

Exciton Dynamics in Molecular Crystals and Aggregates

Contributions by
V. M. Kenkre P. Reineker

With 37 Figures



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