Efficient Search Space Exploration for HW-SW Partitioning^{*}

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ABSTRACT

Hardware/software (HW-SW) partitioning is a key problem in the codesign of embedded systems, studied extensively in the past. One major open challenge for traditional partitioning approaches - as we move to more complex and heterogeneous SOCs - is the lack of efficient exploration of the large space of possible HW/SW configurations, coupled with the inability to efficiently scale up with larger problem sizes. In this paper, we make two contributions for HW-SW partitioning of applications represented as procedural callgraphs: 1) we prove that during partitioning, the execution time metric for moving a vertex needs to be updated only for the immediate neighbours of the vertex, rather than for all ancestors along paths to the root vertex; consequently, we observe faster run-times for move-based partitioning algorithms such as Simulated Annealing (SA), allowing call graphs with thousands of vertices to be processed in less than a second, and 2) we devise a new cost function for SA that allows frequent discovery of better partitioning solutions by searching spaces overlooked by traditional SA cost functions. We present experimental results on a very large design space, where several thousand configurations are explored in minutes as compared to several hours or days using a traditional SA formulation. Furthermore, our approach is frequently able to locate better design points with over 10 % improvement in application execution time compared to the solutions generated by a Kernighan-Lin partitioning algorithm starting with an all-SW partitioning. Categories and Subject Descriptors: B.6.3 [C.0]

General Terms: Algorithms

Keywords: HW-SW partitioning, dynamic cost function

1. INTRODUCTION

Partitioning is an important problem in all aspects of design. HW-SW (hardware-software) partitioning, i.e, the decision to partition an application onto hardware (HW) and software (SW) execution units, is possibly the most critical decision in HW-SW codesign. The effectiveness of a HW-SW design in terms of system execution time, area, power consumption, etc, are primarily influenced by partitioning decisions. In this paper, we consider the problem of minimizing execution time of an application for a system with hard area constraints. We consider an application specified as a call

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graph DAG (directed acyclic graph) extracted from a sequential application written in 'C' or any other procedural language, where the graph vertices represent functions, and the graph edges represent function calls or accesses between functions.

In this paper, we make two contributions to HW-SW partitioning. First we prove that for a callgraph representation, when a vertex is moved to a different partition, it is only necessary to update the *execution time change* metric [6] for its immediate parents and immediate children instead of all ancestors along the path to the root. This in general allows for a more efficient application of move-based algorithms like simulated annealing (SA).

Second, we present a cost function for simulated annealing to search regions of the solution space often not thoroughly explored by traditional cost functions. This enables us to frequently generate more efficient design points.

Our two contributions result in a very fast simulated annealing (SA) implementation that generates partitionings such that the application execution times are often better by over 10% compared to a KLFM (Kernighan-Lin/Fiduccia-Matheyes) algorithm for HW-SW partitioning for graphs ranging from 20 vertices to 1000 vertices. Equally importantly, graphs with a thousand vertices are processed in much less than a second.

2. RELATED WORK

HW-SW partitioning is an extensively studied "hard" problem with a plethora of approaches- dynamic programming [11], genetic algorithms [3], greedy heuristics [10], to name a few. Most of the initial work, [11], [12], focussed on the problem of meeting timing constraints with a secondary goal of minimizing the amount of hardware. Subsequently there has been a significant amount of work on optimizing performance under area constraints, [1], [2], [6]. With the goal of searching a larger design space, techniques such as simulated annealing (SA) have been applied to HW-SW partitioning using fairly simple cost functions. While a lot of initial work such as [12] was based exclusively on SA, recent approaches commonly measure their quality against a SA implementation. For example, [1] compares simulated annealing with a knowledge-based approach, and [2] compares SA with tabu search.

It is well-known that SA requires careful attention in formulating a cost function that allows the search to "hill-climb" over suboptimal solutions. However, much of the published work in HW-SW partitioning have not studied in detail the SA cost functions that permit a wider exploration of the search space. As an example, in [2], [7], the SA formulation considers only valid solutions satisfying constraints, thus restricting the ability of SA to "hill-climb" over invalid solutions to reach a valid better solution.

The two previous pieces of work in HW-SW partitioning that are most directly related to our work are [6], [4]. Our model for HW-SW partitioning is based on [6], a well-known adaptation of the

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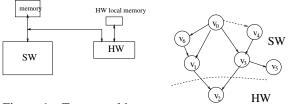


Figure 1: Target architecture

Figure 2: Simple callgraph

KL paradigm for HW-SW partitioning; our efforts in improving the quality of the cost function are closely related to [4].

Our partitioning granularity is similar to [6], effectively that of a loop-procedure call-graph; each partitioning object represents a function and the DAG edges are annotated with callcounts. [6] introduced the notion of execution time change metric for a DAG, and updating the metric potentially by evaluation of ancestors along the path to the root. The linear cost function in [6] ignores the effect of HW area as long as the area constraint is satisfied.

[4] provides an in-depth discussion of cost functions and the notion of improving the results obtained from a simple linear cost function by dynamically changing the weights of the variables. We differ from [4] in the following ways: [4] addresses the problem of choosing a suitable granularity for HW-SW partitioning that minimizes area while meeting timing constraints; since we consider the problem of minimizing execution time while satisfying HW area constraints, the proposed cost function in [4] needs significant adaptation for our problem. In [4], the dynamic weighting technique was applied towards the secondary objective of minimizing HW area once the primary objective, the timing constraint, was almost satisfied. We however, apply a dynamic weighting factor to our cost functions in various regions of the search space to better guide the search. Last but not the least, since their primary focus was on the granularity selection problem, there was no quantitative comparison of their approach with other algorithms- we have compared our approach to the KLFM approach with an extensive set of test cases and demonstrated the effectiveness of our approach.

3. PROBLEM DESCRIPTION

We consider the problem of HW-SW partitioning of an application specified as a callgraph extracted from a sequential program written in C, or, any other procedural language. For the purpose of illustrating the basic partitioning formulation, we assume a simple target architecture that contains one SW processor and one HW unit connected by a system bus, as shown in Figure 1. ¹ We assume mutually exclusive operation of the two units, i.e, the two units may not be computing concurrently. We also assume that the HW unit does not have dynamic RTR (run-time reconfiguration) capability.

The problem considered in this paper is to partition the application into HW and SW components such that the execution time of the application is minimized while simultaneously satisfying the hard area constraints of the HW unit. Essentially, given a software program, we want to map as many functions as possible to the fixed HW unit to improve program performance (thereby maximally utilizing available HW resources in a computing platform). **Preliminaries**

The input to the partitioning algorithm is a directed acyclic graph (DAG) representing a call-graph, CG = (V, E). *V* is the set of graph vertices and *E* the set of edges. Each partitioning object corresponding to a vertex $v_i \in V$ is essentially a function that can be mapped to HW or SW. Each edge $e_{ij} \in E$ represents a call or an

access to the callee function v_j from the caller function v_i . The SW execution times and callcounts are obtained from profiling the application on the SW processor. In this model, the HW execution time and the HW area for the functions are estimated from synthesis of the functions on the given HW unit. The simple model for HW area estimates assumes that the area of a cluster of components can be obtained by summing the individual HW areas. Communication time estimates are made by simply dividing the volume of data transferred by the bus speed. Since the execution time model is sequential, bus contention is assumed to play an insignificant role.

Each edge e_{ij} has 2 weights (cc_{ij}, ct_{ij}) . cc_{ij} represents the call count, i.e, the number of times function v_j is accessed by its parent v_i . ct_{ij} represents the HW-SW communication time, i.e, if v_i is mapped to SW and its child v_j is mapped to HW (or vice-versa), ct_{ij} represents the time taken to transfer data between the SW and the HW unit for each call. (Note: we assume that vertices mapped onto the same computing unit have negligible communication latency)

Each vertex v_i has 3 weights (t_i^s, t_i^h, h_i) . t_i^s is the execution time of the function corresponding to v_i on the SW unit (processor). t_i^h and h_i are the execution time, and, area requirement, respectively for the function on the HW unit. Note that in this work we do not consider compiler (synthesis) optimizations leading to multiple HW implementations with different area and timing characteristics.

A partitioning of the vertices can be represented as $P = \{v_0^s, v_1^h, v_2^s, \dots\}$. This denotes that in partitioning P, vertex v_0 is mapped to SW, v_1 is mapped to HW, v_2 is mapped to SW, etc. Two key attributes of a partitioning are (T^P, H^P) . T^P denotes the execution time of the application under the partitioning P, H^P denotes the aggregate area of all components mapped to hardware under partitioning P.

4. EFFICIENT COMPUTATION OF EXE-CUTION TIME CHANGE METRIC

Given a sequential execution paradigm and a call-graph specification, the execution time of a vertex v_i is computed as the sum of its self-execution time and the execution time of its children. The execution time for v_i additionally includes HW-SW communication time for each child of v_i mapped to a different partition. Thus, if T_i^P denotes the execution time for vertex v_i under a partitioning P,

$$T_i^P = t_i + \sum_{j=1}^{|C_i|} (cc_{ij} * T_j) + \sum_{j=1}^{|C_i^{diff}|} (cc_{ij} * ct_{ij})$$

where t_i is either t_i^h or t_i^s depending on whether v_i is currently mapped to HW or SW in the partitioning *P*. C_i represents the set of all children of vertex v_i , C_i^{diff} represents the set of all children of v_i mapped to a different partition. Note that if v_0 corresponds to main in a 'C' program, T_0^P equals the complete program execution time when partitioning *P* specifies whether vertices are mapped to HW or SW.

For a partitioning *P*, the *execution time change* metric Δ_i^P , for a vertex v_i , is defined as the change in execution time when the vertex v_i is moved to a different partition. That is, Δ_i^P denotes the change in T_0^P when vertex v_i is mapped to a different partition.

From the definition of the *execution time change* metric, it would appear that when a vertex is moved to a different partition, the metric values for all its ancestors would need to be updated. Indeed, in previous work, [6], the change equations assumed it was necessary to update ancestors all the way to the root. In the simple example shown in Figure 2, the execution time of the program (same as the execution time for vertex v_0) obviously depends on the execution time of its descendant v_2 . Let us assume all vertices were initially in SW. If we move the vertex v_2 to HW, the execution time changes due to HW-SW communication on the edges (v_3, v_2) , (v_1, v_2) and change in execution time for vertex v_2 . It would appear that any execution time related metric for the vertices v_0, v_6, v_4 , would need

¹Of course, our formulation can be extended to more contemporary SoC's containing multiple HW and SW components where we have a fixed area constraint and want to maximize performance

to be updated when this move is made. This, however, is not the case, as proved in the following lemma:

Lemma: For any two vertices v_x and v_y , if a vertex v_x is moved to a different partition, Δ_y needs to be updated only if there is an edge (x, y) or, (y, x). This update requires changing exactly one term in Δ_y , i.e this update can be done in O(1) time per edge.

PROOF. We define the *aggregate call count*, CC_i for a vertex v_i in the following recursive manner: $CC_i = \sum_{j=1}^{|P_i|} (cc_{ji} * CC_j)$. P_i represents the set of all parent vertices (all functions it is called from) for the vertex v_i . CC_0 , i.e the *aggregate call count* for the root vertex, is 1.

 CC_i represents the exact number of times the function corresponding to vertex v_i is called along all possible paths from the root. Now, if we recursively expand T_0^P , an unrolled representation for T_0^P is:

$$T_0^P = \sum_{i=0}^{|V|} (CC_i * t_i) + \sum_{i=0}^{|V|} \delta_{ij}^P * CC_i * ct_{ij}.$$

 δ_{ij}^{P} is the *Kronecker delta* function defined for edge (i, j) in the partitioning P - it takes a value of 1 if the vertex v_i and its child vertex v_j are mapped to different partitions, 0 otherwise. The first expression has exactly one term per vertex and the second expression has exactly one term per edge. If we now evaluate $T_0^{P_x}$, the new execution time when vertex v_x is moved to generate the new partitioning P_x ,

$$T_0^{P_x} = \sum_{i=0}^{(V-v_x)} (CC_i * t_i) + t_x^{P_x} * CC_x + \sum_{i=0}^{(i,j) \in (E-X)} (\delta_{ij}^P * CC_i * ct_i) + \sum_{i=0}^{(i,j) \in X} (\delta_{ij}^{P_x} * CC_i * ct_i)$$

where X is the set of all edges adjacent to vertex v_x , including its immediate parents and immediate children. The *Kronecker delta* values can change only for edges adjacent to v_x . We can now evaluate $\Delta_x^P = T_0^{P_x} - T_0^P$ corresponding to the change in execution time when vertex v_x is moved.

$$\Delta_x^P = CC_x * (t_x^{P_x} - t_x) + \sum_{i=1}^{n} \sum_{x \in X} ((\delta_{ij}^{P_x} - \delta_{ij}^{P_x}) * CC_i * ct_{ij})$$

We can similarly compute Δ_v^P for any other vertex v_y as

$$\Delta_y^P = CC_y * (t_y^{P_y} - t_y) + \sum_{i,j} \varepsilon^Y ((\delta_{ij}^{P_y} - \delta_{ij}^P) * CC_i * ct_{ij}) - \mathbf{Eqn} (\mathbf{A})$$

Next, we evaluate the execution time $T_0^{P_{xy}}$ corresponding to the new partitioning when vertex v_x is moved, followed by vertex v_y being moved.

$$T_{0}^{P_{xy}} = \sum_{i=0}^{(V-v_{x}-v_{y})} (CC_{i} * t_{i}) + t_{x}^{P_{x}} * CC_{x} + t_{y}^{P_{y}} * CC_{y} + \sum_{(i,j)\in(E-X-Y)} (\delta_{ij}^{P} * CC_{i} * ct_{ij}) + \sum_{(i,j)\in(X-[x,y])} (\delta_{ij}^{P_{x}} * CC_{i} * ct_{ij}) + \sum_{(i,j)\in(X-[x,y])} (\delta_{ij}^{P_{xy}} * CC_{i} * ct_{ij})$$

where [x, y] denotes either (x, y) or (y, x). Note that from our problem definition we can not have both (x, y), and, (y, x).

Thus, we can compute
$$\Delta_{y}^{P_x} = T_0^{P_{xy}} - T_0^{P_x}$$
 as
 $\Delta_{y}^{P_x} = CC_y * (t_y^{P_y} - t_y) - ((i,j) = [x,y]) (\delta_{ij}^{P_x} * CC_i * ct_{ij}) - \sum_{(i,j) \in (Y-[x,y])} (\delta_{ij}^{P_x} * CC_i * ct_{ij}) + \sum_{(i,j) \in Y} (\delta_{ij}^{P_{xy}} * CC_i * ct_{ij}) + \sum_{(i,j) \in (Y-[x,y])} ((\delta_{ij}^{P_{xy}} - t_y) + \sum_{(i,j) \in (Y-[x,y])} ((\delta_{ij}^{P_{xy}} - \delta_{ij}^{P_y}) * CC_i * ct_{ij}) + ((i,j) = [x,y]) ((\delta_{ij}^{P_{xy}} - \delta_{ij}^{P_x}) * CC_i * ct_{ij}) - Eqn (B)$

 δ_{ij} depends only on whether vertices v_i and v_j are in the same partition, or in different partitions. That is, $\delta_{ij}^{P_{iy}} = \delta_{ij}^{P}$ if $(i, j) \neq [x, y]$. So, comparing Equations (A) and (B), we have

$$\Delta_y^{P_x} - \Delta_y^{P} = ((i,j) = [x,y]) \left((\delta_{ij}^{P_{xy}} - \delta_{ij}^{P_x}) - (\delta_{ij}^{P_y} - \delta_{ij}^{P}) \right) * CC_i * ct_{ij}$$

Thus we have proved that when vertex us is moved to a different

Thus we have proved that when vertex v_x is moved to a different partition, Δ_y needs to be updated only if there is an edge [x, y]. Also, the update involves changing exactly one term in Δ_y .

Our experimental results will show that this result allows us to have very fast run-times for move-based algorithms like SA.

5. SIMULATED ANNEALING

Algorithm SAwhile (NOT_EQUILIBRIUM)For i = 1 to I_t // iterations at current temperatureP' = random perturbation of the current configuration, P $COST^{\Delta} = COST(P') - COST(P)$ if $(COST^{\Delta} < 0)$ P = P'else, generate random number x ε [0,1]if $(x < e^{-COST^{\Delta}/T})$ P = P'endforUPDATE T () (from annealing schedule) $EVALUATE_EQUILIBRIUM_CONDITION()$ endwhile

The above SA algorithm represents a typical formulation of simulated annealing for problems in combinatorial optimization, as initially proposed in [15]. The SA algorithm essentially tries to find an optimal solution to a "hard" problem such as partitioning, by conceptually representing the problem as a physical system with a huge number of particles at an initial temperature T. The system is randomly perturbed and the temperature is successively decremented allowing the system to reach statistical equilibrium at each temperature step: a state of minimal energy of the system corresponds to an optimal solution to the "hard" problem. Thus, key parameters in any formulation are the initial temperature T, the cooling (annealing) schedule mandating how the temperature is decremented, and the number of iterations at each temperature step.

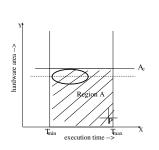
In HW-SW partitioning, perturbation is commonly defined as a move of a single vertex from HW to SW and vice versa, though experiments have been conducted with perturbations involving multiple moves [7]. A typical cost function is a linear combination of normalized metrics [1], [4], [2]. For our problem, the two metrics we need to consider are the execution time and the HW area.

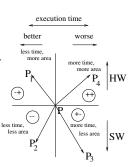
For a SA approach to HW-SW partitioning, execution time is primarily driven by the computation cost of the cost function. A cost of O(E) to compute the execution time of a partitioning by a traversal of the call-graph for every new configuration is too expensive for graphs with 100's to 1000's of vertices. For our problem, we can simply use the *execution time change* metric defined earlier to efficiently update the execution time for a new partitioning by updating only the immediate neighbours of a vertex. Since the average indegree and outdegree of a call graph is expected to be a low number, the average cost of a move is very low and enables the SA algorithm to do a very rapid evaluation of the search space. Notationally, for a partitioning P with attributes (T^P, H^P) , a HW to SW move of vertex v_i generates a new partitioning P_1 with attributes $(T^P + \Delta_i^P, H^P - h_i)$, and similarly for a SW to HW move.

5.1 Cost function for simulated annealing

Often, a statically weighted linear combination of metrics is used as a cost function for SA algorithms in an attempt to overcome its well-known limitations in handling multiobjective problems. In this section we first provide the intuition for developing cost functions that explore points often not considered in traditional cost functions, and then describe the cost function.

SA uses randomization to overcome local minima by accepting suboptimal moves with some probability: our goal is to guide the algorithm towards potentially more interesting design points by explicitly forcing the algorithm to accept apparently bad moves when far away from the objective. Simultaneously, we force the algorithm to probabilistically reject some apparently good moves that would always be accepted by most heuristics. As an example, when





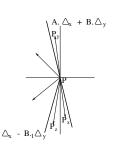


Figure 3: Solution space

Figure 4: Neighbourhood move

we are far away from our optimization goal, we would prefer not to always accept a move that improves execution time only slightly at the cost of a significant amount of hardware area.

Given our view of SA as a sequence of moves each of which is blindly accepted, or probabilistically rejected depending upon its degree of suboptimality, we define a cost function on the parameters that change for a given move, i.e, execution time, and HW area. The change in execution time for a move, Δ_T , is the same as execution time change metric for the moved vertex. The change in area, Δ_A , is positive, h_i for a SW-HW move, and negative, $-h_i$ for a HW-SW move of vertex v_i .

In Figure 3, each possible partitioning *P* is represented by a point in the two-dimensional plane with x and y co-ordinates. The x-axis represents the execution time corresponding to the given partitioning, while the y-axis represents the aggregate HW area. The vertical lines T_{min} and T_{max} represent the execution times for an all HW and an all SW solution respectively. The horizontal line A_c represents the area constraint. To solve our problem of minimizing execution time under a hard area constraint, we effectively need to search for a point as close as possible to the upper left corner of the bounded rectangular region A.

A move of a single component from SW to HW in partitioning P is expected to lead to a new partitioning with improved (less) execution time and more HW area, such as P_1 in Figure 4. Similarly, P_2 corresponds to a HW to SW move with less HW area. More generally, when a single component in partitioning P is moved between partitions, the new partitioning P_i lies in one of the four quadrants centred at P. A partitioning P_1 with improved execution time and additional HW area lies in the quadrant (-t, +h), represented in Figure 4 as (-,+). Similarly, a partitioning P_2 with improved execution time and reduced HW area lies in the quadrant (-t, -h), represented as (-, -), and so on for partitionings P_3 , P_4 .

We next consider the evaluation of a cost function $(A * \Delta_T + B *$ Δ_A) at the point P, corresponding to a random move generated by the SA algorithm. A and B are weights that include the normalization factors required to be able to combine the two cost function components which are in completely different units. This cost function is a simple straight line through P splitting the region around P into 2 equal parts. In traditional cost functions like [6], where the HW area component of the cost function is ignored as long as the area constraint is satisfied, essentially every random move that improves the execution time component of the cost function is accepted with a probability of 1. An example of such moves are P_1 , P_2 in Figure 4, i.e all moves lying in quadrants (-t, +h), (-t, -h),represented in the figure as (-+), (--).

If we now specifically consider a partitioning P in Figure 3 such that few components have been mapped to HW, and the execution time is hence expected to be closer to the SW execution time, our goal is to bias the move acceptance such that:

(a) we provide additional weightage to some moves like P_x in

Figure 5, that cause the execution time to deteriorate slightly but in

Figure 5: Cost functions

exchange free up a large amount of HW area. Such moves would be probabilistically rejected by traditional cost functions that ignore the HW area component, but we force their acceptance by explicitly introducing a cost function $(A * \Delta_T + B * \Delta_A), A >> B$ in the quadrant (+t, -h).

(b) we reduce weightage on some moves like P_v in Figure 5, that improve execution time slightly but consume an additional large amount of HW area. This is based on a similar reasoning of enabling the cost function to explore more combinatorial possibilities.

(c) we reduce weightage on some moves like P_7 in Figure 5 that improve the execution time slightly but free up a large amount of HW area. We are now actually attempting to guide the search away from making moves that do not appear to be headed towards our desired solution space. Intuitively, for a partitioning where there are relatively few HW components, the HW-SW communication cost can potentially play a dominant role. For moves like P_z , freeing up a large amount of HW could potentially result in a slight improvement in execution time due to significant reduction in HW-SW communication. Blindly accepting such moves translates to attempting to reduce communication cost between some vertex v_x mapped to HW and its neighbours in SW by moving back v_x to SW. When we are far from our desired solution space, we would instead prefer to encourage the algorithm to reduce communication cost by adding more of its neighbours to HW.

We next consider the notion of dynamically weighting the components of the cost function as suggested in [4]. This is a powerful technique which essentially changes the slope of the line through P, thus dynamically changing the search region. In [4], this technique was applied towards the secondary objective of minimizing HW area once the primary objective, the timing constraint was almost satisfied. We however, apply a dynamic weighting factor to our cost functions in various regions in an attempt to better guide the search. Conceptually we dynamically weight the time component with the distance from the boundary in our attempt to guide the search more towards the top left corner of the bounded region A in Figure 3.

Among other key issues considered in our cost function are the impact of boundary violations, i.e when a move leads us to a partitioning with HW area greater than the constraint. We penalize all such moves with a factor proportional to the extent of the boundary violation. We can clearly achieve this with a high weightage on the area component , i.e., a function $(A * \Delta_T + B * (Area_{new} - A_c))$, where B >>> A. Similarly when a move leads from an invalid partitioning to a valid partitioning, we reward it with a factor proportional to the extent that it is inside the boundary.

Another important aspect of our cost function is the notion of a threshold. When we are very close to the boundary, we need a cost function that has only a slight bias towards the component representing execution time. In our cost function, the time component is dynamically weighted by the distance from the boundarywe have observed experimentally that close to the boundary, desirable weights for the time component in this region are even lower than what our cost function provides. Thus, we needed to add the notion of a threshold region very close to the boundary where we explicitly assign a lower weightage to the time component of the cost function.

Based on the above discussion, our cost function is algorithmically described as follows:

if (current partititioning is a valid solution)

if (move causes boundary violation)

Significant penalty proportional to area violation (i) else if (current partitioning is very near to boundary)

Slightly reduced weightage on time (as compared to (iii)) else

if (move in quadrant –) $(A_1 * \Delta_T + B_1 * \Delta_A)$, where $A_1 >> B_1$ (iii) else $(A_2 * \Delta_T + B_2 * \Delta_A)$ (iv)

a mirror image of the above set of rules.

In Equations (iii) and (iv), the terms A_1 and A_2 are dynamically weighted by the distance from the boundary. The HW area component of the cost function is normalized with respect to the area-Constraint. A more detailed description of the actual values implementing rules (i), (iii), etc, are in [18].

5.2 Key parameters in SA

In order to obtain quality results, we tuned the algorithm SA by using the following parameter settings. For decrementing the temperature, we chose the popular geometric cooling schedule, where the new temperature is given by $T_{new} = \alpha * T$. α is a constant that typically varies between 0.9 - 0.99. After a lot of experiments, we fixed α at 0.96.

The stopping criterion is an important parameter, often formulated as the maximum number of moves that did not produce any improvement in the solution. In previous work, this has typically been a fixed number. We observed that this criterion has a strong correlation with problem size and hence, we scale the criterion from 5000 moves without improvement for graphs with 50 vertices, to 15000 moves without improvement for graphs with a 1000 vertices.

Our experiments indicated that there was only a weak correlation between the initial temperature and the problem size. So, we kept the initial temperature T fixed at 5000.

Another key parameter that we have often found missing in previous work on HW-SW partitioning is the inner loop in *Algorithm SA* where there are multiple iterations at each temperature. We have observed experimentally that the solution quality degrades when there is a single iteration at each temperature step as compared to the approach of applying multiple iterations at each temperature step.

6. EXPERIMENTS

As shown in Figure 6, we explored a very large space of possible designs by generating graphs which varied the following set of parameters: (1) varying indegree and outdegree (2) widely varying number of vertices (3) varying CCRs (computation-to-communication ratio). (4) varying area constraints.

We augmented the parameterizable graph generator TGFF [13] to generate the graphs used in our experiments. An example of an augmentation was one that enabled TGFF to generate HW execution times for vertices such that the HW execution time of a vertex was faster than the SW execution time by a number between 3 and 8 times.

Let $S = \{20, 50, 100, 200, 500, 1000\}$ denote the range of graph

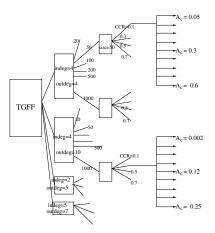


Figure 6: Set of experiments

sizes generated where size corresponds approximately to the number of vertices in the graph. As an example, for a graph size 50, TGFF generates a graph with between 48 to 52 vertices. We chose S to observe how our algorithm worked on a large range of graph sizes. Let $CR = \{0.1, 0.3, 0.5, 0.7\}$ denote the set of CCR's

(communication-to-computation ratio). The notion of CCR is very important in partitioning and scheduling algorithms that consider communication between tasks/functions. A CCR of 0.1 means that on an average, communication between tasks/functions in a call-graph/task graph requires 1/10'th the execution times of the functions/tasks in the graph. As CCR increases, communication starts playing a more important role in coarse-grain partitioning and scheduling algorithms.

We generated data for over 12000 individual runs of the SA with the following configurations from Figure 6.

Step 1 The maximum indegree and outdegree of a vertex were set to 4 each, which are reasonably representative of realistic callgraphs. Corresponding to these fixed parameters, we generated a set of graphs with the following characteristics. Each run of SA chose a graph size from $S = \{20, 50, 100, 200, 500, 1000\}$; for each graph size we chose CCR from CR = $\{0.1, 0.3, 0.5, 0.7\}$ Thus, we effectively generated a set of graphs $|S| \times |CR|$. Note that in the tables that follow, graphs with size 50 are denoted as v50, graphs with size 100 are denoted as v100, etc.

Step 2 For each of the graphs generated in Step 1, we varied the area constraint A_c as a percentage of the aggregate area needed to map all the vertices to HW. On one extreme, we set A_c such that very few partitioning objects would fit into HW, while at the other extreme, a significant proportion of the objects would fit into HW. **Step 3** We repeated the above two steps with a maximum indegree and outdegree of (i) 4 and 10 (ii) 2 and 5 (iii) 5 and 7.

Thus, the experimental data presented represents information collected from over 12000 experiments.

To measure the quality of results, we simply record the program execution times computed by the SA algorithm with our new cost function, and the KLFM algorithm as in [6]. In prior work, however, experiments to measure the quality of a partitioning algorithm have often been formulated by forcing constraint violations and attempting to integrate the degree of violations into some unitless number, as in [6], [1].

For a given design configuration, if T_{kl} is the execution time of the partitioned application computed by the KLFM algorithm, and T_{sa} is the execution time of the partitioned application computed by the SA algorithm, our quality measure is the performance difference given by: $(T_{kl} - T_{sa})/T_{kl} * 100$

Thus, a positive number, say, 5%, implies that the KLFM algorithm computed an execution time better than SA by 5%, while a nega-

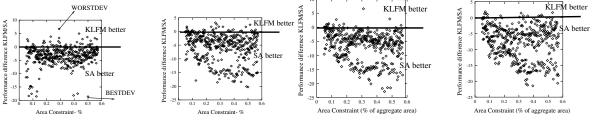


Figure	7:	v50,	CCR					
0.1:	Perf	ormanc	e Vs					
constra	constraint							

Graph	BESTDEV	WORSTDEV	AVG	SA	KFM
type	(%)	(%)	(%)	rt	rt
v20	-24.9%	12.3%	-4.17%	.07	.05
v50	-22.9%	6.7%	-5.75%	.08	.05
v100	-18.2%	5.7%	-5.47%	.1	.07
v200	-13.9%	4.3%	-3.74%	.19	.11
v500	-16%	6.8%	-4.53%	.25	.48
v1000	-13.7%	6.4%	-4.17%	.36	1.6

Table 1: Aggregate data for all graphs

tive number, say -10%, implies that the SA algorithm computed an execution time better than the KLFM algorithm by 10%.

While the results of all the experiments are too voluminous to present here (and are detailed in [18]), we present sample results for problem sizes v50 and also aggregate average over all experiments. Figure 7 represents the data collected for graphs with 50 vertices, and a fixed CCR of 0.1 for various area constraints. The *x*-axis corresponds to the various area constraints and the *y*-axis corresponds to the performance difference. In this figure, a significant majority of points show negative performance difference (below 0)- this indicates that our SA formulation mostly generates better results than the KLFM algorithm. The point BESTDEV represents the best performance improvement by our SA formulation over the KLFM algorithm, while point WORSTDEV represents the best solutions computed by the KLFM algorithm. Similarly, Figure 8, Figure 9, Figure 10 represent the data for graphs with 50 vertices and a CCR of 0.3, 0.5, 0.7 respectively.

Figs 7-10 represent the data for graphs with 50 vertices, which is only a fraction of the aggregate data. In Table 1, we provide a summary of the aggregate data. The column header *BESTDEV* represents the best improvement in execution time computed by the SA algorithm compared to the KLFM algorithm for the set of experiments represented by a row like v50. The column header *WORSTDEV* represents the best results produced by the KLFM algorithm. The column header *AVGDEV* represents the average deviation between the two algorithms. The column header *rt* represents the average run-time of each algorithm in seconds, measured on a SunOS 5.8 machine with a 502 Mhz Sparcv9 processor.

Table 1 thus clearly shows that our SA formulation often computes a better partitioning with over 10% improvement in execution time compared to a KLFM formulation and moreover, processes graphs with a thousand vertices in less than half a second, enabling rapid exploration of a very large design space.

7. CONCLUSION

In this paper, we made two contributions. We first proved that for HW-SW partitioning of an application represented as a callgraph, when a vertex is moved between partitions, it is necessary to update the execution time metric only for the immediate neighbours of the vertex. We additionally developed a new cost function for SA that attempts to explore regions of the search space often not considered in other cost functions. Our two contributions result

Figure 8: v50, CCR Figure 9: v50, CCR 0.3: Performance Vs 0.5: Performance Vs constraint constraint

Figure 10: v50, CCR 0.7: Performance Vs constraint

in a SA implementation that generates partitionings such that the execution times are often better by 10 % over a KLFM algorithm for graphs ranging from 20 vertices to 1000 vertices. Equally importantly, the algorithm execution times are very fast- graphs with 1000 vertices are processed in less than half a second. We believe that such a fast SA formulation makes it feasible to fine-tune the function further in a real design environment to generate partitioning solutions with a quality significantly better than that obtained from traditional KLFM implementations.

One important limitation of this work is a simple additive HW area estimation model that does not consider resource sharing- this could potentially be overcome in a future implementation with an approach like [8].

In the future, we plan to extend these concepts to systems where HW and SW execute concurrently, i.e, consider scheduling issues as part of the problem formulation. Also, based on our learning experience of individually tuning a lot of different parameters in SA, we would like to extend the cost function concepts developed here to algorithms with fewer tunable parameters.

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