

Energy Dependence of Multiplicity Fluctuations in Heavy Ion Collisions

Benjamin Lungwitz*, Fachbereich Physik der Universität, Frankfurt, Germany.

E-mail: lungwitz@ikf.uni-frankfurt.de

for the NA49 Collaboration

C. Alt⁹, T. Anticic²³, B. Baatar⁸, D. Barna⁴, J. Bartke⁶, L. Betev¹⁰, H. Białkowska²⁰,
C. Blume⁹, B. Boimska²⁰, M. Botje¹, J. Bracinik³, R. Bramm⁹, P. Bunčić¹⁰, V. Cerny³,
P. Christakoglou², P. Chung¹⁹, O. Chvala¹⁴, J.G. Cramer¹⁶, P. Csató⁴, P. Dinkelaker⁹,
V. Eckardt¹³, D. Flierl⁹, Z. Fodor⁴, P. Foka⁷, V. Friese⁷, J. Gál⁴, M. Gaździcki^{9,11},
V. Genchev¹⁸, G. Georgopoulos², E. Gładysz⁶, K. Grebieszko²², S. Hegyi⁴,
C. Höhne⁷, K. Kadija²³, A. Karev¹³, D. Kikola²², M. Kliemant⁹, S. Kniege⁹,
V.I. Kolesnikov⁸, E. Kornas⁶, R. Korus¹¹, M. Kowalski⁶, I. Kraus⁷, M. Kreps³,
A. Laszlo⁴, R. Lacey¹⁹, M. van Leeuwen¹, P. Lévai⁴, L. Litov¹⁷, B. Lungwitz⁹,
M. Makariev¹⁷, A.I. Malakhov⁸, M. Mateev¹⁷, G.L. Melkumov⁸, A. Mischke¹,
M. Mitrovski⁹, J. Molnár⁴, St. Mrówczyński¹¹, V. Nolic²³, G. Pála⁴,
A.D. Panagiotou², D. Panayotov¹⁷, A. Petridis², W. Peryt²², M. Pikna³, J. Pluta²²,
D. Prindle¹⁶, F. Pühlhofer¹², R. Renfordt⁹, C. Roland⁵, G. Roland⁵, M. Rybczyński¹¹,
A. Rybicki^{6,10}, A. Sandoval⁷, N. Schmitz¹³, T. Schuster⁹, P. Seyboth¹³, F. Siklér⁴,
B. Sitar³, E. Skrzypczak²¹, M. Slodkowski²², G. Stefanek¹¹, R. Stock⁹, C. Strabel⁹,
H. Ströbele⁹, T. Susa²³, I. Szentpétery⁴, J. Sziklai⁴, M. Szuba²², P. Szymanski^{10,20},
V. Trubnikov²⁰, D. Varga^{4,10}, M. Vassiliou², G.I. Veres^{4,5}, G. Vesztegombi⁴,
D. Vranić⁷, A. Wetzler⁹, Z. Włodarczyk¹¹, A. Wojtaszek¹¹, I.K. Yoo¹⁵, J. Zimányi⁴

- ¹NIKHEF, Amsterdam, Netherlands.
²Department of Physics, University of Athens, Athens, Greece.
³Comenius University, Bratislava, Slovakia.
⁴KFKI Research Institute for Particle and Nuclear Physics, Budapest, Hungary.
⁵MIT, Cambridge, USA.
⁶Institute of Nuclear Physics, Cracow, Poland.
⁷Gesellschaft für Schwerionenforschung (GSI), Darmstadt, Germany.
⁸Joint Institute for Nuclear Research, Dubna, Russia.
⁹Fachbereich Physik der Universität, Frankfurt, Germany.
¹⁰CERN, Geneva, Switzerland.
¹¹Institute of Physics Świętokrzyska Academy, Kielce, Poland.
¹²Fachbereich Physik der Universität, Marburg, Germany.
¹³Max-Planck-Institut für Physik, Munich, Germany.
¹⁴Institute of Particle and Nuclear Physics, Charles University, Prague, Czech Republic.
¹⁵Department of Physics, Pusan National University, Pusan, Republic of Korea.
¹⁶Nuclear Physics Laboratory, University of Washington, Seattle, WA, USA.
¹⁷Atomic Physics Department, Sofia University St. Kliment Ohridski, Sofia, Bulgaria.
¹⁸Institute for Nuclear Research and Nuclear Energy, Sofia, Bulgaria.
¹⁹Department of Chemistry, Stony Brook Univ. (SUNYSB), Stony Brook, USA.
²⁰Institute for Nuclear Studies, Warsaw, Poland.
²¹Institute for Experimental Physics, University of Warsaw, Warsaw, Poland.
²²Faculty of Physics, Warsaw University of Technology, Warsaw, Poland.
²³Rudjer Boskovic Institute, Zagreb, Croatia.

The energy dependence of multiplicity fluctuations was studied for the most central $Pb + Pb$ collisions at 20A, 30A, 40A, 80A and 158A GeV by the NA49 experiment at the CERN SPS. The multiplicity distribution for negatively and positively charged hadrons is significantly narrower than Poisson one for all energies. No significant structure in energy dependence of the scaled variance of multiplicity fluctuations is observed. The measured scaled variance is lower than the one predicted by the grand-canonical formulation of the hadron-resonance gas model. The results for scaled variance are in approximate agreement with the string-hadronic model UrQMD.

Correlations and Fluctuations in Relativistic Nuclear Collisions
July 7-9 2006
Florence, Italy

*Speaker.

1. Introduction

At high energy densities ($\approx 1 \text{ GeV}/\text{fm}^3$) a phase transition from hadron gas to quark-gluon-plasma (QGP) is expected to occur. There are indications that at RHIC and top SPS energies quark-gluon-plasma is created at the early stage of heavy ion collisions [1, 2]. The energy dependence of various observables show anomalies at low SPS energies which might be related to the onset of deconfinement [3]. Lattice QCD calculations suggest furthermore the existence of a critical point in the phase diagram of strongly interacting matter which separates the line of the first order phase transition from a crossover. Models predict an increase of multiplicity fluctuations near the onset of deconfinement [4] or the critical point [7].

This motivates a vigorous experimental and theoretical study of multiplicity fluctuations in high energy nuclear collisions [5, 6]. In addition to the effects mentioned above also the “background” statistical fluctuations are interesting to study. In a grand-canonical statistical model scaled variance ω^1 is close to one. In the past it was commonly believed that the result of the grand-canonical, canonical and micro-canonical ensemble should be similar in the infinite volume limit, like it is for mean quantities. Recent calculations showed that this assumption is wrong. The scaled variance in the infinite volume limit is largest for the grand-canonical ensemble and smallest for the micro-canonical one [8, 9]. It is because the fluctuations in the canonical and micro-canonical ensembles are reduced by conservation laws and this reduction is, unlike for the mean, volume independent for $V \rightarrow \infty$.

The first preliminary results on the energy dependence of multiplicity fluctuations in central $Pb + Pb$ collisions at SPS energies were presented in this paper in order to look for experimental signatures of increased fluctuations due to a phase transition or the critical point and for the predicted reduction of fluctuations in relativistic hadron gas due to conservation laws.

2. The NA49 Experiment

The NA49 detector [10] (see figure 1) is a large acceptance fixed target hadron spectrometer. Its main devices are four large time projection chambers (TPCs). Two of them, called vertex TPCs, are located in two superconducting dipole magnets with a total bending power of 7.8 Tm. The other two TPCs are installed behind the magnets left and right of the beam line allowing precise particle tracking in the high density region of heavy ion collisions. The measurement of the energy loss dE/dx allows particle identification and a good rejection of electrons in a large momentum regime.

A large variety of different colliding systems was studied. Beams of p and Pb are available at the CERN SPS directly, C and Si beams were produced via fragmentation of the primary Pb beam. Targets of liquid hydrogen or solid foils of different materials were used. Data on central $Pb + Pb$ collisions at 20A, 30A, 40A, 80A and 158A GeV were recorded and analysed for this analysis.

¹a commonly used measure of fluctuations, $\omega = \frac{\text{Var}(n)}{\langle n \rangle}$, where $\text{Var}(n)$ and $\langle n \rangle$ are variance and mean of multiplicity distributions, respectively.

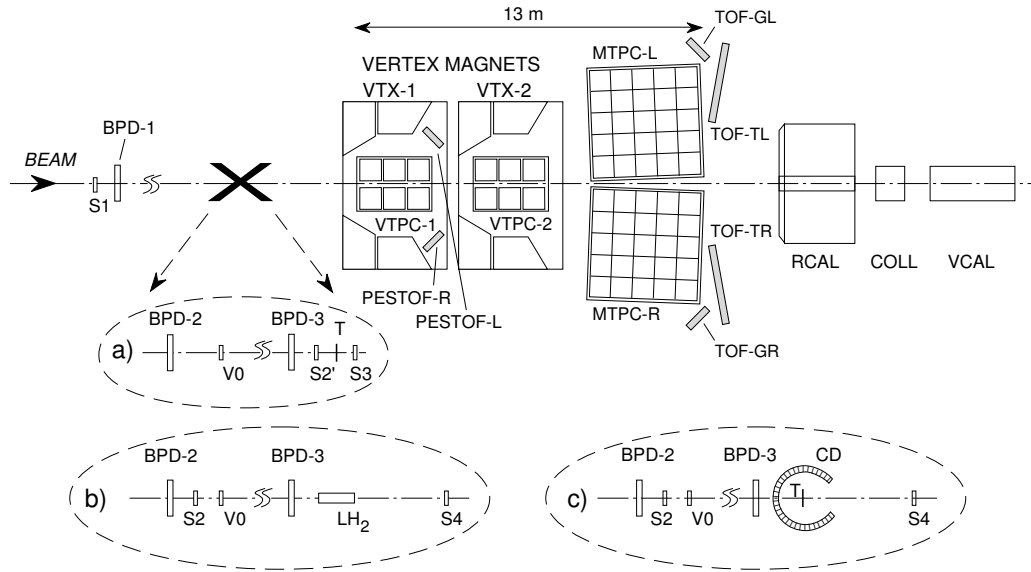


Figure 1: Setup of the NA49 experiment and different target configurations, a) for $Pb + Pb$, b) for $p + p$ and c) for $p + A$ collisions.

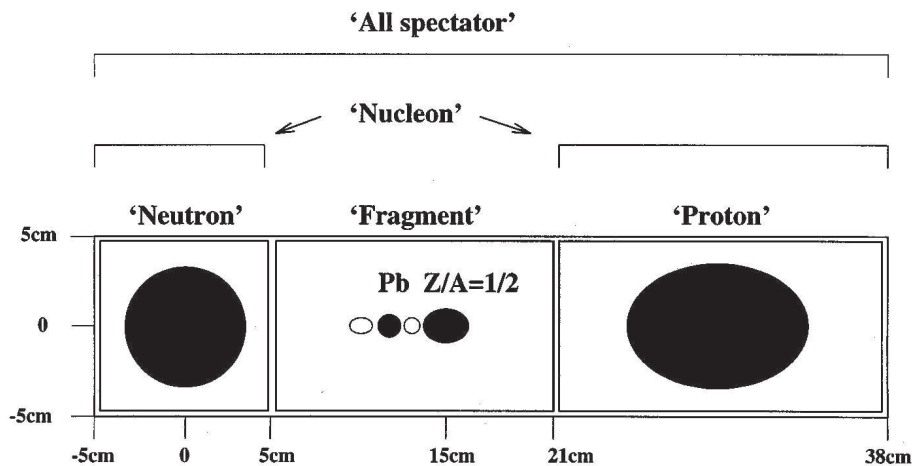


Figure 2: Collimator in front of the Veto calorimeter at 158A GeV [11].

2.1 Centrality Determination

The downstream veto calorimeter, originally designed for NA5, allows a determination of the centrality of a collision by measuring the energy in the projectile spectator region [11]. A collimator is located 25 m downstream from the target and is adjusted for each energy in such a way that all projectile spectator protons, neutrons and fragments can reach the veto calorimeter. For 158A GeV the hole in the collimator is with respect to the beam axis ± 5 cm in vertical direction and -5 cm and $+38$ cm in horizontal direction taking into account the deflection of charged particles by the magnetic field (figure 2). For 40A and 80A GeV the hole is ± 12 cm in vertical and -13 cm respectively $+47$ cm in horizontal direction. For 20A and 30A GeV the ring calorimeter with a

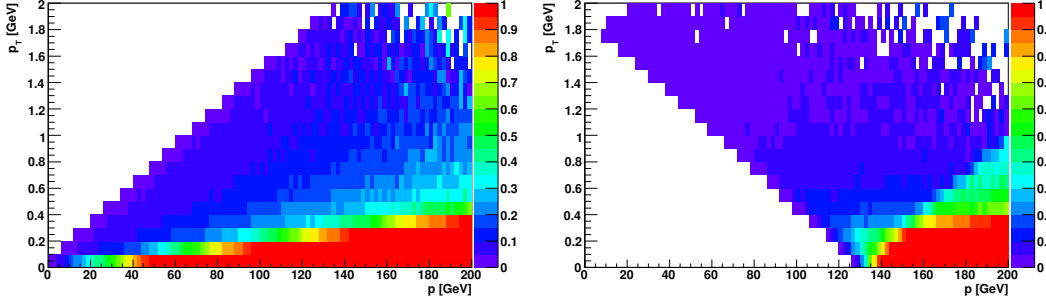


Figure 3: Acceptance of the Veto calorimeter for neutral (left) and positively charged (right) main vertex particles at 158A GeV as a function of total momentum p and transverse momentum p_T .

hole of radius 28 cm and positioned 18 m away from the target and 10 cm away from beam axis in horizontal direction is used as a collimator. For higher energies the ring calorimeter is positioned 17 cm off in horizontal direction and has only a small influence on the acceptance of the veto calorimeter.

For the following analysis the collisions are selected according to their energy in the veto calorimeter. A large fraction of the Veto energy is due to projectile spectators. However also a fraction of non-spectator particles, mostly protons and neutrons, contribute to Veto energy. The acceptance of the Veto calorimeter at 158A GeV is shown in figure 3 for neutral and positively charged particles.

The centrality C of an event with a veto energy E_{Veto} can be calculated using the known trigger centrality $C_{trig} = \frac{\sigma_{trig}}{\sigma_{inel}}$ and the veto energy distribution as:

$$C = \frac{\sigma_{E_{Veto}}}{\sigma_{inel}} = C_{trig} \cdot \frac{\int_0^{E_{Veto}} dN/dE_{Veto,trig}}{\int_0^{\infty} dN/dE_{Veto,trig}} \quad (2.1)$$

where $dN/dE_{Veto,trig}$ is the Veto energy distribution for a given trigger.

2.2 Track Selection

Since detector effects like track reconstruction efficiency might have a large influence on multiplicity fluctuations, it is important to select a very clean track sample for the analysis (figure 4). Therefore the acceptance for this analysis is limited to a part of the forward hemisphere, where the NA49 detector has the highest tracking efficiency. This was done by restricting the analysis to the rapidity interval $1 < y(\pi) < y_{beam}$ ² for 20A to 80A GeV and $1.08 < y(\pi) < 2.57$ for 158A GeV³. In addition a cut on transverse momentum according to [13] was applied, which is dependent both on rapidity and azimuthal angle. This ensures that only tracks with sufficient points both in the vertex TPC 2 and in one of the main TPCs are used. For them the reconstruction efficiency is larger than 98%. The disadvantage of this track selection is that the fraction of accepted tracks is small and depends on collision energy, see figure 5.

²Rapidity is calculated in the center of mass system assuming pion mass.

³A different rapidity cut is used for this energy because of missing geometrical acceptance near beam rapidity [14].

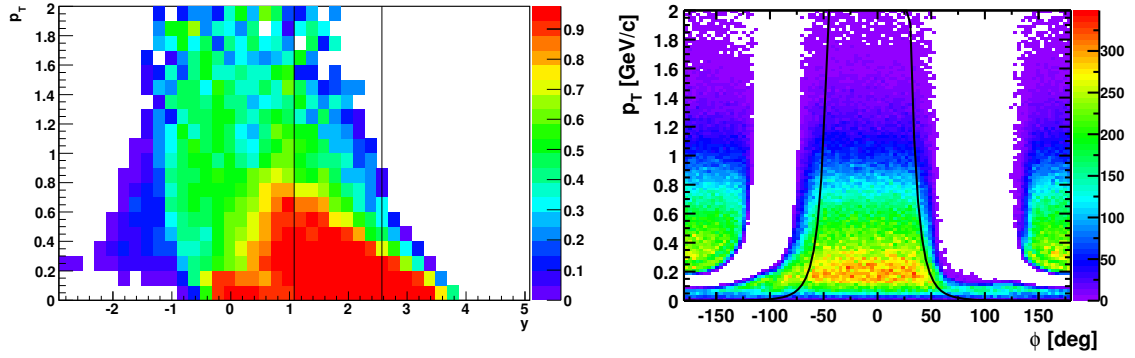


Figure 4: Acceptance for negative hadrons at 158A GeV as a function of rapidity (pion mass assumed) and p_T (left), as well as a function of ϕ and p_T ($1.4 < y < 1.6$, right).

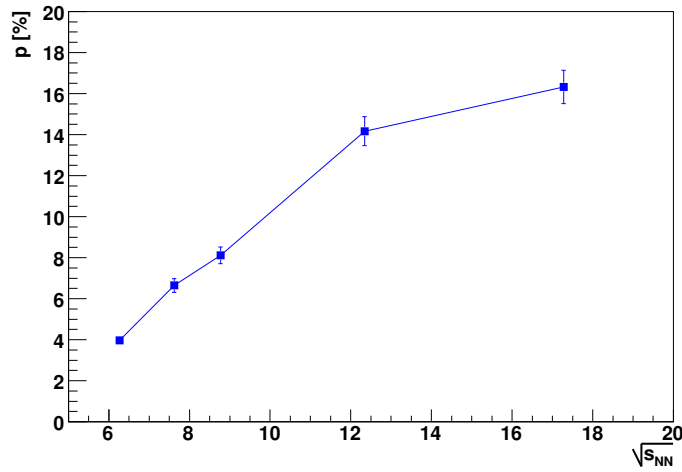


Figure 5: Acceptance for negative hadrons as a function of collision energy calculated using Venus model and GEANT detector simulation. The acceptance was also estimated using the ratio of measured multiplicity of negatively charged hadrons to the published or preliminary NA49 total π^- and K^- yields, the difference ($< 5\%$) is shown by vertical error bars.

A cut on the distance between the interaction point and the track trajectory extrapolated to the target is used to reduce the background of secondary particles originating from weak decays (track impact parameter)⁴. Removing this cut would change the scaled variance by less than 2%.

A cut on the energy loss of particles in the detector gas (dE/dx) removes electrons and allows the study of hadron multiplicity fluctuations only. The scaled variance will be less than 2% different if this cut is removed.

3. Fluctuation Analysis

The multiplicity distribution in central (7 – 10%) $Pb + Pb$ collisions at 158A GeV is shown in

⁴The difference has to be smaller than 4 cm orthogonal and 2 cm parallel to the magnetic field direction.

figure 6. The measured distribution is significantly narrower than a Poisson one.

The basic measure of multiplicity fluctuations used in this analysis is the scaled variance:

$$\omega = \frac{\text{Var}(n)}{\langle n \rangle} \quad (3.1)$$

where $\text{Var}(n)$ and $\langle n \rangle$ are variance and mean of multiplicity distributions, respectively.

The scaled variance for positively ($\omega(h^+)$), negatively ($\omega(h^-)$) and all charged hadrons ($\omega(h^\pm)$) will be presented. The scaled variance of a Poisson distribution is 1, independent of its mean multiplicity. A larger ω might indicate additional non-statistical fluctuations, a smaller ω might be a hint for a suppression of fluctuations e.g. due to conservation laws.

Figure 7 shows the centrality dependence of multiplicity fluctuations in $Pb + Pb$ collisions at different energies for central collisions. In general ω decreases with increasing centrality (i.e. decreasing Veto energy), this trend is stronger for higher energies.

The results for collisions selected by minimum bias and central on-line trigger are shown separately in figure 7 and they agree within errors. For further analysis the results for central data sets are used because of larger statistics in comparison to the minimum bias data sets.

3.1 Experimental Biases

In superposition models (e.g. the Wounded Nucleon Model [12]) the total number of particles produced in a collision n is the sum of the number of particles produced by different independent particle production sources:

$$n = \sum_i n_{i,so} \quad (3.2)$$

In these models the scaled variance has two contributions. The first is due to the fluctuations of the number of particles emitted by a single source ω_{so} , the second is due to the fluctuations in the number of sources ω_k :

$$\omega = \omega_{so} + \langle n_{so} \rangle \cdot \omega_k \quad (3.3)$$

where $\langle n_{so} \rangle$ is the mean multiplicity of hadrons from a single source.

The number of sources related to projectile participants is fixed by fixing the energy detected in the Veto Calorimeter and consequently the number of projectile spectators (see chapter 2.1).

For very central collisions analysed here the Veto energy is dominated by the energy of forward going participants and not spectators. For these collisions the number of projectile participants is in good approximation fixed and independent of Veto energy. Therefore no correction for the finite width of the Veto energy bins is applied.

The finite resolution of the Veto calorimeter introduces additional fluctuations in N_p^{proj} even for a fixed Veto energy. For very central collisions their influence on the scaled variance is estimated to be small, in contrast to peripheral collisions. The data is not corrected for this effect, introducing a correction would reduce the scaled variance by less than 5%.

In the NA49 experiment the number of target participants N_p^{arg} is not fixed, it fluctuates substantially (see figure 8). These fluctuations might contribute even to multiplicity fluctuations in the forward hemisphere and increase the scaled variance [14, 16].

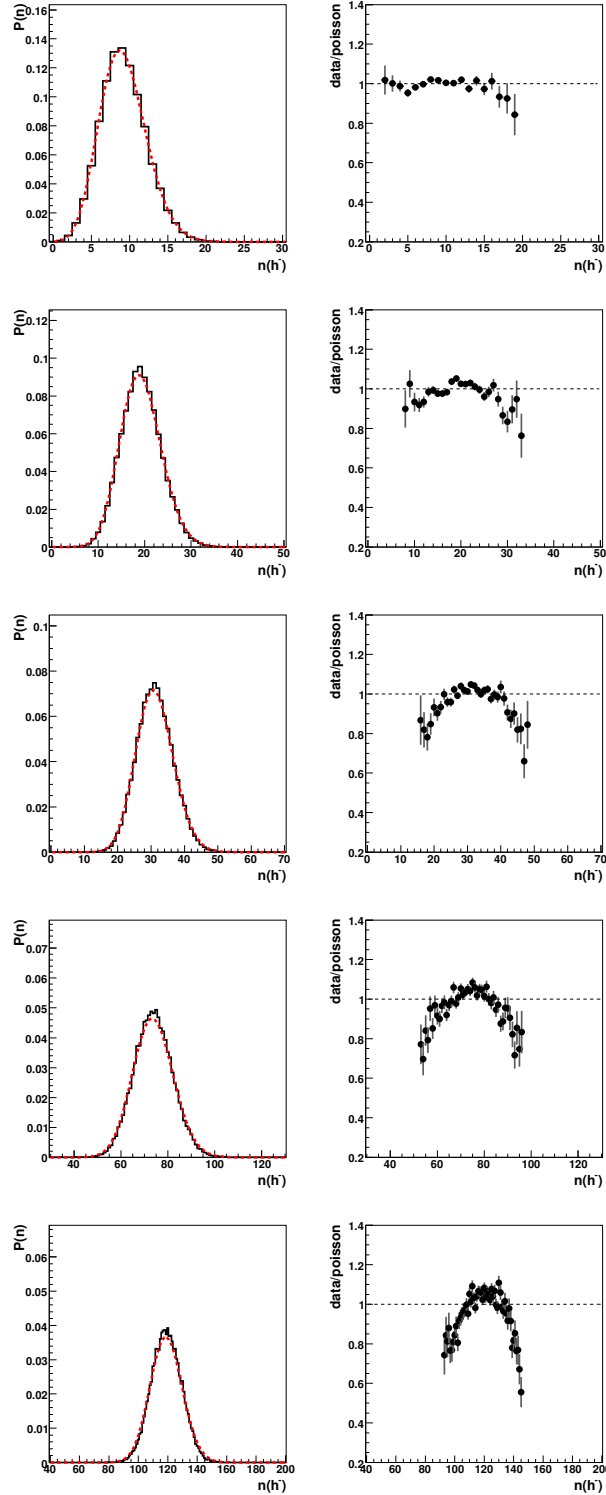


Figure 6: Left: multiplicity distribution of negative hadrons in central ($C < 1\%$) $Pb+Pb$ collisions from 20A (top) to 158A GeV (bottom). The red line indicates a Poisson distribution with the same mean multiplicity. Right: ratio of the measured multiplicity distribution over Poisson distribution. It is visible that the measured distribution is significantly narrower than the Poissonian one for all energies. Note that the multiplicity fluctuations are not corrected for the finite centrality bin width.

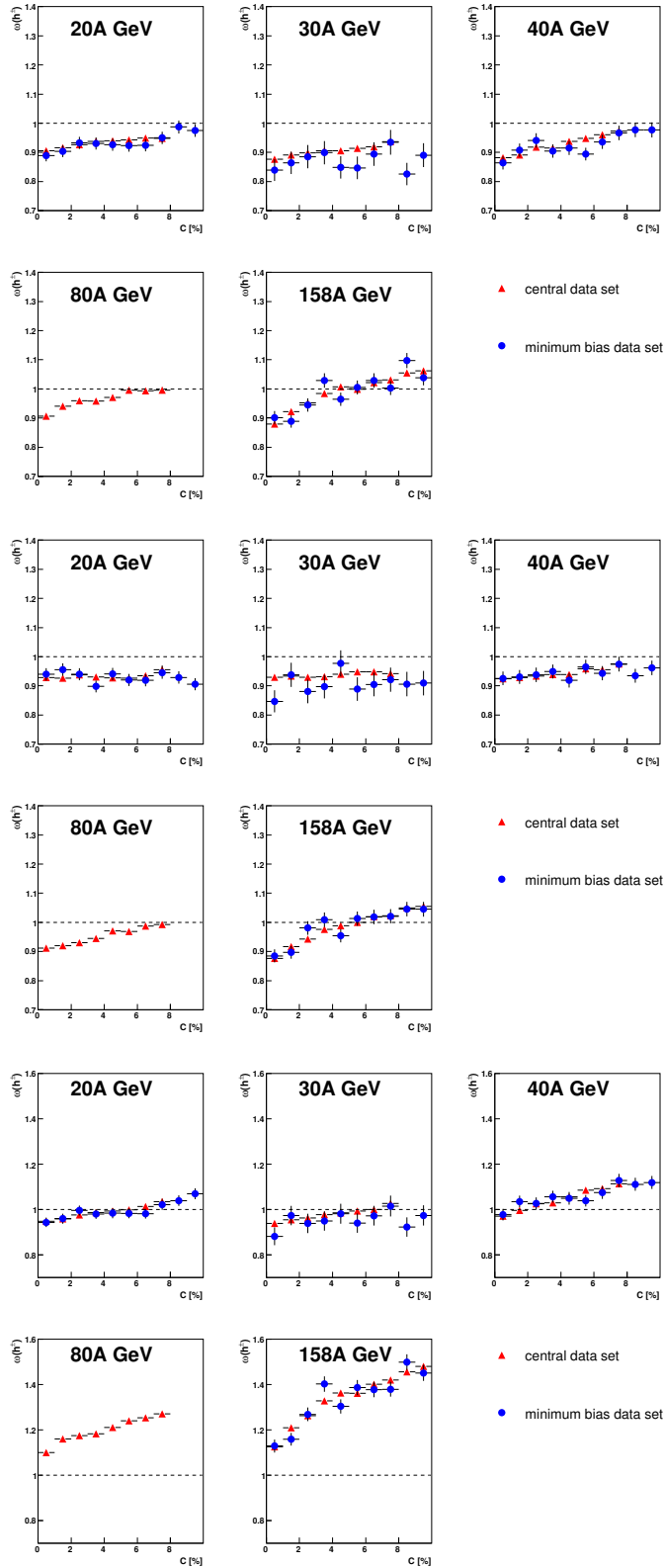


Figure 7: Centrality dependence of $\omega(h^+)$ (top), $\omega(h^-)$ (middle) and $\omega(h^\pm)$ (bottom) for $Pb+Pb$ collisions at different energies. $C < 1\%$ corresponds to the most central collisions. The shown centrality range of $C < 10\%$ corresponds approximately to number of projectile participants $N_p^{proj} > 160$. Only statistical errors are shown.

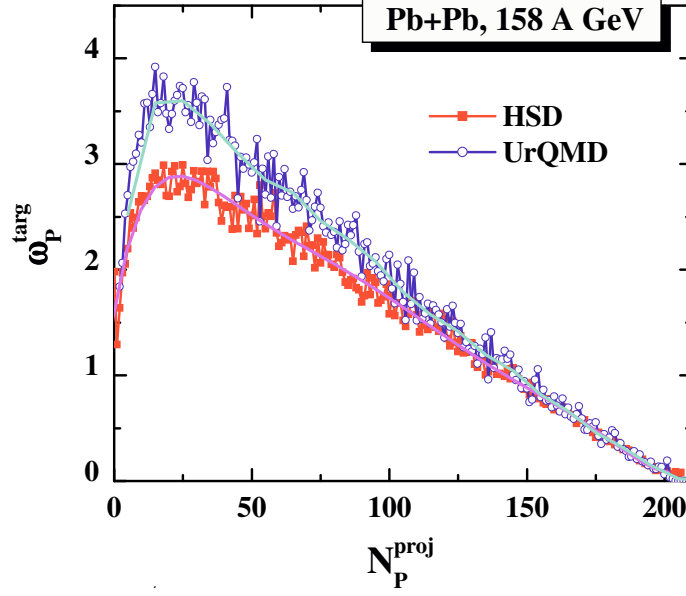


Figure 8: Fluctuations in the number of target participants for a fixed number of projectile participants in the UrQMD and HSD [15] models.

Model calculations (HSD, UrQMD) [15] show that the scaled variance of target participant fluctuations $\omega(N_P^{targ}) = \frac{\text{Var}(N_P^{targ})}{\langle N_P^{targ} \rangle}$ is small for central collisions, and thus the corresponding increase of the scaled variance of multiplicity distributions is also expected to be small.

In order to minimize the contribution due to both Veto calorimeter resolution and N_P^{targ} fluctuations further analysis was done for very central collisions ($C < 1\%$, which corresponds to $N_P^{proj} > 193$).

The systematic error is estimated taking into account the influence of the track impact parameter cut ($\pm 2\%$), the cut on electron rejection ($\pm 2\%$), the effect of finite resolution of the Veto calorimeter (-5%) and possible remaining participant fluctuations due to the finite width of the selected centrality bin (-5%). The total systematic error is estimated to be $\sigma_{\text{sys}} \approx \pm 5\%$.

Model calculations (Venus and UrQMD) show that for higher energies (80A and 158A GeV) the details of centrality selection have a significant effect on multiplicity fluctuations. When the centrality is determined by fixing the number of projectile spectators the scaled variance obtained by these models is up to 30% larger than the one obtained by fixing the energy in the Veto Calorimeter using a detailed simulation of its acceptance. For lower energies (20A- 40A GeV) no significant difference of the scaled variance for different centrality selections was observed.

4. Results and Discussion

The results on energy dependence of multiplicity fluctuations in $Pb + Pb$ collisions are shown in figure 9. It can be seen that at all energies the scaled variance for positively and negatively charged hadrons is smaller than 1, the value for a Poissonian distribution.

A model independent comparison of results at different energies is not possible because the acceptance is different for each energy (figure 5).

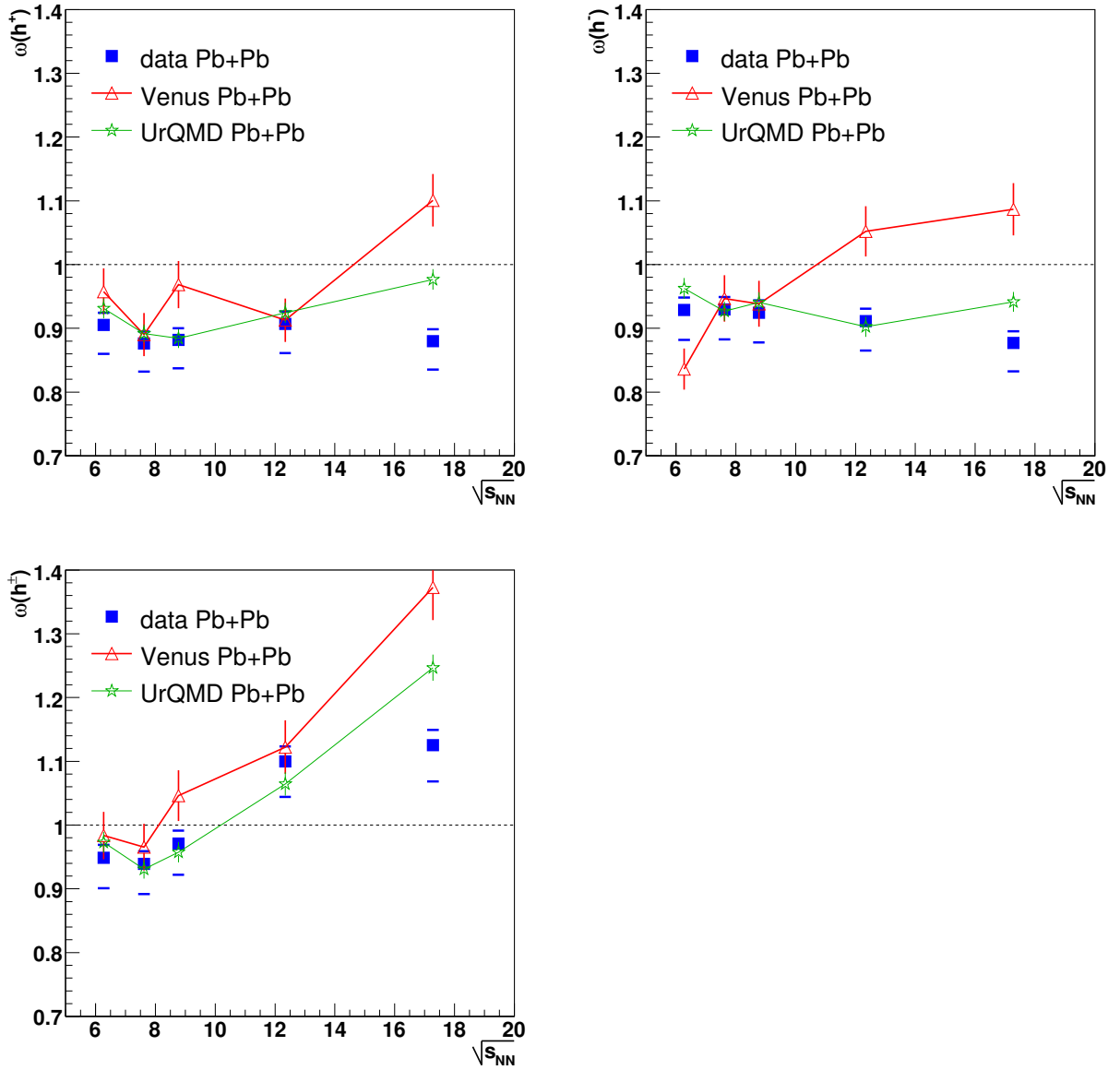


Figure 9: Energy dependence of multiplicity fluctuations in the most central ($C < 1\%$, Venus calculations: $C < 2\%$) $Pb + Pb$ collisions in comparison to string hadronic model (Venus and UrQMD) predictions for $\omega(h^+)$ (top left), $\omega(h^-)$ (top right) and $\omega(h^\pm)$ (bottom). Horizontal bars indicate systematic errors of data points.

The scaled variance for all charged hadrons is larger than the scaled variance for positively and negatively charged hadrons. This is probably due to the effect of resonance decays which correlated final state hadrons and thus leads to an increase of fluctuations. This effect is largest for all charged hadrons as the majority of resonances decay into one positively and one negatively charged daughter. It is smallest for negatively charged hadrons as only a very few resonances decay into two negatively charged hadrons (e.g. $\Delta^{--} \rightarrow \pi^- + p^-$).

The multiplicity fluctuations of all charged hadrons in $Pb + Pb$ collisions at the top SPS energy have been studied previously by WA98 [6]. A direct comparison of scaled variance of multiplicity distributions obtained in NA49 to the results of WA98 is not possible because of different experimental acceptance and centrality selection. The WA98 results were obtained in a pseudorapidity region around midrapidity ($2.35 \leq \eta \leq 3.75$), whereas the NA49 results are obtained in the forward hemisphere ($1.08 < y(\pi) < 2.57$). The centrality of the collisions in WA98 was determined by fixing transverse energy in a calorimeter located in the pseudorapidity interval $3.5 \leq \eta \leq 5.5$. In contrast in NA49 centrality is fixed using the energy in the forward Veto calorimeter (see section 2.1).

4.1 String- Hadronic Models

For a comparison of data to string hadronic models (Venus 4.12 [17] and UrQMD 1.3 [18]) the model predictions were calculated in the data acceptance. The centrality selection in the models is done in a similar way as in the data by a detailed simulation of the acceptance of the Veto Calorimeter.

The multiplicity distributions for negatively charged hadrons in data and models are compared in figure 10. In comparison to data the multiplicity distributions in Venus are shifted towards lower multiplicities, whereas in UrQMD they are shifted towards higher multiplicities.

Figure 9 shows a comparison of the scaled variance between data and the predictions of the Venus and UrQMD model. The Venus model overpredicts scaled variance for central $Pb + Pb$ collisions at most energies. In general the scaled variance obtained by the UrQMD model is in agreement with data. Only for $\omega(h^+)$ and $\omega(h^-)$ at 158A GeV as well as for $\omega(h^\pm)$ at 80A and 158A GeV the differences are significant.

4.2 Acceptance Dependence

Only a fraction of all produced particles is used for scaled variance determination in the experiment. A simple parametrisation of the acceptance dependence of ω would be useful for comparison of different energies and a comparison to models. In Appendix A a derivation of a simple formula describing the dependence of the scaled variance on the acceptance is given. It is obtained under the assumption that all particles are produced independently in momentum space. If a fraction p of all particles N_{tot} is accepted, the scaled variance ω is related to the scaled variance ω_{tot} in 4π as: $\omega = \frac{Var(N)}{\langle N \rangle} = 1 + p(\omega_{tot} - 1)$ (see equation A.7).

In figure 11 the fluctuations of negative hadrons for the five analysed energies are plotted as a function of the fraction of accepted tracks. If the simple acceptance dependence A.7 works and if the scaled variance in 4π is similar for all energies, the data points for all five energies should lie on a common straight line which starts at $\omega = 1$ for $p = 0$. It can be seen that the data seem to follow

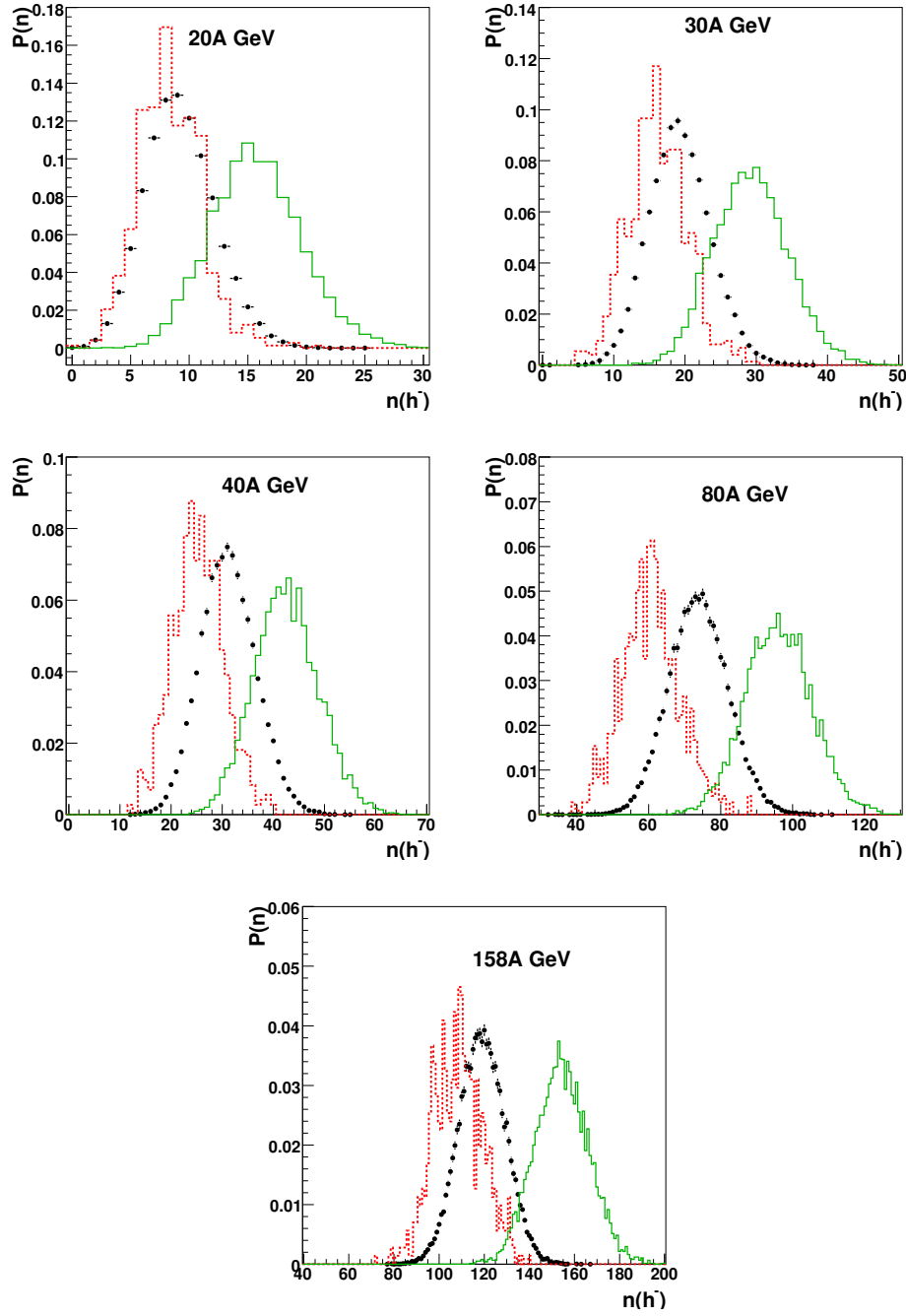


Figure 10: Multiplicity distributions of negatively charged hadrons in the most central ($C < 1\%$) $Pb + Pb$ collisions from 20A to 158A GeV; data - black circles, Venus model - dashed red line and UrQMD - solid green line. Note that the multiplicity fluctuations are not corrected for the finite centrality bin width.

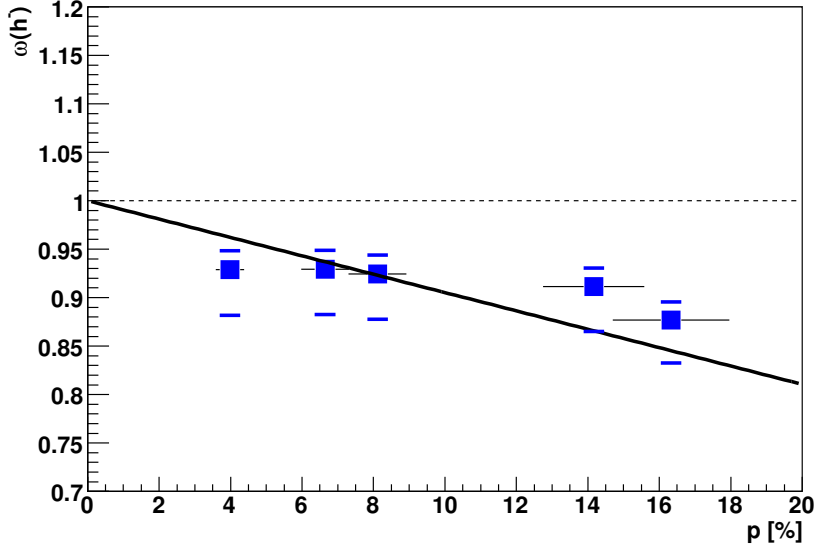


Figure 11: Acceptance dependence of scaled variance for negatively charged hadrons. The data points correspond from left to right to the energies of 20A to 158A GeV. Horizontal bars indicate systematic errors of data points.

approximately the predicted scaling. A more detailed study of rapidity and transverse momentum dependence of multiplicity fluctuations is in progress, but first results indicate that the acceptance scaling seen in figure 11 should be considered only as a rough approximation.

For $\omega(h^+)$ this scaling does not work so well probably because a larger fraction of resonance decays (e.g. Δ^{++}) into two positively charged daughters, introducing more correlation in momentum space. The situation is even worse for $\omega(h^\pm)$ because both daughters of a decay into two unlike sign charged hadrons (e.g. $\rho^- \rightarrow \pi^+ + \pi^-$) are used for the fluctuation analysis. Therefore acceptance scaling plots are shown only for $\omega(h^-)$.

4.3 Statistical Models

Predictions of the statistical hadron-resonance gas model [19] on energy dependence of the scaled variance of negatively charged hadrons are shown in figure 12. In this model multiplicity fluctuations in 4π were calculated for the limit of $V \rightarrow \infty$ using both canonical and grand-canonical ensembles. The effects of resonance decays and quantum statistics are taken into account. The calculated value ω for the canonical ensemble is much lower than for the grand-canonical one in the SPS energy regime. In the canonical ensemble fluctuations are suppressed due to conservation laws of electric charge, baryon number and strangeness by about a factor of two. Preliminary calculations show a further suppression of fluctuations in the micro-canonical ensemble due to additional energy conservation.

Figure 13 shows data on multiplicity fluctuations in comparison to the model calculations.

The scaled variance in the limited acceptance was extrapolated using equation A.7 from the model results in full acceptance. As discussed above equation A.7 may be considered as a reasonable approximation only for $\omega(h^-)$. Use of equation A.7 introduces an uncertainty in the compar-

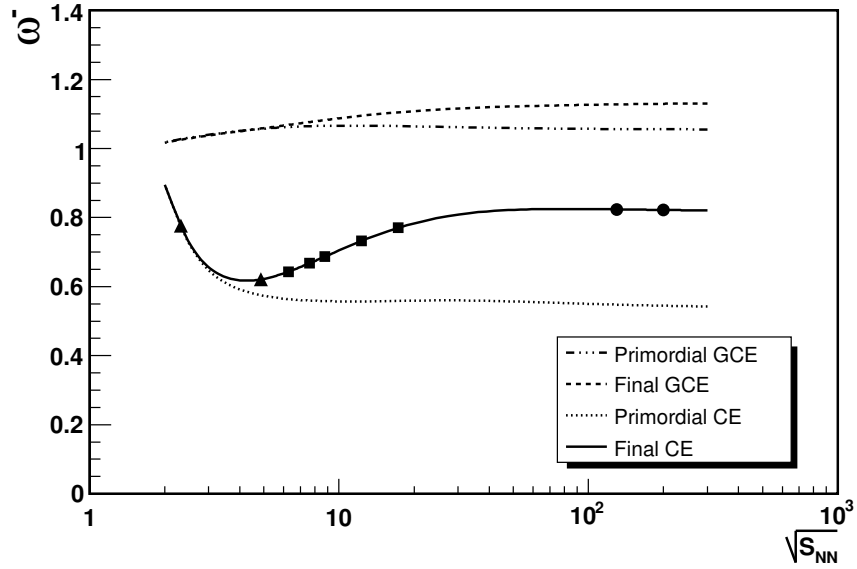


Figure 12: Energy dependence of the scaled variance of negatively charged hadrons in full acceptance in statistical hadron-resonance gas model [19] for grand-canonical (GCE) and canonical (CE) ensemble. The “Final” lines show results after resonance decays.

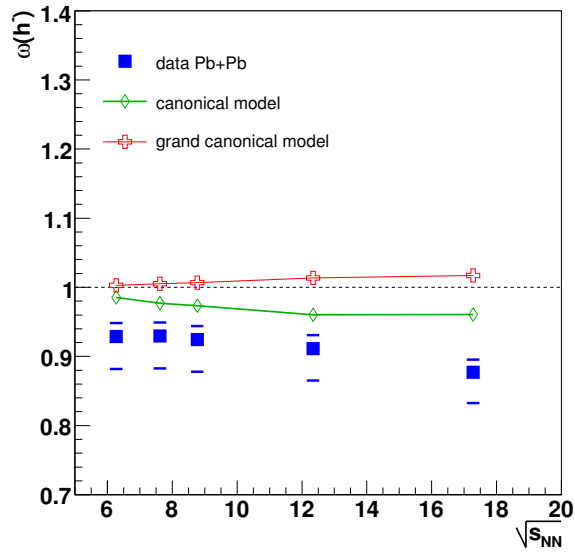


Figure 13: Energy dependence of multiplicity fluctuations of negatively charged hadrons in $Pb + Pb$ collisions in comparison to canonical and grand-canonical statistical hadron-resonance gas model [19]. Horizontal bars indicate systematic errors of data points.

ison of data and model. Note also that in the model calculations the volume of the fireball is fixed, but in data the energy in the Veto calorimeter.

The comparison in figure 13 shows that multiplicity fluctuations in data are much lower than predicted by the grand-canonical model. This is an indication of suppression of fluctuations in relativistic gases due to conservation laws. The predictions of the canonical ensemble are also higher than the data. Energy- momentum conservation and the finite volume of hadrons are expected to cause an additional suppression of fluctuations.

5. Summary

Multiplicity fluctuations in the most central $Pb + Pb$ collisions at 20A, 30A, 40A, 80A and 158A GeV were studied by NA49 at CERN SPS. At all energies multiplicity distributions for positively and negatively charged hadrons are significantly narrower than a corresponding Poissonian distribution.

In comparison to data the multiplicity distributions in Venus are shifted towards lower multiplicities, whereas in UrQMD they are shifted towards higher multiplicities. The Venus model overpredicts scaled variance for central $Pb + Pb$ collisions at most energies, whereas the scaled variance obtained by the UrQMD model is in approximate agreement with data.

Non-monotonic energy dependence of fluctuations, which might be related to the onset of deconfinement or a critical point, is not observed in data.

The hadron-resonance gas model [19] in grand-canonical formulation overpredicts the measured scaled variance. Introduction of the material conservation laws (canonical model) improve agreement with the data.

The presented results may be the first experimental observation of the effect of conservation laws in relativistic gases.

Acknowledgements: Acknowledgements: This work was supported by the US Department of Energy Grant DE-FG03-97ER41020/A000, the Bundesministerium für Bildung und Forschung, Germany, the Virtual Institute VI-146 of Helmholtz Gemeinschaft, Germany, the Polish State Committee for Scientific Research (1 P03B 006 30, 1 P03B 097 29, 1 P03B 121 29, 1 P03B 127 30), the Hungarian Scientific Research Foundation (T032648, T032293, T043514), the Hungarian National Science Foundation, OTKA, (F034707), the Polish-German Foundation, the Korea Science & Engineering Foundation (R01-2005-000-10334-0) and the Bulgarian National Science Fund (Ph-09/05).

A. Acceptance Dependence of Scaled Variance

Let us assume that particles are emitted independently in momentum space. For a given total number of produced particles N_{tot} , the probability to measure a number of particles N in a fixed acceptance p is a binomial distribution.

$$P(N|N_{tot}) = P_{N_{tot}}(N) = \frac{N_{tot}!}{N!(N_{tot} - N)!} p^N (1 - p)^{N_{tot} - N} \quad (\text{A.1})$$

Consequently the mean number of accepted particles is

$$\langle N \rangle = N_{tot} p \quad (\text{A.2})$$

and the variance of the binomial distributions is

$$\text{Var}(N) = N_{tot} p(1 - p) \quad (\text{A.3})$$

If one allows the total number of produced particles to vary according to distribution $P(N_{tot})$, the probability to measure a number of particles N is

$$P(N) = \sum_{N_{tot}} P(N|N_{tot})P(N_{tot}) \quad (\text{A.4})$$

The mean number of particles the in acceptance is

$$\langle N \rangle = p \langle N_{tot} \rangle \quad (\text{A.5})$$

The variance of N is given by:

$$\begin{aligned} \text{Var}(N) &= \langle \text{Var}(N|N_{tot}) \rangle + \text{Var}(\langle N|N_{tot} \rangle) \\ &= \langle \text{Var}(N|N_{tot}) \rangle + \text{Var}(pN_{tot}) \\ &= \langle N_{tot} \rangle p(1 - p) + p^2 \text{Var}(N_{tot}) \end{aligned} \quad (\text{A.6})$$

Finally the scaled variance is

$$\omega = \frac{\text{Var}(N)}{\langle N \rangle} = 1 + p(\omega_{tot} - 1) \quad (\text{A.7})$$

or

$$\omega_{tot} = \frac{\text{Var}(N_{tot})}{\langle N_{tot} \rangle} = 1 + (\omega - 1)/p \quad (\text{A.8})$$

where ω_{tot} is the scaled variance of N_{tot} .

References

- [1] U. W. Heinz and M. Jacob, “Evidence for a new state of matter: An assessment of the results from the CERN lead beam programme,” arXiv:nucl-th/0002042.
- [2] M. Gyulassy and L. McLerran, “New forms of QCD matter discovered at RHIC,” Nucl. Phys. A **750** (2005) 30 [arXiv:nucl-th/0405013].
- [3] M. Gazdzicki *et al.* [NA49 Collaboration], “Report from NA49,” J. Phys. G **30** (2004) S701 [arXiv:nucl-ex/0403023].
- [4] M. Gazdzicki, M. I. Gorenstein and S. Mrowczynski, “Fluctuations and deconfinement phase transition in nucleus nucleus collisions,” Phys. Lett. B **585** (2004) 115 [arXiv:hep-ph/0304052].
- [5] M. Rybczynski *et al.* [NA49 Collaboration], “Multiplicity fluctuations in nuclear collisions at 158-A-GeV,” J. Phys. Conf. Ser. **5** (2005) 74 [arXiv:nucl-ex/0409009].
- [6] M. M. Aggarwal *et al.* [WA98 Collaboration], “Event-by-event fluctuations in particle multiplicities and transverse energy produced in 158-A-GeV Pb + Pb collisions,” Phys. Rev. C **65** (2002) 054912 [arXiv:nucl-ex/0108029].

- [7] M. A. Stephanov, K. Rajagopal and E. V. Shuryak, “Event-by-event fluctuations in heavy ion collisions and the QCD critical point,” *Phys. Rev. D* **60** (1999) 114028 [arXiv:hep-ph/9903292].
- [8] V. V. Begun, M. Gazdzicki, M. I. Gorenstein and O. S. Zozulya, “Particle Number Fluctuations in Canonical Ensemble,” *Phys. Rev. C* **70** (2004) 034901 [arXiv:nucl-th/0404056].
- [9] V. V. Begun, M. I. Gorenstein, A. P. Kostyuk and O. S. Zozulya, “Particle Number Fluctuations in the Microcanonical Ensemble,” *Phys. Rev. C* **71** (2005) 054904 [arXiv:nucl-th/0410044].
- [10] S. Afanasev *et al.* [NA49 Collaboration], “The NA49 large acceptance hadron detector,” *Nucl. Instrum. Meth. A* **430** (1999) 210.
- [11] H. Appelshauser *et al.* [NA49 Collaboration], “Spectator nucleons in Pb + Pb collisions at 158-A-GeV,” *Eur. Phys. J. A* **2** (1998) 383.
- [12] A. Bialas, M. Bleszynski and W. Czyz, “Multiplicity Distributions In Nucleus-Nucleus Collisions At High-Energies,” *Nucl. Phys. B* **111** (1976) 461.
- [13] C. Alt *et al.* [NA49 Collaboration], “Electric charge fluctuations in central Pb + Pb collisions at 20-AGeV, 30-AGeV, 40-AGeV, 80-AGeV and 158-AGeV,” *Phys. Rev. C* **70** (2004) 064903 [arXiv:nucl-ex/0406013].
- [14] M. Rybczynski *et al.* [NA49 Collaboration], “Centrality and System Size Dependence of Multiplicity Fluctuations,” this issue
- [15] V. P. Konchakovski, S. Haussler, M. I. Gorenstein, E. L. Bratkovskaya, M. Bleicher and H. Stoecker, “Particle number fluctuations in high energy nucleus nucleus collisions from microscopic transport approaches,” *Phys. Rev. C* **73** (2006) 034902 [arXiv:nucl-th/0511083].
- [16] M. Gazdzicki and M. Gorenstein, “Transparency, mixing and reflection of initial flows in relativistic nuclear collisions,” *Phys. Lett. B* **640** (2006) 155 [arXiv:hep-ph/0511058].
- [17] K. Werner, “Strings, pomerons, and the venus model of hadronic interactions at Phys. Rept. **232** (1993) 87.
- [18] S. A. Bass *et al.*, “Microscopic models for ultrarelativistic heavy ion collisions,” *Prog. Part. Nucl. Phys.* **41** (1998) 225 [arXiv:nucl-th/9803035].
- [19] V. V. Begun, M. I. Gorenstein, M. Hauer, V. P. Konchakovski and O. S. Zozulya, “Multiplicity fluctuations in hadron-resonance gas,” *Phys. Rev. C* **74** (2006) 044903 [arXiv:nucl-th/0606036].