

Evidence for a non-zero Λ and a low matter density from a combined analysis of the 2dF Galaxy Redshift Survey and cosmic microwave background anisotropies

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ABSTRACT

We perform a joint likelihood analysis of the power spectra of the 2dF Galaxy Redshift Survey (2dFGRS) and the cosmic microwave background (CMB) anisotropies under the assumptions that the initial fluctuations were adiabatic, Gaussian and well described by power laws with scalar and tensor indices of n_s and n_t . On its own, the 2dFGRS sets tight limits on the parameter combination $\Omega_m h$, but relatively weak limits on the fraction of the cosmic matter density in baryons Ω_b/Ω_m . (Here h is Hubble's constant H_0 in units of $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$. The cosmic densities in baryons, cold dark matter and vacuum energy are denoted by Ω_b , Ω_c and Ω_Λ , respectively. The total matter density is $\Omega_m = \Omega_b + \Omega_c$ and the curvature is fixed by $\Omega_k = 1 - \Omega_m - \Omega_\Lambda$.) The CMB anisotropy data alone set poor constraints on the cosmological constant and Hubble constant because of a 'geometrical degeneracy' among parameters. Furthermore, if tensor modes are allowed, the CMB data allow a wide range of values for the physical densities in baryons and cold dark matter ($\omega_b = \Omega_b h^2$ and $\omega_c = \Omega_c h^2$). Combining the CMB and 2dFGRS data sets helps to break both the geometrical and tensor mode degeneracies. The values of the parameters derived here are consistent with the predictions of the simplest models of inflation, with the baryon density derived from primordial nucleosynthesis and with direct measurements of the Hubble parameter. In particular, we find strong evidence for a positive cosmological constant with a $\pm 2\sigma$ range of $0.65 < \Omega_\Lambda < 0.85$, independently of constraints on Ω_Λ derived from Type Ia supernovae.

Key words: galaxies: clusters: general – cosmic microwave background – cosmology: miscellaneous – large-scale structure of Universe.

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1 INTRODUCTION

Until recently, cosmology was a subject starved of data, with poor or non-existent constraints on fundamental quantities such as the curvature of the Universe, the power spectrum of density irregularities and the cosmic densities in baryons, cold dark matter and vacuum energy. The situation has changed dramatically over the last few years. Following the discovery of the cosmic microwave background (CMB) anisotropies (Smoot et al. 1992) it was realized that many of the fundamental parameters of our Universe could be determined via accurate, high-resolution measurements of the CMB (e.g. Bond et al. 1994; Jungman et al. 1996). This has now become a reality through a number of exquisite ground-based and balloon experiments (see Halverson et al. 2001; Lee et al. 2001; Netterfield et al. 2002). Constraints on cosmological parameters derived from these experiments are described in several recent papers (de Bernadis et al. 2002; Pryke et al. 2001; Stompor et al. 2001; Wang, Tegmark & Zaldarriaga 2001).

Significant advances have also been made in surveying large-scale structure in the Universe. The development of wide-field correctors and multifibre spectroscopy means that it is now possible to measure redshifts of hundreds of thousands of galaxies. Two such redshift surveys are underway. The 2dF Galaxy Redshift Survey (2dFGRS) utilizes the 2dF instrument at the Anglo-Australian Telescope and is based on a revised version of the Automated Plate Measurement (APM) Galaxy Survey (Maddox et al. 1990) limited at $b_J = 19.45$. Redshifts have now been measured for over 175 000 galaxies (see Colless et al. 2001 for a description of this survey). The Sloan Digital Sky Survey (SDSS; York et al. 2000) is a CCD imaging and spectroscopic survey that aims to measure redshifts for a sample of 900 000 galaxies. An analysis of the galaxy power spectrum from the 2dFGRS is described by Percival et al. (2001, hereafter P01). First results on galaxy clustering from a subsample of the SDSS are presented by Zehavi et al. (2002).

In addition, a number of other investigations have greatly improved the accuracy of various cosmological parameters. For example, surveys of high-redshift Type Ia supernovae have revealed tantalizing evidence for an accelerating Universe (Riess et al. 1998; Perlmutter et al. 1999); the *Hubble Space Telescope* (HST) Hubble key project has concluded that $H_0 = 72 \pm 8 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Freedman et al. 2001); primordial nucleosynthesis and deuterium abundance measurements from quasar absorption lines imply a baryon density $\omega_b = 0.020 \pm 0.002$ (Burles & Tytler 1998a,b; Burles, Nollett & Turner 2001). With these and many other ambitious projects at various stages of development (e.g. weak shear lensing surveys, CMB interferometers, CMB polarization experiments, the MAP, Planck and SNAP satellites¹) it is clear that the era of quantitative cosmology has arrived.

In this paper, we perform a combined likelihood analysis of the CMB anisotropy data and of the 2dFGRS galaxy power spectrum measured by P01. We assume that the initial fluctuations were Gaussian, adiabatic and described by power-law fluctuation spectra. Matter is assumed to consist of baryons and cold dark matter (CDM) and neutrinos are assumed to have negligible rest masses (i.e. we exclude the possibility of a strong degeneracy

amongst neutrino mass eigenstates; see Valle 2002). We allow tensor and scalar modes and place no constraints on their respective spectral indices and relative amplitudes. Almost all previous analyses of the CMB anisotropies have neglected tensor modes. However, including tensor modes introduces a major new degeneracy (referred to as the *tensor degeneracy* in this paper) that significantly widens the range of allowed parameters (see Efstathiou & Bond 1999; Wang et al. 2002; Efstathiou 2002). The tensor degeneracy can be broken by invoking additional data sets. Wang et al. (2001) combine the CMB data with measurements of the galaxy power spectrum from the *IRAS* Point Source Catalogue redshift (PSCz) survey (Hamilton, Tegmark & Padmanabhan 2000), estimates of the power spectrum on small scales from observations of the Ly α forest (Croft et al. 2001) and limits on the Hubble constant from the *HST* Hubble Key Project. Here we investigate how the major parameter degeneracies can be broken by combining the CMB data with the 2dFGRS power spectrum. The 2dFGRS power spectrum is based on a large survey, with well-controlled errors, and as demonstrated by P01 already sets interesting limits on the matter content of the Universe. Our expectation (see Efstathiou 2001) is that a joint analysis of the CMB and 2dFGRS will produce accurate estimates of the baryonic and matter densities of the Universe and set useful limits on a cosmological constant. This expectation is borne out by the results described in the rest of this paper.

2 LIKELIHOOD ANALYSIS

2.1 Analysis of the 2dFGRS power spectrum

We use the estimates of the galaxy power spectrum and associated covariance matrix computed by P01. As in P01, we fit these estimates to theoretical models of the linear matter power spectrum of CDM models using the fitting formulae of Eisenstein & Hu (1998). The fits are restricted to the wavenumber range $0.02 < k/(h \text{ Mpc}^{-1}) < 0.15$. Redshift-space distortions (see Peacock et al. 2001) and non-linear evolution of the power spectrum have negligible effect on the shape of the power spectrum at these wavenumbers. We will assume that the galaxy power spectrum within this wavenumber range is directly proportional to the linear matter power spectrum. This is a key assumption in the analysis presented in this paper and is partially justified by tests on N -body simulations using physically motivated biasing schemes as described in section 4 of P01. The lower wavenumber limit is imposed (conservatively) to reduce the sensitivity of the analysis to fits to the redshift distribution of galaxies, which are computed independently for different zones of the survey. As the 2dFGRS has a complex geometry, the theoretical power spectra must be convolved with the spherical average over wavenumber of the survey ‘window function’. These convolved theoretical estimates are used together with the spherically averaged estimates of the power spectrum of the data and the covariance matrix (computed from Gaussian realizations of the 2dFGRS) to form a likelihood function. We refer the reader to P01 for a full discussion of each of these steps in the analysis.

In general, the linear power spectrum with wavenumber measured in inverse Mpc depends on the baryonic and CDM physical densities (ω_b and ω_c), the scalar spectral index n_s and an overall amplitude A (the amplitude is treated as an ‘ignorable’ parameter in this paper and so its precise definition is unimportant). However, because we use redshift to measure distances, the wavenumber of the observations scales as $h \text{ Mpc}^{-1}$. The comparison of theory with observations therefore requires the introduction of the

¹ Descriptions of these satellites can be found on the following web pages: <http://snap.lbl.gov/>, <http://map.gsfc.nasa.gov> and <http://astro.estec.esa.nl/SA-general/Projects/Planck>.

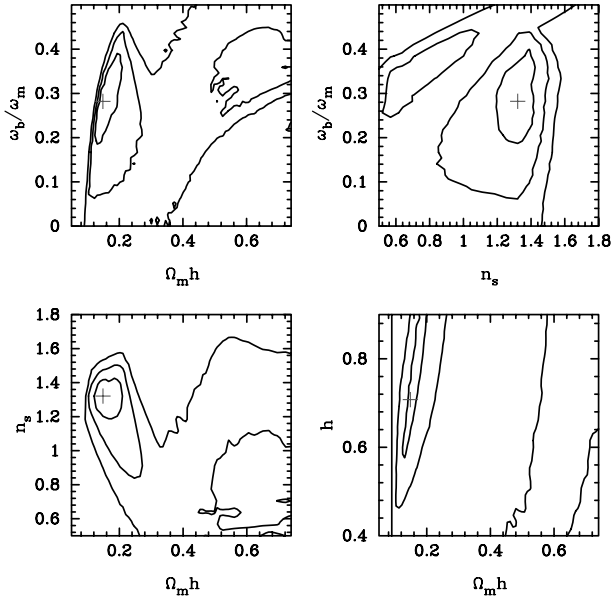


Figure 1. Contours (1, 2 and 3σ) of the pseudo-marginalized likelihood functions (see text for details) for various pairs of parameters computed by fitting to the galaxy power spectrum of the 2dFGRS. These contours correspond to changes in the likelihood of $2\Delta\ln(\mathcal{L})$ of 2.3, 6.0 and 9.2. The crosses show the position of maximum likelihood.

parameter h . In fact, the set of variables A , n_s , $\Omega_m h$, ω_b/ω_m and h are natural variables for an analysis of large-scale structure: the combination $\Omega_m h$ defines the overall shape of the CDM transfer function (and for negligible baryon density is sometimes denoted by the shape parameter Γ), while the ratio ω_b/ω_m determines the amplitude of baryonic oscillatory features in the transfer function (Eisenstein & Hu 1998; Meiksin, Peacock & White 1999).

Fig. 1 shows various two-dimensional projections of the ‘pseudo-marginalized’ 2dFGRS likelihood function. When using a large number of parameters (as in the CMB and CMB+2dFGRS analyses described in the next two subsections), it is impractical to compute marginalized likelihood contours by numerically integrating over the likelihood distribution. Instead, a ‘pseudo-marginalized’ likelihood function in p out of M parameters is computed by setting the remaining $M - p$ parameters at the values which maximize the likelihood. For a multivariate Gaussian distribution, this is equivalent to integrating over the $M - p$ parameters assuming uniform prior distributions (see Tegmark, Zaldarriaga & Hamilton 2001). However, the actual likelihood distributions are not exactly Gaussian (as is evident from the asymmetrical contours in Figs 1 and 3, later) and so confidence limits assigned to pseudo-marginalized distributions are approximate. The contours in the $(\omega_b/\omega_m, \Omega_m h)$ plane can be compared with fig. 5 of P01 where the spectral index was assumed to be scale invariant. Relaxing the constraint on the spectral index clearly widens the allowed range of ω_b/ω_m , but the data still place a tight constraint on the ‘shape’ parameter $\Omega_m h$. As we will see below, the constraints on $\Omega_m h$ and n_s prove particularly important in breaking degeneracies among parameters inherent in the analysis of CMB data.

2.2 Analysis of the CMB anisotropies

The likelihood analysis presented here uses the compilation of band power estimates ΔT_B^2 and their covariance matrix $\mathbf{C}_{BB'}$

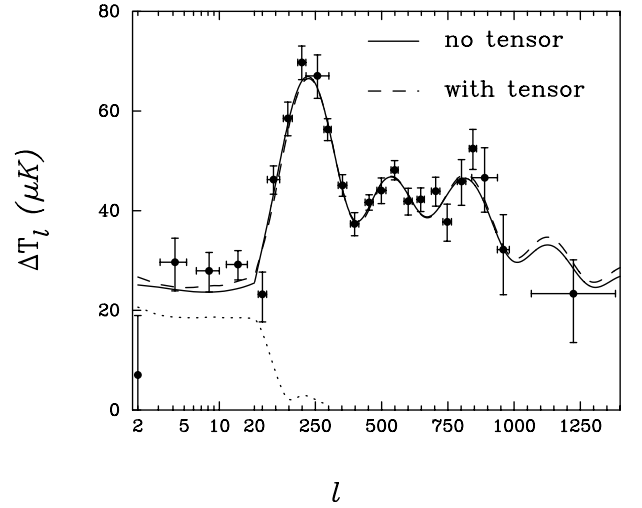


Figure 2. The points show band-averaged observational estimates of the CMB power spectrum from Wang et al. (2001) together with $\pm 1\sigma$ errors. The lines show the CMB power spectra for the adiabatic fiducial inflationary models that provide the best fit to the CMB and 2dFGRS power spectra. The parameters of these model are listed in Table 1. The solid line shows the best fit without a tensor component (fit B). The dashed line shows the best fit (fit C) including a tensor component (shown by the dotted line).

(including a model for calibration and beam errors) computed by Wang et al. (2002) from 105 CMB anisotropy measurements. Each band power estimate is related to the power spectrum C_ℓ of the CMB anisotropies by

$$\Delta T_B^2 = \frac{T_0^2}{2\pi} \sum_{\ell} \ell(\ell+1) C_\ell W_B(\ell) \quad (1)$$

where W_B is the window function for each band power computed by Wang et al. These band-power estimates are plotted in Fig. 2.

The likelihood analysis of the CMB data uses nine parameters. These are: ω_b and ω_c ; Ω_Λ and Ω_k ; the scalar and tensor spectral indices n_s and n_t ; the optical depth to Thomson scattering τ_{opt} , assuming that the inter-galactic medium was abruptly re-ionized some time after recombination; the amplitude Q^2 of the scalar component and the ratio of \bar{r} of the tensor to scalar amplitudes. Note that definitions of the scalar and tensor amplitudes differ from paper to paper. Here we scale the scalar and tensor spectra so that

$$\frac{1}{4\pi} \sum_{\ell=2}^{1000} (2\ell+1) \hat{C}_\ell^S = (4 \times 10^{-5})^2, \quad (2a)$$

$$\frac{1}{4\pi} \sum_{\ell=2}^{50} (2\ell+1) \hat{C}_\ell^T = (2 \times 10^{-5})^2, \quad (2b)$$

and fit to the data by scaling with the parameters Q and \bar{r} , $C_\ell = C_\ell^S + C_\ell^T = Q^2(\hat{C}_\ell^S + \bar{r}\hat{C}_\ell^T)$. The numbers in equation (2) were chosen so that models with Q of approximately unity match the data points plotted in Fig. 2 and models with $\bar{r} \approx 1$ have scalar and tensor modes of comparable amplitude. We normalize the spectra in this way to reduce the sensitivity of the normalization parameters to other parameters that affect the low order multipole moments (e.g. Ω_Λ and Ω_k) and to decouple Q from the optical depth parameter τ_{opt} . This method of normalizing helps to stabilize searches for global maxima of the likelihood functions. For our best-fitting models of Table 1 we list values of the more commonly used parameter $r_{10} \equiv C_{10}^T/C_{10}^S$ in addition to \bar{r} . In simple models of

Table 1. Parameter values and errors.

	Approximate $\pm 2\sigma$ parameter ranges						
	Fit A CMB alone + tensor	Fit B CMB + 2dFGRS no tensor	Fit C CMB + 2dFGRS + tensor	Fit D CMB + 2dFGRS + BBN + tensor	Fit A CMB alone + tensor	Fit C CMB + 2dFGRS + tensor	Fit D CMB + 2dFGRS + BBN + tensor
ω_b	0.020	0.021	0.027	0.020	0.016–0.045	0.018–0.034	0.018–0.022
ω_c	0.13	0.12	0.085	0.10	0.03–0.18	0.07–0.13	0.08–0.13
n_s	0.96	1.00	1.20	1.04	0.89–1.49	0.95–1.31	0.95–1.16
Ω_k	–0.04	0.001	–0.030	–0.013	–0.68–0.06	–0.05–0.04	–0.05–0.04
Ω_Λ	0.43	0.71	0.80	0.73	<0.88	0.65–0.85	0.65–0.80
τ_{opt}	0	0	0	0	<0.5	<0.5	<0.5
n_t		–	–0.10	0.13			
\bar{r}	0	–	0.60	0.20	<0.98	<0.87	<0.82
r_{10}	0	–	1.24	0.26			
ω_b/ω_m	0.14	0.15	0.24	0.17	0.10–0.40	0.13–0.28	0.13–0.22
$\Omega_m h$		0.21	0.16	0.19		0.12–0.22	0.16–0.21
h		0.69	0.71	0.66		0.60–0.86	0.61–0.84

inflation, the parameters r_{10} (or \bar{r}), n_s and n_t are related to each other (see e.g. Hoffman & Turner 2001 for a recent discussion). The relations are model-dependent, however, and can be violated in multi-field inflation models and in superstring inspired models such as the pre-big bang (Buonanno, Damour & Veneziano 1999) and ekpyrotic scenarios (Khoury et al. 2002). We therefore assume no relations between r_{10} , n_s and n_t in this paper.

Results from the likelihood analysis of the CMB data are illustrated in Fig. 3. Almost all of the variance of the parameters used in this analysis, with the exception of Q , comes from two major degeneracies (see Efstathiou 2002 for a detailed discussion). These two degeneracies are illustrated by the likelihood contours plotted in Fig. 3(a). The top two panels illustrate the ‘geometrical’ degeneracy. This degeneracy arises because models with identical matter content, primordial power spectra and angular diameter distance to the last scattering surface produce almost identical CMB power spectra. This leads to a strong degeneracy between Ω_Λ and Ω_k , which is broken only for extreme values of Ω_Λ by the integrated Sachs–Wolfe effect which modifies the shape of the CMB power spectrum at low multipoles (see Efstathiou & Bond 1999). Because the Hubble constant is fixed by the constraint equation,

$$h = \frac{(\omega_b + \omega_c)^{1/2}}{(1 - \Omega_k - \Omega_\Lambda)^{1/2}}, \quad (3)$$

it is almost unconstrained by the CMB data.

The lower two panels in Fig. 3(a) show the constraints on the parameter combinations $w_c - \omega_b$ and $n_s - \omega_b$. These panels illustrate the tensor degeneracy: including a tensor component significantly broadens the allowed ranges of parameters. For example, values of ω_b that are more than twice the value favoured from primordial nucleosynthesis are allowed by the CMB data (Efstathiou 2002). The tensor degeneracy can be broken by the detecting or setting constraints on the B-mode polarization of the CMB anisotropies. However, in the absence of polarization information the degeneracy can be broken by either measuring the CMB anisotropies with Planck-like precision (Efstathiou & Bond 1999) or by invoking other data sets such as the 2dFGRS.

Fig. 3(b) shows likelihood contours using the CMB data alone, but computed using the natural variables of the galaxy power spectrum analysis as in Fig. 1. The parameter combination $\Omega_m h$ that essentially fixes the shape of the matter power spectrum is extremely unnatural for an analysis of the CMB anisotropies.

Because $\Omega_m h \equiv (\omega_b + \omega_c)/h$, the indeterminacy in h arising from the geometrical degeneracy smears the likelihoods along the direction of $\Omega_m h$. The wide range of allowed values of ω_b/ω_m and the tight correlation with n_s is a consequence of the tensor degeneracy.

2.3 Combining the CMB and 2dFGRS likelihoods

Fig. 3(b) is interesting because it shows that the CMB likelihoods in three of these plots are complementary to those of the 2dFGRS analysis ($\omega_b/\omega_m - \Omega_m h$, $n_s - \Omega_m h$ and $\omega_b/\omega_m - n_s$). The addition of the 2dFGRS constraints breaks both the geometrical and tensor degeneracies, resulting in strong constraints on ω_b , ω_c , Ω_Λ and h . The way that this works is evident from Figs 1 and 3(b): the constraints on n_s from the 2dFGRS help to break the tensor degeneracy by excluding high values of ω_b and low values of ω_c . The resulting values of ω_b and ω_c fix the Hubble radius at the time at which matter and radiation have equal density, which in turn largely fixes the shape of the CDM transfer function in physical Mpc. Comparing with the power spectrum of the 2dFGRS in h^{-1} Mpc constrains the Hubble constant, thus breaking the geometrical degeneracy.

The lower panels in Fig. 3 show the results of combining the CMB and 2dFGRS likelihoods. The results are striking, showing a significant tightening of the constraints in each plot. Table 1 lists parameters corresponding to maximum likelihood fits to the data and the approximate $\pm 2\sigma$ ranges of each parameter. The second column lists the maximum likelihood fit to the CMB alone (fit A). The parameters of this fit are identical whether or not a tensor component is included. The third and fourth columns (fits B and C) list the maximum likelihood fits to the CMB and 2dFGRS data excluding and including a tensor mode. The fifth column (fit D) adds the constraint from big-bang nucleosynthesis (BBN) of a Gaussian distribution for ω_b centred at $\omega_b = 0.020$ with a dispersion of $\Delta\omega_b = 0.001$ (Burles et al. 2001). The contours shown in Figs 3(c) and 3(d) would broaden somewhat had we adopted a more conservative maximum wavenumber in the analysis of the 2dFGRS power spectrum (e.g. reducing the upper wavenumber to $k_{\text{max}} = 0.1h \text{ Mpc}^{-1}$). However, the analysis is insensitive to small changes in k_{max} because the tensor degeneracy is broken primarily from the constraint on n_s which depends on the full extent of the wavenumber range.

The parameters of fit B, which provides a perfectly acceptable fit to the data, are very close to those of the standard ‘concordance’

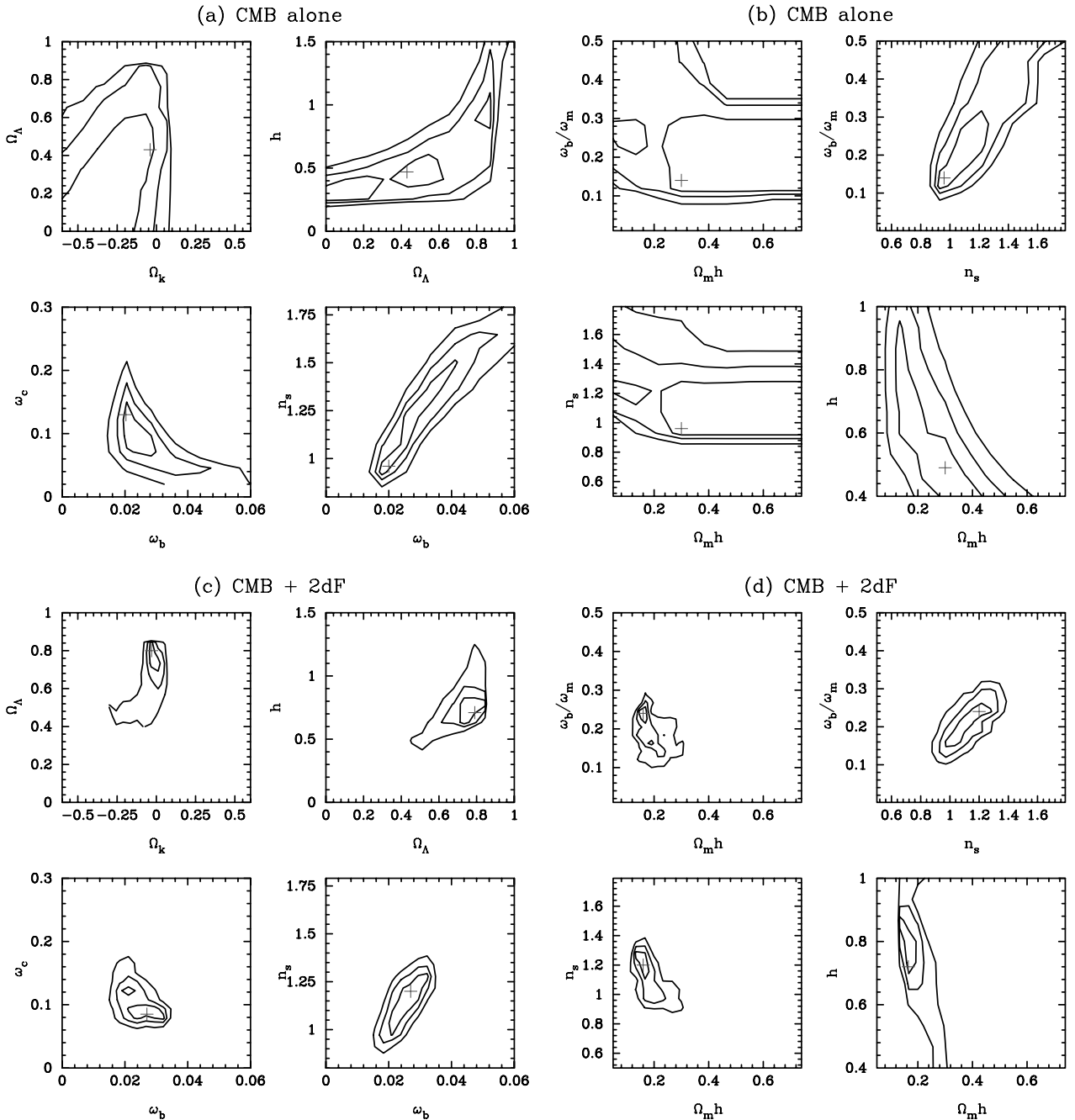


Figure 3. Results of the nine-parameter likelihood analysis. Figs 3(a) and 3(b) show approximate 1, 2 and 3σ likelihood contours for various parameter pair combinations computed from an analysis of the CMB data alone. The panels in 3(a) use variables natural to the CMB analysis and illustrate the geometrical and tensor degeneracies. The panels in 3(b) use the variables natural to the analysis of the galaxy power spectrum (as used in Fig. 1). Figs 3(c) and 3(d) show the likelihood contours of CMB and 2dFGRS data combined. The crosses in each panel show the position of the maximum likelihood.

cosmology (e.g. Bahcall et al. 1999). In particular, the baryon density is compatible with the primordial nucleosynthesis value, and the Hubble and cosmological constants are compatible with more direct observational estimates. The CMB power spectrum for this solution is plotted as the solid line in Fig. 2 and the linear matter power spectrum is plotted together with the 2dFGRS data points in Fig. 4. Both curves provide acceptable fits to the data. Fit B has a low baryon fraction of $\omega_b/\omega_m = 0.15$. As a consequence, the amplitudes of the baryonic features in the matter power spectrum are almost imperceptibly small (see Fig. 4).

Allowing a tensor component produces a slightly better fit to the

data, but the parameters are less concordant with other observations (Fit C, Table 1). The CMB power spectrum for this model is plotted as the dashed line in Fig. 2. According to this solution, a significant part of the *COBE* anisotropies comes from a tensor component. The baryon density of fit C is $\omega_b = 0.027$ and is well outside the range of values inferred from primordial nucleosynthesis. The matter power spectrum for this model is plotted as the dashed line in Fig. 4. This shows clearly what is happening with this solution. The apparent wiggles in the 2dFGRS power spectrum pull the solution towards a high baryon fraction. However, to produce a good fit to the CMB anisotropies with a high

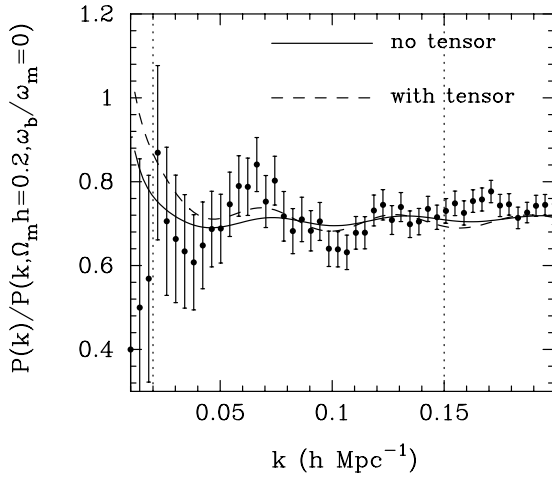


Figure 4. The points show the galaxy power spectrum of the 2dFGRS measured by P01 divided by the power spectrum of a scale-invariant CDM model with $\omega_b = 0$, $\Omega_m h = 0.2$. The error bars are computed from the diagonal components of the covariance matrix. The lines show the linear matter power spectra of the maximum likelihood fits to the combined CMB and 2dFGRS power spectra after convolution with the spherically averaged window function of the survey. The solid line shows fit B from Table 1 (no tensor component). The dashed line shows fit C (including a tensor component).

baryon fraction, the tensor degeneracy of Fig. 3 requires high values of n_s and significant tensor anisotropies. The likelihood ratio of fits B and C is $\mathcal{L}_B/\mathcal{L}_C = 0.34$ and so fit C is only marginally preferred over fit B. In two of the panels from Fig. 3(c) and (d), the likelihood distributions have two peaks centred at the parameters of fits B and C. Adding the BBN constraint on ω_b (fit D) selects one of these peaks with parameters close to those of fit B.

Fits B and C predict a lower normalization for the present-day matter power spectrum than implied by the local abundance of rich clusters of galaxies. In a recent analysis of the number density distribution of rich clusters as a function of X-ray temperature, Pierpaoli, Scott & White (2001) deduce

$$\sigma_8 = (0.495_{-0.037}^{+0.034}) \Omega_m^{-0.60}, \quad (4)$$

where σ_8 is the rms fluctuation in the mass density distribution averaged in spheres of radius $8 h^{-1} \text{Mpc}$. Fit B gives $\sigma_8 = 0.72$ and fit C gives $\sigma_8 = 0.61$, whereas equation (4) implies that $\sigma_8 = 1.04$ and $\sigma_8 = 1.20$, respectively. Most of the error in equation (4) comes from uncertainties in the cluster mass–X-ray temperature relation and it is not clear whether the quoted error reflects the true uncertainties. A number of effects could boost the best fitting values of σ_8 , for example, a realistic value for τ_{opt} [recent observations of high-redshift quasars suggest that re-ionization occurs just prior to $z \approx 6$ (Becker et al. 2001; Fan 2001), suggesting that $\tau_{\text{opt}} \approx 0.03\text{--}0.04$] or possible calibration errors in the CMB data might affect σ_8 at the about the 10 per cent level. Such effects may reconcile fit B with the cluster data, but are probably not large enough to explain the discrepancy with fit C. Furthermore, as we have discussed above, the discrepancy with the primordial nucleosynthesis value of ω_b provides another reason to disfavour fit C.

3 DISCUSSION

The results of this paper are based on the key assumption that the galaxy power spectrum on large scales (wavenumbers

$k < 0.15 h \text{Mpc}^{-1}$) is proportional to the linear matter power spectrum. Under this assumption, we have shown that the galaxy power spectrum of the 2dFGRS can be used to partially break the two major parameter degeneracies inherent in the analysis of CMB anisotropies. The limits on the scalar spectral index from the 2dFGRS help to break the tensor degeneracy. The resulting constraints on the matter density provide a measure of a standard physical distance (the Hubble radius at the time at which matter and radiation have equal density). This standard length constrains the Hubble constant and so breaks the geometrical degeneracy.

The resulting constraints are in remarkable agreement with the baryon density inferred from primordial nucleosynthesis (Burles & Tytler 1998a,b), estimates of the Hubble constant from the *HST* Hubble key project (Freedman et al. 2001) and evidence for a non-zero cosmological constant from observations of distant Type Ia supernovae (Riess et al. 1998; Perlmutter et al. 1999). The best-fitting model excluding a tensor component has parameters that are very close to those of the standard ‘concordance’ cosmology (Bahcall et al. 1999). However, the combined CMB + 2dFGRS data provide weak upper limits on a tensor component (Table 1) and other solutions are possible which have a higher baryon density and baryon fraction. These solutions conflict with the limits on ω_b from primordial nucleosynthesis and require a scalar spectral index $n_s > 1$. The model with high n_s and high ω_b provides a somewhat closer match to the apparent ‘wiggles’ in the galaxy power spectrum at wavenumbers $k \sim 0.08 h \text{Mpc}^{-1}$ and $k \sim 0.12 h \text{Mpc}^{-1}$ than is achieved by the scalar-only model (Fig. 4). Neither model fully matches the data points, however, and it is plausible that the apparent features are enhanced by the noise. New power spectrum data from the 2dFGRS and the SDSS will soon allow us to test this hypothesis. It is particularly encouraging that the combination of the 2dFGRS and CMB data yields strong evidence for a cosmological constant in the range $0.65 \lesssim \Omega_\Lambda \lesssim 0.85$ based on completely different arguments to those applied to distant Type Ia supernovae. This significantly strengthens the case in favour of an accelerating universe.

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