



Article Experimental Research on a New Mini-Channel Transcritical CO₂ Heat Pump Gas Cooler

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Abstract: This paper presents the results of an experimental study on the heat transfer and pressure drop characteristics of a novel spiral plate mini-channel gas cooler designed for use with supercritical CO_2 . The CO_2 channel of the mini-channel spiral plate gas cooler has a circular spiral cross-section with a radius of 1 mm, while the water channel has an elliptical cross-section spiral channel with a long axis of 2.5 mm and a short axis of 1.3 mm. The results show that increasing the mass flux of CO_2 can effectively enhance the overall heat transfer coefficient when the water side mass flow rate is 0.175 kg·s⁻¹ and the CO_2 side pressure is 7.9 MPa. Increasing the inlet water temperature can also improve the overall heat transfer coefficient. The overall heat transfer coefficient is higher when the gas cooler is vertically oriented compared to horizontally oriented. A Matlab program was developed to verify that the correlation based on Zhang's method has the highest accuracy. The study found a suitable heat transfer correlation for the new spiral plate mini-channel gas cooler through experimental research, which can provide a reference for future designs.



1. Introduction

It is widely known that the emergence of transcritical CO₂ heat pump technology has led to increased attention to the flow and heat transfer characteristics of supercritical flu-ids. As a natural working fluid, CO_2 has a lower critical point compared to other fluids, with a critical temperature of 31.1 °C and critical pressure of 7.38 MPa, making it easier for CO_2 to reach its supercritical state. This has made the CO_2 heat pump cycle very popular worldwide due to its excellent environmental protection and wide operating range [1]. Since fluids at supercritical state have unique properties, the heat transfer characteristics are more complicated and the design of heat exchanges is more challenging than that of conventional heat exchanges. In addition, considering the requirements of the operating pressure of 8–10 MPa and a small volume of the system, the heat exchanger calls for high strength and high compactness [2]. Therefore, it is critical to study the heat transfer and pressure drop characteristics of supercritical CO_2 in compact heat exchangers. Figure 1 shows the variation of specific heat, thermal conductivity, viscosity, and density of CO_2 with the temperature at the pressure of 8 MPa. In the early days of research about heat transfer of supercritical CO₂, considerable efforts have been made to study the convective heat transfer characteristics of supercritical CO_2 in a single tube or simple types of heat exchangers [3-6]. Research on the heat transfer characteristics of supercritical CO₂ in spiral channels is currently limited. However, with the rapid development of processing and manufacturing technologies such as diffusion welding and brazing, several types of compact heat exchangers have been used in supercritical CO₂ facilities. The printed circuit



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). heat exchanger (PCHE) is considered suitable for recuperators due to its small channels and excellent pressure and temperature tolerance. Some scholars also investigate the heat transfer between CO_2 and water in PCHEs. It has been noted that the high cost of PCHEs can make them less competitive as a gas cooler option. As an alternative, a microtube shell-and-tube heat exchanger (MSTE) was proposed. However, it has a small shell-side space, being prone to scale, difficult to clean, and not suitable for use as a CO_2 heat pump gas cooler. In transcritical CO_2 heat pumps, the water side of the gas coolers can be prone to fouling during long-term operations, but spiral plate heat exchangers (SPHEs) can ad-dress the issue. SPHEs' unique geometry eliminates stagnant areas in the channel, resulting in a low fouling tendency. Therefore, SPHEs may be a more suitable option for CO_2 heat pump gas coolers than MSTEs or PCHEs. The spiral plate heat exchanger has a long history dating back to 1930, when it was first proposed by Rosenblad in Sweden. Over the years, it has undergone numerous improvements and innovations. Coons et al. [7] tested five different SPHEs and collected data on pressure, temperature, velocity, mass flow rate, and pressure drop for the heating and cooling of oil, water, brine, and steam. For spiral exchangers operating under laminar flow conditions, the average Nusselt number correlation was suggested. Baird et al. [8] developed a correlation for calculating the heat transfer coefficient for a Rosenblad SPHE. Water was used as the working fluid for both ducts. They assumed that the temperature change would be linear along the spiral length and used the mean spiral radius as the radius at the mean spiral length. Tangri and Jayaraman [9] tested the applicability of the Dittus–Boelter equation for predicting heat transfer in an SPHE. The overall heat transfer coefficient was found to decrease with an increase in the spiral radius. Buonopane and Troupe [10] derived the equations to describe the thermal performance of SPHEs by making energy balance on a differential wedge element of an SPHE. Heat transfer correlations were developed using a modified Wilson plot technique. Zhang et al. [11] developed a computational method for the thermal design of an SPHE. Bes and Roetzel [12–14] analyzed the thermal performance of a spiral heat exchanger and developed an analytical method to evaluate fluid temperature variation in a countercurrent spiral heat transfer. Shirazi et al. [15] developed a new algorithm for spiral plate heat exchangers; the algorithm was optimized in terms of geometric aspect ratio, pressure drop, and total cost. The relative heat rate capacity per volume of the newly designed spiral plate heat exchanger reached up to 54%, compared to other designs. Rajavel et al. [16] tested a spiral plate heat exchanger, and a new correlation based on the experimental data was given for practical applications. A numerical method was proposed by Garcia et al. [17] to estimate the temperature distribution and overall heat transfer coefficients based on the flow rates and temperatures at inlet and outlet. The first significant numerical study was published by Devois et al. [18]. They produced a thermal model of the heat exchanges in both steady-state and time-dependent cases with a 2D spiral geometry, allowing computation with different materials, forced convective heat transfer models in turbulent flow, and geometrical parameters options. Nguyen et al. [19,20] developed a numerical method to investigate the heat transfer performance of a spiral heat exchanger. Many researchers have focused mainly on experimental studies to validate their research results and numerical methods, with particular emphasis on designing and optimizing spiral plate heat exchangers. However, there are relatively few examples of innovative designs on the original structure. The heat transfer correlation proposed by the researchers is mostly based on water, and little research has been carried out on carbon dioxide. In addition, the forms of heat transfer correlation vary among researchers. Therefore, further research is needed to establish more accurate and reliable heat transfer correlations for spiral plate mini-channel gas coolers. Furthermore, there has been no experimental study to date on the heat transfer and pressure drop characteristics of the new spiral plate mini-channel gas cooler. Further research is therefore needed to better understand these characteristics and optimize the design of this type of heat exchanger. This study described in this paper builds on previous research that demonstrated the feasibility of gas coolers using numerical simulations [21]. The authors produced a physical

prototype using diffusion bonding and conducted experiments to analyze internal heat transfer patterns. Through these experiments, the authors were able to develop accurate heat transfer correlations and pressure drop calculation methods. The traditional method of calculating pressure drops for spiral plate heat exchangers is no longer applicable, as previous studies have been based on hot and cold water, and numerical simulation methods are not universally applicable. The authors' work represents an important contribution to the field, providing new insights into the performance characteristics of spiral plate heat exchangers with gas cooling applications. By developing more accurate heat transfer correlations and pressure drop calculation methods, the authors have laid the foundation for future research aimed at optimizing the design and operation of these systems.



Figure 1. Physical properties of supercritical CO_2 at p = 8 MPa.

In this study, a 10 kW supercritical CO_2 heat exchanger experimental platform is built, and a new spiral plate mini-channel gas cooler is designed and processed to have a better understanding of the cooling heat transfer characteristics of supercritical CO_2 in the new spiral plate mini-channel gas cooler. In Section 2, the experimental system and gas cooler structure are described. In Section 3, the effects of different variables on heat transfer, the accuracy of different heat transfer correlations, and the accuracy of pressure drop calculation methods are analyzed. The findings are provided in Section 4.

2. Experiment Setup

2.1. Experiment System

Figure 2 shows a schematic diagram of the experiment system, and Figure 3 shows a physical diagram of the experiment system. The system consists of various components, including a compressor, liquid CO₂ storage tank, buffer tank, chiller, cooler, measuring sensors, electric heater, data acquisition module, and control console. The compressor used in this system is a plunger pump that can be cooled by compressed air at room temperature. This approach allows CO₂ pressurization under a variety of conditions without any concern for seal failure due to overheating of the pump chamber. Carbon dioxide is directly heated by the electric heater. The outlet pressure of the compressor can reach 25 MPa, and the maximum flow rate is $0.05 \text{ kg} \cdot \text{s}^{-1}$. The maximum heating power of the preheater is 25 kW. In addition to the various components described above, the experimental platform is also equipped with a remote console. This console can remotely control the compressor, pneumatic valves, electric heater heating power, and data monitoring and recording via a computer. Overall, this feature adds another layer of safety to the experimental setup,

ensuring that researchers can conduct experiments effectively and without risk to their personal safety. The object-in-kind of the new spiral plate mini-channel gas cooler is shown in Figure 4. The overall schematic is shown in Figure 4b, and the important dimensions of the gas cooler are listed in Table 1. Information on experimental equipment is summarized in Table 2.



Figure 2. Schematic of experimental system.



Figure 3. Test platform and console.





(b)

Figure 4. (a) Object-in-kind; (b) overall schematic.

Overall Dimensions				
Gas cooler length	200 mm			
Gas cooler width	200 mm			
Gas cooler height	86 mm			
Gas cooler single later plate thickness	2 mm			
Carbon Dioxide Side				
Carbon dioxide channel length	2.2 m			
Carbon dioxide channel radius	1 mm			
Water Side				
Elliptical channel length	2.2 m			
Elliptical channel short semiaxis	1.3 mm			
Elliptical channel long semiaxis	2.5 mm			

Table 1. Important dimensions of the gas cooler.

Table 2. The information of the experimental equipment.

Equipment	Types	Models	Range	Accuracy
Compressor	Air-driven gas booster compressor	Haskel, AGD-32	25 MPa, 0~0.05 kg/s	-
CO_2 flowmeter	Coriolis mass flowmeter	Sincerity, DMF-1-3A	0.0139~0.1389 kg/s	0.2%
Water flowmeter	electromagnetic flowmeter	YIHUA	0~0.3 kg/s	0.5%
Heater	Electric heater	HY-380-25kW	25 kŴ	-
Chiller	Air-cooled	XX-05A	15 kW	-
Differential pressure sensors	-	Yokogawa	0~200 kPa	0.075%
Pressure sensors	-	GAPT-I-H-0.25-25	0~25 MPa	0.25%
Temperature sensors	RTD	WZPB-230	0~100 °C; 0~150 °C	±0.2 °C

During the experiment, liquid CO_2 is initially filled into the entire system loop from the storage tank. Once the liquid CO_2 filling is complete, the filling circuit valve is closed, and the main circulation circuit valve is opened to circulate CO_2 using the booster pump. To heat and pressurize the system, an electric heater is used, while cooling water is introduced into the terminal cooler to ensure that the temperature at the pump inlet does not exceed the limit. In addition, a buffer tank after the compressor can effectively eliminate flow fluctuations caused by the reciprocating movement of the pump, making the experimental flow more stable and the results more accurate.

2.2. Date Reduction

The experimental system used in this study was designed to test the performance of a gas cooler when placed horizontally and vertically. To ensure the accuracy of the results, efforts were made to minimize heat dissipation from the experimental system to the environment. Experimental data revealed that there was a difference of no more than 15% be-tween the heat absorbed by the cold fluid and the heat released by the hot fluid that is acceptable for engineering applications. Figure 5 shows the heat exchange error under different working conditions. In most of the working conditions tested, the heat release from the hot side of the gas cooler was greater than the heat absorption from the cold side. It is possible that the experimental conditions were constantly changing, resulting in some of the heat being absorbed by the solid wall. As a result, the temperature between the solid and the two fluids did not reach thermal equilibrium. These findings suggest that the gas cooler is effective in cooling and could be used in a variety of engineering applications. The overall heat exchange of the gas cooler was calculated using the mass flow rate of carbon dioxide and enthalpy at the inlet and outlet points, as shown:

$$Q_{\rm CO_2} = \dot{m}_{\rm CO_2} (h_{\rm CO_2, in} - h_{\rm CO_2, out})$$
(1)



Figure 5. Heat balance diagram under different working conditions. The blue line is the heat balance line, the red line is the error line.

The temperature difference between the cold and the hot fluid can be calculated using the logarithmic mean temperature difference, as follows:

$$\Delta T_{\text{LMTD}} = \frac{\max(\Delta T_1, \Delta T_2) - \min(\Delta T_1, \Delta T_2)}{\ln(\max(\Delta T_1, \Delta T_2) / \min(\Delta T_1, \Delta T_2))}$$
(2)

As the heat transfer areas on the sides are not the same, the heat transfer area on the carbon dioxide side is used as the basis for calculating the total heat transfer coefficient for the spiral plate mini-channel gas cooler, as shown:

$$U = \frac{1}{\frac{1}{U_{\rm CO_2}} + \frac{\delta}{\lambda} + \frac{A_{\rm CO_2}}{U_{water}A_{water}}}$$
(3)

The total heat transfer coefficient can also be calculated according to the following formula:

$$Q = UA\Delta T_{LMTD} \tag{4}$$

The heat transfer coefficient of water can be calculated using the empirical correlation as follows:

$$U_{water} = 0.05 \text{Re}^{0.6459} \text{Pr}^{0.4} \left(\frac{\mu_b}{\mu_w}\right)^{0.14} \frac{\lambda}{d}$$
(5)

Multiple correlations were used on the CO₂ side for comparison, including Mcadams, Inagaki, Morimoto, Zhang, and Minton, as shown in Table 3 [11–26]. The traditional flow resistance calculation method for a spiral plate heat exchanger is mainly based on the Sauder equation, which was derived experimentally to calculate pressure loss. However, since conventional spiral plate heat exchangers have a fixed column distance, these equations cannot be applied. Therefore, a more accurate calculation method needs to be found. An adjusted formula was introduced incorporating the number of spiral turns and the length, as given in [27,28]:

$$\Delta P = \frac{1.5G^2N}{2}(\frac{1}{\rho_i} + \frac{1}{\rho_o}) + \frac{fLG^2}{2d\rho_m} + G^2(\frac{1}{\rho_o} - \frac{1}{\rho_i}) + \frac{\rho_m v^2}{2}k \tag{6}$$

$$\frac{1}{\sqrt{f}} = 3.48 - 1.7372 \ln\left[\frac{\varepsilon}{a} - \frac{16.2426}{\text{Re}} \ln\left(\frac{(\varepsilon/a)^{1.1098}}{6.0983} + \left(\frac{7.149}{\text{Re}}\right)^{0.8981}\right)\right]$$
(7)

where ε is the surface roughness, and a is half of the hydraulic diameter.

Table 3. Different heat transfer coefficient correlations of CO₂.

Literatures	Correlations	Notes
Coons (1947) [2]	$\overline{Nu} = 8.4 \left(\frac{mc_p}{kL}\right)^{0.2}$	Laminar flow
McAdams (1954) [25]	$\overline{Nu} = 0.023 \operatorname{Re}^{0.8} \operatorname{Pr}^{m}$ $Nu = 0.023 \left(1.0 + 3.54 \frac{d}{22}\right) \operatorname{Re}^{0.8} \operatorname{Pr}^{m}$	Turbulent flow m = 0.3 for cooling m = 0.4 for heating m = 0.3 for cooling, m = 0.4 (colored by the second s
Baird (1957) [8]	$\overline{Nu} = CRe^{0.75}Pr^m$	m = 0.4 for heating m = 0.3 for fluid gaining heat, $m = 0.4for fluid losing heatC = 0.055, 4 < Pr < 10and 9000 < Re < 78 000$
Minton (1970) [26]	$U = 0.023 \Big[1.0 + 3.54 \Big(\frac{d}{D_s} \Big) \Big] c_p G \text{Re}^{-0.2} \text{Pr}^{-2/3}$	$\operatorname{Re} > \operatorname{Re}_{cr}$
Buonopance and Troupe (1970) [10]	$\frac{\overline{Nu}}{\overline{Nu}} = 0.0235 \text{Re}^{0.81} \text{Pr}^{1/3}$ $\overline{Nu} = 0.0111 \text{Re}^{0.87} \text{Pr}^{1/3}$	Parallel flow
Zhang (1988) [11]	$Nu = 0.023 \left(1.0 + 10.3 \left(\frac{d}{R} \right)^3 \right) \operatorname{Re}^{0.8} \operatorname{Pr}^m$	m = 0.3 for cooling, m = 0.4 for heating
	$\overline{Nu} = 0.10027 \mathrm{Re}^{0.682} \mathrm{Pr}^m$	8000 < Re < 80,000 <i>m</i> = 0.3 for cooling, <i>m</i> = 0.4 for heating
Morimoto and hotta (1988) [27]	$\overline{Nu} = 0.0239 \left(1.0 + 5.54 \frac{d}{R_m} \right) \operatorname{Re}^{0.806} \operatorname{Pr}^{0.268} R_m = \frac{R_{\min} + R_{\max}}{2}$	
Inagaki (1998) [28]	$Nu = 0.78 \text{Re}^{0.51} \text{Pr}^{0.3}$	6000 < Re < 22,000

The heat transfer and hydraulic characteristics of fluids within spiral channels can be predicted based on the geometric parameters of spiral channels. Figure 6 shows the primary geometric parameters of a counterflow spiral plate heat exchanger, including channel width, channel spacing, initial spiral diameter, outer spiral diameter, and initial spiral channel diameter, which can be calculated using Equation (8):

$$d_{f1} = d_{21} + b_1 + \delta \tag{8}$$

In the equation, d_{21} represents the inner diameter of the water side channel, and the outer diameter of the spiral channel can be calculated using Equation (9):

$$D_s = \sqrt{d_{f1}^2 + 1.28L(b_1 + b_2 + 2\delta)} \tag{9}$$

The number of spiral turns can be obtained from the following equation.

$$N = \frac{-(d_{f1} - \frac{b_1 + b_2 + 2\delta}{2}) + \sqrt{(d_{f1} - \frac{b_1 + b_2 + 2\delta}{2})^2 + \frac{4L(b_1 + b_2 + 2\delta)}{\pi}}}{2(b_1 + b_2 + 2\delta)}$$
(10)

The hydraulic diameter is calculated by the following equation.

$$d = \frac{4 \times \text{cross section}}{\text{wetted perimeter}} \tag{11}$$

The Reynolds number is calculated as follows:

$$\operatorname{Re} = \frac{md}{\mu A} \tag{12}$$

The Prandtl number is calculated as follows:

$$\Pr = \frac{\mu c_p}{\lambda} \tag{13}$$



Figure 6. Scheme for calculation of the outer diameter.

For the supercritical CO_2 -water experiment, it is not suitable to directly analyze the heat transfer coefficient using the logarithmic mean temperature difference method due to the large change in the physical properties of supercritical CO_2 . The complex manufacturing technique also makes it difficult to measure the temperature of the tube wall directly. As a result, a segmented calculation program is developed based on the existing correlations of the CO_2 heat transfer coefficient to predict heat transfer and pressure drop between supercritical CO_2 and water in the spiral plate mini-channel gas cooler, as shown in Figure 7. The gas cooler model is based on the principles of energy conservation, and establishes a one-dimensional submodel with variable physical properties of s CO_2 . The model assumes that the temperature of the CO_2 inner wall can be used to calculate the heat flux on both the CO_2 and the water sides, and from there the heat transfer coefficients on both sides can be calculated. The model then iteratively calculates until the difference between the CO_2 and the water side heat exchange is less than 0.1% of the CO_2 side heat exchange.



Figure 7. Spiral plate mini-channel gas cooler design program.

However, there are some assumptions made in this model.

- (1) Axial thermal conductivity and ambient heat dissipation are ignored;
- (2) The specific heat, density, and thermal conductivity of the metal wall are constants;
- (3) There is a fully developed turbulent flow without entrance and exit effects;
- (4) A uniform flow distribution in each channel of the plate is assumed by the model.

2.3. Uncertainty Analysis

In the supercritical CO_2 -water heat exchange experiment, the uncertainty in the water-side heat exchange mainly arises from the error in the flow and temperature measurements. The calculated error resulting from the temperature measurement is expressed using the following formula, which represents the difference between inlet and outlet temperatures [29]:

$$\frac{\delta \Delta T_{\text{water}}}{\Delta T_{\text{water}}} = \frac{|\delta T_{\text{water,in}}| + |\delta T_{\text{water,out}}|}{T_{\text{water,in}} - T_{\text{water,out}}}$$
(14)

where δT_{water} is determined to be ± 0.2 °C. The calculation error of the heat exchange is as follows:

$$\frac{\delta Q_{\text{water}}}{Q_{\text{water}}} = \sqrt{\left(\frac{\delta \dot{m}_{\text{water}}}{\dot{m}_{\text{water}}}\right)^2 + \left(\frac{\delta \Delta T_{\text{water}}}{\Delta T_{\text{water}}}\right)^2}$$
(15)

The error in measuring the mass flow rate for water is $\pm 0.5\%$. The error of the logarithmic mean temperature difference is calculated by the following formula:

$$\frac{\delta \Delta T_{\text{LMTD}}}{\Delta T_{\text{LMTD}}} = \frac{\delta T_{\text{CO}_2,\text{in}} + \delta T_{\text{CO}_2,\text{out}} + \delta T_{\text{water,in}} + \delta T_{\text{water,out}}}{\max(\Delta T_1, \Delta T_2) - \min(\Delta T_1, \Delta T_2)}$$
(16)

The calculation of the CO_2 heat exchange is based on the calculation of the mass flow rate of CO_2 and the enthalpy of inlet and outlet, and its uncertainty is calculated as follows:

$$\left|\frac{\delta Q_{\rm CO_2}}{Q_{\rm CO_2}}\right| = \sqrt{\left(\frac{\delta \dot{m}_{\rm CO_2}}{\dot{m}_{\rm CO_2}}\right)^2 + \left(\frac{|\delta H_{\rm in}| + |\delta H_{\rm out}|}{H_{\rm in} - H_{\rm out}}\right)^2} \tag{17}$$

The mass flow rate error is $\pm 0.2\%$ from a Coriolis mass flowmeter, and the calculation of CO₂ inlet and outlet enthalpy is mainly based on the experimentally measured CO₂ inlet and outlet temperature and pressure. Therefore, the error mainly includes the mass flow rate, temperature, and pressure of inlet and outlet, which is calculated as follows:

$$\frac{\delta H}{H} = \frac{H(T \pm \delta T, P \pm \delta P) - H(T, P)}{H(T, P)}$$
(18)

Under the experimental pressure and temperature range, the error of total heat transferred by CO_2 is within 10%.

3. Results and Discussion

3.1. Effect of Inlet Mass Flux of CO₂ on Heat Transfer

In this section, the effects of CO_2 mass fluxes on heat transfer characteristics are discussed. Figure 8 shows the variation in the total heat transfer coefficient and heat exchange for different mass fluxes of CO_2 in the gas cooler. The mass flow rate of water is 0.175 kg·s⁻¹, and the pressure of CO_2 is 7.9 MPa. The maximum CO_2 mass flow rate is 0.03 kg·s⁻¹. As the CO_2 mass flux increased from 57 kg·m⁻²·s⁻¹ to 182 kg·m⁻²·s⁻¹, the heat exchange and total heat transfer coefficient increased in an essentially linear trend, and the heat exchange increased by 3 kW. With a mass flux of CO_2 of 182 kg·m⁻²·s⁻¹, the total heat transfer coefficient reaches 1570 W·m⁻²·K⁻¹. The total heat transfer coefficient is mainly influenced by the heat transfer coefficient of CO_2 and water. The larger the mass flux of CO_2 , the stronger the turbulence of the fluid in the channel, and the higher the heat transfer coefficient. Increasing the mass flux of CO_2 can significantly improve the total heat transfer coefficient. Increasing the heat transfer coefficient on either side is beneficial to the increase of the total heat transfer coefficient.



Figure 8. Effect of heat exchange and heat transfer coefficient of CO₂ at different mass flux.

3.2. Effect of Placement Style of CO₂ on Heat Transfer

Figure 9 shows the variation in the total heat transfer coefficient of the gas cooler in the case of parallel flow when placed horizontally and vertically. The mass flow rate of water is $0.175 \text{ kg} \cdot \text{s}^{-1}$, and the CO₂ pressure is 7.9 MPa. It can be observed that when placed vertically, the total heat transfer coefficient is greater than in the horizontal placement case because the water affected by gravity accumulates in the lower part of the gas cooler. CO₂ enters the middle of the gas cooler and is in full contact with cooling water, resulting in a higher heat transfer coefficient than in horizontal placement. When placed vertically, high-temperature CO₂ and water flow into the gas cooler at the same time, gravity accelerates the speed of the water flow to remove the heat gained faster, and the cycle continues.



Figure 9. Variation of the heat transfer coefficient of CO₂ at different placement style.

3.3. Effect of Inlet Temperature of Water on Heat Transfer

Figure 10 shows the effect of inlet water temperature on the heat transfer coefficient in the 301~308 K range. The heat exchange of the gas cooler decreases by 1.6 kW. The total heat transfer coefficient shows an increasing trend, indicating that the total heat transfer coefficient can be improved by increasing the inlet water temperature. The main reason is that the temperature reduction of carbon dioxide is greater than the temperature reduction of the inlet water. This is good for maintaining the temperature slippage between CO_2 and water, making the heat exchange between water and CO_2 sufficient. The logarithmic mean temperature difference reduction is greater than the heat exchange reduction, thus improving the total heat transfer coefficient. As the inlet water temperature increases, the total heat transfer coefficient increases from 1489 W·m⁻²·K⁻¹ to 2063 W·m⁻²·K⁻¹, and the CO_2 outlet temperature is far from the critical point, leading to a in heat transfer.



Figure 10. Effect of inlet temperature on heat transfer coefficient of CO₂.

3.4. Supercritical CO₂–Water Experiment

In this section, heat transfer between supercritical CO_2 and cooling water is examined experimentally. The results of heat transfer of CO_2 and water in the spiral plate minichannel gas cooler under different working conditions are presented in Table 4. CO_2 pressure ranges from 7.5 MPa to 8.5 MPa, and water temperature ranges from 26 °C to 31 °C. Based on five supercritical CO_2 correlations of the heat transfer coefficient, as shown in Table 3, a computational procedure for the spiral plate mini-channel gas cooler is developed. In addition, the CO_2 outlet temperature, total length, CO_2 , and water pressure drop are obtained from the calculation, and the comparison between the experimental results and calculation results is discussed.

 Table 4. Experiment conditions.

Case	$G_{\mathbf{co}_2}$ (kg·m ⁻² ·s ⁻¹)	P (MPa)	T _{water,in} (°C)
1	183	8	31
2	162	8	31
3	146	8	31
4	162	7.5	26
5	162	7.5	27
6	183	8.5	31

Figure 11 compares the calculated CO_2 outlet temperature of the program with the experimental results under different conditions. The outlet temperatures calculated from Zhang's correlation show the best agreement with the experimental results among the five correlations. Most errors are within 1 °C. Inagaki's correlation underestimates the CO_2 outlet temperature in all cases and shows larger errors of 3–5 °C. Morimoto's correlation also shows greater errors.



Figure 11. The comparison between predicted $T_{CO_2,out}$ and experimental $T_{CO_2,out}$.

Figure 12 shows the channel lengths calculated by different correlations under different working conditions, and the accuracy of each correlation for engineering calculation can be assessed by comparing the actual length of the spiral plate mini-channel gas cooler with the length calculated by the program. The design length of the existing correlations is longer than the actual length, i.e., 2.2 m. Zhang's and Minton's correlations overestimate the design length under high mass flow rate conditions. Zhang's correlation has the least deviation and Minton's correlation is also acceptable because it accounts for the effect of variable specific heat capacity of CO₂ at different pressures. However, Inagaki's correlation shows the highest discrepancy, indicating that it overestimates the heat exchange between CO₂ and water. Mcadams and Morimoto's correlations yield similar design values for each case, but with different coefficients, and both methods show similarities in predicting rotational flow. All the correlations show a decrease in design values with a decrease in mass flux. Moreover, the prediction errors of all correlations are greater at lower inlet water temperature and higher CO₂ pressure. Inagaki's correlation exhibits an unacceptable prediction error of up to 40% at 8.5 MPa. This is mainly because Inagaki studied a spiral coil heat exchanger rather than a spiral plate heat exchanger. Based on the comprehensive analysis, Zhang's correlation is considered to provide the most accurate results in onedimensional engineering design.



Figure 12. The predicted *l* under different cases.

Figures 13 and 14 illustrate the comparison between predicted and experimental pressure drops under various mass fluxes of CO_2 and water. It is evident that the experimental

pressure drop is lower than predicted due to the lower viscosity of CO_2 at supercritical pressure. The error between predicted and experimental pressure drops on both carbon dioxide and water is small. Maximum error between predicted and experimental carbon dioxide pressure drops is only 4 kPa. The experimental pressure drops on both sides are higher than those of the conventional heat exchanger; therefore, we must consider the balance of heat transfer and pressure drop in the subsequent design.



Figure 13. The comparison between predicted Δp_{CO_2} and experimental Δp_{CO_2} .



Figure 14. The comparison between predicted Δp_{water} and experimental Δp_{water} .

4. Conclusions

In this study, an experimental analysis of the heat transfer between CO_2 and water in the spiral plate mini-channel gas cooler is made. The key findings are outlined as follows:

- (1) Increasing the CO₂ mass flux intensifies the turbulence within the channel, enhances heat transfer, and boosts the heat transfer coefficient of the gas cooler. The heat exchange and the total heat transfer coefficient show an almost linear increase within the range of 57 kg·m⁻²·s⁻¹ to 182 kg·m⁻²·s⁻¹ for the CO₂ mass flux.
- (2) Increasing the inlet water temperature not only results in an improved outlet water temperature, but also enhances heat exchange, thus promoting the total heat transfer coefficient.

- (3) The total heat transfer coefficient is greater when the gas cooler is positioned vertically compared to horizontally placed in the parallel flow.
- (4) Different heat transfer correlations were summarized to evaluate their accuracy when applied to engineering design. Zhang's correlation was found to be more precise, and the calculation methods for pressure drop were summarized. The maximum error in calculating the CO₂ pressure drop was found to be 4 kPa. However, due to the smaller viscosity of CO₂, the calculation error for CO₂ pressure drop was relatively large.

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Nomenclature

LMTD	logarithmic mean temperature difference
Q	heat exchange, kW
m	mass flow rate, kg·s ^{-1}
Н	enthalpy, kJ·kg $^{-1}$
T	temperature, °C
Р	pressure, MPa
U	total heat transfer coefficient, $W \cdot m^{-2} \cdot K^{-1}$
h	enthalpy, kJ·kg $^{-1}$
Α	heat exchange area, m ²
Nu	Nusselt number
Re	Reynolds number
Pr	Prandtl number
d	diameter, mm
Ν	number of spiral turns
L	spiral channel length, m
G	mass flux, kg·m ^{-2} ·s ^{-1}
k	constant
ν	velocity, $m \cdot s^{-1}$
f	friction factor
Greek symbol	
λ	thermal conductivity, $W \cdot m^{-1} \cdot K^{-1}$
μ	dynamic viscosity, Pa·s
ρ	density, kg·m ^{−3}
Subscription	
b	bulk
w	wall
i	inlet
0	outlet

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