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ExoMol line lists – XXXIX. Ro-vibrational molecular line list for CO₂

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ABSTRACT

A new hot line list for the main isotopologue of CO_2 , $^{12}C^{16}O_2$ is presented. The line list consists of almost 2.5 billion transitions between 3.5 million rotation-vibration states of CO_2 in its ground electronic state, covering the wavenumber range 0–20 000 cm⁻¹ ($\lambda > 0.5~\mu m$) with the upper and lower energy thresholds of 36 000 cm⁻¹ and 16 000 cm⁻¹, respectively. The ro-vibrational energies and wavefunctions are computed variationally using the accurate empirical potential energy surface Ames-2. The ro-vibrational transition probabilities in the form of Einstein coefficients are computed using an accurate *ab initio* dipole moment surface with variational program TROVE. A new implementation of TROVE which uses an exact nuclear-motion kinetic energy operator is employed. Comparisons with the existing hot line lists are presented. The line list should be useful for atmospheric retrievals of exoplanets and cool stars. The UCL-4000 line list is available from the CDS and ExoMol data bases.

Key words: molecular data – planets and satellites: atmospheres – stars: atmospheres – infrared: general.

1 INTRODUCTION

Carbon dioxide is well known and much studied constituent of the Earth's atmosphere. However, it is also an important constituent of planetary atmospheres. The Venusian atmosphere is 95 per cent CO₂ which therefore dominates its opacity (Snels et al. 2014). Similarly studies of exoplanets have emphasized the importance of CO₂. It was one of the first molecules detected in the atmospheres of hot Jupiter exoplanets (Swain et al. 2009a, b, 2010) where it provides an important measure of the C/O ratio on the planet (Moses et al. 2013). Similarly it is considered an important marker in directly imaged exoplanets (Moses et al. 2013) and the atmospheres of lower mass planets are expected to be dominated by water and CO₂ (Massol et al. 2016). Heng & Lyons (2016) provide a comprehensive study of CO₂ abundances in exoplanets. Recently, Baylis-Aguirre, Creech-Eakman & Güth (2020) detected emission and absorption from excited vibrational bands of CO2 in the mid-infrared spectra of the M-type Mira variable R Tri using the *Spitzer* infrared spectrograph.

Most of the environments discussed above are considerably hotter than the Earth: for example Venus is at about 735 K and hot Jupiter exoplanets have typical atmospheric temperatures in excess of $1000 \, \text{K}$. Hot CO_2 is also important for industrial applications on Earth (Evseev, Fateev & Clausen 2012) and studies of combustion engines (Rein & Sanders 2010). These applications all require information on CO_2 spectra at higher temperatures. It is this problem that we address here.

The importance of CO₂ has led to very significant activity on the construction of list of important rotation-vibration transition lines. The HITRAN data base provides such lists for studies of the Earth's atmosphere and other applications at or below 300 K. The CO₂ line

lists where comprehensively updated in the 2016 release of HITRAN (Gordon & et al. 2017) in part to provide higher accuracy data to meet the demands of Earth observation satellites such as OCO-2 (Connor et al. 2016; Oyafuso et al. 2017). The 2016 update made extensive use of variational nuclear motion calculations (Zak et al. 2016, 2017a, b) of the type employed here.

HITRAN is not designed for or suitable for high-temperature applications which demand much more extensive line lists. The HITEMP data base (Rothman et al. 2010) is designed to address this issue. The original HITEMP used the direct numerical diagonalization calculations of Wattson & Rothman (1992), which were an early example of the use of large-scale variational nuclear motion calculations to provide molecular line lists. The 2010 HITEMP update used the CDSD-1000 (carbon dioxide spectroscopic databank) line list (Tashkun et al. 2003). The CDSD-1000 line list is based on the use of effective Hamiltonian fits to experimental data and was designed to be complete for temperatures up to 1000 K. CDSD-1000 subsequently was replaced by CDSD-4000. The empirical CO₂ line list CDSD-4000 computed by Tashkun & Perevalov (2011) is designed for temperatures up to 5000 K, but has limited wavenumber coverage. Furthermore, while usually good at reproducing known spectra, experience has shown that the effective Hamiltonian approach can struggle to capture all the unobserved hot bands resulting in underestimates of the opacity at higher temperatures (Chubb, Tennyson & Yurchenko 2020). A compact version of CDSD-4000 has recently been made available (Vargas, Lopez & da Silva 2020).

The NASA Ames group have produced a number of CO_2 line lists (Huang et al. 2013, 2014, 2017; Huang, Schwenke & Lee 2019) using highly accurate potential energy surfaces (Huang et al. 2012, 2017) and variational nuclear motion calculations. Most relevant for this work is the Ames-2016 CO_2 line list of Huang et al. (2017)

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which considers wavenumbers up to $15\,000~\rm cm^{-1}$ and J up to $150~\rm with$ upper state energies limited to $hc \times 24\,000~\rm cm^{-1}$. Due to this fixed upper energy cut-off, the temperature coverage depends on the wavenumber range, from $T \sim 4000~\rm K$ at the higher end up to $\sim 1500~\rm K$ at the lower end. The Ames-2016 line list was based on an accurate empirically generated potential energy (PES) surface Ames-2 and their high-level *ab initio* dipole moment surface (DMS) DMS-N2.

High accuracy room temperature line lists for 13 isotopologues of CO_2 was computed by Zak et al. (2016, 2017a, b), using the Ames-2 PES (Huang et al. 2017) and UCL's highly accurate DMS (Polyansky et al. 2015). These line lists are now part of the HITRAN (Gordon & et al. 2017) and ExoMol (Tennyson & Yurchenko 2012) data bases. The room temperature properties of this line list have been subject to a number experimental tests and the results have been found to be competitive in accuracy to state-of-the-art laboratory experiments (Odintsova et al. 2017; Čermák et al. 2018; Kang et al. 2018; Long et al. 2020).

Here, we present a new hot line list for the main isotopologue of CO_2 ($^{12}C^{16}O_2$) generated using UCL's *ab initio* DMS (Polyansky et al. 2015) and the empirical PES Ames-2 (Huang et al. 2017) with the variational program TROVE (Yurchenko, Thiel & Jensen 2007). Our line list is the most comprehensive (complete and accurate) data set for CO_2 . This work is performed as part of the ExoMol project (Tennyson & Yurchenko 2012) and the results form an important addition to the ExoMol data base (Tennyson et al. 2016) which, as discussed below, is currently being upgraded (Tennyson et al. 2020).

2 TROVE SPECIFICATIONS

For this work, we used a new implementation of the exact kinetic energy operator for triatomics in TROVE (Yurchenko & Mellor 2020) based on the bisector embedding for triatomic molecules (Carter, Handy & Sutcliffe 1983; Sutcliffe & Tennyson 1991).

The variational TROVE program (Yurchenko et al. 2007) solves the ro-vibrational Schrödinger equation using a multilayer contraction scheme (see e.g. Yurchenko, Yachmenev & Ovsyannikov 2017). At step 1, the 1D primitive basis set functions $\phi_{v_1}(r_1)$, $\phi_{v_2}(r_2)$ (stretching) and $\phi_{v_3}(\rho)$ (bending) are obtained by numerically solving the corresponding Schrödinger equations. Here, r_1 and r_2 are two stretching valence coordinates and $\rho=180^\circ-\alpha$ with α being the interbond valence angle. A 1D Hamiltonian operator for a given mode is constructed by setting all other degrees of freedom to their equilibrium values. The two equivalent stretching equations are solved on a grid of 1000 points using the Noumerov–Cooley approach (Noumerov 1924; Cooley 1961), with the grid values of r_i ranging from $r_e-0.4$ to $r_e+1.0$ Å. The bending mode solutions are obtained on the basis of the associated Laguerre polynomials as given by

$$\phi_{n,l}^{(l)}(\rho) = C_{n,l} \, \rho^{l+1/2} \, L_n^{(l)}(a\rho^2) \, e^{-a\rho^2/2}, \tag{1}$$

normalized as

$$\int_0^{\rho_{\text{max}}} \phi_{n,l}^{(l)}(\rho)^2 \,\mathrm{d}\rho = 1,$$

where a is a structural parameter, $l \ge 0$, $\rho_{\rm max}$ was set to 170°, and all primitive bending functions were mapped on a grid of 3000 points. The kinetic energy operator is constructed numerically as a formal expansion in terms of the inverse powers of the stretching coordinates r_i (i=1,2): $1/r_i$ and $1/r_i^2$ around a non-rigid configuration (Hougen, Bunker & Johns 1970) defined by the ρ_i points on the grid. The singularities of the kinetic energy operator at $\rho=0^\circ$ ($\sim 1/\rho$ and $1/\rho^2$) are resolved analytically with the help of the factors $\rho^{l+1/2}$ in the defini-

tion of the associated Laguerre basis set in equation (1). The details of the model will be published elsewhere (Yurchenko & Mellor 2020).

At step 2 two reduced problems for the 2D stretching and 1D bending reduced Hamiltonians are solved variationally on the primitive basis set of $|v_1, v_2\rangle = \phi_{v_1}(r_1)\phi_{v_2}(r_2)$ and $|v_3, l\rangle = \phi_{v_3}^{(l)}(\rho)$, respectively. The reduced Hamiltonians are constructed by averaging the 3D vibrational (J=0) Hamiltonian over the ground state basis functions as follows:

$$\hat{H}_{\text{str}}^{(1)}(r_1, r_2) = \langle 0_3, l = 0 | \hat{H}^{3D} | 0_3, l = 0 \rangle, \tag{2}$$

$$\hat{H}_{\text{bnd}}^{(2)}(\rho) = \langle 0_1, 0_2 | \hat{H}^{3D} | 0_1, 0_2 \rangle, \tag{3}$$

where $|v_1, v_2\rangle$ are stretching and $|v_3, l\rangle$ are bending vibrational basis functions with $v_i = 0$ and l = 0. In the bending basis set, l is treated as a parameter with the corresponding Hamiltonian matrices

$$H_{i,j}^{(2),l} = \left\langle i, l | \hat{H}_{\text{bnd}}^{(2)}(\rho) | j, l \right\rangle,$$

block-diagonal in l ($l=0,\ldots,l_{\rm max}$). The eigenfunctions of the reduced Hamiltonians in equations (2) and (3), $\Phi_{i_1}^{(1)}(r_1,r_2)$ and $\Phi_{i_2,l}^{(2)}(\rho)$ are obtained variationally and then symmetrized using the automatic symmetry adaptation technique (Yurchenko et al. 2017). A 3D vibrational basis set for the J=0 Hamiltonian for step 3 is then formed as symmetry adapted products given by

$$\Phi_{i_1,i_2,l}^{\Gamma_{\text{vib}}} = \left\{ \Phi_{i_1}^{(1)}(r_1, r_2) \Phi_{i_2,l}^{(2)}(\rho) \right\}^{\Gamma_{\text{vib}}}, \tag{4}$$

where $\Gamma_{\rm vib}$ is the vibrational symmetry in the $\mathcal{C}_{\rm 2v}(M)$ molecular symmetry group (Bunker & Jensen 1998) used to classify the irreducible representations (irreps) of the ro-vibrational states of ${\rm CO}_2$. $\mathcal{C}_{\rm 2v}(M)$ comprises four irreps A_1 , A_2 , B_1 , and B_2 . The allowed vibrational symmetries are A_1 and B_2 . The allowed ro-vibrational symmetries of ${}^{12}{\rm C}^{16}{\rm O}_2$ are A_1 and A_2 due to the restriction on the nuclear-spin-ro-vibrational functions imposed by the nuclear spin statistics (Pauli exclusion principle).

At step 3, the vibrational (J=0) Hamiltonians are solved on the symmetry adapted vibrational basis in equation (4). These eigenfunction $\Psi_{\lambda,l}^{(J=0)}$ are parametrized with l and associated with a vibrational symmetry A_1 or B_2 and then used to build a ro-vibrational basis set $(J \ge 0)$ as a symmetrized product:

$$\Psi_{\lambda,K}^{(J,\Gamma)} = \left\{ \Psi_{\lambda,K}^{(J=0,\Gamma_{\text{vib}})} | J, K, \Gamma_{\text{rot}} \rangle \right\}^{\Gamma}, \tag{5}$$

where the rotational part $|J, K, \Gamma_{\text{rot}}\rangle$ is a symmetrized combination of the rigid rotor functions (Yurchenko et al. 2017) and the rotational quantum number $K(K \ge 0)$ is constrained to the vibrational parameter l(K = l).

An $E = hc \times 36\,000$ cm⁻¹ energy cut-off was used to contract the J = 0 eigenfunctions. All energies and eigenfunctions up to J = 202 were generated and used to produce the dipole lists for CO₂.

The size of the vibrational basis was controlled by a polyadnumber condition:

$$P = v_1 + v_2 + v_3 \le P_{\text{max}} = 64,$$

chosen based on the convergence tests with v_1 and $v_2 \le 56$.

Some vibrational energies computed using the Ames-2 PES by Huang et al. (2017) are shown in Table 1 and compared to the empirical $^{12}\text{C}^{16}\text{O}_2$ band centres (HITRAN's estimates, see below). In order to improve the accuracy of the ro-vibrational energies, we have applied vibrational band centre corrections to the TROVE J=0 energies by shifting them to the HITRAN values, where available (see Yurchenko, Barber & Tennyson (2011)). This trick in combination with the J=0 contracted basis set allowed us to replace the diagonal

Table 1. Examples of vibrational band centres of CO_2 computed using Ames-2 PES with TROVE (\tilde{E}_{λ}^T) , average differences with the HITRAN band centres $(\Delta \tilde{E}_{\lambda} = \tilde{E}_{\lambda}^H - \tilde{E}_{\lambda}^T)$, the shifted band centres adopted for ro-vibrational calculations $(\tilde{E}_{\lambda}^T + \Delta \tilde{E}_{\lambda})$ and three sets of quantum numbers (QN) used in this work. See the complete table in supplementary material.

	Linear molecule QN					HITRAN QN					OVE Q		Term values (cm ⁻¹)			
λ	n_1	n_2^{lin}	l_2	n_3	m_1	m_2	l_2	m_3	r	v_1	v_2	v ₃	$\tilde{E}_{\lambda}^{\mathrm{T}}$ $\Delta \tilde{E}_{\lambda}$		$ ilde{E}_{\lambda}^{\mathrm{T}} + \Delta ilde{E}_{\lambda}$	
1	0	0	0	0	0	0	0	0	1	0	0	0	0.000	0.000	0.000	
2	0	1	1	0	0	1	1	0	1	0	0	0	667.755	0.015	667.769	
3	0	2	0	0	1	0	0	0	2	0	0	1	1285.404	0.004	1285.408	
4	0	2	2	0	0	2	2	0	1	0	0	0	1336.673	0.020	1336.693	
5	1	0	0	0	1	0	0	0	1	1	0	0	1388.209	-0.024	1388.185	
6	0	3	1	0	1	1	1	0	2	0	0	1	1932.821	0.039	1932.860	
7	0	3	3	0	0	3	3	0	1	0	0	0	2006.732	0.035	2006.766	
8	1	1	1	0	1	1	1	0	1	1	0	0	2077.233	0.013	2077.246	
9	0	0	0	1	0	0	0	1	1	0	1	0	2349.174	-0.032	2349.141	
10 11	1	2 4	0 2	0	2	0 2	0 2	0	3 2	1 0	0	1 1	2548.343 2586.546	0.024 0.039	2548.367 2586.585	
12	2	0	0	0	2	0	0	0	2	1	1	0	2671.144	0.039	2671.144	
13	0	4	4	0	0	4	4	0	1	0	0	0	2677.936	0.049	2677.985	
14	1	2	2	0	1	2	2	0	1	1	0	0	2762.269	0.049	2762.287	
15	1	2	0	0	2	0	0	0	1	1	0	1	2797.157	-0.020	2797.137	
16	0	1	1	1	0	1	1	1	1	0	1	0	3004.453	-0.058	3004.395	
17	1	3	1	0	2	1	1	0	3	1	0	1	3181.792	0.062	3181.854	
18	0	5	3	0	1	3	3	0	2	0	0	1	3244.101	0.045	3244.146	
19	2	1	1	0	2	1	1	0	2	1	1	0	3339.706	0.040	3339.746	
20	0	5	5	0	0	5	5	0	1	0	0	0	3350.284	0.058	3350.343	
21	1	3	3	0	1	3	3	0	1	1	0	0	3445.706	0.030	3445.735	
22	1	3	1	0	2	1	1	0	1	1	0	1	3501.033	0.030	3501.063	
23	0	2	0	1	1	0	0	1	2	0	1	1	3612.891	-0.052	3612.839	
24	0	2	2	1	0	2	2	1	1	0	1	0	3660.884	-0.073	3660.811	
25	1	0	0	1	1	0	0	1	1	2	0	0	3714.852	-0.071	3714.781	
26	1	4	0	0	3	0	0	0	4	1	0	2	3792.656	0.027	3792.683	
27	1	4	2	0	2	2	2	0	3	1	0	1	3823.531	0.046	3823.577	
28	0	6	4	0	1	4	4	0	2	0	0	1	3904.544	0.045	3904.589	
29	3	0	0	0	3	0	0	0	3	1	2	0	3942.517	0.025	3942.542	
30	2	2	2	0	2	2	2	0	2	1	1	0	4009.441	0.035	4009.476	
31 32	0	6 0	6 0	0	0	6 0	6	0	1 2	0 1	0 2	0	4023.775 4064.277	0.061 -0.002	4023.836 4064.275	
33	1	4	4	0	1	4	4	0	1	1	0	0	4128.500	0.002	4128.536	
34	1	4	2	0	2	2	2	0	1	1	0	1	4128.300	0.036	4128.330	
35	1	4	0	0	3	0	0	0	1	1	0	2	4225.111	-0.014	4225.097	
36	0	3	1	1	1	1	1	1	2	0	1	1	4248.131	-0.044	4248.088	
37	0	3	3	1	0	3	3	1	1	0	1	0	4318.455	-0.070	4318.386	
38	1	1	1	1	1	1	1	1	1	2	0	0	4391.058	-0.046	4391.012	
39	1	5	1	0	3	1	1	0	4	1	0	2	4416.480	0.061	4416.541	
40	1	5	3	0	2	3	3	0	3	1	0	1	4470.630	0.034	4470.665	
41	0	7	5	0	1	5	5	0	2	0	0	1	4567.381	0.036	4567.417	
42	3	1	1	0	3	1	1	0	3	1	2	0	4591.448	0.060	4591.508	
43	0	0	0	2	0	0	0	2	1	1	1	0	4673.371	-0.049	4673.322	
44	2	3	3	0	2	3	3	0	2	1	1	0	4680.274	0.037	4680.311	
45	0	7	7	0	0	7	7	0	1	0	0	0	4698.403	0.055	4698.458	
46	3	1	1	0	3	1	1	0	2	1	2	0	4753.794	0.048	4753.841	
47	1	5	5	0	1	5	5	0	1	1	0	0	4811.138	0.037	4811.175	
48	1	2 4	0 2	1 1	2	0 2	0 2	1 1	3 2	2	0 1	1	4853.681 4889.592	-0.060 -0.062	4853.622	
49 50	1	5	3	0	2	3	3	0	1	1	0	1 1	4893.567	0.030	4889.531 4893.597	
51	1	5	1	0	3	1	1	0	1	1	0	2	4938.732	0.030	4938.775	
52	0	4	4	1	0	4	4	1	1	0	1	0	4977.178	-0.065	4977.113	
53	2	0	0	1	2	0	0	1	2	3	0	0	4977.889	-0.055	4977.833	
54	1	6	0	0	4	0	0	0	5	1	0	3	5022.354	-0.002	5022.352	
55	1	6	2	0	3	2	2	0	4	1	0	2	5048.803	0.023	5048.825	
56	1	2	2	1	1	2	2	1	1	2	0	0	5063.368	-0.051	5063.317	
57	1	2	0	1	2	0	0	1	1	2	0	1	5099.731	-0.072	5099.659	
58	1	6	4	0	2	4	4	0	3	1	0	1	5121.776	0.013	5121.788	
59	3	2	0	0	4	0	0	0	4	1	2	1	5197.228	0.026	5197.255	
60	0	8	6	0	1	6	6	0	2	0	0	1	5232.314	0.019	5232.333	

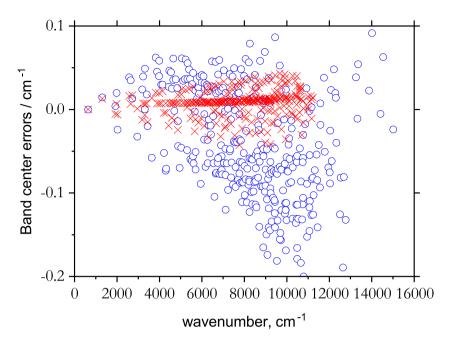


Figure 1. Blue circles: Average ro-vibrational errors for 337 vibrational (J=0) states from HITRAN estimated as CO_2 $\tilde{E}_{\lambda}^H - \tilde{E}_{\lambda}^T$ (HITRAN-TROVE) term values for $J \le 40$, which were used as band centre corrections (see the text). Red crosses: Average residuals for the ro-vibrational CO_2 term values (for $J \le 40$) between TROVE (before the band centre correction) and calculations from Zak et al. (2016) using DVR3D and the same PES Ames-2016 for 294 vibrational states.

vibrational matrix elements in the ro-vibrational Hamiltonian by the corresponding empirical band centres; for this reason the approach was named by Yurchenko et al. (2011) the empirical basis set correction. The band centre corrections were estimated as average residuals $\tilde{E}_i^T - \tilde{E}_i^H$ ($J = 0, \ldots, 40$) by matching the TROVE \tilde{E}_i^T and HITRAN \tilde{E}_i^H ro-vibrational term values for $J \leq 40$, wherever available, for each vibrational state present in HITRAN. In total, 337 band centres¹ ranging up to ~15 500 cm⁻¹ were corrected, with the total root-mean-square (rms) error of 0.06 cm⁻¹. This is illustrated in Table 1, where 60 lowest term values before and after correction are shown together with the three alternative assignment cases, and in Fig. 1, where the average ro-vibrational errors for 337 bands are plotted. The complete list of the band centres and their corrections is given as supplementary material to the paper.

As an independent benchmark of the TROVE calculations, the initial TROVE energies ($J \leq 40$) before the band centre corrections were compared to the theoretical CO₂ energies computed by Zak et al. (2016) using the DVR3D program (Tennyson et al. 2004) and the same PES as the Ames-2016 line list. Fig. 1 shows averaged residuals for 294 bands matched to the CO₂ energy term values from Zak et al. (2016) up to 10 500 cm⁻¹ with the total rms error of 0.02 cm⁻¹.

The ro-vibrational energies were computed variationally using the CO_2 empirical PES Ames-2 by Huang et al. (2017) for J=0...230 and used to compute the temperature-dependent partition function of CO_2 . The transition intensities (Einstein A coefficients) were then computed using the UCL *ab initio* DMS (Polyansky et al. 2015) covering the wavenumber range from 0 to 20 000 cm⁻¹ with the lower energy term value up to $16\,000$ cm⁻¹ ($J \le 202$). To speed up the calculation of the dipole moment matrix elements, a threshold of 10^{-12} to the eigen-coefficients was applied (see Yurchenko

et al. 2011). We have also applied a threshold of 10^{-8} Debye to the vibrational matrix elements of the dipole moment in order to reduce an accumulation error for higher overtones, see discussion by Medvedev et al. (2016, 2020).

3 LINE LIST

3.1 Quantum numbers

In TROVE calculations, the ro-vibrational states are uniquely identified by three numbers, the rotational angular momentum quantum number J, the total symmetry Γ (molecular symmetry group) and the eigen-state counting number λ (in the order of increasing energies). Each state can be further assigned with approximate quantum numbers (QN) associated with the corresponding largest basis set contribution (Yurchenko et al. 2007). There are two main sets of approximate QNs corresponding to the contractions steps 1 and 3. The first set is connected to the primitive basis set excitation numbers v_1 , v_2 , v_3 , and l_2 . The second set is associated with the vibrational counting number λ from the (J = 0)-contracted basis set equation (5). Even though v_1 , v_2 , v_3 , and l_2 are more physically intuitive than the counting number of the vibrational states λ , the latter is useful for correlating TROVE's states to the experimental (e.g. normal mode) QNs or indeed to any other scheme. Table 1 shows vibrational (J = 0)term values of CO2 together with all assignment schemes either used in these work or relevant to the spectroscopy of CO₂: (i) TROVE primitive QNs v_1 , v_2 , v_3 , and l, (ii) TROVE band centres counting number λ , (iii) HITRAN QNs m_1 , m_2 , l_2 , m_3 , r adopted for CO₂, and (iv) spectroscopic (normal mode) QNs n_1 , n_2^{lin} , l_2 , n_3 used for other general linear triatomic molecules. Our preferred choice is (iv). According to this convention, n_1 and n_3 are two stretching quantum numbers associated with the symmetric and asymmetric modes; n_2^{lin} is the (symmetric) linear molecule bending quantum number; and l_2 is the bending quantum number satisfying the standard conditions

¹The band centres in question correspond to the fundamental or overtone bands and represent pure vibrational (J=0) term values.

Table 2. Extracts from the final states file for UCL-4000.

i	$ ilde{E}$	g_{tot}	J	unc.	Γ	e/f	n_1	n_2^{lin}	l_2	n_3	C_i	m_1	m_2	m_3	m_4	r	v_1^{T}	v_2^{T}	v_3^{T}
1	0.000000	1	0	0.0005	A1	e	0	0	0	0	1.00	0	0	0	0	1	0	0	0
2	1285.408200	1	0	0.0005	A1	e	0	2	0	0	1.00	1	0	0	0	2	0	0	1
3	1388.184200	1	0	0.0050	A1	e	1	0	0	0	1.00	1	0	0	0	1	1	0	0
4	2548.366700	1	0	0.0005	A1	e	1	2	0	0	1.00	2	0	0	0	3	1	0	1
5	2671.142957	1	0	0.0050	A1	e	2	0	0	0	1.00	2	0	0	0	2	1	1	0
6	2797.136000	1	0	0.0050	A1	e	1	2	0	0	1.00	2	0	0	0	1	1	0	1
7	3792.681898	1	0	0.0050	A1	e	1	4	0	0	1.00	3	0	0	0	4	1	0	2
8	3942.541358	1	0	0.0050	A1	e	3	0	0	0	1.00	3	0	0	0	3	1	2	0
9	4064.274256	1	0	0.0050	A1	e	3	0	0	0	1.00	3	0	0	0	2	1	2	0
10	4225.096148	1	0	0.0050	A1	e	1	4	0	0	1.00	3	0	0	0	1	1	0	2
11	4673.325200	1	0	0.0005	A1	e	0	0	0	2	1.00	0	0	0	2	1	1	1	0
12	5022.349428	1	0	0.0050	A1	e	1	6	0	0	1.00	4	0	0	0	5	1	0	3
13	5197.252900	1	0	0.0050	A1	e	3	2	0	0	1.00	4	0	0	0	4	1	2	1
14	5329.645446	1	0	0.0050	A1	e	4	0	0	0	1.00	4	0	0	0	3	2	2	0
15	5475.553054	1	0	0.0005	A1	e	3	2	0	0	1.00	4	0	0	0	2	1	2	1
16	5667.644584	1	0	0.0050	A1	e	2	4	0	0	1.00	4	0	0	0	1	1	1	2
17	5915.212302	1	0	0.0005	A1	e	0	2	0	2	1.00	1	0	0	2	2	1	1	1
18	6016.690121	1	0	0.0005	A1	e	1	0	0	2	1.00	1	0	0	2	1	0	3	0
19	6240.044061	1	0	0.08	A1	e	2	6	0	0	1.00	-1	-1	-1	- 1	- 1	1	1	3
20	6435.507278	1	0	0.06	A1	e	4	2	0	0	1.00	- 1	-1	-1	- 1	-1	2	2	1
21	6588.323819	1	0	0.05	A1	e	5	0	0	0	1.00	- 1	-1	-1	- 1	- 1	3	2	0

Note. i: State counting number.

 \tilde{E} : State energy in cm⁻¹.

gtot: Total state degeneracy.

J: Total angular momentum.

unc.: Uncertainty cm⁻¹: The empirical (4 decimal places) and estimated (2 decimal places) values.

 Γ : Total symmetry index in $\mathcal{C}_{2v}(M)$.

elf: Kronig rotationless parity.

 n_1 : Normal mode stretching symmetry (A_1) quantum number.

 n_2^{lin} : Normal mode linear molecule bending (A_1) quantum number.

l₂: Normal mode vibrational angular momentum quantum number.

 n_3 : Normal mode stretching asymmetric ($B1_1$) quantum number.

 C_i : Coefficient with the largest contribution to the (J=0) contracted set; $C_i \equiv -1$ for J=0.

 m_1 : CO₂ symmetric vibrational Fermi-resonance group quantum number (-1 stands for non-available).

 m_2 : CO₂ vibrational bending quantum number (similar but not exactly identical to n_2^{lin}).

 l_2 : CO₂ vibrational bending quantum number (similar but not exactly identical to standard l_2).

 m_3 : CO₂ asymmetric vibrational stretching quantum number, the same as n_3 .

r: CO₂ additional ranking quantum number identifying states within a Fermi-resonance group.

 $v_1^{\rm T}$: TROVE stretching vibrational quantum number.

 $v_2^{\rm T}$: TROVE stretching vibrational quantum number.

 v_3^{T} : TROVE bending vibrational quantum number.

Table 3. Extract from the transitions file for the UCL-4000 line list.

f	i	A_{fi}				
1176508	1137722	2.8564E-02				
1861958	1849078	1.6327E-03				
631907	665295	8.1922E-12				
1344897	1331267	4.2334E-07				
983465	944281	1.4013E-08				
183042	170520	1.6345E-02				
2695389	2668685	5.9366E-07				
811518	822542	1.4353E-01				
406949	369902	2.3774E-02				

Note. f: Upper state counting number.

i: Lower state counting number.

 A_{fi} : Einstein-A coefficient in s⁻¹.

on the vibrational angular momentum of an isotropic 2D Harmonic oscillator (Bunker & Jensen 1998)

$$l_2 = n_2^{\text{lin}}, n_2^{\text{lin}} - 2, \dots 1(0).$$

All ro-vibrational states are automatically assigned the QN schemes (i) and (ii), which were then automatically correlated to the general linear molecule QN (iv) using the following rules:

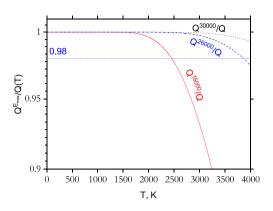
$$l = l_2$$
, $v_1 + v_2 = n_1 + n_3$, $v_3 = n_2^{\text{lin}}$

for a given stretching polyad $n_1 + n_2$, where we assumed that the asymmetric quanta has higher energies than symmetric. For example, for $v_1 + v_2 = n_1 + n_3 = 2$ the stretching QNs (n_1, n_3) are assigned to the vibrational term values according with the order of energies: (2,0) 3339.702 cm⁻¹, (1,1) 3714.853 cm⁻¹, and (0,2) 4673.392 cm⁻¹. The linear molecule bending quantum number n_2^{lin} is given by

$$n_2^{\text{lin}} = 2v_3 + l_2,$$

where v_3 is the TROVE vibrational bending quantum number. The standard linear molecule QN scheme (iv) was favoured for example by Herzberg & Herzberg (1953) and is also recommended here.

We could not perform similar automatic correlation to the HI-TRAN quantum labels (m_1, m_2, l_2, m_3, r) for all the states in our line lists, only for states present in the CO₂ HITRAN data base.



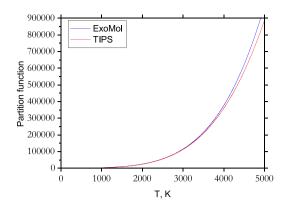


Figure 2. Partition functions of CO₂. Left display: Ratio $Q^{E_{\text{max}}}(T)/Q(T)$ of the CO₂ partition functions at with energy cut-offs $hc \times 16\,000~\text{cm}^{-1}$, $hc \times 26000~\text{cm}^{-1}$, and $hc \times 30\,000~\text{cm}^{-1}$, as a function of temperature. Q(T) is chosen as $Q^{36000~\text{cm}^{-1}}$. The line 0.98 shows that the recommended temperature varies with the wavenumber region, from T = 2500~K ($> 0~\text{cm}^{-1}$) to T = 4000~K ($> 10\,000~\text{cm}^{-1}$). Right display: ExoMol values were computed using all UCL-4000 energies for $J \le 230$; TIPS values were obtained using the TIPS app provided in Gamache et al. (2017).

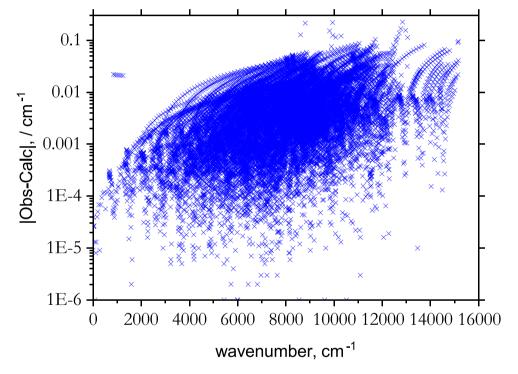


Figure 3. Ro-vibrational Obs.-Calc. errors $|\tilde{E}_i^{\rm H} - \tilde{E}_i^{\rm T}|$ (HITRAN-TROVE) in cm⁻¹ for all HITRAN's 18 392 empirical values as a function of the energy term values, covering $J \leq 129$ giving an rms error of 0.016 cm⁻¹.

The HITRAN convention of quantum numbers (iii) for CO₂ is more empirical. It is motivated by energy clusters formed by states in accidental Fermi resonance and their order within a cluster (Rothman & Young 1981). The quantum number m_1 is associated with Fermi resonance groups of (symmetric) states of different combinations of l_2 and $2m_1 + m_2 = 2n_1 + n_2^{\text{lin}}$; r is the ranking index, with r = 1 for the highest vibrational level of a Fermi resonance group and assuming the values $1, 2, \ldots m_1 + 1$ (Rothman & Young 1981). HITRAN's version of the bending quantum number m_2 is by definition equal to l_2 (so-called AFGL notation) and thus redundant, while the stretching quantum number m_3 is the same as the linear molecule asymmetric quantum number n_3 from scheme (iv). In order to simplify correlation with HITRAN and experimental literature, the scheme (iii) is retained, but only for the ro-vibrational states present in HITRAN.

4 LINE LIST

The CO $_2$ UCL-4000 line list contains 3480 477 states and 2557 551 923 transitions and covers the wavenumber range from 0 to 20 000 cm $^{-1}$ (wavelengths, $\lambda > 0.5~\mu m$) with the lower energy up to 16 000 cm $^{-1}$ and $J \leq 202$ with a threshold on the Einstein coefficients of $10^{-14}~s^{-1}$. The line list consists of two files (Tennyson et al. 2016), called States and Transitions, which in the case of UCL-4000 are summarized in Tables 2 and 3. The first 4 columns of the States file have the compulsory structure for all molecules: State ID, Energy term value (cm $^{-1}$), the total degeneracy and the total angular momentum. According to the new ExoMol-2020 format (Tennyson et al. 2020), the fifth column is also compulsory representing the uncertainty estimate of the corresponding term value (cm $^{-1}$), which is followed by the lifetime, Landé *g*-factor (if provided) and

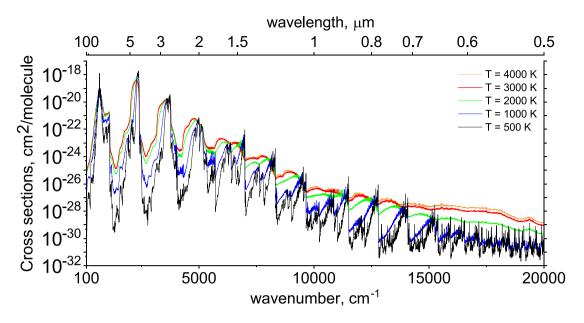


Figure 4. Temperature dependence of the CO_2 spectrum using the Gaussian line profile of $HWHM = 1 \text{ cm}^{-1}$. The spectrum becomes systematically flatter with increasing temperature.

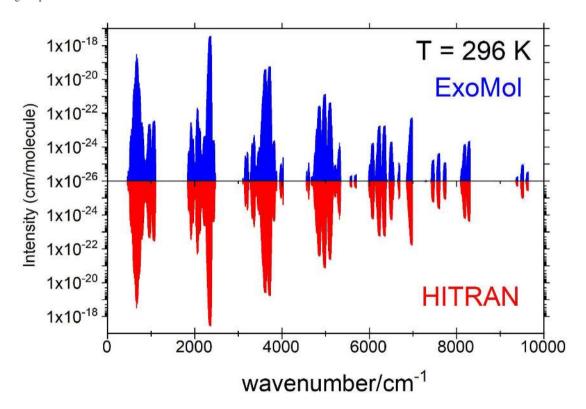


Figure 5. CO_2 stick spectrum comparing using UCL-4000 to HITRAN at T = 296 K.

molecular specific quantum numbers, including rigorous (symmetry, parity) and non-rigorous (vibrational, rotational, etc.). The States file covers all states up to $J=230~(3526~057~{\rm states})$. The Transitions part consists of three columns with the upper State ID, lower State ID and the Einstein A coefficient, see Table 3. For convenience, the Transition part is split into 20 files each covering $1000~{\rm cm}^{-1}$.

The uncertainty of the CO_2 energies were estimated based on the two main criteria. For the states matched to and replaced by the HITRAN energies, the uncertainties σ (in cm⁻¹) are taken as the

HITRAN errors of the corresponding line positions as specified by the HITRAN error codes (Rothman et al. 2005). For all other states the following conservative estimate is used:

$$\sigma = 0.01 \, n_1 + 0.01 \, n_2^{\text{lin}} + 0.01 \, n_3.$$

With the lower state energy threshold of 16 000 cm⁻¹ our line list should be valid for temperatures up to at least 2500 K. Fig. 2 (left) illustrates the effect of the lack of the population for the states higher than 16 000 cm⁻¹ with the help of the CO₂ partition function

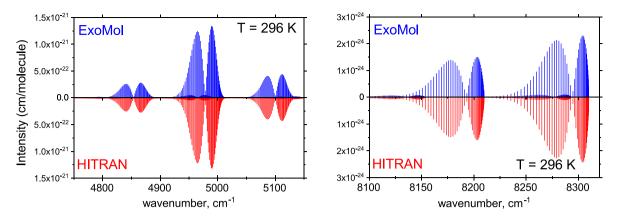


Figure 6. Absorption stick spectrum of CO_2 computed using UCL-4000 and compared to HITRAN at T = 296 K for two spectroscopic regions.

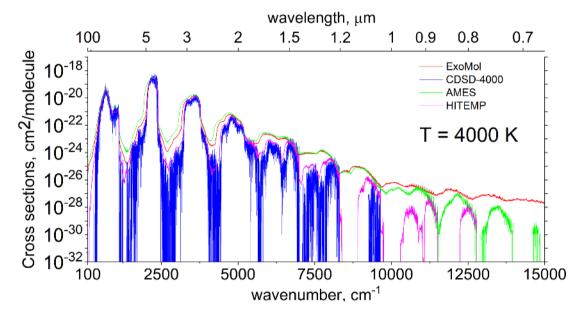


Figure 7. Comparing UCL-4000, CDSD-4000 (Tashkun & Perevalov 2011), Ames-2016 (Huang et al. 2017), and 2010 HITEMP (Rothman et al. 2010) spectra of CO_2 at T = 4000 K. A Gaussian line profile of HWHM = 1 cm⁻¹ was used in each case.

Q(T). In this figure, we show a ratio of incomplete $Q^{E_{\text{max}}}(T)$ (using only states below $E_{\rm max}$) over 'complete' $Q^{36\,\hat{0}00}(T)$. This ratio has the difference of 2 per cent for Q^{16000} at T = 2500 K and Q^{26000} at T = 4000 K, which are the estimates for maximal temperature of the line list for wavenumber regions 0–20 000 and 10 000–20 000 cm⁻¹, respectively. In Fig. 2 (right), we compare the partition functions of CO₂ computed using our line list with the total internal partition sums (TIPS) values for CO₂ (Gamache et al. 2017). The energies in our line list cover higher rotational excitations ($J_{\text{max}} = 230$) compared to TIPS, which was based on the threshold of $J_{\text{max}} = 150$. The energy thresholds in both cases are comparable, $hc \times 36\,000 \text{ cm}^{-1}$ versus $hc \times 30~383~{\rm cm}^{-1}$ (TIPS). The threshold value of $J_{\rm max}~=150$ corresponds to energy term value of ~ 10000 cm $^{-1}$ and it use thus leads to an underestimate of the partition function at high T, while with the threshold of $J_{\text{max}} = 230 \text{ all states below } 20\,000 \text{ cm}^{-1} \text{ are}$ included.

In order to improve the calculated line positions, CO_2 energies from HITRAN were used to replace the TROVE energies where available, taking advantage of the two-part structure of the UCL-4000 line list consisting of a States file and Transition files (Tennyson et al. 2016). A HITRAN energy list consisting of 18 392 empirical values from 337 vibrational states covering J values up to 129 was

generated by collecting all lower and upper state energies from the $^{12}C^{16}O_2$ HITRAN transitions. Comparison of the calculated TROVE term energies with these 18 668 HITRAN values gives an rms error of 0.016 cm $^{-1}$ and is illustrated in Fig. 3 in a log-scale.

The overview of the CO_2 absorption spectrum and its temperature dependence are illustrated in Fig. 4. CO_2 has a prominent band at 4.3 μ m, commonly used for atmospheric and astrophysical retrievals. For example, it was used as one of the photometric bands for the *Spitzer Space Telescope* (Werner et al. 2004).

Our line list is designed to almost perfectly agree with the HITRAN line positions, which was achieved by replacing the TROVE energies with the energies collected from the HITRAN data set for CO₂. Figs 5 and 6 offer some comparisons with HITRAN. In turn, the accuracy of the line intensities agree well with the HITRAN values as guaranteed by the quality of the UCL *ab initio* DMS used. The mean ratio of our intensities to HITRAN is 1.0029 with the standard error of 0.00029 for 171 143 HITRAN lines we could establish a correlation to

Fig. 7 compares the performance of the four main line lists for hot CO₂, UCL-4000 (this work), CDSD-4000 (effective Hamiltonian) (Tashkun & Perevalov 2011), Ames-2 (variational) (Huang et al. 2017) and 2010 HITEMP (empirical) (Rothman et al. 2010) for the

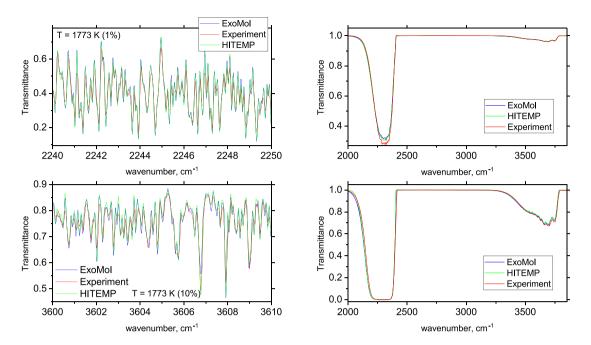


Figure 8. Comparing HITEMP and ExoMol to experimental transmittance (Evseev et al. 2012) at T = 1773 K and 1 bar using a Voigt profile. The experiments were performed with 1 per cent (upper) and 10 per cent (lower) CO_2 in N_2 buffer gas. HITEMP line width parameters were used for HITEMP, while for UCL-4000 we used an approximate scheme a0 from the ExoMol diet (Barton et al. 2017) based on the HITRAN values. The left display shows two selected windows at high resolution (0.0125 cm⁻¹), while the right display is with broader overview and lower resolution (6 cm⁻¹).

wavenumber range from 0 to 15 000 cm $^{-1}$. In general the UCL-4000 line list gives the highest opacity at T=4000 K which is due to its being more complete, while both CDSD-4000 and 2010 HITEMP omit too many hot bands to be able to compete with the other two line lists at high T. The Ames-2016 line list also lacks a significant portion of the opacity at short wavelengths at this temperature as expected from the low-energy threshold used (Huang et al. 2017).

Fig. 8 compares the UCL-4000 spectrum of CO_2 at T=1773~K with the experiment by Evseev et al. (2012), who recorded transmittance of CO_2 at the normal pressure. The displays on the left show small windows from the two strongest CO_2 bands, 2.7 and 4.3 μm at higher resolution, while the displays on the right gives an overview of the whole region covering these bands at lower resolution. As a reference, spectra computed with the 2010 HITEMP line list are also shown. At this temperature, UCL-4000 performs very similarity to 2010 HITEMP and shows excellent agreement with the experiment.

5 CONCLUSION

A new hot line list for the main isotopologue of CO_2 ($^{12}C^{16}O_2$) is presented, which is the most comprehensive (complete and accurate) data set for carbon dioxide to date. The line list is an important addition to the ExoMol data base which now contains line lists for all the major constituents of hot Jupiter and mini-Neptune exoplanets. Line lists are still being added to address the problem of hot super Earth exoplanets, or lava planets, the composition of whose atmospheres are currently not well constrained.

The line lists can be downloaded from the CDS (http://cdsweb.u -strasbg.fr/) or from ExoMol (www.exomol.com data bases.

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DATA AVAILABILITY STATEMENT

Full data is made available. The line lists can be downloaded from the CDS (http://cdsweb.u-strasbg.fr/) or from ExoMol (www.exom ol.com) data bases.

The complete list of the band centres and their corrections is given as supplementary material to the paper.

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SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.

Table 1. Examples of vibrational band centres of CO_2 computed using Ames-2 PES with TROVE (\tilde{E}_{λ}^T) , average differences with the HITRAN band centres $(\Delta \tilde{E}_{\lambda} = \tilde{E}_{\lambda}^H - \tilde{E}_{\lambda}^T)$, the shifted band centres adopted for ro-vibrational calculations $(\tilde{E}_{\lambda}^T + \Delta \tilde{E}_{\lambda})$ and three sets of quantum numbers (QN) used in this work.

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