

Ellipsometric Selective Sensitivity to Magnetic Nanostructures

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Recently, we have shown that the approach of depth sensitivity of magneto-optic ellipsometry can be generalized to selectivity from different materials in nanostructures. We use the condition number as the figure of merit to quantify the magneto-optic selectivity to two different magnetic contributions in magnetic nanostructure. The method is demonstrated on nanostructures containing magnetically hard Fe particles in surface layer of soft FeNbB amorphous ribbon. We separated both magnetic contributions from measurement of hysteresis loops using magneto-optic Kerr effect in longitudinal configuration. Magneto-optic selectivity is discussed and theoretical model on the basis of effective medium is compared with experimental data of longitudinal magneto-optic Kerr effect depending on angle of incidence.

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1. Introduction

Magnetic information included in the magneto-optic (MO) Kerr effect can be detected either using the Kerr rotation θ_K or the Kerr ellipticity ϵ_K . Both quantities are represented by the complex MO Kerr effect $\Phi_K = \theta_K + i\epsilon_K$. When we have two magnetization contributions m_1, m_2 in material, then the total MO response is in very good approximation the sum of the contributions from particular magnetizations $\Phi_{\text{tot}} = \Phi_1 + \Phi_2$ [1]. The measured polar MO Kerr rotation θ_{tot} and ellipticity ϵ_{tot} can be expressed as weight sum of normalized particular magnetizations $m_1 = M_1/M_{S1}$, $m_2 = M_2/M_{S2}$, where $M_{S1,2}$ are corresponding saturated magnetizations [2]:

$$\Phi_{\text{tot}} = \begin{bmatrix} \theta_{\text{tot}} \\ \epsilon_{\text{tot}} \end{bmatrix} = \begin{bmatrix} a_1 & a_2 \\ b_1 & b_2 \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \end{bmatrix} = \mathbf{A}\mathbf{M}. \quad (1)$$

If we determine the elements of the matrix \mathbf{A} , we can obtain both magnetic contributions using the matrix inversion $\mathbf{M} = \mathbf{A}^{-1}\Phi$ [2].

2. Theory

When we measure MO effect Φ with the tolerance $\Delta\Phi$, then nominal error of magnetic contribution is proportional to the condition number $\kappa(\mathbf{A})$ [3]:

$$\frac{\|\Delta\mathbf{M}\|}{\|\mathbf{M}\|} \leq \kappa(\mathbf{A}) \frac{\|\Delta\Phi\|}{\|\Phi\|}, \quad (2)$$

$$\kappa(\mathbf{A}) = \|\mathbf{A}^{-1}\| \|\mathbf{A}\|, \quad (3)$$

where $\|\mathbf{A}\|$ is the norm of the matrix \mathbf{A} . In our calculations we used the spectral norm [3].

To express the condition number analytically we express Φ_1 and Φ_2 as $\Phi_1 = |\Phi_1| \exp(i\alpha_0)$ and $\Phi_2 = |\Phi_2| \exp[i(\alpha_0 + \Delta\alpha)]$. This we can visualize in the $\theta\epsilon$ plane in Fig. 1a [4]. Then we can write matrix \mathbf{A} :

$$\mathbf{A} = |\Phi_1| \begin{pmatrix} \cos \alpha_0 & k \cos(\alpha_0 + \Delta\alpha) \\ \sin \alpha_0 & k \sin(\alpha_0 + \Delta\alpha) \end{pmatrix}. \quad (4)$$

Then the condition number is only function of angle $\Delta\alpha$ between vectors Φ_1 and Φ_2 and the ratio $k = |\Phi_2|/|\Phi_1|$ of absolute values of vectors $|\Phi_2|, |\Phi_1|$

$$\kappa(\mathbf{A}) = \frac{1}{2k|\sin \Delta\alpha|} \times \left(1 + k^2 + \sqrt{(k^2 - 1)^2 + 4k^2 \cos^2 \Delta\alpha} \right). \quad (5)$$

Figure 1b shows dependence of the condition number $\kappa(\mathbf{A})$ from Eq. (5) on the parameters $\Delta\alpha$ and k . We see that we can obtain reasonable small condition number if parameter k is not too different from 1 and vectors Φ_1 and Φ_2 are not collinear.

Then we can separate magnetization contributions of one material from two different depths [5, 6] but also magnetization contributions from two different materials [2, 7, 8].

3. Experimental results

We can demonstrate this e.g. for magnetically hard Fe particles in surface layer of soft FeNbB amorphous ribbons [9]. On wheel side of Fe_{80.5}Nb_{6.9}B_{12.6} ribbon MO hysteresis loops in longitudinal configuration were measured [9, 10]. Similar loops measured at different angle of incidence (65°) are presented in Fig. 2a. The loops confirm that the near-surface region is inhomogeneous and contains contribution of different phases [10]. Transmission electron microscopy (TEM) measurements show the

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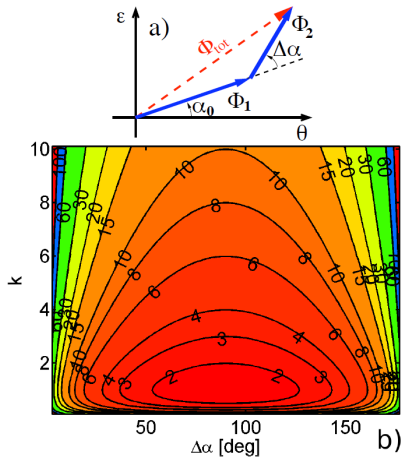


Fig. 1. (a) MO contributions Φ_1 , Φ_2 to the total MO effect Φ_{tot} displayed in θ, ϵ plane. (b) Dependence of condition number $\kappa(\mathbf{A})$ of 2×2 matrix \mathbf{A} of two column vectors Φ_1 , Φ_2 on angle $\Delta\alpha$ between the vectors and parameter k corresponding to the ratio of absolute values $|\Phi_1|, |\Phi_2|$. See Eq. (5).

α -Fe crystallites with average size of grains about 100 nm situated near the wheel surface, Fig. 2b. By rotating of vector Φ_{tot} with respect to the θ and ϵ axes we separated two different phases showed in Fig. 2c,d from measured loops in Fig. 2a. The corresponding matrix \mathbf{A} and the condition number $\kappa(\mathbf{A})$ are

$$\mathbf{A}_{exp} = \begin{pmatrix} -0.26 & -0.28 \\ -0.12 & 0.19 \end{pmatrix}, \quad \kappa(\mathbf{A}_{exp}) = 1.8. \quad (6)$$

We suppose that the hard magnetic phase corresponds to the α -Fe crystallites and the soft one corresponds to the amorphous FeNbB. The small value of the condition number $\kappa(\mathbf{A}_{exp})$ shows that the magnetic contributions are well separable.

Theoretically we describe the structure as spherical Fe particles with different size in amorphous bulk FeNbB. We calculated effective permittivity tensor using the Maxwell-Garnett approximation for anisotropic particles inserted in anisotropic medium [11]. For Fe particles we used optical and MO constants from [12, 13] and for bulk FeNbB the optical and MO constants from [9]. We supposed that the Fe volume fraction f decreases exponentially with depth in amorphous material according to the function

$$f = f_0 \exp(-d/\Delta d). \quad (7)$$

On the surface we supposed an oxidation layer with refractive index $n = 2.1$ (the refractive index of Nb_2O_5 [14]).

Using Yeh's matrix formalism [15], we calculated contribution Φ_{tot} and separately both magnetic contributions Φ_1 and Φ_2 to the longitudinal MO Kerr effect at wavelength of incident light 670 nm for angle of incidence varying from 0° to 90° . We fitted parameters f_0 , Δd and thickness of surface oxidation layer t_s to the ex-

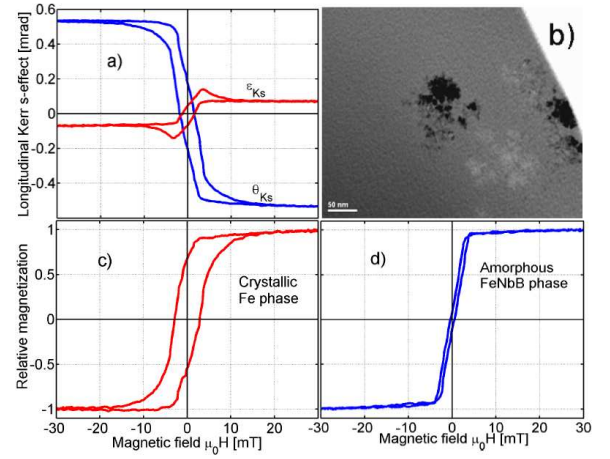


Fig. 2. (a) Sketch of the MO longitudinal Kerr rotation θ_{Ks} and ellipticity ϵ_{Ks} measured on wheel side of FeNbB ribbon for incident s -polarized wave at wavelength 670 nm and angle of incidence 65° . (b) Transmission electron microscopy on wheel side of the FeNbB ribbon. Dark and light areas show the crystalline α -Fe phase. (c), (d) Hysteresis loops of the crystalline Fe phase and the amorphous FeNbB phase separated from data in (a), respectively.

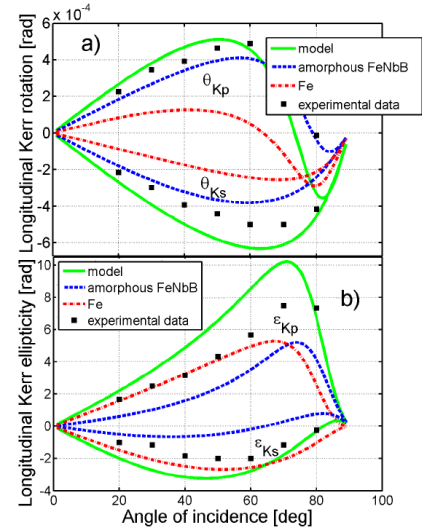


Fig. 3. Calculated dependence of longitudinal Kerr effect: (a) rotation, (b) ellipticity on angle of incidence for spherical Fe particles in homogeneous FeNbB material. The wavelength of incident light is 670 nm. The contributions from Fe and from FeNbB are also shown separately. The model is compared with experimental data from [9] (square dots).

perimental data from [9] (Fig. 3). We obtained $f_0 = 0.8$, $\Delta d = 7$ nm and $t_s = 7$ nm. Further we confirmed that $\Phi_{tot} = \Phi_1 + \Phi_2$. For incident s -polarization wave at angle of incidence 65° we calculated from Φ_1 and Φ_2 according to (1) matrix

$$\mathbf{A}_{\text{eff}} = \begin{pmatrix} -0.25 & -0.37 \\ -0.23 & 0.004 \end{pmatrix}, \quad \kappa(\mathbf{A}_{\text{eff}}) = 2.5.$$

The matrix \mathbf{A}_{eff} and corresponding condition number $\kappa(\mathbf{A}_{\text{eff}})$ obtained from model corresponds reasonably good with \mathbf{A}_{exp} and $\kappa(\mathbf{A}_{\text{exp}})$ (6) obtained from the experiment. The difference occurs because our model does not involve relatively big surface roughness, complicated shape of Fe crystallites and the fact that the structure of amorphous FeNbB bulk inside the ribbon can differ from the material filling space among Fe crystallites. Nevertheless, reasonably good agreement shows us that both contributions to the magnetization (from Fe particles and from amorphous FeNbB) are well separable and that we can use introduced model to describe the structure of wheel side of FeNbB ribbons.

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