

Evidence of environmental dependencies of Type Ia supernovae from the Nearby Supernova Factory indicated by local $H\alpha$ *

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ABSTRACT

Context. Use of Type Ia supernovae (SNe Ia) as distance indicators has proven to be a powerful technique for measuring the dark-energy equation of state. However, recent studies have highlighted potential biases correlated with the global properties of their host galaxies, large enough to induce systematic errors into such cosmological measurements if not properly treated.

Aims. We study the host galaxy regions in close proximity to SNe Ia in order to analyze relations between the properties of SN Ia events and environments where their progenitors most likely formed. In this paper we focus on local $H\alpha$ emission as an indicator of young progenitor environments.

Methods. The Nearby Supernova Factory has obtained flux-calibrated spectral timeseries for SNe Ia using integral field spectroscopy. These observations enabled the simultaneous measurement of the SN and its immediate vicinity. For 89 SNe Ia we measured or set limits on $H\alpha$ emission, used as a tracer of ongoing star formation, within a 1 kpc radius around each SN. This constitutes the first direct study of the local environment for a large sample of SNe Ia with accurate luminosity, color, and stretch measurements.

Results. Our local star formation measurements provide several critical new insights. We find that SNe Ia with local $H\alpha$ emission are redder by 0.036 ± 0.017 mag, and that the previously noted correlation between stretch and host mass is driven entirely by the SNe Ia coming from locally passive environments, in particular at the low-stretch end. There is no such trend for SNe Ia in locally star-forming environments. Our most important finding is that the mean standardized brightness for SNe Ia with local $H\alpha$ emission is 0.094 ± 0.031 mag fainter on average than for those without. This offset arises from a bimodal structure in the Hubble residuals, with one mode being shared by SNe Ia in all environments and the other one exclusive to SNe Ia in locally passive environments. This structure also explains the previously known host-mass bias. We combine the star formation dependence of this bimodality with the cosmic star formation rate to predict changes with redshift in the mean SN Ia brightness and the host-mass bias. The strong change predicted is confirmed using high-redshift SNe Ia from the literature.

Conclusions. The environmental dependences in SN Ia Hubble residuals and color found here point to remaining systematic errors in the standardization of SNe Ia. In particular, the observed brightness offset associated with local $H\alpha$ emission is predicted to cause a significant bias in current measurements of the dark energy equation of state. Recognition of these effects offers new opportunities to improve SNe Ia as cosmological probes. For instance, we note that the SNe Ia associated with local $H\alpha$ emission are more homogeneous, resulting in a brightness dispersion of only 0.105 ± 0.012 mag.

Key words. cosmology: observations

* Appendix is available in electronic form at <http://www.aanda.org>

1. Introduction

Luminosity distances from Type Ia supernovae (SNe Ia) were key to the discovery of the accelerating expansion of the universe (Perlmutter et al. 1999; Riess et al. 1998). Among the current generation of surveys, more than 600 spectroscopically confirmed SNe Ia are available for cosmological analyses (e.g., Suzuki et al. 2012). Thus, even today SNe Ia remain the strongest demonstrated technique for measuring the dark-energy equation of state.

The fundamental principle behind the use of these standardized candles is that the standardization does not change with redshift. SNe Ia have an observed M_B dispersion of approximately 0.4 mag, which makes them naturally good distance indicators. Empirical light-curve fitters, such as SALT2 (Guy et al. 2007, 2010) or MLCS2K2 (Jha et al. 2007), correct M_B for the “brighter-slower” and “brighter-bluer” relation (Phillips 1993; Riess et al. 1996; Tripp 1998). This stretch (or x_1) and color (c) standardization enables the reduction of their magnitude dispersion down to ≈ 0.15 mag.

However, a major issue remains: despite decades of study, their progenitors are as yet undetermined. (See Maoz & Mannucci 2012, for a detailed review.) Like all stars, it is expected that these progenitors will have a distribution of ages and metal abundances, and these distributions will change with redshift. These factors in turn may affect details of the explosion, leading to potential bias in the cosmological measurements. The remaining 0.15 mag “intrinsic” scatter in SN Ia standardized brightnesses is a direct indicator that hidden variables remain. Host galaxy dust – and peculiar velocities if the host is too nearby – complicate the picture.

Several studies have found that the distribution of SNe Ia light-curve stretch values differs across host galaxy total stellar mass (Hamuy et al. 2000; Neill et al. 2009; Sullivan et al. 2010) and global specific star formation rate (sSFR; Lampeitl et al. 2010; Konishi et al. 2011). Lampeitl et al. (2010) concluded that the distribution of SNe Ia colors appears to be independent of the star-forming properties of the host, even though more dust is expected in actively star-forming environments. However, in Childress et al. (2013a) we found that SNe Ia colors do correlate with host metallicity. This may be intrinsic, but also metals are a necessary ingredient for dust formation. Stretch is correlated with observed M_B , so after standardization, the influence of this environmental property disappears.

A dependence of corrected Hubble residuals on host mass is now well-established (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Childress et al. 2013a; Johansson et al. 2013). This has been modeled as either a linear trend or a sharp step in corrected Hubble residuals between low- and high-mass hosts. In Childress et al. (2013a) we established that a “mass step” at $\log(M/M_\odot) = 10.2$ gives a much better fit than a line, and we found that the RMS width of the transition is only 0.5 dex in mass. Because the mass of a galaxy correlates with its metallicity, age, and sSFR (see Tremonti et al. 2004; Gallazzi et al. 2005; Pérez-González et al. 2008, respectively), this mass step is most likely driven by an intrinsic SN progenitor variation. For instance, a brightness offset between globally star-forming and passive galaxies provides a fair phenomenological description of the mass step (D’Andrea et al. 2011), being driven by the sharp change in the fraction of star-forming hosts at $\log(M/M_\odot) \sim 10$ present in the local universe (Childress et al. 2013a).

However, the interpretation of these results is limited by the use of global properties of the host galaxies. The measured quantities – gas metallicity, star formation rate, etc. – are

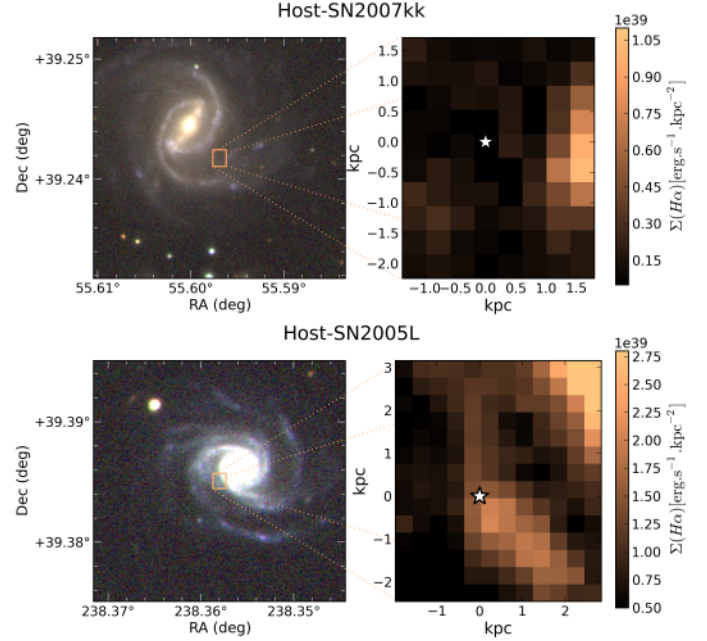


Fig. 1. Top and bottom: the hosts of SN 2007kk (UGC 2828) and SN 2005L (MCG+07-33-005), respectively, both classified as globally star-forming (Childress et al. 2013b). Left: color images made using observations from SNIFS and SDSS-III (Aihara et al. 2011). On both images, the field-of-view of SNIFS, centered on the SN position (white-star marker), is indicated by the orange central square. Right: $H\alpha$ surface brightness maps of the SN vicinities (the generation of these maps is detailed in Sect. 2.3). SN 2007kk occurred in a passive environment more than 1.5 kpc from the closest star-forming region, while SN 2005L is located at the edge of such a region.

light-weighted. Thus global analyses are most representative of galaxy properties near the core, which can be significantly different than the actual SN environment. This is illustrated in Fig. 1: inside these two spiral star-forming galaxies, a SN occurred either in an old passive inter-arm environment (SN 2007kk) or inside a star-forming one (SN 2005L).

In this work we analyze the host galaxy regions in the immediate vicinity for a large sample of SNe Ia from the Nearby Supernova Factory (SNfactory, Aldering et al. 2002). Our integral field spectrograph accesses the local environment of observed SNe, and therefore probes local host properties, such as gas and stellar metallicities and star formation history. While Stanishev et al. (2012) have conducted such a study by looking at the metallicity of the local environments of a sample of seven nearby SNe Ia, ours is the first such large-scale study.

Delay-time distribution studies (Scannapieco & Bildsten 2005; Mannucci et al. 2005, 2006; Sullivan et al. 2006) predict that a fraction of SNe Ia, known as “prompt” SNe, should be associated with young stellar populations. The rest, referred to as “tardy” or “delayed” SNe, should be related to older stars. Individual star-forming regions (H II regions) have a typical lifetime of a few Myr (Alvarez et al. 2006), much shorter than expected – even for the fastest – SN Ia progenitor systems (few tens of Myr, Girardi et al. 2000). It is therefore impossible to make a physical connection between a SN and the H II region in which its progenitor formed. However such star-forming regions are gathered in groups (see for instance M 51 in Lee et al. 2011), concentrated in spiral arms whose lifetimes are longer than the time scale for a prompt SN. (See Kauffmann et al. 2003, for details on the star formation history of galaxies.) This motivated us

to employ H α for our first analysis of SNe Ia local environments. H α will be taken to indicate active local star formation, and thus the likelihood that a given progenitor was especially young.

Long before the “prompt” and “tardy” distinction, association with HII regions or spiral arms was a common approach for understanding the stellar populations from which SNe formed. For instance, with small samples of SNe, [Bartunov et al. \(1994\)](#) and later [James & Anderson \(2006\)](#) showed that Type Ia SNe were less associated with such regions than are core-collapse SNe. A key ingredient missing in such studies needed to understand SNe Ia in detail is accurate standardized luminosities, which we have for our sample. Also, in light of the “prompt”/“tardy” dichotomy, it will be important to consider the possibility that SNe Ia will fall into discrete subsets based on the strength of star formation in their local environment.

After the presentation of our data (Sect. 2) and our method for quantifying neighboring star-forming activity (Sect. 3), we investigate the correlation of SNe Ia light-curve parameters with the local environment (Sect. 4). This includes a review of how our results based on the local environment compare with the aforementioned global host galaxy studies. In particular, we present evidence for excess dust obscuration of SNe Ia in actively star-forming environments. We also show that the corrected SN Ia brightnesses depend significantly on the local H α environment. We discuss the implications of our results in Sect. 5, where the standardization of SNe Ia is examined. We then compare our local H α analysis with previous results concerning the total host stellar mass, finding important clues to the origin of the mass step. In Sect. 6, we estimate the impact of the local trends on the cosmological parameters using a simple model, and then use this model to show redshift evolution in SNe Ia from the literature. We further demonstrate the existence of a SN Ia subset having a significantly reduced brightness dispersion. Finally, in Sect. 7 we test the robustness of our results, and end with a summary in Sect. 8.

2. Integral field spectroscopy of immediate SN Ia neighborhoods

2.1. SNIFS and the SNfactory

The SNfactory has observed a large sample of nearby SNe and their immediate surroundings using the SuperNova Integral Field Spectrograph (SNIFS, [Lantz et al. 2004](#)) installed on the UH 2.2 m telescope (Mauna Kea). SNIFS is a fully integrated instrument optimized for semi-automated observations of point sources on a structured background over an extended optical window at moderate spectral resolution. The integral field spectrograph (IFS) has a fully filled $6''.4 \times 6''.4$ spectroscopic field-of-view subdivided into a grid of 15×15 contiguous square spatial elements (spaxels). The dual-channel spectrograph simultaneously covers 3200–5200 Å (*B*-channel) and 5100–10 000 Å (*R*-channel) with 2.8 and 3.2 Å resolution, respectively. The data reduction of the x, y, λ data cubes was summarized by [Aldering et al. \(2006\)](#) and updated in Sect. 2.1 of [Scalzo et al. \(2010\)](#). A preview of the flux calibration is developed in Sect. 2.2 of [Pereira et al. \(2013\)](#), based on the atmospheric extinction derived in [Buton et al. \(2013\)](#).

For each followed SN, the SNfactory creates a spectrophotometric time series typically composed of ~ 13 epochs, with the first spectrum taken on average three days before maximum light in *B* ([Bailey et al. 2009](#); [Chotard et al. 2011](#)). In addition, observations are obtained at the SN location at least one year after the explosion to serve as a final reference to enable the

subtraction of the underlying host. For this analysis, we gathered a subsample of 119 SNe Ia with good final references and properly measured light-curve parameters, including quality cuts suggested by [Guy et al. \(2010\)](#).

2.2. Local host observations

The SNfactory software pipeline provides flux-calibrated x, y, λ cubes corrected for instrumental and atmospheric responses ([Buton et al. 2013](#)). Each spaxel of an SN cube includes three components, each one characterized by its own spatial signature:

1. the SN is a pure point source, located close to the center of the SNIFS field of view (FoV);
2. the night sky spectrum is a spatially flat component over the full FoV;
3. the host galaxy is a (potentially) structured background.

In this section, we present the algorithm used to disentangle the three components. In Sect. 2.2.1, we describe the method used to subtract the SN component from the original cubes, and in Sect. 2.2.2 our sky-subtraction procedure, using a spectral model for the sky that prevents host-galaxy signal contamination. All cubes from the same host are finally combined to produce high signal-to-noise (S/N) cubes and spectra. This process is detailed in Sect. 2.2.3.

2.2.1. SN subtraction

The point source extraction from IFS data requires the proper subtraction of any structured background. Using a 3D deconvolution technique, [Bongard et al. \(2011\)](#) show how we construct a “seeing-free” galaxy x, y, λ cube from final reference exposures taken after the SN Ia has vanished (typically one year after maximum light). After proper registration and reconvolution with the appropriate seeing, this model is subtracted from each observed cube to leave the pure point-source component plus a spatial constant similar to a sky signal. Three-dimensional PSF photometry is then applied to the host-subtracted cube to extract the point source spectrum (e.g., [Buton et al. 2013](#)).

For the present local host property analysis, we went one step further and subtracted the aforementioned fitted PSF from the original cubes to obtain SN-subtracted host cubes. Figure 2 shows an example of such a subtraction procedure. Since the SNfactory acquires SN Ia time series, this technique provides as many local host observations as SN pointings (on average 13), in addition to the final references (on average 2).

2.2.2. Sky subtraction

Since SNIFS has a FoV spanning only $\sim 6''$ across, it is usually not possible to find a region entirely free of host signal, as is usually done in photometry or long-slit spectroscopy. The night sky spectrum is a combination of the atmospheric molecular emission, zodiacal light, and scattered star light, along with the moon contribution if any ([Hanuschik 2003](#)). We have developed a sky spectrum model from a principal component analysis (PCA) on 700 pure sky spectra obtained from standard star exposures in various observing conditions. The *B* and *R* channels are analyzed independently and in slightly different ways.

The emission lines in *R* sky spectra (mainly oxygen and OH bands) are easily isolated from the underlying continuum. This continuum is fitted by a fourth-order Legendre polynomial over emission line-free wavelength regions. The PCA is then

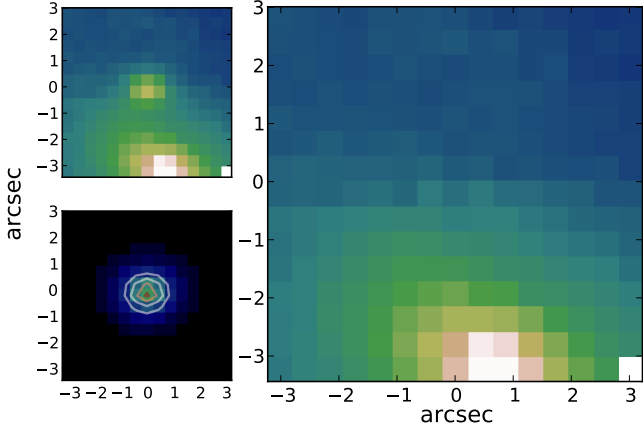


Fig. 2. SN subtraction from a host cube. Different reconstructed images, made by integrating x, y, λ cubes along the λ axis, are shown for a single observation of SNF20070326-012. *Top left*: original flux-calibrated cube containing host, sky, and SN signals. *Bottom left*: pure SN cube obtained after host subtraction (image) and fitted PSF model (contours). *Right*: SN-subtracted host cube.

performed on the continuum-subtracted emission line component. Eight principal components (PCs) are necessary to reconstruct the emission spectrum with a median reduced χ^2 of 1. An example of a red-sky spectrum fit using this 13-parameter model is given in Fig. 3.

The B sky spectrum is dominated by diffuse light and shows absorption features, as well as a few Herzberg O_2 lines in the bluer part of the spectrum. For this channel a PCA is performed directly on the observed sky spectra, since it was not possible to disentangle the different physical components as easily as for the R sky spectra. We find that four PCs are necessary to reach a median reduced χ^2 of 1.

In total, our $B+R$ sky model is therefore described by $4 + (5 + 8) = 17$ linear parameters. Since this model is trained on selected pure sky spectra, none of the PCs should mimic galactic features: even if some chemical elements are common (e.g., the hydrogen or nitrogen lines), host galactic lines are redshifted and cannot be spuriously fit by the model.

Each spaxel of the SN-subtracted cube can be decomposed as follows:

$$\text{spaxel}(x, y, \lambda) = \text{host}(x, y, \lambda) + \text{sky}(\lambda), \quad (1)$$

where the spatially flat sky component does not depend on the spaxel location (x, y) . We define the *presumed* sky as the mean spectrum of the five faintest spaxels, i.e. with the smallest host contribution. Since the $\text{host}(x, y, \lambda)$ component of Eq. (1) may not be strictly null for these spaxels, the *presumed* sky may still contain galactic features, such as hydrogen emission lines, and cannot be used directly as a valid estimate of the true sky spectrum. We therefore fit the presumed sky spectrum with our model: the resulting *modeled* sky is free of any galactic features and can safely be subtracted from each spaxel to obtain a pure host cube. (See Fig. 3 for an example using the R -channel.)

This procedure could slightly overestimate the sky continuum in cases of bright host signals even in the faintest spaxels, and ultimately lead to a underestimation of the $H\alpha$ flux measurements (Groves et al. 2012). This effect is, however, insignificant in comparison to our main source of $H\alpha$ measurement error, related to our inability to correct for host dust extinction (see Sect. 2.3).

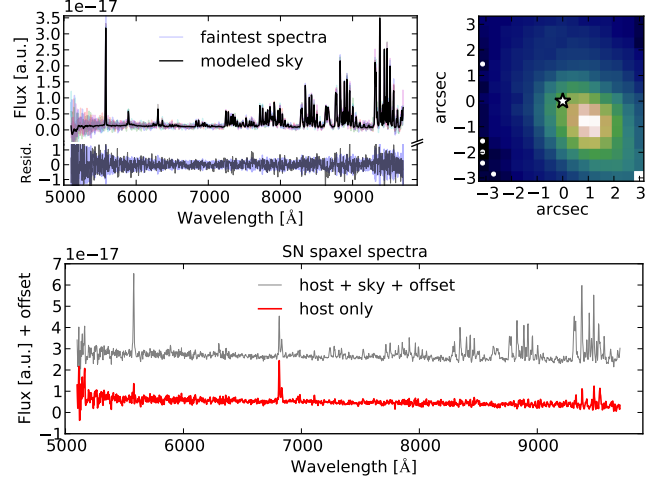


Fig. 3. Sky subtraction process for an R cube of host-SNF20060512-001. *Top right*: reconstructed image of a final reference acquisition (it could as well be an SN-subtracted cube); the central star marker indicates the SN location. The dot markers indicate the faintest spaxels used to measure the presumed sky. *Top left*: modeled sky (thick black) fit over the mean of the five faintest spectra (thin colored); the bottom part shows the fit residuals, compared to the presumed sky error (blue band). *Bottom*: host spectrum at the SN location before (upper thin gray line) and after (lower thick red line) the sky subtraction. The emission at 6830 \AA is the $H\alpha + [N II]$ gas line complex, left untouched by the sky subtraction procedure. The few small features further toward the red are residuals from the sky subtraction, but this part of the spectrum is not used in this analysis. See Sect. 2.3 for details.

2.2.3. Spectral merging

In this analysis, we focus on the host properties of the SN local environment, which we define as having projected distances less than 1 kpc from the SN. This radius has been chosen since it is greater than our median seeing disk for our most distant host galaxies, at $z = 0.08$. ($1'' = 1.03 \text{ kpc}$ at $z = 0.05$.) No allowance was made for host galaxy inclination in defining this local region.

Once the SN and the sky components have been subtracted, we computed the mean host spectrum from each cube within 1 kpc around the SN. This requires precise spatial registration (a by-product of the 3D deconvolution algorithm, see Sect. 2.2.1) and atmospheric differential refraction correction. Those spectra (15 on average per SN) are then optimally averaged and merged to get one host spectrum of the local environment per SN. The spectral sampling of these merged-channel spectra is set to that of the B -channel, which is 2.38 \AA . In the same fashion, we are able to combine 3D-cubes to create 2D-maps of any host property.

The spectra are corrected for Milky-Way extinction (Schlegel et al. 1998). In this paper, observed fluxes are expressed as surface brightnesses, and wavelengths are shifted to rest frame. We only consider the 89 SNe Ia in the main SNfactory redshift range $0.03 < z < 0.08$ for spatial sampling reasons; namely, at lower z the final SNIFS field of view remaining after spectral merging often subtends a radius of less than 1 kpc surrounding the SN location, while at higher z the typical seeing disk subtends substantially more than 1 kpc. Since this selection is only based on redshift, it does not introduce bias with respect to host or SN Ia properties. (See Childress et al. 2013b, who showed that our host data follow regular galaxy characteristics.)

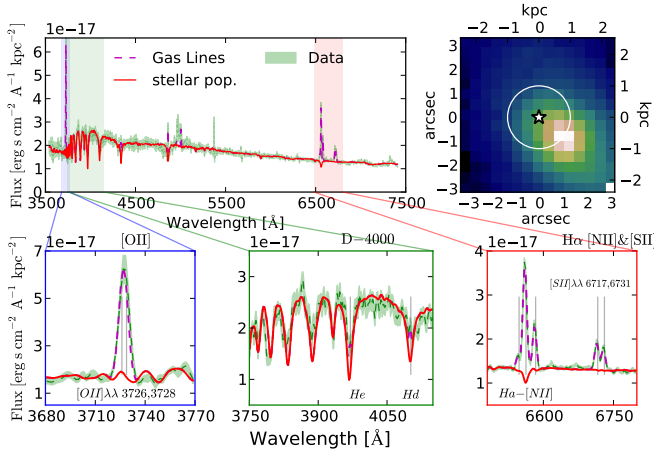


Fig. 4. Spectral fit of the host mean spectrum in the projected 1 kpc radius around SNF20060512-001. *Top right:* reconstructed image of a final reference exposure. The circle aperture shows the 1 kpc aperture centered on the SN location (central star marker). *Top left:* mean host spectrum within 1 kpc radius around the SN (rest-frame, green dashed-line with $\pm 1\sigma$ error band), averaged over 21 cubes (including two final references). The best ULYSS fit is shown as the sum of a stellar continuum (red line) and gas lines (magenta dashed line). *Bottom, from left to right:* zoom on [O II] $\lambda\lambda$ 3726, 3728, 4000 Å break, and $H\alpha$ + [N II] $\lambda\lambda$ 6548, 6584 + [S II] $\lambda\lambda$ 6716, 6731 wavelength regions.

The influence of the PSF, i.e., the variation in the amount of independent information with redshift for a given kpc-radius aperture, is discussed in Sect. 7, where we show that our analysis is free of any redshift bias.

2.3. Measurement of the local host properties

A galactic spectrum is a combination of a continuum component with absorption lines mostly from the stars and emission lines from the interstellar gas. In this paper, we restrict our analysis to the $H\alpha$ signal around the SN. Since hydrogen emission line intensities can be affected by underlying stellar absorption, it is necessary to estimate the stellar continuum to obtain accurate $H\alpha$ measurements. (See Fig. 4.)

The University of Lyon Spectroscopic analysis Software¹ (ULYSS, Koleva et al. 2008, 2009) is used to disentangle the stellar and gas components. It fits the following three components simultaneously: stellar populations from the MILES library (Sánchez-Blázquez et al. 2006); a set of emissions lines – Balmer’s hydrogen series in addition to [O II] $\lambda\lambda$ 3726, 3728, [O III], [N II], and [S II]; and a multiplicative ad hoc continuum correcting for both internal dust extinction and any remaining large-scale flux mismatch between the data and the template library. Only wavelengths matching the MILES library rest frame are considered (3540–7410 Å), and gas emission lines all share a common redshift and velocity dispersion. Because of this added constraint, gas emission flux uncertainties given by ULYSS cannot be trusted readily. We therefore ultimately fit Gaussian profiles on stellar-corrected emission lines to derive $H\alpha$ fluxes and accurate uncertainties.

Figure 4 presents the fit of the mean spectrum of the local environment for SNF20060512-001. In this particular case 21 exposures per channel, including two final references, have been combined. The stellar component is strongly constrained by the

D4000 feature, and thereby gas flux measurements properly account for stellar absorption.

In this paper, we focus our study on the $H\alpha$ line as a tracer of the star-forming activity (Kennicutt 1998). The spectra are not corrected for the internal host extinction, because the Balmer decrement method (Calzetti et al. 1994) cannot be reliably applied: the $H\gamma$ lines are usually too faint, and $H\beta$ lines happen to lie at the SNIFS dichroic cross-over ($4950 < \lambda < 5150$ Å in the observer frame, see Fig. 4), where the S/N is low and fluxes harder to calibrate.

3. Local $H\alpha$ surface brightness analysis

The $H\alpha$ emission within a 1 kpc projected radius can be conveniently recast as a surface brightness, which we designate with $\Sigma_{H\alpha}$. Because the measurement is projected, it actually represents the total $H\alpha$ emission in a 1 kpc radius column passing through the host galaxy centered on the SN position. Thus, it is possible that $H\alpha$ we detect, in whole or in part, is in the foreground or background of the 1 kpc radius sphere surrounding the SN.

However, there are several factors that greatly suppress projection effects for $H\alpha$ relative to stars. One is that $H\alpha$ depends on the square of the electron density, so most $H\alpha$ comes from those rare regions with high gas density. This advantage is compounded by the fact that young stars capable of ionizing hydrogen also tend to occur in clumps and regions of higher gas density (see Kennicutt & Evans 2012, especially Sect. 2.2, for a detailed discussion of H II regions and their clumpiness). In addition, while stars are spread across thin and thick disks, bulges and halos, H II regions are concentrated in the thin galactic disk, where a typical scale height is only ~ 0.1 kpc (Paladini et al. 2004). Thus the line-of-sight depth extends beyond our canonical 1 kpc radius only for very high inclinations (i.e., $i > 84$ deg). Finally, the $H\alpha$ covering fraction is generally low because H II regions are so short-lived (see Calzetti 2012, for a detailed review of tracers of star formation activity.).

In the following analysis, a few cases (7/89) of SNe with locations projected close to the core of very inclined hosts have been set aside because of the high probability of such misassociation (designated as “p.m.s.”, see Table 1). In Sect. 7 we show that these cases have no influence on our results.

A different projection effect occurs if SNe Ia travel far from their formation environment before they explode. Owing to random stellar motions this will occur, and its importance will itself depend on SNe Ia lifetimes and the host velocity dispersion. If as expected, tardy SNe Ia are associated with old stellar populations, this correspondence may be lost only in cases where the host is globally star forming – i.e., for spiral rather than elliptical galaxies – and the SN motion has projected it onto a region of active star formation. As with the line-of-sight projection discussed above, this situation should be uncommon. On the other hand, prompt progenitors should not have drifted from their stellar cohort by more than our fiducial 1 kpc radius. This cohort is likely to have been an open cluster or OB association; open clusters remain bound on the relevant timescale, while OB associations have very low velocities dispersions (~ 3 km s⁻¹ de Zeeuw et al. 1999; Portegies Zwart et al. 2010; Röser et al. 2010). Consequently, there should be little contamination due to this type of projection effect for young progenitors.

Thus, the net effect will be that for some old SN progenitors in globally star-forming galaxies a false positive association with $H\alpha$ may arise from these projection effects. However, we expect

¹ <http://ulyss.univ-lyon1.fr>

Table 1. Definition of the two $\Sigma_{H\alpha}$ subgroups, and their respective weighted mean light-curve parameters.

Label	Group	$\log(\Sigma_{H\alpha})$	SNe	$\langle x_1 \rangle$	$\langle c \rangle$	$\langle \Delta M_B^{\text{corr}} \rangle$ [mag]	p.m.s.
Ia ϵ	<i>Locally</i> passive	<38.35	41	-0.29 ± 0.14	0.029 ± 0.010	-0.039 ± 0.023	2
Ia α	<i>Locally</i> star-forming	≥ 38.35	41	$+0.08 \pm 0.10$	0.065 ± 0.013	$+0.056 \pm 0.020$	5

Notes. The “p.m.s.” column indicates the number of SNe with a potential misassociation of a $H\alpha$ detection due to projection effects, which have been excluded from the main analysis.

the number of such cases to be small, as discussed later in this section.

For ease in interpretation, we split our sample in two, using the median $\Sigma_{H\alpha}$ value of our distribution, $\log(\Sigma_{H\alpha}) = 38.35$, as the division point. This corresponds to a star formation surface density of $1.22 \times 10^{-3} M_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$ assuming Eq. (5) of Calzetti et al. (2010). Cases where no $H\alpha$ signal was found are arbitrarily set to $\log(\Sigma_{H\alpha}) = 37$ in the figures.

The median $\Sigma_{H\alpha}$ value happens to correspond to the threshold at which we achieve a minimal 3σ -level measurement sensitivity. It also corresponds to the mean $\log(\Sigma_{H\alpha})$ of the warm interstellar medium (WIM) distribution reported by Oey et al. (2007). The source of the WIM is controversial. The long-standing interpretation has been that the WIM is due to Lyman continuum photons that have escaped from star-forming regions and then ionize the ISM. In this interpretation, the WIM would still trace star formation, but its distribution would be more diffuse than an H II region. This distinction would not matter given our large metric aperture since even in the ISM the optical depth to Lyman continuum photons is large. Recently, however, Seon & Witt (2012) have interpreted the WIM as due to reflection of light from H II regions off of ISM dust. In this case WIM $H\alpha$ would still arise from star formation, but possibly from distances well outside our metric aperture since the optical depth to $H\alpha$ photons can be low. By setting our division point above the nominal $\log(\Sigma_{H\alpha})$ of the WIM we minimize the importance of these details for our analysis.

We designate these two $\Sigma_{H\alpha}$ subgroups as follows (see Table 1):

- 41 SNe Ia α with $\log(\Sigma_{H\alpha}) \geq 38.35$, which we refer to as “locally star forming”,
- 41 SNe Ia ϵ with $\log(\Sigma_{H\alpha}) < 38.35$, which we refer to as “locally passive”.

Figure 5 presents a quantitative picture of the point made visually in Fig. 1 by illustrating the non-trivial relationship between local and global measurements for cases considered passive. The global quantities for our hosts are taken from our compilation in Childress et al. (2013b); in three cases, global host sSFR measurements are unavailable for SNe Ia in our local environment sample. Figure 5 shows that half of the SNe with locally passive environments (20/38) have a globally star-forming host (traditionally defined as $\log(sSFR) > -10.5$). This highlights the existing degeneracy when employing global properties: the SNe Ia hosted in star-forming galaxies can have *either* star-forming or passive local environments whereas SNe hosted in passive galaxies are almost certain to have a locally passive environment.

With $\Sigma_{H\alpha}$ above the median value, SNe Ia α are most likely to have young progenitors since an $H\alpha$ signal has been positively detected in their vicinities. The large number of SNe Ia with detections of local star formation in Fig. 5 itself provides an indication that young progenitors exist, in agreement with the statistical analysis of Aubourg et al. (2008). On the other hand, the wide range of observed $\Sigma_{H\alpha}$ is an indication of SNe from

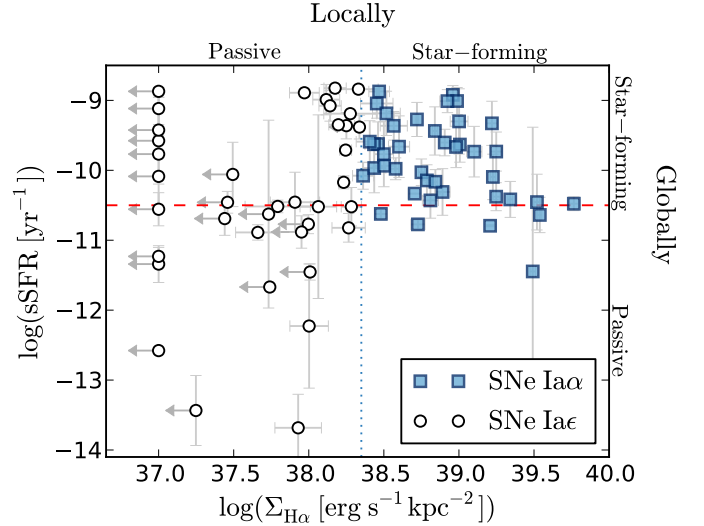


Fig. 5. Local vs. global star-forming environment. Blue squares and open-circles show the SNe Ia from locally star-forming and passive regions, respectively ($\log(\Sigma_{H\alpha}) \gtrless 38.35$, blue-dotted line). Gray arrows indicate points with $\Sigma_{H\alpha}$ signals compatible with zero (detection at less than 2σ). The red-dashed line indicates the limit that is commonly used to distinguish between star-forming and passive galaxies when using global host galaxy measurements ($\log(sSFR) \gtrless -10.5$). Three SNe Ia from our sample do not have sSFR measurements.

both passive and star-forming regions, i.e. from both young and old progenitors (Scannapieco & Bildsten 2005; Mannucci et al. 2005, 2006; Sullivan et al. 2006).

In Fig. 5 there is a relative dearth of SNe Ia with $H\alpha$ detections for $\log(\Sigma_{H\alpha}) < 37.9$ in hosts that are globally star-forming. This then highlights a population having $38.0 < \log(\Sigma_{H\alpha}) < 38.35$ in globally star-forming hosts that are counted as locally passive when we split our sample. Their proximity to the typical WIM level suggests that these could be cases of SNe Ia from old progenitors whose $\Sigma_{H\alpha}$ value is boosted by projection onto the WIM in their hosts. But, they may equally well be SNe Ia from young/intermediate age progenitors where strong star formation has already ebbed at that location in their host. In Sect. 7 we show that moving these cases into the star-forming sample does not change our results significantly. Therefore we prefer to employ a simple split since it is not tuned to any patterns in the data.

4. $\Sigma_{H\alpha}$ and SN Ia light-curve properties

We now compare $\log(\Sigma_{H\alpha})$ to the SN light-curve parameters (Sect. 4.1) and to the corrected Hubble residuals ΔM_B^{corr} (Sect. 4.2). We show that SNe from locally passive regions have faster light-curve decline rates, that the color of SNe Ia is correlated with $\Sigma_{H\alpha}$, and that there is a significant magnitude offset

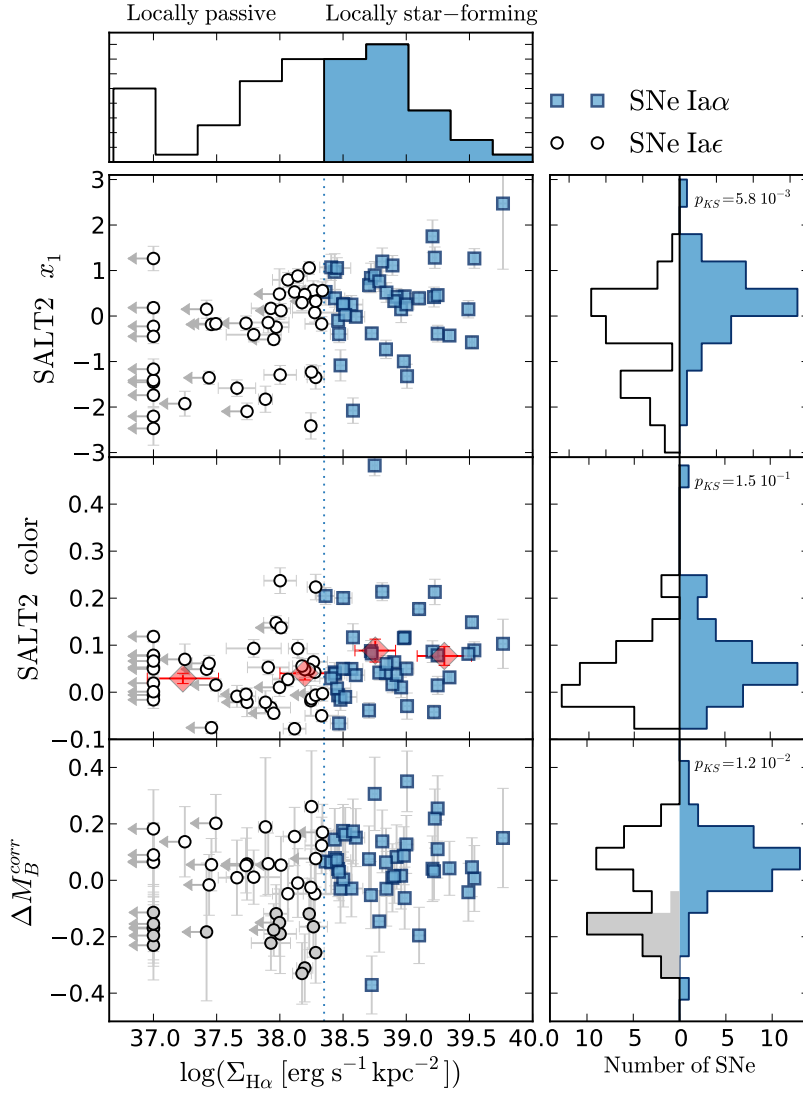


Fig. 6. SN Ia parameters as a function of $\log(\Sigma_{\text{H}\alpha})$, the surface brightness in the 1 kpc radius around the SNe Ia. *Upper panel:* the $\log(\Sigma_{\text{H}\alpha})$ distribution colored with respect to $\Sigma_{\text{H}\alpha}$ subgroups: Ia ϵ and Ia α are shown as empty-black and filled-blue histograms, respectively. *Main panels, from top to bottom:* SALT2 stretch x_1 , color c , and the Hubble residuals corrected for stretch and color ΔM_B^{corr} (with a standardization done over the whole sample). Symbol shapes and colors are the same as in Fig. 5. In the middle panel, filled-red diamonds show the mean SALT2 color measured in bins of $\log(\Sigma_{\text{H}\alpha})$: x-axis error bars indicate the $\log(\Sigma_{\text{H}\alpha})$ dispersion of the SNe of the considered bin. In the ΔM_B^{corr} panel, the M_2 SNe (Ia ϵ with $\Delta M_B^{\text{corr}} < -0.1$, see text) are shown as filled-gray circles. *Right panels, from top to bottom:* marginal distributions of x_1 , c , and ΔM_B^{corr} by subgroups. These bi-histograms follow the same color code as the $\log(\Sigma_{\text{H}\alpha})$ histogram. The contribution of the M_2 SNe to the Ia ϵ ΔM_B^{corr} distribution is shown in gray in the lower right panel.

between SNe from locally star-forming (Ia α) and locally passive (Ia ϵ) regions.

The SALT2 light-curve parameters c and x_1 are known to correlate with the uncorrected absolute B -magnitude at maximum light, M_B . The dispersion in M_B can be reduced significantly by taking advantage of these correlations (Guy et al. 2007):

$$\Delta M_B^{\text{corr}} \equiv (M_B - M_B^0) + (\alpha x_1 - \beta c), \quad (2)$$

where the stretch coefficient α , the color coefficient β , and the average absolute magnitude of the SNe Ia, M_B^0 , are simultaneously fit over the SN sample during the standardization process. The SALT light-curve parameters and Hubble residuals for our SNe Ia have been presented previously in Bailey et al. (2009), Chotard et al. (2011), and Childress et al. (2013a).

For the statistical analyses that follow we use the Kolmogorov-Smirnov test (KS-test) to estimate the discrepancy between observed parameter distributions (x_1 , c , and ΔM_B^{corr}). We also compare the weighted-mean values of those distributions between the $\Sigma_{\text{H}\alpha}$ groups, which we denote using the form $\delta\langle X \rangle(A - B) \equiv \langle X \rangle_A - \langle X \rangle_B$. When exploring correlations we employ the non-parametric Spearman rank correlation test, quoting the correlation strength, r_s , and probability, p_s . p -values below 5% (e.g., $p_{KS} < 0.05$) highlight statistically important

differences between distributions, and we will consider p -values below 1% to be highly significant.

4.1. Light-curve stretch and color

The stretch parameter x_1 and color c are shown in Fig. 6 as a function of $\log(\Sigma_{\text{H}\alpha})$. The weighted means and dispersions for the two subgroups are summarized in Table 1.

4.1.1. The light-curve stretch

The SALT2 stretch x_1 and the $\log(\Sigma_{\text{H}\alpha})$ values are correlated, as demonstrated by a highly significant Spearman rank correlation coefficient: $r_s = 0.42$, $p_s = 7.4 \times 10^{-5}$, 4.2σ . This shows that SNe Ia from low $\Sigma_{\text{H}\alpha}$ environments have on average faster light-curve decline rates. When comparing $\Sigma_{\text{H}\alpha}$ subgroups, we find $\delta\langle x_1 \rangle(\text{Ia}\alpha - \text{Ia}\epsilon) = 0.37 \pm 0.17$ ($p_{KS} = 5.8 \times 10^{-3}$).

At first this might appear to be just the same as the well-established effect whereby globally passive galaxies are found to host SNe Ia with lower stretch, while star-forming host galaxies dominate at moderate stretches (Hamuy et al. 2000; Neill et al. 2009; Lampeitl et al. 2010). Indeed, the x_1 distributions of SNe in globally passive and star-forming hosts ($\log(s\text{SFR}) \leq -10.5^2$)

² See Childress et al. (2013b) for details on the measurement of sSFR for the SNfactory sample.

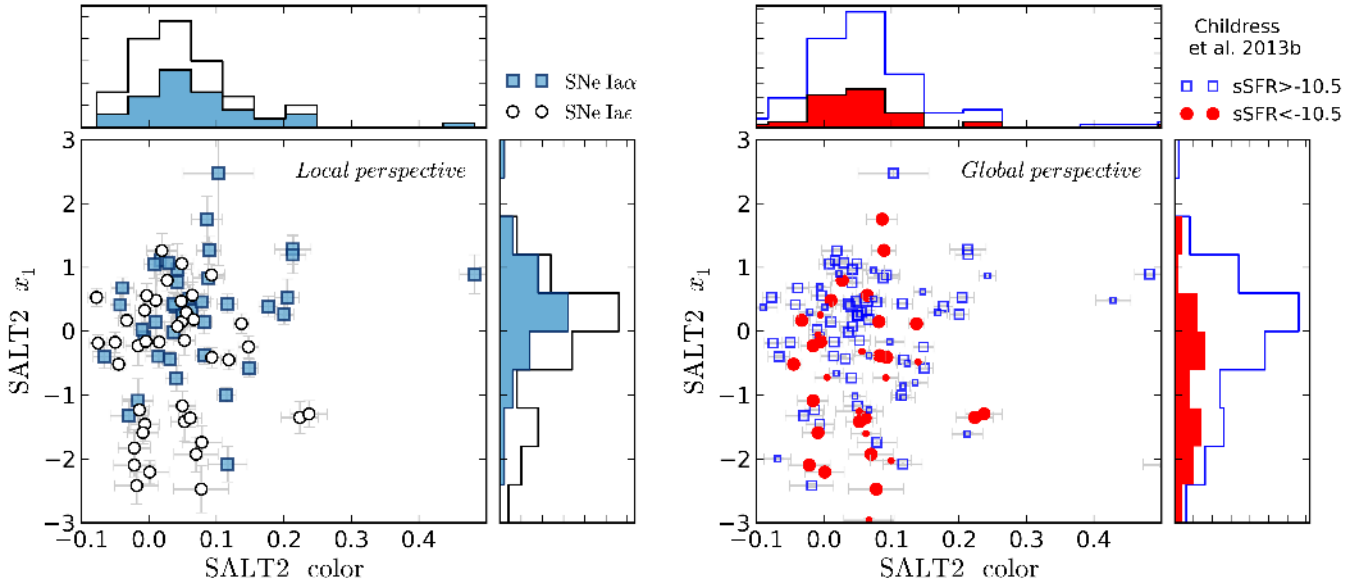


Fig. 7. SALT2 stretch x_1 vs. color c . *Left:* the local perspective. SNe markers and x_1 and c marginalized stacked distributions follow the same color-shape code as Fig. 6. *Right:* the global perspective. Open-blue squares show the globally star-forming hosts and red dots show the globally passive hosts ($\log(sSFR) \leq -10.5$ respectively). Big markers indicate SNe with local measurements, while small markers denote SNe not in our local sample (failed redshift cut, but passed the quality cuts, see Sect. 2.1). Stacked histograms are the marginalized distributions of x_1 and c using the marker color codes. These figures compare to Fig. 2 of Lampeitl et al. (2010). Notice the mix of local environments for moderate x_1 while low x_1 are almost exclusively from passive environments.

differ significantly, having $p_{KS} = 2.0 \times 10^{-3}$ for the SNfactory and $p_{KS} = 10^{-7}$ for SDSS (Lampeitl et al. 2010). We compare in Fig. 7 the global and local pictures in the (c, x_1) plane. These two figures can be compared to Fig. 2 of Lampeitl et al. (2010) for the SDSS sample.

However, our analysis of the local environment displays quite a different stretch distribution for passive environments. We find that 40% of SNe that are locally passive have moderate stretches. This is in strong contrast to global analyses. For our SN sample only 25% of globally passive hosts have SNe Ia with $x_1 > -1$, and in the global analysis of the SDSS dataset (Lampeitl et al. 2010) the percentage of passive environments with moderate stretch is even lower, a mere 11%. This suggests that many SNe Ia originating in passive environments have been mistakenly categorized as coming from star-forming environments by analyses employing galactic properties integrated over the entire host. Were we to lower our dividing line to $\log(\Sigma_{H\alpha}) = 38$, our global and local analyses would then agree, but this still would not result in the paucity of passive environments at moderate stretches seen in the SDSS sample.

Furthermore, we find even stronger evidence that SNe with fast decline rates ($x_1 < -1$) arise in passive environments. In our local analysis 15/18, or 83% are Ia ϵ , and all have a $\log(\Sigma_{H\alpha}) \leq 39$. In contrast, as Fig. 7 shows, our global analysis for $x_1 < -1$ shows only mild dominance by passive galaxies, with 60% being such hosts. In the SDSS sample of Lampeitl et al. (2010), among the SNe Ia with fast decline rates only 54% are globally passive.

In summary, we find that lower stretch SNe Ia are hosted almost exclusively in passive local environments, but that SNe Ia having moderate stretches are hosted by all types of environments.

4.1.2. The light-curve color

We also find that SNe Ia from star-forming environments are on average redder than those from passive environments at the 2.2σ

level: $\delta\langle c \rangle(\text{Ia}\epsilon - \text{Ia}\epsilon) = 0.036 \pm 0.017$ (0.031 ± 0.015 when removing the reddest, SNF20071015-000). This effect is more significant when comparing the tails of the $\log(\Sigma_{H\alpha})$ distribution (lower and upper quartiles), where we find distribution differences with $p_{KS} = 0.026$. As seen in Fig. 6, the SALT2 color, c , and the $\log(\Sigma_{H\alpha})$ values are correlated, with a 2.0σ non-zero Spearman rank correlation coefficient $r_s = 0.21$, with $p_s = 0.054$.

Since dust is associated with active star formation (e.g. Charlot & Fall 2000), a color excess is expected for SNe Ia in strong $\Sigma_{H\alpha}$ environments. (See Chotard et al. 2011, for a discussion of the Type Ia color issue.) This trend has been suggested for SNLS SNe in Sullivan et al. (2010) but is not seen in SDSS data (Lampeitl et al. 2010).

As discussed earlier, by analyzing integrated galaxy properties, global host studies merge SNe Ia ϵ with $x_1 > -1$, and the SNe Ia ϵ , into a single star-forming host category. Figure 7 shows that low and moderate stretch Ia ϵ share the same color distribution. It is then difficult for global analyses to detect the color variation between the star-forming and passive hosts, since both kinds harbor some Ia ϵ . Indeed, in the SNfactory sample globally passive and star-forming hosts produce SNe Ia having the same SALT2 color distribution ($p_{KS} = 0.654$).

4.2. Hubble residuals

The SALT2 raw Hubble residuals ΔM_B are corrected for their stretch and color dependencies (ΔM_B^{corr}) and are shown in Fig. 6 as a function of $\log(\Sigma_{H\alpha})$. The weighted mean values per $\Sigma_{H\alpha}$ group are summarized in Table 1.

4.2.1. The H α bias

We find with a 3.1σ significance that SNe from locally passive environments are brighter than those SNe Ia in locally star-forming environments after color and stretch correction: $\delta\langle M_B^{\text{corr}} \rangle(\text{Ia}\epsilon - \text{Ia}\epsilon) = -0.094 \pm 0.031$ mag ($p_{KS} = 0.012$). The amplitude of this significant brightness offset – hereafter called

the “ $H\alpha$ bias” – is a concern for precision cosmology, since the fraction of SNe Ia from passive environments most likely evolves with redshift, thus creating a redshift dependence on the average SNe Ia luminosity. Distance measurements to these standardizable candles are therefore biased. A more complete discussion of the potential impact on cosmological measurements is presented in Sect. 6.

4.2.2. Corrected Hubble residual distributions

We now investigate the possible origin of this brightness offset between the SNe Ia α and the SNe Ia ϵ ($H\alpha$ bias) by examining the ΔM_B^{corr} distributions of each subgroup. In Fig. 6 we notice the presence of a subgroup of significantly brighter SNe hosted exclusively in locally passive environments. We thus distinguish two modes in the distribution of corrected Hubble residuals: (1) The first mode exists in all environments and has $\Delta M_B^{\text{corr}} \gtrsim 0$. (2) The second mode is exclusive to SNe Ia from low $H\alpha$ environments (Ia ϵ), and it populates the brighter part of the diagram almost exclusively: among the 20 SNe Ia with $\Delta M_B^{\text{corr}} < -0.1$, 17 are Ia ϵ , and only one has a $\log(\Sigma_{H\alpha}) > 39$. For analysis purposes we define and label these modes as follows:

- *Mode 1* (M_1): 65 SNe consisting of all SNe Ia α along with SNe Ia ϵ that have $\Delta M_B^{\text{corr}} > -0.1$ mag.
- *Mode 2* (M_2): 17 SNe Ia ϵ with $\Delta M_B^{\text{corr}} < -0.1$ mag.

Except that both are from locally passive environments, the M_2 subgroup and the subgroup of 15 fast declining ($x_1 < -1$) SNe Ia turn out to not be directly related, having only six SNe in common.

Figure 8 shows the distribution of these two modes fitted by normal distributions (with 3σ clipping). The M_1 SNe are on average fainter ($\langle \Delta M_B^{\text{corr}} \rangle_{M_1} = 0.072 \pm 0.012$ mag) and M_2 SNe Ia are brighter ($\langle \Delta M_B^{\text{corr}} \rangle_{M_2} = -0.191 \pm 0.015$ mag) than the full sample. The standard deviations are 0.099 ± 0.009 mag and 0.060 ± 0.010 mag for M_1 and M_2 , respectively. The weighted RMS gives similar results, with variations at a tenth of the error level. With no clipping, one additional, bright SN is then retained in M_1 , raising the M_1 standard deviation to 0.113 ± 0.010 mag.

These differences in $\langle \Delta M_B^{\text{corr}} \rangle$ would appear to be extremely significant; however, in this case we chose the dividing point in ΔM_B^{corr} , and thus the added degrees of freedom are not accounted for. To better assess the significance of the bimodal structure we use the Akaike Information Criterion corrected for finite sample size (AICc; Burnham & Anderson 2002). When comparing two models, the one with the smallest AICc provides a better fit to the data. The AICc test is similar to a maximum likelihood ratio that penalizes additional parameters.

The two models that we compare are the following: (1) The reference model is a regular normal distribution, with two parameters: a mean and an intrinsic dispersion. (2) The alternative model is bimodal with three parameters: two means and the ratio of the two mode amplitudes. In the bimodal model no intrinsic dispersion is needed, because the SALT2 and peculiar velocity uncertainties are able to fully explain the dispersion of each mode. In both cases the integral of the model is required to equal the number of SNe used in the fit. For the full sample we find $\Delta \text{AICc}(\text{bimodal} - \text{unimodal}) = -5.6$, which strongly favors the bimodal structure. If we remove the possibly contaminated “p.m.s.” cases we find a slightly reduced value of $\Delta \text{AICc}(\text{bimodal} - \text{unimodal}) = -4.3$. Thus, whether we include these or not has little impact. The fact that the bimodal model

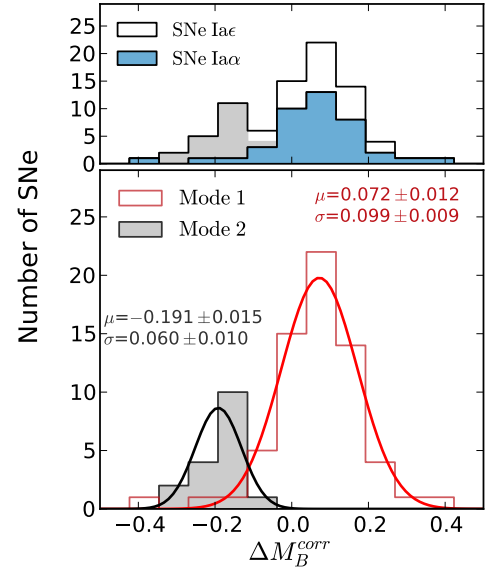


Fig. 8. Distribution of corrected Hubble residuals per $\Sigma_{H\alpha}$ group (top, as in Fig. 6) and per mode (bottom) for the full sample. In the lower panel, the open-red and the filled-gray histograms represent the corrected Hubble residual distributions of M_1 and M_2 , respectively. By definition of the modes, the red histogram corresponds to the stack of the blue distribution with the open histogram above $\Delta M_B^{\text{corr}} = -0.1$ (see the top-panel), while the filled-gray histogram corresponds to the part of the open histogram below $\Delta M_B^{\text{corr}} = -0.1$. Colored solid lines (red for M_1 and black for M_2) show the best fit by a normal distribution (with 3σ clipping). Fit parameters are quoted beside each Gaussian.

does not require the introduction of an ad hoc intrinsic dispersion lends it further weight.

In addition we have tested for bimodality in the Hubble residuals for the locally passive subset alone. Here the first normal mode is forced to match the mean ΔM_B^{corr} of the Ia α subset ($\mu_1 = 0.056$), while the mean of second normal mode and the ratio of the two mode amplitudes are free parameters. Here again there is no need to include intrinsic dispersion, so there are only two parameters. When comparing those two models, $\Delta \text{AICc}(\text{bimodal} - \text{unimodal}) = -3.5$, which again favors the bimodal structure, though less strongly.

In Sect. 5.2.2 we show how this peculiar structure introduces the brightness offset observed between SNe in low- and high-mass hosts. This “mass step” is seen in our sample (Childress et al. 2013a), as well as in all other large surveys (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Johansson et al. 2013). This suggests that this bimodality is not exclusive to the SNfactory data, but is an intrinsic property of SALT2-calibrated SNe Ia. That it has not been noticed before is very likely due to the rarity of SNe Ia having all of the necessary ingredients: well-measured light curves, small uncertainties due to peculiar velocities, and a wide range of $\Sigma_{H\alpha}$, and/or total stellar mass.

5. Discussion

Here we discuss the results presented previously. First, we look for the potential environmental dependency of stretch and color coefficients among the two $\Sigma_{H\alpha}$ subgroups (Sect. 5.1). Next, we investigate the previously-observed relations between host masses and both the SNe stretches (Sect. 5.2.1) and the SNe-corrected Hubble residuals (Sect. 5.2.2). These relations are interpreted from our local analysis perspective.

5.1. The standardization process

Since the distributions of SN Ia parameters have been shown to vary between our two $\Sigma_{H\alpha}$ subgroups, we now investigate whether a unique standardization process applies in the context of SALT2 by comparing stretch and color coefficients (α and β respectively; see Eq. (2)) between the $\Sigma_{H\alpha}$ subgroups. We find that the stretch coefficient, α , is consistent between $\Sigma_{H\alpha}$ groups, having $\delta\alpha(Ia\alpha - Ia\epsilon) = -0.020 \pm 0.037$.

The color coefficient of SNe between low- and high- $\Sigma_{H\alpha}$ differ by $\delta\beta(Ia\alpha - Ia\epsilon) = 1.0 \pm 0.41$, but this difference is dominated by the reddest SN, SNF20071015-000. After removing it, the color coefficients are not significantly different: $\delta\beta(Ia\alpha - Ia\epsilon) = 0.67 \pm 0.45$. Therefore, our analysis is insensitive to any color coefficient variations between $\Sigma_{H\alpha}$ groups. The color of the outlier, SNF20071015-000, is likely to be dominated by dust, for which a larger color coefficient is expected, as we have shown in Chotard et al. (2011).

We also measured what influence the lowest-stretch SNe Ia ϵ from passive environments may have on the existence of the brighter M_2 mode. Our sample contains 15 Ia ϵ with $x_1 < -1$; we performed an independent standardization on the remaining 67 SNe, among which 26 are Ia ϵ , 11 of which have $\Delta M_B^{\text{corr}} < -0.1$. This fraction, 11 $M_2/26$ Ia ϵ , is exactly the same as that computed from the full sample (17/41). Therefore, we conclude that the existence of the M_2 mode is unrelated to the presence of a fast decline rate subgroup in passive environments.

5.2. Host mass vs. SN properties: A local environment perspective

We investigate here the correlations found by global host studies between total host stellar mass and both the stretch and the SN-corrected Hubble residuals (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Childress et al. 2013a; Johansson et al. 2013).

5.2.1. Mass-stretch correlation

Stretch has been shown to correlate with the host's stellar mass (e.g., Sullivan et al. 2010). Figure 9 shows x_1 as a function of host mass for our sample (see Childress et al. 2013a, for details on the SNfactory host mass analysis). In agreement with the literature, we find a correlation between mass and stretch when all the SNe Ia are considered together, with a Spearman rank correlation coefficient that is non-zero at the 3.4σ level ($r_s = -0.36$, $p_s = 9.2 \times 10^{-4}$).

When looking at $\Sigma_{H\alpha}$ subgroups, though, we notice that SNe Ia from locally star-forming environments (Ia α) show no correlation between their stretch and the mass of their host ($r_s = -0.02$; $p_s = 0.89$). The original correlation is actually driven by SN Ia ϵ from locally passive environments ($r_s = -0.55$; $p_s = 4.8 \times 10^{-3}$, a 3.0σ significance). More precisely, the correlation appears to arise from the bimodal x_1 structure of this subgroup, which we previously noted in Fig. 6. Figure 9 clearly shows that the correlation is related to the L-shaped distribution of SNe Ia ϵ in the x_1 -mass plane: SNe with $x_1 > -1$ contribute to the whole range of host masses, whereas the ones with $x_1 < -1$ arise exclusively in massive galaxies ($\log(M/M_\odot) > 10$).

Measurements of the local environment indicate that the light-curve widths of SNe in locally star-forming regions are independent of the total stellar mass of their hosts. For SNe Ia ϵ , the total stellar mass of the host is not a stretch proxy as suggested by Sullivan et al. (2010) but an indicator of whether the two

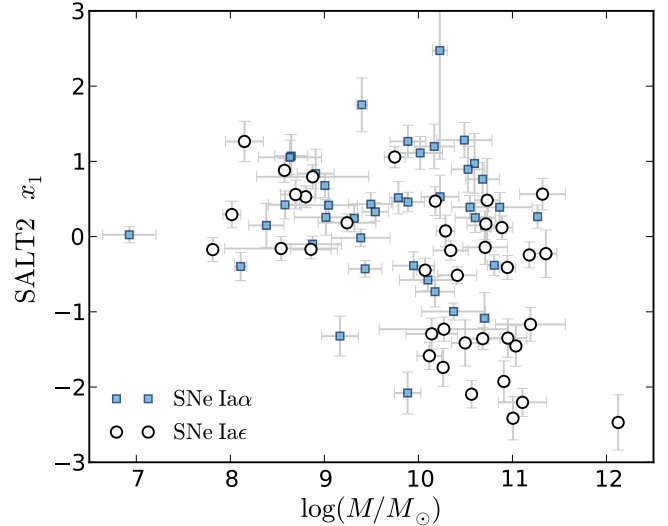


Fig. 9. SN Ia x_1 vs. total host stellar mass (Childress et al. 2013a). Markers follow the same color and shape code as in Fig. 6. Note the distinctive “L”-shaped distribution of the SNe Ia ϵ .

stretch subgroups ($x_1 \lesssim -1$) are represented or not. From this new perspective, the mass-stretch correlation shown in Fig. 2 of Sullivan et al. (2010) could be re-interpreted as being driven by a relatively independent grouping of SNe having higher masses ($\log(M/M_\odot) > 10.2$) and lower stretches ($s < 0.9 \sim x_1 < -1$; Guy et al. 2007).

5.2.2. The “mass step”

The second known correlation between host masses and SNe Ia properties is an offset in corrected Hubble residuals between SNe hosted by high-mass galaxies (brighter) and those from low-mass hosts (fainter). This can be seen in Fig. 10. This mass effect has been observed by all of the large SNe Ia surveys (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Childress et al. 2013a; Johansson et al. 2013), and compiled in Childress et al. (2013a). Hereafter, we use the term “plateau” to denote the averaged ΔM_B^{corr} values for SNe from either high- (H) or low-mass (L) galaxies, with a dividing point set at $\log(M/M_\odot) = 10$. In Childress et al. (2013a), we showed that such a step function is a very good description of the data. We refer to the difference in the brightness of these two plateaus as the “mass step.” For our subset of the SNfactory sample this offset reaches $\delta\langle M_B^{\text{corr}} \rangle(H - L) = -0.098 \pm 0.031$ mag.

We notice in Fig. 10 (see also Fig. 2 of Childress et al. 2013a) that the upper part of the envelope of the distribution is constant with mass, whereas the lower part of the distribution extends to bright ΔM_B^{corr} values for masses above $\log(M/M_\odot) \sim 10$. We see that the high-mass plateau is brighter only because a subgroup of bright SNe exists in massive hosts. A similar trend can be observed in Fig. 4 of Sullivan et al. (2010) for SNLS, in Fig. 15 of Johansson et al. (2013) for SDSS, and in Fig. 5 of Childress et al. (2013a) where we combined all available data.

We see in the top panel of Fig. 10 that the local $H\alpha$ environment changes with the total stellar mass of the host. For low masses up to $\log(M/M_\odot) \lesssim 10$, locally star-forming environments dominate (23 Ia α /34). In more massive hosts ($\log(M/M_\odot) \gtrsim 10$), however, the local SN environment presents a marked change, and the locally passive cases are favored (27 Ia ϵ /45). Since only a few M_2 SNe Ia ϵ are present in lower

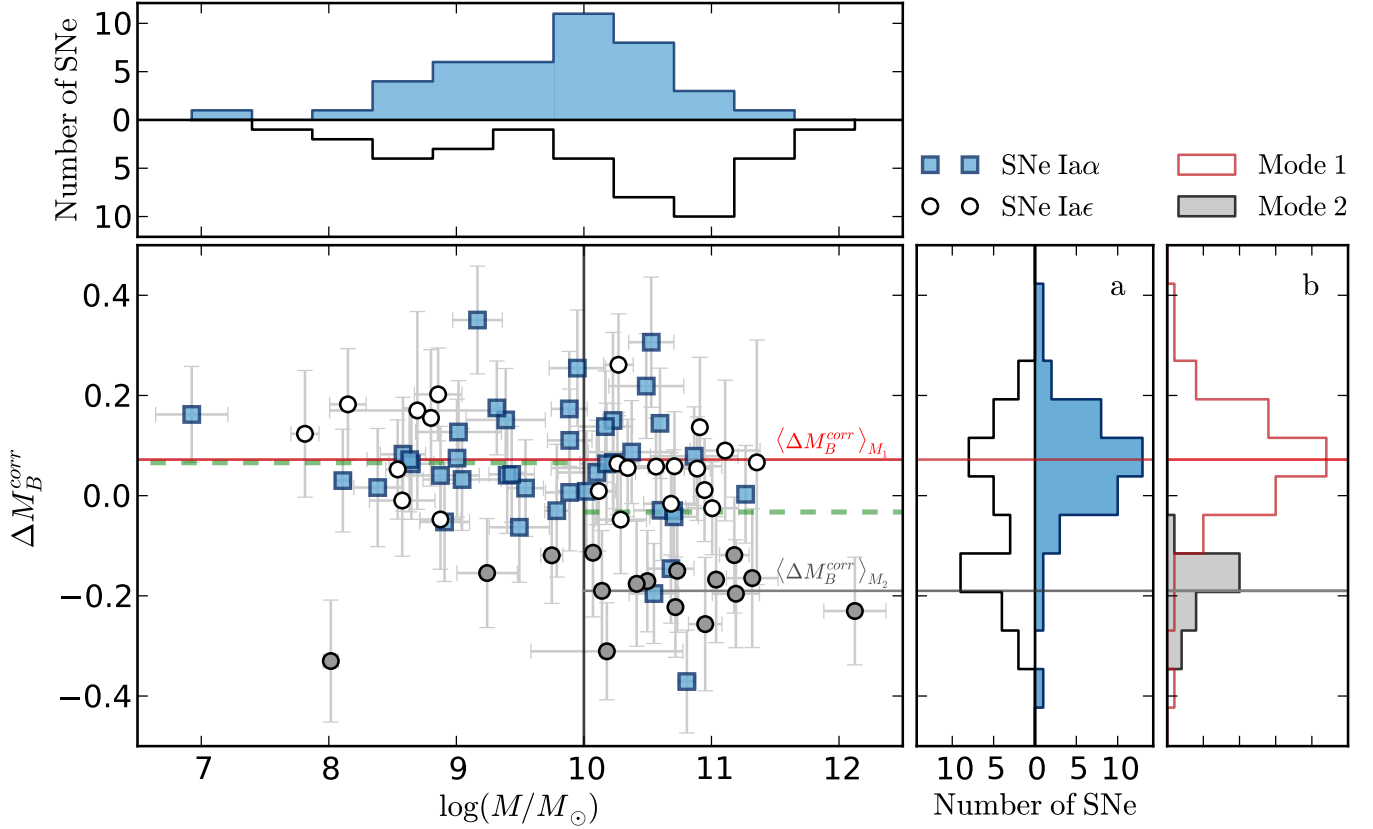


Fig. 10. Corrected Hubble residuals as a function of the total host stellar mass, showing the mass step. Markers follow the same color and shape code as in Fig. 6. *Top*: total host stellar mass distribution per $\Sigma_{\text{H}\alpha}$ subgroup. *Right*: ΔM_B^{corr} distribution per $\Sigma_{\text{H}\alpha}$ subgroup **a**) and per mode **b**), as shown in Fig. 8. Horizontal red and gray lines indicate M_1 and M_2 weighted mean values, respectively. *Central panel*: left and right green horizontal dashed lines indicate the weighted mean ΔM_B^{corr} of SNe Ia hosted by galaxies more or less massive than log(M/M $_{\odot}$) = 10 (vertical gray line). The difference between those two magnitudes defines the “mass step.”

mass hosts (3 $M_2/34$), the first plateau happens to be equal to the mean M_1 value, with $\langle \Delta M_B^{\text{corr}} \rangle_L = 0.066 \pm 0.021$. In the upper mass range, because of the rise of the Ia ϵ subgroup populating the brighter M_2 mode, the average brightness increases up to the level of the second plateau. The Ia α population shows no appreciable mass step; we find $\delta \langle M_B^{\text{corr}} \rangle_{\text{Ia}\alpha}(\text{H} - \text{L}) = -0.06 \pm 0.04$, largely driven by the bright SNF20070701-005. There is a strong possibility that this SN Ia is a false-positive H α association (see Sect. 6.2), and if we remove it we find $\delta \langle M_B^{\text{corr}} \rangle_{\text{Ia}\alpha}(\text{H} - \text{L}) = -0.04 \pm 0.04$. *We conclude therefore that the existence of a brighter mode, completely dominated by SNe having locally passive environments, causes both the H α bias and the mass step.*

6. Consequences for cosmology

The proportion of SNe from locally passive environments has surely changed with time, so the fraction of M_2 SNe will depend on redshift, leading us to expect the amplitude of the mass step will change as well. In this section we develop a first estimate of this evolution bias and its consequence for measuring cosmological parameters. In Sect. 6.1, we predict the redshift dependence of the magnitude bias due to evolution in the relative numbers of SNe Ia α and SNe Ia ϵ given the H α bias we observe. We then estimate the bias on measurement of the dark energy equation of state parameter, w , that would result if this evolution does indeed occur. By then coupling the H α bias and the mass step as discussed in Sect. 6.1.2, we verify the predicted evolution of the mass step using data from the literature. In Sect. 6.2, we

introduce a subclass of SNe whose Hubble-residual dispersion is significantly reduced by avoiding this bimodality. We discuss possible strategies for mitigating this bias in Sect. 6.3.

6.1. Evolution of the SNe Ia magnitude with redshift

6.1.1. Evolution model

The mean sSFR is known to increase with redshift (e.g. Pérez-González et al. 2008), which most likely decreases the proportion of SNe associated with locally passive environments (Sullivan et al. 2006; Hopkins & Beacom 2006). Because of the H α bias, the average SN brightness is expected to be redshift dependent.

We define $\psi(z)$ as the fraction of SNe located in locally passive environments (Ia ϵ) as a function of redshift. Assuming that the brightness offset between Ia α and Ia ϵ is constant with redshift, the mean corrected B -magnitude of SNe Ia at maximum light can then be written as

$$\begin{aligned} \langle M_B^{\text{corr}} \rangle(z) &= (1 - \psi(z)) \times \langle M_B^{\text{corr}} \rangle_{\text{Ia}\alpha} + \psi(z) \times \langle M_B^{\text{corr}} \rangle_{\text{Ia}\epsilon} \\ &= \langle M_B^{\text{corr}} \rangle_{\text{Ia}\alpha} + \psi(z) \times \delta \langle M_B^{\text{corr}} \rangle_{\text{Ia}\epsilon}(\text{Ia}\epsilon - \text{Ia}\alpha). \end{aligned} \quad (3)$$

Pérez-González et al. (2008) demonstrate that the global galactic sSFR increases by a factor of ~ 40 between $z = 0$ and 2 (see also Damen et al. 2009). This evolution can be adequately approximated as

$$\log(\text{sSFR})(z) \simeq \log(\text{sSFR}_0) + 0.95 \times z. \quad (4)$$

Since sSFR measures the fraction of young stars in a galaxy, we suggest as a toy model that the proportion of SNe from locally passive environments evolves in complement (Sullivan et al. 2006) and therefore decreases with z :

$$\psi(z) = (K \times 10^{0.95z} + 1)^{-1}. \quad (5)$$

From the definition of the Ia α /Ia ϵ subgroups, the SNfactory sample sets the normalization to $\psi(z = 0.05) = 41/82 = 50 \pm 5\%$ (Cameron 2011); hence $K = 0.90 \pm 0.15$.

Then, using SN, CMB, BAO, and H_0 constraints as in Suzuki et al. (2012), along with the assumption that the Universe is flat, we estimate the impact of a bias in SN Ia luminosity distance measurements. Relative to existing SN cosmological fits, we find that shifting the SN Ia luminosity distances according Eqs. (3) and (5) would shift the estimate of the dark energy equation of state by $\Delta w \approx -0.06$ (Rubin, priv. comm., as estimated using the Union machinery, Kowalski et al. 2008; Amanullah et al. 2010; Suzuki et al. 2012).

6.1.2. Prediction of the mass step evolution

The H α bias is due to a brightness offset between SNe Ia from locally star-forming and locally passive environments. Guided by Fig. 10, in Sect. 5.2.2, we then made a connection between the H α bias and the mass step by noting the strong change in the proportion of SNe Ia α and SNe Ia ϵ on either side of the canonical mass division at $\log(M/M_\odot) = 10$.

In Appendix A the mathematical connection between the H α bias and the amplitude of the mass step is laid out. To a good approximation, the near absence of bright SNe Ia ϵ among low-mass hosts means that the low-mass plateau is equal to the average magnitude of the SNe Ia α , and is therefore constant with redshift. By contrast, the brighter high-mass plateau has been shown to arise from a subgroup of bright SNe Ia ϵ ; thus, the amplitude of the mass-step will evolve along with the fraction of SNe Ia ϵ , as given by $\psi(z)$.

Thus, while local H α measurements are not available for high-redshift SNe Ia in the literature, our hypothesis – that the redshift evolution of the fraction of SNe Ia ϵ induces a reduction of the influence of the bright SNe that creates both the mass step and the H α bias – can be tested using the same evolutionary form, $\psi(z)$. We consequently predict (see Appendix A.2) that the amplitude of the mass-step, $\delta\langle M_B^{\text{corr}} \rangle(\text{H} - \text{L})$, evolves as

$$\delta\langle M_B^{\text{corr}} \rangle(\text{H} - \text{L}; z) \simeq \psi(z) \times \frac{\delta\langle M_B^{\text{corr}} \rangle(\text{H} - \text{L}; z = 0.05)}{\psi(z = 0.05)}, \quad (6)$$

where setting the constant term, $\delta\langle M_B^{\text{corr}} \rangle(\text{H} - \text{L}; z = 0.05)$, equal to our measured mass step provides the normalization.

6.1.3. Verification of mass-step evolution

Figure 11 shows the predicted redshift evolution of the amplitude of the mass step when assuming our simple SNfactory-normalized model. We compare this model to mass steps measured using literature SNe from SNLS, SDSS, and non-SNfactory low- z datasets (Sullivan et al. 2010; Gupta et al. 2011; Kelly et al. 2010, respectively) from the combined dataset of Childress et al. (2013a). We split those data into four redshift bins with equal numbers of SNe Ia (≈ 120 SNe Ia in $z < 0.18$, $0.18 < z < 0.31$, $0.31 < z < 0.6$ and $0.6 < z$ ranges), and we measured the magnitude offset between SNe in low- and high-mass hosts assuming a step located at $\log(M/M_\odot) = 10$. Figure 11 shows that our simple model qualitatively reproduces

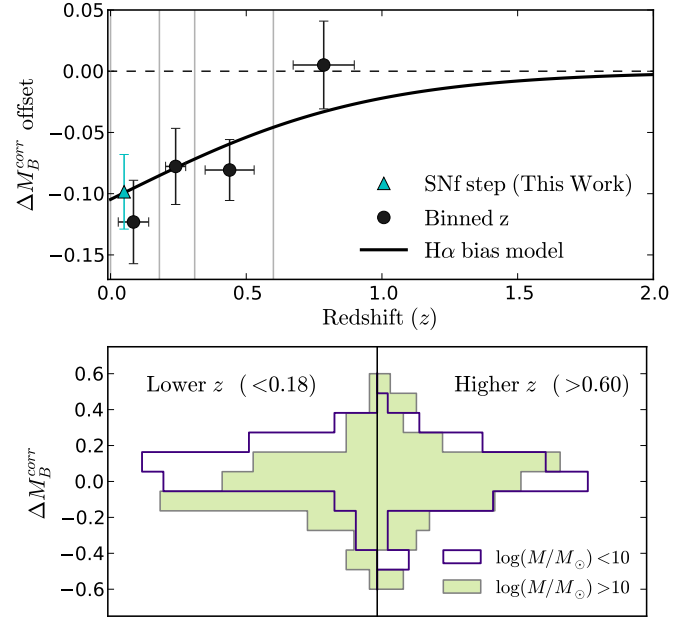


Fig. 11. Observed and predicted redshift evolution of the ΔM_B^{corr} offset between SNe from low- and high-mass hosts ($\log(M/M_\odot) \lessgtr 10$), i.e. the “mass step”. *Top*: black markers show the observed mass step offset per redshift bin (delimited by gray vertical lines). Error bars in redshift represent the dispersion within each redshift bin. The black line is the prediction from Eq. (5), whose amplitude has been set to the SNfactory mass step amplitude at $z = 0.05$ (filled-cyan triangle). *Bottom*: distribution of the ΔM_B^{corr} of SNe Ia from low- (filled-yellow) and high-mass (open-purple) hosts. The left histograms correspond to the closest SNe ($z < 0.18$) while the right ones are for the highest- z SNe ($z > 0.6$). The difference within a redshift bin of the mean value for low- and high-mass distributions defines the mass step at this redshift, as plotted in the upper panel.

the measured mass-step evolution with redshift. Compared to a fixed mass-step anchored by the SNfactory data, our model gives $\Delta\chi^2 = -5.7$ for the literature datasets. This provides external confirmation of behavior consistent with the H α bias at greater than 98% confidence.

6.1.4. Interpretation and Literature Corrections

From this observation we draw several conclusions. (1) The amplitude of the mass step indeed decreases at higher redshift, so host mass cannot be used as a third SN standardization parameter in the manner it has been (Lampeitl et al. 2010; Sullivan et al. 2010). (2) The observed mass steps follow the predicted evolution based on the H α bias quite well. This in turn lends further support to the idea that the H α bias is the origin of the magnitude offset with host mass. As the mass-step bias is observed in different datasets, the H α bias appears to be a fundamental property of SNe Ia standardized using SALT2. (3) Any ad hoc correction of the mass step by letting SNe Ia from low- and high-mass hosts have different absolute magnitudes will be inappropriate since this assumes that high-mass hosted SNe are brighter in a constant way (Conley et al. 2011), ignoring the observed redshift evolution. Doing so will bias the SN Ia α population from high-mass hosts that dominate at higher z and miss the observed evolution of mean SNe Ia magnitude. Therefore, such a correction will not remove the bias on the dark energy equation of state, which we estimate to be $\Delta w \sim 0.06$.

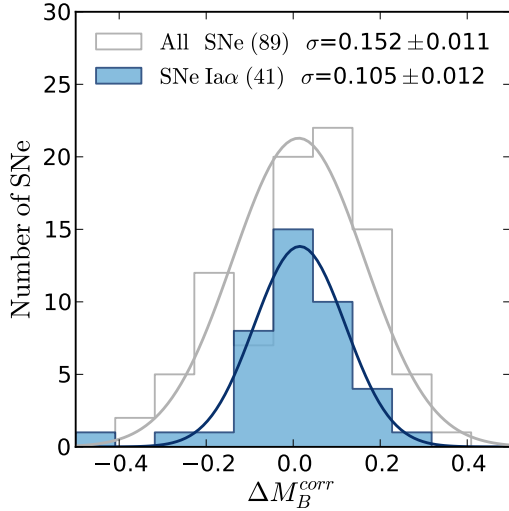


Fig. 12. SN Ia α corrected Hubble residual distributions ($\Delta M_B^{\text{corr}}(\text{Ia}\alpha)$, blue-filled histogram), and its best Gaussian fit (solid-blue line, one 3σ -outlier rejected). The standardization has been performed on only SN Ia α . For comparison, the full sample residual distribution (for a full sample standardization) is shown by the open histogram, with its best Gaussian fit in gray. Both distributions were generated from independent standardizations and are therefore centered on zero.

Of course application of a fixed mass-step correction remains useful for bringing into agreement two datasets at the same redshift that have different proportions of low-mass and high-mass host galaxies due to survey selection effects. Whether a correction using a fixed mass step might accidentally help or hurt in correcting the redshift evolution of the $H\alpha$ bias depends on the – currently unknown – correlation of the parameters of Eqs. (3) and (5) with the redshift evolution in the ratio of high- to low-mass host galaxies.

6.2. Type Ia α SNe: Homogeneous SALT2 candles

The SN Ia α are unimodal in stretch and in corrected Hubble residuals, and are therefore free of the aforementioned $H\alpha$ bias/mass step. The ΔM_B^{corr} distribution for this new group of supernovae, when the SALT2 standardization is performed on this subsample alone, is shown in Fig. 12.

SN Ia α standardization generates a smooth symmetric residual distribution, with a significantly smaller magnitude dispersion of $\sigma = 0.105 \pm 0.012$ mag (after 3σ clipping) than the full initial sample ($\sigma = 0.152 \pm 0.011$ mag, no outlier). This dispersion agrees with the original M_1 fit (0.099 ± 0.009 mag) and corresponds to a significant reduction of $\sim 30\%$ of the Hubble residual dispersion.

To check the robustness of this result we conducted several additional tests. First we considered the effect of including the 3σ outlier, SNF20070701-005. Doing so increases the residual standard deviation to 0.126 ± 0.014 mag (nMAD of 0.108 mag), but we note that this outlier falls within the brighter part of the distribution, potentially polluted by M_2 SNe. This SN might just be a case of misassociation with a star-forming environment, as discussed in Sect. 3. This possibility is reinforced by the fact that this host is globally passive, with $\log(sSFR) = -10.8$ (Childress et al. 2013a).

Next, we performed a permutation test based on independent standardization trials for 41 randomly selected SNe from the full

sample. The results attest to the high significance of the environmental selection, giving $p = 1.9 \times 10^{-3}$.

Finally, K -fold cross-validation was employed to measure the predictive power of our model. Since it avoids overfitting the sample, cross-validation results are not expected to be as good as the original fit (Kim et al. 2013). We find $\sigma = 0.117 \pm 0.014$ mag using $k = 10$, which is compatible with our original results. The quoted error includes a marginal dispersion of 0.004 mag from random “fold” selections.

6.3. Mitigation strategies

The $H\alpha$ bias is a concern for cosmology, since it reveals a local environmental dependency, most probably a progenitor effect not accounted for by current SN standardization methods. It is necessary for ongoing and future surveys to consider it. The best solution would be if additional light curve or spectral features could be identified that can be used to remove the impact of local host properties. Another possibility would be to include the bimodality in the cosmology fitter, treating the redshift dependence and relative fraction of passive environments as free parameters. However, this seems perilous because it could mask or induce signatures of exotic dark energy, and would likely require light curves with much better statistical accuracy in order to resolve the bimodality. Implementation of our model from Sect. 6.1.1 also could be considered. Examining these and other model-dependent correction possibilities is left for future work. Alternatively, it could prove useful to focus on the Ia α subgroup for cosmological analyses, since these appear to be free of environmental biases.

For cosmological measurements naturally it is not permissible to split the SN Ia sample based solely on Hubble diagram residuals, e.g. one cannot directly select only the homogeneous Mode 1 SNe. However, one may select a subsample of SN Ia based on their local environment properties: it is then possible to remove the brighter Mode 2, which is exclusively found in locally passive environments, by discarding the entire Ia ϵ group. This is not as draconian as it may sound; while only $\sim 50\%$ of the sample would be retained, this subset has roughly $1.8\times$ as much statistical weight per SN. Thus, the statistical power is nearly the same as using the full sample. Of course obtaining local environment measurements could be observationally expensive, but Fig. 11 indicates that most of the bias is at lower redshifts, where local environment measurements are less difficult. Since Ia α appear to be dustier, this might add some complications, but in our dataset the Ia α standardize well despite this. We note that removing SNe from globally passive hosts will only remove approximately half of the SN Ia ϵ . However, at least then local measurements would not be needed for these.

In conclusion, SN Ia from passive environments (Ia ϵ) appear to cause the known (yet not understood) environmental biases, and we raise the possibility of removing them for cosmological studies. As SN Ia α form an homogeneous subgroup of standardizable candles, free of environmental biases and therefore showing a tighter dispersion on the Hubble diagram, they could be used exclusively for cosmological analyses.

7. Robustness of the analysis

In this section, we analyze the robustness of our results, by testing potential issues in our analysis: (1) the impact of seeing given our 1 kpc aperture; (2) the influence of SNe potentially misassociated with $H\alpha$ signal from host galaxy cores and (3) the influence of the $\Sigma_{H\alpha}$ boundary defining the Ia ϵ and Ia α subgroups.

The general conclusion of these tests is that our results are not significantly affected by changes in our assumptions.

7.1. Restframe aperture and redshift bias

All our spectra have been averaged over an identical spatial aperture of 1 kpc radius (see Sect. 2.2.3). However, the atmospheric seeing PSF correlates spaxels on the arcsecond scale. For the SNfactory dataset the median seeing is 1''.1. This corresponds to a projected correlation length of ~ 0.65 kpc at $z = 0.03$; ~ 1.1 kpc at $z = 0.05$, and ~ 1.6 kpc at $z = 0.08$. The redshift therefore has an influence on the amount of independent information in the 1 kpc radius aperture around the SN due to the seeing. Seeing also allows contamination of the local environment from bright sources outside the aperture.

However, a Spearman rank correlation analysis shows no correlation between $\log(\Sigma_{H\alpha})$ and z ($r_s = 0.17$, $p_s = 0.14$), and both $\Sigma_{H\alpha}$ subgroups have similar redshift distributions ($p_{KS} = 0.25$). Consequently, we believe that our analysis is relatively unaffected by a redshift bias induced by seeing.

7.2. SNe with potentially misassociated $H\alpha$ signals

Supernovae close to the center of very inclined hosts (referred to as “p.m.s”, see Sect. 3) have been directly removed from the main analysis, given the possible misassociation with $H\alpha$ from the core of the galaxy. As described below, when we include those SNe, none of the previous results are significantly affected:

Color relation: the observed correlation between c and $\Sigma_{H\alpha}$ is slightly more significant, with a Spearman rank correlation coefficient of $r_s = 0.22$ ($p_s = 0.035$);

$H\alpha$ bias: the bias increases marginally, with $\delta\langle M_B^{\text{corr}} \rangle(Ia\epsilon - Ia\alpha) = -0.102 \pm 0.031$ mag, ($p_{KS} = 6.5 \times 10^{-3}$);

Stretch and host mass: x_1 and the total host stellar mass remain uncorrelated for SNe $Ia\alpha$ ($r_s = 0.07$, $p_s = 0.66$);

SNe $Ia\alpha$ dispersion: the $Ia\alpha$ ΔM_B^{corr} dispersion increases to 0.115 ± 0.012 mag ($p = 0.011$), which is still compatible with our fiducial result.

7.3. Influence of the $Ia\alpha/Ia\epsilon$ boundary

In our fiducial analysis the division between locally passive ($Ia\epsilon$) and locally star-forming ($Ia\alpha$) subgroups was set at the median value $\log(\Sigma_{H\alpha}) = 38.35$ of a 82 SN sample. The confidence interval for this population split is 37–45 (Cameron 2011). The numerical values for our main results when using this range for the $Ia\alpha/Ia\epsilon$ boundary are as follows:

$H\alpha$ bias: the bias changes within the errors bars, with $\delta\langle M_B^{\text{corr}} \rangle(Ia\epsilon - Ia\alpha) = -0.101 \pm 0.031$ mag and $\delta\langle M_B^{\text{corr}} \rangle(Ia\epsilon - Ia\alpha) = -0.075 \pm 0.032$ mag for 37 and 45 $Ia\epsilon$, respectively;

Stretch and host mass: x_1 and the total host stellar mass of the SNe $Ia\alpha$ remain uncorrelated in both cases, giving $p_s = 0.84$;

SNe $Ia\alpha$ dispersion: the $Ia\alpha$ ΔM_B^{corr} dispersion is the same within the error bars, with 0.115 ± 0.012 mag and 0.112 ± 0.012 mag for 37 and 45 $Ia\epsilon$, respectively.

The changes are minor, demonstrating the robustness of our analysis to a shift in the $Ia\alpha/Ia\epsilon$ limits.

Furthermore, in Sect. 3 we pointed out cases of SNe $Ia\epsilon$ in globally star-forming hosts located near our division point, e.g., having $\log(\Sigma_{H\alpha}) \sim 38$ and $sSFR > -10$. Whether they are truly locally passive or locally star-forming is therefore somewhat uncertain. As itemized below, we find that our main results do not

depend on whether those SNe are included in the $Ia\alpha$ subgroup. However, three of these cases are bright and have been counted as M_2 in our fiducial analysis, therefore moving them from $Ia\epsilon$ to $Ia\alpha$ increases the dispersion of Hubble residuals of the SNe $Ia\alpha$ subset.

$H\alpha$ bias: the bias marginally changes, with $\delta\langle M_B^{\text{corr}} \rangle(Ia\epsilon - Ia\alpha) = -0.097 \pm 0.032$ mag;

Stretch and host mass: x_1 and the total host stellar mass of the SNe $Ia\alpha$ remain uncorrelated, giving $p_s = 0.57$;

SNe $Ia\alpha$ dispersion: the $Ia\alpha$ ΔM_B^{corr} dispersion is degraded by the inclusion of bright SNe that skew the normal distribution: $\sigma = 0.144 \pm 0.014$ mag (no SNe have been clipped).

8. Summary and conclusion

Using the SuperNova Integral Field Spectrograph (SNIFS), we have assembled a sample of 89 nearby SNe Ia in the redshift range $0.03 < z < 0.08$ with accurate measurements of the $H\alpha$ surface brightness within a 1 kpc radius ($\Sigma_{H\alpha}$) used as a tracer of young stars in the SN neighborhood.

This sample was split in two at the median value $\log \Sigma_{H\alpha} = 38.35$, which happens to correspond to the mean WIM $H\alpha$ surface brightness of galaxies (Oey et al. 2007) and to the mean $H\alpha$ sensitivity level at our highest redshift. SNe with low $\Sigma_{H\alpha}$ were then designated as “locally passive” ($Ia\epsilon$), while those with high $\Sigma_{H\alpha}$ were designated as “locally star-forming” ($Ia\alpha$). The wide range of measured $\Sigma_{H\alpha}$ indirectly confirms the existence of SNe Ia associated to both young and old stellar populations. We then studied variations in SNe properties as a function of this local host parameter as listed below.

Color: our local analysis highlights a 2σ significance correlation between $\log(\Sigma_{H\alpha})$ and the SALT2 color c , with the SNe $Ia\alpha$ being redder, as expected (Charlot & Fall 2000).

Stretch: the relationship between SN light-curve stretch and local star formation activity is more complex than suggested by previous global host studies. Faster declining SNe ($x_1 < -1$) are indeed strongly favored by locally passive environments, but passive local environments also host SNe with moderate stretches. Lower stretch SNe Ia are hosted in locally passive environments, but we find that moderate stretch SNe Ia are hosted by all types of environments. The local perspective also shows that the correlation between the host stellar mass and SN stretch is entirely created by the SNe $Ia\epsilon$. The stretches of SNe $Ia\alpha$, from locally star-forming regions, are uncorrelated with the total stellar masses of their hosts.

Hubble residuals: after routine SALT2 standardization using stretch and color, we showed that the SN Ia Hubble residuals (ΔM_B^{corr}) are significantly environment-dependent. SNe $Ia\epsilon$ from locally passive regions are 0.094 ± 0.031 mag brighter than SNe $Ia\alpha$ from locally star-forming regions. This $H\alpha$ bias stems from a bimodal structure in the Hubble residual distribution. The first mode, denoted as M_1 , is present in all environments, independent of the local star formation activity. The second mode, M_2 , is intrinsically brighter, is exclusive to locally passive environments, and occurs predominately in high-mass hosts. We noted that this peculiar structure naturally explains the previously observed “mass step”, i.e. the offset in brightness between SNe from low- and high-mass hosts (e.g., Childress et al. 2013a).

This suggests that the $H\alpha$ bias is not exclusive to our sample and has a more fundamental origin than the global host effect. Additional SN data, with measurement uncertainties below the 0.1 mag, will be critical for confirming the Hubble residual bimodality. Our analysis does not suggest any significant dependence on the local $H\alpha$ environment of the stretch or color coefficients used in standardization.

Cosmological implications: the $H\alpha$ bias is a concern for cosmology since the fraction of SNe in star-forming environments most likely changes with redshift, which implies an evolution with z of the mean B -magnitude of SNe Ia after standardization. Using a simple toy model based on the evolution of the specific star formation rate of galaxies with redshift, we estimated that this effect could shift the measurement of the dark energy equation of state parameter by $\Delta w \sim -0.06$. Currently employed constant mass-step corrections might accidentally reduce or increase the bias on w , but not remove it. Moreover, the amplitude of the mass step is shown to evolve with redshift as predicted, which supports our claim that both the $H\alpha$ bias and the mass step arise from the same underlying phenomenon. Future cosmological analyses will need to consider these environmental dependencies. An ideal solution would be to find additional light curve or spectral features able to correct this bias. Another solution would be to focus on a subsample of SNe Ia free from this known – yet not understood – biases.

SNe Ia α as homogeneous SALT2 candles: SNe Ia from locally passive environments (Ia ϵ) appear to be the cause of all the biases we have observed. We raised the idea of removing them from cosmological fits for this reason. The remaining bias-free SNe Ia α have an intrinsic Hubble residual dispersion reduced to 0.105 ± 0.012 mag, suggesting that a selection based on local environment would significantly improve the quality of SNe Ia as cosmological distance indicators. We further noted that this remaining dispersion is entirely consistent with our measurement uncertainties; no intrinsic dispersion is necessary. The cost of suppressing this serious bias would be a minor loss in net statistical power compared to using the full SN sample, and the need for measurements of the local environment.

At this juncture SN cosmology is limited by systematic errors (Conley et al. 2011; Saunders et al. 2013). Calibration issues are thought to set the current limits, but our first analysis of the local SN environments has revealed strong correlations between SNe and the star-forming activity of their immediate environment. This is most likely caused by our limited knowledge of the progenitors of the SNe Ia, the existence of potential SN subgroups, and the evolution with redshift of these standardizable candles.

For future SN cosmology efforts, we thus suggest further studies exploring the properties of SN Ia local host environments. Notably, the following local host properties may bring essential clues leading to the minimization of progenitor dependencies: gas and stellar metallicities, star formation history surrounding the SNe, and local interstellar dust extinction. Continuing to refine these measurements will constitute a major step forward in the direction of constructing an accurate “likes-to-likes” SN cosmology.

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Appendix A: Relation between the H α bias and the mass step

In this Appendix we provide the mathematical details needed to understand the relation between the $\Sigma_{H\alpha}$ group magnitudes and the observed mass step. This derivation provides the relation between the numerical values of the H α bias and the mass step in the SNfactory dataset.

To begin with, the dataset is partitioned into four subsets consisting of SNe Ia ϵ and SNe Ia α above and below the canonical mass division point of $\log(M/M_\odot) = 10$. We denote the number in each subset as $N_{\alpha,L}$, $N_{\alpha,H}$, $N_{\epsilon,L}$, and $N_{\epsilon,H}$, with L and H symbolizing SNe Ia in low- and high-mass hosts, respectively. Likewise, the mean Hubble residuals for each subset are denoted as $\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}$, $\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H}$, $\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L}$, and $\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H}$.

To make the equations more readable we introduce the following notation for fractions: F_B^A means “the fraction of SNe from subset A that have property B”. For instance, F_ϵ^H means “the fraction of SNe Ia from high-mass hosts that are Ia ϵ ”, i.e., $N_{\epsilon,H}/N_H$. Mathematically, B is the numerator and A the denominator. Naturally, the partitioning imposes the requirement that $F_B^A + F_{\neg B}^A = 1$, e.g., $F_\epsilon^H + F_\alpha^H = (N_{\epsilon,H} + N_{\alpha,H})/N_H = 1$.

A.1. General equations

The H α bias, $\delta\langle M_B^{\text{corr}}\rangle(\text{Ia}\epsilon - \text{Ia}\alpha)$, is defined as the weighted mean difference of the ΔM_B^{corr} between the Ia ϵ and Ia α subsamples:

$$\delta\langle M_B^{\text{corr}}\rangle(\text{Ia}\epsilon - \text{Ia}\alpha) \equiv \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\epsilon} - \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha}. \quad (\text{A.1})$$

The mass step, $\delta\langle M_B^{\text{corr}}\rangle(H - L)$, is defined as the weighted mean difference of the ΔM_B^{corr} between SNe Ia in low-mass and the high-mass hosts:

$$\delta\langle M_B^{\text{corr}}\rangle(H - L) \equiv \langle\Delta M_B^{\text{corr}}\rangle_H - \langle\Delta M_B^{\text{corr}}\rangle_L. \quad (\text{A.2})$$

The individual weighted mean magnitudes entering Eqs. (A.1) and (A.2) can be written in terms of the weighted mean magnitudes for each portion. Introduction of our F_B^A notation then gives

$$\begin{aligned} \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\epsilon} &= \frac{N_{\epsilon,L}\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + N_{\epsilon,H}\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H}}{N_{\epsilon,L} + N_{\epsilon,H}} \\ &= F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} \end{aligned} \quad (\text{A.3})$$

$$\begin{aligned} \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha} &= \frac{N_{\alpha,L}\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L} + N_{\alpha,H}\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H}}{N_{\alpha,L} + N_{\alpha,H}} \\ &= F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L} + F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} \end{aligned} \quad (\text{A.4})$$

$$\begin{aligned} \langle\Delta M_B^{\text{corr}}\rangle_H &= \frac{N_{\epsilon,H}\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} + N_{\alpha,H}\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H}}{N_{\epsilon,H} + N_{\alpha,H}} \\ &= F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} + F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} \end{aligned} \quad (\text{A.5})$$

$$\begin{aligned} \langle\Delta M_B^{\text{corr}}\rangle_L &= \frac{N_{\epsilon,L}\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + N_{\alpha,L}\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}}{N_{\epsilon,L} + N_{\alpha,L}} \\ &= F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}. \end{aligned} \quad (\text{A.6})$$

Combining these we obtain the equations for the H α bias and mass step in terms of the partitioned data:

$$\begin{aligned} \delta\langle M_B^{\text{corr}}\rangle(\text{Ia}\epsilon - \text{Ia}\alpha) &= F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} \\ &\quad - F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L} - F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} \end{aligned} \quad (\text{A.7})$$

$$\begin{aligned} \delta\langle M_B^{\text{corr}}\rangle(H - L) &= F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} + F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} \\ &\quad - F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} - F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}. \end{aligned} \quad (\text{A.8})$$

With this development it is now possible to write the mass step directly in terms of the H α bias, as follows:

$$\begin{aligned} \delta\langle M_B^{\text{corr}}\rangle(H - L) &= \delta\langle M_B^{\text{corr}}\rangle(\text{Ia}\epsilon - \text{Ia}\alpha) \\ &\times \frac{F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} - F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} - F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}}{F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} + F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} - F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} - F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}}. \end{aligned} \quad (\text{A.9})$$

In this expression we have simply rearranged terms to demonstrate that the same weighted mean magnitudes, just having different signs and fractions, appear in both the numerator and denominator.

A.2. Observational constraints

Equation (A.9) is exact when all of the quantities can be directly measured, as they are in our dataset. These variables can be generalized to any similar dataset. In order to be exact, though, observations of the local environment would be required. However, in the main text we presented two observational constraints that can be used to greatly simplify Eq. (A.9). First, we have shown in Sect. 5.2.2 that the averaged ΔM_B^{corr} of SNe Ia α does not depend on the masses of their hosts:

$$\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L} \simeq \langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} \simeq \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha}. \quad (\text{A.10})$$

Second, we observed in Fig. 10 that SNe Ia α and Ia ϵ from low-mass hosts share the same mean magnitude (within error bars):

$$\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} \simeq \langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L} \simeq \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha}. \quad (\text{A.11})$$

As a consequence of these two observations, the righthand side of Eq. (A.7) becomes

$$\begin{aligned} &F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} - (F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L} + F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H}) \\ &\simeq F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + (1 - F_\epsilon^L)\langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha} - \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha} \\ &\simeq F_\epsilon^L \times (\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} - \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha}). \end{aligned} \quad (\text{A.12})$$

Similarly, the righthand side of Eq. (A.8) becomes

$$\begin{aligned} &F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} + F_\alpha^H\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,H} - (F_\epsilon^L\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,L} + F_\alpha^L\langle\Delta M_B^{\text{corr}}\rangle_{\alpha,L}) \\ &\simeq F_\epsilon^H\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} + (1 - F_\epsilon^H)\langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha} - \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha} \\ &\simeq F_\epsilon^H \times (\langle\Delta M_B^{\text{corr}}\rangle_{\epsilon,H} - \langle\Delta M_B^{\text{corr}}\rangle_{\text{Ia}\alpha}). \end{aligned} \quad (\text{A.13})$$

Finally, using the relation $F_\epsilon^H/F_\epsilon^L = (N_{\epsilon,H}/N_H) \times (N_\epsilon/N_{\epsilon,H}) = (N_\epsilon/N) \times (N/N_H) = F_\epsilon/F_H$, where F_ϵ is the fraction of SNe Ia ϵ , and F_H the fraction of SNe Ia from high-mass hosts, Eq. (A.9) can simply be expressed as

$$\delta\langle M_B^{\text{corr}}\rangle(H - L) \simeq F_\epsilon \times \frac{\delta\langle M_B^{\text{corr}}\rangle(\text{Ia}\epsilon - \text{Ia}\alpha)}{F_H}. \quad (\text{A.14})$$

In the main text, the dependence of F_ϵ with redshift is denoted $\psi(z)$, and $\delta\langle M_B^{\text{corr}}\rangle(\text{Ia}\epsilon - \text{Ia}\alpha)$ is assumed to be constant. Furthermore, based on the dataset we compiled in Childress et al. (2013a), F_H appears to be constant within 10% up to $z \sim 1$. Subject to these approximations, we conclude that the mass-step evolution is simply proportional to $\psi(z)$, as given in Eq. (6).