# Enhanced Mining of Association Rules from Data Cubes

Riadh Ben Messaoud, Sabine Loudcher Rabaséda, Omar Boussaid, and Rokia Missaoui\*

Laboratoire ERIC – Université Lumière Lyon 2 – France
\*Laboratoire LARIM – Université du Québec en Outaouais – Canada







# **General Context**OLAP context

#### **OLAP** capabilities

- Visual exploration of multidimensional data.
- Navigation through hierarchical levels of dimensions.
- Extraction of relevant information for decision-making.

#### OLAP limitations

- Limitation to exploratory tasks.
- Automatic explanation of associations within data.

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An example: a sales data cube

	Quarter 1	Quarter 2	Quarter 3	Quarter 4
Soccer shoes	\$ 9,400	\$ 10,000	\$ 12,600	\$ 10,600
Sleeping bag	\$ 20,500	\$ 13,700	\$ 52,400	\$ 21,000
Tennis racket	\$ 13,100	\$ 14,600	\$ 15,200	\$ 12,300
Bicycle	\$ 11,400	\$ 12,000	\$ 28,000	\$ 10,000

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Sales of sleeping bags are particulary high in the third quarter?



## **General Context**

**Problem** 

#### An example: a sales data cube

		Quarter 3				
		June	July	August		
Sleeping bag	Young	\$ 9,300	\$ 9,300   \$ 24,300			
	Adult	\$ 1,200	\$ 600	\$ 1,600		
	Old		\$ 300			

#### Explanation

- Summer season and young customers are associated with high sales of sleeping bags
- Young ∧ July ⇒ Sleeping bag

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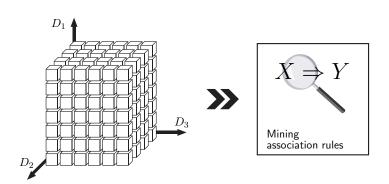
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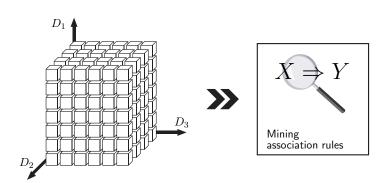
## **Objectives**



#### Key idea

Mine association rules in data cubes in order to explain relationships within multidimensional data.

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Mine **association rules** in **data cubes** in order to **explain** relationships within **multidimensional data**.

## **Outline**

- Related Work
- Our Framework
  - Inter-dimensional meta-rules
  - Measure-based support and confidence
  - Advanced evaluation of association rules
- Proposed Algorithm
- 4 Performance Evaluation
- **5** Conclusion and Perspectives



#### Traditional association rules

- Agrawal et al. (1993): the mining of association rules.
- Srikant and Agrawal (1995): categorical data.
- Han and Fu (1995): multilevel association rules.
- Srikant and Agrawal (1996): quantitative association rules.
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Mining association rules in multidimensional data?

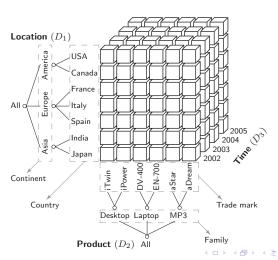
#### Association rules in multidimensional data

	Dimension		Leve	I	Pred	icate	Measure		Application domain	
	Intra-dimensional	Inter-dimensional	Single level	Multiple levels	Repetitive	Non-repetitive	COUNT	All measures	Market basket analysis	General
Kamber <i>et al.</i> (1997)		•	•			•	•			•
Zhu (1998)	•	•	•		•	•	•		•	
Imieliński <i>et al.</i> (2002)		•		•	•			•		•
Dong <i>et al.</i> (2004)		•		•	•			•		•
Chen <i>et al.</i> (2000)	•			•	•		•		•	
Nestorov & Jukić (2003)	•		•		•		•		•	
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Our proposal (2006)										

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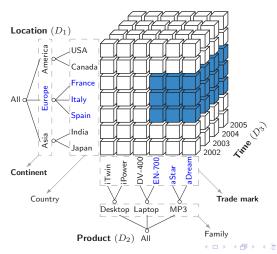
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Sub-cube (example)



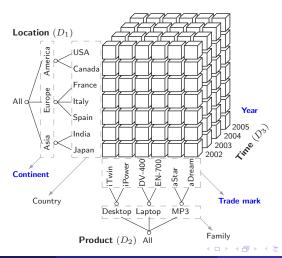
Sub-cube (example)

### (Europe, {EN-700, aStar, aDream})



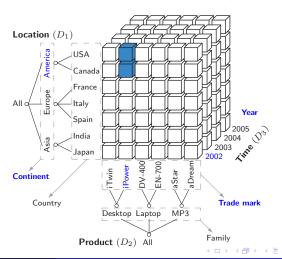
Inter-dimensional predicate (example)

 $\langle a_1 \in \mathsf{Continent} \rangle \land \langle a_2 \in \mathsf{Trade} \; \mathsf{mark} \rangle \land \langle a_3 \in \mathsf{Year} \rangle$ 



Inter-dimensional predicate (example)

### $\langle America \rangle \land \langle iPower \rangle \land \langle 2002 \rangle$



Inter-dimensional meta-rules

We consider two distinct subsets of dimensions in the original data cube:

- $\mathcal{D}_{\mathcal{C}}$  is a subset of **context dimensions**
- ullet  $\mathcal{D}_{\mathcal{A}}$  is a subset of **analysis dimensions**

#### Inter-dimensional meta-rules

In the context of a sub-cube according to  $\mathcal{D}_{\mathcal{C}}$  Head  $\Rightarrow$  Body

ullet Head  $\wedge$  Body is an inter-dimensional predicate in  $\mathcal{D}_{\mathcal{A}}$ 

Inter-dimensional meta-rules

### Example of an inter-dimensional meta-rule

- $\mathcal{D}_{\mathcal{C}} = \{ \text{Profession, Gender} \}$
- $\mathcal{D}_{\mathcal{A}} = \{ \text{Location, Product, Time} \}$

In the context (Student, Female)  $\langle a_1 \in \text{Continent} \rangle \land \langle a_2 \in \text{Year} \rangle \Rightarrow \langle a_3 \in \text{Trade mark} \rangle$ 

#### Example of an inter-dimensional rule

R<sub>1</sub> In the context (Student, Female)
America  $\land$  2004  $\Rightarrow$  Laptop

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Support and confidence

#### With the **COUNT** measure:

- the support and the confidence are computed according to the frequency of units of facts;
- only the number of facts is taken into account to decide whether a rule is large, or strong, or not.

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 Users are usually interested in observing facts according to summarized values of measures more expressive than their simple number of occurrences.

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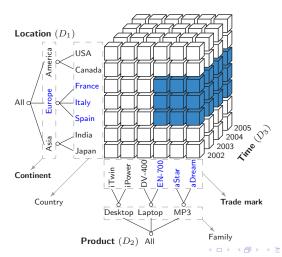
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 $\triangleright$  It is **more significant** to compute **support** and **confidence** according to the **SUM** of fact measures supporting the rule.

### Profit(Europe, {EN-700, aStar, aDream})



Measure-based support and confidence

### Key idea

With the sum-based aggregate measure:

- The rule mining process can handle any measure in order to evaluate the interestingness of extracted association rules.
- A rule is evaluated according to the quantity of measures of its corresponding facts.
- Studied associations concern the population of units of measures of these facts.
- The choice of the measure closely depends on the analysis objectives.

Advanced evaluation of association rules

Only support and confidence ...

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#### Only support and confidence ...

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#### Descriptive Vs. Statistical criteria

- A statistical criterion:
  - depends on the size of the mined population;
  - loses its discriminating power and tends to take a value close to one for large number of examples;
  - requires a probabilistic approach to model the mined population.
- A descriptive criterion:
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- A descriptive criterion:
  - is **easy to use** and **express interestingness** of association rules in a more **natural manner**.
- $\triangleright$  We use **two descriptive criteria** : the **Lift** criterion (Lift) and the **Loevinger** criterion (Loev).

Advanced evaluation of association rules

For a rule  $X \Rightarrow Y$ :

$$Lift(R) = \frac{P_{YX}}{P_X P_Y} = \frac{Supp(R)}{P_X P_Y}$$

#### Interpretation (Lift)

- **Deviation** of the support of the rule from the support expected under the independence hypothesis of the head and the body.
- Scale coefficient of having the body when head occurs.
- Greater Lift values indicate stronger associations.

Advanced evaluation of association rules

For a rule  $X \Rightarrow Y$ :

$$Loev(R) = \frac{P_{Y/X} - P_Y}{P_{\overline{Y}}} = \frac{Conf(R) - P_Y}{P_{\overline{Y}}}$$

#### Interpretation (Loevinger)

- Linear transformation of the confidence in order to enhance it.
- Expresses the confidence according to the probability of not satisfying its head.
- Greater Loevinger values indicate stronger associations.

## **Proposed Algorithm**

Search for large itemsets

#### Search for large itemsets

- The top-down approach:
  - starts with *k*-itemsets and steps down to 1-itemsets;
  - if a *k*-itemset is frequent, then all sub-itemsets are frequent.
- The bottom-up approach:
  - starts from 1-itemsets to longer itemsets;
  - complies with the Apriori property "for each non frequent itemset, all its super-itemsets are definitely not frequent";
  - enables the **reduction** of the **search space**, especially when it deals with **large** and **sparse** data sets.

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# Proposed Algorithm Properties

#### Our algorithm

- An adaptation of the Apriori algorithm for the multidimensional data structure.
- Directly extracts inter-dimensional association rules from data cubes.
- Enables a guided-mining process according to an inter-dimensional meta-rule defined by users.
- Extracts significant rules, for OLAP users, by taking into account any measure in the cube.
- Provides advanced evaluation of extracted associations by using Lift and Loevinger.

# Proposed Algorithm Implementation



## **Performance Evaluation**

Configuration

 Food Mart data cube from Analysis Services of MS SQL Server 2000

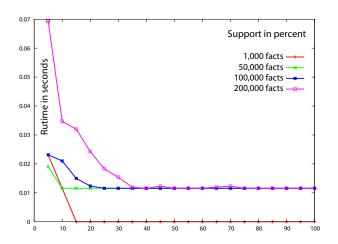
System: Windows XP

Processor: Intel Pentium 4 (1.60GHz)

• Main memory: 480MB

#### **Performance Evaluation**

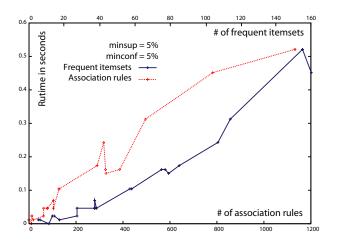
Runtime according to minsupp for different sizes



⊳ For **large** *minsupp*, the mining process has already equal response times **independently** from the **number of mined facts**.

#### **Performance Evaluation**

Runtime according to # of frequent itemsets and # of association rules



The generation of association rules from frequent itemsets is more
time consuming than the extraction of frequent itemsets themselves.

## **Conclusion and Perspectives**

Conclusion

- **1** A general framework for a **guided mining** of **inter-dimensional** association rules from data cubes.
- Inter-dimensional meta-rule which allows users to limit the mining process to specific contexts.
- A general computation of support and confidence that can be based on any measure from the data cube.
- Wide analysis objectives not restricted to associations only driven by the COUNT measure.
- Interestingness of mined rules according to two additional descriptive criteria (Lift and Loevinger).
- An adaptation of the Apriori algorithm in order to handle multidimensional data.

## **Conclusion and Perspectives**

Perspectives

- Extension to handle inter-dimensional association rules with repetitive predicates.
- 2 Extension to handle intra-dimensional association rules.
- **3** Embedding the **measure** in the **expression** of mined association rules.
- Profit from the hierarchical aspect of cube dimensions to mine multi-level association rules.
- Ope with the visualization for an easier interpretation of mined associations by OLAP users.
- Explore other approaches for association rule mining: closed itemset generation and non-redundant rule generation.

#### The end

Thank you for your attention!

Feel free to ask questions...