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Electrical conductivity of microemulsions : a case of stirred percolation (*)

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Résumé. — La conductivité électrique G de microémulsions — eau dans l'huile — présente un comportement de percolation [1] : en-dessous d'une concentration d'eau critique ϕ_c , la conductivité semble diverger comme $(\phi_c - \phi)^{-S'}$, tandis qu'au-dessus de ϕ_c elle augmente comme $(\phi - \phi_c)^{T'}$. Dans cette situation physique que l'on peut qualifier de *percolation brassée* (par le mouvement Brownien du liquide) les exposants S' et T' n'ont *a priori* pas de raison d'être identiques aux exposants S et T de la situation classique de percolation gelée. Un modèle simplifié de percolation brassée rend compte de façon satisfaisante de l'exposant $S' = 1,2 \pm 0,1$, alors que la valeur admise pour S est 0,7. L'exposant T', dont la valeur mesurée varie de 1,4 à 1,6, est moins significatif pour la différence entre percolation gelée et brassée : Les valeurs prévues pour S' seraient environ 1,8 contre 1,6 pour S.

Abstract. — The electrical conductivity G of water in oil microemulsions may be described by percolation models [1]: below a critical water concentration ϕ_e , G seems to diverge as $(\phi_e - \phi)^{-S'}$, while for $\phi > \phi_e G$ increases as $(\phi - \phi_e)^{-T'}$. This physical situation may be called *stirred percolation*, referring to the Brownian motion of the medium. The exponents S' and T' are a priori different from the corresponding S and T in the classical situation of *frozen percolation*. A simple model of stirred percolation accounts fairly well for the measured value of $S' = 1.2 \pm 0.1$ while the accepted value for S is 0.7. The exponent T' (1.4 to 1.6 in our experimental case) is less significant of the difference between stirred and frozen percolation : the values for S' should be about 1.8 and the value accepted for S should be about 1.6.

1. Electrical conductivity of microemulsions. — We measured the electrical conductivity of microemulsions — water in oil — containing cyclohexan, sodium dodecyl sulphate (SDS) and 1 pentanol. The conductivity is extremely sensitive both to temperature and composition. The following procedure allowed a reproducibility of a few percent :

a) all the components, except a small quantity of alcohol, are introduced in the conductivity cell, the temperature of which is fixed at 20 °C \pm 0.1 °C,

b) the alcohol is added slowly while the conductivity is measured,

c) a maximum of conductivity is reached when the mixing clears up to make a microemulsion. This value is the conductivity of the microemulsion containing the minimum of alcohol which provides stability.

A suitable dilution procedure allows ϕ to be varied while the structure of droplets remains fixed [2]. We studied two different types of microemulsions characterized by a volumic ratio, soap to water, in the droplets :

type A
$$s/w = 0.69$$

type B $s/w = 0.345$

The conductivity increases steeply (five orders of magnitude) around a critical concentration ϕ_c . The variation above ϕ_c allows an independent determination of T and ϕ_c :

 $G^{1/T'} \sim (\phi - \phi_c)$ is linear in ϕ and tends to zero at $\phi = \phi_c$.

The plot of $G^{1/x}$ for different values of x has opposite concavities when T is greater or smaller than T'(Fig. 1). The results for the three types of microemulsions are presented in table I.

When the water concentration is very low $(\phi < 0.01)$ the conductivity is linear in ϕ , in agreement with a conduction mechanism involving the migration of charged droplets [1]. The percolation contribution to G is thus obtained by $G_p \sim G/\phi$. Figure 2 presents

^(*) La version française sera publiée dans le nº 20 des C.R.A.S., série B, du 28 mai 1979.



Fig. 1. — Determination of the exponent T' and of the critical water concentration ϕ_e , for $\phi > \phi_e : G^{1/x}$ is plotted for various x values as a function of ϕ .

Table I. — Exponents T' and S' measured for microemulsions of different soap/water ratios.

Microemulsion	Α	В
—		
Soap Water	0.69	0.345
T'	1.6 ± 0.1	1.55 ± 0.1
S'	1.28 ± 0.1	1.08 ± 0.1



Fig. 2. — The conductivity of a microemulsion for $\phi < \phi_c$ is plotted versus ($\phi_c - \phi$). Two different ratios soap/water are presented (see text).

Log (G/ϕ) versus Log $(\phi_c - \phi)$ for the three types of microemulsions. In each case, the slope is not much different of 1.2 (Table I).

2. A model for stirred percolation. — The electrical conductivity G of an insulating solid containing conductive particles is described by frozen percolation. G is very low if the concentration ϕ is lower than a critical value ϕ_c at which an infinite path through the conductive particles appears. Around and above this concentration, G increases steeply.

Essam *et al.* have suggested that G behaves in the vicinity of ϕ_c as [3]

$$\phi < \phi_{c} \qquad G = G_{0}(\phi_{c} - \phi)^{-S}$$

$$\phi > \phi_{c} \qquad G = G_{1}(\phi - \phi_{c})^{T}$$

where S and T are independent of the physical details. Computer simulations [4, 5, 6] and theoretical calculation [7, 8] give the following values for a 3 D system :

$$S = 0.5$$
 to 0.78
 $T = 1.5$ to 2.0.

Measured values of T on different physical systems are in the range 1.4 to 2, in agreement with the theory (A review of principal results is presented in reference [9]) while G. Deutscher and M. L. Rappaport measured S = 0.7, for the conductivity of Al-Ge films [10].

When the conductive particles are suspended in a fluid, the stirred percolation case, the conductivity may behave very differently. In the following model, conductive particles move with a diffusion coefficient D and they are assumed to interact through a *hard-sphere type* potential. A cluster which exists at time will disappear after the time $t + \tau_{\rm R}$ and reorder in different clusters. The time $\tau_{\rm R}$ is of the order of :

 $\tau_{\rm R} \sim a^2/D$ where a is the radius of particles, whatever the $(\phi - \phi_{\rm c})$.

To account for the kinetics of charge migration, we use a lattice with nodes connected by two types of conductances, a high one σ_+ (probability ϕ) and a low one σ_- (probability $1 - \phi$), each node being grounded through a capacitance C. The potential V_i at node *i* satisfies

$$C \frac{\partial V_i}{\partial t} = \sum_j \sigma_{ij}(t) \left(V_i - V_j \right)$$

which is formally identical to the diffusion equation of a species at concentration V_i with a jump frequency

$$W_{ij} = \frac{\sigma_{ij}}{C} = \frac{1}{\theta_{ij}}$$

The conductivity G is thus formally identical to the diffusion coefficient \overline{D}_{v} of this species.

We define two times θ_+ and θ_- , corresponding to σ_+ and σ_- :

* θ_+ is the (short) migration time of charges in a conducting cluster :

$$\theta_+ = \frac{C}{\sigma_+} f(\phi)$$

* θ_{-} is the (long) migration time of charges between large clusters in the frozen case :

$$\theta_{-} = \frac{C}{\sigma_{-}} g(\phi)$$

To calculate g, we use the variation of G in the frozen case :

and

$$G \sim (\phi_{\rm c} - \phi)^{-S}$$

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$$G \sim \overline{D}_{\mathbf{v}} \sim \left(\frac{\overline{R_{G}^{2}}}{\theta_{-}}\right) \qquad (\text{if } \theta_{+} \ll \theta_{-})$$

where R_{G} , the gyration radius of the clusters, increases as [8, 11]

$$\overline{R_G^2} \sim (\phi_c - \phi)^{\beta - 2\nu}$$

with β and v having the common definition. The variation of θ_{-} is thus :

$$\theta_{-} \sim (\phi_{\rm c} - \phi)^{S + \beta - 2\nu}$$
.

The time θ_{-} thus diverges when $\phi \rightarrow \phi_{c}$, with an exponent

$$2\nu-S-\beta\sim0.6$$

3. Different situations. — Depending on the values of θ_+ , θ_- and $\tau_{\mathbf{R}}$, three cases appear :

a) $\theta_+ \ll \theta_- \ll \tau_{\mathbf{R}}$ is the frozen case :

$$G \sim \frac{\overline{R_G^2}}{\overline{\theta}_-} \sim (\phi_c - \phi)^{-s}$$
.

b) $\tau_{\mathbf{P}} \ll \theta_{+} \ll \theta_{-}$

is the completely stirred case. G is the mean between $G_{+}(\phi = 1)$ and $G_{-}(\phi = 0)$:

$$G = \phi G_{+} + (1 - \phi) G_{-}$$

and it increases linearly with ϕ .

c) $\theta_+ \ll \tau_{\mathbf{R}} \ll \theta_-$

is the mixed case, always existing near ϕ_c , because $\theta_$ diverges when $\phi \rightarrow \phi_c$. The migration of charges between large clusters does not depend anymore on θ_{-} but only on $\tau_{\mathbf{R}}$. One may then assume that

$$G \sim \frac{\overline{R_G^2}}{\tau_{\rm R}} \sim (\phi_{\rm c} - \phi)^{\beta - 2\nu}$$

and in three dimensions the exponent will be :

$$S'=2\nu-\beta\sim 1.2$$

This value is also the value of S for a space dimension $d \ge 4$ [11].

For $\phi > \phi_c$, the exponent T' measured for microemulsions are not very different from the accepted value for $T \sim 1.6$.

A theoretical guess of T' could be obtained in assuming the same scaling law that for S': one could extrapolate at d = 3 the law obtained by A. S. Skal and B. I. Shklovskii [12]

$$T = 1 + v(d - 2)$$

which should give T' = 1.84 in three dimensions. An experimental check would thus be difficult in view of the small difference between T and T'.

4. Conclusion. — We suggest here a simplified description of the intricate behaviour of stirred percolation. Three different cases appear depending on the reordering time $\tau_{\mathbf{R}}$ of the clusters. If $\tau_{\mathbf{R}}$ is very large, the results of frozen percolation apply. If τ_{R} is much shorter than the typical times θ_+ and θ_- of charge migration in and between the clusters, the conductivity is the mean between the conductivities of both phases. When $\tau_{\mathbf{R}}$ has an intermediate value between θ_{+} and θ_{-} , we assume that only the size of clusters accounts for the divergence of G for $\phi < \phi_{\rm s}$.

This assumption agrees fairly with the measured conductivity of microemulsions for $\phi < \phi_{c}$.

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