

Efficient Bidirectional DFE for Doubly Selective Wireless Channels

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The bidirectional decision feedback equalizer (DFE) performs two equalizations, one on the received signal and one on its time-reversed version. In this paper, we apply the bidirectional DFE to wireless transmissions on rapidly time-varying dispersive channels and we propose an efficient implementation obtained by implementing the feedforward filter in the frequency domain. The feedback filter is adapted to the channel variations within one block and we propose a simplified design of the feedback filter coefficients based on a polynomial model of channel variations. Simulations performed on time-varying channels show that the proposed structure significantly outperforms existing architectures.

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1. INTRODUCTION

Recent developments in wireless communications have seen the extension to mobile applications of existing standards originally conceived for static receivers [1–4]. The push to provide access to wideband services on mobile terminals has posed a number of issues in the design of transmit and receive physical layers. In particular, the channel on which communication takes place is affected by both frequency selectivity and time selectivity, thus yielding a time-varying intersymbol interference (ISI) on the received signal.

In order to compensate for the distortion introduced by doubly selective channels, equalization is required. Among various equalization techniques, we mention the block linear equalizer (BLE) [5, 6] which has a high complexity, since it requires the inversion and multiplication of huge matrices. The time-invariant BLE has been considered in [5]. An extension to a time-varying finite impulse response (FIR) equalization has been considered in [6], where the doubly selective channel is described using a basis expansion model.

For time-invariant dispersive channels, it is well known that nonlinear equalization outperforms linear equalization, due to its ability of reducing ISI by means of interference cancellation through past detected symbols [7]. In particular, decision feedback equalization (DFE) is able to significantly lower the bit error rate below linear equalization. This comes in general at a relatively high cost in terms of computational complexity, which can be reduced by implementing the filters in the frequency domain (FD) with the use of efficient discrete Fourier transforms (DFTs) [8–10]. The

FD implementation requires a particular transmission format that forces the circularity of the convolution between the channel and the transmitted signal. On the other hand, DFE is prone to error propagation, since errors in symbol detection are propagated to next detections through the feedback part. This phenomenon can be partially alleviated with the use of a bidirectional DFE, where equalization is performed both on the received signal and on its time-reversed version [11, 12]. In [12], the bidirectional DFE was studied for the special case of a feedforward filter limited to be a pure gain. It was later extended to the general case of a finite impulse response feedforward filter and the research has focused on how decisions are taken from the signals coming from the two equalizers. The bidirectional arbitrated DFE performs a selection on the basis of a local maximum a posteriori (MAP) criterion [13] and achieves better performance than the linear combining of the equalized signals [14].

In this paper we propose a time-varying bidirectional DFE (TV-Bi-DFE) for the equalization of broadband signals distorted by time-varying channels. The TV-Bi-DFE comprises two blocks: (a) a direct time-varying FD DFE (TV-FD-DFE) that processes blocks of the received signal, (b) a time-reversed TV-FD-DFE that processes time-reversed blocks of the received signal. The double processing provides signals affected by partially uncorrelated errors. For an efficient implementation, the feedforward (FF) part of TV-FD-DFEs is implemented in the frequency domain by means of a static equalizer. On the other hand, the variations of the channel are compensated for by the feedback (FB) part of the DFEs, which is implemented with a time-varying filter. For

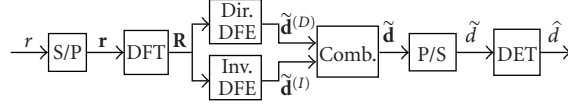


FIGURE 2: General scheme of the TV-Bi-DFE receiver. S/P and P/S blocks are serial-to-parallel and parallel-to-serial converters, respectively.

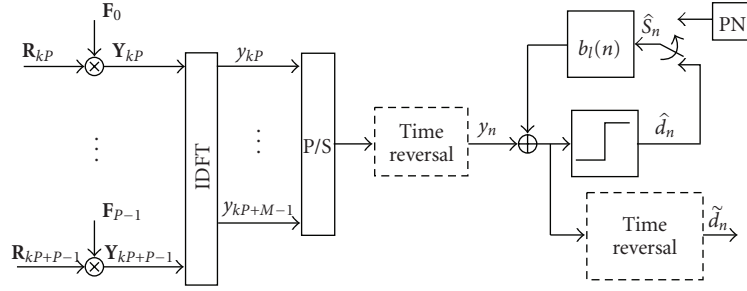


FIGURE 3: Scheme of TV-FD-DFE.

The scheme of TV-Bi-DFE is shown in Figure 2. First, the receiver transforms the received block into the FD to obtain the vector signal:

$$\mathbf{R} = [R_0, R_1, \dots, R_{P-1}], \quad (7)$$

where

$$R_k = \sum_{\ell=0}^{P-1} e^{-j2\pi(k\ell/P)} r_\ell. \quad (8)$$

Then, the vector signal \mathbf{R} is fed to the two TV-FD-DFEs (dir. DFE and inv. DFE, in Figure 2) that operate in parallel. A detailed description of TV-FD-DFE is provided in Section 3.1.

The output signal vectors $\tilde{\mathbf{d}}^{(D)}$ and $\tilde{\mathbf{d}}^{(I)}$, from the direct and inverse DFEs, are combined in the block comb. to provide the signal $\{\tilde{d}_n\}$. Note that the combining block may also perform an arbitrated ML sample selection. Lastly, a detector (DET) or decoder follows, and user data $\{\hat{d}_n\}$ are obtained.

3.1. Time-varying frequency-domain DFE

The purpose of the equalizer is to compensate for the time-varying ISI of the channel. This objective is achieved by a bidirectional nonlinear operation. The TV-FD-DFE comprises a feedforward (FF) filter implemented in the FD and a feedback (FB) filter implemented in the time domain. The implementation of the FF filter in the FD allows to reduce complexity, in terms of complex operations per received sample, with respect to the time-domain implementation. At the same time, the FB filter is still implemented in time domain in order to allow adaptation to channel variations. The overall scheme is similar to the DFE structure proposed in [8, 9] while here the FB filter is time varying in order to track the variations of the channel. Moreover, here the DFE is extended to operate on the time-reversed signal.

The scheme of TV-FD-DFE is shown in Figure 3. The blocks with dashed lines are used for the implementation of the time-reversed part of TV-Bi-DFE.

The input of the equalizer is the block of the received samples after DFT, \mathbf{R} . The first operation of the equalizer is the FF filtering, implemented in the FD as the elementwise multiplication of \mathbf{R} by the feedforward (FF) vector of coefficients. The FF filter is static and this allows the efficient implementation in the FD. The time variations of the channel are compensated for by the FB filter. For the direct and time-reversed TV-FD-DFEs, the FF coefficient vectors are denoted as $\mathbf{F}^{(D)}$ and $\mathbf{F}^{(I)}$, respectively. In the scheme of Figure 3, the coefficients are denoted by \mathbf{F} to accommodate both direct and time-reversed TV-FD-DFEs. The signal in the FD after FF filtering for the direct TV-FD-DFE is

$$Y_p^{(D)} = R_p^{(D)} F_p^{(D)}, \quad p = 0, 1, \dots, P-1, \quad (9)$$

while for the time-reversed TV-FD-DFE (9) holds with the index (D) substituted with (I) . The coefficients of the FF filter are computed for each block, in order to track the channel variations.

After FF equalization, the FB part of TV-FD-DFE is implemented in the time domain. First, the signal in the FD is converted into the time domain by means of an inverse DFT (IDFT), providing the vector signal

$$y_n^{(D)} = \sum_{p=0}^{P-1} e^{2\pi j(np/P)} Y_p^{(D)}, \quad n = 0, 1, \dots, P-1. \quad (10)$$

Feedback filtering follows, which we describe now for the direct and inverse TV-FD-DFEs.

FB for the direct TV-FD-DFE

For the direct TV-FD-DFE, the first FF equalized sample in the time domain is fed to a threshold detector, and the

decided symbols are used for the removal of residual interference before the detection of the next sample follows. The removal of ISI is performed by the FB filter which is time varying according to the channel variations. Details on the design of the FB filters are provided in Section 4. Let us indicate with $\{b_\ell^{(D)}(n)\}$ the impulse response of the FB filter of the direct TV-FD-DFE for the ℓ th output sample at time n . The FB filter will be designed to have a support $\ell = 1, 2, \dots, N_{\text{FB}}$, where $N_{\text{FB}} \leq L$.

Let us indicate with $\hat{d}_p^{(D)}$ the detected symbol at time p . The generic sample $p = 0, 1, \dots, P - 1$ at the input of the detector is obtained by subtracting from $y_n^{(D)}$ the interference generated by the previously detected symbols, that is,

$$\tilde{d}_n^{(D)} = y_n^{(D)} + \sum_{\ell=1}^{N_{\text{FB}}} b_\ell^{(D)}(n) \hat{d}_{n-\ell}^{(D)}, \quad n = 0, 1, \dots, M - 1. \quad (11)$$

Initially, the feedback filter is fed with the PN extension, that is, in (11) we set

$$\hat{d}_{-n}^{(D)} = p_{L-n}, \quad n = 1, 2, \dots, L. \quad (12)$$

FB for the time-reversed TV-FD-DFE

The time-reversed TV-FD-DFE processes the FF equalized block in reverse order, that is, detection starts from the last sample of the equalized block $\tilde{d}_{p-1}^{(I)}$ and the removal of the residual ISI is performed from the last symbol to the first. In other words, the equivalent channel model, obtained by the cascade of the discrete-time channel and the feedforward filter, is an anticausal filter. In this case, we indicate with $b_\ell^{(I)}(n)$, $\ell = 1, 2, \dots, N_{\text{FB}}$, the impulse response of the FB filter for the time-reversed TV-FD-DFE at time n . Then the signal at the input of the detector is

$$\tilde{d}_n^{(I)} = y_n^{(I)} + \sum_{\ell=1}^{N_{\text{FB}}} b_\ell^{(I)}(n) \hat{d}_{n+\ell}^{(I)}, \quad n = 0, 1, \dots, M - 1, \quad (13)$$

where we set

$$\hat{d}_{M+n}^{(I)} = p_n, \quad n = 0, 1, \dots, L - 1. \quad (14)$$

In order to perform the FB time-reversed filtering, the FF equalized block is time reversed (dashed block in Figure 3) and a conventional FB follows. The result of the FB equalization is again time reversed (indicated by the corresponding dashed block in Figure 3) to obtain the signal $\tilde{d}_\ell^{(I)}$.

Note that both the direct and the time-reversed TV-FD-DFEs rely on the presence of the PN extension. In fact, the ISI on the first (last) samples of the FF equalized blocks is due to the PN extension, which is known at the receiver and then can be effectively removed. Indeed, any other permutation of the block and consequent equalization could not remove ISI from the beginning of the permuted block, since the FB filter could not be properly initialized.

3.2. Signal combining and arbitration

The direct and time-reversed TV-FD-DFEs provide signals that are affected by errors also due to error propagation in

the FB parts. Since they process the received block in opposite directions, the errors are at least partially uncorrelated. There are two major methods to combine the signals of the two TV-FD-DFEs before decoding or detection: (a) maximal ratio combining (MRC), (b) symbol arbitration.

In MRC, the two signals are linearly combined with weights obtained by the signal-to-interference-plus-noise ratio (SINR) of each equalized signal. As will be seen in Section 4, by an MSE design of the filters, the average SINR is the same for both signals and MRC boils down to equal gain combining (EGC).

As described in [13], the arbitrated Bi-DFE performs the decision on a symbol-by-symbol basis, according to a local maximum a posteriori (MAP) criterion. In particular, the quality of the local match between the estimated and the received sequence is estimated in a window of W samples around the bit of interest (see [13] for details). The symbol which provides a closer match with the received sequence for a set of neighboring samples is selected in the arbitration.

4. FILTER DESIGN

The filter design of the Bi-FD-DFE takes into account two issues: (i) the transmission channel is time varying and the FB filters track its variations; (ii) filters must be designed for both the direct and time-reversed signals.

As a design criterion, we aim at the minimization of the mean square error (MSE) at the equalizer output:

$$J = E[|y_n - d_n|^2], \quad (15)$$

where y_n must be read as $y_n^{(D)}$ and $y_n^{(I)}$ for the direct and time-reversed TV-FD-DFEs, respectively.

Since the channel is time varying during one slot, each sample will be characterized by a different MSE. The MSE design criterion would require the minimization of a compound function of the MSEs, for example, their arithmetic average. However, this criterion would be exceedingly complex since the MSE should be evaluated for each sample. On the other hand, by considering that the FB filter compensates for time variations of the channel, we can assume that the MSE is almost constant for each symbol of a block.

Under this assumption and in order to obtain a simpler solution, we model the time-varying channel by expanding into a Taylor series each time-varying tap and truncating the expansion to the linear terms. Overall, for each block, the ℓ th channel tap is modeled as

$$h_\ell(n) = h_\ell(0) \left(1 - \frac{n}{P}\right) + h_\ell(P) \frac{n}{P}, \quad n = 0, 1, \dots, P - 1, \quad \ell = 0, 1, \dots, L - 1, \quad (16)$$

where $h_\ell(0)$ and $h_\ell(P)$ are the values of the ℓ th tap at the beginning of the current and the next blocks, respectively. We design the filters according to the linear model of the channel. For a practical implementation, $h_\ell(0)$ and $h_\ell(P)$ are provided by channel estimation techniques, for example, by

inserting a training sequence at the beginning of each transmitted block [8].

In particular, the FF filter is designed through the average channel on the block, that is,

$$\bar{h}_\ell = \frac{h_\ell(P) - h_\ell(0)}{2}, \quad \ell = 0, 1, \dots, L-1. \quad (17)$$

The design criterion aims at minimizing the MSE at the detector input, under the assumption that the channel is time invariant with an impulse response \bar{h}_ℓ . Let us define the P -size DFT of \bar{h}_ℓ as

$$\bar{H}_p = \sum_{\ell=0}^{L-1} e^{-j2\pi(\ell p/P)} \bar{h}_\ell, \quad p = 0, 1, \dots, P-1. \quad (18)$$

4.1. Feedforward filter design

We describe now the design of the FF filters of TV-FD-DFEs.

FF filter design of the direct TV-FD-DFE

For the direct DFE, the FF filter minimizes the MSE by taking into account that the FB filter removes up to N_{FB} taps of the residual ISI. For a time-invariant channel, in [9] it has been shown that an efficient technique for the computation of the FF filter coefficients is based first on the design of the FB filter for $\{\bar{h}_\ell\}$ through the solution of a linear system and then the derivation of the FF filter. Following the procedure described in [9], let us define the matrix \mathbf{A}_D and the column vector \mathbf{b}_D as

$$[\mathbf{A}_D]_{m,\ell} = \sum_{n=0}^{P-1} \frac{e^{-j2\pi(n(\ell-m)/P)}}{|\bar{H}_n|^2 + \sigma_w^2/\sigma_d^2}, \quad 1 \leq m, \ell \leq L, \quad (19)$$

$$[\mathbf{b}_D]_m = \sum_{n=0}^{P-1} \frac{e^{j2\pi(nm/P)}}{|\bar{H}_n|^2 + \sigma_w^2/\sigma_d^2}, \quad 1 \leq m \leq L, \quad (20)$$

where $\sigma_d^2 = E[|d_\ell|^2]$ and σ_w^2 is the noise power.

For the design of the FF filter, we first design the causal FB filter that equalizes \bar{h}_ℓ with coefficients $\bar{\mathbf{g}}_D = [\bar{g}_{D,1}, \bar{g}_{D,2}, \dots, \bar{g}_{D,L}]^T$. Note that this filter will not be used in TV-FD-DFE since it will be substituted by a time-varying filter. The FF filter that minimizes the MSE is obtained by first solving the following linear system [9]:

$$\mathbf{A}_D \bar{\mathbf{g}}_D = \mathbf{b}_D, \quad (21)$$

and then obtaining the FF filter as

$$F_p^{(D)} = \frac{\bar{H}_p^* \left(1 - \sum_{\ell=1}^{N_{\text{FB}}} \bar{g}_{D,\ell} e^{-j2\pi(\ell p/P)}\right)}{|\bar{H}_p|^2 + \sigma_w^2/\sigma_d^2}, \quad p = 0, 1, \dots, P-1. \quad (22)$$

Note that $\{\bar{g}_{D,\ell}\}$ is the FB filter that minimizes the MSE for a time-invariant channel having impulse response $\{\bar{h}_\ell\}$. For the direct TV-FD-DFE, the resulting MSE relative to the average channel is

$$J_D = \frac{\sigma_w^2}{P} \sum_{p=0}^{P-1} \frac{1}{|\bar{H}_p|^2 + \sigma_w^2/\sigma_d^2} \left| 1 - \sum_{\ell=1}^{N_{\text{FB}}} \bar{g}_{D,\ell} e^{-j2\pi(\ell p/P)} \right|^2. \quad (23)$$

FF filter design for the time-reversed TV-FD-DFE

The time-reversed TV-FD-DFE equalizes the transmission on the time-reversed channel with the following impulse response:

$$\bar{h}'_{-\ell} = \bar{h}_\ell, \quad \ell = 0, 1, \dots, L-1. \quad (24)$$

In the frequency domain, the DFT of $\bar{h}'_{-\ell}$ is

$$\bar{H}'_p = \bar{H}_{P-1-p}^*, \quad p = 0, 1, \dots, P-1, \quad (25)$$

where $*$ denotes the complex conjugate.

On the other hand, the FB filter is still causal and with L taps, since it is fed with time-reversed detected symbols. Hence, for the design of the FF filter, we can model the time-reversed TV-FD-DFE as a time-invariant FD-DFE that equalizes the channel $\{\bar{H}'_p\}$ by minimizing the MSE for the average channel \bar{h}'_ℓ . The solution is provided by solving the following linear system:

$$\mathbf{A}_I \bar{\mathbf{g}}_I = \mathbf{b}_I, \quad (26)$$

where, similarly to (19) and (20), we obtain

$$[\mathbf{A}_I]_{m,\ell} = \sum_{n=0}^{P-1} \frac{e^{-j2\pi(n(\ell-m)/P)}}{|\bar{H}'_n|^2 + \sigma_w^2/\sigma_d^2}, \quad 1 \leq m, \ell \leq L, \quad (27)$$

$$[\mathbf{b}_I]_m = \sum_{n=0}^{P-1} \frac{e^{j2\pi(nm/P)}}{|\bar{H}'_n|^2 + \sigma_w^2/\sigma_d^2}, \quad 1 \leq m \leq L. \quad (28)$$

Now, by observing that $e^{j2\pi(\ell n/P)} = e^{-j2\pi(\ell(P-n)/P)}$ and by comparing (19) with (27) and (20) with (28), we conclude that

$$\mathbf{A}_I = \mathbf{A}_D^*, \quad \mathbf{b}_I = \mathbf{b}_D^*, \quad (29)$$

and consequently

$$\bar{\mathbf{g}}_I = \bar{\mathbf{g}}_D^*. \quad (30)$$

This observation has two important consequences: (a) the design of the FF filters requires only the solution of one linear system, (b) from (23), the MSE of the direct and inverse DFEs is the same since

$$\begin{aligned} J_I &= \frac{\sigma_w^2}{P} \sum_{p=0}^{P-1} \frac{1}{|\bar{H}_{P-p}|^2 + \sigma_w^2/\sigma_d^2} \left| 1 - \sum_{\ell=1}^{N_{\text{FB}}} \bar{g}_{I,\ell} e^{-j2\pi(\ell p/P)} \right|^2 \\ &= \frac{\sigma_w^2}{P} \sum_{p=0}^{P-1} \frac{1}{|\bar{H}_{P-p}|^2 + \sigma_w^2/\sigma_d^2} \left| 1 - \sum_{\ell=1}^{N_{\text{FB}}} \bar{g}_{D,\ell}^* e^{-j2\pi(\ell p/P)} \right|^2 \\ &= \frac{\sigma_w^2}{P} \sum_{p=0}^{P-1} \frac{1}{|\bar{H}_{P-p}|^2 + \sigma_w^2/\sigma_d^2} \left| 1 - \sum_{\ell=1}^{N_{\text{FB}}} \bar{g}_{D,\ell} e^{-j2\pi(\ell(P-p)/P)} \right|^2 \\ &= J_D. \end{aligned} \quad (31)$$

Note that the equivalence of the MSE of the two DFEs also holds for time-domain implementation, as shown in [12],

even if both the architecture and the filter derivations are different. Since both direct and time-reversed DFEs yield the same useful signal gain, we conclude that both DFEs provide the same SINR at the detection point.

The resulting FF filter for the inverse DFE is

$$F_p^{(I)} = \frac{\bar{H}_{P-p}^* \left(1 - \sum_{\ell=1}^{N_{\text{FB}}} \bar{g}_{I,\ell} e^{-j2\pi(p\ell/P)}\right)}{|\bar{H}_{P-p}|^2 + \sigma_w^2/\sigma_d^2}, \quad p = 0, 1, \dots, P-1. \quad (32)$$

4.2. Adaptation of the feedback filter

The feedback filter tracks the variations of the channel and compensates for the residual ISI after the feedforward equalization. We now describe how that FB filter is adapted for the direct and time-reversed TV-FD-DFEs.

Direct TV-FD-DFE

For the direct TV-FD-DFE, the FB filter cancels the interference generated by the previous N_{FB} symbols, that is, compensates for the first N_{FB} taps of the overall impulse response of the cascade of the channel and the FF filter. In particular, by indicating the impulse response of the FF filter as

$$f_\ell^{(D)} = \sum_{p=0}^{P-1} F_p^{(D)} e^{j2\pi(p\ell/P)}, \quad \ell = 0, 1, \dots, P-1, \quad (33)$$

the overall impulse response of the cascade of the channel and FF filter seen by the direct DFE at time n is

$$h_\ell^{(D,\text{eq})}(n) = \sum_{m=0}^{P-1} f_m^{(D)} \hat{h}_{\ell-m}(n), \quad (34)$$

and the FB filter is

$$b_\ell^{(D)}(n) = -h_\ell^{(D,\text{eq})}(n), \quad \ell = 1, 2, \dots, N_{\text{FB}}. \quad (35)$$

For a general time-varying channel, (34) and (35) provide the equations for the update of the FB filter, independently of the channel model. In the following, we derive the particular expression of the FB filter update when the channel is modeled as linearly time varying. Note that for a higher order polynomial model the derivation of the FB coefficients would be straight forward, though with a consequent increase in complexity, due to the higher number of coefficients that must be taken into account.

Considering that the channel is modeled in (16) as linearly time varying, the FB filter can also be described as linearly time varying. In particular, by inserting (16) into (34) and (35), we obtain

$$b_\ell^{(D)}(n) = -h_\ell^{(D,\text{eq})}(0) \left(1 - \frac{n}{P}\right) - \frac{n}{P} h_\ell^{(D,\text{eq})}(P), \quad (36)$$

$$\ell = 1, 2, \dots, N_{\text{FB}},$$

where $h_\ell^{(D,\text{eq})}(0)$ and $h_\ell^{(D,\text{eq})}(P)$ are the equivalent filters computed from (34) with the channel at the first symbol of the current and next blocks, respectively.

Time-reversed TV-FD-DFE

For the time-reversed TV-FD-DFE, (33) and (34) hold with the indices (I) instead of (D), and the FB filter is

$$b_\ell^{(I)}(n) = -h_{-\ell}^{(I,\text{eq})}(0) \left(1 - \frac{n}{P}\right) - \frac{n}{P} h_{-\ell}^{(I,\text{eq})}(P), \quad (37)$$

$$\ell = 1, 2, \dots, N_{\text{FB}}.$$

Note that if $N_{\text{FB}} < L$, the time variations of the channel are only partially tracked by TV-FD-DFE, since taps $\{h_\ell^{(D,\text{eq})}(n)\}$ and $\{h_\ell^{(I,\text{eq})}(n)\}$ are not compensated for by the FB when $\ell > N_{\text{FB}}$. On the other hand, if the FB filter has $N_{\text{FB}} = L$ taps, then all taps of the equivalent channels are tracked.

4.3. Time-varying gain adaptation

The variations in the channel impulse response yield changes not only on the ISI but also on the gain of the useful signal, that is, $h_0^{(D,\text{eq})}(n)$ and $h_0^{(I,\text{eq})}(n)$. These variations change the amplitude and the phase of the signal at the input of the detector/decoder. In order to compensate for these variations, we multiply the equalized signal by the complex conjugate of the gain, and arbitration or MRC combining is performed on the signals

$$\tilde{d}_n^{(D)'} = h_0^{(D,\text{eq})*}(n) \tilde{d}_n^{(D)}, \quad (38)$$

$$\tilde{d}_n^{(I)'} = h_0^{(I,\text{eq})*}(n) \tilde{d}_n^{(I)}.$$

4.4. Time-invariant bidirectional DFE

For comparison purposes, we consider also a time-invariant bidirectional FD-DFE, implemented with the scheme of Figure 2. In this case the FF filters are designed as for TV-Bi-DFE, while the FB filters are not adapted to the channel variations but are kept static for the entire burst. In particular, the FB filters for the direct and time-reversed DFEs are provided by \bar{g}_D and \bar{g}_I in (26) and (30), respectively.

5. NUMERICAL RESULTS

In order to assess the performance of TV-Bi-DFEs, we have evaluated the averaged uncoded bit error rate (BER) for transmissions on time-varying dispersive channels. TV-Bi-DFE has been compared with the static FD-DFE, designed according to the MSE criterion outlined in [9] for the average channel \bar{h}_ℓ . Moreover, we also compared the performance of TV-Bi-DFE with the time-invariant bidirectional FD-DFE.

We have considered two channel scenarios. In the first scenario, the BER is averaged over randomly time-varying channels according to the Jakes model [16]. In the second case, the channel taps are linearly varying. In both cases, we assume that the channel is perfectly estimated at the beginning of each block, that is, $\{h_\ell(0)\}$ and $\{h_\ell(P)\}$ are available at the receiver.

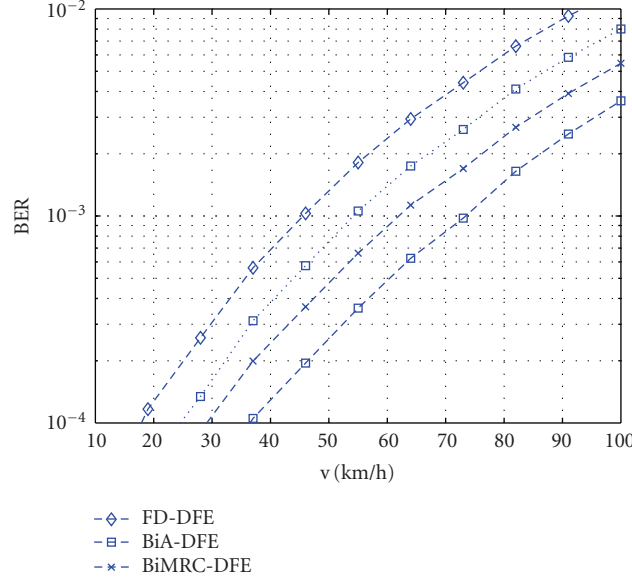


FIGURE 4: Average BER as a function of the speed. The performance of TV-Bi-DFEs is shown in dashed lines, while dotted lines show the performance of TI-Bi-DFEs.

Randomly time-varying dispersive channels

First, we assume that the channel taps have a Rayleigh statistic and a uniform random phase. The power profile is exponentially decreasing and the average root mean square delay spread is $2T$, where T is the duration of a transmitted symbol. The time-varying taps have a Jakes' spectrum which is related to the Doppler frequency:

$$f_D = \frac{v}{c} f_0, \quad (39)$$

where v is the terminal speed, c is the light speed, and f_0 is the carrier frequency. We consider a transmission operating at $f_0 = 20$ GHz, with a symbol rate $1/T = 2$ MHz.

Linearly time-varying channels

The second scenario that we consider is a time-varying channel that evolves linearly from the channel impulse response [13]

$$\mathbf{h}^{(\text{ref},1)} = [0.183 \ 0.916 \ 0.289 \ -0.183 \ 0.092 \ -0.046 \ 0.018] \quad (40)$$

to the impulse response of the channel C of [17]

$$\mathbf{h}^{(\text{ref},2)} = [0.227 \ 0.460 \ 0.688 \ 0.460 \ 0.227 \ 0 \ 0]. \quad (41)$$

The variation of the channel from $\mathbf{h}^{(\text{ref},1)}$ to $\mathbf{h}^{(\text{ref},2)}$ is made linearly on a per tap basis, that is,

$$h_\ell(n) = \left(1 - \frac{n}{N-1}\right) h_\ell^{(\text{ref},1)} + \frac{n}{N-1} h_\ell^{(\text{ref},2)}, \quad (42)$$

$$n = 0, 1, \dots, N-1,$$

where the number of symbols N determines the speed of variation between the two channels. Although being favorable to our TV-Bi-DFE with linear interpolation of the FB filter, this scenario provides an insight into the capabilities of the equalizers against channels with spectral nulls, which are usually hard to equalize.

We will indicate with BiMRC-DFE the TV-Bi-DFE using the MRC rule for the combination of the TV-FD-DFE signals, while TV-Bi-DFE using the arbitration technique is denoted as BiA-DFE.

For both TV-Bi-DFEs, we consider blocks of size $P = 128$, a PN extension of $L = 16$ symbols, and QPSK modulated data. For the feedback filter, we consider $N_{\text{FB}} = 16$ taps, and for the arbitration of BiA-DFE, we consider a window size $W = 5$.

Figure 4 shows the average BER as a function of the speed for an SNR of 30 dB. Dashed lines report the results for TV-Bi-DFEs, while the dotted line shows the performance of the time-invariant bidirectional DFE (TI-Bi-DFE) with arbitration. Indeed, the TI-Bi-DFE with MRC has not been shown since it has a performance very close to FD-DFE. We observe that TV-Bi-DFE provides an advantage of about 15 km/h over FD-DFE, and BiA-DFE further outperforms BiMRC-DFE by about 5 km/h. We also observe that by adapting the FB filter to the channel variations, TV-Bi-DFEs significantly outperform TI-Bi-DFEs. Lastly, from this figure we can also derive the impact of the block length P on the system performance. In fact, a higher P yields a larger time variation of the channel within each block.

Figures 5, 5, and 7 show the average BER for different equalizer structures operating on linearly time-varying channels as described by (42), for increasing values of N . We observe that for a low N , the channel changes more rapidly and FD-DFE is more affected by the variations of the channel

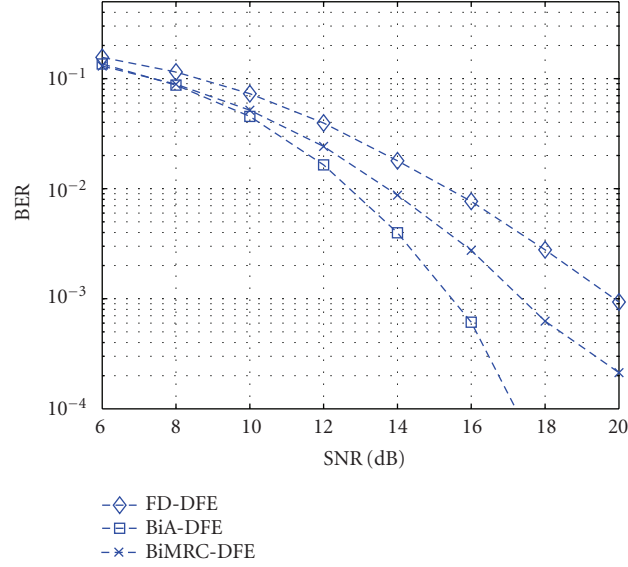


FIGURE 5: Average BER as a function of the average E_b/N_0 for different equalizer structures. Linearly time-varying channel according to (42), with $N = 3P$.

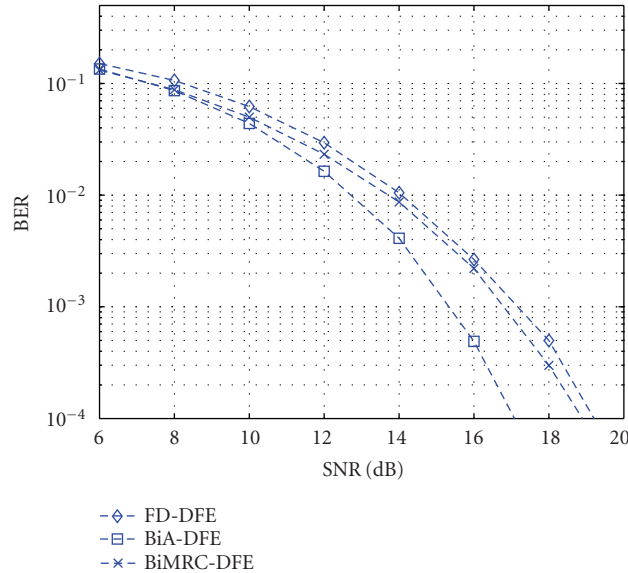


FIGURE 6: Average BER as a function of the average E_b/N_0 for different equalizer structures. Linearly time-varying channel according to (42), with $N = 30P$.

within each frame. Moreover, we note that BiA-DFE outperforms significantly BiMRC-DFE since it performs a MAP choice on the equalized signals provided by the DFEs.

5.1. Computational complexity

The computational complexity of the proposed schemes is compared with existing schemes in terms of number of complex multiplications (CMUL) required both for signal processing and for filter design. For the computation, we assume that a P -size DFT requires $(P/2) \log_2(P) - P$ CMULs.

The TV-Bi-DFE requires one DFT and two IDFTs, and CMULs for two FF filters. When BiMRC-DFE is considered, the combining does not require additional CMULs, while for BiA-DFE, two filters with L taps are applied to the equalized signals, requiring L CMULs per received sample each.

Table 1 shows the computational complexity of the various equalization architectures in terms of CMULs per received sample. We observe that the complexity of BiMRC-DFE is almost doubled with respect to FD-DFE. When the arbitration is included, the complexity further increases by about 30%. For comparison purposes, we considered the

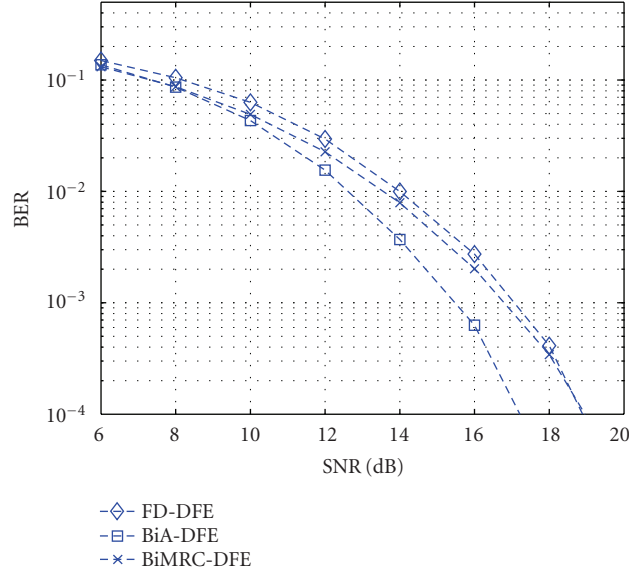


FIGURE 7: Average BER as a function of the average E_b/N_0 for different equalizer structures. Linearly time-varying channel according to (42), with $N = 300P$.

TABLE 1: Computational complexity of the system.

Structure	Computational complexity	
	CMULs/sample	Simulation scenario
FD-DFE	$\frac{P}{M} \log_2(P) + N_{FB}$	24
BiMRC-DFE	$\frac{3P}{2M} \log_2 P - \frac{P}{M} + 2N_{FB}$	43
BiA-DFE	$\frac{3P}{2M} \log_2 P - \frac{P}{M} + 2N_{FB} + 2L$	58
Block DFE [5]	$2P$	256
TV-FIR-DFE [18]	$(Q' + 1)(L' + 1) + (Q'' + 1)L''$	169

block DFE (B-DFE) of [5] and TV-FIR-DFE of [18]. The B-DFE requires a signal processing complexity of $2P$ CMULs/sample. For TV-FIR-DFE, we model the channel with $L = 16$ taps and with $Q = 2$ basis functions (corresponding to a speed up to 100 km/h) and we consider a feedforward (feedback) filter with $L' = 10$ ($L'' = 16$) taps and $Q' = 10$ ($Q'' = 2$) basis functions. The signal processing complexity of TV-FIR-DFE is $(Q' + 1)(L' + 1) + (Q'' + 1)L''$ CMULs/sample [18].

For the design of the filter coefficients, we observe that the most relevant operation is the solution of the linear system (21) which is shared by both the direct and the inverse TV-Bi-DFEs. Hence, the design of BiA-DFE does not yield an increase in complexity with respect to FD-DFE, providing in particular [9]

$$C_{\text{design}} = \mathcal{O}\left(L^2 + \frac{L}{2} \log_2 L + \frac{P}{2} \log_2 P\right). \quad (43)$$

The TV-FIR-DFE [18] has a complexity in design of $[(Q + Q' + 1)(L + L' + 1)]^3$, which is considerably higher than that of our proposed scheme.

6. CONCLUSIONS

In this paper we presented a novel bidirectional time-varying FD-DFE structure which is suitable for the equalization of rapidly time-varying channels. By exploiting the duality of time convolution and frequency-domain multiplication, the feedforward filtering is implemented in the frequency domain by means of efficient discrete Fourier transforms. At the same time, the feedback part of DFEs is implemented in the time domain and adaptively changed in order to track the channel variations. Moreover, two DFEs are applied on blocks of the received signal and their time-reversed versions, thus achieving a diversity gain. For the combination of the two equalized signals, we considered two alternatives and we evaluated the bit error rate of the proposed schemes for a time-varying transmission scenario. We conclude that the proposed structure is effective in equalizing time-varying channels with an efficient architecture.

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