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Estimation of High Velocities in Synthetic Aperture Imaging: I: Theory

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Abstract—The paper describes a new pulse sequence design and estimation approach, which can increase the maximum detectable velocity in synthetic aperture (SA) velocity imaging. In SA N spherical or plane waves are emitted, and the sequence is repeated continuously. The N emissions are combined to form a High Resolution Image (HRI). Correlation of HRIs is employed to estimate velocity, and the combination of N emissions lowers the effective pulse repetition frequency by N . Inter-leaving emission sequences can increase the effective pulse repetition frequency to the actual pulse repetition frequency, thereby increasing the maximum detectable velocity by a factor of N . This makes it possible to use longer sequences with better focusing properties. It can also increase the possible interrogation depth for vessels with large velocities. A new cross-correlation vector flow estimator is also presented, which can further increase the maximum detectable velocity by a factor of three. It is based on Transverse Oscillation (TO), a pre-processing stage, and cross-correlation of signals beamformed orthogonal to the ultrasound propagation direction. The estimator is self-calibrating without estimating the lateral TO wavelength. This paper develops the theory behind the two methods. The performance is demonstrated in the accompanying paper for convex and phased array probes connected to the SARUS scanner for parabolic flow for both conventional and SA imaging.

I. INTRODUCTION

Synthetic Aperture (SA) velocity estimation was introduced in 2001 [1], [2]. Here a repeated sequence of diverging emissions was used for reconstructing a continuous imaging sequence usable for velocity and vector velocity estimation. This resulted in highly accurate velocity estimates using directional beamforming [3] with relative standard deviations down to 0.36% and very fast in-vivo velocity images [2]. Only 24 emissions were used for imaging the carotid artery potentially yielding frame rates up to 10 kHz at a pulse repetition frequency f_{prf} of 24 kHz. Such continuous sequences

can also be used with plane wave imaging, and the possibility of infinite observation times has been used to estimate very slow flow in the brain [4], [5] and to derive functional brain activity images. The main possibilities and advantages have been demonstrated by a number of research groups and are described in review papers [6], [7], [8].

There is, however, one disadvantage of SA as imaging sequences with a number of emissions have to be acquired to attain a high resolution and low side lobes. The effective pulse repetition frequency $f_{prf,eff}$ is the emissions pulse repetition frequency f_{prf} divided by the emissions sequence length N , i.e. $f_{prf,eff} = f_{prf}/N$. The highest velocity detectable is directly proportional to $f_{prf,eff}$ and is therefore reduced by a factor N , which can lead to erroneous estimates for large velocities in the major arteries or in the heart. The solution is often to employ a very high f_{prf} , which generates massive amounts of data, precludes the investigation of deep vessels, and often creates probe temperature problems and limitations on the emitted fields.

Several factors influence the resolution limit and contrast for images, which also affects the velocity range possible to estimate. The resolution is determined by the F-number of the system, which is determined by the width of the aperture or rather the number of elements combined in reception, and the spread of the emissions in either angle for plane wave emissions or space for spherical emissions. Having a high number of emissions and receiving elements yield a good contrast and resolution as demonstrated in [9] for plane waves and in [10] for spherical waves. A long sequence will, however, reduce the effective $f_{prf,eff}$, and the effective frame rate of fully independent images is also reduced by a factor of N . In velocity imaging the maximum detectable velocity is usually proportional to $\lambda f_{prf}/4$ for phase estimation methods before aliasing takes place [11], where λ is the wavelength. The maximum detectable velocity is, thus,

also reduced by N , and obtaining both a high contrast for separating out adjacent vessels and a high velocity range seems unbreakable in SA velocity imaging. A choice must therefore be made between looking at low velocity flow in small vessels with a long sequence or having a shorter sequence for estimating fast flow as described in [12]. One approach to break the aliasing limit is to use cross-correlation methods [13], [14], [15] rather than the autocorrelation method [16] limited to motions within $\pm\lambda/2$. The largest velocities are, however, still limited by rapid de-correlation of the data. An other approach is to use a staggered pulse repetition method for ultrafast imaging of high velocities [17], which is restricted to be used for anti-aliasing in phase shift estimators.

This paper describes two methods for increasing the aliasing limit to obtain both a high contrast using a long sequence and at the same time obtain a high aliasing limit. The first improvement is a new sequence design presented in Section II, which maintains the highest possible $f_{prf,eff}$ equal to f_{prf} . This maintains a high peak detectable velocity with a reduced amount of data and makes interrogation of deep lying vessels with a high peak velocity possible. The approach can be combined with any velocity estimator.

Secondly a new estimator for the transverse oscillation (TO) approach is introduced [18], [19], [20], where cross-correlation is used. It can increase the detectable maximum velocity by a factor of three breaking the aliasing limit as demonstrated in the accompanying paper [21]. The lateral oscillation period can also be controlled dynamically during receive processing to increase or lower it depending on the flow velocities investigated. The estimator is derived in Section IV.

The accompanying paper [21] presents Field II simulations [22], [23] and measurements using the SARUS experimental scanner [24] for revealing the performance of the methods.

II. SYNTHETIC APERTURE FLOW IMAGING

Synthetic aperture imaging (SAI) insonifies a whole region of interest using spherical waves [25], [6] as illustrated in Fig. 1. A virtual source in the form of a spherical or plane wave is emitted. The spherical virtual source can have its origin behind or in front of the array and can use one or a number of elements combined [26], [27], [28]. A plane emission is defined by its tilt angle compared to the array, and all elements are usually needed in transmit. A low resolution image (LRI), $L^{(1)}$, is beamformed after each emission, and this is dynamically focused during the receive beamforming based on the placement of the transmitted wave. A new wave is

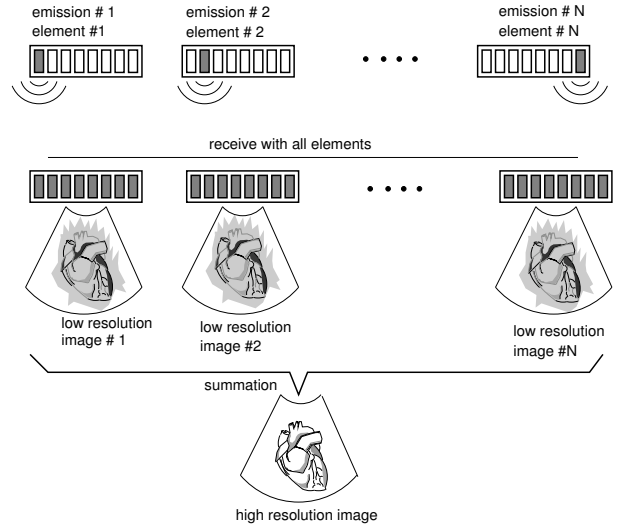


Fig. 1. Visualization of SA imaging. Spherical waves are emitted from a number of elements and the scattered signals are received on all the elements. A low resolution image is beamformed for each emission, and they are combined to yield a high resolution image with dynamic focusing in both transmit and receive (from [1]).

then emitted and the received data beamformed to yield $L^{(2)}$. The process is repeated for all N emissions in the sequence and all low resolution images are combined to yield a high resolution image (HRI), $H^{(N)}$, which is dynamically focused in both transmit and receive. The image is, thus, reconstructed over a number of emissions, and will therefore be affected by motion of the interrogated volume.

This is depicted in Fig. 2, which shows the point spread functions (PSF) for the individual LRIs and the corresponding HRIs for a short 2-emission sequence. The scatterer imaged is moving towards the probe by a distance of $\Delta z = v_z T_{prf} = v_z / f_{prf}$ between pulse emissions, where v_z is the axial velocity. The PSFs for the LRI are tilted towards the emitting source and are therefore different for each LRI in the sequence. The combined HRIs are also different, but it should be noted that the only difference for the same combination of LRIs $L^{(n-3)} + L^{(n-2)} = H^{(n-2)}$ and $L^{(n-1)} + L^{(n)} = H^{(n)}$ is the shift in position. These two HRIs can therefore be correlated to find the motion, and this is the key feature used in SA and plane wave flow imaging as was noticed and introduced by Nikolov and Jensen [1], [25], [2].

This ordering of the processing yields continuous data everywhere in the image, which makes it possible to track targets continuously and have very long echo canceling filters and averaging over as long time as the correlation functions are coherent [2], [29], [30]. The velocity can, thus, be found from any of the methods mentioned in [31]. Beamforming can also be performed

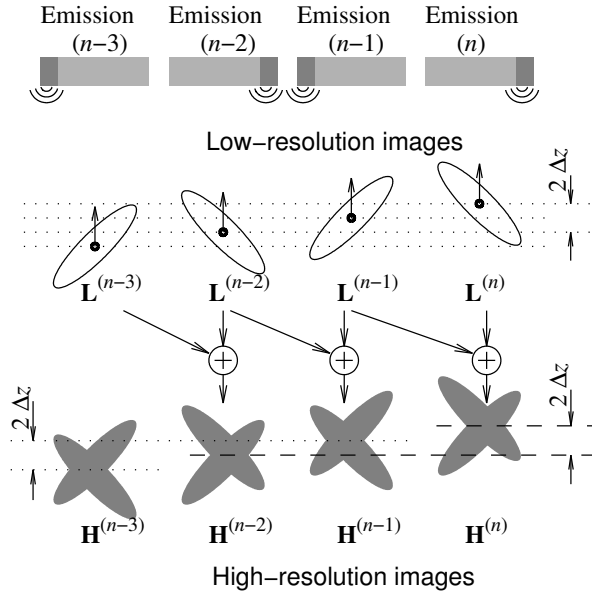


Fig. 2. SA sequence used for flow estimation using a two emission sequence. The top row shows the emitting virtual sources, the second row shows the point spread function for the LRIs, and the last row visualizes the resulting HRIs. Similar HRIs can be correlated to estimate the velocity and the repeated sequence yields continuous data for the whole image (from [2]).

in any direction and the flow can thus be tracked to minimize de-correlation effects from velocity gradients.

The standard method for SA flow imaging is shown in Fig. 3. A single HRI is created from the same colored block of LRIs and the correlation for finding velocities are between HRIs with a time difference of $T_{prf}N$. The averaging is across a number of HRI correlations to yield a low SD velocity estimate.

III. EMISSION SEQUENCE DESIGN

The largest velocity detectable for both spherical and plane wave SAF $v_{z,max}$ is determined by the time interval between the two received signal that are correlated, and is for an autocorrelation (phase shift) estimator given as

$$v_{z,max} = \frac{\lambda}{4} f_{prf,eff}. \quad (1)$$

Keeping $f_{prf,eff}$ high, thus, ensures the highest detectable velocity. Ideally the emissions for velocity estimation should be adjacent in time. This is precluded in a SAF system with a sequence length N so $f_{prf,eff} = f_{prf}/N$. The sequence should therefore be modified, so that HRIs are only one emission apart at the same time as the sequence length N is maintained. This can be accomplished by inter-leaving two sequence. The normal sequence is given by

$$\begin{matrix} v_1^{(1)} & v_2^{(1)} & v_3^{(1)} & v_4^{(1)} & \dots & v_N^{(1)}, \dots \\ v_1^{(2)} & v_2^{(2)} & v_3^{(2)} & v_4^{(2)} & \dots & v_N^{(2)} \end{matrix}$$

where $v_x^{(1)}$ is velocity emission sequence number 1 for spherical or plane wave source x . The source is here a virtual ultrasound source emission [27] or a plane wave in a given direction. Data are then beamformed for all emissions $v_1^{(1)}$ to $v_N^{(1)}$ to create high resolution data $H^{(1)}$, and for emissions $v_1^{(2)}$ to $v_N^{(2)}$ to create high resolution data $H^{(2)}$. The two high resolution data sets are then correlated to estimate the velocity as shown in Fig. 3.

The suggested new sequence interleaves two sequences as shown in Fig. 4:

$$v_1^{(1)} \quad v_1^{(2)} \quad v_2^{(1)} \quad v_2^{(2)} \quad \dots \quad v_N^{(1)} \quad v_N^{(2)}$$

The two high resolution data sets are beamformed, but $H^{(1)}$ and $H^{(2)}$ are now only one pulse emission apart, and this yields a correlation estimate with the highest possible maximum velocity for both the axial and lateral components. The correlation functions can be averaged over a number of correlation pairs only limited by the acceleration of the flow. The length of averaging is limited by

$$aT < \sigma_v, \quad (2)$$

where T is the averaging interval, a is acceleration, and σ_v is the standard deviation on the estimate, which generally is dependent on T . This states that the correlation functions should be averaged as long as the peak position has not moved beyond the precision of the estimate. After this limit the correlation will start to degrade.

This new sequence gives the optimal data for high velocity estimation, due to the shortest temporal distance between the high resolution data. It breaks the link between sequence length N and maximum detectable velocity, and it can include long sequences with an optimal resolution and side lobe level for detecting small vessels. The data sequence is continuous and can therefore be averaged over as long time as needed.

It can also be used for recursive SA imaging [32] as shown in Fig. 5. Here a new HRI is created after each emission regardless of the imaging length for the fastest possible imaging. The notation $HRI\ 2(2)\ 3(2)\ 4(2)\ I(4)$ indicates which set of emission are used. The first number is the emission (virtual source) from 1 to N in the sequence. The second number in parentheses is the sequence number used. So $3(2)$ is emission number 3 in the second sequence indicated by the light green color. It should be ensured that the same sequence of LRIs is used due to the distortion of the PSF, but after correlation the functions are similar and can be averaged to increase precision.

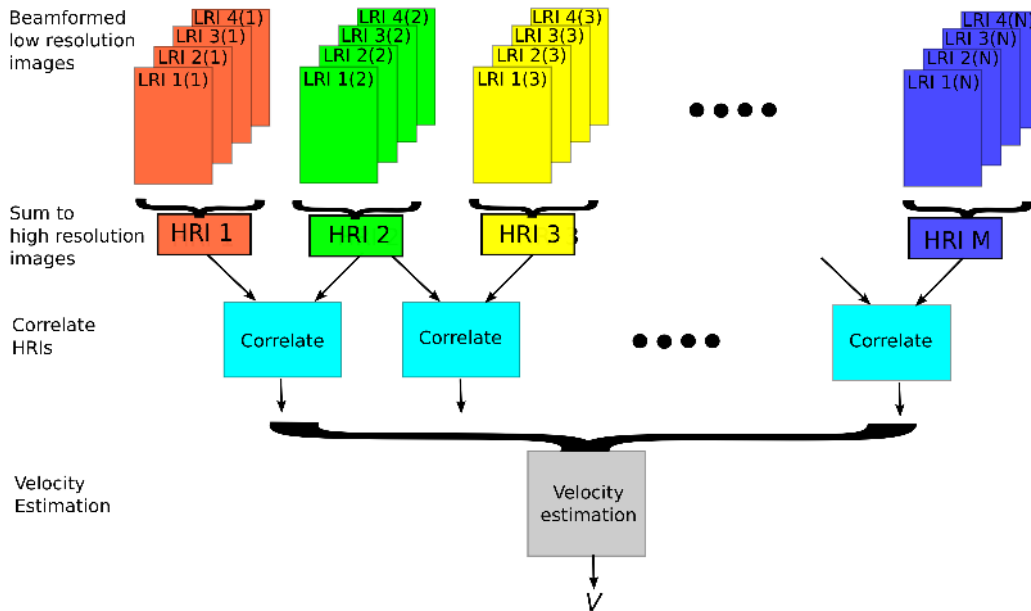


Fig. 3. Traditional SA sequence for velocity estimation. HRIs are created in blocks making the effective $f_{prf,eff}$ low. LRI 1(2) denotes low resolution image for emission 1 in high resolution sequence 2 (first emission in the green block).

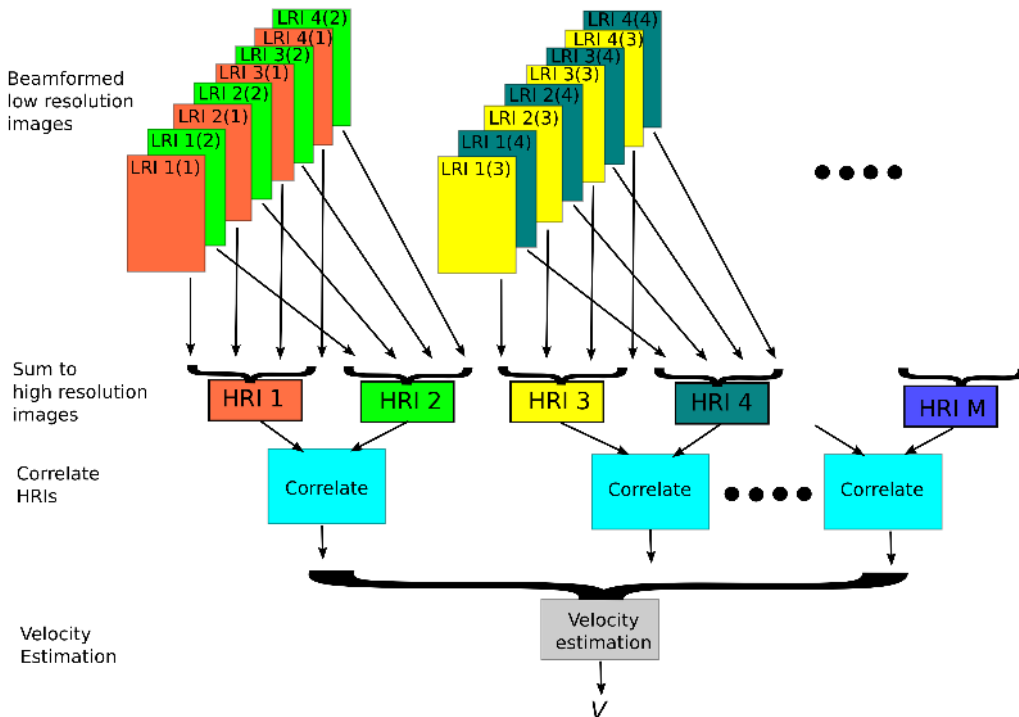


Fig. 4. Inter-leaved SA sequence where LRIs are repeated to minimize the distance between HRIs. The same colored LRIs are summed to yield one HRI. The effective $f_{prf,eff}$ is equal to the highest possible value due to the inter-leaving. Correlations in the blue boxes yield the same correlation function, which are then averaged to improve precision.

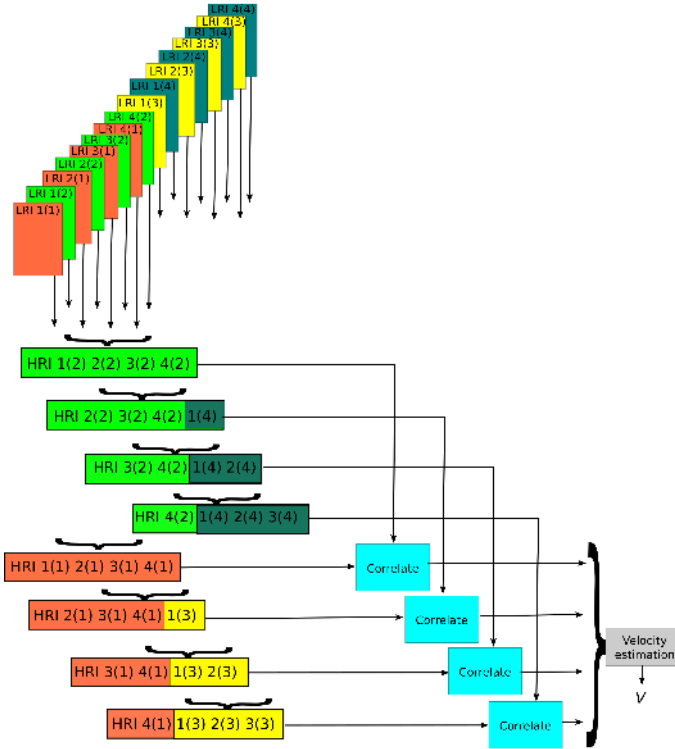


Fig. 5. Processing scheme for recursive SAF, where a new HRI is created after each pulse emission. *HRI 2(2) 3(2) 4(2) 1(4)* indicates which set of emission are used. The first number is the emission (virtual source), and the second number in parentheses is the sequence number used. So 3(2) is emission number 3 in the second sequence indicated by the light green color.

The PSF will be affected by the velocity and, thus, the motion between emissions. This will result in a de-correlations of the LRIs, which affects the PSFs as described in [33]. This results in a reduction in SNR and higher side-lobes, which affects the velocity estimates. The length of the SA sequence will, therefore, be limited by the time over which the LRIs can be considered correlated. The correlation is affected by the interleaving as the sequence length is essentially doubled, which can lead to a drop in amplitude compared to a non-interleaved sequence. It has, however, been shown that the PSF can be fully recovered, if the velocity vector can be reliably estimated [33], [34], which is more likely for an interleaved sequence. The interleaving can also affect the variance of the estimates, as the length for acquiring data is doubled, thus reducing the averaging in half. The averaging time duration is restricted by the acceleration as given in (2), but often the estimates are more influenced by the echo canceling filter than limited by the averaging duration.

A. Echo canceling

Echo canceling can be performed on the HRIs using the standard methods for removing stationary tissue signals [11]. It is benefited from having continuous data everywhere in the image [6], and a simple approach is to take the mean value across all HRIs and subtract this from the individual HRIs as used in the accompanying paper. Other more advanced techniques based on e.g. decompositions [35], [36], [37], [38], [29], [39] can also be employed, when the continuous data is used as two interleaved high resolution sequences, if equidistant sampling of the data is a requirement. FIR and IIR filters can thereby be used, and the continuous data removes limitations from the initial response of the filters. SVD and other decomposition approaches can easily be adapted to handle the interleaving in one processing stage.

IV. DIRECTIONAL TRANSVERSE OSCILLATION USING CROSS-CORRELATION

The new sequence can be employed with any type of velocity estimation scheme based on correlation functions including autocorrelation [16], [40], cross-correlation [13], speckle tracking [15], directional beamforming [3], and Transverse Oscillation (TO) [18]. TO introduces a lateral oscillation in the ultrasound field by employing a two-peak apodization waveform during receive beam formation. It can be optimized by focusing a directional signal transverse to the ultrasound propagation direction (DTO) [41]. A Hilbert transform along this line is calculated to yield a complex signal usable for finding the sign of the transverse velocity. An autocorrelation estimator has been used to find the transverse velocity. This is limited to shifts less than quarter lateral wavelength, and the maximum velocity is given by [11]:

$$v_{x,max} = \frac{\lambda_x}{4} f_{prf}, \quad (3)$$

where λ_x is the lateral wavelength. This restriction on maximum velocity coming from employment of phase shift estimation can be alleviated by using a cross-correlation estimator, where the maximum velocity is only limited by the de-correlation of the involved signals [13], [11]. This can be used on the directional signal, but at beam-to-flow angles different from 90° , a significant oscillation from the axial motion will introduce a detrimental de-correlation. It can be seen from a model of the received signal. The received signal is $x(n, k, i)$ and its Hilbert transform along k is $y(n, k, i) = \mathcal{H}_k\{x(n, k, i)\}$, where \mathcal{H}_k denotes Hilbert transform along k . Here n is RF sample number, k is sample along the directional

signal, and i is emission number. The complex combined signal is [41]:

$$\begin{aligned} r_{sq}(n, k, i) &= x(n, k, i) + j\mathcal{H}_k\{x(n, k, i)\} \\ &= x(n, k, i) + jy(n, k, i). \end{aligned} \quad (4)$$

The received signals are Hilbert transformed in the temporal direction n , and a new directional beamformed signal formed $r_{sqh}(n, k, i)$ as:

$$r_{sqh}(n, k, i) = \mathcal{H}_n\{x(n, k, i)\} + j\mathcal{H}_n\{y(n, k, i)\}. \quad (5)$$

The signals can be modeled as [19], [41]:

$$\begin{aligned} r_{sq}(n, k, i) &= a \frac{1}{2} \left(\exp \left(j2\pi \left(\left(\frac{v_x}{\lambda_x} + \frac{2v_z}{\lambda} \right) iT_{prf} - \frac{k\Delta x}{\lambda_x} - f_0 \frac{n}{f_s} + \frac{2d}{c} f_0 \right) \right) \right. \\ &\quad \left. + \exp \left(j2\pi \left(\left(\frac{v_x}{\lambda_x} - \frac{2v_z}{\lambda} \right) iT_{prf} - \frac{k\Delta x}{\lambda_x} - f_0 \frac{n}{f_s} + \frac{2d}{c} f_0 \right) \right) \right) \\ r_{sqh}(n, k, i) &= a \frac{1}{2j} \left(\exp \left(j2\pi \left(\left(\frac{v_x}{\lambda_x} + \frac{2v_z}{\lambda} \right) iT_{prf} - \frac{k\Delta x}{\lambda_x} - f_0 \frac{n}{f_s} + \frac{2d}{c} f_0 \right) \right) \right. \\ &\quad \left. - \exp \left(j2\pi \left(\left(\frac{v_x}{\lambda_x} - \frac{2v_z}{\lambda} \right) iT_{prf} - \frac{k\Delta x}{\lambda_x} - f_0 \frac{n}{f_s} + \frac{2d}{c} f_0 \right) \right) \right), \end{aligned}$$

when assuming monochromatic signals. Here c is the speed of sound, Δx is the sampling interval along the lateral signal, a is the scattered amplitude, f_s is the temporal sampling frequency, $\Delta z = c/f_s$, and T_{prf} is the time between pulse emissions. The interrogation depth is d , and the two frequencies received from the axial and lateral motions are given by:

$$f_p = \frac{2v_z}{c} f_0 = \frac{2v_z}{\lambda}, \quad f_x = \frac{v_x}{\lambda_x}. \quad (6)$$

Two new signals are then formed from:

$$\begin{aligned} r_1(n, k, i) &= r_{sq}(n, k, i) + jr_{sqh}(n, k, i) \\ r_2(n, k, i) &= r_{sq}(n, k, i) - jr_{sqh}(n, k, i). \end{aligned}$$

The combined signal can be written as:

$$\begin{aligned} r_1(n, k, i) &= a \cdot \exp \left(j \frac{2\pi}{\lambda} (2v_z iT_{prf} - n\Delta z - 2d) \right) \\ &\quad \cdot \exp \left(j \frac{2\pi}{\lambda_x} (v_x iT_{prf} - k\Delta x) \right), \end{aligned} \quad (7)$$

and

$$\begin{aligned} r_2(n, k, i) &= a \cdot \exp \left(j \frac{2\pi}{\lambda} (2v_z iT_{prf} - n\Delta z - 2d) \right) \\ &\quad \cdot \exp \left(-j \frac{2\pi}{\lambda_x} (v_x iT_{prf} - k\Delta x) \right). \end{aligned} \quad (8)$$

Both r_1 and r_2 are influenced by the lateral and axial velocities, and this has previously been separated out using the fourth order autocorrelation estimators derived in [19], [41]. For a purely lateral velocity, there is no influence from the axial velocity, and the signals can be cross-correlated to find the spatial shift between two

emissions and thereby v_x . For other angles the estimation process will be distorted to not yield the correct v_x . This is for example addressed in directional beamforming [42], [43], which noted the same problem with the transverse correlation approach suggested by Bonnefous [44].

The axial velocity component can be removed by multiplying the two signals as suggested by Anderson [45]. This results in the signal:

$$\begin{aligned} r_{mult}(n, k, i) &= r_1^*(n, k, i) r_2(n, k, i) \\ &= a \cdot \exp \left(-j \frac{2\pi}{\lambda} (2v_z iT_{prf} - n\Delta z - 2d) \right) \\ &\quad \cdot \exp \left(-j \frac{2\pi}{\lambda_x} (v_x iT_{prf} - k\Delta x) \right) \\ &\quad \times \exp \left(j \frac{2\pi}{\lambda} (2v_z iT_{prf} - n\Delta z - 2d) \right) \\ &\quad \cdot \exp \left(-j \frac{2\pi}{\lambda_x} (v_x iT_{prf} - k\Delta x) \right), \\ &= a \cdot \exp \left(-j \frac{2\pi}{\lambda_x} (v_x iT_{prf} - k\Delta x) \right), \end{aligned} \quad (9)$$

where $r_1^*(\cdot)$ denotes complex conjugate. The multiplication, thus, removes the influence from the axial velocity, and the resulting signals can be directly correlated to

yield the velocity as:

$$\begin{aligned}
R_{12}(n, m) &= \sum_{i=1}^{N_e} \sum_{k=1}^{N_s} r_{mult}^*(n, k, i) r_{mult}(n, k + m, i + 1) \\
&= \sum_{i=1}^{N_e} \sum_{k=1}^{N_s} a \exp \left(j \frac{2\pi}{\lambda_x} (v_x i T_{prf} - k \Delta x) \right) \\
& a \exp \left(-j \frac{2\pi}{\lambda_x} (v_x (i + 1) T_{prf} - (k + m) \Delta x) \right) \\
&= a^2 \exp \left(j 2 \frac{2\pi}{\lambda_x} (v_x T_{prf} - m \Delta x) \right), \quad (10)
\end{aligned}$$

where N_e is the number of emissions, and N_s is the number of samples in the directional line. This correlation function has a global maximum for $m_p = v_x T_{prf} / \Delta x$, when a pulsed signal is used. The maximum can be found from the absolute value of the complex correlation function or from the real part of $R_{12}(n, m)$, where the last method gives the most precise determination. The peak value is found as an integer, which limits the precision. It can be increased by using parabolic interpolation by fitting a second-order polynomial to the three points around the peak value. An interpolated peak value is found by [46]:

$$m_{int} = m_p - \frac{\hat{R}_{12}(m_p + 1) - \hat{R}_{12}(m_p - 1)}{2(\hat{R}_{12}(m_p + 1) - 2\hat{R}_{12}(m_p) + \hat{R}_{12}(m_p - 1))} \quad (11)$$

to yield the interpolated estimate:

$$\hat{v}_{int} = \frac{m_{int} \Delta x}{T_{prf}}. \quad (12)$$

Similar expressions can also be found for the axial cross-correlation estimator.

This new estimator has a number of advantages over the autocorrelation approach. Only knowledge of T_{prf} and Δx are needed to get quantitative results. No calibration estimate of $f_x = 1/\lambda_x$, thus, has to be found as in [41]. Further, the velocity range is not restricted to spatial shifts between $-\lambda_x/2$ and $+\lambda_x/2$ as cross-correlation estimators have no inherent aliasing limit, apart from the de-correlation of signals from transverse beam modulation. This can potentially yield a much higher detectable velocity range, with a reduced beam-forming load compared to directional beamforming [42], [43]. This estimator design can also be used for making the transverse spectrum as described in [47].

The cross-correlation limit is determined by the time over which two received signals are correlated, which is determined by the width of the PSF compared to the motion $v_x T_{prf}$. In SAF the entire focusing is performed during the receive processing, and this can be adapted to the velocity investigated. The lateral oscillation wavelength can be increased by changing the apodization

function to have peaks closer to each other on the virtual aperture for high velocities, or they can be separated more to increase the lateral oscillation frequency for low velocity estimation. It is also possible to increase the lateral oscillation frequency by using a two-peak apodization in both transmit and receive focusing. An alternative approach is to use full dynamic focusing and then create the lateral oscillation in the frequency domain as suggested in [48], [49].

V. CONCLUSION

This paper has described two new methods for increasing the maximum detectable velocity of SA velocity imaging using spherical or plane waves. A new sequence design can increase the velocity limit by a factor N equal to the sequence length, and the new TO directional cross-correlation estimator can break the aliasing limit. It also has a higher aliasing limit by a factor 2-4 than for axial autocorrelation estimation as the lateral wavelength easily can be made 2-4 times larger than the axial wavelength [18]. The employment of a cross-correlation estimator instead of the autocorrelation approach further adds a factor of 3 as experimentally shown in the accompanying paper [21]. The combination of all these features makes it possible to estimate lateral velocity components $6N$ to $12N$ times higher than for axial velocity components in previous SA velocity sequences. The approach described in [3] used $N = 8$ and $f_{prf} = 3$ kHz to estimate peak velocities around 0.15 m/s using directional cross-correlation. The aliasing limit for an autocorrelation system would be 0.04 m/s. The same setup could translate to a peak detectable velocity of 4.6 to 9.2 m/s using the new scheme and estimator at 3 MHz. Increasing f_{prf} to 5 kHz for full cardiac imaging could lead to velocity range above 10 m/s; enough to detect jets from regurgitation in heart valves.

The interleaved approach is not restricted to use with the new DTO cross-correlation estimator, but can be used with any of the current velocity estimators used for axial and vectorial velocity estimation [31], [8] and still attain a factor of N increase in maximum detectable velocity.

The accompanying paper [21] investigates the methods using Field II simulations [22], [23] and measurements from the SARUS experimental scanner [24]. It is demonstrated that velocities of 0.5 m/s can be estimated for an f_{prf} of 450 Hz, which translates to 5.6 m/s at $f_{prf} = 5$ kHz, and in certain cases at $f_{prf} = 225$ Hz a velocity of 0.5 m/s could be estimated corresponding to 11.2 m/s at 5 kHz.

The method still has the advantage of continuous data, and the lowest velocity detectable is therefore

only limited by the duration over which data can be acquired for the position in the image. The velocity range therefore both cover high velocities in the major arteries, at the same time as low velocity flow in small vessels can be estimated from the same data.

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