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Explicit treatment of hydrogen bonds in the universal force field: Validation and application for metal-organic frameworks, hydrates, and host-guest complexes

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A straightforward means to include explicit hydrogen bonds within the Universal Force Field (UFF) is presented. Instead of treating hydrogen bonds as non-bonded interaction subjected to electrostatic and Lennard-Jones potentials, we introduce an explicit bond with a negligible bond order, thus maintaining the structural integrity of the H-bonded complexes and avoiding the necessity to assign arbitrary charges to the system. The explicit hydrogen bond changes the coordination number of the acceptor site and the approach is thus most suitable for systems with under-coordinated atoms, such as many metal-organic frameworks; however, it also shows an excellent performance for other systems involving a hydrogen-bonded framework. In particular, it is an excellent means for creating starting structures for molecular dynamics and for investigations employing more sophisticated methods. The approach is validated for the hydrogen bonded complexes in the S22 dataset and then employed for a set of metal-organic frameworks from the Computation-Ready Experimental database and several hydrogen bonded crystals including water ice and clathrates. We show that the direct inclusion of hydrogen bonds reduces the maximum error in predicted cell parameters from 66% to only 14%, and the mean unsigned error is similarly reduced from 14% to only 4%. We posit that with the inclusion of hydrogen bonding, the solvent-mediated breathing of frameworks such as MIL-53 is now accessible to rapid UFF calculations, which will further the aim of rapid computational scanning of metal-organic frameworks while providing better starting points for electronic structure calculations. *Published by AIP Publishing.* [<http://dx.doi.org/10.1063/1.4985196>]

I. INTRODUCTION

Metal-Organic Frameworks (MOFs) are now a well-known class of crystalline, porous materials, where inorganic connectors are joined by organic linkers, forming a 3-dimensional network. Since the publication of MOF-5 in 1999,¹ research into MOFs has grown almost exponentially and there are now several thousand synthesised MOFs.² Several reviews have been written on various aspects of MOF chemistry,^{3,4} including their interactions with water.^{5,6}

Water is an important solvent for MOFs, and it serves as a synthetic medium,^{7–9} a structural component,¹⁰ and an adsorbate.¹¹ Water plays a major role in mediating the defects and dissolution of many MOFs.^{12–14} Some MOFs, such as the UiO series, are highly water stable,¹⁵ while others break down or transform^{16–19} when exposed to water. Proposed applications of MOFs include separation of organic contaminants²⁰ and arsenic²¹ from aqueous mixtures and capture of water from air.¹¹

The requirement to computationally scan or screen the nearly infinite number of possible MOFs led to the development of a UFF4MOF.^{22,23} The UFF4MOF extends

the universal force field of Rappe²⁴ to include several atom types present in MOFs but not accounted for in the original list of atom types. The UFF4MOF thus permits the rapid calculation of structures for a wide range of actual and hypothetical MOFs. The structures predicted using the UFF4MOF are typically within 5% of experimental cell parameters, and it is therefore of interest whether a similar accuracy can be maintained when the structural parameters are significantly determined by hydrogen bonding within the framework. MIL-53²⁵ represents a notable case of water not only stabilizing but also determining the framework structure. The transition from (evacuated) a large pore (LP) to a narrow pore (NP) and to hydrated and superhydrated large pores has been extensively studied by both experimental and computational methods.^{26–29} The empty, large pore (LP) structures of MIL-53(M) (M = Cr, Al, Fe) have all been replicated using the UFF4MOF, and in this work, we seek to replicate the hydrated narrow pore (NP) structures, whose cell parameters are dictated by the hydrogen bonds that occur between the guest water molecules and the framework.^{30,31}

Treatment of hydrogen bonds is challenging for classical force fields. On the one hand, the bonds are readily formed and broken in solution so that an explicit, permanent bond would be an inappropriate description if investigating dynamical processes or, for example, the liquid state. Many force fields treat

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hydrogen bonds as non-bonded interactions: the bonding is achieved by attractive components arising from the London dispersion and the Coulomb interaction. In the Universal Force Field (UFF), the former is defined by a Lennard-Jones (LJ) potential, while the latter relies on the definition of charges. As the Coulomb interaction dominates, charge definition is crucial for the results. However, this approach works well for water and is particularly useful in quantum mechanics/molecular mechanics (QM/MM) calculations, as was previously shown in DFTB/UFF calculations with electrostatic embedding.^{32,33}

Several force fields attempt to explicitly treat hydrogen bonds: MM2,³⁴ MM3,³⁵ and Assisted Model Building with Energy Refinement (AMBER) force fields all employ (optionally in the case of AMBER) an angle-independent 10, 12 Lennard-Jones potential to describe nonbonded interactions. MM3 was later updated to include directional hydrogen bonding.³⁶ Paton and Goodman³⁷ reviewed these force fields along with Optimized Potentials for Liquid Simulations (OPLS)*, Optimized Potentials for Liquid Simulations - All Atom (OPLSAA), and MMFF, which do not include explicit hydrogen bonding, and concluded that for the S22 database, the OPLSAA and MMFF force fields performed best, yielding accurate geometries and interaction energies. The same two force fields also ranked highest against the JSCH2005 database, but some optimized geometries differed from the benchmark geometry.

Despite these advances, there generally remains a technical problem. For host-guest systems that are treated entirely using a force field, it is often not practical to define charges to treat the electrostatic interactions. Indeed, although a charge equilibration scheme was designed for use with the UFF,³⁸ the original parameterization was done without an electrostatic model: the implementation is thus open to interpretation. Some codes forego explicit charges completely.^{39,40} The UFF also explicitly includes electrostatic interactions for 1st and 2nd neighbours so that most electrostatics is screened for a bonded system. This, of course, does not hold for non-bonded interactions, where significant electrostatic contributions arise due to the proximity of atoms formally carrying a charge. There is a further, merely technical aspect for the choice of an explicit hydrogen bond that is crucial when studying static hydrogen-bonded frameworks including MOFs, ice, clathrates, or inclusion compounds: upon generation of their starting structure, the non-bonded character in conjunction with substantial forces at initial geometry optimization, or, worse, the kinetic energy gain upon molecular dynamics startup, makes it hard to converge to or to maintain the anticipated local minimum representing the desired framework topology.

II. DEFINITION OF EXPLICIT HYDROGEN BONDS WITHIN THE UNIVERSAL FORCE FIELD

To provide a fast and topology-preserving structure generation method and to avoid the definition of charges in order to account for the Coulomb interaction in the hydrogen bonds, we take advantage of the implicit definition of the electronegativity correction r_{EN} , which is contributing to the UFF natural bond length r_{ij} ,

$$r_{ij} = r_i + r_j + r_{\text{BO}} - r_{\text{EN}}, \quad (1)$$

where r_i and r_j are the bond radii of atoms i and j , respectively, r_{BO} is a bond order correction to the bond distance. The bond order correction, in turn, is defined as

$$r_{\text{BO}} = -\lambda(r_i + r_j) \ln(n), \quad (2)$$

where λ is a proportionality constant derived using propane, propene, and propyne with the C_3, C_2, and C_1 radii and is equal to 0.1332. There is a precedent for assigning unique bond orders for special types of bonds, with the amide bond order set to 1.41 in order to reproduce the C–N bond distance in *N*-methylformamide.²⁴ Assigning a similar bond order for hydrogen bonds requires selecting an appropriate reference. At first glance, this is less than straightforward, given the variety of hydrogen bonds that may be encountered in framework structures. However, considering the prime importance of water to the synthesis, structure, and behaviour of MOFs, a reasonable reference is the prototypical C_s global minimum of the water dimer. We further require that our treatment of hydrogen bonds can reproduce the hydrogen bond mediated breathing that occurs in hydrated MIL-53.

Treating hydrogen bonds as explicit bonds without bond order does have negative consequences: The dynamical breaking and formation of hydrogen bonded networks, essential for the description of the liquid state, become impossible (though it may work if the Reactive Force Field, ReaxFF,⁴¹ was used instead of the UFF). We note that defining an explicit hydrogen bond increases the coordination number of the central atom by one; however, this typically does not pose a problem for otherwise under-coordinated sites, and fully coordinated atoms typically are not hosting extra solvent. Second, because the defined bonding network is changed in the hydrogen-bonded system, it is not possible to calculate binding energies or relative stabilities using this approach. However, for the problem of rapid structural pre-optimization, neither of these disadvantages apply, and furthermore, they are offset by the ability to rapidly produce high quality structures, without requiring the relatively expensive calculation of electrostatic terms.

As we will show below, for “frozen” configurations of hydrogen bonded dimers, our approach performs significantly better than the traditional UFF treatment using nonbonded interactions with Coulomb interactions defined via HF/3-21G charges and should provide a much better starting point for subsequent electronic structure calculations.

The water dimer has been extensively studied over decades, by both experimental^{42,43} and computational^{44–46} means. Earlier calculations yielded a H...O distance of 1.72 Å,⁴⁷ and a subsequent study including some of the same authors yielded a value of 1.80 Å.⁴⁸ By the 1990s, calculations using second order Møller-Plesset (MP2) and Coupled Electron Pair Theory (CEPA-1)⁴⁹ yielded geometries and energies in good agreement with the experiment,^{50,51} and the “gold standard” Coupled Cluster Singles and Doubles with perturbative Triples with a Quadruple Zeta basis set [CCSD(T)/QZ] geometry found in the S22 database⁵² also agrees very well with $R_{\text{H}\cdots\text{O}} = 1.952$ Å (corresponding to $R_{\text{OO}} = 2.91$ Å). If we therefore consider the UFF bond length and bond order correction in Eqs. (1) and (2), we note that λ , r_i , r_j , and r_{EN}

are all fixed within the UFF framework. Therefore, for water, where the oxygen atom has the O₃ atom type and hydrogen has the H₁ atom type, $r_i + r_j = 0.354 + 0.658 = 1.012$ Å, the electronegativity correction for a H–O₃ bond is 0.0021, and thus the required bond order correction is equal to 0.9380 Å. A bond order of 0.001 yields a correction of 0.9312 Å, and noting the diminishing returns of further optimization of such a “bond order,” combined with the large range of acceptable bond lengths for a hydrogen bond, we propose this value as a reasonable approximation to a bond order for describing hydrogen bonds in UFF calculations on metal-organic frameworks. Employing this bond order yields a bond length of 2.025 Å for a H₁···N₃R bond and 1.899 Å for a H₁···O₂ bond, both of which are reasonable lengths for a hydrogen bond.

III. RESULTS AND DISCUSSION

To check the basic sensibility of using a bond order to correct hydrogen bond distances, we undertook geometry optimizations of the hydrogen bonded complexes in the S22 database. The C_{2h} ammonia dimer was excluded from analysis as the angle terms resulting from the addition of the two hydrogen bonds considerably change the geometry of the dimer. The hydrogen bond distances of the other six complexes are shown in Table I and this is the only metric we employ for these non-bonded clusters.⁵³ Calculations were undertaken in the General Utility Lattice Program (GULP)^{54,55} except those employing atomic charges, where deMonNano⁵⁶ was employed. Hartree-Fock (HF) calculations were undertaken in Gaussian 09.⁵⁷

For these simple complexes, the results show reasonable agreement with the *ab initio* reference and are far superior to UFF + Lennard-Jones + electrostatics. The two N₃R–H₁···N₃R bonds are overestimated by approximately 10%, as is the unusually short hydrogen bond in the formic acid dimer. Other bonds are within 6% of their reference values. Undertaking the calculations without the specification of the hydrogen bond results in bond distances increasing by approximately 1 Å which is clearly poor.

We note in Tables I and II that the only failure of the explicit hydrogen-bond approach is the C_{2h} ammonia dimer,

which upon the inclusion of two explicit hydrogen bonds optimizes to a singly hydrogen-bonded complex of the C_s symmetry. In this case, the two hydrogen bonds in the reference structure form H–N₃···H angles of 58°, a significant deviation from the 106.7° angle of the N₃ parameter, and the optimizer prefers to allow a single hydrogen bond with a close-to-ideal angle (i.e., essentially tetrahedral geometry around the acceptor nitrogen atom), rather than two hydrogen bonds with large errors on the angle term. This is a general limitation of this approach, in which by making the hydrogen bond explicit, the coordination number of both the hydrogen atom and the accepting atom is increased by one and the hydrogen bonded atom consequently figures the angle terms around the acceptor atom. In most cases, this effect is either desired or benign, such as in the case of hydrogen bonding to an under-coordinated metal atom in a paddle wheel.

A. Metal-organic frameworks

Having thus established the validity of the approach, a set of framework materials where hydrogen bonding is important for maintaining the structural integrity was selected from the Computation Ready Experimental (CoRE) database.² The original crystal structures were re-sourced from the Cambridge Structural Database⁵⁸ in order to recover the solvent molecules. To this test set we add the particular case of MIL-53(AI) NP.²⁵ After assigning atom types to each structure, we detect hydrogen bonds by looking for hydrogen atoms. For every H atom that is directly connected to (O, S, N), we assign a larger covalent radius (of 2 Å), then with this, we re-build the connectivity list, and we add to the original connectivity list every new bond between these super-big hydrogen atoms and (O, N, S, F, Cl, Br, I), provided that the bond angle is between 140° and 220°. For all structures, we calculate the structure both with and without the specification of hydrogen bonds and note the resultant cell parameters, which are listed in Table II.

In framework systems, the explicit inclusion of hydrogen bonds should yield even a better agreement with the experimental reference structure, as the terms corresponding to regular covalent bonds far outnumber the contribution

TABLE I. Hydrogen bond distances calculated using the UFF for hydrogen bonded complexes in the S22 database.⁵² Percent errors are calculated as $(X_{\text{UFF}} - X_{\text{ref}})/X_{\text{ref}} \times 100$, where X_{UFF} denotes the UFF-predicted value and X_{ref} denotes the original *ab initio* value.

Complex (symmetry)	Hydrogen bond atom types	UFF with HF/3-21G charges	UFF with explicit H-bonds	Reference	% error
(H ₂ O) ₂ (C_s)	O ₃ –H ₁ ···O ₃	2.666	1.920	1.952	–1.7
Ammonia dimer (C_{2h})	N ₃ –H ₁ ···N ₃	2.854	...	2.504	...
Formic acid dimer (C_{2h})	O ₁ –H ₁ ···O ₁	2.488	1.886	1.670	12.9
Formamide dimer (C_{2h})	N ₃ –H ₁ ···O ₁	2.520	1.884	1.840	2.4
Uracil dimer (C_{2h})	N ₃ –H ₁ ···O ₂	2.481	1.882	1.774	6.1
2-pyridoxine-2-aminopyridine (C_1)	N ₃ –H ₁ ···N ₃	2.609	2.030	1.860	9.1
	N ₃ –H ₁ ···O ₁	2.585	1.858	1.874	–0.8
Adenine-thymine WC (C_1)	N ₃ –H ₁ ···N ₃	2.556	2.030	1.819	11.6
	N ₃ –H ₁ ···O ₁	2.477	1.857	1.929	–3.7

TABLE II. Comparison of UFF calculated and experimental cell parameters of selected MOFs. The first 10 structures possess primarily intermolecular hydrogen bonds, and the second 10 structures possess more intramolecular hydrogen bonds. Percent errors are calculated as $(X_{\text{UFF}} - X_{\text{exp}})/X_{\text{exp}} \times 100$, where X_{UFF} denotes the UFF-predicted value and X_{exp} denotes the original value.

CSD refcode	Experimental	UFF without H-bonds	UFF with H-bonds	% error without H-bonds	% error with H-bonds
MIL-53(AI) NP ²⁵	$a = 19.504$	18.593	19.423	-4.7	-0.4
	$b = 15.201$	21.839	15.427	43.7	1.5
	$c = 6.569$	6.366	6.470	-3.1	-1.5
CDLGLU01 ⁵⁹	$a = 11.575$	10.099	11.217	-12.8	-3.1
	$b = 10.764$	15.304	9.920	42.2	-7.8
	$c = 7.256$	7.435	7.775	2.5	7.2
CUGLTM ⁶⁰	$a = 11.084$	13.404	10.989	20.9	-0.9
	$b = 10.350$	11.262	9.412	8.8	-9.1
	$c = 7.238$	6.330	7.246	-12.6	0.1
FUFREE ⁶¹	$a = 7.785$	8.312	7.808	6.8	0.3
	$b = 10.238$	12.172	9.780	18.9	-4.5
	$c = 15.851$	15.524	16.074	-2.1	1.4
HURNOX ⁶²	$a = 7.149$	6.891	6.158	-3.6	-13.9
	$b = 10.468$	14.307	9.573	36.7	-8.5
	$c = 11.295$	10.156	11.518	-10.1	2.0
ICOWON ⁶³	$a = 8.754$	8.240	8.232	-5.9	-6.0
	$b = 10.003$	10.693	9.775	6.9	-2.3
	$c = 11.790$	11.446	11.479	-2.9	-2.6
JUCXEK ⁶⁴	$a = 11.382$	13.971	12.306	22.7	8.1
	$b = 11.382$	14.020	12.509	23.2	9.9
	$c = 11.734$	9.592	10.169	-18.3	-13.3
MAZTIR ⁶⁵	$a = 19.014$	19.839	19.215	4.3	1.1
	$b = 6.843$	9.715	6.782	42.0	-0.9
	$c = 9.420$	9.217	9.753	-2.2	3.5
MEHPAQ ⁶⁶	$a = 7.221$	6.350	7.205	-12.1	-0.2
	$b = 10.295$	11.218	9.948	9.0	-3.4
	$c = 11.041$	13.425	10.966	21.6	-0.7
MUTVUT ⁶⁷	$a = 9.335$	9.255	9.399	-0.9	0.7
	$b = 22.203$	25.664	23.168	15.6	4.3
	$c = 27.514$	26.756	27.710	-2.8	0.7
SALLAT ⁶⁸	$a = 15.686$	12.126	15.023	-22.7	-4.2
	$b = 8.165$	13.522	8.865	65.6	8.6
	$c = 13.119$	12.225	12.767	-6.8	-2.7
DUQSEO ⁶⁹	$a = 8.884$	7.930	7.606	-10.7	-14.4
	$b = 13.093$	11.963	12.266	-8.6	-6.3
	$c = 13.135$	16.660	14.021	26.8	6.7
FAPTUN ⁷⁰	$a = 14.304$	11.704	14.757	-18.2	3.2
	$b = 16.970$	17.091	16.907	0.7	-0.4
	$c = 11.098$	11.342	11.373	2.2	2.5
KOJCUI ⁷¹	$a = 18.326$	21.776	18.356	18.8	0.2
	$b = 25.300$	21.273	24.369	-15.9	-3.7
	$c = 7.524$	6.804	6.900	-9.6	-8.3
RATVEP ⁷²	$a = 7.764$	9.142	8.044	17.8	3.6
	$b = 10.177$	11.938	10.240	17.3	0.6
	$c = 15.949$	15.840	16.222	-0.7	1.7
SARBOE ⁷³	$a = 14.389$	14.925	14.477	3.7	0.6
	$b = 15.475$	14.511	15.006	-6.2	-3.0
	$c = 8.424$	10.610	8.788	26.0	4.3
SIVKAK ⁷⁴	$a = 7.583$	9.243	8.340	21.9	10.0
	$b = 31.086$	27.033	29.315	-13.0	-5.7
	$c = 13.799$	14.199	13.523	2.9	-2.0
VEFLUP ⁷⁵	$a = 8.002$	7.283	7.460	-9.0	-6.8
	$b = 9.091$	10.877	9.031	19.6	-0.7
	$c = 12.935$	13.070	13.071	1.0	1.0

TABLE II. (Continued.)

CSD refcode	Experimental	UFF without H-bonds	UFF with H-bonds	% error without H-bonds	% error with H-bonds
YORZAH ⁷⁶	$a = 16.493$	16.283	16.334	-1.3	-1.0
	$b = 6.820$	7.905	6.597	15.9	-3.3
	$c = 22.220$	23.331	21.906	5.0	-1.4
YUVSUE ⁷⁷	$a = 15.435$	17.188	15.518	11.4	0.5
	$b = 15.435$	17.188	15.793	11.4	2.3
	$c = 22.775$	18.122	21.005	-20.4	-7.8
ZNGLUD ⁷⁸	$a = 11.190$	13.840	12.126	23.7	8.4
	$b = 10.463$	11.273	10.112	7.7	-3.4
	$c = 7.220$	6.369	7.203	-11.8	-0.2
Maximum unsigned error				65.6	14.4
Mean unsigned error				13.9	4.0

due to hydrogen bonds, and this is indeed the case. Without specifying hydrogen bonds, each structure has at least one cell parameter expand by 15% or greater, and the mean unsigned error on all cell parameters is 13.9%. Once hydrogen bonds are specified, the maximum unsigned error in cell parameters is only 14.4% and the mean unsigned error is only 4.0%.

The narrow pore structure of MIL-53(Al) is of particular note. Each pore contains two water molecules which are hydrogen-bonded to the framework oxygen atoms and the hydrogen of the framework hydroxyl group. Optimising the structure with 16 hydrogen bonds specified (two hydrogen bonds per water molecule, see Fig. 1), the cell parameters of MIL-53(Al) are all predicted within 1.5%, including the b dimension, which otherwise expands by over 43% to resemble the large pore structure.

B. Hydrogen-bonded crystal structures

The prediction of the structures of hydrogen-bonded MOFs is perhaps the primary use-case of this approach; however, the structure of any static hydrogen-bonded system is amenable to calculation in this way. To illustrate the broader utility of the approach, a variety of structures where hydrogen bonding is crucial to defining the structure were recalculated.

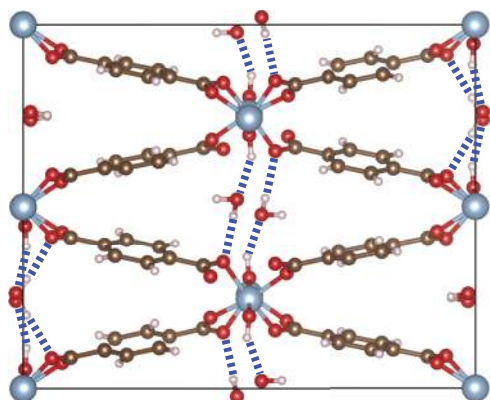


FIG. 1. MIL-53(Al) narrow pore structure (CCSD refcode: SABWAU²⁵) with hydrogen bonds between included water and the framework indicated by dashed blue lines.

Hydrogen bonds were inserted following the literature description of each structure. Table III shows the results for these structures.

1. Methanol

The case of α -methanol⁷⁹ deserves special consideration as it illustrates how the choice of hydrogen bonds affects the optimized structure. There are two distinct types of hydrogen bond in α -methanol; a bond from the hydroxyl hydrogen to the neighbouring oxygen with a $\text{OH} \cdots \text{O}$ distance of 1.75 Å and a $\text{CH} \cdots \text{O}$ distance of 2.51 Å, both illustrated in Fig. 2. Choosing only the strong $\text{OH} \cdots \text{O}$ results in a correct estimate of the a parameter but exchanges the errors on the b and c parameters. Including $\text{CH} \cdots \text{O}$ in addition results in an underestimation of both the b and c parameters and a moderate overestimation of a . While none of the three calculated structures is a clear winner, arguably including only $\text{OH} \cdots \text{O}$ results in the best quality structure. This choice is then consistent with the structure of β -methanol,⁸⁰ the high temperature phase, which possesses only $\text{OH} \cdots \text{O}$ hydrogen bonds. These bonds, arranged in sheets, are crucial to the accurate description of the structure, neglecting them results in a strong distortion of the crystal, with the a parameter being underestimated by 32% and the c parameter being overestimated by 48%.

2. Water ice and hydrate structures

The classic hydrogen-bonded structure is that of water. The approach of fixing hydrogen bonds as actual bonds makes the description of fluxional systems, such as liquid water, impossible. However, the structure of non-fluxional ice is readily amenable to calculation, the structures of both cubic and hexagonal water ice were calculated using all hydrogen bonds, and making each oxygen atom formally tetrahedral with two single bonds and two hydrogen bonds. Employing this approach results in a nearly uniform overestimation of the lattice parameters by 4.5%-7.5% for both structures, a clear improvement over neglecting the hydrogen bonds which results in parameters being over/underestimated by 20%-40%.

The success of the explicit approach to hydrogen bonds in water ice has further significance in describing clathrate structures. Methane hydrates, in particular, are the subject of

TABLE III. Comparison of UFF calculated and experimental cell parameters of selected hydrogen bonded crystals. Percent errors are calculated as $(X_{\text{UFF}} - X_{\text{exp}})/X_{\text{exp}} \times 100$, where X_{UFF} denotes the UFF-predicted value and X_{exp} denotes the original value.

CSD refcode	Experimental	UFF without H-bonds	UFF with H-bonds	% error without H-bonds	% error with H-bonds	
Ic ice ⁹⁰	<i>a</i>	6.358	8.805	6.839	38.5	7.6
	<i>b</i>	6.358	9.019	6.641	41.8	4.5
	<i>c</i>	6.358	9.019	6.641	41.8	4.5
Ih ice ⁹⁰	<i>a</i>	4.506	5.483	4.756	21.7	5.5
	<i>b</i>	4.506	6.284	4.717	39.5	4.7
	<i>c</i>	7.346	5.205	7.776	-29.2	5.9
Alpha methanol ⁷⁹ Figure 2(c)	<i>a</i>	4.873	4.645	4.955	-4.7	1.7
	<i>b</i>	4.641	5.000	4.487	7.7	-3.3
	<i>c</i>	8.867	9.835	7.798	10.9	-12.1
Alpha methanol ⁷⁹ Figure 2(b)				4.876		0.1
				5.178		11.6
				8.592		-3.1
Beta methanol ⁸⁰	<i>a</i>	6.409	4.362	6.702	-31.9	4.6
	<i>b</i>	7.199	7.268	7.099	1.0	-1.4
	<i>c</i>	4.649	6.895	4.554	48.3	-2.0
Ammonia ⁹¹	<i>a</i>	5.138	5.313	4.919	3.4	-4.3
	<i>b</i>	5.138	5.313	4.919	3.4	-4.3
	<i>c</i>	5.138	5.313	4.919	3.4	-4.3
Methane hydrate-I ⁸³	<i>a</i>	11.620	12.181	12.492	4.8	7.5
	<i>b</i>	11.620	16.164	12.490	39.1	7.5
	<i>c</i>	11.620	10.436	12.431	-10.2	7.0
Methane hydrate-II ⁸³	<i>a</i>	11.890	12.262	12.745	3.1	7.2
	<i>b</i>	11.890	11.775	12.723	-1.0	7.0
	<i>c</i>	11.890	15.180	12.712	27.7	6.9
Methane hydrate-H ⁸³	<i>a</i>	11.910	10.826	12.789	-9.1	7.4
	<i>b</i>	11.910	14.074	12.813	18.2	7.6
	<i>c</i>	9.894	11.302	10.456	14.2	5.7
WUVZIW ⁹²	<i>a</i>	7.400	7.393	7.355	-0.1	-0.6
	<i>b</i>	24.448	24.958	25.248	2.1	3.3
	<i>c</i>	14.265	15.399	14.707	8.0	3.1
PgC ₂ cocrystal 5 ⁸⁹	<i>a</i>	10.059	9.642	9.693	-4.1	-3.6
	<i>b</i>	14.556	15.927	13.886	9.4	-4.6
	<i>c</i>	15.558	17.731	14.945	14.0	-3.9
PgC ₄ cocrystal 6 ⁸⁹	<i>a</i>	21.075	23.775	21.334	12.8	1.2
	<i>b</i>	12.796	13.363	12.452	4.4	-2.7
	<i>c</i>	18.229	18.353	17.438	0.7	-4.3
PgC ₄ cocrystal 7 ⁸⁹	<i>a</i>	21.075	23.490	20.088	11.5	-4.7
	<i>b</i>	12.796	13.506	12.380	5.6	-3.2
	<i>c</i>	18.229	18.251	17.118	0.1	-6.1
ABAZOS ⁸⁴	<i>a</i>	16.338	17.022	16.306	4.2	-0.2
	<i>b</i>	21.933	22.805	20.839	4.0	-5.0
	<i>c</i>	16.338	16.870	16.310	3.3	-0.2
ABEBUF ⁸⁷	<i>a</i>	10.722	10.989	10.851	2.5	1.2
	<i>b</i>	10.900	11.831	11.230	8.5	3.0
	<i>c</i>	27.635	25.745	27.648	-6.8	0.0
ABUCIJ ⁸⁶	<i>a</i>	11.281	10.924	11.076	-3.2	-1.8
	<i>b</i>	17.888	18.370	17.973	2.7	0.5
	<i>c</i>	23.950	24.319	23.863	1.5	-0.4
SIYRAU ⁸⁸	<i>a</i>	13.456	13.861	13.257	3.0	-1.5
	<i>b</i>	14.394	13.727	14.647	-4.6	1.8
	<i>c</i>	15.935	18.019	16.945	13.1	6.3
WARWOB ⁸⁵	<i>a</i>	19.297	22.634	20.706	17.3	7.3
	<i>b</i>	4.616	5.599	4.589	21.3	-0.6
	<i>c</i>	8.705	6.954	7.972	-20.1	-8.4
Maximum unsigned error				48.3	12.1	
Mean unsigned error				12.6	4.2	

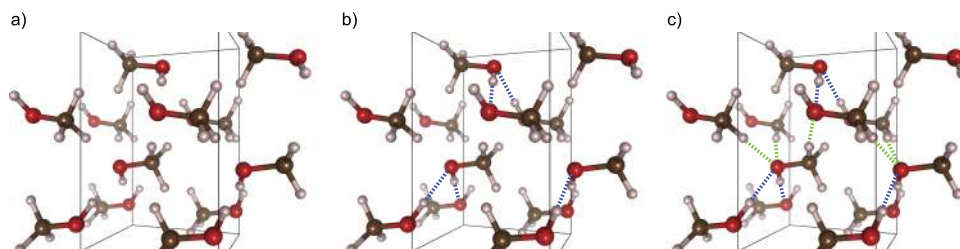


FIG. 2. α -methanol with (a) no explicit hydrogen bonds, (b) explicit O-H \cdots O hydrogen bonds only, and (c) adding C-H \cdots O hydrogen bonds to (b). A single unit cell contains four methanol molecules.

renewed research as, found on the ocean floor and in polar regions, they are estimated to contain up to 12% of all the organic carbon on Earth,⁸¹ making them an important energy resource. In addition, hydrates are often formed within gas pipelines, where they are unwanted and cause significant damage.⁸² The structures of three methane hydrates, MH-I, MH-II, and MH-H (hexagonal),⁸³ were calculated, yielding results broadly similar to those of water ice, whereby the specification of hydrogen bonds gives a structure with cell parameters uniformly overestimated by approximately 7% and neglecting those bonds results in very poor structures with parameters under- and over-estimated by up to 40%. More modest improvement is seen for the structure of *n*-butanol hexahydrate (CCSD refcode WUVZIW).

3. Host-guest inclusion complexes and cocrystals

To further illustrate the diversity of hydrogen-bonded systems to which this simple approach may be applied, structures described as being hydrogen-bonded were sourced from the CCSD.⁵⁸ Structures included two urea-based inclusion compounds (ABAZOS⁸⁴ and WARWOB⁸⁵), a macrocyclic inclusion complex, ABUCIJ,⁸⁶ a porous diamide matrix, ABEBUF,⁸⁷ a Cu coordination compound forming a hydrogen-bonded helicate, SIYRAU⁸⁸ and three cocrystals of pyrogallol⁴ arenes, and the ionic liquid 1-ethyl-3-methylimidazolium ethylsulfate.⁸⁹ In these cases, neglecting hydrogen bonds typically leads to at least one cell parameter in error by greater than 10%. Overall, employing explicit hydrogen bonds reduces the maximum unsigned error for these complexes from 48.3% to 12.1% and the mean unsigned error from 12.6% to 4.2%.

IV. POTENTIAL APPLICATIONS

When used to predict solvent effects, the accuracy of the structures produced by our approach is highly dependant on the guessed positions of the solvent molecules. For the structures where case by case reasoning is impossible, using a genetic algorithm (e.g., as implemented in the Atomic Simulation Environment (ASE)^{93,94}) to maximize the number of hydrogen bonds in the structure of interest can yield reasonable starting points, enabling the use of explicit bonding in automated tasks. An active area of research like water confinement in carbon nanotubes of varying diameters,⁹⁵ where the hydrogen bonding is the single most important factor for structure determination, would likely benefit from cheap, systematic structure elucidation. Appropriate modifications to the ASE code are underway to allow for solvent rigid motions

during optimizations, and a proof of the concept script is available on github (<https://github.com/DCoupry/GenAlGHbond>). However, the main application of explicit hydrogen bonding is case-by-case reasoning for a reasonable pre-optimization, followed by electronic structure methods. More complex properties of the structures, like frequencies (for which the UFF was not parameterized) or the effects of H-bond anisotropy, fall squarely outside of the scope of this paper.

V. CONCLUSIONS

We report a simple approach to explicitly treat hydrogen bonds within the universal force field. The approach does not require any definition of atomic charges, which is a great technical (codes such as GULP and Amsterdam Density Functional (ADF) do not include long-range and non-bonded electrostatic interactions within the UFF) and practical (the definition of atomic charges is not well-defined) advantage. Moreover, it avoids the computationally costly electrostatic interaction term and is equally applicable for periodic and non-periodic systems.

The specification of hydrogen bonds with a negligible (0.001) bond order increases the coordination number of the acceptor site by one, which is compatible with the definition of the main acceptor sites O and N, as well as with under-coordinated metal sites as present in metal-organic frameworks.

The approach was validated for the hydrogen bonded complexes in the S22 database. We show that it is very effective for both framework-framework hydrogen bonds and, importantly, for framework-adsorbate bonds. Using this approach, both the large pore and narrow pore structures of MIL-53 can be calculated accurately with the UFF. We show the generality of the approach by also applying it to hydrogen bonded crystal structures and host-guest inclusion complexes, including the environmentally and commercially important clathrates.

Finally, we note that this approach does not require any implementation and thus works in any software that includes a UFF implementation. We propose this method to be most useful for pre-optimization and screening of static hydrogen-bonded systems.

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