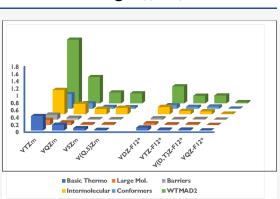
Explicitly Correlated Double-Hybrid DFT: A Comprehensive Analysis of the Basis Set Convergence on the GMTKN55 Database

Nisha Mehta and Jan M. L. Martin*

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ABSTRACT: Double-hybrid density functional theory (DHDFT) offers a pathway to accuracy approaching composite wavefunction approaches such as G4 theory. However, the Görling–Levy second-order perturbation theory (GLPT2) term causes them to partially inherit the slow $\propto L^{-3}$ (with L the maximum angular momentum) basis set convergence of correlated wavefunction methods. This could potentially be remedied by introducing F12 explicit correlation: we investigate the basis set convergence of both DHDFT and DHDFT-F12 (where GLPT2 is replaced by GLPT2-F12) for the large and chemically diverse general main-group thermochemistry, kinetics, and noncovalent interactions (GMTKN55) benchmark suite. The B2GP-PLYP-D3(BJ) and revDSD-PBEP86-D4 DHDFs are investigated as test cases, together with orbital basis sets as large as aug-cc-pV5Z and F12 basis sets as large as cc-pVQZ-F12. We show that F12 greatly accelerates



basis set convergence of DHDFs, to the point that even the modest cc-pVDZ-F12 basis set is closer to the basis set limit than ccpV(Q+d)Z or def2-QZVPPD in orbital-based approaches, and in fact comparable in quality to cc-pV(5+d)Z. Somewhat surprisingly, aug-cc-pVDZ-F12 is not required even for the anionic subsets. In conclusion, DHDF-F12/VDZ-F12 eliminates concerns about basis set convergence in both the development and applications of double-hybrid functionals. Mass storage and I/O bottlenecks for larger systems can be circumvented by localized pair natural orbital approximations, which also exhibit much gentler system size scaling.

1. INTRODUCTION

The two most common methodologies in computational chemistry are wavefunction ab initio methods¹ and density functional theory (DFT).^{2,3} Although (correlated) wavefunction ab initio methods provide a clear road map for the convergence to the exact solution, they suffer from slow basis set convergence and hence they are only practical for small molecules. The alternative solution to the quantum many problems is given by DFT, thanks to Hohenberg-Kohn² and Kohn-Sham theorems,³ DFT currently provides the best costaccuracy ratio for main-group thermochemistry, kinetics, and noncovalent interactions. Among various density functional theory approximations, double-hybrid density functionals (DHDFs) stand out for their general applicability, reliability, and robustness.⁴⁻¹³ In DHDFs, a portion of semilocal DFT exchange and correlation are replaced by non-local Fock exchange and second-order Görling-Levy perturbation theory¹⁴ (GLPT2) type correlation contributions, respectively. (An earlier usage^{15,16} of the term "double hybrid" referred to the combination of semilocal DFT for short-range correlation with regular MP2 correlation in a HF orbital basis for longrange correlation; see also the work of the late Angyán¹⁷ on range-separated correlation. For a detailed numerical analysis of the benefits of GLPT2 over HF-MP2 correlation, see ref 18). DHDFs offer^{8,19} a level of agreement approaching

composite wavefunction theory schemes such as G3 and G4 theories. $^{\rm 20-22}$

Hybrid DFT functionals (rung four on "Jacob's Ladder"²³) exhibit basis set convergence resembling that of Hartree–Fock theory. Double hybrids (rung five on "Jacob's Ladder") contain a GLPT2 part, the basis set convergence of which is similar to the well-known asymptotic $\propto L^{-3}$ (with L the highest angular momentum in the basis set) behavior of MP2²⁴ and of electron correlation methods more broadly.²⁵

Thus, double hybrids inherit the slow basis set convergence of MP2, although the problem is not as severe as in MP2 itself owing to the scale factors of the GLPT2 correlation (e.g., 0.25 for B2PLYP,⁴ 0.36 for B2GP-PLYP²⁶). Additionally, the computational cost can be greatly mitigated by introducing density fitting in the MP2 part,^{27,28} and two-point basis set extrapolation (e.g., refs 29–31 and references therein) can be applied.

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The greatest stumbling block for basis set convergence in MP2 and GLPT2 alike is the need to model the interelectronic correlation cusp, which explicitly depends on r_{12} , in terms of products of orbitals in r_1 and r_2 . In explicitly correlated approaches (see refs 32-34 for reviews), functions of r_{12} (so-called geminals) are added to the calculation to ensure that the cusp is well-described at short range, "freeing up" the orbital basis set, as it were, to cover other correlation effects.

Kutzelnigg and Morgan²⁵ showed that for two-electron model systems, the singlet-coupled pair correlation energy converges as $\propto L^{-7}$, compared to $\propto L^{-3}$ for pure orbital calculations.

Initial studies (e.g., refs 35 and 36) featured a simple R12 geminal. In the last decade and a half, the F12 geminal³⁷ (1 – exp γr_{12})/ γ has become the de facto standard. Meanwhile, the computational cost barrier resulting from the need for threeand four-electron integrals^{38–40} was circumvented through the introduction of auxiliary basis sets and density fitting.^{41–43}

Meanwhile, MP2-F12 and various approximations to CCSD(T)-F12 have become a mainstream tool in high-accuracy wavefunction methods: see, for example, refs 44–46 and from the Weizmann group, refs 47–49 in small-molecule thermochemistry, and refs 50–53 in noncovalent interactions.

It stands to reason that MP2-F12 in a basis of Kohn–Sham orbitals might be a way through the basis set convergence bottleneck of double-hybrid DFT. Karton and Martin⁵⁴ showed that this might be the case for a rather small set of closed-shell reactions, but to our knowledge, this has never been verified for a large and chemically diverse benchmark suite such as GMTKN55 (general main-group thermochemistry, kinetics, and noncovalent interactions,⁶ 55 problem types) or the Head-Gordon group's even larger main-group chemistry database (MGCDB84⁵⁵). GMTKN55 has previously been used for both evaluation and parametrization of DHDFs as well as composite wavefunction methods.^{6,8–10,56–58}

We will show below that for DHDFs applied to GMTKN55, F12 accelerates basis set convergence to the point that even spd basis sets are quite close to the complete basis set limit, and that spdf basis sets effectively reach it.

2. COMPUTATIONAL DETAILS

We assess the basis set convergence of conventional and explicitly correlated DHDFs using the GMTKN55 database for general main-group thermochemistry, kinetics, and noncovalent interactions. GMTKN55 consists of 2462 total single point calculations, which are distributed over 55 subsets. The latter are divided into five categories. The first category (basic properties and reaction energies of small systems) addresses problems associated with reaction energies for small systems, total atomization energies, ionization potentials, electron affinities, and self-interaction error. The second category covers problems related to reaction energies of large systems and isomerization. The third category consists of barrier height-related problems. Intermolecular noncovalent interactions related problems are covered in the third category, while conformer equilibria (driven by intramolecular noncovalent interactions) make up the fourth category. The respective abbreviations for the five categories are "Thermo", "Large", "Barrier", "Intermol", and "Conf". Table 1 provides a summary of GMTKN55.

We used the weighted total mean absolute deviation, type 2 (WTMAD2)—originally defined in eq 2 of ref 6—as our primary metric.

Table 1. Overview of the GMTKN55 Database and Its Five Categories: Basic Properties and Reactions of Small Systems ("Thermo"), Reaction Energies of Larger Systems and Isomerization ("Large"), Barrier Heights ("Barrier"), Intermolecular Noncovalent Interactions ("Intermol"), and Intramolecular Noncovalent Interactions ("Conf")^a

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Category	names of constituent benchmark sets	references
Thermo	W4-11, G21EA, G21IP, DIPCS10, PA26, SIE4x4, ALKBDE10, YBDE18, AL2X6, HEAVYSB11, NBPRC, ALK8, RC21, G2RC, BH76RC, FH51, TAUT15, DC13	6,59-82
Large	MB16-43, DARC, RSE43, BSR36, CDIE20, ISO34, ISOL24, C60ISO, PArel	6,65,83-89
Barrier	BH76, BHPERI, BHDIV10, INV24, BHROT27, PX13, WCPT18	6,68,69,82,90–96
Intermol	RG18, ADIM6, S22, S66, HEAVY28, WATER27, CARBHB12, PNICO23, HAL59, AHB21, CHB6, IL16	97–106
Conf	IDISP, ICONF, ACONF, AMINO20x4, PCONF21, MCONF, SCONF, UPU23, BUT14DIOL	6,67,82,87,107-116
a Ear more	datails san raf 6	

^aFor more details, see ref 6.

WTMAD2 =
$$\frac{1}{\sum_{i=1}^{55} N_i} \sum_{i=1}^{55} N_i \frac{56.85 \text{ kcal/mol}}{|\overline{\Delta E_i}|} \text{MAD}_i$$
 (1)

where N_i represents the number of systems in each subset, $|\overline{\Delta E_i}|$ is the mean absolute value of all the reference energies for i = 1 to 55, and MAD_i is the mean absolute deviations of the calculated and reference energies for each subset of GMTKN55.

All electronic structure calculations were performed using the MOLPRO2022 package¹¹⁷ on the ChemFarm HPC cluster of the Faculty of Chemistry at the Weizmann Institute of Science. The B2GP-PLYP 26 -D3(BJ) 118 and revDSD-PBEP86-D4⁸ double hybrids were investigated as test cases. The dispersion model for B2GP-PLYP considered here was DFT-D3 of Grimme et al.⁹⁷ with the Becke–Johnson damping function.¹¹⁹ We used the B2GP-PLYP-D3(BJ)²⁶ dispersion parametrization $s_6 = 0.560$, $s_8 = 0.2597$, $a_1 = 0.000$, and $a_2 =$ 6.3332 from ref 118. For revDSD-PBEP86,⁸ we used the DFT-D4 dispersion correction of Grimme et al.^{120,121} with the parameters $s_6 = 0.5132$, $s_8 = 0.000$, $a_1 = 0.4400$, $a_2 = 3.60$, and $s_9 = 0.5132$ from ref 8. As per the DFT-D4 defaults, we used electronegativity equalization¹²² partial charges and the 3-body Axilrod-Teller-Muto correction term. DFT-D3 and DFT-D4 type dispersion corrections were obtained with the respective standalone programs by Grimme and co-workers.^{123,12}

Whenever possible, all of the KS, MP2, and MP2-F12 steps were carried out with density fitting (DF-KS, DF-MP2, and DF-MP2-F12 approximations). We employed the OptRI auxiliary basis set¹²⁵ within the complementary auxiliary basis set approach,¹²⁶ the JKFIT basis sets of Weigend¹²⁷ for the DF-KS calculations, and the MP2FIT set of Hättig and co-workers^{128,129} for the DF-MP2/DF-MP2-F12 steps. Through-out the manuscript, DHDF-F12 refers to the double-hybrid calculations with the MP2-F12 (or DF-MP2-F12) method, whereas DHDF refers to the orbital-only (i.e., non-F12) double-hybrid calculations. In all of the DHDF-F12 calculations, the default fixed-amplitude "3C(FIX)" approximation was employed. All self-consistent-field energies were corrected with the complementary auxiliary basis set (CABS) singles correction. Energy convergence criteria for the KS calculations

WTMAD HENO MARIERS JAKGE CONF MTERMOL FARENCO MARIERS JAKGE CONF MTERMOL U22 1394 1230 0.874 1049 4.100 2.53 (N17) 2.549 0.531 0.631 0.733 U22 5.649 1.040 4.100 2.530 (V17) 2.549 0.531 0.660 0.69 0.69 0.751				B2GP-PLYP-D3(BJ)	D3(BJ)					B2GP-PL	B2GP-PLYP-F12-D3(BJ)			
UNZ 11904 2.015 0.064 100 4160 3.256 AVUZF12 3.011 0.581 0.331 0.600 0.01 VIZ 5.332 1.333 0.677 1.096 1.495 0.593 0.334 0.600 0.01 VIZ 5.342 1.333 0.677 1.096 1.495 0.593 0.334 0.600 0.01 VIZ 5.349 1.022 0.535 0.635 1.405 1.405 1.405 0.536 0.334 0.600 0.01 VIZ 3.347 0.646 0.389 0.694 1.061 1.405 1.415 VIZ 2.393 0.581 0.314 0.665 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.55 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53 0.53		WTMAD2	THERMO	BARRIERS	LARGE	CONF	INTERMOL		WTMAD2	THERMO	BARRIERS	LARGE	CONF	INTERMOL
UD2* 0601 1030 0607 1000 1400 1503 VUZE112 2333 0.583 0.344 0.600 0.01 VTZ* 549 1033 0.667 1000 1493 1383 VUZE112 2393 0.583 0.344 0.600 0.01 VTZ* 5495 0.666 0.339 0.667 1.033 0.667 1.333 0.533	VDZ	11.904	2.205	0.964	1.049	4.160	3.526	AVDZ-F12	3.011	0.581	0.333	0.680	0.623	0.793
VD2* 6.33 1.33 0.67 1.00 1.89 VIX2+11* 2.999 0.584 0.314 0.660 0.014 VTZ* 5.669 1.063 0.583 0.688 1.403 1.50 VTZ+11* 2.999 0.584 0.311 0.653 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533 0.545 0.533<	VDZ*	9.661	1.323	0.627	1.049	4.160	2.503	VDZ-F12	2.953	0.585	0.334	0.660	0.619	0.756
VTZ 5640 1062 0533 0686 1405 1356 VTZ-F12 2.979 0.544 0.331 0.662 0.333 VTZ* 3447 0.666 0.389 0.684 1.365 VTZ-F12 2.979 0.541 0.645 0.533 0.633 0.634 0.666 0.339 0.666 0.339 0.666 0.339 0.666 0.336 0.666 0.336 0.669 0.669 0.760 1.113 VQZF12* 2.903 0.331 0.665 0.337 0.666 0.337 0.666 0.336 0.673 1.113 VQZF12* 2.903 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337 0.666 0.337	VDZ^m	6.332	1.323	0.627	1.002	1.498	1.883	VDZ-F12*	2.939	0.580	0.334	0.660	0.619	0.747
VTZ* 449 0.646 0.339 0.698 1405 1.356 VTZ* 2.969 0.531 0.631 0.663 0.533 0.631 0.663 0.533 0.63	VTZ	5.649	1.062	0.553	0.698	1.405	1.930	VTZ-F12	2.979	0.584	0.331	0.652	0.587	0.825
VIZ" 347 0666 0.39 0644 1064 V(D)T[Z=F12 3.005 0.582 0.344 0.665 0.685 0.685 0.685 0.685 0.685 0.685 0.685 0.685 0.685 0.685 0.685 0.685 0.686 0.690 V(D)T[Z=F12.* 2.093 0.330 0.665 0.58 0.685 <th0.685< th=""> <th0.685< th=""> 0.685</th0.685<></th0.685<>	VTZ^*	4.495	0.646	0.389	0.698	1.405	1.356	VTZ-F12*	2.969	0.582	0.331	0.652	0.587	0.817
QQZ 3978 0761 0445 0.539 0.700 1374 V(D:TZ:F1.* 2.993 0.531 0.645 <th< td=""><td>VTZ^m</td><td>3.427</td><td>0.646</td><td>0.389</td><td>0.694</td><td>0.634</td><td>1.064</td><td>V{D,T}Z-F12</td><td>3.005</td><td>0.582</td><td>0.334</td><td>0.645</td><td>0.585</td><td>0.860</td></th<>	VTZ^m	3.427	0.646	0.389	0.694	0.634	1.064	V{D,T}Z-F12	3.005	0.582	0.334	0.645	0.585	0.860
VQ2* 3417 0.538 0.348 0.659 0.700 1113 VQ2F12* 3007 0.591 0.330 0.667 0.53 VCQ* 3131 0.538 0.448 0.653 0.673 1.472 3014 0.599 0.347 0.667 0.58 0.633 0.673 0.53 0.673 1.472 3015 0.592 0.330 0.669 0.58 0.57 0.591 0.327 0.666 0.58 0.58 0.591 0.327 0.669 0.58 0.58 0.591 0.591 0.327 0.669 0.58 0.591 0.591 0.327 0.669 0.58 0.591 <	ZOV	3.978	0.761	0.445	0.639	0.760	1.374	V{D,T}Z-F12*	2.993	0.581	0.333	0.645	0.585	0.849
VQZ" 3131 0538 0348 0646 0.590 0990 VQZF12* 3.04 0.589 0.337 0.666 0.581 V[T,QZ" 3351 0533 0633 0673 1.472 V[T,Q]Z+F12 3.016 0.391 0.337 0.669 0.583 V[T,QZ" 3351 0533 0633 0537 0.573 0.593 0.337 0.669 0.583 V[SZ" 3004 0573 0.333 0.603 0.593 0.593 0.593 0.593 0.584 0.583 0.583 0.583 0.583 0.583 0.583 0.583 0.583 0.584 0.584 0.584 0.584 0.584 0.584 0.584	vQZ*	3.417	0.558	0.348	0.639	0.760	1.113	VQZ-F12	3.007	0.591	0.330	0.667	0.585	0.833
V(T,Q)Z 3955 0.738 0.448 0.625 0.673 1.472 V(T,Q)Z+R12,8 3.015 0.339 0.339 0.669 0.583 V(T,Q)Z* 3.341 0.933 0.333 0.629 0.637 1.277 V(T,Q)Z+R12,8 3.016 0.391 0.337 0.669 0.689 0.683 0.581<	VQZ ^m	3.131	0.558	0.348	0.646	0.590	066.0	VQZ-F12*	3.004	0.589	0.327	0.666	0.584	0.838
V(T,Q)2*3.5210.5930.5330.6250.6731.277V(T,Q)2.F12*3.0160.3910.3270.6680.603V(T,Q)2*3.300.5330.3330.6030.6090.8851.1790.9110.3210.6610.685V(Q,S)2*3.1050.5330.3280.6610.6090.8850.9300.9300.8910.861 <td>V{T,Q}Z</td> <td>3.955</td> <td>0.738</td> <td>0.448</td> <td>0.625</td> <td>0.673</td> <td>1.472</td> <td>V{T,Q}Z-F12</td> <td>3.015</td> <td>0.592</td> <td>0.330</td> <td>0.669</td> <td>0.585</td> <td>0.839</td>	V{T,Q}Z	3.955	0.738	0.448	0.625	0.673	1.472	V{T,Q}Z-F12	3.015	0.592	0.330	0.669	0.585	0.839
V(T,Q)Z ^m 3331 0.593 0.333 0.639 0.597 1.179 V3Z* 3.04 0.573 0.328 0.660 0.584 0.885 V(Q,S)Z* 3.030 0.573 0.328 0.661 0.584 0.885 V(Q,S)Z* 3.105 0.589 0.326 0.666 0.597 0.937 V(Q,S)Z* 3.115 0.589 0.326 0.660 0.597 0.937 V(Q,S)Z* 3.115 0.589 0.326 0.660 0.597 0.937 V(Q,S)Z* 3.115 0.589 0.326 0.660 0.393 0.890 deD.TZVPP* 3.142 0.660 0.342 0.633 0.890 0.833 deD.TZVPP* 3.167 0.667 0.333 0.890 0.833 deD.ZVPP* 3.167 0.667 0.333 0.891 0.833 deD.ZVPP* 3.17 0.653 0.341 0.843 0.641 deD.ZVPP* 3.17 0.653 0.342<	V{T,Q}z*	3.521	0.593	0.353	0.625	0.673	1.277	V{T,Q}Z-F12*	3.016	0.591	0.327	0.668	0.583	0.847
VSZ* 3.054 0.573 0.328 0.660 0.690 0.885 VSZ* 3.020 0.573 0.328 0.661 0.593 0.930 VG_5)Z* 3.105 0.879 0.326 0.666 0.597 0.930 V(Q.5)Z* 3.115 0.839 0.326 0.666 0.597 0.930 V(Q.5)Z* 3.115 0.839 0.326 0.666 0.597 0.937 de2-TZVPP* 3.412 0.660 0.342 0.633 0.890 0.883 de2-TZVPP* 3.157 0.660 0.342 0.633 0.890 0.883 de2-TZVPP* 3.167 0.660 0.342 0.633 0.890 0.883 de2-QZVPP 3.167 0.663 0.849 0.833 0.890 0.883 de2-QZVPP 3.167 0.663 0.840 0.833 0.890 0.883 de2-QZVPP 3.167 0.663 0.840 0.833 0.842 0.843 de2-QZVPP<	$V{T,Q}Z^{m}$	3.351	0.593	0.353	0.629	0.597	1.179							
VSZ" 3200 0573 0.328 0.661 0.584 0.874 V(Q.S)Z* 3.105 0.589 0.326 0.668 0.393 0.930 V(Q.S)Z* 3.115 0.589 0.326 0.668 0.397 0.931 dd:D.TZVPP 3.115 0.589 0.326 0.666 0.397 0.331 dd:D.TZVPP* 3.112 0.689 0.342 0.633 0.890 1.166 dd:D.TZVPP* 3.142 0.660 0.342 0.633 0.890 0.383 dd:D.TZVPP* 3.157 0.660 0.342 0.633 0.890 0.383 dd:D.TZVPP* 3.157 0.660 0.342 0.633 0.890 0.883 dd:D.QZVPP* 3.157 0.653 0.643 0.624 0.833 dd:D.QZVPP* 3.157 0.653 0.653 0.893 0.833 dd:D.GZVPP* 3.177 0.532 0.643 0.654 0.843 dd:D.QZVPP* 3.177 0.531	V5Z*	3.054	0.573	0.328	0.660	0.609	0.885							
V(Q_5)Z* 3.105 0.589 0.326 0.668 0.593 0.930 v(Q_5)Z** 3.115 0.589 0.326 0.666 0.597 0.937 deD_TZVPP* 3.115 0.680 0.332 0.830 11.166 deD_TZVPP* 3.412 0.660 0.342 0.633 0.830 11.66 deD_TZVPP* 3.162 0.660 0.342 0.633 0.830 0.888 deD_TZVPP* 3.167 0.660 0.342 0.633 0.800 0.883 deD_TZVPP* 3.167 0.660 0.342 0.633 0.800 0.883 deD_QZVP* 3.167 0.653 0.643 0.634 0.833 0.800 deD_QZVPP* 3.07 0.591 0.322 0.643 0.634 0.833 deD_QZVPP* 3.07 0.591 0.322 0.643 0.834 0.833 deD_QZVPP 3.17 0.653 0.393 0.833 0.803 0.803 deD_CTQXPP*	VSZ^m	3.020	0.573	0.328	0.661	0.584	0.874							
V(Q_5)Z ^m 3.115 0.589 0.326 0.666 0.342 0.633 0.890 1.166 deD-TZVPP 3.412 0.660 0.342 0.633 0.890 1.166 deD-TZVPP 3.162 0.660 0.342 0.633 0.890 0.188 deD-TZVPP 3.162 0.660 0.342 0.633 0.890 0.888 deD-TZVPP 3.167 0.663 0.342 0.633 0.890 0.888 deD-TZVPP 3.157 0.663 0.333 0.582 0.600 0.342 deD-TZVPP 3.167 0.653 0.643 0.624 0.828 deD-QXVPP 3.366 0.593 0.643 0.624 0.828 deD-QXVPP 3.366 0.593 0.644 0.828 0.644 deD-QXVPP 3.366 0.593 0.643 0.624 0.828 deD-QXVPP 3.37 0.651 0.593 0.593 0.664 0.863 deD-T_TQVP 3.17	V{Q.5}Z*	3.105	0.589	0.326	0.668	0.593	0.930							
def2.TZVPP 3966 0.834 0.443 0.633 0.890 1166 def2.TZVP* 3.412 0.660 0.342 0.633 0.890 0.888 def2.TZVPP* 3.162 0.660 0.342 0.633 0.890 0.888 def2.TZVPP* 3.167 0.660 0.342 0.639 0.689 0.883 def2.TZVPP* 3.167 0.657 0.333 0.582 0.689 0.883 def2.QZVPP 3.267 0.653 0.643 0.644 0.828 def2.QZVPP 3.267 0.591 0.522 0.643 0.624 0.833 def2.QZVPP 3.307 0.591 0.322 0.643 0.624 0.833 def2.QZVPP 3.367 0.531 0.532 0.643 0.624 0.833 def2.QZVPP 3.367 0.531 0.371 0.654 0.833 def2.QZVPP 3.367 0.531 0.57 0.593 0.303 def2.QZVPP 3.17 0.623 </td <td>$V{Q_5}Z^m$</td> <td>3.115</td> <td>0.589</td> <td>0.326</td> <td>0.666</td> <td>0.597</td> <td>0.937</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>	$V{Q_5}Z^m$	3.115	0.589	0.326	0.666	0.597	0.937							
def2_TZVPP*3.1120.6600.3420.6330.8900.888def2_TZVPP3.1620.6600.3420.6390.6890.833def2_TZVPPD3.1570.6570.3330.5820.6850.900def2_QZVPP3.3670.6530.3440.6430.6240.984def2_QZVPP3.070.5910.3220.6430.6240.833def2_QZVPP3.070.5910.3220.6430.6240.894def2_QZVPP3.070.5910.3220.6430.6340.835def2_QZVPP3.3260.5910.3220.6450.5920.803def2_TQJZVPP3.3260.6510.3710.6570.59810.50def2_TQJZVPP3.1170.6230.3290.6570.5980.969def2_TQJZVPP3.1110.6230.3210.6120.966def2_TQJZVPP3.1110.6230.3230.5911.539VDZ_F125.8330.8800.3230.9161.5392.225VDZ*f125.8330.8800.3230.9161.5392.225VDZ*f125.8330.8800.3230.9161.5392.225VDZ*f125.8330.8800.3230.9161.5392.225VDZ*f125.8330.9161.5392.2255.8455.545VDZ*f125.8330.9161.5392.2255.8455.225VDZ*f25.8410.7610.733	def2-TZVPP	3.966	0.834	0.443	0.633	0.890	1.166							
def2_TZVPP"3.1620.6600.3420.6390.6890.833def2_TZVPPD3.1570.6570.3330.5820.6850.900def2_QZVPP*3.1570.6530.3640.6430.6240.984def2_QZVPP*3.0070.5910.3220.6430.6240.828def2_QZVPP2.9550.5910.3220.6450.5920.803def2_QZVPP2.9650.5910.3220.6450.5920.803def2_TQ_ZVPP3.3260.6510.3710.6570.5980.659def2_TQ_ZVPP3.1770.6230.3290.6570.5980.969def2_TQ_ZVPP3.1110.6230.3290.6570.6120.965def2_TQ_ZVPPM3.1110.6230.3210.6500.8940.894VDZ_FI25.8830.8800.3230.9161.5392.225VDZ_F125.8830.8800.3230.9161.5392.225VDZ*F125.8830.8800.3230.9161.5392.225VDZ*F125.8830.8800.3230.9161.5392.225VDZ*F125.8830.8121, ATHE21, ATTER27, BH76, and BH76RC. In the "VnZ"" variant, we additionally treated the BUT14D10, S22, S66, S	def2-TZVPP*	3.412	0.660	0.342	0.633	0.890	0.888							
def2-TZVPPD3.1570.6570.3330.5820.6850.900def2-QZVPP3.2670.6530.5340.6430.6240.84def2-QZVPP3.0070.5910.3220.6430.6240.828def2-QZVPPD2.9650.5910.3220.6450.5920.803def2-(T,Q)ZVPP3.3260.5910.3220.6450.5920.803def2-(T,Q)ZVPP3.1770.6510.3180.5981.050def2-(T,Q)ZVPP3.1770.6230.3290.5981.050def2-(T,Q)ZVPP3.1110.6230.3290.6120.969def2-(T,Q)ZVPP3.1110.6230.3290.6120.969def2-(T,Q)ZVPP3.1110.6230.3210.6100.969def2-(T,Q)ZVPP3.1110.6230.3230.6120.969def2-(T,Q)ZVPP3.1110.6230.3230.6120.969def2-(T,Q)ZVPP3.1110.6230.3230.6120.969def2-(T,Q)ZVPP3.1110.6230.3230.6120.969VDZ-FI25.8330.8800.3230.9161.5392.225def2-(T,Q)ZVPP5.830.8060.8842.325VDZ*: AVnZ was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76, and BH76RC. In the "VnZ"" variant, we additionally treated the BU714DDL, S22, S66, S	def2-TZVPP‴	3.162	0.660	0.342	0.639	0.689	0.833							
def2_QZVPP 3.267 0.653 0.344 0.643 0.624 0.984 def2_QZVPP* 3.007 0.591 0.322 0.643 0.624 0.828 def2_QZVPP" 3.007 0.591 0.322 0.645 0.592 0.803 def2_QZVPP" 2.965 0.591 0.322 0.645 0.592 0.803 def2_QZVPP 2.965 0.595 0.318 0.653 0.598 0.803 def2_TQJZVPP 3.326 0.651 0.371 0.657 0.598 0.969 def2_TQJZVPP" 3.117 0.623 0.329 0.6612 0.969 def2_TQJZVPP" 3.118 0.623 0.329 0.657 0.598 0.969 def2_TQJZVPP" 3.111 0.623 0.329 0.660 0.869 0.966 def2_TQJZVPP" 3.111 0.623 0.323 0.612 0.966 def2_TQJZVPP" 3.111 0.623 0.323 0.516 1.539 VDZ_FI12 5.883	def2-TZVPPD	3.157	0.657	0.333	0.582	0.685	0.900							
def2-QZVPP* 3.007 0.591 0.322 0.643 0.624 0.828 def2-QZVPP" 2.953 0.591 0.322 0.645 0.592 0.803 def2-QZVPPD 2.965 0.591 0.322 0.645 0.592 0.803 def2-QZVPPD 2.965 0.591 0.321 0.650 0.584 0.837 def2-(T,Q)ZVPP 3.326 0.651 0.371 0.657 0.598 1.050 def2-(T,Q)ZVPP 3.177 0.623 0.329 0.657 0.598 0.969 def2-(T,Q)ZVPP 3.111 0.623 0.329 0.657 0.598 0.969 def2-(T,Q)ZVPP 3.111 0.623 0.329 0.660 0.969 def2-(T,Q)ZVPP 3.111 0.623 0.323 0.916 1.539 2.225 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225	def2-QZVPP	3.267	0.653	0.364	0.643	0.624	0.984							
def2-QZVPP ^m 2.953 0.591 0.322 0.645 0.892 0.803 def2-QZVPPD 2.965 0.595 0.318 0.630 0.584 0.837 def2-QTVPPD 2.965 0.595 0.318 0.657 0.598 0.837 def2-(T,Q]ZVPP 3.177 0.651 0.371 0.657 0.598 1.050 def2-(T,Q]ZVPP ^m 3.187 0.623 0.329 0.657 0.598 0.969 def2-(T,Q]ZVPP ^m 3.111 0.623 0.329 0.661 0.965 def2-(T,Q]ZVPP ^m 3.111 0.623 0.329 0.612 0.965 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225	def2-QZVPP*	3.007	0.591	0.322	0.643	0.624	0.828							
def2-QZVPPD 2.965 0.595 0.318 0.630 0.584 0.837 def2-{T,Q}ZVPP 3.326 0.651 0.371 0.657 0.598 1.050 def2-{T,Q}ZVPP* 3.177 0.651 0.371 0.657 0.598 1.050 def2-{T,Q}ZVPP* 3.177 0.623 0.329 0.657 0.598 0.969 def2-{T,Q}ZVPP" 3.187 0.623 0.329 0.657 0.612 0.965 def2-{T,Q}ZVPD" 3.111 0.623 0.321 0.670 0.600 0.894 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225 *VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225	def2-QZVPP ^m	2.953	0.591	0.322	0.645	0.592	0.803							
def2-{T,Q}ZVPP 3.326 0.651 0.371 0.657 0.598 1.050 def2-{T,Q}ZVPP* 3.177 0.623 0.329 0.657 0.598 0.969 def2-{T,Q}ZVPP" 3.187 0.623 0.329 0.657 0.612 0.965 def2-{T,Q}ZVPPD 3.111 0.623 0.329 0.670 0.600 0.894 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225 *VDZ-F12 5.883 0.880 0.321 0.610 0.894	def2-QZVPPD	2.965	0.595	0.318	0.630	0.584	0.837							
def2-{T,Q}ZVPP* 3.177 0.623 0.329 0.657 0.598 0.969 def2-{T,Q}ZVPP ^m 3.187 0.623 0.329 0.657 0.612 0.965 def2-{T,Q}ZVPPD 3.111 0.625 0.321 0.670 0.600 0.894 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225 "VDZ*: AVnZ was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76, and BH76RC. In the "VnZ ^m " variant, we additionally treated the BUT14DIOL, S22, S66, S ⁴	def2-{T,Q}ZVPP	3.326	0.651	0.371	0.657	0.598	1.050							
def2-{T,Q}ZVPP" 3.187 0.623 0.329 0.657 0.612 0.965 def2-{T,Q}ZVPPD 3.111 0.625 0.321 0.670 0.600 0.894 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225 ^a VnZ*: AVnZ was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76, and BH76RC. In the "VnZ ^m " variant, we additionally treated the BUT14DIOL, 522, S66, S ⁴	def2-{T,Q}ZVPP*	3.177	0.623	0.329	0.657	0.598	0.969							
def2-{T,Q}ZVPPD 3.111 0.625 0.321 0.670 0.600 0.894 VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225 ^a VnZ*: AVnZ was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76 RC. In the "VnZ ^m " variant, we additionally treated the BUT14DIOL, S22, S66, S ¹	def2-{T,Q}ZVPP‴	3.187	0.623	0.329	0.657	0.612	0.965							
VDZ-F12 5.883 0.880 0.323 0.916 1.539 2.225 ^a VnZ*: AVnZ was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76, and BH76RC. In the "VnZ ^m " variant, we additionally treated the BUT14D10L, S22, S66, S ¹	def2-{T,Q}ZVPPD	3.111	0.625	0.321	0.670	0.600	0.894							
^a VnZ*: AVnZ was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76, and BH76RC. In the "VnZ"" variant, we additionally treated the BUT14D10L, S22, S66, S1	VDZ-F12	5.883	0.880	0.323	0.916	1.539	2.225							
PCONF21, PArel, MCONF, and AMINO20x4 test sets with the hAVnZ basis set. VnZ-F12*: AVnZ-F12 was employed for RG18, AHB21, G21EA, IL16, WATER27, BH76, and BH76RC. In the "VnZ-F12"	^a VnZ*: AVnZ was er PCONF21, PArel, MC	nployed for R ONF, and AM	G18, AHB21, 11NO20x4 test	G21EA, IL16 t sets with the	6, WATER2 hAVnZ basi	7, BH76, a is set. VnZ-	and BH76RC. 1 F12*: AVnZ-F	in the "VnZ ^m vari 12 was employed fo	ant, we additions of RG18, AHB.	onally treated 21, G21EA, II	the BUT14DI 16, WATER27	OL, S22, S , BH76, and	66, SCON d BH76RC	F, PNIC . In the '

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were set to $10^{-9}E_h$ throughout, with MOLPRO's default integration grids for this accuracy and the basis set at hand.

We considered different families of basis sets. The first category are the correlation consistent basis sets of Dunning,^{130–132} which were developed with orbital-based correlated wavefunction calculations in mind (optimized for CISD valence correlation energies of atoms). The notation VnZ, in this paper, is shorthand for the combination of regular cc-pVnZ on first-row elements, cc-pV(n+d)Z on second-row elements, and cc-pVnZ-PP for the heavy p-block elements, where PP stands for pseudopotential. Finally, we employed ad hoc modifications: for RG18⁶ and the anion-containing subsets AHB21,¹⁰⁶ G21EA,^{60,82} IL16,¹⁰⁶ WATER27,^{101,102} BH76,^{6,68,70,82} and BH76RC,^{6,82} we employed aug-cc-pVnZ ("VnZ*"). In the "VnZ^m" variant, we additionally treated the BUT14DIOL,^{6,116} S22,^{98,99} S66,¹⁰⁰ SCONF,^{6,82,114} PNICO23,^{6,100} PCONF21,^{6,111} PArel,⁶ MCONF,^{6,133} and AMINO20x4^{6,110} test sets with the hAVnZ basis set (cc-pVnZ on hydrogen, aug-cc-pVnZ on first-row elements, aug-cc-pVnZ (n+d)Z on second-row elements, and aug-cc-pVnZ-PP for the heavy p-block elements).

The second class of basis sets considered are the cc-pVnZ-F12 (abbreviated VnZ-F12 in this manuscript) of Peterson and co-workers,¹³⁴ or their anionic-friendly variants aug-cc-pVnZ-F12 (AVnZ-F12).¹³⁵ These basis sets were explicitly developed with F12 calculations in mind. In fact, non-F12 basis sets in explicitly correlated calculations lead to non-monotonous convergence because of elevated and erratic basis set superposition errors (BSSEs).⁴⁹ VnZ-F12* indicates that the VnZ-F12 basis set was used for all subsets of GMTKN55 except WATER27, IL16, G21EA, BH76, BH76RC, AHB21, and RG18, where we used AVnZ-F12. Again, we employed ccpVnZ-F12-PP for the heavy p-block elements. The geminal Slater exponent (β) values of 0.9, 1.0, and 1.0 were used for the (A-)VDZ-F12, (A-)VTZ-F12, and (A-)VQZ-F12, respectively.

Finally, we also considered the Weigend–Ahlrichs/Karlsruhe def2 family,¹³⁶ namely def2-TZVPP and def2-QZVPP, and their diffuse function-augmented variants def2-TZVPPD and def2-QZVPPD.¹³⁷ def2-*n*ZVPP* and def2-*n*ZVPP^m variants are defined analogously to the above.

The geometries, charge/multiplicity information and reference energies were obtained from ref 6 and used verbatim throughout. The most computationally demanding subset isomerization energies of fullerene C_{60} structures (C60ISO)⁸⁹ might just barely have been feasible with the VDZ-F12 basis set with available computational resources, but near-singularity in the overlap matrix (smallest eigenvalue 3×10^{-11}) effectively made the KS calculations impossible to converge. This subset's omission does not significantly affect WTMAD2 because of its small weight in the WTMAD2 formula. For explicitly correlated DHDF calculations on the UPU23 subset,¹¹⁵ we settled for (A-)VDZ-F12 basis to reduce computational cost.

3. RESULTS AND DISCUSSION

3.1. Basis Set Convergence for Conventional Double Hybrids. Let us first consider the basis set convergence with the orbital basis sets in conventional double-hybrid calculations, that is, B2GP-PLYP-D3(BJ)/VnZ, where n = D,T,Q, and 5 (Table 2). The PT2 component slows down basis set convergence, albeit mitigated (compared to MP2 in a Hartree–Fock basis set) by the PT2 coefficients in the double hybrid (typically in the 0.1–0.5 range). Although DHDFs

converge faster than ab initio methods, their PT2 part acquires a slower basis set convergence. The VDZ basis set yields an unacceptably large WTMAD2 of 11.904 kcal/mol for the entire GMTKN55 database. This goes down to 9.661 kcal/mol when substituting the AVDZ basis set for the rare gas clusters RG18 and the six anion-containing subsets WATER27, BH76, BH76RC, AHB21, G21EA, and IL16. A further reduction to 6.332 kcal/mol was achieved for the VDZ^{*m*} variant, where the haVDZ basis set additionally was applied to BUT14DIOL, S22, S66, SCONF, PNICO23, PCONF21, PArel, MCONF, and AMINO20x4. Therefore, we will mostly discuss our statistics of conventional double-hybrid calculations with the VnZ^m variant. The VTZ^m basis set nearly halves WTMAD2 to 3.427 kcal/mol. In order to surpass this level of accuracy, VQZ^m has to be employed, yielding a WTMAD2 of 3.131 kcal/mol. For still better basis set convergence, we employed V5Z^m, which slightly further lowers WTMAD2 to 3.020 kcal/ mol. As the orbital-only B2GP-PLYP-D3(BJ) complete basis set limit estimate, we extrapolate VQZ^m and $V5Z^m$ reaction energies using the two-point extrapolation formula $(A + B/L^{\alpha})$, L = highest angular momentum present in the basis set) where α = 8.7042 for KS and 2.7399 for PT2 (as recommended in refs 138 and 139) components, respectively. The B2GP-PLYP- $D3(BJ)/V{Q,5}Z^{m}$ level of theory results in a WTMAD2 of 3.115 kcal/mol for the entire GMTKN55 database. B2GP-PLYP-D3(BJ)/V{T,Q} Z^m (α = 7.6070 for KS and 2.5313 for PT2) yields WTMAD2 of 3.351 kcal/mol.

A breakdown into the five top-level subdivisions of GMTKN55 (Table 2) showed that all five of them smoothly approach the basis set limit at the B2GP-PLYP-D3(BJ)/ $V{Q,5}Z^m$ level. More detailed scrutiny of the individual subsets revealed that HEAVY28^{6,97} is the major contributor to the difference between $V5Z^m$ and $V{Q,5}Z^m$, with Δ WTMAD2 increased by 0.048 kcal/mol. Because of the way HEAVY28, RG18, and HAL59^{6,104,105} are weighted in WTMAD2, a small change in those subsets has an outsize contribution.

3.2. Effect of Introducing F12 Terms. Next, we investigate the basis set convergence in the explicitly correlated double-hybrid calculations. These calculations need to be done with the cc-pVnZ-F12 basis sets of Peterson et al. 134 Table 2 presents a statistical analysis of B2GP-PLYP-F12-D3(BJ) calculations. The B2GP-PLYP-F12-D3(BJ)/VDZ-F12 level of theory results in a WTMAD2 of only 2.953 kcal/mol. We would like to emphasize that this is not just a matter of the basis set: for illustration, we also evaluated orbital-only B2GP-PLYP-D3(BJ)/VDZ-F12 and found that WTMAD2 shot up to 5.883 kcal/mol. The difference is entirely owing to the presence versus absence of geminal F12 terms in the GLPT2 evaluation. Somewhat surprisingly, WTMAD2 with VDZ-F12* basis (AVDZ-F12 basis for the rare gas clusters RG18 and six anion containing subsets WATER27, BH76, BH76RC, AHB21, G21EA, and IL16) only was reduced to 2.939 kcal/ mol, indicating that not even for anionic subsets is AVDZ-F12 required. (We do note that, unlike the VDZ orbital basis set, the VDZ-F12 already includes one diffuse function each of s and p symmetries for p-block elements, and one diffuse s function for hydrogen.) In explicitly correlated B2GP-PLYP-F12-D3(BJ), the energy differences that make up the GMTKN55 benchmark converge markedly, one might even say dramatically, faster with respect to the basis set size. For example, VDZ-F12*, VTZ-F12*, and VQZ-F12* provide WTMAD2 which are 2.939, 2.969, and 3.004 kcal/mol

Table 3. A Comparison of Total WTMAD2 of GMTKN55 Data Set (i.e., WTMAD2 (all)) and WTMAD2 after Excluding RG18, HEAVY28, and HAL59 from the Statistics (i.e., WTMAD2 (mod))^{*a*}

	WTMAD2 (all)	WTMAD2 (mod.)	WTMAD2 (all)	WTMAD2 (mod.)
	GMTKNS	55 as reference	CBS limit	as reference
		B2GP-PLYP-F12-D3(BJ)		
AVDZ-F12	3.011	2.706	0.418	0.320
VDZ-F12	2.953	2.686	0.499	0.391
VDZ-F12*	2.939	2.671	0.467	0.358
VTZ-F12	2.979	2.632	0.220	0.191
VTZ-F12*	2.969	2.626	0.207	0.172
V{D,T}Z-F12	3.005	2.625	0.232	0.205
V{D,T}Z-F12*	2.993	2.621	0.215	0.191
VQZ-F12	3.007	2.657	0.065	0.042
VQZ-F12*	3.004	2.649	0.032	0.024
V{T,Q}Z-F12	3.015	2.662	0.038	0.018
V{T,Q}Z-F12*	3.016	2.653	0.002	0.001
		B2GP-PLYP-D3(BJ)		
VDZ	11.904	11.295	11.303	10.825
VDZ*	9.661	9.120	9.014	8.582
VDZ^m	6.332	5.540	5.602	4.911
VTZ	5.649	5.185	4.317	3.942
VTZ*	4.495	4.132	3.020	2.779
VTZ^m	3.427	2.984	1.752	1.414
VQZ	3.978	3.517	1.913	1.717
VQZ*	3.417	2.969	1.172	1.065
VQZ ^m	3.131	2.662	0.723	0.582
V{T,Q}Z	3.955	3.334	1.578	1.264
V{T,Q}Z*	3.521	2.892	0.977	0.733
$V{T,Q}Z^m$	3.351	2.710	0.596	0.323
V5Z*	3.054	2.678	0.372	0.278
$V5Z^m$	3.020	2.641	0.299	0.199
V{Q,5}Z*	3.105	2.660	0.302	0.167
$V{Q_5}Z^m$	3.115	2.671	0.275	0.138
def2-TZVPP	3.966	3.701	2.534	2.369
def2-TZVPP*	3.412	3.158	1.883	1.750
def2-TZVPP ^m	3.162	2.889	1.633	1.480
def2-TZVPPD	3.157	2.781	1.530	1.405
def2-QZVPP	3.267	2.878	1.045	0.899
def2-QZVPP*	3.007	2.671	0.748	0.636
def2-QZVPP ^m	2.953	2.613	0.750	0.638
def2-QZVPPD	2.965	2.577	0.743	0.625
def2-{T,Q}ZVPP	3.326	2.856	0.743	0.560
def2-{T,Q}ZVPP*	3.177	2.719	0.573	0.387
def2-{T,Q}ZVPP ^m	3.187	2.730	0.519	0.329
def2-{T,Q}ZVPPD	3.111	2.724	0.456	0.289
lues are reported in kca	1/mal			

above the reference values, respectively. Small discrepancies between the three basis sets are mostly because of rare-gas clusters RG18 with their outsize weights, which contribute 0.042 and 0.016 kcal/mol, respectively, toward the increase in WTMAD2 for VDZ-F12* to VTZ-F12* and VTZ-F12* to VQZ-F12*. The other test sets that contribute toward deviations between VDZ-F12* and VTZ-F12* are HEAVY28 (0.021 kcal/mol) and HAL59 (0.008 kcal/mol).

A reviewer inquired whether the mildly non-monotonic basis set convergence observed in Table 2 could be attributable to the excessive weights given to the three subsets RG18, HEAVY28, and HAL59 in eq 1. Table 3 compares convergence behavior for GMTKN55 including versus excluding these three subsets from the summations in the numerator and denominator of eq 1. Although the "exclusive" WTMAD2 values are naturally considerably smaller, the mild non-monotonicity persists and likely needs to be attributed to subtle error compensations in the individual subsets between basis set incompleteness and intrinsic functional error. Consistent with this conjecture, we observe that WTMAD2 values relative to the complete basis set limit of the functional (right-hand pane of Table 3) do converge monotonically both with and without the said three subsets.

WTMAD2 obtained with V{D,T}Z-F12* (2.993 kcal/mol) and V{T,Q}Z-F12* (3.016 kcal/mol) pairs can essentially be regarded as the basis set limit. We used the two-point extrapolation formula ($A + B/L^{\alpha}$, L = highest angular momentum present in the basis set) for the PT2 components with α = 3.0878 for the V{D,T}Z-F12 pair and α = 4.3548 for the V{T,Q}Z-F12 pair.¹³⁸ The extrapolation of the KS component essentially provides the same WTMAD2 as obtained with just the highest angular momentum present in the basis set and CABS. Switching off the CABS correction only increases the WTMAD2 value for V{D,T}Z-F12 from 3.005 to 3.013 kcal/mol.

In order to explore whether MP2-F12 extrapolation exponents can be safely used for the PT2-F12 component in DHDF-F12, we performed a sensitivity analysis of B2GP-PLYP-F12-D3(BJ)/V{D,T}Z-F12 extrapolation by calculating rmsd differences [rmsd(extrapolation exponent α)— rmsd(∞)] for the atomization energies of the W4-11 set calculated relative to B2GP-PLYP-F12-D3(BJ)/V{T,Q}Z-F12. Figure 1 shows a minimum near α = 3.4. α = 3.0878 taken

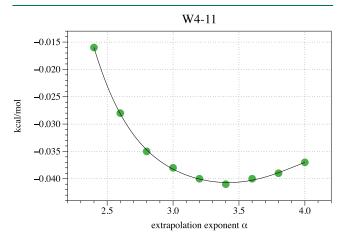


Figure 1. Sensitivity analysis of the B2GP-PLYP-F12-D3(BJ)/ V{D,T}Z extrapolation.Root-mean-square deviation (rmsd) differences [rmsd(extrapolation exponent α —rmsd(∞)] for the atomization energies of the W4-11⁵⁹ set calculated relative to B2GP-PLYP-F12-D3(BJ)/V{T,Q}Z-F12.

from ref 138 yields $rmsd(\alpha)$ — $rmsd(\infty) = -0.040$ kcal/mol instead of -0.041 kcal/mol for $\alpha = 3.4$, which is a negligible difference in the larger scheme of things. For different double hybrids, the minimum of this shallow curve might vary slightly around $\alpha = 3.4$, without significantly affecting rmsd. Hence, we elected to retain the MP2-F12 extrapolation exponent.

3.3. Aside on BSSE. A brief digression on BSSE might shed more light on basis set convergence behavior. For the intermolecular subset of GMTKN55, one has the option of applying counterpoise (CP) corrections¹⁴⁰ (for detailed

discussion and further references, see Burns et al.¹⁴¹ for WFT methods, Brauer et al.¹⁴² for F12 methods, and ref 143 for DFT and double hybrids). For the intramolecular subset, CP corrections would be rather more awkward, although geometric CP corrections do exist^{144,145} for some levels of theory. (For an alternative approach to noncovalent interactions for large systems, involving small tailored basis sets, see ref 146 and references therein). Hence, most groups that employ GMTKN55 avoid CP corrections, which of course presuppose basis sets large enough that these no longer matter (much).

One major benefit of F12 methods (with F12 basis sets) was previously found to be^{142,147} a drastic reduction in BSSE, as shown for thermochemistry¹⁴⁷ and for noncovalent interactions.^{142,143}

Table 4 presents CP corrections for the Watson–Crick and stacked uracil dimers (systems 17 and 26, respectively, in S66), as representative examples of strong hydrogen bonding and π -stacking, respectively. As seen in Table 4, B2GP-PLYP-F12/VnZ-F12 leads to a BSSE reduction by an order of magnitude (or more) over the corresponding B2GP-PLYP/VnZ calculation, and indeed one has to go all the way to VSZ to find a basis set with a similarly low BSSE as B2GP-PLYP-F12/VDZ-F12 (!). For haVnZ-F12 versus haVnZ, and for AVnZ-F12 versus AVnZ, one likewise sees one order of magnitude reduction in BSSE. Additionally, AVnZ-F12 further reduced BSSE by about a factor 2–3 over the already low values for VnZ-F12.

At the CBS limit, the BSSE correction should of course be zero, as raw and CP-corrected calculations should yield the same answer. The deviation from zero when extrapolating CP corrections to the CBS limit is a good proxy for the quality of the extrapolation (and its underlying basis sets). For V{T,Q}Z-F12 and AV{T,Q}Z-F12, this evidently works beautifully. For V{D,T}Z-F12 and AV{D,T}Z-F12, not much improvement over the already low BSSE of VTZ-F12 viz. AVTZ-F12 can be seen. For V{Q,5}Z, on the other hand, we find a large negative BSSE that indicates overcorrection. In fact, simple VDZ-F12 has less BSSE than V{Q,5}Z and similar to haV{Q,5}Z.

3.4. Basis Set Convergence Relative to the Complete Basis Set Limit. Furthermore, we explored the basis set convergence of conventional and explicitly correlated double-hybrid calculations using basis set limit reference values (Table 5). For this purpose, we used energies calculated at the B2GP-PLYP-F12-D3(BJ)/V{T,Q}-F12* level of theory, as they are sufficiently converged to the basis set limit. Conventional

Table 4. B2GP-PLYP-F12 Compared to B2GP-PLYP CP Corrections (kcal/mol) for the Two Uracil Dimer Structures in S66 Using Different Basis Sets^a

	dimer 17 Watson-Crick	dimer 26 π -stacked		dimer 17 Watson-Crick	dimer 26 π -stacked		dimer 17 Watson-Crick	dimer 26 π -stacked
B2GP-PI	XP-F12							
VDZ-F12	0.191	0.317	haVDZ-F12	0.107	0.128	AVDZ-F12	0.097	0.124
VTZ-F12	0.106	0.208	haVTZ-F12	0.056	0.113	AVTZ-F12	0.065	0.116
VQZ-F12	0.042	0.068	haVQZ-F12	0.014	0.026	AVQZ-F12	0.017	0.027
B2GP-PI	ΥР							
VDZ	4.768	4.545	haVDZ	1.285	2.927	AVDZ	1.848	3.083
VTZ	1.630	2.089	haVTZ	0.650	1.120	AVTZ	0.901	1.223
VQZ	0.634	0.908	haVQZ	0.261	0.465	AVQZ	0.348	0.507
V5Z	0.210	0.289	haV5Z	0.108	0.169	AV5Z	0.160	0.188

^ahaVnZ-F12, by analogy with haVnZ, corresponds to AVnZ-F12 on nonhydrogen elements and VnZ-F12 on hydrogen.

Table 5. Statistical Analysis of the Basis Set Convergence in Conventional and Explicitly Correlated B2GP-PLYP-D3(BJ) Calculations for the GMTKN55 Database and Its Categories, Relative to the B2GP-PLYP-F12-D3(BJ)/V $\{T,Q\}Z$ -F12* Reference Data^a

			B2GP-PLYP	-D3(BJ)					В	2GP-PLYP-F1	2-D3(BJ)		
	WTMAD2	THERMO	BARRIERS	LARGE	CONF	INTERMOL		WTMAD2	THERMO	BARRIERS	LARGE	CONF	INTERMOL
VDZ	11.303	2.251	0.869	0.854	4.110	3.220	AVDZ-F12	0.418	0.087	0.036	0.061	0.083	0.152
VDZ*	9.014	1.340	0.464	0.854	4.110	2.246	VDZ-F12	0.499	0.096	0.042	0.050	0.098	0.212
VDZ^m	5.602	1.340	0.464	0.755	1.416	1.627	VDZ-F12*	0.467	0.082	0.038	0.050	0.098	0.199
VTZ	4.317	0.853	0.373	0.174	1.325	1.592	VTZ-F12	0.220	0.035	0.019	0.021	0.055	0.090
VTZ*	3.020	0.399	0.137	0.174	1.325	0.984	VTZ-F12*	0.207	0.025	0.016	0.021	0.055	0.090
VTZ^m	1.752	0.399	0.137	0.145	0.404	0.666	V{D,T}Z-F12	0.232	0.033	0.023	0.027	0.062	0.088
VQZ	1.913	0.407	0.201	0.082	0.431	0.792	V{D,T}Z-F12*	0.215	0.026	0.020	0.027	0.062	0.079
VQZ*	1.172	0.160	0.054	0.082	0.431	0.446	VQZ-F12	0.065	0.012	0.006	0.004	0.006	0.038
VQZ^m	0.723	0.160	0.054	0.075	0.151	0.284	VQZ-F12*	0.032	0.005	0.002	0.004	0.006	0.016
V{T,Q}Z	1.578	0.244	0.180	0.075	0.246	0.833	V{T,Q}Z-F12	0.038	0.006	0.004	0.000	0.001	0.028
$V{T,Q}Z^*$	0.977	0.061	0.045	0.075	0.246	0.550	V{T,Q}Z-F12*	REF	REF	REF	REF	REF	REF
$V{T,Q}Z^m$	0.596	0.061	0.045	0.073	0.066	0.351							
V5Z*	0.372	0.063	0.016	0.023	0.091	0.179							
$V5Z^m$	0.299	0.063	0.016	0.023	0.050	0.147							
V{Q,5}Z*	0.302	0.021	0.014	0.027	0.063	0.178							
$V{Q,5}Z^m$	0.275	0.021	0.014	0.024	0.042	0.175							
def2-TZVPP	2.534	0.600	0.240	0.169	0.694	0.831							
def2-TZVPP*	1.883	0.400	0.098	0.169	0.694	0.523							
$def2-TZVPP^{m}$	1.633	0.400	0.098	0.157	0.474	0.505							
def2-TZVPPD	1.530	0.326	0.074	0.175	0.473	0.483							
def2-QZVPP	1.045	0.253	0.106	0.082	0.202	0.402							
def2-QZVPP*	0.748	0.171	0.038	0.082	0.202	0.254							
$def2-QZVPP^{m}$	0.750	0.171	0.038	0.082	0.201	0.258							
def2-QZVPPD	0.743	0.157	0.030	0.078	0.209	0.269							
def2-{T,Q}ZVPP	0.743	0.132	0.077	0.070	0.091	0.372							
def2-{T,Q}ZVPP*	0.573	0.089	0.025	0.070	0.091	0.298							
$def2-{T,Q}ZVPP^{m}$	0.519	0.089	0.025	0.067	0.085	0.254							
def2-{T,Q}ZVPPD	0.456	0.090	0.020	0.033	0.088	0.225							
VDZ-F12	5.324	0.795	0.324	0.576	1.238	2.392							

"Values are heat-mapped from red for the largest via yellow for median to green for the smallest. Note that values are heat-mapped separately for each category of GMTKN55 and the entire database.

B2GP-PLYP-D3(BJ) calculations in conjunction with the VDZ^m basis set yield a WTMAD2 value that is 5.602 kcal/ mol above the basis set limit. Increasing the basis set to VTZ^m and VQZ^m reduces this deviation to 1.752 and 0.723 kcal/mol, respectively. V5Z^m yields a deviation that is only 0.299 kcal/ mol above our best estimate (B2GP-PLYP-F12-D3(BJ)/ V{T,Q}-F12*). Basis set limit reaction energies for the conventional B2GP-PLYP-D3(BJ)/V{Q,5}^{*m*} calculations differ by only 0.275 kcal/mol from explicitly correlated B2GP-PLYP-F12-D3(BJ)/V{T,Q}-F12*, of which inter- and intramolecular noncovalent interactions account for the lion's share. A closer inspection of the individual subsets revealed that HEAVY28, HAL59, and RG18 are the three largest contributors to the discrepancies, their Δ WTMAD2 of HEAVY28, RG18, and HAL59 being 0.086, 0.034, and 0.027 kcal/mol, respectively, relative to B2GP-PLYP-F12-D3(BJ)/V{T,Q}-F12*. As discussed above, the way these three subsets are weighted in the WTMAD2 formula, a small change in reaction energies has a disproportionate contribution to WTMAD2.

B2GP-PLYP-D3(BJ) in conjunction with def2-TZVPP, def2-QZVPP, and def2-{T,Q}ZVPP (α = 7.6070 for KS and 2.5313 for PT2) basis sets provides WTMAD2 which are 2.534, 1.045, and 0.743 kcal/mol above our best estimate, respectively. Adding diffuse functions to RG18, AHB21, BH76, BH76RC, IL16, G21EA, and WATER27 (i.e., def2-nZVPP* basis set) lowers the WTMAD2 values to 1.883, 0.748, and 0.573 kcal/mol, respectively, for TZ, QZ, and {T,Q}Z basis. On the other hand, def2-TZVPPD, def2-QZVPPD, and def2-{T,Q}ZVPPD provide WTMAD2 which are 1.530, 0.743, and 0.456 kcal/mol, respectively.

Turning our attention to explicitly correlated B2GP-PLYP-F12-D3(BJ) calculations with VnZ-F12 type basis sets, we note that VDZ-F12* already yields an acceptable WTMAD2 which

is only 0.467 kcal/mol from the F12 basis set limit. Moving on to AVDZ-F12 provides a WTMAD2 which is just 0.050 kcal/ mol below VDZ-F12*. The WTMAD2 component breakdown revealed that S66, HEAVY28, and AMINO20x4 together account for 0.043 kcal/mol of the total improvement in Δ WTMAD2 of AVDZ-F12 in comparison to VDZ-F12*. Increasing the basis set size to VTZ-F12* yields a WTMAD2 of 0.207 kcal/mol. WTMAD2 obtained with the VQZ-F12* basis set (0.032 kcal/mol) can essentially be regarded as the basis set limit.

3.5. Note on Systematic Errors. Thus far, we have only discussed WTMAD2. It would be of interest to compare, as a measure of systematic error, the basis set convergence of conventional and explicitly correlated double hybrids in terms of weighted total mean signed deviations (WTMSDs), where MAD in eq 1 is replaced by the MSD. (For clarity, the way the reference data's sign conventions work, a positive WTMSD2 indicates overbinding, and a negative one underbinding). Tables S1 and S2 in Supporting Information present the WTMSD2 of conventional and explicitly correlated B2GP-PLYP-D3(BJ) relative to the reference data⁶ and to the complete basis set limit as obtained at the B2GP-PLYP-F12- $D3(BJ)/V\{T,Q\}Z\text{-}F12^*$ level. WTMSD2 obtained for B2GP-PLYP-F12-D3(BJ) with VDZ-F12* (0.081 kcal/mol), VTZ-F12* (0.071 kcal/mol), and V{D,T}Z-F12* (0.087 kcal/mol) basis sets are all close to zero and indicate that there is little systematic error relative to the complete basis set limit (Table S2). Turning our attention to conventional B2GP-PLYP-D3(BJ), we obtained WTMSD2 of 2.693, 1.077, 0.501, 0.076, and 0.042 kcal/mol for the VDZ*, VTZ*, VQZ*, V5Z*, and $V{Q,5}Z^*$ basis sets, respectively. These results indicate that even VQZ* still overbinds significantly due to BSSE: a breakdown into the five top-level subsets (Table S2) reveals

Table 6. Relative CPU Timings for the B2GPPLYP-D3(BJ) and B2GPPLY-F12-D3(BJ) Calculations for $(C_{\mu}H_{\mu+2})_{2}^{a}$

	B2GP-PLYP-F12				B2GP-F	PLYP		
	PNO-LPT2	canonical						
	PNO-F12 VDZ-F12	VDZ-F12	{T,Q}ZVPP	{T,Q}ZVPPD	$_{\rm V{T,Q}Z}$	$haV\{T,Q\}Z$	$haV{Q,5}Z$	$_{\rm AV\{T,Q\}Z}$
$(\text{ethane})_2$	1.08	1.00	1.38	1.92	1.74	2.02	7.20	3.69
$(\text{propane})_2$	1.05	1.00	1.22	1.84	1.53	2.19	8.33	4.15
$(butane)_2$	0.83	1.00	0.91	1.47	1.58	1.84	7.15	3.47
$(\text{pentane})_2$	0.63	1.00	0.70	1.16	0.91	1.49	5.83	2.78
$(hexane)_2$	0.49	1.00	0.57	0.95	0.73	1.23	4.93	2.30
$(heptane)_2$	0.38	1.00	0.48	0.81	0.62	1.05	4.24	1.96
$(n-octane)_2$	0.28	1.00	0.38	0.66	0.49	0.85	3.43	1.58
$(n-nonane)_2$	0.22	1.00	0.32	0.56	0.41	0.72	2.96	1.34
$(n-decane)_2$	0.18	1.00	0.28	0.49	0.36	0.63	2.60	1.16
$(n-dodecane)_2$	0.11	1.00	0.22	0.39	0.28	0.49	2.09	0.92

^aTiming is shown relative to B2GP-PLYP-F12-D3(BJ)/VDZ-F12; white = 1, blue = faster, and red = slower.

that intermolecular interactions account for about two-thirds, and conformers for almost all the remainder. Turning to the VnZ^m variants, VDZ^m yields a deceptively low WTMSD2 = 0.345 kcal/mol owing to compensation between sizable systematic underestimates of basic thermochemistry, barrier heights, a large molecule reaction, systematic overestimates of conformer energies, and especially intermolecular interactions. Although VTZ^m sees WTMSD2 "only" reduced to 0.235 kcal/ mol, the constituent values for the five top-level subsets are actually reduced by factors of 3-4. (This, incidentally, illustrates the dangers of blindly relying on a single global metric). The 0.182 kcal/mol for VQZ^m is mostly driven by the noncovalent interactions (0.213 kcal/mol), slightly compensated by basic thermochemistry and barrier heights. Finally, $V5Z^m$ has only a mild systematic error, again mostly from noncovalent interactions. $V{T,Q}Z^m$ extrapolation yields a WTMSD2 of 0.337 kcal/mol, which at first sight seems inferior even to VDZ^m; however, closer inspection reveals that essentially all of that number comes from overbinding in the intermolecular interactions due to BSSE and that the remaining four top-level subsets are nearly free of systematic bias. For $V{Q,5}Z^m$, WTMSD2 is down to a paltry 0.048 kcal/ mol, essentially all of it again from intermolecular interactions. Interestingly, def2-QZVPP (-0.228 kcal/mol) and especially def2-QZVPP* (-0.024 kcal/mol) and def2-QZVPPD (-0.016 kcal/mol) have much smaller WTMSD2 values, also for the top-level subsets: the negative signs reflect mostly underestimates for small-molecule thermochemistry. The different signs of the def2-{T,Q}ZVPPD* and def2-{T,Q}ZVPPD WTMSD2s essentially reflect systematic overbinding versus underbinding of intermolecular interactions, where the former lacks diffuse functions on such subsets as S22, S66, and the like.

3.6. Computational Cost Considerations. It is of interest to compare the relative computational cost of conventional B2GP-PLYP-D3(BJ) and B2GP-PLYP-F12-D3(BJ) procedures. Each of these timing evaluation jobs was run on otherwise empty nodes with identical hardware (Intel Haswell 2.4 GHz with 256 GB RAM and a 3.6TB SSD RAID array). These jobs were run serially, on a single core, in order to eliminate differences in parallelization as a confounding factor. Timing data relative to VDZ-F12 are reported in Table 6 for the six linear *n*-alkane dimers in ADIM6,^{6,97} (ethane)₂ through (*n*-heptane)₂, plus additionally (*n*-octane)₂, (*n*-non-ane)₂, (*n*-decane)₂, and (*n*-dodecane)₂ with the structures

obtained by manually inserting additional CH_2 groups (because we needed them only for timing purposes). As we have seen above, even the VDZ-F12 basis set yields results of a quality comparable to $V{Q_2S}Z^m$. In view of the fact that no CP correction is being applied, one would definitely want to use haV $\{Q,S\}Z$ for this subset rather than $V{Q_2S}Z$. The sum of timings for both calculations involved in the extrapolation ranges from 8 times longer than VDZ-F12 for propane dimer to twice as long for *n*-dodecane dimer, with the ratio increasingly less favorable to VDZ-F12 as the chain lengths increase. For AV $\{T,Q\}Z$, one goes from about 4 times to about the same time, and for def2- $\{T,Q\}ZVPPD$ that falls from 2 times slower to over twice as fast. In addition, the canonical VDZ-F12 calculations will be increasingly more demanding in mass storage requirements, at least for MOLPRO.

However, in a very recent communication,¹⁴⁸ we have shown that the F12 step can be drastically accelerated by evaluating it in terms of localized pair natural orbitals (i.e., PNO-DHDF-F12) without materially sacrificing accuracy. In addition, it is shown there that the scratch storage requirements are an order of magnitude smaller and that parallelization is more efficient than canonical F12 as well. By way of illustration of what this approximation enables, we offer a PNO-B2GP-PLYP-LMP2/VDZ-F12 calculation on C_{60} (no symmetry): after deleting a diffuse p function that causes insurmountable near-linear dependence issues, it took just S1 min wall clock time on 16 cores of an Ice Lake 2.2 GHz node.

For the discussion at hand here, single-core PNO-DHDF-F12 timing data can be found in the first column of Table 6. For the smallest systems, as expected, the localized approach offers no benefit, but as the chain length increases ever-better speedup is realized, to reach an order of magnitude for *n*dodecane dimer. By way of illustration, we applied a power fit to the canonical DHDF-F12 and PNO-DHDF-F12 wall clock times for *n*-pentane through *n*-dodecane dimers and found very good fits with $R^2 = 0.99917$ and $R^2 = 0.99996$, respectively: the scaling exponents are 4.57 and 2.60, respectively, showing the scaling advantage of the PNO-F12 approach. Indeed, in ref 148 we show that for still longer chains through *n*-tetracosane dimer (i.e., *n* = 24), scaling with *n* decreases further toward linearity.

It is clear that PNO-DHDF-F12/VDZ-F12 offers a more economical alternative than any of the basis set extrapolations that would yield comparable, or even somewhat inferior, accuracy. We therefore do believe that the DH-F12 approach, especially in its localized orbital form, compares favorably in both accuracy and efficiency with large basis set B2GP-PLYP-D3(BJ).

3.7. Spin-component-scaled Double Hybrids. We will now evaluate GMTKN55 performance for the more recent and accurate revDSD-PBEP86-D3(BJ) functional⁸ with and without explicit correlation. Table 7 presents statistical analysis for conventional revDSD-PBEP86-D4 and explicitly correlated revDSD-PBEP86-F12-D4 calculations. Using the VnZ^m basis set in conjunction with conventional revDSD-PBEP86-D4 results in WTMAD2 values of 2.236 and 2.104 kcal/mol, respectively, for VQZ^m and VSZ^m basis sets. Leaving out diffuse functions altogether—including in the anionic subsets such as the G21EA electron affinities and the hydroxide clusters in WATER27— WTMAD2 unacceptably increases by 0.6 kcal/mol from VQZ* to VQZ and by 0.4 kcal/mol from VSZ* to VSZ. G21EA alone accounts for 0.176 (VQZ) and 0.077 (VSZ) kcal/mol, respectively.

Finally, the V{Q,5}Z^m pair yields a WTMAD2 of 2.233 kcal/ mol. Clearly, in the F12 calculations, WTMAD2 converges spectacularly faster with respect to the basis set size, with even VDZ-F12* reaching statistics comparable to V5Z* in the non-F12 approach. VDZ-F12* and VTZ-F12* yield WTMAD2 values which are 2.233 and 2.218 kcal/mol above the reference values; the latter is close to the "basis set limit" goal as WTMAD2 of V{D,T}Z-F12* is only 0.006 kcal/mol below VTZ-F12*.

At a reviewer's request, we further explored the basis set convergence of the same spin and opposite spin components of the PT2 term in a double hybrid. It is well established (see, e.g., Kutzelnigg and Morgan²⁵) that in the large-*L* limit, MP2 same-spin correlation energies converge as L^{-5} and their opposite-spin counterparts as L^{-3} . Hence, for sufficiently large basis sets, opposite-spin will dominate the convergence behavior and same-spin will be effectively saturated.

Although it stands to reason that this would also be the case for GLPT2 correlation, by way of illustration we show in Figure S1 that this is indeed the case for the same-spin (E_{2ss}) and opposite-spin (E_{2ab}) components of the B2GP-PLYP atomic correlation energy of neon atom along the *n*ZaP basis set sequence (n = 3-8, with maximum angular momentum L = n) of Petersson.^{149,150} Hence, for sufficiently large *L*, same-spin and opposite-spin contributions in B2GP-PLYP converge as L^{-5} and L^{-3} , respectively, and the latter will completely dominate convergence of the overall correlation energy.

4. CONCLUSIONS

We have investigated the basis set convergence of double hybrids in conjunction with explicitly correlated (F12) on a large and chemically diverse GMTKN55 database. We chose B2GP-PLYP-D3(BJ) and revDSD-PBEP86-D3(BJ) as test cases. Two families of basis sets were considered: orbital basis sets as large as aug-cc-pV(5+d)Z and F12 basis sets as large as cc-pVQZ-F12. We found that explicitly correlated double-hybrid calculations with F12 basis converge markedly faster than the conventional double-hybrid calculations with orbital (aug-)cc-pV(5+d)Z or def2 basis sets. In fact, DHDF-F12 calculations with just a cc-pVDZ-F12 basis set are closer to the basis set limit than DHDF/cc-pV(Q+d)Z or def2-QZVPPD and approach DHDF/cc-pV(5+d)Z in quality at about one-third the cost. One significant benefit of DHDF-F12 is reducing BSSE by an order of magnitude over orbital-only DHDF in a similar-sized basis set: this particularly benefits the

			revDSD-PBEP86-D4	P86-D4					revDSD-F	revDSD-PBEP86-F12-D4			
	WTMAD2	THERMO	BARRIERS	LARGE	CONF	INTERMOL		WTMAD2	THERMO	BARRIERS	LARGE	CONF	INTERMOL
ZOV	3.087	0.767	0.355	0.489	0.539	0.937	VDZ-F12	2.247	0.518	0.310	0.545	0.412	0.463
vQZ*	2.494	0.547	0.244	0.489	0.539	0.675	VDZ-F12*	2.233	0.513	0.306	0.545	0.412	0.458
VQZ^m	2.236	0.547	0.244	0.487	0.399	0.559	VTZ-F12	2.216	0.520	0.308	0.530	0.397	0.462
VSZ	2.502	0.628	0.318	0.501	0.386	0.670	$VTZ-F12^*$	2.218	0.521	0.305	0.530	0.397	0.466
VSZ^*	2.101	0.496	0.226	0.501	0.386	0.492	V{D,T}Z-F12	2.213	0.517	0.310	0.526	0.389	0.471
VSZ^m	2.104	0.496	0.226	0.499	0.402	0.480	V{D,T}Z-F12*	2.213	0.520	0.307	0.526	0.389	0.471
V{Q_5}Z	2.563	0.600	0.313	0.503	0.451	0.696							
V{Q.5}Z*	2.235	0.516	0.227	0.503	0.451	0.537							
$V{Q,S}Z^{m}$	2.233	0.516	0.227	0.502	0.433	0.555							

Table 7. Statistical Analysis of the Basis Set Convergence in Conventional and Explicitly Correlated revDSD-PBEP86-D4 Calculations for the GMTKN55 Database and Its

noncovalent interaction subsets (both intermolecular and conformer). We also found that even for anionic systems, the anion-friendly aug-cc-pVDZ-F12 basis set proved unnecessary and cc-pVDZ-F12 was adequate. Finally, although the application of DH-F12 to larger molecules will eventually face mass storage and I/O bandwidth challenges in a disk-based algorithm, these can be circumvented through localized pair natural orbital approaches, ¹⁴⁸ which also reduce CPU time scaling by (in practice) about n^2 .

Summing up, explicitly corrected double-hybrid calculations are an economical and accurate alternative if (near-)basis set limit results are required, for example, for benchmarking or parametrizing double-hybrid DFT methods. Implementation in other electronic structure systems of MP2-F12 in a basis of Kohn–Sham orbitals would be a very worthwhile endeavor, especially if said implementation is parsimonious in I/O requirements.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jctc.2c00426.

Statistical results of all assessed methods, as well as sample MOLPRO input files for B2GP-PLYP-F12-D3(BJ) and revDSD-PBEP86-F12-D4 and Figure S1 (PDF)

GMTKN55 statistical summary files for various basis set - functional combinations (ZIP)

Excel spreadsheet with additional timing information (ZIP)

AUTHOR INFORMATION

Corresponding Author

Jan M. L. Martin – Department of Molecular Chemistry and Materials Science, Weizmann Institute of Science, 7610001 Rehovot, Israel; orcid.org/0000-0002-0005-5074; Phone: +972-8-9342533; Email: gershom@ weizmann.ac.il; Fax: +972-8-9343029

Author

Nisha Mehta – Department of Molecular Chemistry and Materials Science, Weizmann Institute of Science, 7610001 Rehovot, Israel; © orcid.org/0000-0001-7222-4108

Complete contact information is available at: https://pubs.acs.org/10.1021/acs.jctc.2c00426

Notes

The authors declare no competing financial interest.

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