

Electronic correlations in Hund metals

E. Bascones

Instituto de Ciencia de Materiales de Madrid



In collaboration with:

Laura Fanfarillo

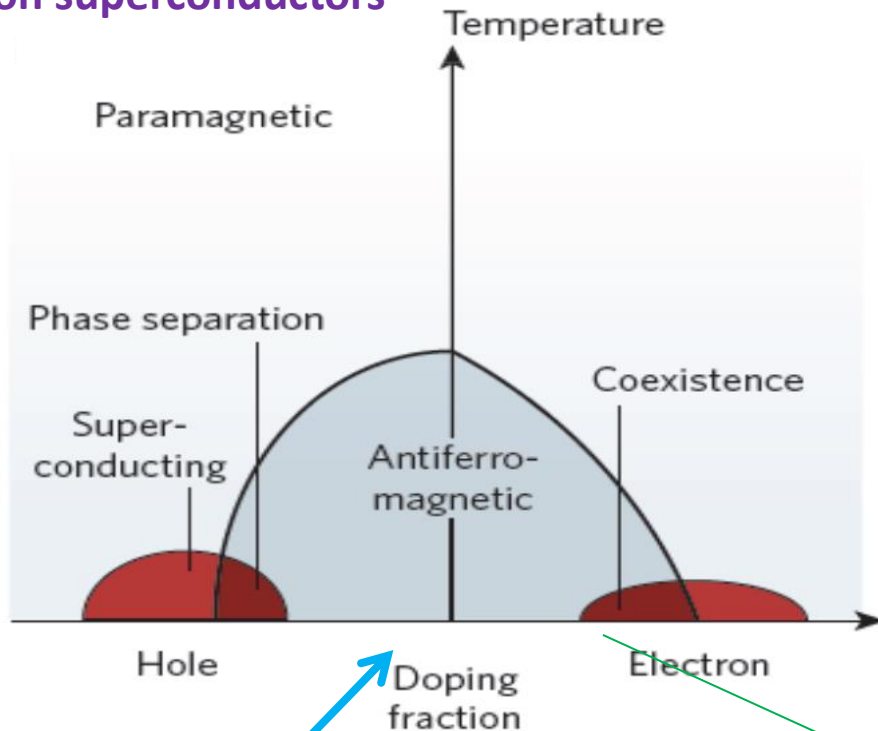
ICMM-CSIC (now at SISSA, Trieste)

[arXiv:1501.04607](https://arxiv.org/abs/1501.04607)



Iron superconductors: metallic when “undoped”

Iron superconductors

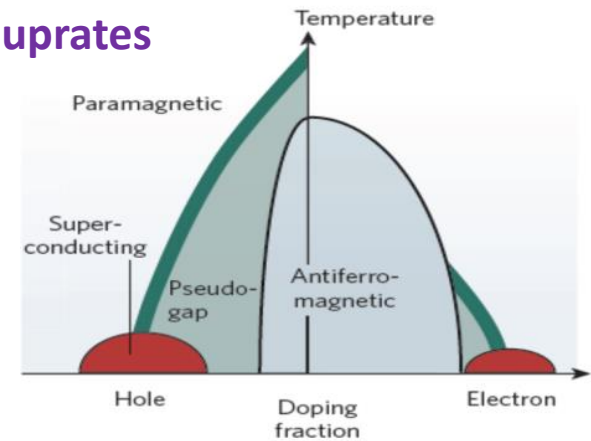


“Undoped” iron superconductors are antiferromagnetic but metallic

**Multi-orbital system:
6 electrons in 5 orbitals**

**Discussion on strength of correlations:
weakly correlated (bands, Fermi surface instabilities),
localized spins, Hund metals**

Cuprates



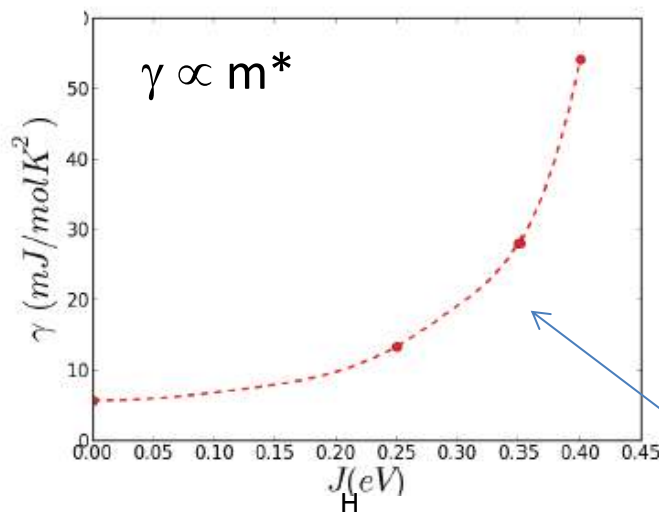
Single orbital system:
1 electron in 1 orbital
(half-filling)

Fig: Nature 464,183 (2010)

Correlations in multi-orbital systems: Hund's coupling & Hund metals

A definition of Hund metals

- Correlations driven by Hund J_H weakly dependent on U ,
- Not in proximity to a Mott insulator
- Properties essentially different to a doped Mott insulator



Haule & Kotliar
NJP 11,025021
(2009)

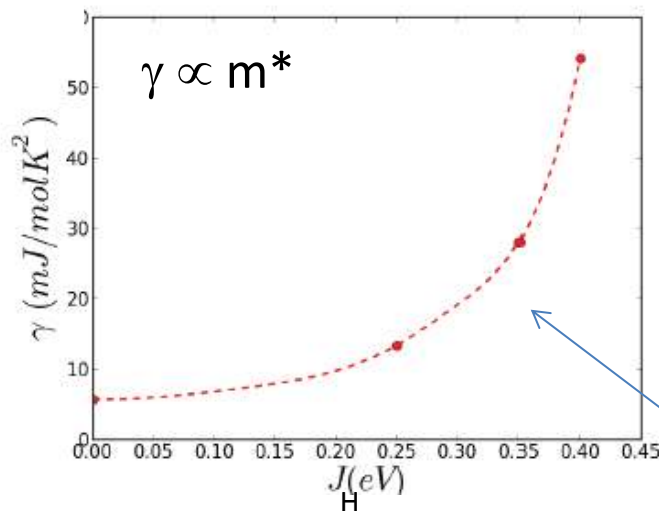
Iron
Superconductors
6 electrons in
5 orbitals

**Understanding Hund metals:
important not only in the context of iron superconductors
but also for many other materials including oxides**

Correlations in multi-orbital systems: Hund's coupling & Hund metals

A definition of Hund metals

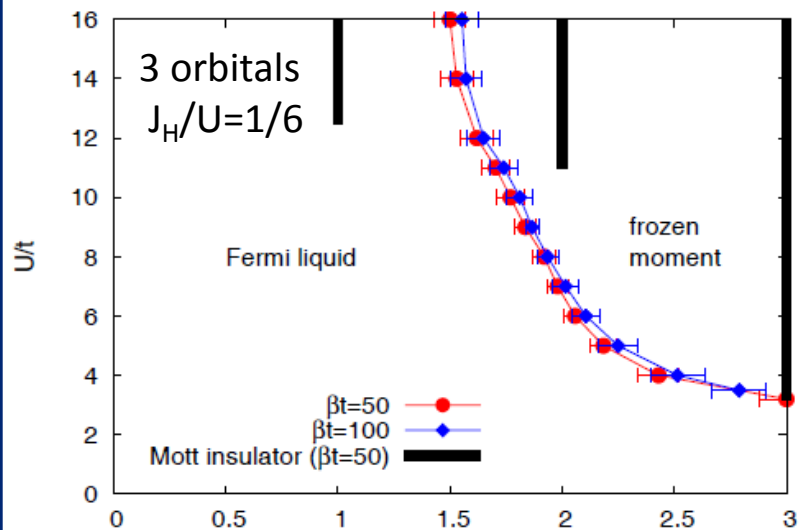
- Correlations driven by Hund J_H weakly dependent on U ,
- Not in proximity to a Mott insulator
- Properties essentially different to a doped Mott insulator



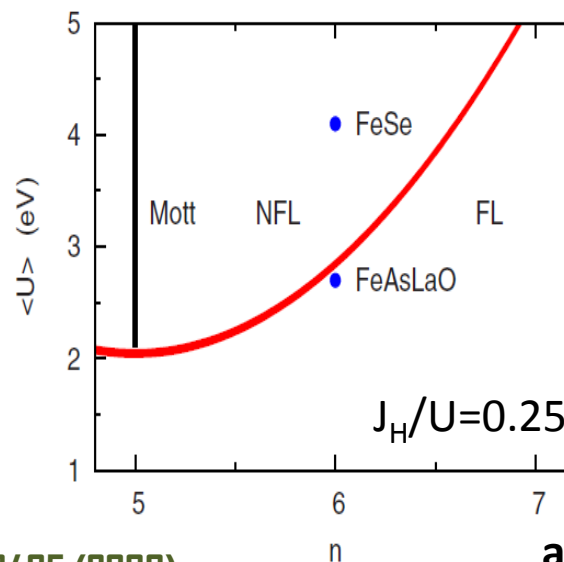
Haule & Kotliar
NJP 11,025021
(2009)

Iron
Superconductors
6 electrons in
5 orbitals

But correlations controlled by proximity in doping to the half-filled Mott insulator



Werner et al PRL 101, 166405 (2008)



Iron superconductors
as doped Mott insulators

Ishida & Liebsch,
PRB 81, 054513 (2010)
Liebsch & Ishida,
PRB 82, 155106 (2010)

Hubbard-Kanamori Hamiltonian for multi-orbital systems

$$\begin{aligned}
 H = & \sum_{i,j,\gamma,\beta,\sigma} t_{i,j}^{\gamma,\beta} c_{i,\gamma,\sigma}^\dagger c_{j,\beta,\sigma} + h.c. + U \sum_{j,\gamma} n_{j,\gamma,\uparrow} n_{j,\gamma,\downarrow} \\
 & \text{Tight-binding (hopping)} \qquad \text{Intra-orbital repulsion} \\
 & + \left(U' - \frac{J_H}{2} \right) \sum_{j,\gamma > \beta, \sigma, \tilde{\sigma}} n_{j,\gamma,\sigma} n_{j,\beta,\tilde{\sigma}} - 2J_H \sum_{j,\gamma > \beta} \vec{S}_{j,\gamma} \vec{S}_{j,\beta} \\
 & \qquad \text{Inter-orbital repulsion} \qquad \text{Hund's coupling} \\
 & + J' \sum_{j,\gamma \neq \beta} c_{j,\gamma,\uparrow}^\dagger c_{j,\gamma,\downarrow}^\dagger c_{j,\beta,\downarrow} c_{j,\beta,\uparrow} \\
 & \qquad \text{Pair hopping}
 \end{aligned}$$

We assume equivalent orbitals
(no hybridization between them)

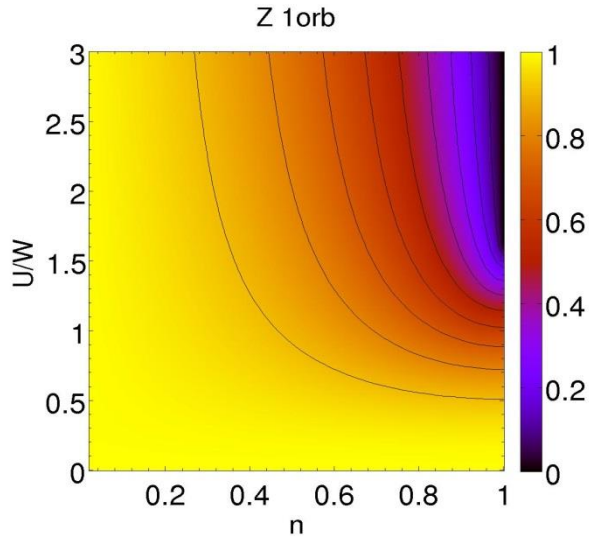
$$U' = U - 2J_H \quad J' = J_H$$

Two interaction parameters: U , J_H

Slave-spin (only density-density terms)

Charge and spin fluctuations in the single-orbital Hubbard model

Quasiparticle weight Z



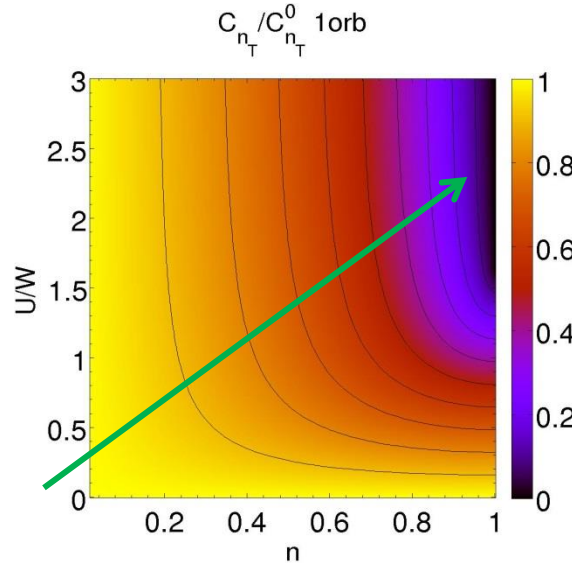
Localization

Charge fluctuations

(local & instantaneous)

$$C_T = \langle n^2 \rangle - \langle n \rangle^2 = \langle (\delta n)^2 \rangle$$

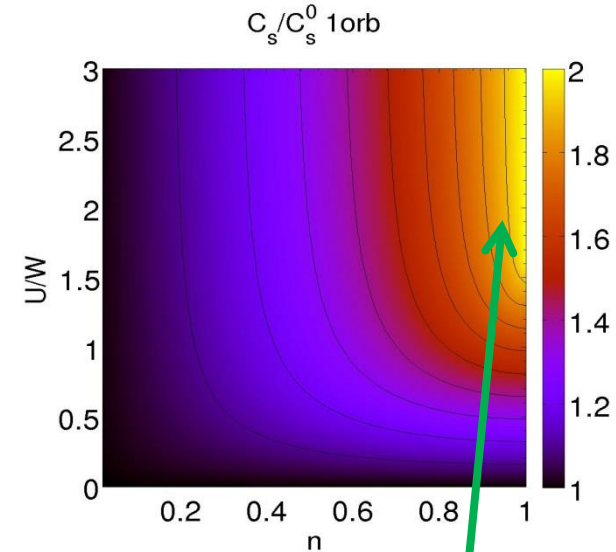
$$n = \langle n \rangle + \delta n$$



Spin fluctuations

(local & instantaneous)

$$C_S = \langle S^2 \rangle - \langle S \rangle^2 = \langle S^2 \rangle$$



Enhancement of spin fluctuations

Mott insulator:

Suppression of charge fluctuations

$$n = \langle n \rangle$$



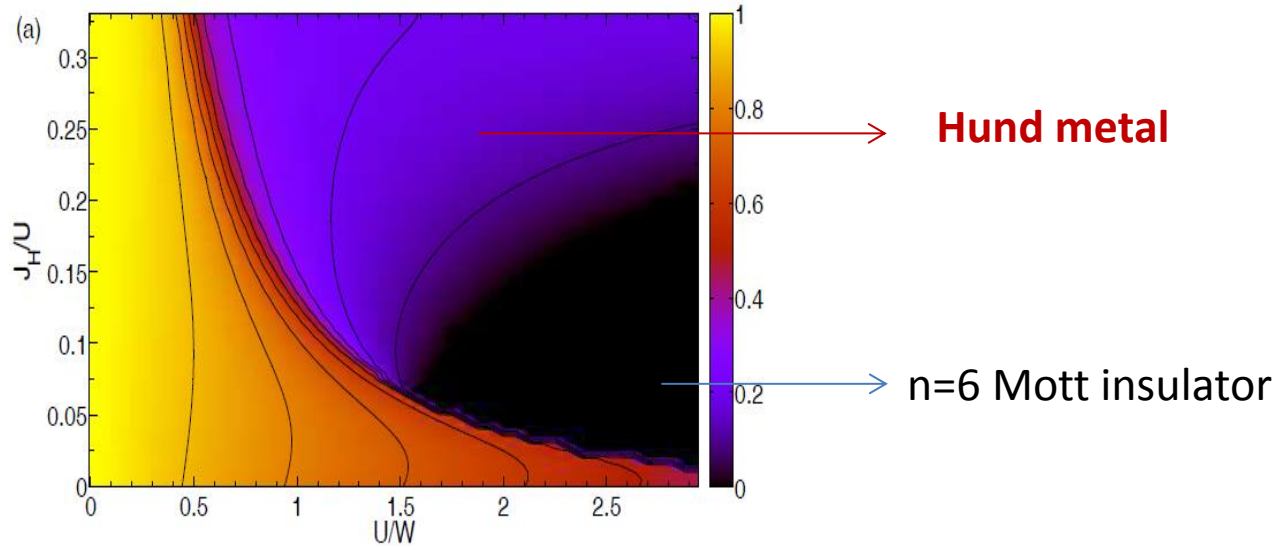
Localized spins
at each
atomic site

C_S larger when atoms are spin polarized even if there is no long-range order

Electronic correlations in multi-orbital systems: Hund metals

6 electrons in 5 orbitals

Colour plots: **Quasiparticle weight Z**

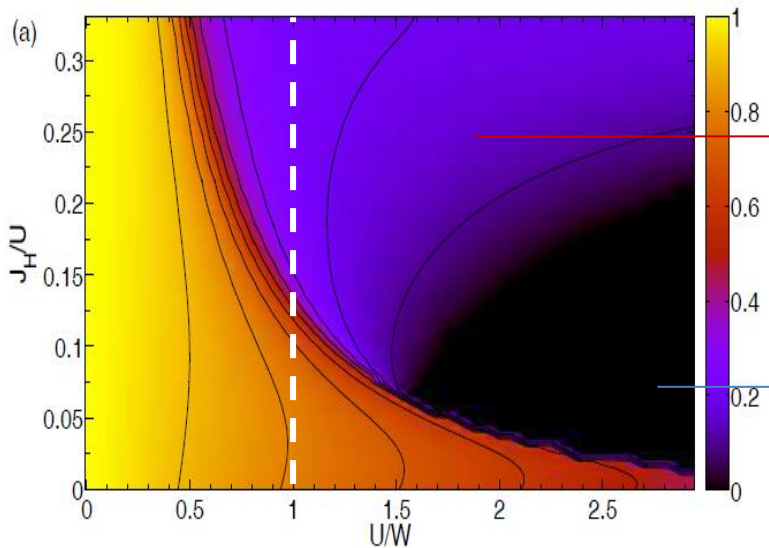


Fanfarillo & EB, arXiv:1501.04607

Electronic correlations in multi-orbital systems: Hund metals

6 electrons in 5 orbitals

Colour plots: **Quasiparticle weight Z**

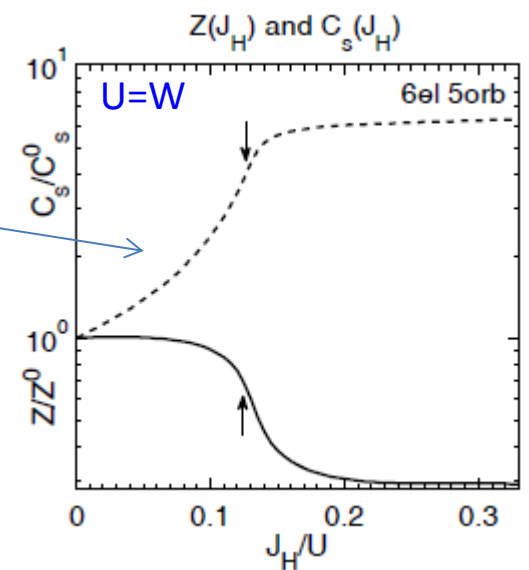


Hund metal

Suppression of Z associated to the atomic spin polarization

n=6 Mott insulator

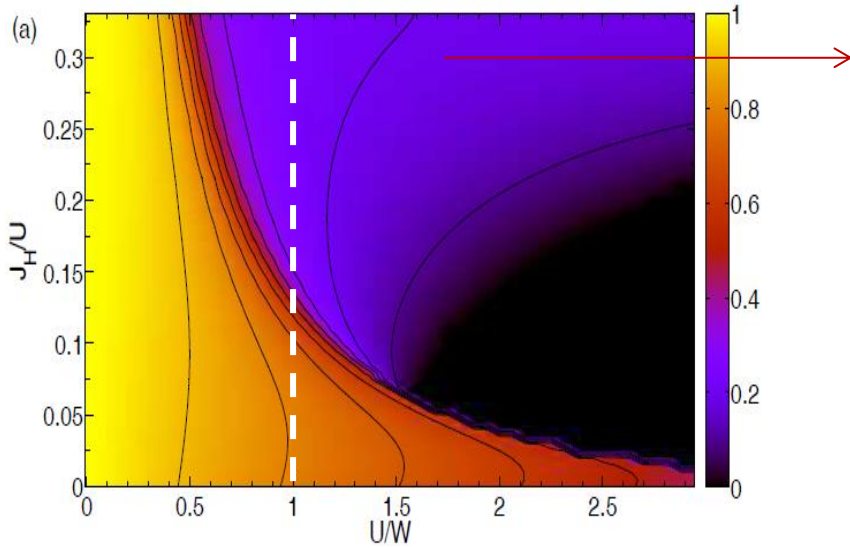
Enhancement of Spin fluctuations



Fanfarillo & EB, arXiv:1501.04607

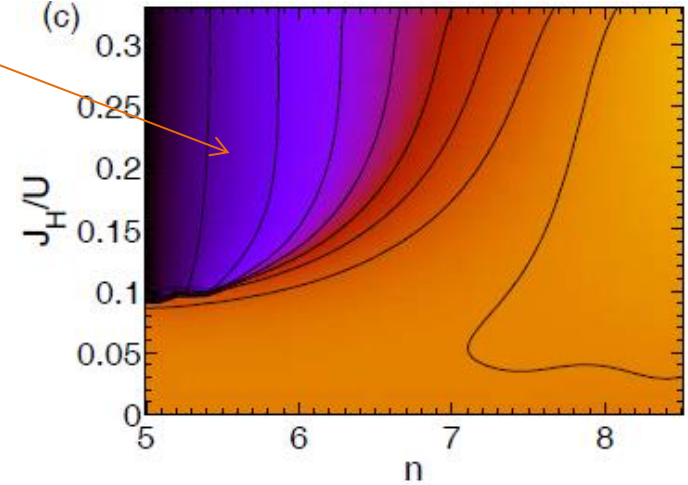
Electronic correlations in multi-orbital systems: Hund metals

6 electrons in 5 orbitals



Colour plots: **Quasiparticle weight Z**

Hund metal

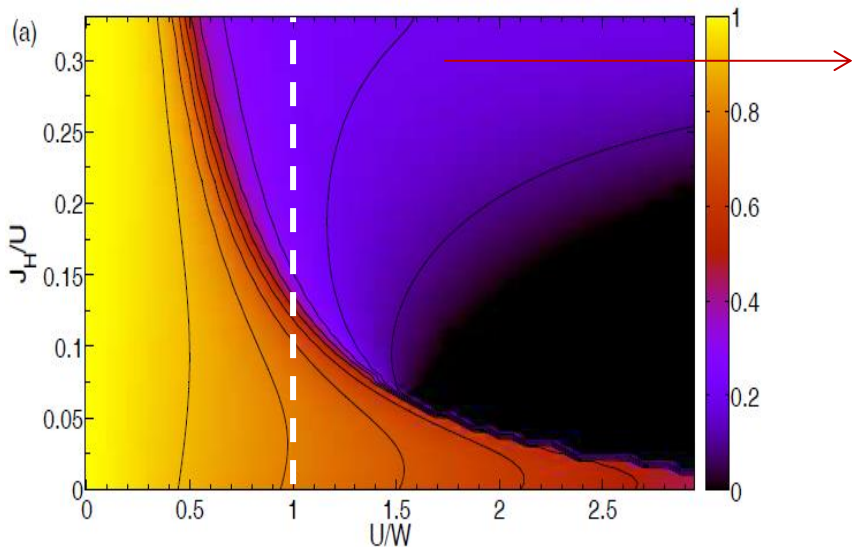


Fanfarillo & EB, arXiv:1501.04607

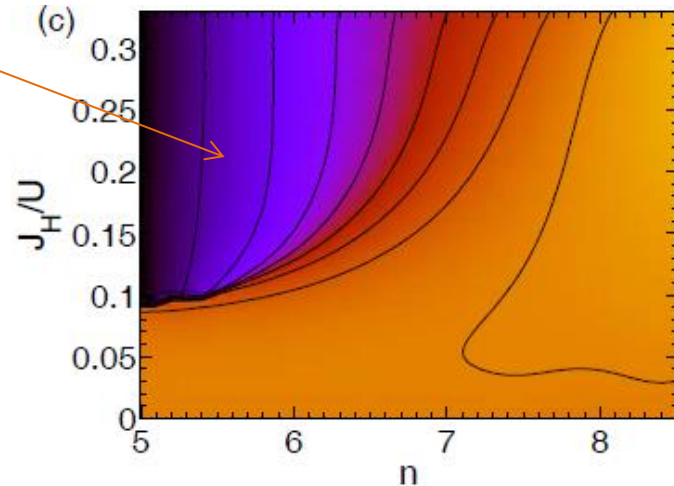
Electronic correlations in multi-orbital systems: Hund metals

6 electrons in 5 orbitals

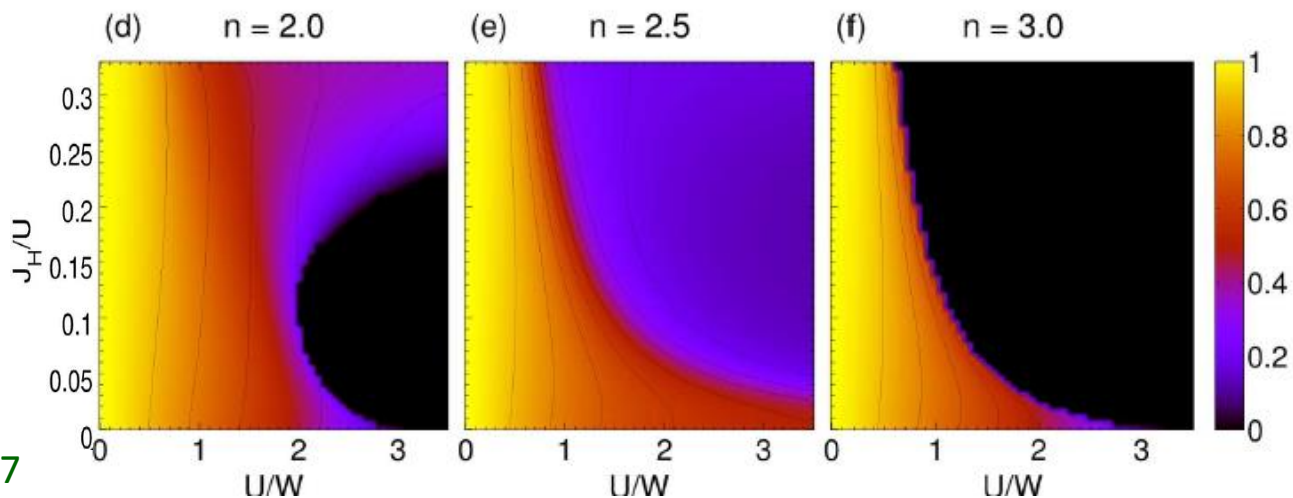
Colour plots: **Quasiparticle weight Z**



Hund metal

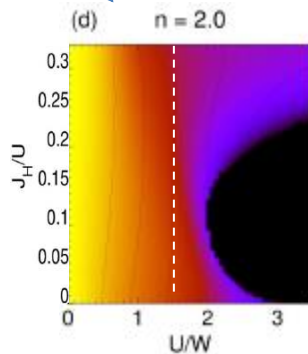
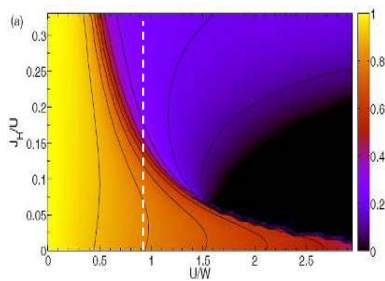
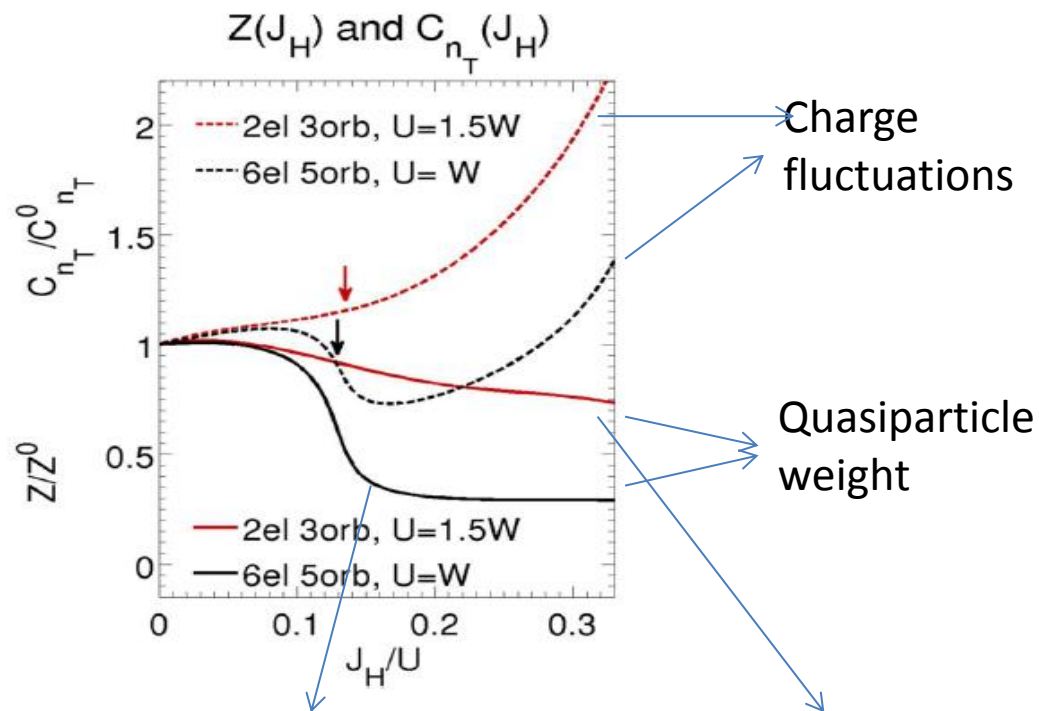


3 orbitals



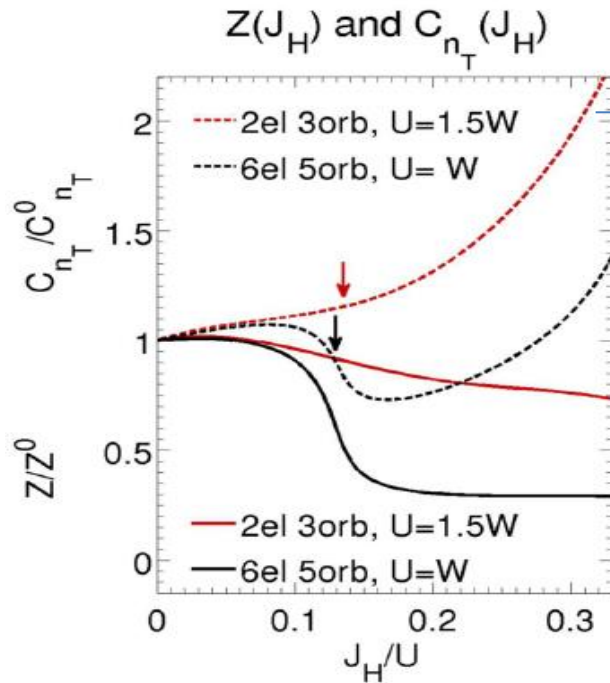
We confirm that the correlations in Hund metals are directly connected to the half-filled Mott insulator

Electronic correlations in multi-orbital systems: Hund metals



Fanfarillo & EB, arXiv:1501.04607

Electronic correlations in multi-orbital systems: Hund metals



Charge fluctuations

Quasiparticle weight

The quasiparticle weight and the charge fluctuations show different behavior

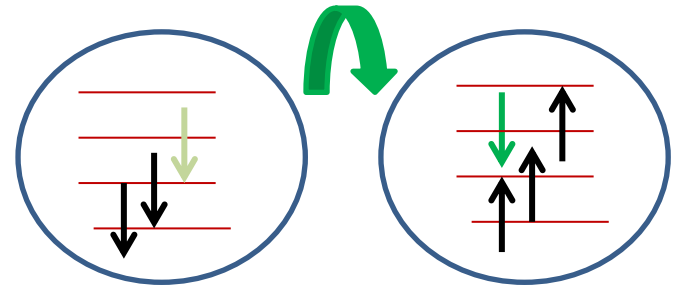
(opposite to what happens in Mott correlated states in the single orbital case)

Contrary to what happens in Mott correlated single-orbital systems, In Hund metals the quasiparticle weight and the mass enhancement are not good measures of charge localization

Electronic correlations in multi-orbital systems: Hund metals

Correlations in Hund metals are directly connected to the half-filled Mott insulator but contrary to what happens in Mott systems, in Hund metals the quasiparticle weight Z can be suppressed on spite of increasing charge correlations

- ❑ Suppression of coherence due to suppression of hopping processes which involve intraorbital double occupancy $E^{intra\uparrow\downarrow} = U + (n - 1)J_H$



Key role!

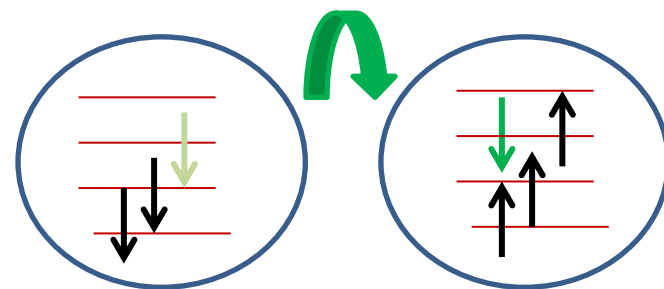
Electronic correlations in multi-orbital systems: Hund metals

Correlations in Hund metals are directly connected to the half-filled Mott insulator but contrary to what happens in Mott systems, in Hund metals the quasiparticle weight Z can be suppressed on spite of increasing charge correlations

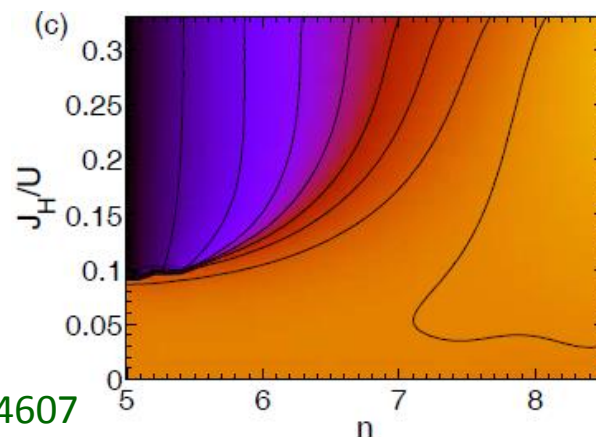
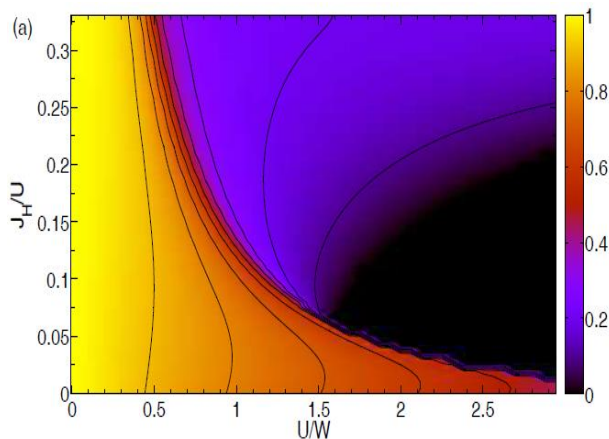
- Suppression of coherence due to suppression of hopping processes which involve intraorbital double occupancy

$$E^{intra\uparrow\downarrow} = U + (n - 1)J_H$$

Suppressed by Hund's coupling



Links correlations in Hund metals with half-filled Mott insulator



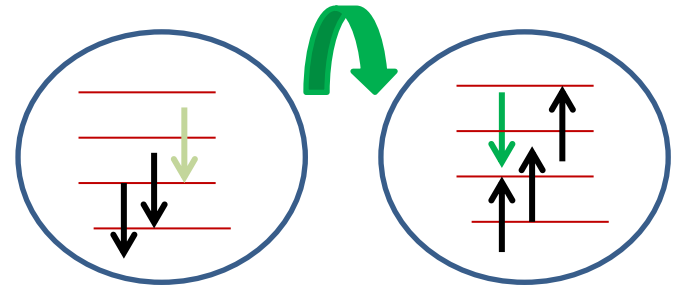
Fanfarillo & EB, arXiv:1501.04607

Electronic correlations in multi-orbital systems: Hund metals

Correlations in Hund metals are directly connected to the half-filled Mott insulator but contrary to what happens in Mott systems, in Hund metals the quasiparticle weight Z can be suppressed on spite of increasing charge correlations

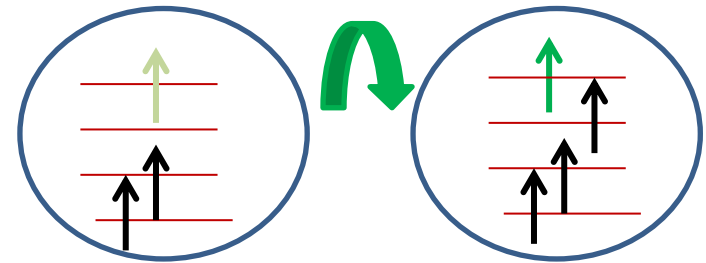
- ❑ Suppression of coherence due to suppression of hopping processes which involve intraorbital double occupancy

$$E^{intra\uparrow\downarrow} = U + (n - 1)J_H$$



- ❑ Enhancement of charge fluctuations due to hopping processes which involve parallel spins to an empty orbital

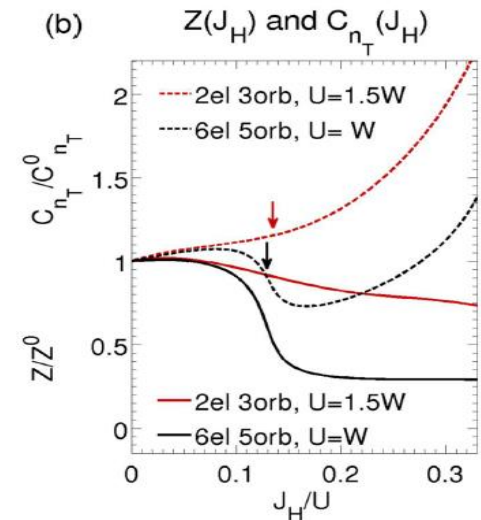
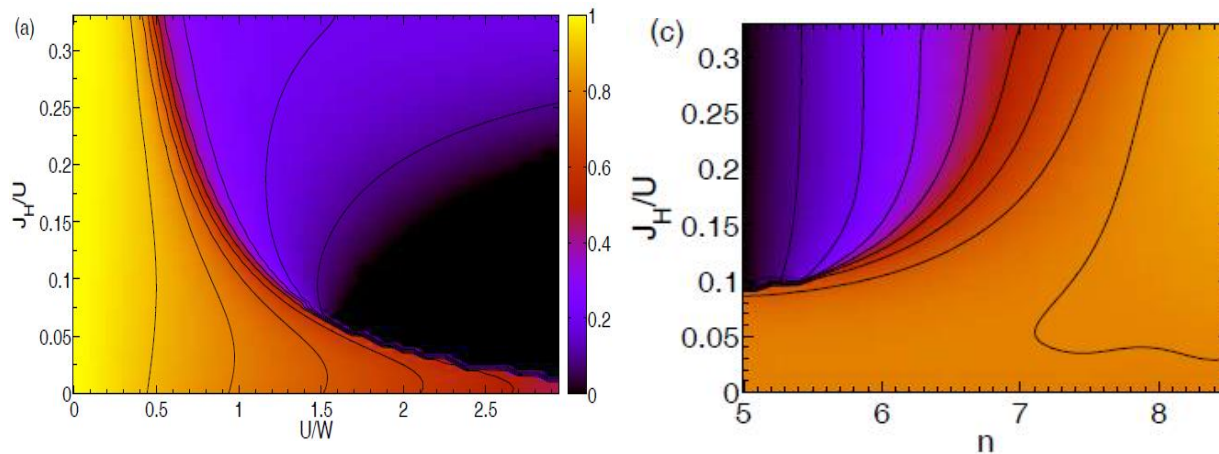
$$E^{\uparrow\uparrow} = U - 3J_H$$



Fanfarillo & EB, arXiv:1501.04607

Summary

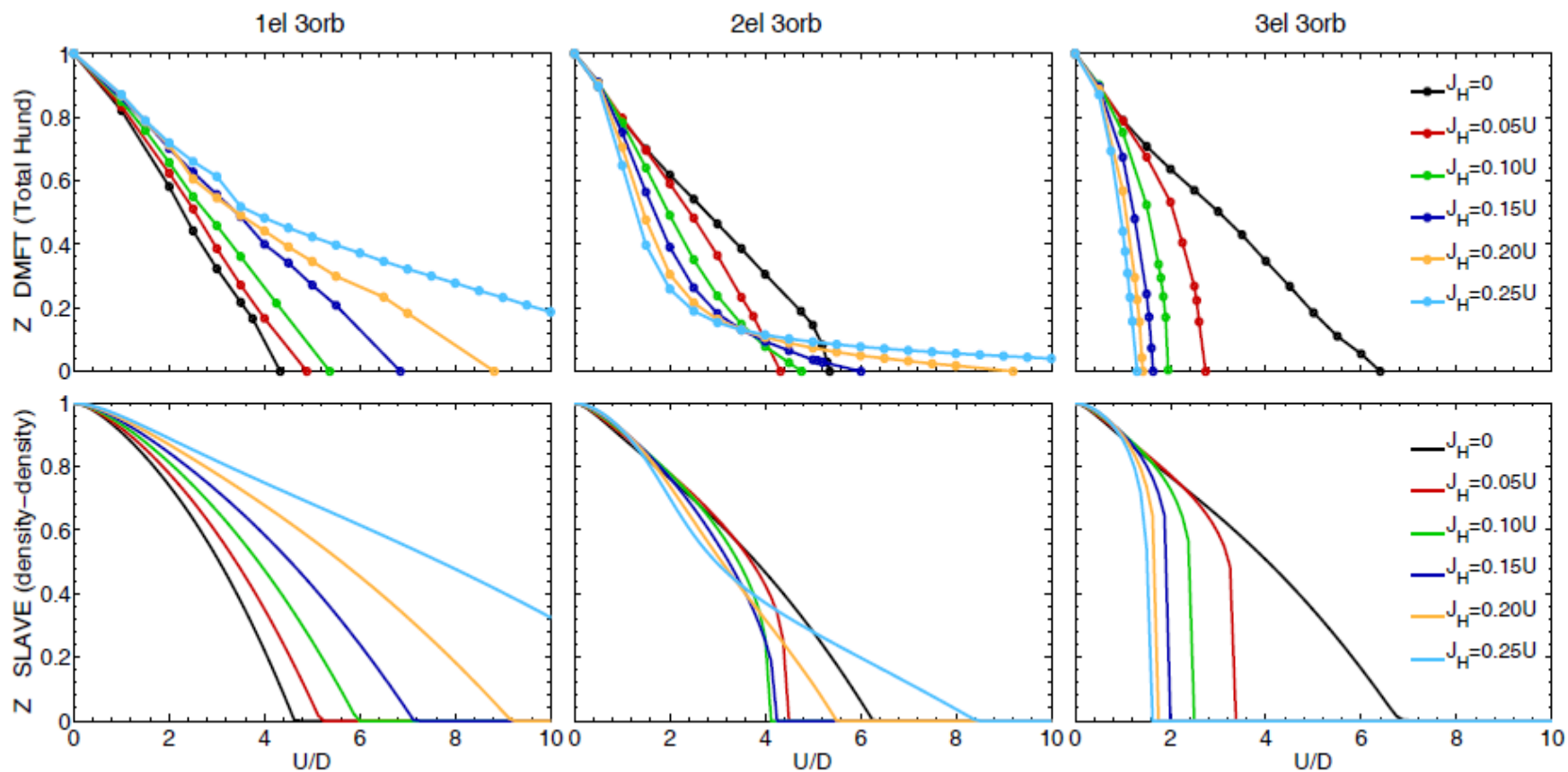
Correlations in Hund metals are directly connected to the half-filled Mott insulator but contrary to what happens in Mott systems, in Hund metals the quasiparticle weight Z can be suppressed on spite of increasing charge correlations



- ❑ Understood in terms of which hopping processes are suppressed (intraorbital double occupancy) or promoted (hopping to an empty orbital with parallel spin)
- ❑ Behavior changes at large U and J_H due to the proximity of non half-filled Mott insulator
- ❑ Understanding of why Hund's coupling promotes orbital decoupling

Slave spin (Density-density): benchmark

3 orbitals, semi-circular density of states



Fanfarillo & EB, arXiv:1501.04607

The quasiparticle weight in the single-orbital Hubbard model

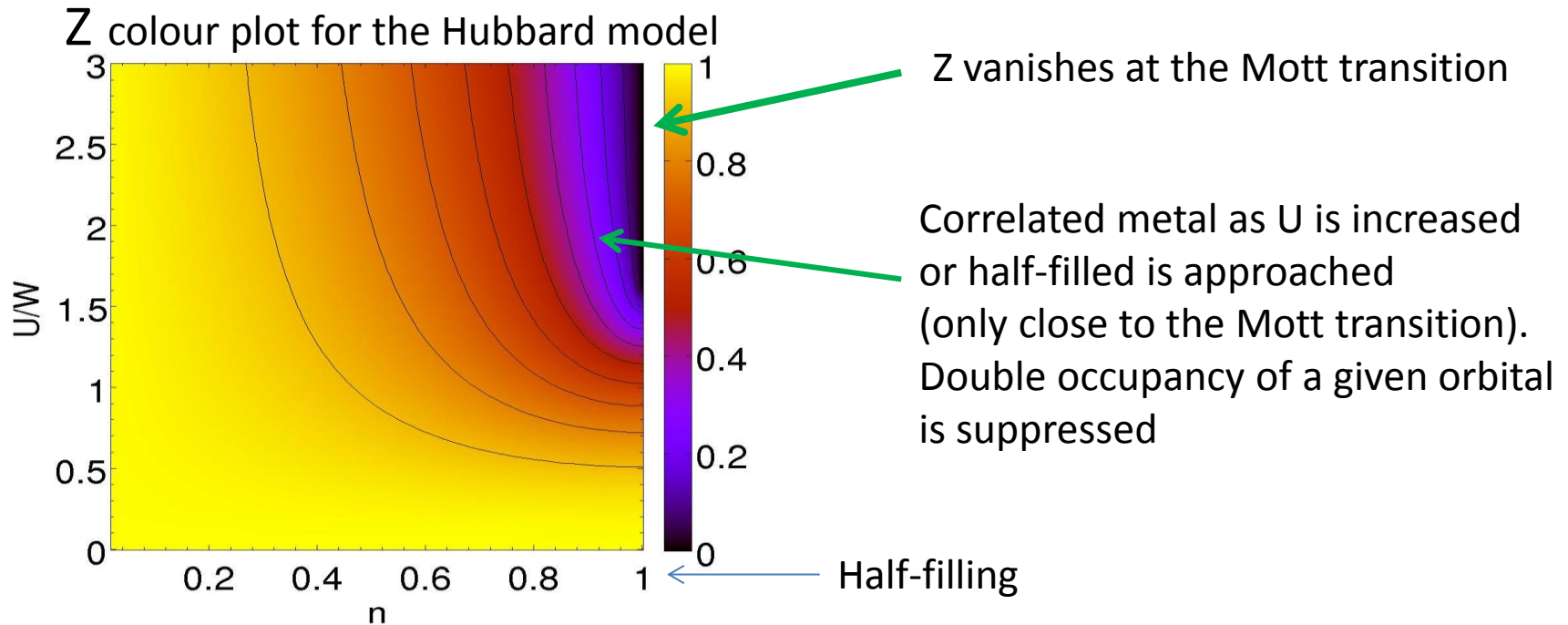
Z: a way to quantify the correlations

$$0 \leq Z \leq 1$$

Z=1 Single-particle picture (U=0)

Z=0 There are no quasiparticles
Breakdown of single-particle picture

Simple Fermi liquid description: Heavy electron $Z^{-1} \propto m^*/m$



W bandwidth

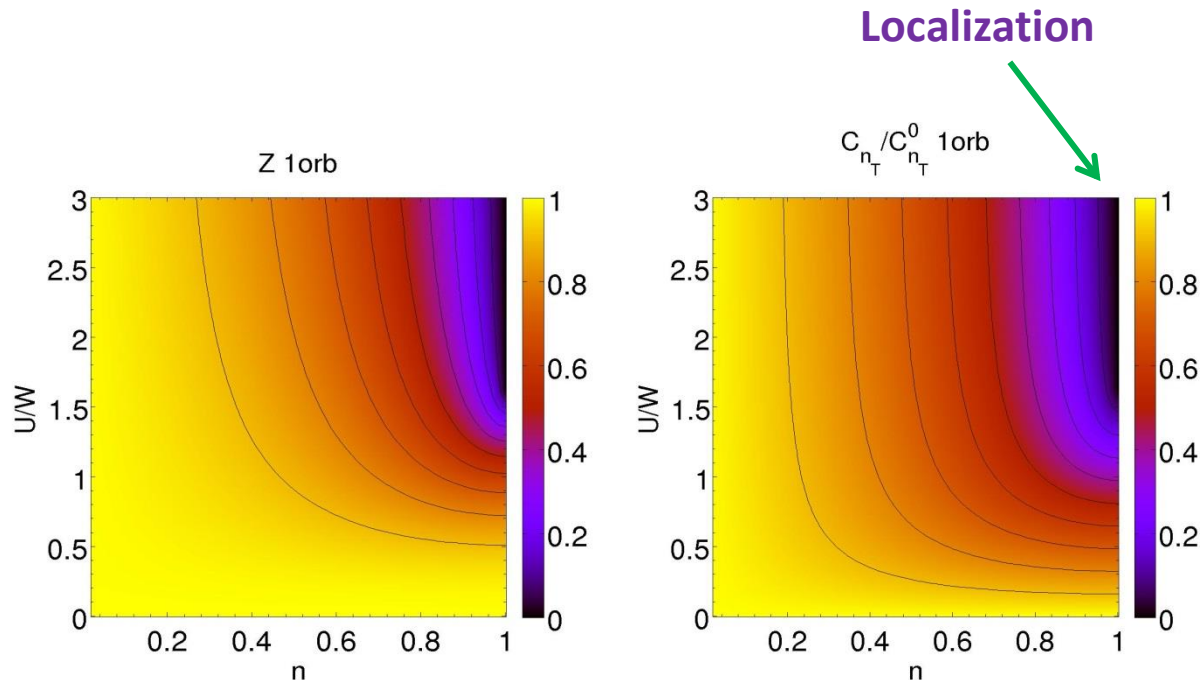
of non interacting system

n: number of electrons per atom

Charge and spin fluctuations in the single-orbital Hubbard model

$$n = \langle n \rangle + \delta n$$

$$C_T = \langle n^2 \rangle - \langle n \rangle^2 = \langle (\delta n)^2 \rangle$$



Very often
the quasiparticle weight Z
or the mass enhancement
are taken as a measure
of charge localization

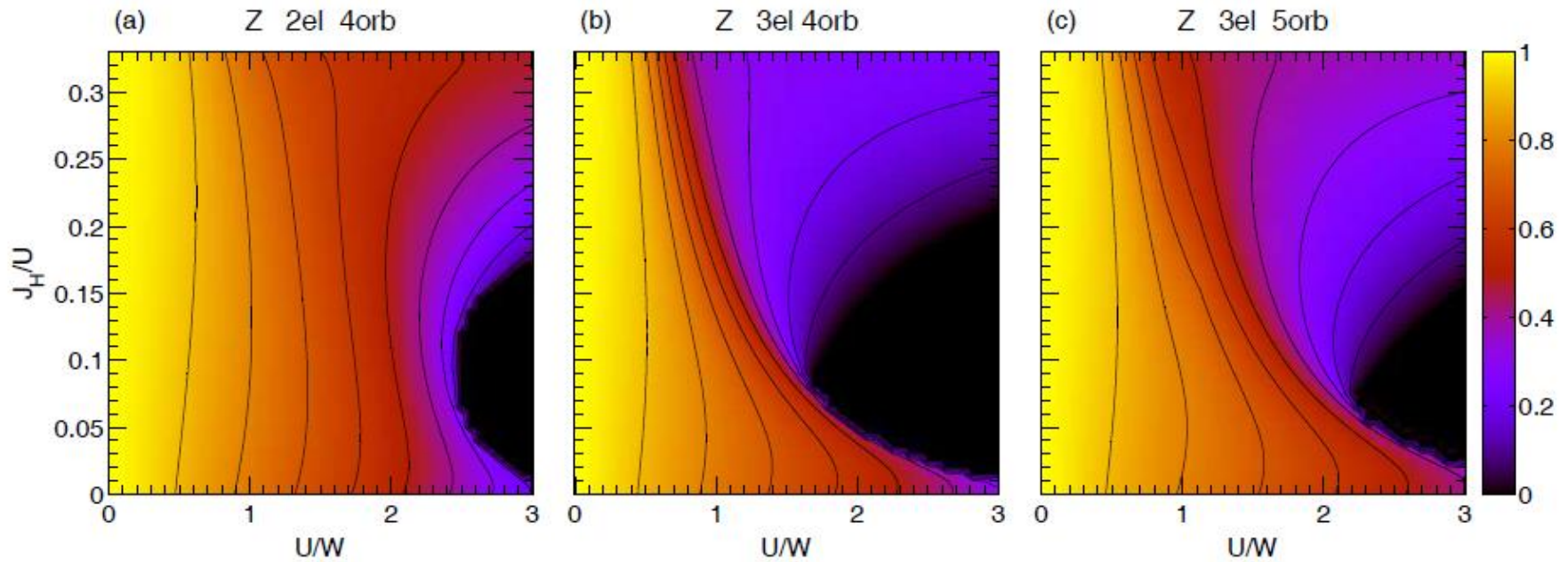
Mott insulator:

Suppression of charge fluctuations

$$n = \langle n \rangle$$

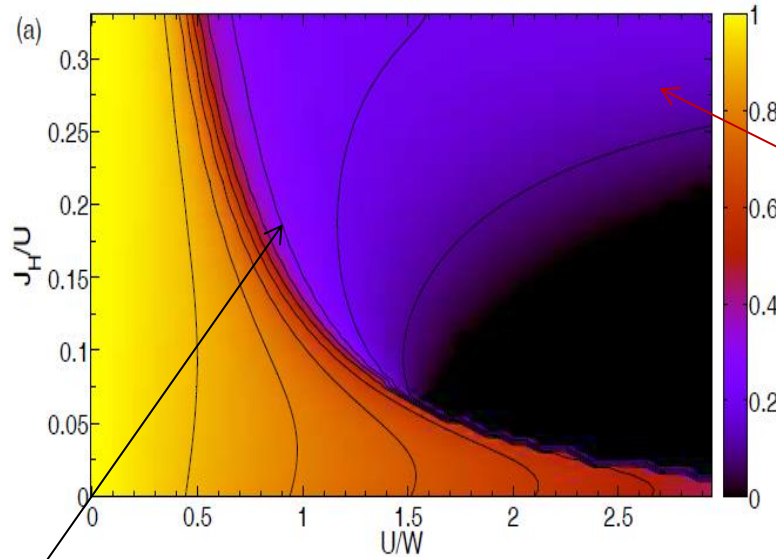
Electronic correlations in Hund metals

Colour plots: **Quasiparticle weight Z**



Fanfarillo & EB, arXiv:1501.04607

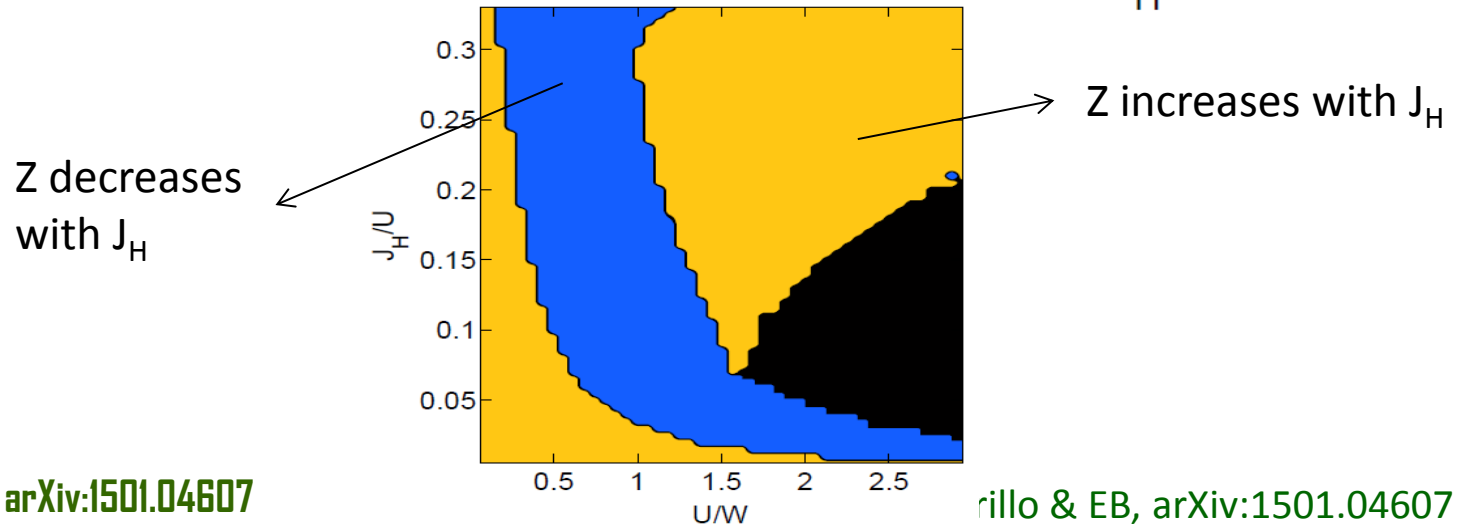
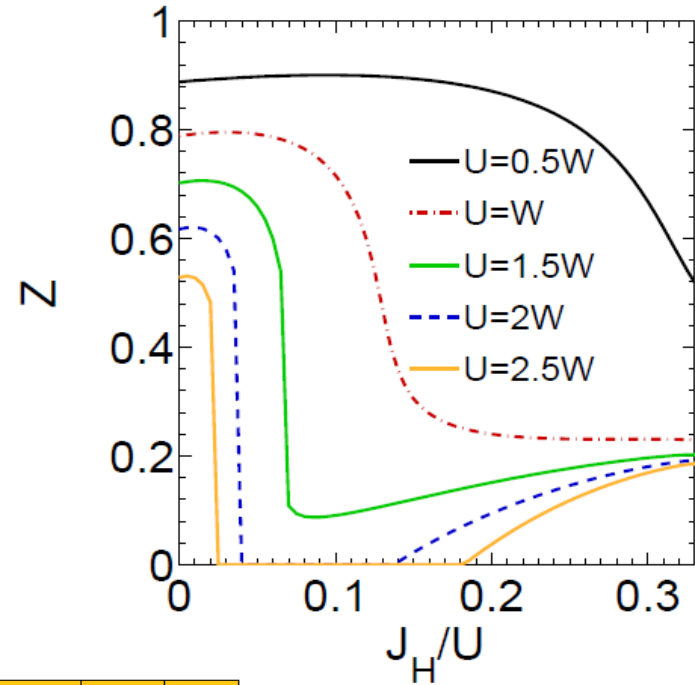
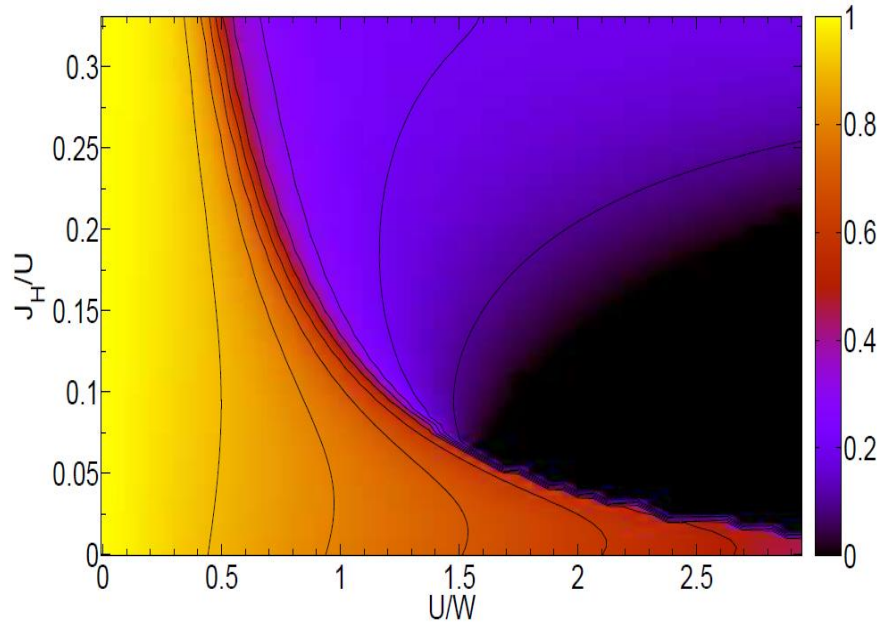
Electronic correlations in multi-orbital systems: Hund metals



Behavior of the system controlled by the proximity to the (n=6) Mott insulating phase (Z increases with J_H , Cs decrease with U)

Suppression of coherence due to atomic spin polarization (Z decreases with J_H , Cs increase with U)

6 electrons in 5 orbitals,

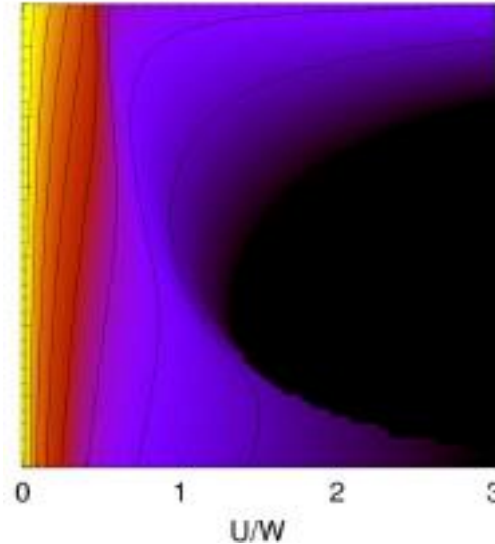
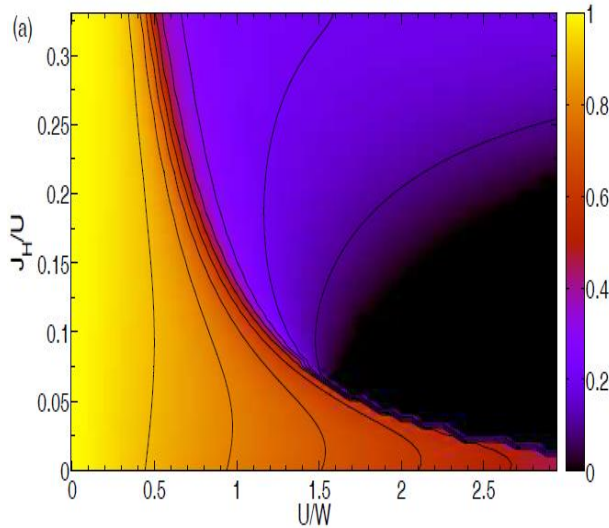


Evolution of charge fluctuations in Hund metals

Quasiparticle Weight Z

Charge Fluctuations

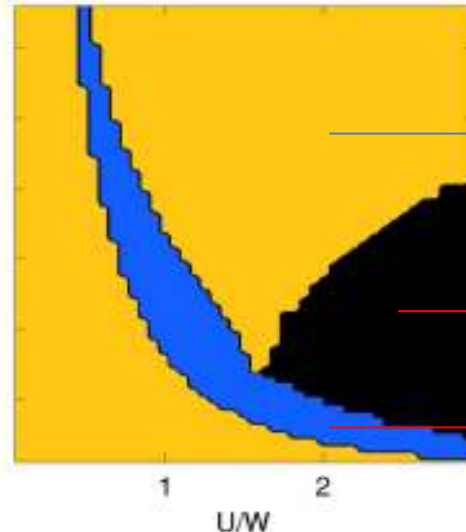
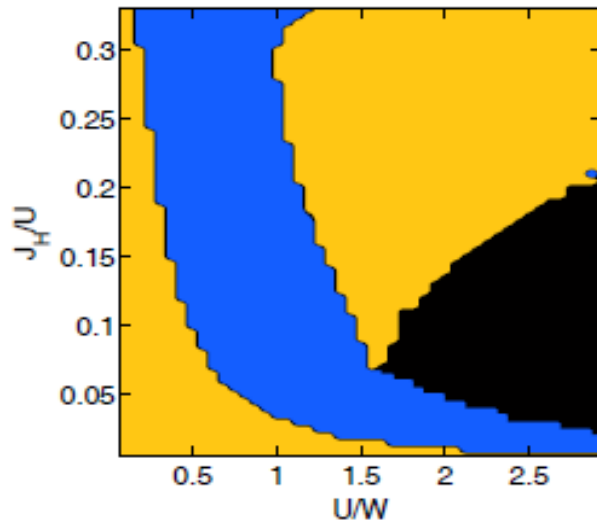
6 electrons in 5 orbitals



The suppression of the quasiparticle weight and the charge fluctuations with interactions follow different patterns

(a) Sign dZ/dJ_H 6el 5orb

(d) Sign dC_{n_T}/dJ_H 6el 5orb



Yellow: increases with J_H

Black: does not change with J_H

Blue: decreases with J_H

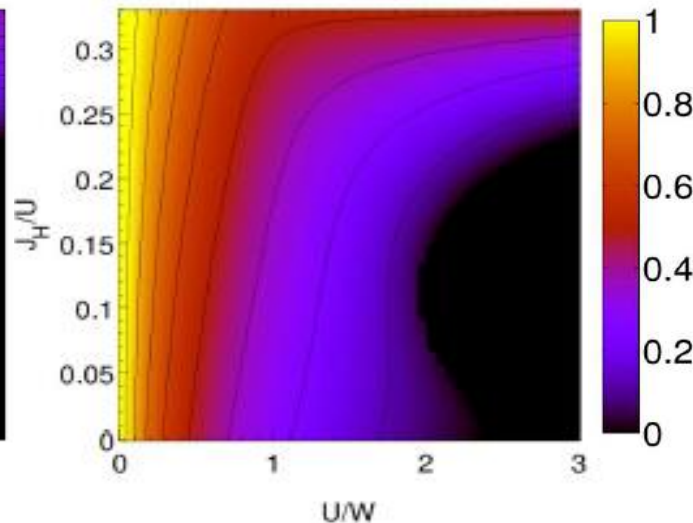
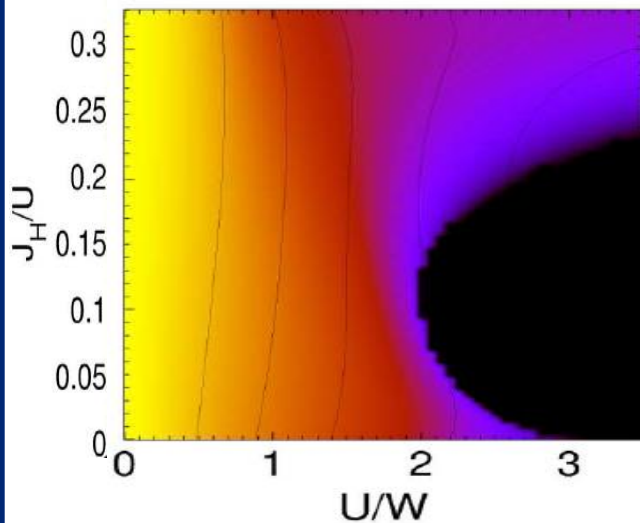
Fanfarillo & EB, arXiv:1501.04607

Evolution of charge fluctuations in Hund metals

2 electrons in 3 orbitals

Quasiparticle Weight Z

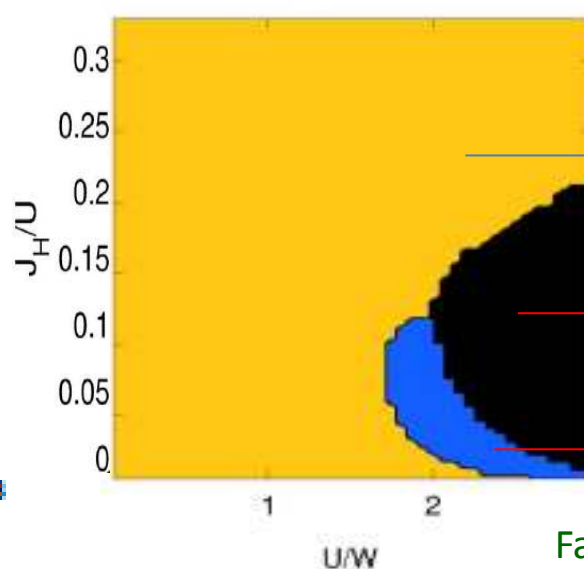
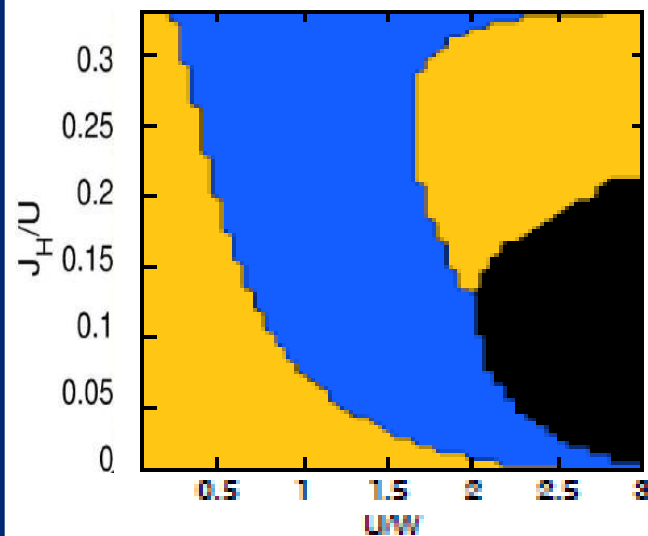
Charge Fluctuations



The suppression of the quasiparticle weight and the charge fluctuations with interactions follow different patterns

(b) Sign dZ/dJ_H 2el 3orb

(b) Sign dC_n/dJ_H 2el 3orb



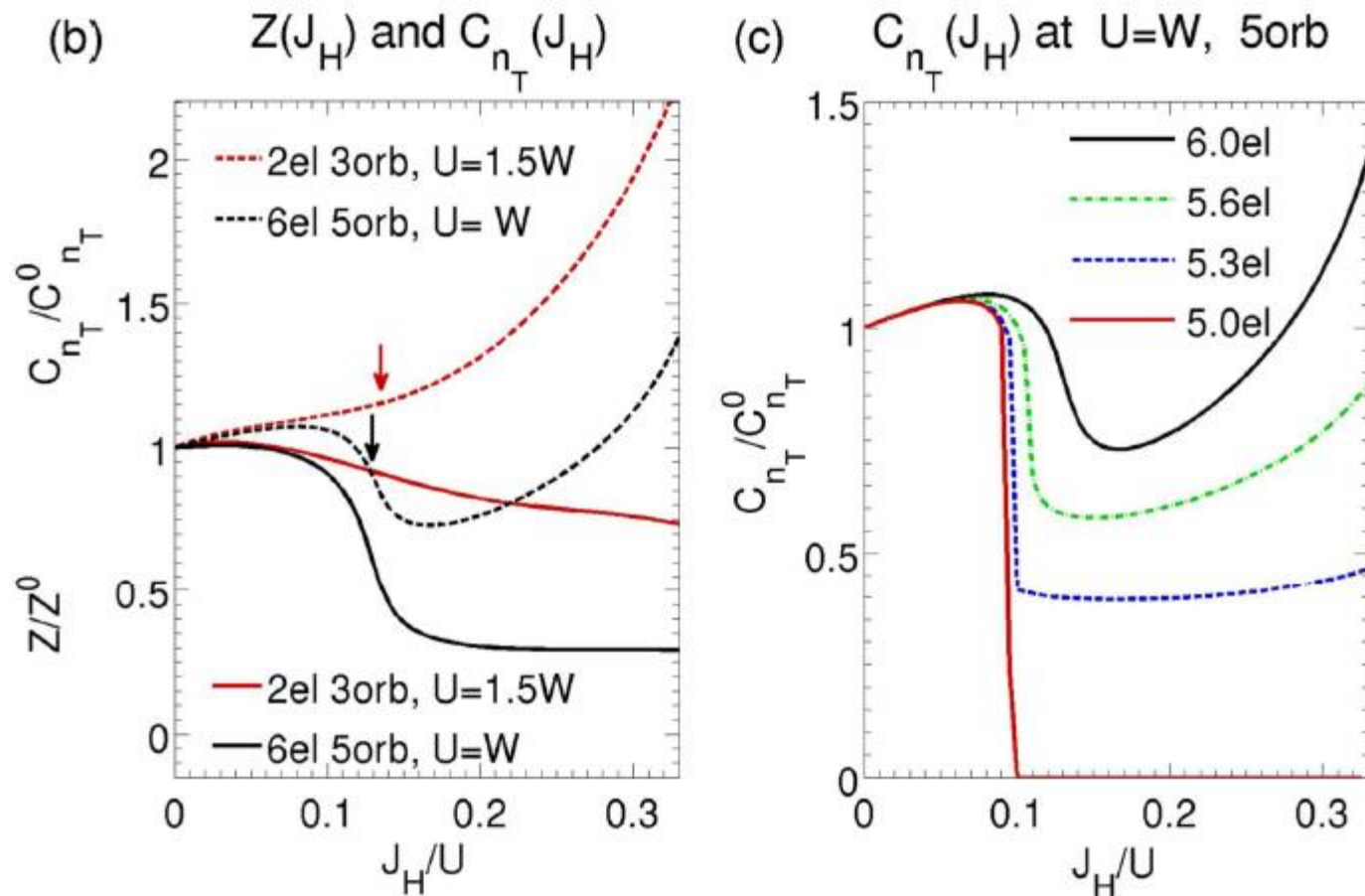
Yellow: increases with J_H

Black: does not change with J_H

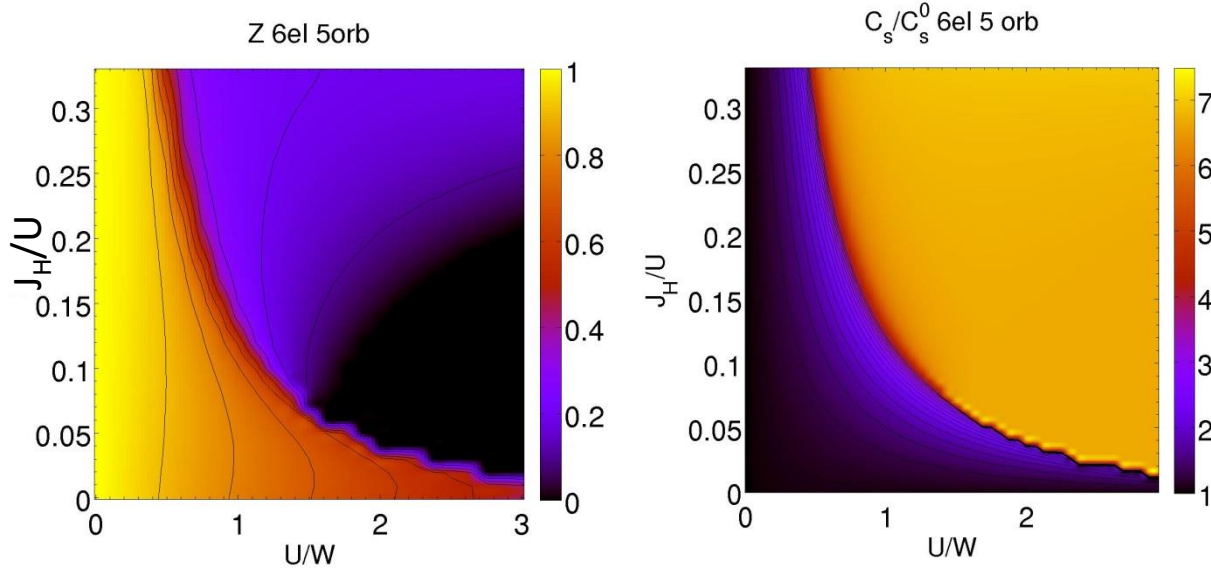
Blue: decreases with J_H

Fanfarillo & EB, arXiv:1501.04607

Evolution of charge fluctuations in Hund metals

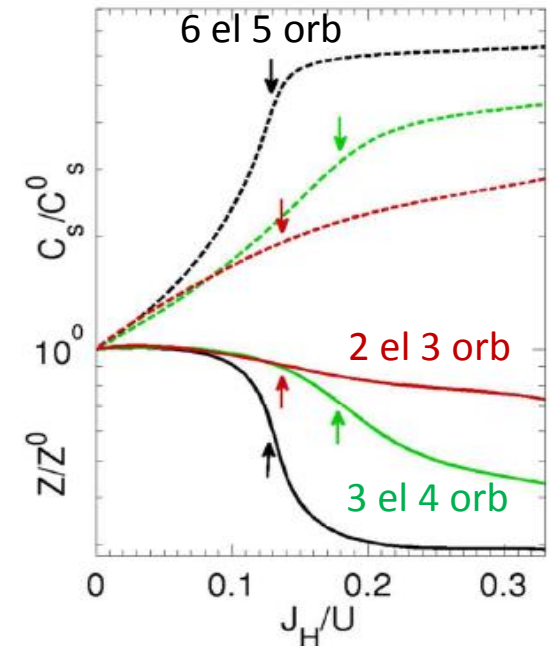


Spin fluctuations in Hund metals



6 electrons in 5 orbitals

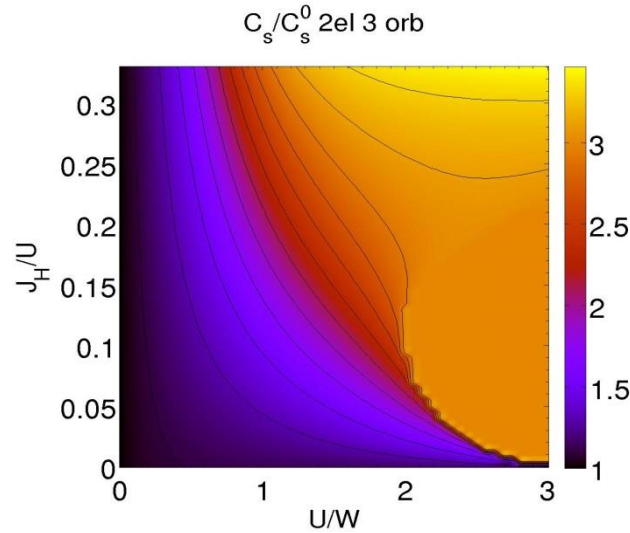
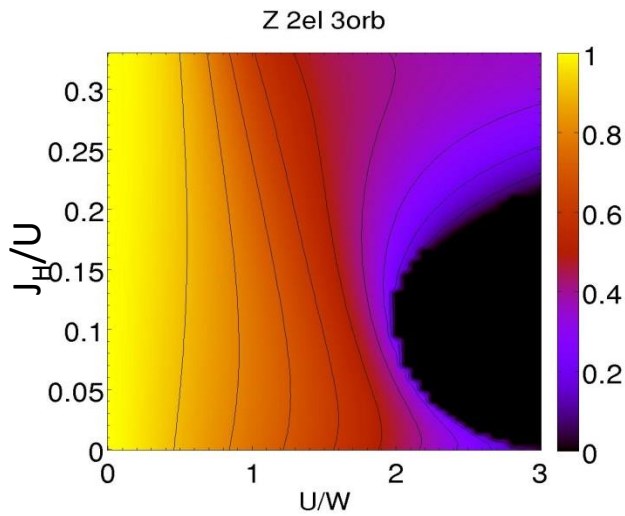
$Z(J_H)$ and $C_s(J_H)$



Atomic moments are formed in the Hund metal

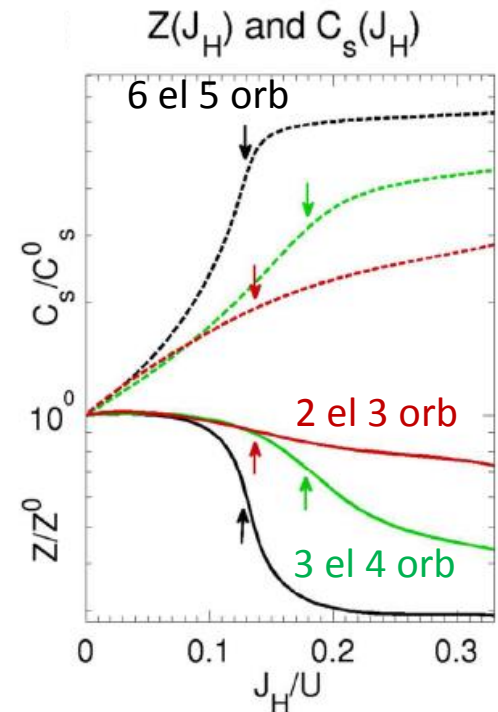
Fanfarillo & EB, arXiv:1501.04607

Spin fluctuations in Hund metals



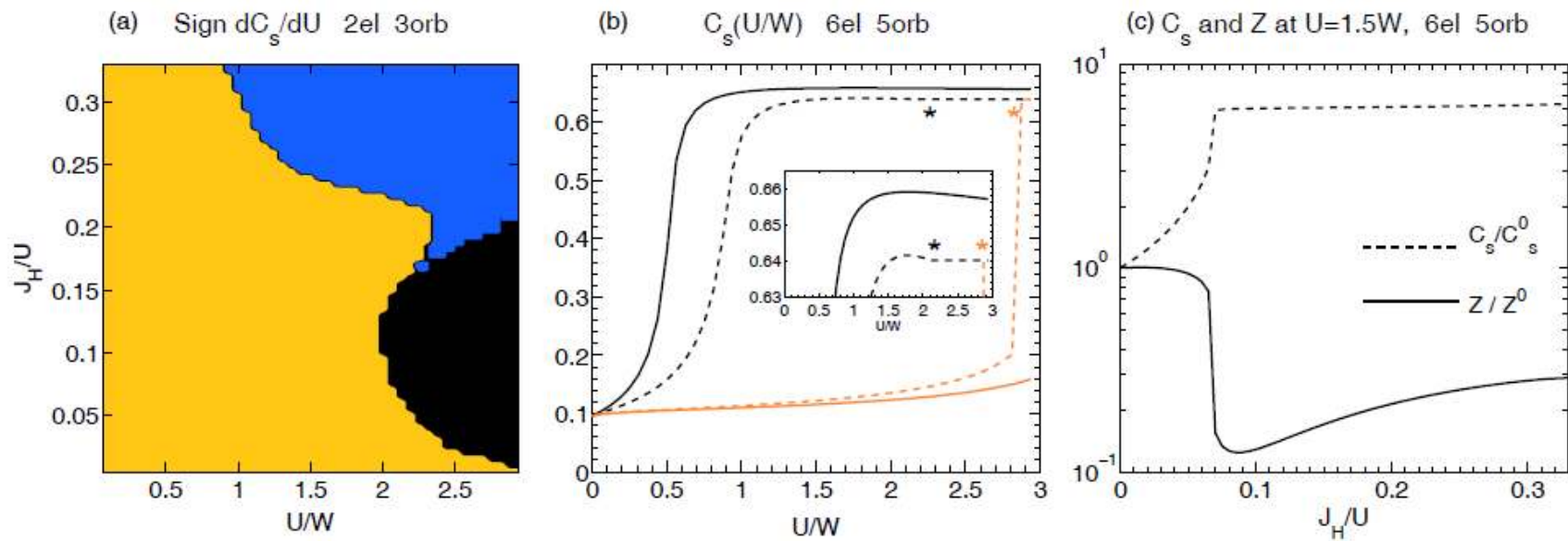
2 electrons in 3 orbitals

Atomic moments are formed in the Hund metal



Fanfarillo & EB, arXiv:1501.04607

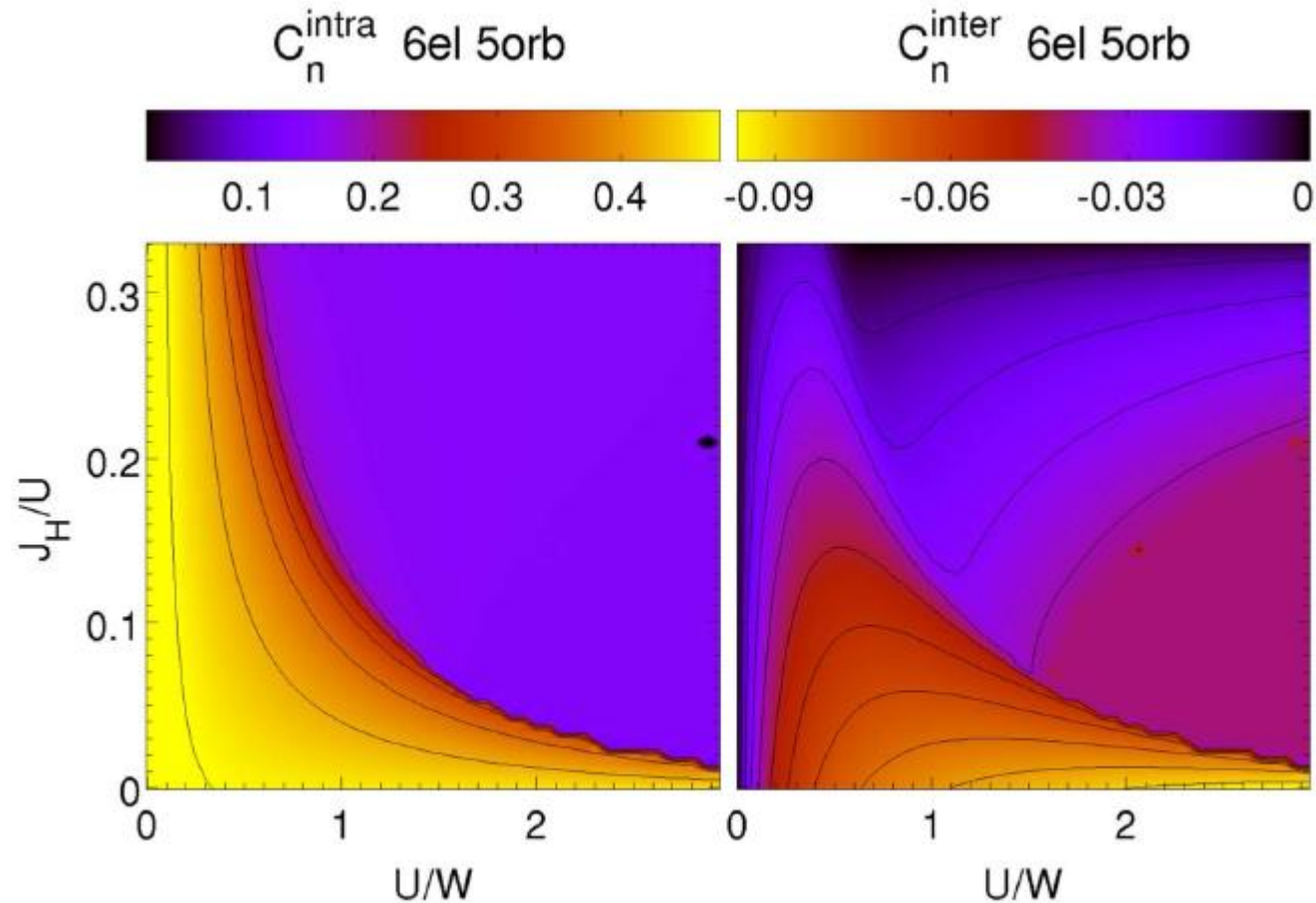
Spin fluctuations in Hund metals



Fanfarillo & EB, arXiv:1501.04607

Electronic correlations in multi-orbital systems: Hund metals

$$C_n^{\text{intra}} = \langle n_a^2 \rangle - \langle n_a \rangle^2 = \langle (\delta n_a)^2 \rangle \quad C_n^{\text{inter}} = \langle n_a n_b \rangle - \langle n_a \rangle \langle n_b \rangle = \langle \delta n_a \delta n_b \rangle$$

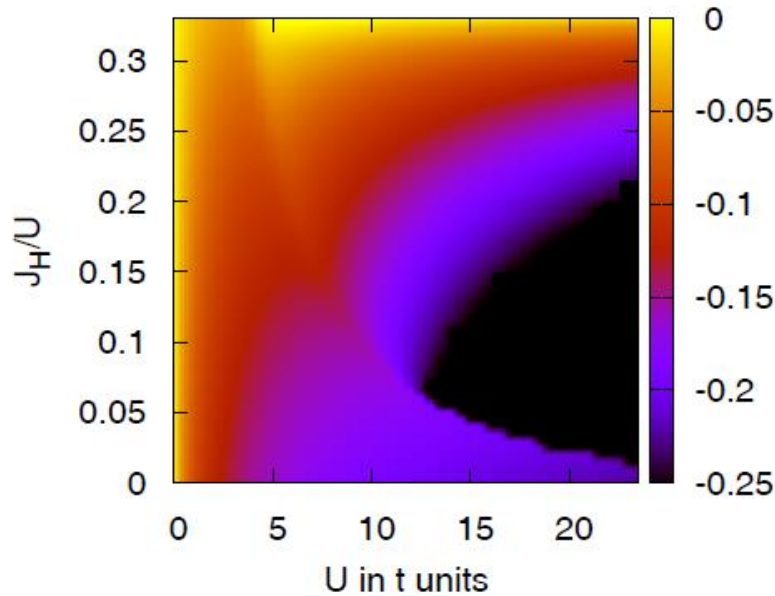


$$C_{n_T} = N \left(C_n^{\text{intra}} + (N - 1) C_n^{\text{inter}} \right)$$

Fanfarillo & EB, arXiv:1501.04607

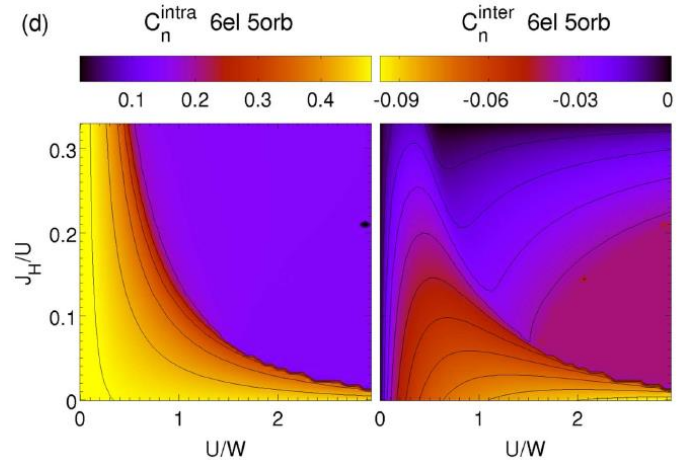
Electronic correlations in multi-orbital systems: Decoupling

Inter/Intra C_n 4.00 electron in 5 orbitals



$$C_n^{\text{inter}} = \langle n_a n_b \rangle - \langle n_a \rangle \langle n_b \rangle = \langle \delta n_a \delta n_b \rangle$$

$$C_n^{\text{intra}} = \langle n_a^2 \rangle - \langle n_a \rangle^2 = \langle (\delta n_a)^2 \rangle$$



The atomic spin polarization effectively reduces the interaction between electrons in different orbitals to $U' - J_H = U - 3J_H$

$$U \sum_m \hat{n}_{m\uparrow} \hat{n}_{m\downarrow} + U' \sum_{m \neq m'} \hat{n}_{m\uparrow} \hat{n}_{m'\downarrow} + (U' - J_H) \sum_{m < m', \sigma} \hat{n}_{m\sigma} \hat{n}_{m'\sigma}$$

$$U' = U - 2J_H$$

Fanfarillo & EB, arXiv:1501.04607

The model: Degenerate orbitals with density-density interactions

- Multi-orbital systems with **N orbitals** ($N=2-5$) and n electrons (half-filling $n=N$)
- **Equivalent orbitals**: No crystal field splitting or hybridization between orbitals
Hopping to 1st nearest neighbors equal for all the orbitals
Non-interacting bandwidth W (2D but generic results)

*Intra-orbital
repulsion*

*Inter-orbital
Repulsion
(different spin)*

*Inter-orbital
Repulsion
(same spin)*

$$U \sum_m \hat{n}_{m\uparrow} \hat{n}_{m\downarrow} + U' \sum_{m \neq m'} \hat{n}_{m\uparrow} \hat{n}_{m'\downarrow} + (U' - J_H) \sum_{m < m', \sigma} \hat{n}_{m\sigma} \hat{n}_{m'\sigma}$$

$U' = U - 2J_H \longrightarrow U, J_H$ two interaction parameters $\max J_H/U = 1/3$

- Hamiltonian solved with Slave Spin Technique: Z, Charge & Spin fluctuations

Hubbard-Kanamori hamiltonian

$$\begin{aligned} H_{\text{int}} &= U \sum_a n_{a\uparrow} n_{a\downarrow} + (U' - J_H) \sum_{a < b, \sigma} n_{a\sigma} n_{b\sigma} \\ &+ U' \sum_{a \neq b} n_{a\uparrow} n_{b\downarrow} - J_H \sum_{a \neq b} c_{a\uparrow}^\dagger c_{a\downarrow} c_{b\downarrow}^\dagger c_{b\uparrow} \\ &+ J' \sum_{a \neq b} c_{a\uparrow}^\dagger c_{a\downarrow}^\dagger c_{b\downarrow} c_{b\uparrow} \end{aligned}$$

This terms are neglected
in our calculation
(Ising approx)

$$U' = U - 2J_H$$

Z₂- Slave spin technique

$$H = U \sum_m \hat{n}_{m\uparrow} \hat{n}_{m\downarrow} + U' \sum_{m \neq m'} \hat{n}_{m\uparrow} \hat{n}_{m'\downarrow} + (U' - J_H) \sum_{m < m', \sigma} \hat{n}_{m\sigma} \hat{n}_{m'\sigma}$$

$$n_{m\sigma} = d_{m\sigma}^\dagger d_{m\sigma}$$

Physical states

$d_{i\sigma}$	↗	Auxiliary fermion $f_{i\sigma}$	$ n_{i\sigma}^d = 1\rangle \Leftrightarrow n_{i\sigma}^f = 1, S_{i\sigma}^z = +1/2\rangle,$
	↘	Pseudospin variable (slave-spin) $S_{i\sigma}$	$ n_{i\sigma}^d = 0\rangle \Leftrightarrow n_{i\sigma}^f = 0, S_{i\sigma}^z = -1/2\rangle.$

Unphysical states

Constraint

$$\begin{array}{l} |n_{i\sigma}^f = 0, S_{i\sigma}^z = +1/2\rangle \\ |n_{i\sigma}^f = 1, S_{i\sigma}^z = -1/2\rangle \end{array} \longrightarrow f_{i\sigma}^\dagger f_{i\sigma} = S_{i\sigma}^z + \frac{1}{2}$$

de Medici et al, PRB 72, 205124 (2005)
Hassan & de Medici, PRB 81, 035106 (2010)

Z₂- Slave spin technique

$$d_{i\sigma} = f_{i\sigma} O_{i\sigma}, \quad d_{i\sigma}^\dagger = f_{i\sigma}^\dagger O_{i\sigma}^\dagger, \quad \text{For non-diagonal operators}$$

$$O_{i\sigma} = \begin{pmatrix} 0 & c_{i\sigma} \\ 1 & 0 \end{pmatrix} \rightarrow c = \frac{1}{\sqrt{n(1-n)}} - 1.$$

$$H_0 = - \sum_m t_m \sum_{\langle ij \rangle, \sigma} O_{im\sigma}^\dagger O_{jm\sigma} (f_{im\sigma}^\dagger f_{jm\sigma} + h.c.) + \sum_{i,m\sigma} (\epsilon_m - \mu) f_{im\sigma}^\dagger f_{im\sigma}$$

$$\frac{U}{2} \sum_i \left(\sum_{m,\sigma} S_{im\sigma}^z \right)^2 + \frac{U'}{2} \sum_i \left(\sum_{m,\sigma} S_{im\sigma}^z \right)^2 + J \sum_{i,m} \left(\sum_{\sigma} S_{im\sigma}^z \right)^2 - \frac{J}{2} \sum_{i,\sigma} \left(\sum_m S_{im\sigma}^z \right)^2$$

$$H_{int} [\{ \vec{S}_{im\sigma} \}]$$

de Medici et al, PRB 72, 205124 (2005)
Hassan & de Medici, PRB 81, 035106 (2010)

Z₂- Slave spin technique

- Constraint treated on average with static and site independent Lagrange multiplier λ_m . Spin variables and auxiliary fermions are decoupled

$$H_{eff}^f = - \sum_m t_m^{eff} \sum_{\langle ij \rangle, \sigma} (f_{im\sigma}^\dagger f_{jm\sigma} + h.c.)$$

$$+ \sum_{i, m\sigma} (\epsilon_m - \mu - \lambda_m) f_{im\sigma}^\dagger f_{im\sigma}$$

$$H_{eff}^S = - \sum_m J_m^{eff} \sum_{\langle ij \rangle, \sigma} O_{im\sigma}^\dagger O_{jm\sigma}$$

$$+ \sum_{i, m\sigma} \lambda_m (S_{im\sigma}^z + \frac{1}{2}) + H_{int}[\{\vec{S}_{im\sigma}\}]$$

$$t_m^{eff} = t_m \langle O_{im\sigma}^\dagger O_{jm\sigma} \rangle$$

$$J_m^{eff} = t_m (f_{im\sigma}^\dagger f_{jm\sigma} + f_{jm\sigma}^\dagger f_{im\sigma})$$

de Medici et al, PRB 72, 205124 (2005)
Hassan & de Medici, PRB 81, 035106 (2010)

Z₂- Slave spin technique

- Spin hamiltonian treated at a single site mean field level

$$H_{eff}^f = \sum_{\mathbf{k}, m\sigma} (Z_m \epsilon_{\mathbf{k}m} + \epsilon_m - \mu - \lambda_m) f_{\mathbf{k}m\sigma}^\dagger f_{\mathbf{k}m\sigma}$$

$$H_s = \sum_{m\sigma} h_m O_{m\sigma}^\dagger + \sum_{m\sigma} \lambda_m (S_{m\sigma}^z + \frac{1}{2}) + H_{int}[\vec{S}_{m\sigma}]$$

$$h_m = \langle O_{im\sigma} \rangle \frac{1}{\mathcal{N}} \sum_{\mathbf{k}} \epsilon_{\mathbf{k}m} \langle f_{\mathbf{k}m\sigma}^\dagger f_{\mathbf{k}m\sigma} \rangle$$

$$Z_m = \langle O_{im\sigma}^\dagger \rangle^2$$

- Solve self-consistently both coupled equations to calculate λ_m , h_m , Z_m

de Medici et al, PRB 72, 205124 (2005)
Hassan & de Medici, PRB 81, 035106 (2010)