

## Estimating EEG source dipole orientation based on singular-value decomposition for connectivity analysis

RUBEGA, Maria, *et al.*

### Abstract

In the last decade, the use of high-density electrode arrays for EEG recordings combined with the improvements of source reconstruction algorithms has allowed the investigation of brain networks dynamics at a sub-second scale. One powerful tool for investigating large-scale functional brain networks with EEG is time-varying effective connectivity applied to source signals obtained from electric source imaging. Due to computational and interpretation limitations, the brain is usually parcelled into a limited number of regions of interests (ROIs) before computing EEG connectivity. One specific need and still open problem is how to represent the time- and frequency-content carried by hundreds of dipoles with diverging orientation in each ROI with one unique representative time-series. The main aim of this paper is to provide a method to compute a signal that explains most of the variability of the data contained in each ROI before computing, for instance, time-varying connectivity. As the representative time-series for a ROI, we propose to use the first singular vector computed by a singularvalue decomposition of all dipoles [...]

### Reference

RUBEGA, Maria, *et al.* Estimating EEG source dipole orientation based on singular-value decomposition for connectivity analysis. *Brain Topography*, 2019, vol. 32, no. 4, p. 704-719

PMID : 30511174

DOI : 10.1007/s10548-018-0691-2

Available at:

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1 Estimating EEG source dipole orientation based on singular-value decomposition for  
2 connectivity analysis

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23 ABSTRACT

24 In the last decade, the use of high-density electrode arrays for EEG recordings combined with the  
25 improvements of source reconstruction algorithms has allowed the investigation of brain networks dynamics at  
26 a sub-second scale. One powerful tool for investigating large-scale functional brain networks with EEG is time-  
27 varying effective connectivity applied to source signals obtained from electric source imaging. Due to  
28 computational and interpretation limitations, the brain is usually parcelled into a limited number of regions of  
29 interests (ROIs) before computing EEG connectivity. One specific need and still open problem is how to represent  
30 the time- and frequency-content carried by hundreds of dipoles with diverging orientation in each ROI with one  
31 unique representative time-series. The main aim of this paper is to provide a method to compute a signal that

32 explains most of the variability of the data contained in each ROI before computing, for instance, time-varying  
33 connectivity. As the representative time-series for a ROI, we propose to use the first singular vector computed by  
34 a singular-value decomposition of all dipoles belonging to the same ROI. We applied this method to two real  
35 datasets (visual evoked potentials and epileptic spikes) and evaluated the time-course and the frequency content  
36 of the obtained signals. For each ROI, both the time-course and the frequency content of the proposed method  
37 reflected the expected time-course and the scalp-EEG frequency content, representing most of the variability of  
38 the sources (~80%) and improving connectivity results in comparison to other procedures used so far. We also  
39 confirm these results in a simulated dataset with a known ground truth.

40 *Keywords.* EEG, source space activity, dipole orientation, visual evoked potentials, epilepsy  
41

## 42 INTRODUCTION

43 Electroencephalography (EEG) records the dynamic of brain networks on a sub-second time scale. The high  
44 temporal resolution of EEG allows to study how brain activity propagates and interacts in large-scale networks by  
45 applying connectivity measures to the recorded signals. However, connectivity measures based on scalp electrode  
46 measurements (sensors space) are not revealing the true interactions among brain sources. Neighbouring  
47 electrodes measure signals that are highly correlated, leading connectivity algorithms to estimate sham links.  
48 Indeed, the measurements of the voltage potential at various locations on the scalp are the result of the  
49 simultaneous activity of many different configurations of distributed current generators in the brain [1] [2] [3] [4].  
50 To obtain physiologically plausible results, the reconstruction of brain source activity before computing  
51 connectivity is strictly required. However, the underlying brain source activity cannot be estimated uniquely from  
52 the scalp data, without invoking priors or constraints on the inverse solution. Functional connectivity analysis in  
53 the source space has been divided into two main groups [5]. One group of methods employs neuronal models of  
54 interacting brain regions, i.e., dynamic causal models (DCM), as priors which are added to the spatial forward  
55 model to reconstruct the scalp EEG data. Thereby, reasonably realistic assumptions of source dynamics are  
56 required [6] [7]. Provided that the model assumptions are physiologically meaningful, the DCM approach allows  
57 to infer not only the source dynamics but also the coupling parameters shaping interactions among sources [7].  
58 The other group of methods does not use assumptions on the network structure and is characterized by a two-  
59 step procedure. First, the scalp data is inverted to the source space using distributed source models and then  
60 functional connectivity measures are applied to the estimated sources. A priori assumptions have to be  
61 introduced to solve the ill-posed inverse problem. For instance, LAURA (Local AUtoRegressive Average), the  
62 distributed linear inverse solution used here, incorporates biophysical laws into the minimum norm solution [8].  
63 By incorporating such priors, the distribution of the simultaneously active sources at each moment in time can be  
64 estimated from the high-density EEG scalp potentials informed by the individual anatomy derived from magnetic  
65 resonance imaging (MRI) and realistic volume conduction physics [9] [10] [11] [12] [13]. The estimated activity at  
66 each solution point in the brain is described by a three dimensional dipole  $(x,y,z)$ . After the estimation of the  
67 dipole activity at each solution point, the brain is usually parceled into regions before connectivity estimation,

68 because the full spatial size of the data (more than 5000 solution points) is unreasonable in terms of computations  
69 and statistical power. The choice of the parcellation scheme and resolution is crucial as it has effects on network  
70 topological characteristics. It depends on the type, quality and resolution of data and on the study purpose and  
71 can be based either on anatomical or functional assumptions [14]. The most commonly used anatomical-based  
72 parcellation atlases are, among others, the Automated Anatomical Labeling (AAL) atlas [15] [16] and FreeSurfer's  
73 Desikan Killiany atlas [17] [18]. After parcellation, it is possible to build a graph representation of the brain [19]  
74 where nodes are associated to the brain regions of interest (ROIs), and edge weights are given by functional [20]  
75 [21] [22] or effective [23] [24] connectivity measures that are robust to volume conduction effects. To estimate  
76 either directed or undirected connectivity, all the solution points estimated in each ROI need to be summed up  
77 in a unique time-series. The approaches proposed in the literature usually consist of two steps. In the first step,  
78 for each dipole, either the norm is computed or the direction of the dipoles is fixed using different techniques.  
79 One approach is the computation of the norm (i.e. computing absolute dipole amplitude while discarding the  
80 orientation of the dipoles) or the power modulation using the Hilbert transform [25] [26]. This, however, may be  
81 problematic for connectivity estimation because the phase information contained in the original signal is lost [27].  
82 Other current methods to fix the dipole orientation within a ROI are either the projection to the refined average  
83 direction across time and epochs [28]; the selection of the dipole orientation orthogonal to the segmented grey  
84 matter based on the assumption that the orientation of the dipoles should resemble the orientation of the apical  
85 dendrites of the pyramidal neurons [29] or the selection of the orientation maximizing the projected power [30].  
86 The second step consists in either averaging all dipole time-series within the ROI once the dipole orientation is  
87 fixed [31] or applying principal component analysis (PCA) to obtain the representative time-series [32] [33].

88 Other popular one-step solutions are either to compute the average cortical activity in each ROI by means of  
89 the instantaneous average of the signed magnitude of all the dipoles within the ROI [34] or to consider only the  
90 source activity of the solution point closest to the geometric center of each ROI, i.e., the centroid, as the  
91 representative source waveform [35] [36] [37] [38]. However, the selection of only one dipole out of hundreds  
92 does not necessarily properly represent the activity in a given ROI. Concerning the averaging approach, a common  
93 observation is a drastic amplitude reduction. Indeed, due to the extensive folding of the human cerebral cortex,  
94 some sources in the ROI may be almost perfectly parallel to each other, but inverted in orientation, leading to  
95 cancelation when averaging them. The resulting signal amplitude reduction could lead to decrease in accuracy of  
96 the subsequent analysis and affect the final results. For instance, connectivity estimation involves computing the  
97 inverse of the matrix containing the representative source waveforms, which, if the values are small, may lead to  
98 a bad-conditioned matrix with a high condition number [39], i.e., even a small error in the data can produce a  
99 large deviation in the solution. Moreover, low-amplitude time-series may increase the rate of false positive  
100 connections, e.g., low-amplitude time-series may easily fit in large-amplitude time-series leading to misleading  
101 high autoregressive coefficients [40].

102 In this work, we propose to extract the dominant signal reflecting the main pattern of variation of all the  
103 solution points in the same ROI by using Singular-Value Decomposition (SVD) and considering the first singular  
104 vector. This method enables both to identify the main direction of all the dipoles of a ROI and to discard the  
105 contribution of the outlier dipoles. The novelty with respect to the other approaches proposed in the literature is

106 that SVD provides a *population* signal that incorporates the behavior of all the dipoles within the ROI without  
107 choosing or selecting specific active voxels, as it is usually done [41] [32] [33] [30].

108 The evaluation of the performance of a functional connectivity analysis method on real data sets is difficult  
109 because an objective ground truth is usually not available. Two type of data that are often used for method  
110 evaluation are: interictal spikes of patients with focal epilepsy where the focus localization is known from  
111 intracranial recordings or from successful surgery [42] [43], and evoked potentials where the generation and the  
112 propagation of information in the brain is well understood [6]. Here, we used these two type of datasets to  
113 demonstrate the validity of the proposed method. We analyzed spike data of patients with focal epilepsy who  
114 had positive outcome of the surgery after 12 months. We expected that our method correctly identifies the  
115 epileptic focus (the ROI lying within the resected zone) as major driver of the epileptic network. For the evoked  
116 potentials, we analyzed a dataset of visual evoked potentials (VEP) after presentation of face stimuli. We expected  
117 that the proposed method would reliably identify the main components of the VEP, i.e. the P100 and the N170 in  
118 the source space, and that the major driver of the network would be localized to the lateral, basal temporal and  
119 occipital cortices including the fusiform gyrus as shown trough EEG changes from implanted electrodes [44] [45]  
120 [46]. In addition, we evaluated the performance of the proposed method in realistically simulated data, where  
121 the ground-truth was known. We also compared the method to the common procedure of both, extracting the  
122 time-series of the centroid in each ROI and extracting the time-series with the highest power in each ROI.

## 123 METHODS

### 124 *Data description*

125 *Dataset 1. Visual evoked potential of face perception.* Many behavioral studies have investigated the process  
126 involved in visual stimuli such as face images [47] [48] [49]. Traditional measures are based on the N170 face-  
127 sensitive evoked response component [50]. Human faces evoke a large negative potential (N170) over the  
128 occipital-parietal scalp, more prominent over the right than the left hemisphere, which is reduced in evoked  
129 potentials elicited by other animate and inanimate non-face stimuli [51]. Applying effective connectivity in face  
130 perception, i.e., describing the network of directional effects of one brain region over another, may be a powerful  
131 instrument to study this visual process. In order to study these causal effects, it is important to precisely  
132 reconstruct the face-response stimulus in the source space. For this reason, we investigated the ability of our  
133 method to reconstruct the dynamics of visual evoked potential (VEP) in source space based on high density EEG  
134 (hdEEG) data.

135 Participants (N=13, 2 males, age=24.15 ± 3.41) sat in a dimly lit sound-attenuated and electrically shielded  
136 room with their head positioned on a chinrest at ~70 cm from the monitor. Each trial lasted 1.2 seconds and  
137 started with a blank screen lasting 500 ms. After the blank interval, one image (either a face or a scramble image)  
138 was presented for 200 ms and participants had the remaining 1000 ms to respond. The task was to report whether  
139 they saw a face or not (Yes/No task) by pressing two buttons in a response box. Faces and scrambled images were

140 randomly interleaved across trials. After the participant's response, there was a random interval (from 600 to 900  
141 ms) before the beginning of a new trial.

142 The experiment consisted of 4 blocks of 150 trials each, for a total of 600 trials, i.e., 300 with faces and 300  
143 with scrambled images [52]. For this study, we used the EEG data in response of the face images (300 trials per  
144 subject).

145 During the experiment, EEG data were recorded continuously at 1024 Hz through a 128-channel Biosemi  
146 Active Two EEG system (Biosemi, Amsterdam, The Netherlands). Electrode impedance was kept  $< 20 \text{ k}\Omega$ .

147 *Dataset 2. Interictal epileptiform discharges in focal epilepsy.* hdEEG source imaging plays a central role in  
148 diagnosis and management of patients with focal epilepsy [42]. However, recent work in the literature provided  
149 evidence that epilepsy is a disorder affecting neural networks [53]. Thus, connectivity measures and graph analysis  
150 are promising tools to extract network information from both hdEEG and neuroimaging data [54] [55] [56]. We  
151 applied our method on pre-surgical interictal spikes (IEDs) recorded in patients with pharmaco-resistant focal  
152 epilepsy, who subsequently underwent epilepsy surgery.

153 The patients ( $N=7$ , 3 males,  $\text{age}=23\pm 14 \text{ y}$ ) were selected from those admitted for pre-surgical evaluation to  
154 the EEG & Epilepsy Unit, Department of Clinical Neurosciences, University Hospital of Geneva (HUG), Switzerland.  
155 They underwent hdEEG long-term ( $>4 \text{ h}$ ) recording with 256 electrodes in the context of their pre-surgical  
156 evaluation, and subsequently underwent resection of the estimated epileptogenic zone causing their focal  
157 epilepsy. The outcomes of the surgery after 12 months along with the exact location of the resection zone were  
158 available from postoperative structural MRI and were used as validation for the localization of the generators of  
159 the interictal epileptic discharges.

160 The hdEEG was recorded with the Geodesic Sensor Net with 256 electrodes (Electrical Geodesic, Inc., Eugene,  
161 OR, U.S.A.). Electrode-skin impedances were maintained  $<15 \text{ k}\Omega$ . The recordings were sampled at 1 kHz,  
162 referenced to Cz. Then, an epileptologist, G.T., marked  $41\pm 18$  hdEEG epochs containing the interictal spikes for  
163 each patient. Then, the 1-s hdEEG epochs centered on the spike peak were used as input of the analysis.

#### 164 *Preprocessing*

165 The VEP EEG signals were downsampled at  $f_s = 200 \text{ Hz}$  and detrended to remove slow fluctuations and  
166 linear trends [57]. The line and monitor noise (50 and 75 Hz, plus harmonics) were attenuated with an adaptive  
167 multitaper filter (Cleanline plugin for EEGLAB). EEG epochs were then extracted from the continuous dataset and  
168 time-locked from  $-1000 \text{ ms}$  to  $1000 \text{ ms}$  relative to the onset of each image. Noisy channels were identified by  
169 visual inspection and removed before preprocessing. Individual epochs containing non-stereotyped artifacts, peri-  
170 stimulus eye blinks and eye movements (occurring within  $\pm 500 \text{ ms}$  from stimulus onset) were also identified by  
171 visual inspection and removed from further analysis (mean number of epochs removed across participants:  $6\pm 5$ ).  
172 Data were cleaned from remaining physiological artifacts (eye blinks, horizontal and vertical eye movements,  
173 muscle potentials and other artifacts) through a PCA-informed ICA algorithm implemented in EEGLAB. After ICA  
174 cleaning, the identified artifact channels were interpolated using the nearest-neighbor spline method and the  
175 data were re-referenced to the average reference.

176 The EEG data containing the spikes of epileptic patients were filtered from  $[0.5 \ 40]$  Hz with 5<sup>th</sup> order  
 177 Butterworth filter avoiding phase distortion. Finally, the data were down-sampled at  $fs = 250$  Hz.

#### 178 *EEG source estimation*

179 In this study, we applied the LAURA algorithm implemented in Cartool [58] to compute the source  
 180 reconstruction in the individual MRI applying the Local Spherical Model with Anatomical Constraints (LSMAC) and  
 181 taking into account the patient's age to calibrate the skull conductivity [8] [59] [60]. The LSMAC method restricts  
 182 the solution space to the gray matter of the individual brain.

#### 183 *Whole brain segmentation and parcellation*

184 Starting from the high-resolution T1-weighted image, using the Connectome Mapper open-source processing  
 185 [61] that calls the version 6 of the Freesurfer image analysis suite [62], we resampled the image to isotropic  
 186  $1 \times 1 \times 1$  mm<sup>3</sup> and we segmented the whole brain in white matter, grey matter, i.e., cortical and sub-cortical  
 187 structures, and cerebrospinal fluid based on the anatomical Desikan-Killiany [17] and Destrieux [63] atlases. At  
 188 the end of the process, the cortex was parcellated into a total of 83 regions, which accounted for all the cortical  
 189 structures of the Desikan-Killiany anatomical atlas, as well as the deep-grey nuclei and the brainstem [61].

#### 190 *Projection method based on SVD*

191 An estimate of the  $x - y - z$  space coordinates of the circa  $M = 5000$  cortical dipoles was obtained for  
 192 each time point. The estimation of the dipole sources  $\tilde{\mathbf{x}}$  is based on the solution of the following regularized  
 193 equation:

$$194 \quad \tilde{\mathbf{x}} = \underset{\mathbf{x}}{\operatorname{argmin}} (\|\mathbf{L}\mathbf{x} - \mathbf{y}\|_N^2 + \gamma^2 \|\mathbf{x}\|_M^2) \quad (1)$$

195 where  $\|\cdot\|_M$  represents the M-norm,  $\mathbf{L}$  is the lead field matrix,  $\mathbf{x}$  the dipole sources,  $\mathbf{y}$  the EEG scalp potentials  
 196 and  $\gamma$  is the regularization parameter which can be estimated by different criteria, e.g., by the L-curve approach  
 197 [64].

198 Subsequently, first, we associated the dipoles to their respective ROI based on the 82 atlas labels (the  
 199 brainstem was excluded). Second, for each ROI separately, we collected all the  $N$  time samples of the  $x - y -$   
 200  $z$  space coordinates of the  $n$  dipoles included in a given ROI and we organized the zero-mean data in a matrix  
 201  $\mathbf{D}$ ,  $[N \times (n \times 3)]$ , as follows:

$$202 \quad \mathbf{D} = \begin{bmatrix} d_{x_1}(t_1) & d_{y_1}(t_1) & d_{z_1}(t_1) & \dots & d_{x_n}(t_1) & d_{y_n}(t_1) & d_{z_n}(t_1) \\ & \vdots & & \ddots & & \vdots & \\ d_{x_1}(t_N) & d_{y_1}(t_N) & d_{z_1}(t_N) & \dots & d_{x_n}(t_N) & d_{y_n}(t_N) & d_{z_n}(t_N) \end{bmatrix} \quad (2)$$

203 After that we applied the SVD to this matrix:

$$204 \quad \mathbf{D} = \mathbf{U}\mathbf{S}\mathbf{V}^T \quad (3)$$

205 where the apex  $T$  stands for the transpose and the columns of  $\mathbf{D}$  can be seen as the linear combinations of  
 206 the columns of  $\mathbf{U}$  with the coefficients given by the columns of  $\mathbf{S}\mathbf{V}^T$ . Because of the singular values contained in  
 207 the diagonal of  $\mathbf{S}$  appear in a decreasing order, we considered the first column of  $\mathbf{U}$   $\mathbf{u}_1 [N \times 1]$ , i.e., the  
 208 orthonormal vector projected along the axis that represents the major orientation of all the dipoles, like the signal

209 that explains most the variability of the data and as the best representation of the ROI content. In other words,  
 210 Equation (3) assumes that the data matrix  $\mathbf{D}$  comprises hidden components  $\mathbf{u}_i$  that are mixed together through  
 211 coefficients  $\mathbf{S}$ . Standard matrix factorizations in linear algebra, such as SVD, owe their uniqueness to hard and  
 212 restrictive constraints such as orthogonality [65].

### 213 *Connectivity estimation*

214 Among the different techniques for extracting effective connectivity, information partial directed coherence  
 215 (*iPDC*) properly accounts for size effects in gauging connection strength, as reported in detail in [66]. In  
 216 particular, *iPDC* is a multivariate spectral measure to compute only the directed influences between any given  
 217 pair of signals ( $i, j$ ) of a multivariate dataset. This information is condensed in a complex function  $iPDC_{i \leftarrow j}(f)$  of  
 218 the frequency  $f$ , which measures the relative interaction of the signal  $j$  with regard to signal  $i$  as compared to all  
 219  $j$ 's interactions to other signals in the multivariate dataset. While we refer the reader to [67] for the mathematical  
 220 details, the procedure for computing *iPDC* is briefly described by the following two steps.

221 In the first step, the cortical waveforms  $\tilde{\mathbf{x}}$  computed after applying the projection method described in the  
 222 previous section, are fitted against a *time-variant* (tv) multivariate autoregressive (MVAR) model to overcome the  
 223 problem of non-stationarity of the EEG data. If the EEG data are available as several trials of the same length, the  
 224 cortical waveforms computed from the EEG data generates a collection of realizations of a multivariate stochastic  
 225 process which can be combined in a multivariate, multi-trial time series:

$$226 \quad \tilde{\mathbf{X}}(t) = \begin{bmatrix} \tilde{\mathbf{x}}_1^{(1)}(t) & \cdots & \tilde{\mathbf{x}}_d^{(1)}(t) \\ \vdots & \ddots & \vdots \\ \tilde{\mathbf{x}}_1^{(K)}(t) & \cdots & \tilde{\mathbf{x}}_d^{(K)}(t) \end{bmatrix} \quad t = t_1, \dots, t_N \quad (4)$$

227 where  $t$  refers to the time points,  $N$  the length of the time-series,  $K$  the number of trials and  $d$  the number  
 228 of ROIs.

229 Then the data in  $\tilde{\mathbf{X}}$  are fitted against a tvMVAR model in the general form:

$$230 \quad \tilde{\mathbf{X}}(t) = -\sum_{r=1}^p \mathbf{A}_r(t) \mathbf{X}(t-r) + \mathbf{W}(t) \quad (5)$$

231 where  $\mathbf{A}_r(t)$  are the  $[d \times d]$  AR matrices containing the model coefficients,  $\mathbf{W}(t)$  is the stationarity zero-mean  
 232 white noise process also called innovation process with covariance matrix  $\Sigma_w$ , and  $p$  is the model order, usually  
 233 estimated by means of the Akaike Information Criteria for MVAR processes [68]. The General Linear Kalman filter  
 234 approach is applied in order to estimate the coefficients of the time-variant AR matrices and the innovation  
 235 process  $\Sigma_w$  [69].

236 As the MVAR model is estimated, for each time-point  $t$ , having defined the complex matrix  $\mathbf{B}(f)$  as:

$$237 \quad \mathbf{B}(f) = \mathbf{I}_d - \sum_{r=1}^p \mathbf{A}_r e^{-j2\pi f r} \quad (6)$$

238 where  $\mathbf{I}_d$  is the identity matrix and  $j$  is the imaginary unit in this equation, the *iPDC* complex function from the  
 239 time-series  $j$  to the time-series  $i$  is obtained by:



240 
$$iPDC_{i \leftarrow j}(f) = \sigma_{w_{ii}}^{-1/2} \frac{b_{ij}(f)}{\sqrt{\mathbf{b}_j^H(f) \Sigma_w^{-1} \mathbf{b}_j(f)}} \quad (7)$$

241 where  $\mathbf{b}_j(f)$  and  $b_{ij}(f)$  are respectively the  $j$ -th column and the  $(j, i)$ -th element of matrix  $\mathbf{B}(f)$ ,  $\sigma_{w_{ii}}$  is the  
 242  $(i, i)$ -th element of the innovation covariance matrix  $\Sigma_w$ , and the apex  $H$  in  $\mathbf{b}_j^H$  stands for Hermitian transpose,  
 243 i.e., obtained from  $\mathbf{b}_j$  by taking the transpose and then the complex conjugate of its components.

244 The complex function  $iPDC_{i \leftarrow j}(f)$  of eq. (7) is usually analysed in terms of its absolute value.

245 *Simulation*

246 To test if the SVD method is capable of detecting an effective connectivity map of the human brain, we  
 247 simulated a simple four-node (ROI) network with different delays. We generated the time-course of the dipoles  
 248 laying in the right occipital region of the brain and then a delayed version of 3 ms with the same profile in the left  
 249 occipital region. The same signals with a reduced amplitude (80%) and a delay of 5 ms were placed in the left and  
 250 right inferior temporal regions of the brain. The time-course chosen was the average VEP reconstructed in the  
 251 source space of the Dataset 1 in the right occipital cortex in the first 500 ms after the stimulus. The orientation of  
 252 the dipoles was chosen perpendicular to the cortex. Each realization had a sample rate of 200 Hz with 100 time  
 253 points.

254 After having reconstructed these waveforms, white Gaussian noise with a SNR=5 was added to the simulated  
 255 waveforms and it also generated the background activity of the other dipoles of the model. These  $M=5000$  dipoles  
 256 were then multiplied with the lead field matrix  $L$  estimated for each subject of the Dataset 1 obtaining the  
 257 simulated EEG. We obtained 20 epochs for each subject by adding 20 different profiles of noise.

258 RESULTS

259 *Application on visual evoked potentials*

260 In **Figure 1** (panel (a)), we report the dipoles (arrows in the figure) representing the source waveforms in the  
 261 right lateral occipital cortex of a representative subject (sub #1) in the 500 ms after the face stimulus from  
 262 different perspective views. We chose the right lateral occipital cortex to visualize the results, because we clearly  
 263 localized the N170 component in this region. In addition, this source localization is also consistent with the  
 264 literature [70] using MRI localizer scan that revealed two additional extrastriate regions beyond the fusiform face  
 265 area that responded more strongly when subjects viewed faces than when they viewed objects. These include  
 266 brain regions in the occipital gyri and in the superior temporal sulcus [49]. To be able to compress four dimensions,  
 267 i.e.,  $x, y, z$  and  $time$  axes, in a 2-D figure, the  $x$ -axis is carrying both the information of the  $x$  dimension and  
 268 the  $time$  dimension. In other words, we rigid translated each dipole along the  $x$ -dimension to represent its time  
 269 evolution. In panel (b), we report the three different projection planes of the space represented in panel (a). In  
 270 panel (c), the time-series representing the time-course of the source waveforms in the right lateral occipital cortex  
 271 projected in the  $x, y$  and  $z$  axes are depicted respectively from top to bottom. Interestingly, in the estimated VEP  
 272 source waveforms after the visual stimulus, the orientation over time of all the set of dipoles is not random.  
 273 Furthermore, we qualitatively observe the existence of a main direction that maximizes the magnitude of the  
 274 majority of dipoles. Having noticed that, summing the dipoles content in each ROI by the orthonormal vector

275 projected along the axis in space that represents the major orientation of all the dipoles should explain most the  
276 variability of the data and be an accurate representation of the ROI content.

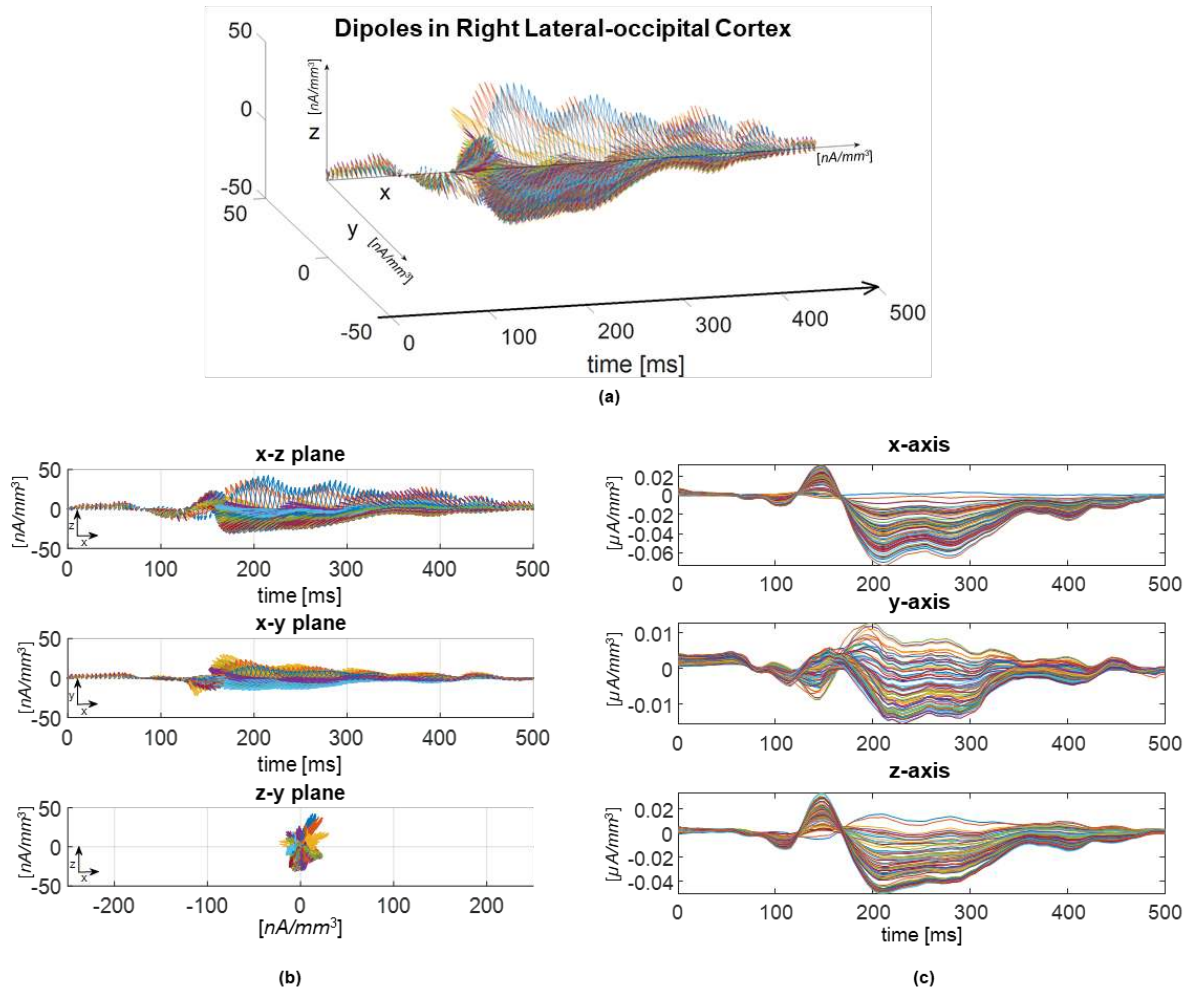


Figure 1 (a) All dipoles representing the solution points in the source space are reported as arrows. Each colour represents the dynamics of a different dipole over time in the right lateral-occipital brain region in a representative subject (sub #1). (b) Views of the x-z-plane, x-y-plane and z-y plane are represented from top to bottom for dipoles of panel (a). (c) x- y- z- time-components of all the dipoles in the Right Lateral-occipital region.

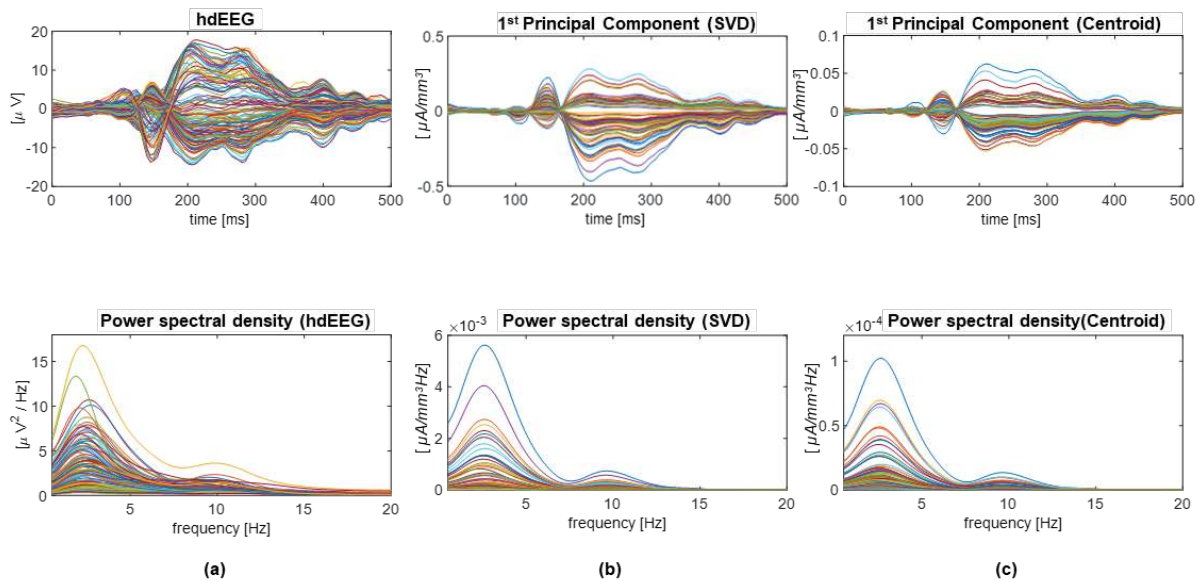
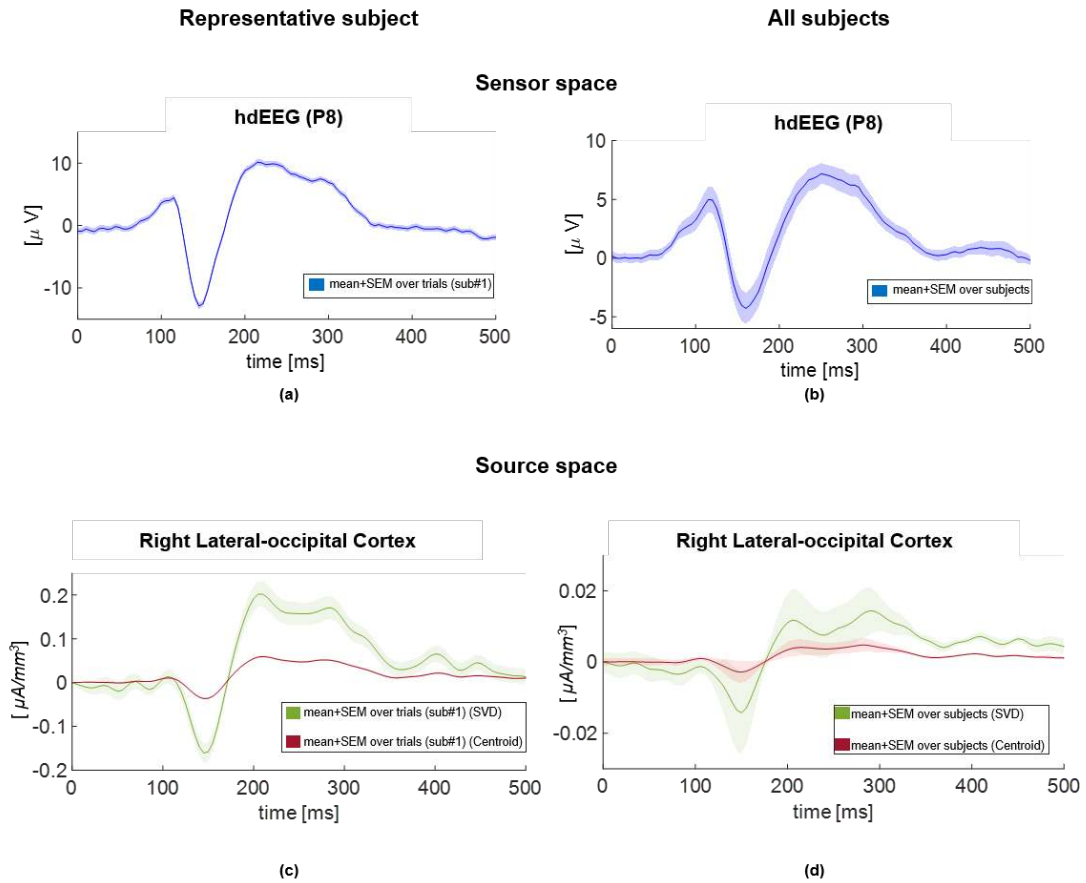


Figure 2 Signal and corresponding power spectral density average among trials of (a) 128 high-density EEG time-courses representing the visual evoked potential in a representative subject (sub #1), (b) ROI time-series computed through SVD in sub #1, and (c) the first principal component of the time-series lying in the centroid of each ROI.

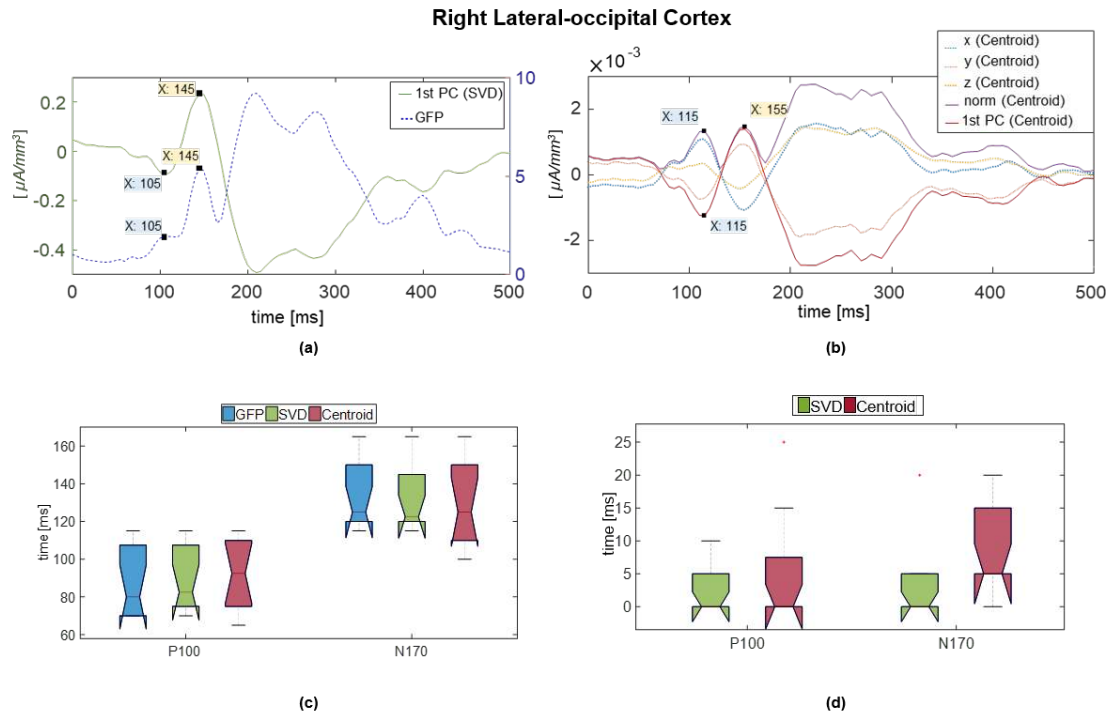
278 as representative for the entire ROI. For this reason, in **Figure 2**, we compared the temporal patterns and the  
279 frequency content of the hdEEG recordings 500 ms following the stimulus presentation (panel (a)) with the  
280 reconstructed time-series in the inverse space obtained from the proposed SVD method (panel (b)) and the source  
281 activity in the centroid (panel (c)) for sub#1. In panels (b) and (c) respectively, we reported the first principal  
282 component computed from both the first eigenvector for each ROI and for the three x- y- z- components of the  
283 source activity in the centroid. After applying SVD, dealing directly with the first eigenvector or re-projecting the  
284 first eigenvector on the original data space is a user choice. It depends if the user needs to deal with normalized  
285 time-series or if she/he cares about the amplitude content of the signal. Observing both the proposed  
286 reconstruction (**Figure 2** panel (b)) and the centroid time-series (**Figure 2** panel (c)), we found that they strongly  
287 differ in the amplitude magnitude as visible in their absolute power spectral density values. However, the relative  
288 power distribution among the canonical EEG-frequency bands does not significantly differ between the two  
289 different reconstructions (Mann-Whitney U-test,  $p>0.98$ ).

290 To emphasize the differences between the two methods, we compared the ability in detecting the P100 and  
291 N170 peaks of the proposed representative time-series based on SVD computation and the centroid one. P100 is  
292 the first dominant component in response to visual stimuli with a lateral occipital positivity [71], followed by the  
293 N170. The N170 is a component of the evoked potential that reflects the neural processing of faces and its  
294 response should be maximal over occipital-temporal electrodes [72] [73]. In **Figure 3**, we report for a  
295 representative subject and for all the subjects the average EEG signal in the sensor space at electrode B11 (P8)  
296 located over the right parietal lobe (panels (a) and (b)) and the reconstructed time-series in the source space  
297 through the SVD and the centroid in the right lateral-occipital cortex (panels (c) and (d)). **Figure 3** shows that the  
298 centroid time-series has lower amplitude and a flatter morphology than the SVD time-series in a representative  
299 subject (panel (c)) and across subjects (panel (d)) in the source space. The results in **Figure 3** confirmed that the  
300 SVD time-series present a coherent pattern compared to the signal recorded on the scalp and the amplitude and  
301 the latency of the peaks of interest can be easily estimated. In order to check for latency differences between the  
302 methods, we computed as reference the Global Field Power (GFP) [59] from the hdEEG for each subject in order  
303 to determine the latency of the maxima of the components P100 and N170. For instance, for sub#1, the two  
304 detected latencies were  $t=105$  ms for P100 and  $t=145$  ms for N170. We then calculated the inverse solution on  
305 the average evoked potential with Cartool [59] and we localized the ROI containing the maximum of the norm of  
306 the source waveforms for both peaks. We then compared the latencies estimated in the time-series obtained by  
307 the proposed projection method (**Figure 4** panel (a)) with the time-series derived from the centroid method  
308 (**Figure 4** panel (b)) in the selected ROI. Results in a boxplot form (**Figure 4** panel (c)) show the latencies  
309 estimated through the GFP, in blue, the SVD time-series, in green, and the centroid time series, in red. **Figure 4**  
310 panel (d) shows that the absolute difference between the latencies estimated through the GFP and the  
311 reconstructed time-series in the source space is higher for the centroid compared to the SVD time-series. From  
312 this evaluation, the SVD time-series seem to more reliably estimate the peak latencies in the VEP.



313

314 *Figure 3 . (a) Average  $\pm$  SEM among trials of the EEG signal recorded on B11 (P8) electrode in sub#1. (b) Average  $\pm$  SEM*  
 315 *among subjects of the average of the EEG signal on B11 (P8). (c)Average  $\pm$  SEM among trials of the proposed representative*  
 316 *time-series in the source space computed through SVD (green) and of the centroid (red) in sub#1 in the right lateral-occipital*  
 317 *cortex. (d) Average  $\pm$  SEM among subjects of the average proposed representative time-series computed through SVD (green)*  
 318 *and of the average centroid (red) in the right lateral-occipital cortex.*



319

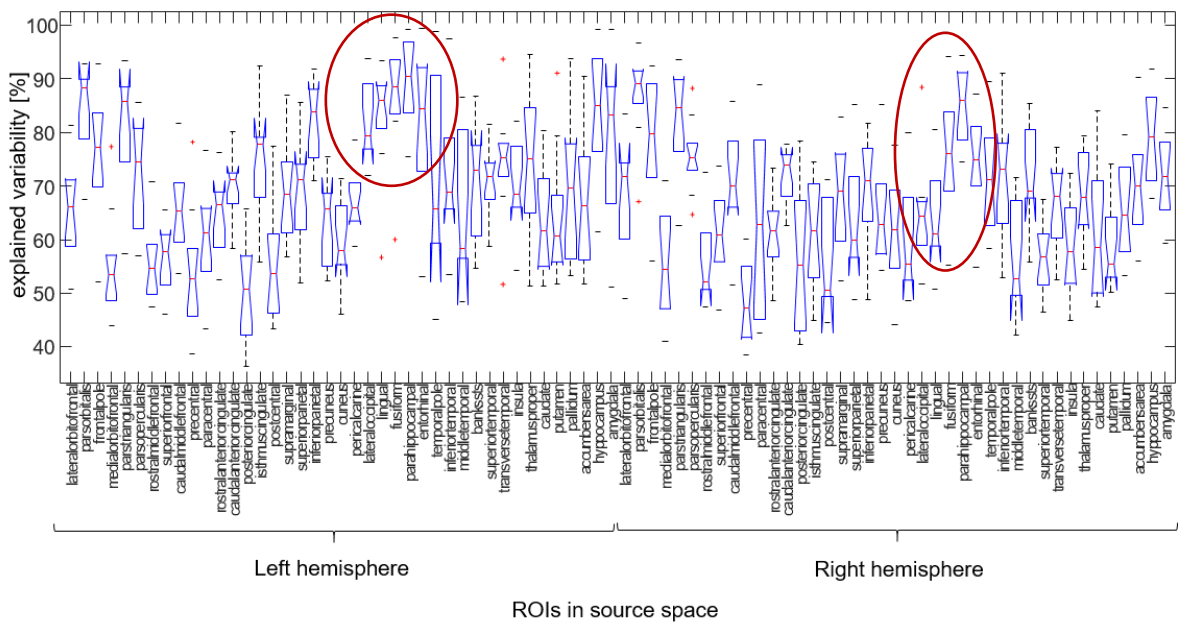
320 *Figure 4 (a) Proposed representative time-series (green) computed through SVD for the Right Lateral-occipital region. (b)*  
 321 *Norm (violet) and the first principal component (green) of the x- y- z- time-components (respectively, blue, orange and yellow*  
 322 *dotted lines) of the dipole lying in the centroid of the Right Lateral-occipital region. (c) Boxplot representing the latency in*  
 323 *ms for each subject for P100 and N170 estimated through the EEG GFP (blue), the representative time-series computed*  
 324 *through SVD (green) and the centroid time-series (red). (d) Boxplot representing the absolute difference in latency in ms for*  
 325 *each subject for P100 and N170 estimated between the EEG GFP and the representative time-series computed through SVD*  
 326 *(green) and the centroid time-series (red).*

327 We then computed the values of the explained variance (average among trials) of each of the 82  
 328 representative time-series summing up the information content of the ROIs for all the subjects (Figure 5 panel  
 329 (a)). The majority of the brain areas expected to be involved in face perception (red circles in Figure 5) show  
 330 higher explained variance. In Figure 5 panels (b) and (c), we report the histogram containing all the explained  
 331 variances for all the trials for sub#1 fitted against the generalized extreme value distribution [43]. For instance,  
 332 the average value of the location parameter was 94% for the left lateral occipital cortex and 70% for the right  
 333 lateral occipital cortex in sub#1.

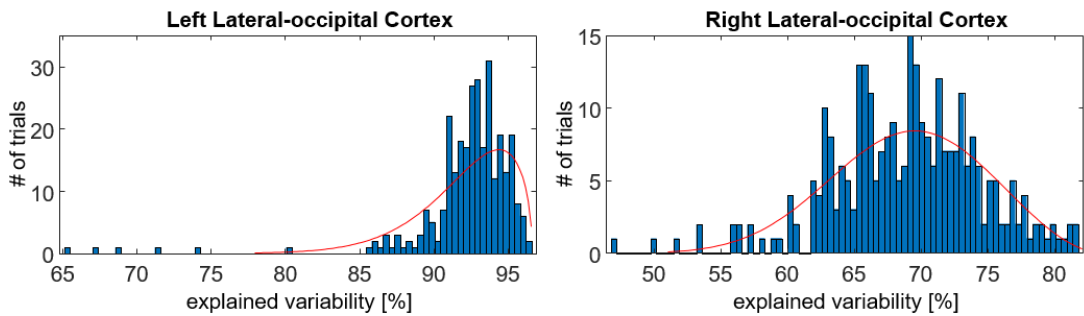
334 Finally, after computing the |iPDC| values during the first 500 ms after the stimulus, we compared the values  
 335 of the outflow from each ROIs at N170 among the reconstructions based on SVD, the selection of the centroid for  
 336 each ROI and the selection of the time-series containing the maximum power for each ROI [30]. The connectivity  
 337 patterns between the different cortical regions were summarized by representing the total outflow from a cortical  
 338 region toward the others, generated by the sum of all the statistically significant links obtained by application of  
 339 the iPDC to the cortical waveforms (with their values). The total outflow for each ROI is represented by a sphere  
 340 centered on the cortical region, whose radius is linearly related to the magnitude of all the outgoing directed  
 341 links to the other regions. Such information is also coded through a color scale. The greatest amount of  
 342 information outflow depicts the ROI as one of the main sources (drivers) of functional connections to the other  
 343 ROIs [74]. In Figure 6, we report the average values computed across subject of the outflow for the SVD-time-

344 series, the centroid time-series and the maximum-power time-series. We can note that the ROIs with the  
 345 maximum outflow (>95% percentile) were localized in the right lateral-occipital cortex, and in the inferior  
 346 temporal cortex (panel (a)) when using the SVD reconstruction, in mesial temporal cortex near the hippocampus  
 347 (panel (b)) when using the centroid time-series and in the right lateral-occipital cortex and in the right inferior  
 348 temporal cortex (panel (c)) when using the maximum-power time-series. In the literature, the generation of N170  
 349 was proposed to be attributed to neural sources in lateral, basal temporal, and extrastriate occipital cortices [70]  
 350 [75] [76] [77] [78] [79], to the fusiform gyrus of the inferior temporal cortex [80] in recognition of faces, which is  
 351 in accordance with our estimation through the SVD reconstruction. The SVD reconstruction results in a precise  
 352 and less blurry localization of the major drivers for the proposed VEP.

353



(a)

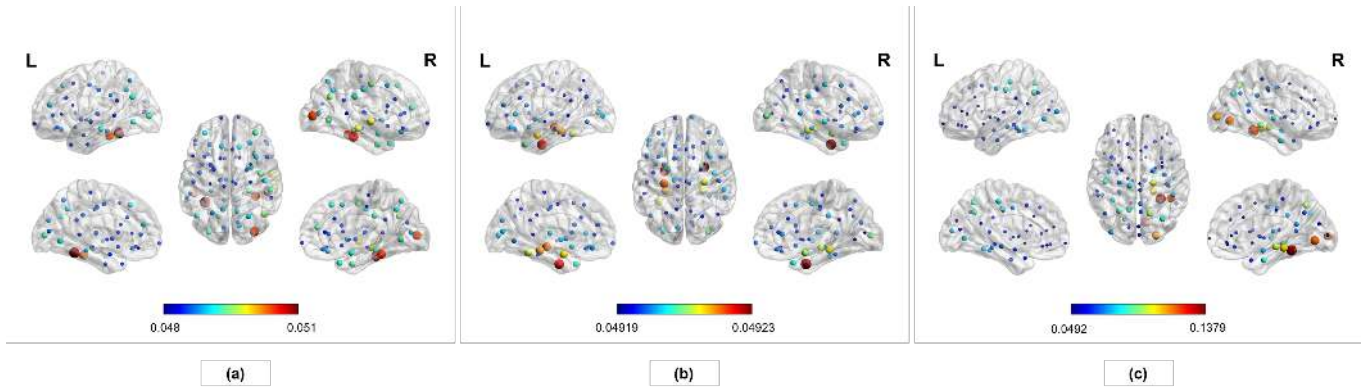


(b)

(c)

354

355 *Figure 5. VEP: (a) Boxplot representing the percentage of explained variability for the proposed representative time-series*  
 356 *for each ROI computed through SVD for all the subjects. Red circles highlight the ROIs that are mainly involved in the VEP.*  
 357 *(b) Histogram representing the percentage of explained variance in the representative subject (sub #1) for all the time-series*  
 358 *representing the left lateral-occipital brain region. (c) Histogram representing the percentage of explained variance in sub #1*  
 359 *for all the time-series representing the right lateral-occipital brain region.*



360

361 *Figure 6 VEP: Mean outflow across subjects computed from iPDC matrix for (a) the SVD time-series, (b) the centroid time-*  
 362 *series and (c) the maximum-power time-series. Nodes dimension and colour identify the value of the outflow.*

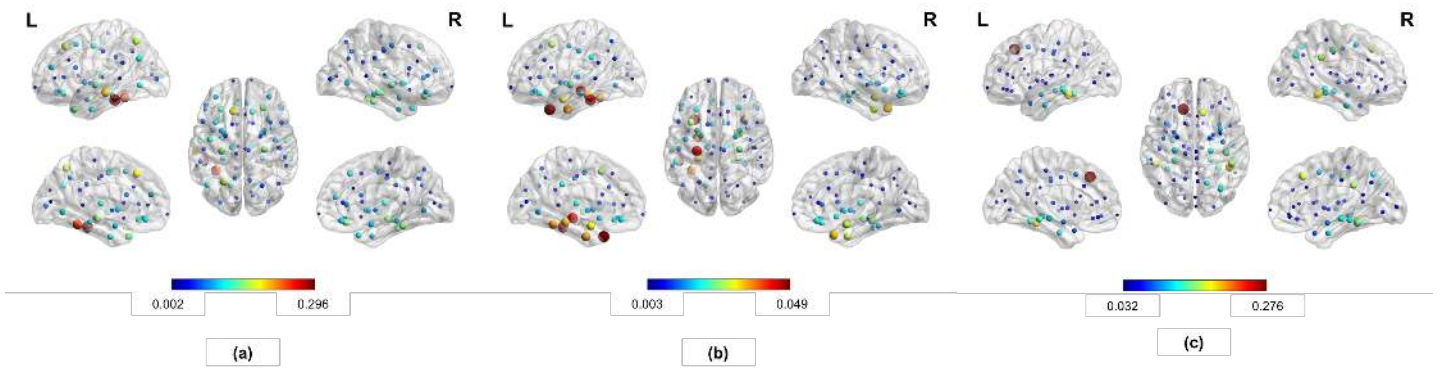
363

364 *Application on interictal spikes*

365 For each epileptic patient, we applied our method to compute the representative time-series for each ROI.  
 366 First, we evaluated if the frequency distribution did not significantly differ passing from the scalp EEG to our  
 367 inverse representation. The Mann-Whitney U-test confirmed that the relative power distributions between scalp  
 368 EEG and our inverse representation were not different in each frequency band for each patient ( $p > 0.95$ ). After  
 369 that, in order to compare the power of localization among the SVD time-series, the centroid time-series and the  
 370 maximum-power time-series, we selected 7 patients with anterior-mesial temporal lobe epilepsy with ILAE class  
 371 I after surgery, i.e., completely seizure free, no auras [81], in which part of the left temporal lobe was removed.  
 372 For each patient, after computing the iPDC matrices, we estimated the outflow of information from each ROI  
 373 during the advent of the spike. In **Figure 7** we report the mean outflow across patients computed with the SVD-  
 374 time-series (panel (a)), the centroid time-series (panel (b)) and the maximum-power time-series (panel (c)). The  
 375 ROIs with the value of the outflow above the 95% percentile, considered to be the main drivers during the advent  
 376 of the spikes are: left fusiform, middle-temporal brain areas for the SVD time-series, left temporal-pole brain areas  
 377 near the hippocampus for the centroid time-series and left inferior frontal brain areas for the maximum-power  
 378 time-series. The first two methods correctly identified the left temporal lobe, but for the centroid time-series we  
 379 can note that the range of outflow values (colorbar in panel (b)) is almost 10 times smaller compared to the one  
 380 of the SVD time-series (colorbar in panel (a)), thus, the resolution obtained exploiting the SVD resulted to be  
 381 higher. We used the postoperative structural MRI as validation for the localization of the generators of the  
 382 interictal epileptic discharges, the area removed from the surgery was the left anterior temporal lobe for all the  
 383 7 patients classified as good outcome. Moreover, considering all the patients, we computed the laterality index  
 384 defined as in [35] to assess whether this group of patients had more summed outflow ipsilateral or contralateral  
 385 to the epileptic source. We found that 7 out of 7 patients had a greater ipsilateral outflow exploiting the SVD time-  
 386 series, whereas 4 out of 7 exploiting the centroid time-series. In addition, we computed the mean efficiency of  
 387 the network across patients. Efficiency is a measure of how efficiently each node exchanges information. Using  
 388 the SVD time-series we found that the most efficient nodes of the network (with values above the 95% percentile)



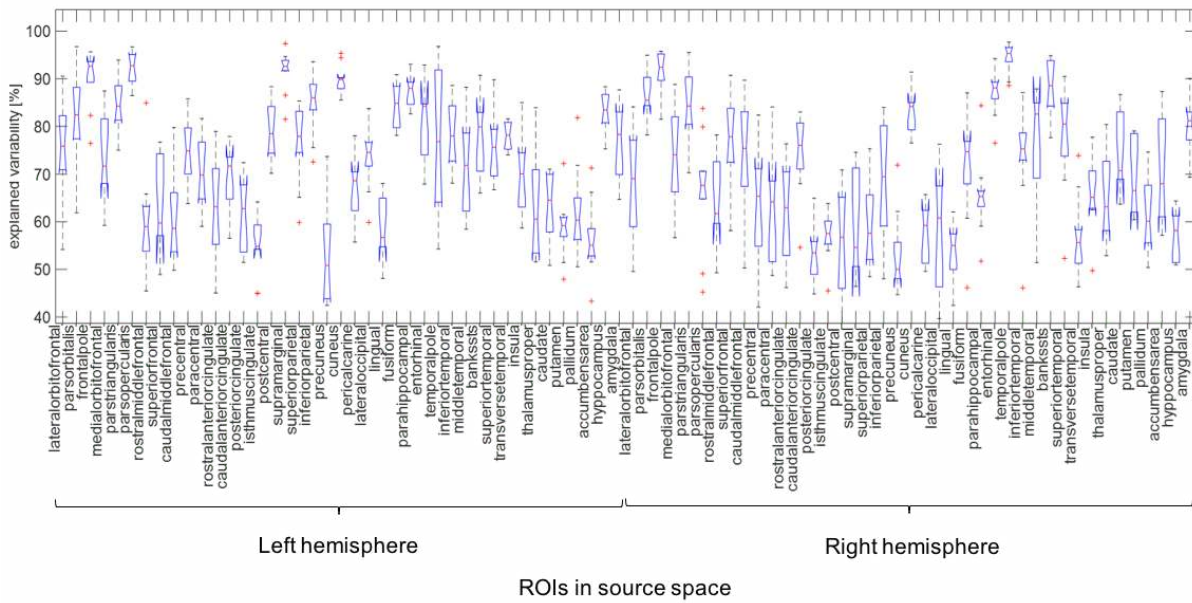
389 were the left fusiform and the left middle-temporal brain areas, the same brain areas labeled as main drivers by  
390 the outflow measure. Brain regions having high efficiency suggest the existence of a high level of efficiency in  
391 communicating with the rest of the brain during the advent of the spike [82].



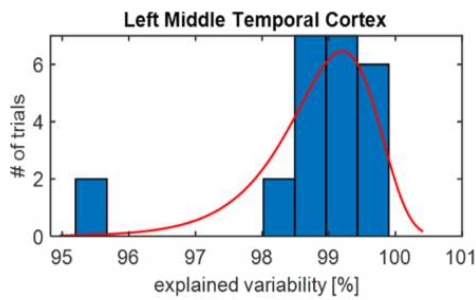
392

393 *Figure 7 Interictal spikes: Mean outflow across good-outcome patients with left temporal lobe epilepsy computed from iPDC*  
394 *matrix for (a) the SVD time-series, (b) the centroid time-series and (c) the maximum-power time-series. Nodes dimension and*  
395 *color identify the value of the outflow.*

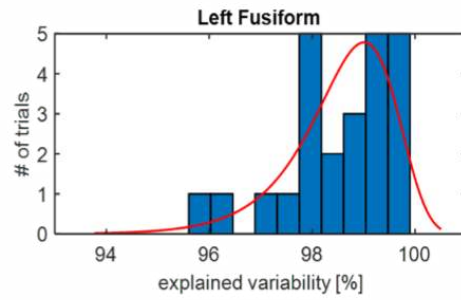
396 Finally, we computed the values of the explained variance of each of the 82 representative time-series  
 397 summing up the information content of the ROIs in all the trials/epochs for each subject (Figure 8). Each obtained  
 398 histogram was fitted against the generalized extreme value distribution [83]. The average value of the location  
 399 parameter  $\pm$  scale parameter was  $75\% \pm 15\%$ . Considering that we are trying to summarize the content of three  
 400 different time-series in a unique signal, explaining more than 60% of the variance of all the dipoles in a ROI means  
 401 being able to capture and describe at least the information contained in two out of three components. The data



(a)



(b)



(c)

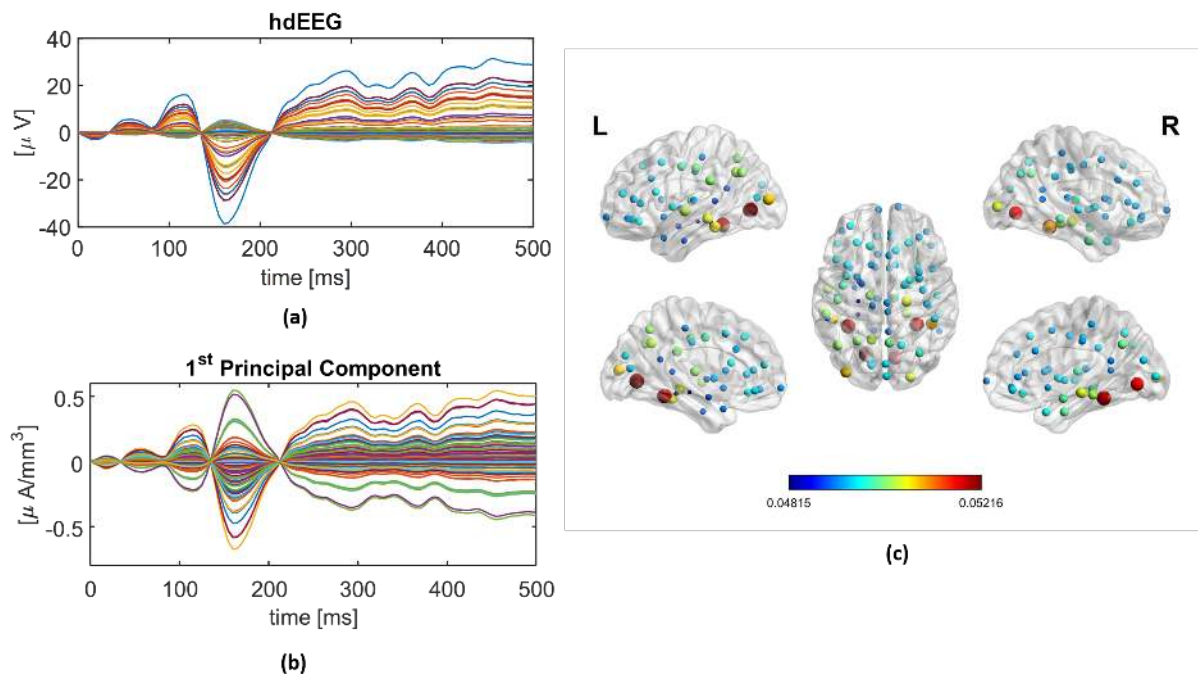
Figure 8 Interictal spikes: Boxplot representing the percentage of explained variability for the proposed representative time-series for each ROI computed though SVD for all the subjects. (b) Histogram representing the percentage of explained variance in the representative subject (sub #1) for all the time-series representing the left middle temporal cortex. (c) Histogram representing the percentage of explained variance in sub #1 for all the time-series representing the left fusiform brain region.

402 loss in a dimensionality reduction is unavoidable, but the fraction of the variance of the original data explained  
 403 with our one-dimension representation seems to be a good achievement.

404  
 405 *Application on simulated data*

406 In Figure 9 (panel (a)), the simulated 128 hdEEG time-courses averaged among the 20 trials for one of the 13  
 407 simulated subjects are shown. These hdEEG signals were the input of the LAURA algorithm to estimate the source

408 waveforms. The obtained SVD time-series averaged among the 20 trials for the same simulated subject of panel  
 409 (a) are reported in panel (b). After computing the  $|iPDC|$  values during the first 500 ms after the stimulus, we  
 410 compared the values of the outflow from each ROIs at N170 for all the simulated subjects. The ROIs with the  
 411 maximum outflow (>95% percentile) were consistently localized in the right lateral-occipital cortex, and in the  
 412 inferior temporal cortex as imposed by the simulation. The average outflow across all simulated subjects is  
 413 displayed in Figure 9 (panel (c)).



414  
 415 *Figure 9 Simulated VEP: (a) 128 high-density EEG time-courses and (b) ROI time-series computed through SVD average*  
 416 *among trials in a representative simulated subject, and (c) mean outflow across all simulated subjects computed from iPDC*  
 417 *matrix for the SVD time-series. Nodes dimension and colour identify the value of the outflow.*

#### 418 CONCLUSION AND DISCUSSION

419 With the final aim to improve connectivity estimation, we proposed a method able to overcome both the  
 420 dipole orientation problem and to sum up of the information of different solution points in the same region of  
 421 interest. The proposed projection method based on singular value decomposition sums up the information carried  
 422 by hundreds of 3-D time-series in a unique 1-D signal representing most of the variability of the sources in each  
 423 region of interest. Thanks to the orthogonality constraints ( $U$   $V$  are orthogonal matrices and  $S$  is a diagonal matrix),  
 424 the solution of SVD is unique and can be considered a reliable way for dimensionality reduction. The amplitude  
 425 of the representative signal computed as the first orthonormal vector of the unitary matrix  $U$  is by definition  
 426 independent on the original signal amplitudes. Thus, this solution overcomes a major drawback of the common  
 427 procedure of averaging the dipoles, namely drastically reduced amplitudes after averaging all the dipoles in the  
 428 same region of interest. Dealing with smaller amplitudes may distort the results of the connectivity estimation  
 429 because it involves computing of the inverse of the matrix containing the data [23] [84].

430 Additionally, we proposed a method able to create a *population* signal that summarizes the sources activity in  
 431 each region of interest (ROI) giving an indication of the global explained variance and considering all gray matter  
 432 solution points in the brain. In the majority of previous studies, a few voxels are selected for each ROI, for example

433 the most active voxels, and afterwards the information carried by these most active voxels is summarized in a  
434 unique signal by a decomposition method. Indeed, in [32] [33], the authors defined the ROIs by carefully selecting  
435 voxels corresponding to cortical areas that showed significant differences in the gamma-band range. For analyzing  
436 the information transfer between the identified regions of interest in source space through partial-directed-  
437 coherence, a multivariate autoregressive model was fitted to the time series revealed by the inverse solution at  
438 each ROI. To overcome the problem that each current source density consists of three directions (X, Y and Z), they  
439 computed the first principal component of each triplet. In our work, we aimed to create a population signal  
440 directly from the activity of all the voxels contained in the same ROI without introducing a priori condition to  
441 select specific points/areas. Also in [41], an fMRI connectivity analysis approach combining both principal  
442 component analysis (PCA) and Granger causality method was proposed to study directional influence between  
443 functional brain regions, but before applying this combined measure, the authors selected only the activated  
444 brain regions/voxels with BrainVoyager QX.

445 Moreover, the computational cost should also be considered as it influences the usefulness of the method in  
446 practice. The computational cost of singular value decomposition is much lower than the computational cost of  
447 other approaches based on the canonical polyadic decomposition [85]. We also showed that the projection  
448 method based on SVD provides robust results for visual evoked potentials and epileptic spikes. The results have  
449 also been confirmed by simulations. Furthermore, by analysing the frequency content of the proposed time-series  
450 and comparing its features with the centroid time-series, the signal based on the SVD seemed to both resemble  
451 the EEG scalp features and to prevent to deal with signals with too low amplitudes for the subsequent connectivity  
452 estimation. The novelty of the SVD method also lies in the fact that it exploits the information of the overall  
453 population of dipoles in each ROI instead of considering only one time-series as representative of the complex  
454 activity pattern in a given brain region. Despite the lack of availability of an objective ground truth in both  
455 estimating the source activities and the causal interactions among them, observing the dynamics and the  
456 orientation of the dipoles over time in visual evoked potential and epileptic spikes seems to confirm the existence  
457 of a principal component that accounts for most of the variability in the data.

458 While the proposed method is computationally cheap and easy to implement, it relies on certain ad-hoc  
459 assumptions and constraints that can influence the accuracy of the results. The first assumptions are imbedded  
460 in the source localization method used to solve the inverse problem. Here, we used the linear inverse solution  
461 LAURA which assumes that the strength of each source falls off with the reciprocal of the cubic distance for vector  
462 fields and with the reciprocal of the squared distance for potential fields, according to Maxwell's laws of  
463 electromagnetic field [8]. Other assumptions might lead to different results. The second constraint lies in the  
464 definition of the regions of interest in the parcellation of the brain. Here, we used anatomic ROI definitions as  
465 proposed in previous studies [28] [69] [34], which might lead to wrong connectivity estimations in cases where  
466 estimated sources cross anatomical boundaries or when distinct sources are located in the same anatomical  
467 region [7]. Anatomical segmentation is appropriate in structures that are anatomically well defined, but are less  
468 ideal in areas such as the frontal and parietal cortices, where there is the risk of mixing temporal signals into  
469 heterogeneous ROIs [86]. Analysing the patterns and the frequency content of the final waveforms computed

470 through SVD, e.g., Fig. 2, and checking the explained variability of each singular vector, e.g., Fig.5 and Fig.8, can  
471 lead the user to choose the most suitable parcellation.

472 Since the results may be influenced by the choice of the algorithm for estimating the source waveforms and  
473 from the brain parcellation, there are other approaches to define EEG networks that circumvent the issue of how  
474 to best segment the source maps into ROIs by explaining the EEG in terms of a discrete set of causally interacting  
475 clusters [87]. While such direct approaches are theoretically appealing since they are based on a generative model  
476 of how the data are probabilistically produced, they also rely on several a-priori assumptions and include many  
477 parameters, leading to significant computational costs. The main assumptions in one direct approach [87] are  
478 that the dynamics of the sources can be modelled as random fluctuations of a small number of mesostates  
479 interacting according to a full Dynamical Causal Network that can be estimated and the dynamics of the  
480 mesostates can switch between multiple approximately linear operating regimes stable over finite periods of  
481 time. Critically, this model accommodates constraints on the number of meso-sources (a meso-source represents  
482 the mean field approximation to its underlying neuronal population dynamics), while retaining the flexibility of  
483 distributed source models in explaining the data [7]. For experimental situations in which there is some a priori  
484 belief that there are multiple approximately linear dynamical regimes, this direct approach provides a natural  
485 modelling tool [87].

486 Whether applying a direct method based on Bayesian statistics or a two-stage method, as the one proposed  
487 in this work, depends on the user hypothesis and the final application. On the one hand, Bayesian approaches  
488 provide a natural and principled way of combining prior information with the data, within a solid decision  
489 theoretical framework, but it comes with a high computational cost, and user prior assumptions have to be  
490 translated into a mathematically formulated prior. Posterior distributions can be heavily influenced by these  
491 priors. On the other hand, two-stage approaches do not need to define priors and they are less computational  
492 demanding, but they may be influenced by the choice of the algorithm for estimating the source waveforms and  
493 from the anatomical segmentation used to define the ROIs. Our intention was to estimate source activity in the  
494 whole brain without any a priori assumption about the generative model of how the data are probabilistically  
495 produced. In our opinion, such an approach is preferred in studies that aim to compare and combine the effective  
496 connectivity among ROIs with the structural connectivity estimated by diffusion MRI in the same framework.

497 FUNDING: This study was supported by the Swiss National Science Foundation (Grant No. CRSII5-170873 to PH, PvM, GP, SV and CMM;  
498 Grant No. 320030\_159705 to CMM; Grant No. PP00P1\_157420 to GP; No. 320030-169198 to SV), by the National Centre of Competence in  
499 Research (NCCR) "SYNAPSY–The Synaptic Basis of Mental Diseases" (NCCR Synapsy Grant No. 51NF40-158776 to PH and CMM), by the  
500 Foundation Gertrude Von Meissner (to SV), and by the European Union's Horizon 2020 research and innovation program under the Marie  
501 Skłodowska-Curie grant agreement (Grant No. 660230 to PvM).

502 CONFLICT OF INTEREST: The authors declare they have no conflict of interest.

503 ACKNOWLEDGMENT: The authors would like to thank the anonymous reviewers for their valuable comments and suggestions to improve  
504 the quality of the paper.

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506

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