$, $Sc=2$ and $R=2$

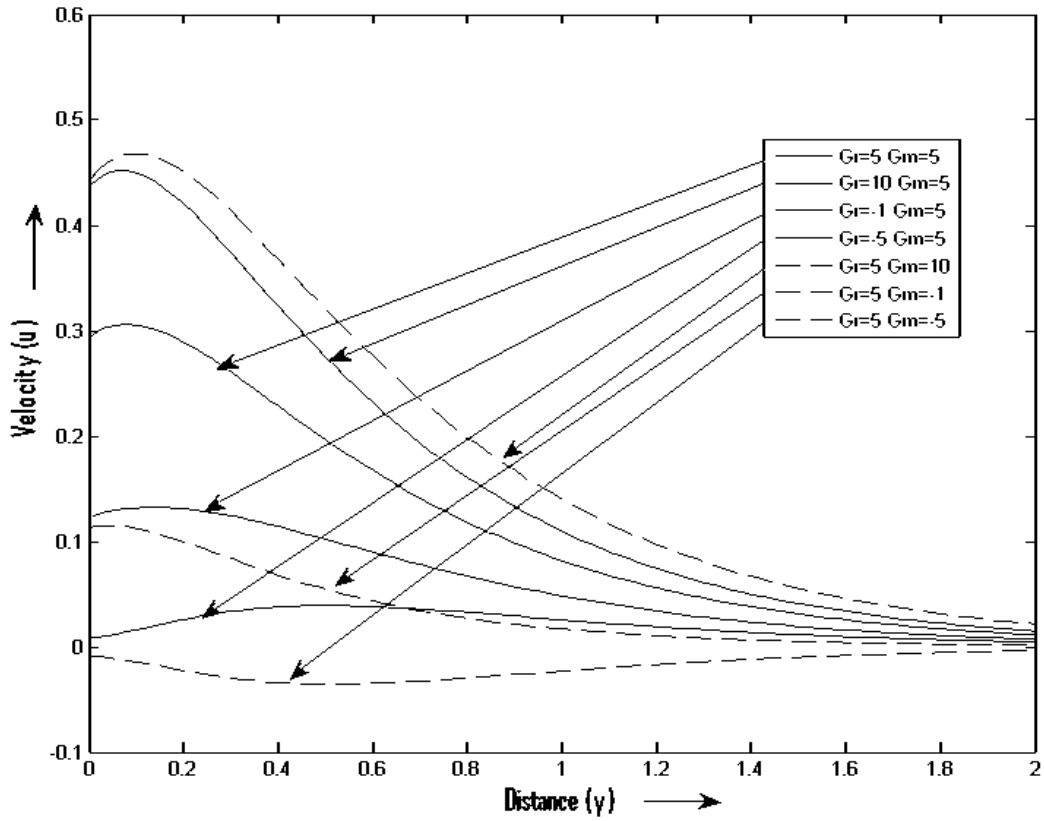


Figure 2. Effect of Gr and Gm on velocity profile when $E=0.05, K=2, M=2, h=1, Pr=7, Sc=2$ and $R=2$

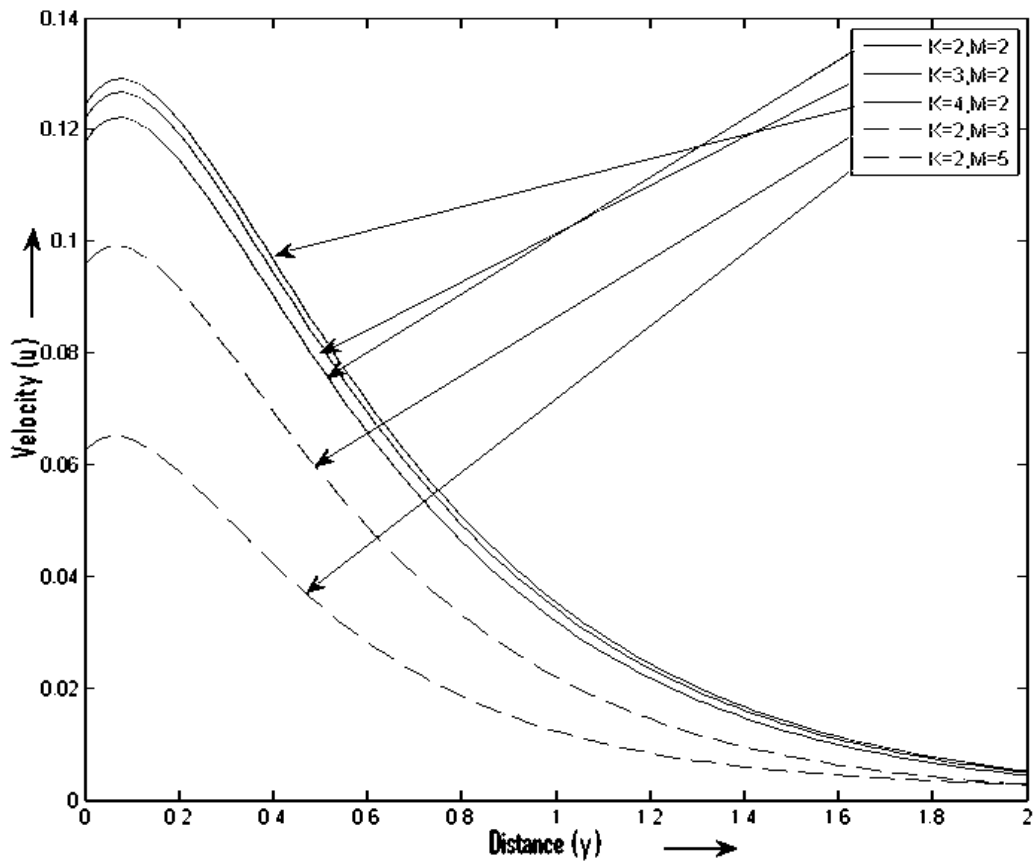


Figure 3. Effect of K and M on velocity profile when $E=0.05, Gm=2, Gr=2, h=1, Pr=7, Sc=2$ and $R=2$

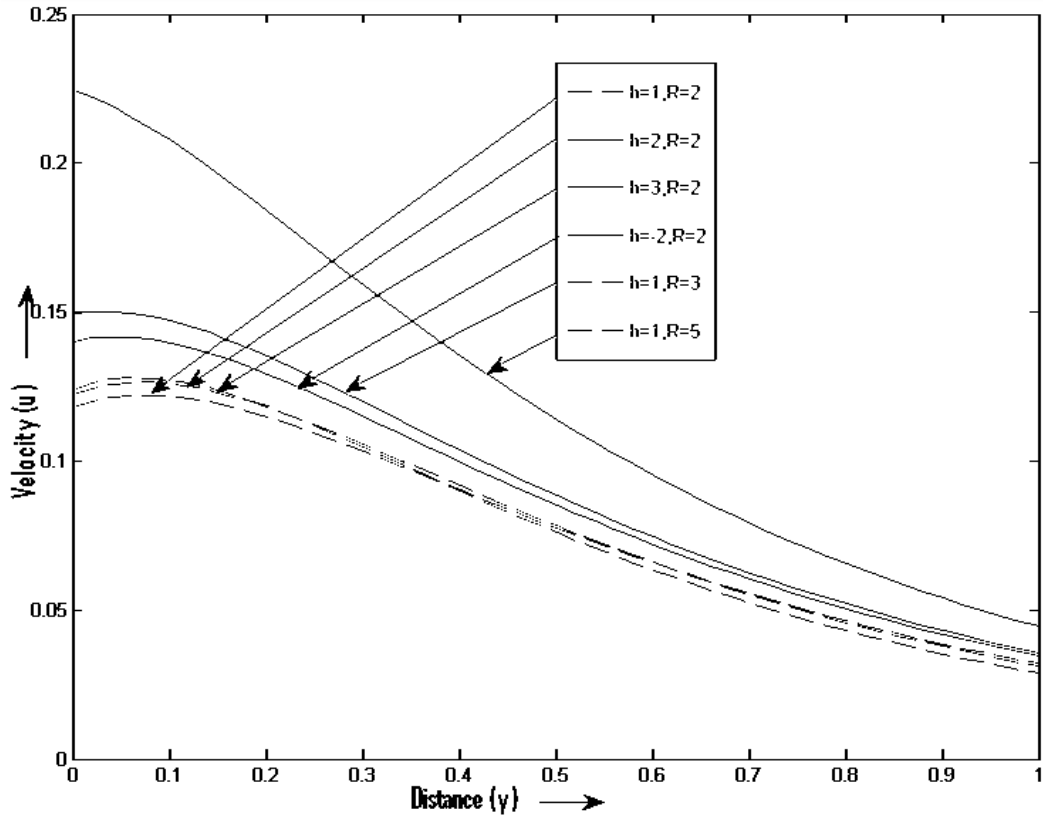


Figure 4. Effect of h and R on velocity profile when $E=0.05$, $Gm=2$, $Gr=2$, $K=2$, $Pr=7$, $Sc=2$ and $M=2$

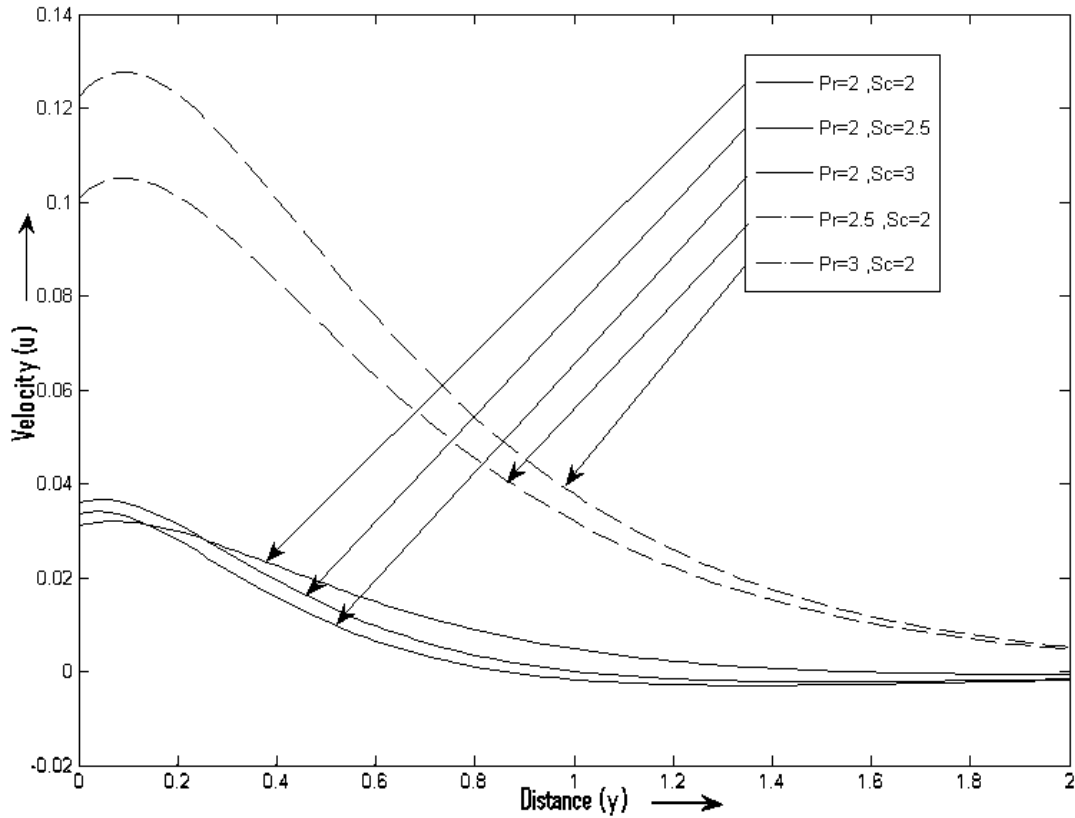


Figure 5. Effect of Pr and Sc on velocity profile when $E=0.05$, $Gm=2$, $Gr=2$, $K=2$, $h=1$, $R=2$ and $M=2$

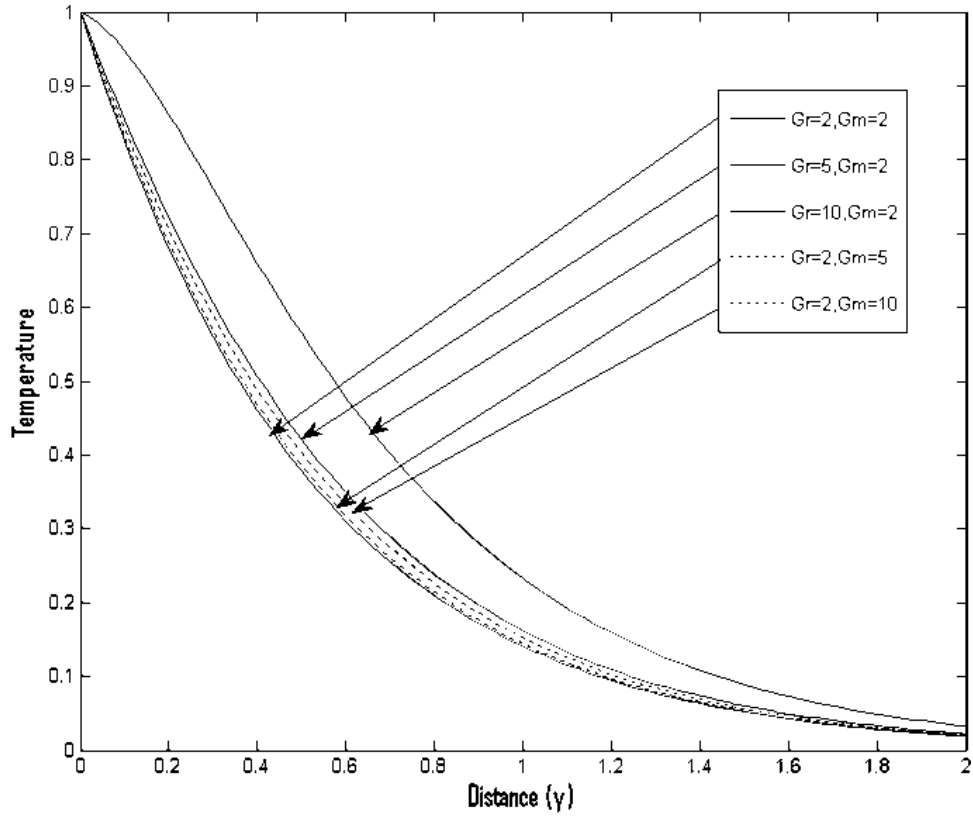


Figure 6. Effect of Gr and Gm on Temperature profile when $E=0.05$, $Pr=2$, $Sc=2$, $K=2$, $h=1$, $R=2$ and $M=2$

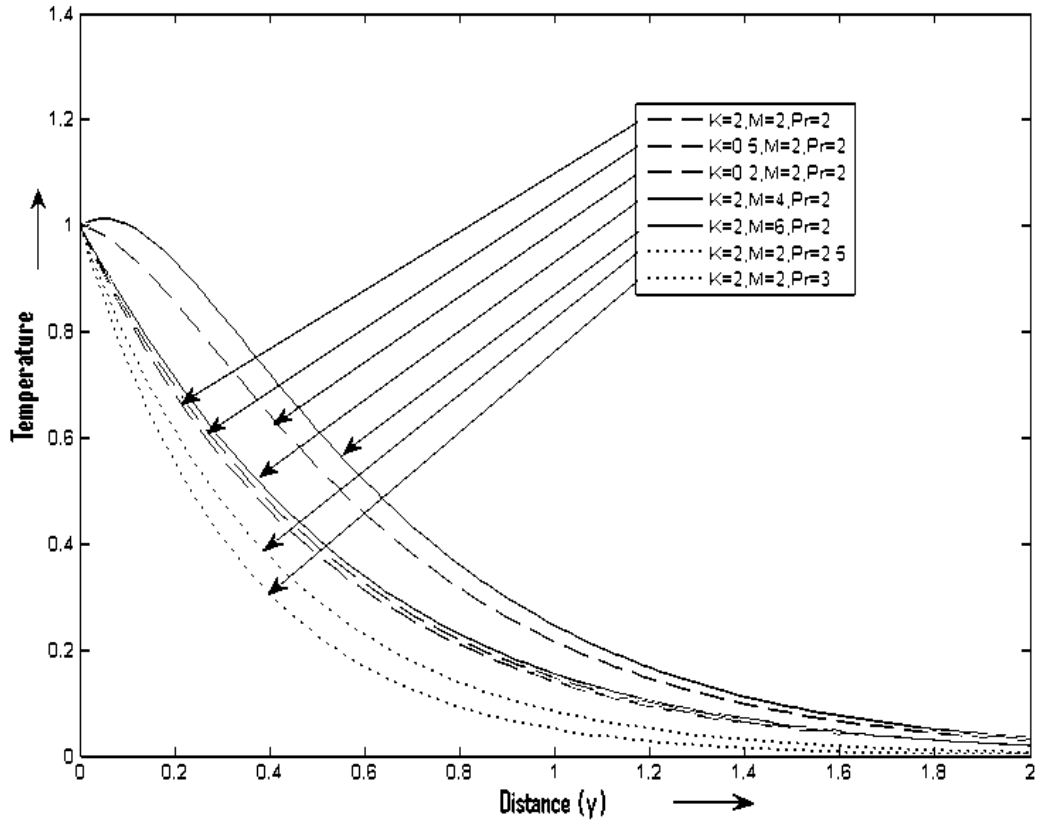


Figure 7. Effect of K, M and Pr on Temperature profile when $E=0.05$, $Gr=2$, $Sc=2$, $h=1$, $R=2$ and $Gm=2$

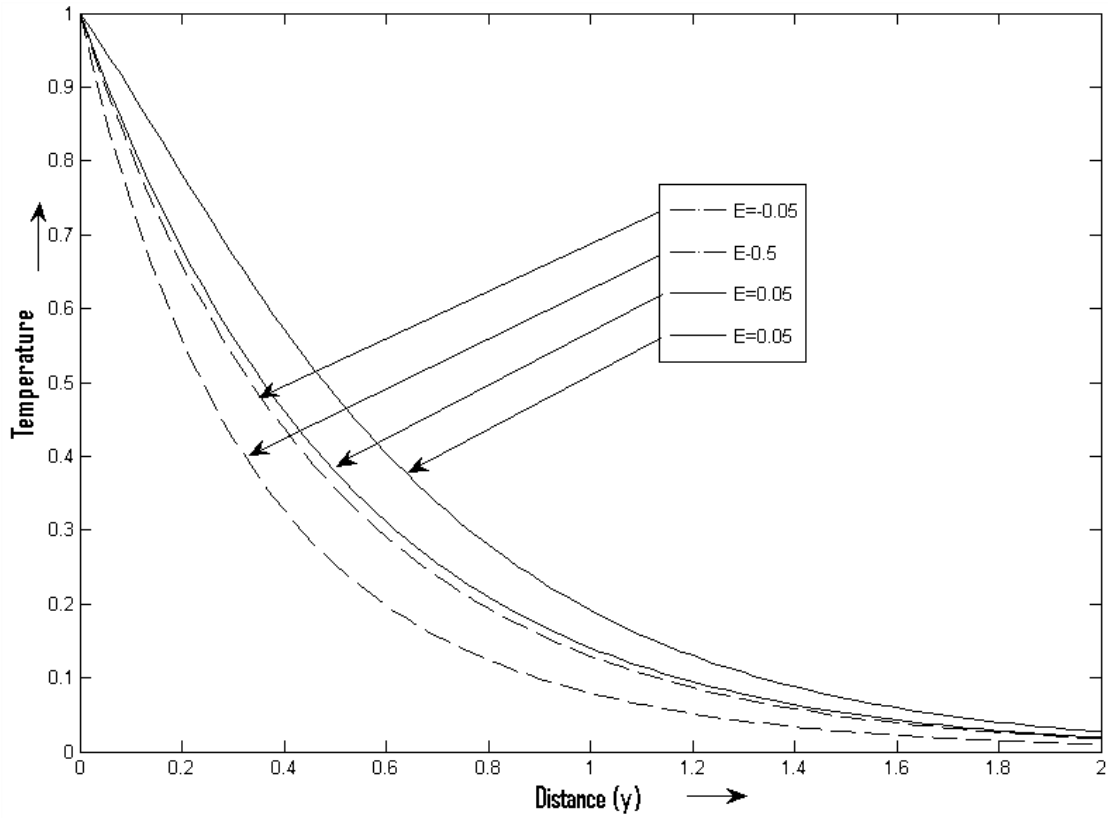


Figure 8. Effect of E on Temperature profile when $Pr=2$, $Gr=2$, $Sc=2$, $h=1$, $R=2$, $K=2$, $M=2$ and $Gm=2$

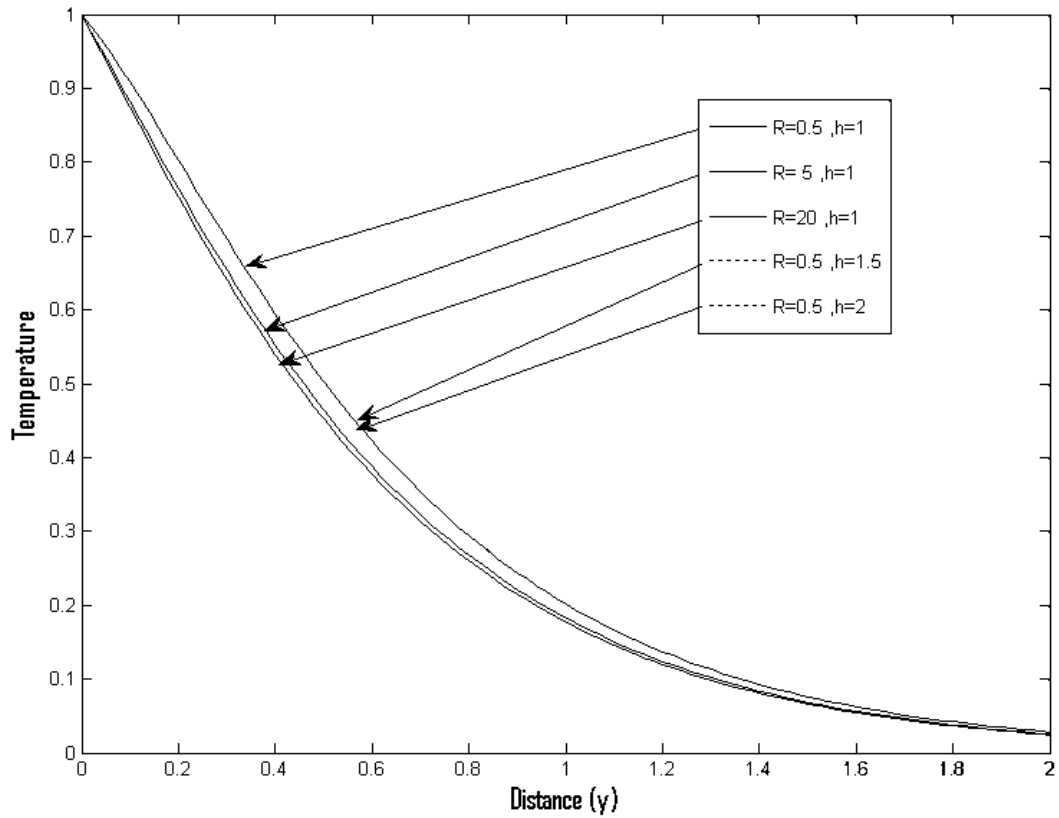


Figure 9. Effect of R and h on Temperature profile when $E=0.05$, $Gr=2$, $Sc=2$, $K=2$, $M=2$, $Pr=2$ and $Gm=2$

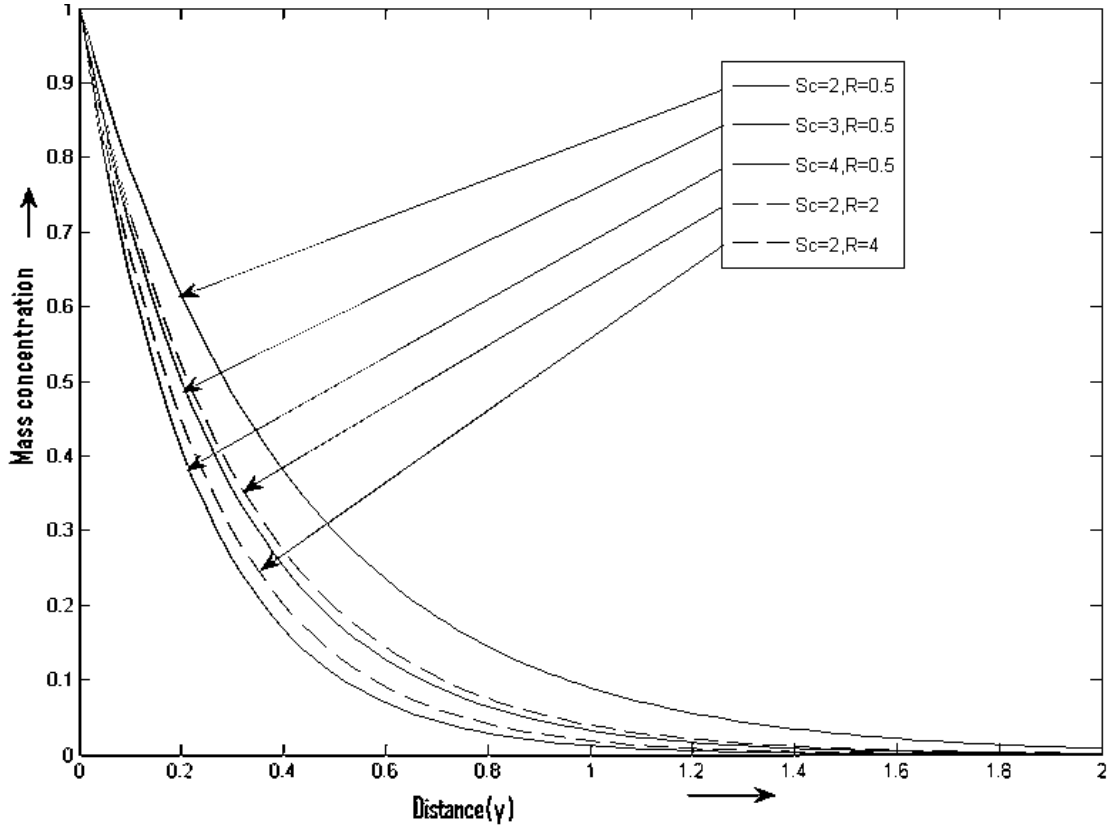


Figure 10. Effect of Sc and R on Mass concentration profile in the absence of other parameters

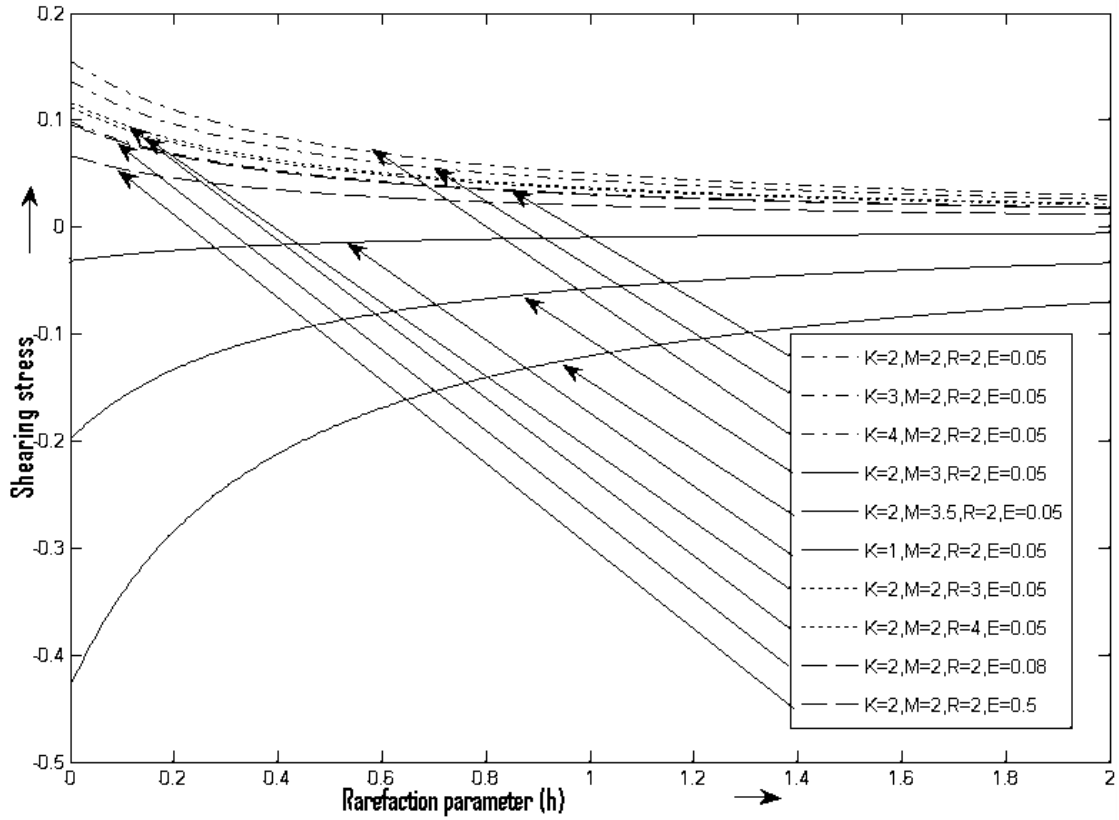


Figure 11. Effect of K,R,E and R on Shearing stress when $Sc=2, Pr=2, Gr=2$ and $Gm=2$

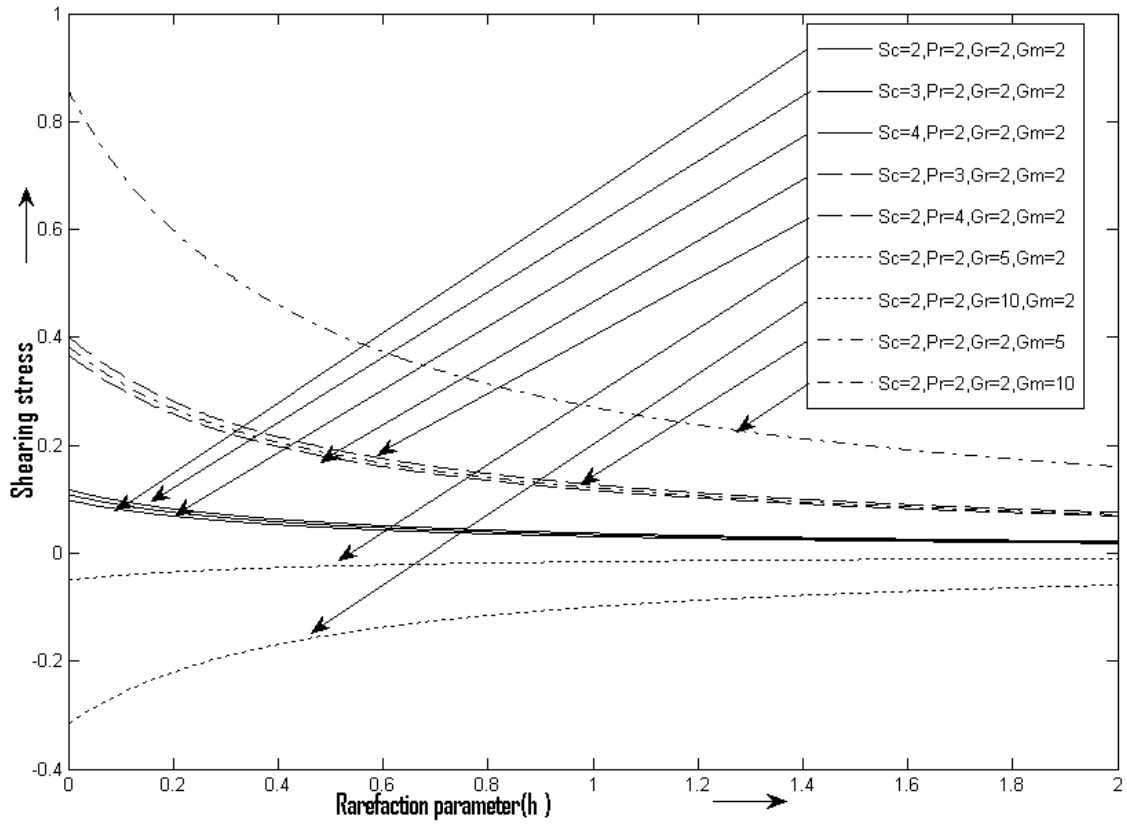


Figure 12. Effect of Sc, Pr, Gr and Gm on Shearing stress when $K=2, M=2, R=2$ and $E=0.05$

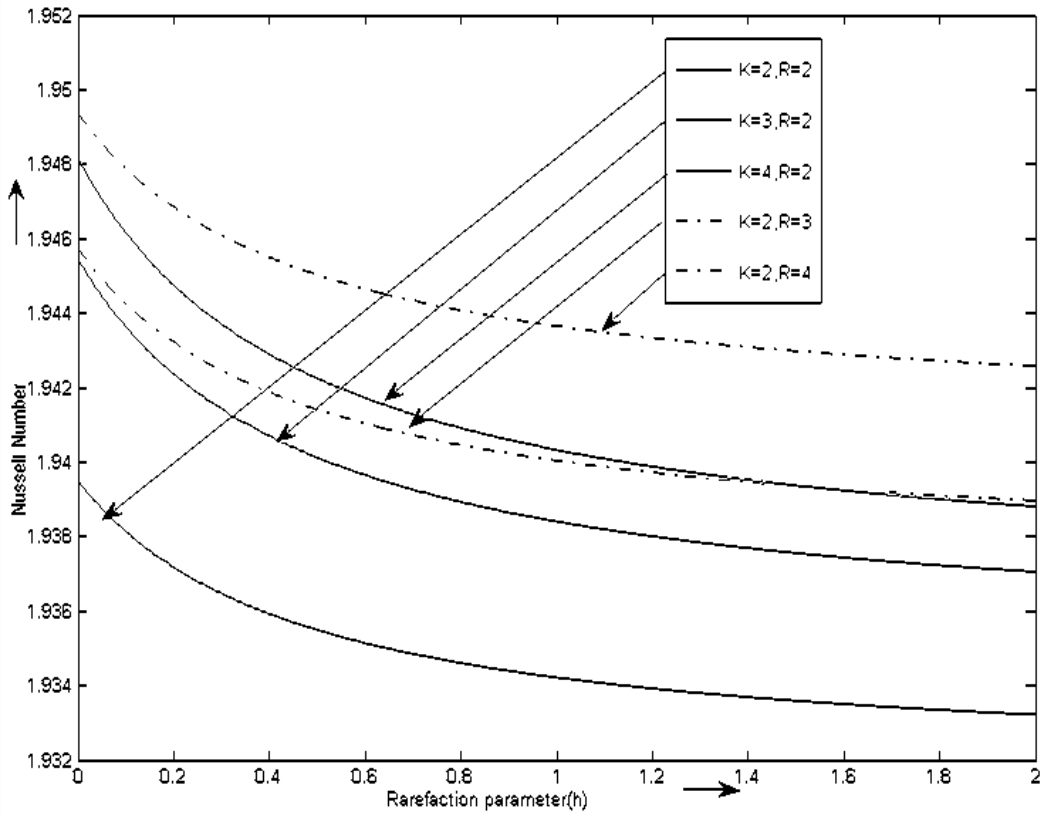


Figure 13. Effect of K and R on Nusselt Number when $Pr=2, Gr=2, Gm=2, M=2$ and $E=0.05$

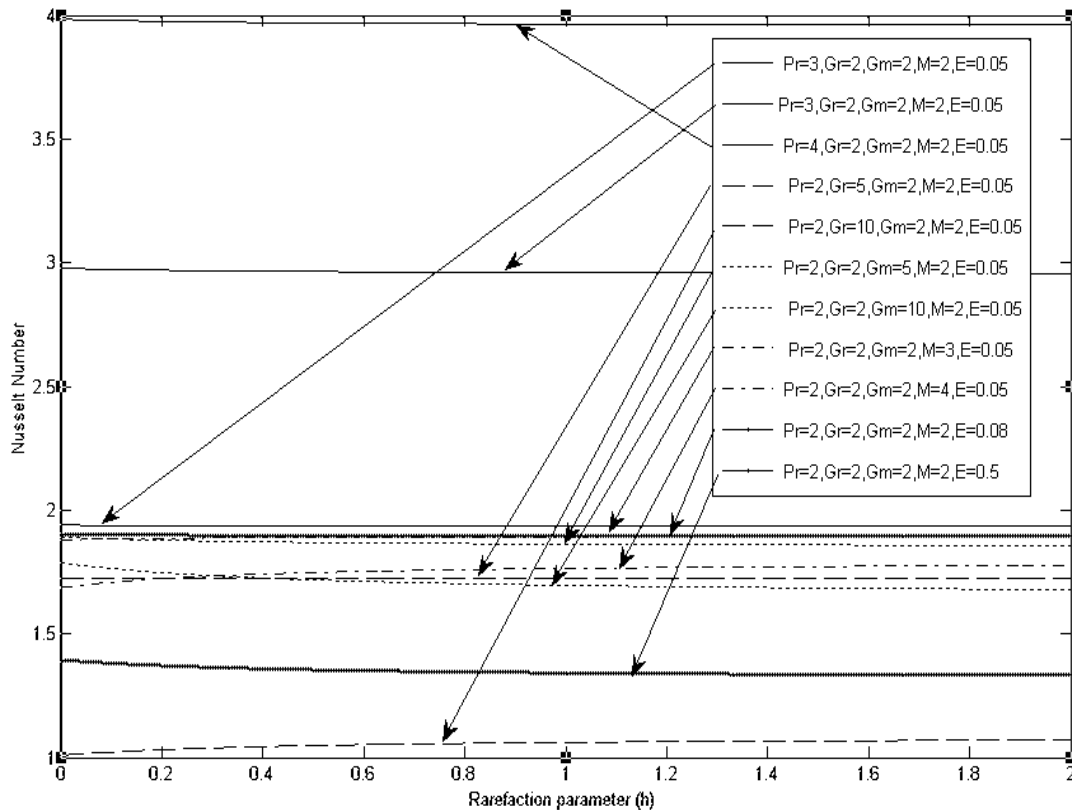


Figure 14. Effect of Pr,Gr,Gm,M,and E on Nusselt Number when $K=2, R=2$ and $Sc=2$

5. Conclusions

i The velocity increases with the increase in E , Gr , K , Pr , Gm , h and R , also decreases with the increase in M and Sc . The velocity near the surface is higher then gradually decreases to zero.

ii The temperature falls for the increasing of Pr , R , K and h and also rises for the increase Gr , Gm , M and E . The excess heat produces during the chemical reaction is diminished due to the presence of porous medium and slip flow region.

iii The mass profile decreases for the increasing of Sc and R .

iv The shearing stress at the surface reduce to zero for the increase of h . Also increases for the increase of K , R , Sc , Pr and Gm and decreases for other parameters.

v The rate of heat transfer at the surface during the process of chemical reaction increases in the presence porous medium with the increase of Prandtl number and decreases for other parameters.

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