Research Article



# Experimental Investigation of Pressure Fluctuation, Vibration, and Noise in a Multistage Pump

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In order to measure the pressure pulsation, vibration, and noise characteristics of multistage centrifugal pump in different flow rates, a five-stage centrifugal pump was chosen as research object. The results show that the main frequency of pressure pulsation was BPF<sub>1</sub>, 9APF, BPF<sub>2</sub>, BPF<sub>2</sub>, and 9APF. According to the order of monitoring points, the intensity of the pressure fluctuation increased and then decreased, with the strongest fluctuation at monitoring point P2. The peak value of pressure fluctuation is 4APF, BPF<sub>2</sub>, 9APF, 2BPF<sub>2</sub>, 3BPF<sub>1</sub>, 4BPF<sub>1</sub>, and 4BPF<sub>2</sub>. The number of characteristic frequencies at the outlet flange was significantly more than the number of characteristic frequencies at the inlet flange. As the flow rate increased, the vibration of motor gradually increased and the vibration of pump increased at first and then decreased. It reached the minimum vibration level in the design flow rate. Motor contributed the largest amount of noise caused by the pump unit. The noise level of measure point which is close to motor is higher than that of other measure points. As the flow rate increased, the noise incrementally increased, and the difference in noise level between measure points decreased gradationally. When the flow rate was 120 m<sup>3</sup>/h, the maximum difference value of different noise monitoring points was only 1.7 dB.

### 1. Introduction

Multistage centrifugal pump has characteristics of high lift and large flow rate, which is widely used in electric power, fire, metallurgy, construction, and other fields. Due to the high rotation speed of the impeller and dynamic and static interference between impeller and volute or guide vane, the internal flow of the centrifugal pump is a kind of complex unsteady turbulence flow, which will cause pressure fluctuation inside the pump. The pressure fluctuation on the wall of pump will lead to the vibration and noise. Too large vibration will affect the reliability of pump operation. Therefore, measures should be taken to reduce the pressure fluctuation in the pump [1–6].

In recent years, scholars had conducted some research on the pressure fluctuation in the pump and obtained encouraging achievements. In the 1990s, the American FFPI company [7] found that the pressure fluctuation caused by the cavitation, along with the interaction of dynamic and static interference of blades, played an important role in the vibration of the centrifugal pump, which could also lead to the operation failure. Takahiro and Yusuke [8] simulated the pressure fluctuation in the centrifugal pump and found that the dominant frequency of the pressure fluctuation in the centrifugal pump was equal to the blade frequency. Spence and Amaral-Teixeira [9, 10] combined numerical simulation with experiment to study pressure fluctuation in the centrifugal pump. The influence of the change of geometric parameters on pressure fluctuation and pump performance was also analyzed. Majidi [11] simulated numerically the internal unsteady flow of centrifugal pump and studied the pressure fluctuation at the blade outlet. Kergourlay et al. [12] used numerical calculation and experimental measurement to research the flow field and pressure fluctuation in the centrifugal pump with splitter blade. It was found that the circumferential speed and pressure in the pump with splitter blade impeller become more uniform and the vibration and noise of the pump can be reduced. Dai et al. [13] studied the effect of impeller outlet width on the pressure fluctuation in pump chamber. It was found that the static pressure and the amplitude of pressure fluctuation in front pump chamber increased with the increase of outlet width and the decrease of radius. Liu et al. [14] detected the pressure fluctuation of the 3 monitoring points on the same circumference of the single channel inlet in each stage of the multistage pump and found that the pressure fluctuation of the first stage was the most severe and the pressure fluctuation decreased gradually with the increase of the stage number.

In the study of vibration and noise of centrifugal pump, Howe [15] pointed out that the coupling between the blades and the fluid vortices would indirectly cause the noise. When the vortex center moved close to the leading edge of the blade, the coupling effect would produce unsteady force on the blade, which caused the vibration of the blade and low frequency noise. Choi et al. [16] performed an experimental investigation on the unsteady flow field and noise generation mechanism for a centrifugal turbomachine by arranging of hot-wire detectors and surface mounted pressure transducers on the blades. Srivastav et al. [17] pointed out that the noise of centrifugal pump decreased with the increase of the gap between the impeller and the volute tongue. Dai et al. [18] measured the vibration and noise of pump as turbine at different rotation speed and flow rate. It was found that the level of vibration and noise increased with the increase of rotation speed and flow rate. The sound pressure level of outlet noise under the same flow rate was higher than that of the inlet. Sun et al. [19] and Zhou [20] studied the effect of off-design condition deviation on vibration and noise. Duan et al. [21] and Escaler et al. [22] measured and analyzed the vibration signal of centrifugal pump when the cavitation was happening. The experimental results show that the vibration acceleration level of vibration signal in some frequency ranges increased after cavitation.

However, the experimental studies about vibration and noise of centrifugal pump mainly focused on single-stage centrifugal pump. The studies on multistage centrifugal pump are relatively less. Therefore, the pressure fluctuation, vibration, and noise characteristics of a five-stage centrifugal pump with guide vane used in mine drainage in this paper under different flow rate are measured and analyzed to provide the basis for the subsequent CFD optimization and reduction of vibration and noise.

# 2. Test Model and Arrangement of Monitoring Points

The test equipment mainly consists of test pump, vacuum pump, submersible pump, flow meter, gate valve, and so on. The test instruments include 2 pressure transmitters, 2 pressure gauges, 1 photoelectric tachometer, 5 HY6503 type high frequency dynamic pressure transmitters, 4 INV9832 type piezoelectric three-direction acceleration sensors, and 1 INV9206 sound pressure sensor. The INV vibration and noise testing system of Beijing Oriental vibration Institute is adopted as data acquisition system. The system contains

 TABLE 1: Main structural parameters.

Main geometric parameters	Value
Inlet diameter of inlet section $D_1$ /mm	100
Impeller outer diameter $D_2$ /mm	314
The number of first-stage impeller blades $Z_1$	6
The outlet width of first-stage impeller $b_2$ /mm	20.5
The number of second-stage impeller blades $Z_2$	7
The outlet width of second-stage impeller $b_3$ /mm	20.5
Inlet diameter of guide vane $D_3$ /mm	316
Outer diameter of guide vane $D_4$ /mm	409
Blade number of positive guide vane $Z_3$	9
Blade number of negative guide vane $Z_4$	10
Outlet diameter of outlet section $D_5$ /mm	80

16 data acquisition channels and the maximum sampling frequency is 102.4 KHz.

2.1. Test Pump. The test pump is five-stage centrifugal pump. The blade number of the first-stage impeller is 6 and blade number of other-stage impeller is 7. The design flow rate  $Q_d$  is 100 m<sup>3</sup>/h, head *H* is 165 m, rotation speed *n* is 1480 r/min, and specific speed  $n_s$  is 65.4. Table 1 shows the main structural parameters of the five-stage centrifugal pump. Figure 1 is the five-stage centrifugal pump.

2.2. Energy Characteristic Test Results. The experimental results of the energy characteristics of the five-stage guidevane centrifugal pump are shown in Figure 2. As seen from Figure 2, under  $0.8Q_d$ , the head is 172.9 m, the power is 56.1 kW, and the efficiency is 67.4%. Under  $1.0Q_d$ , the head is 165.4 m, the power is 61.8 kW, and the efficiency is 72.8%. Under  $1.2Q_d$ , the head is 152.3 m, the power is 68.8 kW, and the efficiency is 72.4%. The highest efficiency point is located in 1.1Qd and the efficiency is 74.06%.

2.3. Arrangement of Pressure Fluctuation Monitoring Points. A total of 5 pressure fluctuation monitoring points are set to measure pressure fluctuation in the pump, as shown in Figure 3. The monitoring points P1, P2, P3, and P4 are located in the pressure port of the middle of the fourth stage. The monitoring point P5 is located in the outlet of the test pump. In the pressure fluctuation test, the sampling frequency of each monitoring point is 51.2 kHz and the sampling time is 30 s.

2.4. Arrangement of Vibration Monitoring Points. A total of 8 vibration monitoring points are set. The monitoring point V1 is located in bearing A near the pump outlet. The monitoring point V2 is located in bearing B near the coupling. The V3 and V4 are located at the inlet flange and the outlet flange of the pump. The V5~V8 are at the four pump foots. Figure 4 gives the location of monitoring points V2, V4, and V5. The installation mode of the sensor is magnetic seat installation. The horizontal, vertical, and axial vibration were measured at each monitoring point.

2.5. Arrangement of Noise Monitoring Points. A total of 8 monitoring points are set. The monitoring points M1, M2,



FIGURE 1: The test pump.



FIGURE 2: Experiment result of energy characteristics.

and M8 are located near the motor. The monitoring points M3~M7 are located near the pump. Each monitoring point is arranged at the distance of 1 meter from the test pump. The height from monitoring point to the base is also 1 meter. The positions of the points are shown in Figure 5.

# 3. Test Results and Analysis of Pressure Fluctuation

*3.1. Pressure Fluctuation Data Processing Method.* There are two methods to deal with the pressure fluctuation data. One is the time domain method, and the other is the frequency domain method. In this paper, the frequency domain method is adopted to deal with the test data.

Frequency domain method decomposes the complex signal of pressure fluctuation according to the frequency magnitude. Taking the frequency as the *X* coordinate and the amplitude of pressure fluctuation as *Y* coordinate, the energy distribution of the pressure fluctuation is presented on the

spectrum. The most common method of frequency domain analysis is Fourier Transform. It transforms the time domain diagram into the frequency domain diagram and intuitively shows the frequency distribution of the pressure fluctuation. In this paper, the Fast Fourier Transform is used to analyze the frequency domain.

Assume that  $X(n\Delta t)$  is a chronological sequence with length M. The calculation equation of discrete value  $X_m$  (m = 0, 1, 2, ..., M - 1) of spectrum X(f) is

$$X_m = X\left(m\Delta f\right) = \frac{1}{M} \sum_{n=0}^{M-1} x\left(n\Delta t\right) \exp\left(-j\frac{2\pi nm}{M}\right), \quad (1)$$

where  $\Delta f$  is the frequency resolution, *M* is the number of samples, and  $\Delta t$  is the time step.

Define the blade frequency multiplier  $N_F$ :

$$N_F = \frac{60F}{n} = \frac{F}{F_n},\tag{2}$$



FIGURE 3: Location of the pressure fluctuation monitoring points.



(a) V2

(b) V4

(c) V5

FIGURE 4: Location of vibration monitoring points.

where *F* is the actual frequency after the Fourier Transform and  $F_n$  is the pump shaft rotation frequency under corresponding rotation speed (APF).

3.2. Pressure Fluctuation Characteristics under Design Flow Rate. The pressure fluctuation frequency domains of the monitoring points P1~P5 under the design flow rate are shown in Figure 6. The impeller rotation speed is 1480 r/min.

The blade number of the first-stage impeller is 6. The blade number of the second-stage impeller is 7. So the pump shaft rotation frequency (APF) is 24.67 Hz. The frequency of the first-stage impeller blades passing through the guide vane (BPF<sub>1</sub>) is 148 Hz and that of the second-stage impeller (BPF<sub>2</sub>) is 172.67 Hz. As can be seen from Figure 6, the dominant frequencies of P1 to P5 are BPF<sub>1</sub>, 9APF, BPF<sub>2</sub>, BPF<sub>2</sub>, and 9APF. The corresponding peak values are 4.91 KPa,





FIGURE 5: Location of noise monitoring points.

17.83 KPa, 13.75 KPa, 9.17 KPa, and 4.35 KPa. Comparing the pressure fluctuation of different stages, it can be found that the intensity of pressure fluctuation increases firstly and then decreases. From the second stage, the pressure fluctuation intensity gradually decreases with the increase of the stage number.

In addition to the dominant frequencies of each monitoring point (BPF<sub>1</sub>, 9APF, and BPF<sub>2</sub>), the other obvious peak values are APF, 2APF, 3APF, 8APF, and 10APF. The frequency components of pressure fluctuation of each monitoring point are complex. However, the blade passing frequency can still be clearly seen and the fluctuation intensity is relatively larger. The blade frequency is attributed to the mutual interference between impeller and guide vane. The peak value of the shaft frequency is obviously less than the peak value of other characteristic frequencies. This is due to the relatively high manufacturing accuracy of the impeller.

3.3. Pressure Fluctuation Characteristics of Each Monitoring Point under Different Flow Rates. In order to further compare the pressure fluctuation characteristics under different flow rates, the pressure fluctuation frequency spectrums of the monitoring points P1~P5 under different flow rates are analyzed, as shown in Figure 7. As can be seen from Figure 7(a), the relatively obvious frequencies are APF, 2APF, and BPF1. The pressure fluctuation intensity under the offdesign flow rate is larger than that under the design flow rate. At the same time, the low frequency peak value of pressure fluctuation increases with the increase of flow rate. With the increase of flow rate, the characteristic blade frequency peak value of the monitoring point P1 increases firstly, then decreases, and reaches the maximum under the design flow rate.

The structure of the second-stage impeller to the fifthstage impeller is the same. As a result, the fluctuation trend of the monitoring points P2~P4 is similar to the fluctuation frequency and the blade frequency is 7 times of the shaft frequency, as shown in Figures 7(b)–7(d). The obvious characteristic frequencies are 6APF, BPF, 9APF, 10APF, and 18.15APF. The 6 times shaft frequency is generated by firststage impeller. The peak value of 6APF decreases with the increase of the stages number. In the frequency spectrum of the monitoring point P2, the dominant frequencies under different flow rate are all the blade frequency. The peak value



FIGURE 6: Spectrogram of pressure fluctuation under design flow rate.



FIGURE 7: Pressure fluctuation spectrogram of each monitoring point.

of blade frequency increases firstly and then decreases with the increase of flow rate, and the maximum value appears at  $0.6Q_d$ , which is 27 KPa. Under different flow rates, the fluctuation intensities of P3 are overall low and the difference between them is small. The dominant frequency is 9APF and the peak value is 8.6 KPa under  $0.4Q_d$ . From  $0.6Q_d$  to  $1.2Q_d$ , the dominant frequency is the blade passing frequency. The general trend of peak value of the blade frequency was firstly increased, then decreased, and reached the maximum at  $1.0Q_d$ , which was 12.6 KPa. The dominant frequency of P4 under  $0.4Q_d$  is 9APF and the peak value is relatively larger, which was 22 KPa. The dominant frequencies under other flow rate are all blade frequency. The relatively obvious characteristic frequency also includes 10APF.



FIGURE 8: Pressure fluctuation amplitude of each monitoring point.

Figure 7(e) is the frequency domain of pressure fluctuation of monitoring point P5 at outlet of the pump. The relatively obvious characteristic frequencies are APF, 2APF, BPF<sub>2</sub>, and 9APF. The dominant frequencies under the five flow rates are 2APF, 2APF, BPA<sub>2</sub>, 9APF, and 2APF. The characteristic peak values of dominant frequencies are 2.6 KPa, 2.8 KPa, 3.1 KPa, 4.1 KPa, and 2.9 KPa. The maximum characteristic peak value appears in 9APF under design flow rate. Comparing the pressure fluctuation of P5 with the pressure fluctuation of P1~P4, it can be found that the intensity of pressure fluctuation at the outlet is significantly smaller than that in the middle section of each stage.

*3.4. Pressure Fluctuation Amplitude Analysis.* The formula of pressure fluctuation amplitude is as follows:

$$A_{p} = \sqrt{\frac{\sum_{i=1}^{N} \left( p(i) - \overline{p} \right)}{N}}$$

$$\overline{p} = \frac{1}{N \sum_{i=1}^{N} p(i)},$$
(3)

where p(i) is transient pressure value in the time domain and  $\overline{p}$  is the average pressure value.

Calculating the root mean square value of the each monitoring data of the first 10 seconds, the amplitudes of each monitoring point are obtained, as shown in Figure 8. As can be seen from Figure 8, the maximum value of the fluctuation appeared at P2 under  $0.4Q_d$ , which was 25.56 KPa. The minimum value of the fluctuation appeared at P1 under  $1.0Q_d$ , which was 10.25 KPa. The fluctuation amplitude of P2 is obviously higher than that of other monitoring points. This is due to the different blade numbers of first-stage impeller and second-stage impeller. The water flows through the first-stage impeller and produces a characteristic frequency of

6APF. The characteristic frequency and the characteristic frequency of 7APF caused by the second-stage impeller interfere with each other, which make the flow chaotic and the fluctuating amplitude high. The values of P3, P4, and P5 are close to each other and the fluctuation amplitude of the monitoring point P1 is the smallest. The lowest values of P1, P2, and P4 are all under  $1.0Q_d$ .

#### 4. Test Results and Analysis of Vibration

The test data of each monitoring point were measured two times to ensure the accuracy. During the test, the pump rotation rate is kept constant. The sampling frequency of each monitoring point is set to be 12.8k and the sampling time is 30 s. The time domain signal of vibration acceleration speed is converted into frequency domain signal by Fast Fourier Transform. For the reduced leakage spectrum in conversion process, window type is adopted to be Hanning window. Acceleration signal analysis spectral range is 10 to 12800 Hz.

4.1. Vibration Data Processing Method. Based on definition of sound pressure level, vibration acceleration speed level  $L_a$  is defined (unit is dB):

$$L_a = 20 \lg \frac{a_e}{a_0},\tag{4}$$

where  $a_e$  is the effective value of vibration acceleration speed,  $a_0$  is the reference value, and  $a_0$  usually is taken to be  $10^{-6} \text{ m/s}^2$ .

4.2. Characteristic Frequency Analysis of Vibration Acceleration Speed under Design Flow Rate. In order to obtain the characteristic frequency of vibration acceleration speed, the vibration acceleration spectrums of different monitoring points under design flow rate are analyzed. Figure 9 shows

Monitoring point	Horizontal	Vertical	Axial
V1	127.88	128.12	118.85
V2	131.08	128.01	116.18
V3	119.26	118.45	121.09
V4	121.55	119.23	131.38
V5	114.72	113.91	113.16
V6	115.44	114.54	113.07
V7	115.12	115.03	113.81
V8	114.53	113.45	113.69

TABLE 2: Vibration acceleration in different monitoring point (dB).

the vibration acceleration speed spectrums of the eight monitoring points. *X*, *Y*, *Z* represent the horizontal, vertical, and axial vibration acceleration speed.

It can be seen from Figure 9 that the characteristic frequencies of vibration acceleration speed of each monitoring point are basically the same. The impeller rotation rate n is 1480 r/min. The blade number of first-stage impeller is 6. The blade number of second-stage impeller is 7. Then the pump shaft rotation frequency (APF) is 24.67 Hz. The blade passing frequency of first-stage impeller is 6APF (BPF<sub>1</sub>). The blade passing frequency of second-stage impeller is 7APF (BPF<sub>2</sub>). The main characteristic frequencies include 4APF, BPF<sub>2</sub>, 9APF, 2BPF<sub>2</sub>, 3BPF<sub>1</sub>, 4BPF<sub>1</sub>, and 4BPF<sub>2</sub>. 4APF is 4 times shaft frequency. BPF<sub>1</sub> and BPF<sub>2</sub> are the vibration frequencies caused by the periodic interaction between blade and guide vane. 3BPF<sub>1</sub>, 4BPF, and 2BPF<sub>2</sub> are higher harmonics of blade frequencies. The characteristic frequency of vibration at the outlet flange is obviously more than that of the inlet flange.

The above characteristic frequencies show that the blade frequency and its higher harmonics are the main source of excitation. It is an effective method to reduce the vibration of the pump by optimizing the structure and internal flow of the pump and reducing the pressure fluctuation caused by the mutual interference between impeller and guide vane. There are no obvious shaft frequency and 2 times shaft frequency on the vibration frequency spectrum. This is due to the high manufacturing accuracy of the impeller. The dynamic balance is relatively good and the coaxiality of pump shaft and motor shaft is relatively high. The excitation that can produce shaft frequency and 2 times shaft frequency is relatively small.

Table 2 shows the vibration acceleration speed levels of each monitoring point under the design flow rate. In this paper, the vibration of frequency below 1000 Hz is defined as low frequency vibration and the vibration frequency higher than 1000 Hz is defined as high frequency vibration. Low frequency vibration usually comes from the vibration of the pump. High frequency vibration usually comes from the vibration of the motor. As can be seen from Table 2, the vibration of the monitoring points V1 and V2 in the horizontal and vertical direction is greater than the axial vibration. This is because the V1 and V2 are located at the bearing. The bearings can bear the radial force and axial force generated by the rotor running. Radial force is generally larger and cyclical changes, which is related to the blade frequency. Axial force, due to function of the balance disc, is generally small and has no obvious change cycle. The vibration of V4 is greater than that of V3. This is because the inlet flow is more stable and the vibration is less. The flow in the outlet is affected by the static and dynamic interference between the impeller and the guide vane. The pressure fluctuation is more obvious. The excitation of the fluid makes the vibration of the outlet flange larger. At the same time, the vibration of the outlet flange is larger than that of the inlet flange, causing axial vibration of V1 at bearing A near outlet flange to be larger than that of V2 at bearing B near inlet flange.

4.3. Comparative Analysis of the Total Pump Vibration Level under Different Flow Rate. In order to further study the variation law of the pump vibration acceleration speed, the low frequency, high frequency, and total vibration level of the vibration acceleration speed level in the vertical direction of four monitoring points V5~V8 located on the pump foots are analyzed (shown in Figure 10).

It is can be seen from Figure 10 that, with the increase of the flow rate, the high frequency and the total vibration acceleration speed level increase gradually. This is because the high frequencies of vibration in the multistage pump group mainly come from the motor. The low frequencies of vibration mainly come from the pump. The amplitude of high frequency vibration is larger and it has the largest contribution to the total vibration level of the pump group. When the flow rate changes from  $40 \text{ m}^3/\text{h}$  to  $100 \text{ m}^3/\text{h}$ , the low frequency vibration acceleration speed level decreases.

The vibration acceleration speed level of the pump is lowest under the design flow rate. It can be concluded from the low frequency vibration that the vibration acceleration speed level of the pump will be increased, when deviated from the design flow rate. When the flow rate increases from  $100 \text{ m}^3/\text{h}$  to  $120 \text{ m}^3/\text{h}$ , the vibration acceleration speed level increases by 7.94 dB. When the flow decreases from  $100 \text{ m}^3/\text{h}$  to  $40 \text{ m}^3/\text{h}$ , the vibration acceleration speed level increases by only 2.51 dB.

4.4. Vibration Intensity Analysis. The vibration intensity is the root mean square (effective speed value) of the vibration velocity under the wide frequency (10~1000 Hz). According to the evaluation criteria of the vibration standard, the vibration intensity of the two bearings (i.e., monitoring points V1 and V2) under the 40 m<sup>3</sup>/h, 100 m<sup>3</sup>/h, and 120 m<sup>3</sup>/h are calculated, as shown in Table 3. The center height of the pump is 290 mm and the rotation rate is 1480 r/min. As can be seen from Table 3, the maximum vibration intensity appears in the Y direction of the bearing B under  $1.2Q_d$  and the vibration intensity value is 1.08 mm/s.

#### 5. Test Results and Analysis of Noise

Measurement of noise is simultaneous with measurement of vibration. The sampling frequency is set as 25.6k. The sampling time is 40 s. The time domain signal of vibration acceleration speed is converted into frequency domain signal by Fast Fourier Transform. For the reduced leakage spectrum in conversion process, window type is adopted to be Hanning window. Noise signal analysis spectral range is 0 to 25600 Hz.



FIGURE 9: Spectrogram of vibration acceleration speed.



FIGURE 10: Vibration acceleration in different flow rate.

TABLE 3: Vibration intensity (mm/s).

	0.4Q <sub>d</sub>		1.0Q <sub>d</sub>		1.2Q <sub>d</sub>	
	Bearing A	Bearing B	Bearing A	Bearing B	Bearing A	Bearing B
Χ	0.78	0.78	0.82	0.82	1.01	0.98
Y	0.87	0.95	0.94	0.91	1.05	1.08
Ζ	0.24	0.22	0.25	0.22	0.53	0.33

The sound pressure level (root mean square acceleration) is adopted to evaluate the noise level. The calculation formula of sound pressure level is as follows:

$$L_p = 20 \lg \frac{p}{p_0},\tag{5}$$

where *p* is the effective value of sound pressure,  $p_0$  is the reference sound pressure, and  $p_0$  in the air is 20  $\mu$ Pa.

Figure 11 shows the sound pressure level of eight monitoring points under different flow rate. As seen from Figure 11, the noise level of the monitoring point can be roughly divided into three grades. The noise levels of M1, M2, and M8 near the motor are relatively higher. The noise levels of M3 and M7 at pump side are secondary. The noise levels of M4, M5, and M6 are the minimum. Thus, the noise generated by the motor accounted for the most noise of the pump group. The closer the motor to monitoring point is, the higher the noise level is. At the same time, the noise levels of the monitoring points with axis symmetric distribution are very close, such as M3 and M7, M4, and M6. When the flow rate is  $40 \text{ m}^3/\text{h}$ , the noise level of M2 is the highest and the noise level of M6 is the lowest. Difference in noise level is 7.7 dB. With the increase of the flow rate, the difference between the noise levels of the monitoring points is getting smaller and smaller. When the flow rate is  $120 \text{ m}^3/\text{h}$ , the highest noise level of M2 is 83.6 dB and the lowest noise level of M6 is 81.9 dB. The difference in noise level is only 1.7 dB.

With the increase of flow rate, the sound pressure levels of M3 to M7 increase. However, M1, M2 and M8 had no obvious regularity. The noise change of the monitoring points shows that the noise of the pump will increase with the increase of the flow rate. When the flow rate is  $120 \text{ m}^3/\text{h}$ , the noise level is obviously higher than other flow rates.

#### 6. Conclusion

(1) The pressure fluctuation dominant frequencies of P1 to P5, respectively, are  $BPF_1$ , 9APF,  $BPF_2$ ,  $BPF_2$ , and 9APF. The corresponding peak values are 4.91 KPa, 17.83 KPa, 13.75 KPa, 9.17 KPa, and 4.35 KPa. From the monitoring point P1 to the monitoring point P5, the intensity of the fluctuation increases firstly and then decreases.

(2) The 6 times shaft frequency caused by first-stage impeller and the 7 times shaft frequency caused by second-stage impeller produce interference. The flow is chaotic, which makes the pressure fluctuation intensity of P2 significantly higher than that of other monitoring points. Under the large flow rate and small flow rate, the fluctuation intensity increases significantly. The minimum amplitudes of the P1, P2, and P4 are under  $1.0Q_d$ .

(3) The main characteristic vibration frequencies of the pump include 4APF,  $BPF_2$ , 9APF,  $2BPF_2$ ,  $3BPF_1$ ,  $4BPF_1$ , and  $4BPF_2$ . The radial force produced by the running rotor is bigger than the axial force and has obvious periodicity,



FIGURE 11: Sound pressure level under different flow rate.

which causes that the vibration intensity of the bearings in the horizontal and vertical direction is bigger than the axial vibration intensity. The maximum vibration intensity of pump bearing is 1.08 mm/s.

(4) The noise generated by the motor accounted for the most of that of the pump group. With the increase of the flow rate, the difference between the noise levels of the monitoring points is getting smaller and smaller. When the flow rate is  $40 \text{ m}^3$ /h, the maximum difference of noise level of each monitoring point is 7.7 dB. When the flow rate is  $120 \text{ m}^3$ /h, the maximum difference of noise level of each monitoring point is only 1.7 dB.

#### **Conflicts of Interest**

The authors declare that they have no conflicts of interest.

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