EXPLORING BIASES OF ATMOSPHERIC RETRIEVALS IN SIMULATED *JWST* TRANSMISSION SPECTRA OF HOT JUPITERS

M. Rocchetto[1], I. P. Waldmann[1], O. Venot[2], P.-O. Lagage[3,4], and G. Tinetti[1]

[1] Department of Physics & Astronomy, University College London, Gower Street, WC1E6BT London, UK; m.rocchetto@ucl.ac.uk
[2] Instituut voor Sterrenkunde, Katholieke Universiteit Leuven, Celestijnenlaan 200D, B-3001 Leuven, Belgium
[3] Irfu, CEA, Université Paris-Saclay, F-9119 Gif-sur Yvette, France
[4] AIM, Université Paris Diderot, F-91191 Gif-sur-Yvette, France

ABSTRACT

With a scheduled launch in 2018 October, the *James Webb Space Telescope* (*JWST*) is expected to revolutionize the field of atmospheric characterization of exoplanets. The broad wavelength coverage and high sensitivity of its instruments will allow us to extract far more information from exoplanet spectra than what has been possible with current observations. In this paper, we investigate whether current retrieval methods will still be valid in the era of *JWST*, exploring common approximations used when retrieving transmission spectra of hot Jupiters. To assess biases, we use 1D photochemical models to simulate typical hot Jupiter cloud-free atmospheres and generate synthetic observations for a range of carbon-to-oxygen ratios. Then, we retrieve these spectra using TauREx, a Bayesian retrieval tool, using two methodologies: one assuming an isothermal atmosphere, and one assuming a parameterized temperature profile. Both methods assume constant-with-altitude abundances. We found that the isothermal approximation biases the retrieved parameters considerably, overestimating the abundances by about one order of magnitude. The retrieved abundances using the parameterized profile are usually within 1σ of the true state, and we found the retrieved uncertainties to be generally larger compared to the isothermal approximation. Interestingly, we found that by using the parameterized temperature profile we could place tight constraints on the temperature structure. This opens the possibility of characterizing the temperature profile of the terminator region of hot Jupiters. Lastly, we found that assuming a constant-with-altitude mixing ratio profile is a good approximation for most of the atmospheres under study.

Key words: methods: data analysis – methods: statistical – techniques: spectroscopic

1. INTRODUCTION

The discovery of over 3000 exoplanets has unveiled a large and diverse population. We see planets in a range of sizes, temperatures, and orbits, far exceeding the diversity found in our own solar system. Today, emphasis in the field of exoplanets is shifting from the *discovery* to the *characterization* of these exoplanetary bodies, as understanding their nature will in turn provide important clues on the planets' formation and evolution history.

The study of exoplanetary atmospheres represents one of the most immediate and direct ways to characterize exoplanets. To date, the atmospheres of several tens of giant planets, sub-Neptunes, and super-Earths have been studied and characterized with the *Hubble Space Telescope* (*HST*; Charbonneau et al. 2002; Tinetti et al. 2010; Swain et al. 2013; Kreidberg et al. 2014; Sing et al. 2016; Tsiaras et al. 2016), the *Spitzer Space Telescope* (Grillmair et al. 2007; Knutson et al. 2007, 2011; Tinetti et al. 2007; Charbonneau et al. 2008; Beaulieu et al. 2010; Stevenson et al. 2010; Deming et al. 2011; Todorov et al. 2013), and other ground-based facilities (Redfield et al. 2008; Snellen et al. 2008; Swain et al. 2010; Waldmann et al. 2012; Bean et al. 2013; Brogi et al. 2014; Danielski et al. 2014; Zellem et al. 2014).

With the imminent launch of the *James Webb Space Telescope* (*JWST*), it has become fundamental to assess whether the current methods used to interpret these spectra will still be valid when higher-quality data sets will be available. In this work we aim to answer this question in part, exploring the biases induced by common assumptions used in atmospheric retrievals.

One of the major limitations of current observations is the limited wavelength coverage. The best-quality data sets, which led to the confident detection of water vapor in several hot Jupiters and warm Neptunes, have been mainly obtained with the Wide Field Camera 3 on board *HST*, covering the spectral range 1.1–1.7 μm. Nevertheless, it is at longer wavelengths that most rovibrational transitions of molecular species occur. While the *Spitzer Space Telescope* has given some insight into the longer-wavelength regime to several tens of close-in hot Jupiters, the data have relatively large uncertainties, and they are mostly only photometric measurements. Significant advances in the field of atmospheric characterization can therefore only happen if high-quality observations extending to the longer-wavelength regime are obtained.

In this scenario, the *JWST* will undoubtedly revolutionize the field of exoplanetary atmospheres, addressing two major problems affecting current observations: wavelength coverage and instrument sensitivity. With a scheduled launch for 2018 October, the large spectral coverage (0.7–28 μm) covered by its multiple instruments, combined with high sensitivity and a high degree of instrumental characterization and calibration, will ensure a significant advance in atmospheric characterization (Beichman et al. 2014; Barstow et al. 2015; Batalha et al. 2015; Cowan et al. 2015; Barstow & Irwin 2016; Greene et al. 2016).

Atmospheric spectra of transiting exoplanets in a broad spectral range will enable us to constrain the abundances of different molecular species, the temperature structure of the atmosphere, and the presence or absence of clouds and hazes. In the case of warm H/He-dominated atmospheres, one of the key elemental ratios that we aim to constrain is the carbon-to-

oxygen ratio (C/O). Such measurements will enable us to distinguish between different formation and migration scenarios, so far poorly constrained (Madhusudhan et al. 2011b; Öberg et al. 2011; Ali-Dib et al. 2014; Thiabaud et al. 2015). While transmission and emission spectra do not provide direct constraints on the elemental abundances, the measurement of the absolute abundances of O-bearing and C-bearing molecules will provide some constraints on the C/O ratio. In particular, the excess carbon and oxygen not locked in CO will form either oxygen-bearing molecules such as H_2O in atmospheres with C/O < 1 or, in atmospheres with C/O > 1, carbon-rich species such as HCN, C_2H_2, and CH_4 (Madhusudhan 2012; Moses et al. 2013a, 2013b; Venot et al. 2015). Determining the atmospheric abundances of these gases in hot Jupiters with high accuracy is therefore paramount, and *JWST* will give us direct access to absorption features of these molecules in both emission and transmission.

Determining the absolute abundances of atmospheric gases from atmospheric spectra requires the use of retrieval methods. Atmospheric retrieval techniques are now commonly used to infer the properties of exoplanetary atmospheres, including molecular abundances and temperature profiles (Irwin et al. 2008; Madhusudhan & Seager 2009; Lee et al. 2011; Madhusudhan et al. 2011a; Benneke & Seager 2012, 2013; Line et al. 2012, 2013, 2014; de Wit & Seager 2013; Waldmann et al. 2015a, 2015b). These tools enable us to fully map the likelihood space of atmospheric models and to place upper limits and constraints on the abundances of molecules and temperature profiles.

The lack of high signal-to-noise ratio and broad wavelength coverage observations has, however, led current retrievals and forward models to make several assumptions and approximations to reduce the parameter space. The forward model included in most retrieval methods is a 1D radiative transfer model (Brown 2001; Liou 2002; Seager 2011; Tinetti et al. 2012; Hollis et al. 2013), implementing opacity cross sections for the major molecular absorbers, Rayleigh scattering, and collision-induced absorption. Transmission spectra are usually retrieved assuming constant-with-altitude temperature and molecular abundances. This might be a fair approximation when probing narrow wavelength ranges, but can lead to significant biases when larger wavelength ranges are probed. One of the pressing questions we are facing today is whether these assumptions will still be valid in the era of *JWST*.

In this paper, we aim to address these issues. We study the biases and degeneracies of atmospheric retrievals of high-quality, broad wavelength range transmission spectra of hot Jupiters, such as those that will be obtained with instruments on board *JWST*. We apply and compare different retrieval approaches to synthetic observations for a range of hot atmospheres with different C/O computed using photochemical models, and we study the biases of common assumptions used in today's retrievals.

This study aims at answering the following questions:

(a) Are our retrieval approaches and forward models appropriate for the high signal-to-noise ratio and broader wavelength range spectra expected from future facilities such as *JWST*?

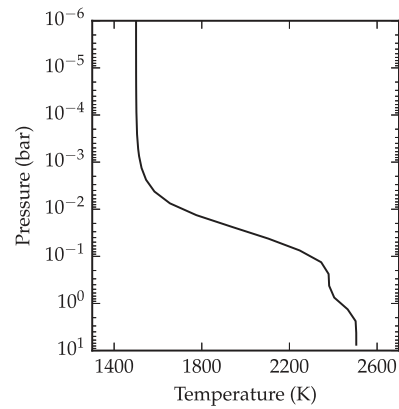(b) Can we confidently retrieve absolute molecular abundances and infer the C/O ratio?

Figure 1. TP profile used for the atmospheres under study.

In Section 2 we describe the chemical and radiative transfer models used to generate the synthetic transmission spectra. We also present the *JWST* synthetic observations and describe the two retrieval approaches used to interpret these synthetic observations. In Section 3 we describe qualitatively the simulated transmission spectra and present the results of the retrievals. In Section 4 we discuss our results, and in Section 5 we summarize the main conclusions of this study.

2. METHOD

2.1. Chemical Models

The 1D atmospheric chemical models were generated using the photochemical model developed for hot atmospheres (Venot et al. 2012, and references therein). These models have been used to study exoplanets (Agúndez et al. 2014; Venot et al. 2014, 2015; Venot & Agúndez 2015; Tsiaras et al. 2016), as well as solar system giant planets (Cavalié et al. 2014; Mousis et al. 2014). The chemical scheme has been developed with combustion specialists and validated in a wide range of pressures (0.001–100 bars) and temperatures (300–2500 K), making this model one of the currently most reliable chemical schemes (Battin-Leclerc et al. 2006; Bounaceur et al. 2007; Anderlohr et al. 2010; Wang et al. 2010). Venot et al. (2015) showed that the use of more complete chemical models, including species with up to six carbon atoms, has little effect on the synthetic spectra. We therefore used the simpler, and computationally faster, scheme that includes species with up to four carbon atoms and is able to model the kinetic behavior of species with up to two carbon atoms. This scheme includes 105 neutral species and 960 reactions (and their reverse reactions). We used a constant diffusion coefficient, $K_{zz} = 10^8 \, cm^2 \, s^{-1}$, due to the uncertainties on the vertical mixing acting in exoplanet atmospheres. A similar value has been often used in the literature (Lewis et al. 2010; Line et al. 2011; Moses et al. 2011; Venot et al. 2013). We note, however, that this value might be too high, as pointed out by Parmentier et al. (2013).

We used a temperature–pressure (TP) profile with a high-altitude temperature of 1500 K. The vertical profile is the same as the one used in Venot et al. (2015). It was computed using the analytical model of Parmentier & Guillot (2014), using coefficients from Parmentier et al. (2015) and the opacities from Valencia et al. (2013). The profile, shown in Figure 1, was obtained by setting the irradiation temperature to 2300 K and the internal temperature $T_{int} = 100$ K. We assumed a planet with $R_p = 1.162 \, _J$ and $M_p = 1.138 \, M_J$.

We computed chemical models for an atmosphere of solar metallicity with C/O of 0.5, 0.7, 0.9, 1.0, 1.1, 1.3, and 1.5.

2.2. Synthetic High-resolution Transmission Spectra

High-resolution ($R \approx 10{,}000$) synthetic transmission spectra were computed using the forward models included in TauREx (Waldmann et al. 2015b). This forward model is based on a 1D radiative transfer model that calculates the optical path through the planetary atmosphere. It results in a transmission spectrum of transit depth, i.e., $(R_p/R_*)^2$, as a function of wavelength. The temperature profile used is the same as the one used for the computation of the photochemical models (Figure 1). We include a precise computation of the pressure–altitude profile and take into account the effect of gravity, temperature, and mean molecular weight in the computation of the scale height in each of the 100 atmospheric layers included in the model. We compute the pressure grid from 10^{-4} to 10 bars and define the 10 bar pressure radius to be $R_p = 1.162\ R_J$. The mass is set to $M_p = 1.138\ M_J$. Among the 105 molecules considered in the photochemical model, we only consider the following seven molecules in the computation of the opacity in the synthetic spectra: C_2H_2, CH_4, CO, CO_2, H_2O, HCN, and NH_3. We found that among the complete set of 105 molecules contained in the chemical model, these are the most abundant ones in all cases and will therefore dominate the spectral modulation. The wavelength-dependent cross sections for these absorbing molecules were computed using line lists from ExoMol (Barber et al. 2006, 2014; Harris et al. 2006; Yurchenko et al. 2011, 2013; Tennyson & Yurchenko 2012), HITRAN (Rothman et al. 2013), and HITEMP (Rothman et al. 2010). Note that the mean molecular weight of each atmospheric layer is coupled to the mixing ratio of all 105 molecules. We included additional opacity from Rayleigh scattering of H_2 and from collision-induced absorption of He and H_2–H_2 and H_2–He pairs (Richard et al. 2012).

2.3. JWST Spectra

We simulated spectra for the Near-Infrared Imager and Slitless Spectrograph (NIRISS) in Single-Object Slitless Spectroscopy (SOSS) mode using the GR700XD optics (Doyon et al. 2012). We applied a lower-wavelength cutoff at 1 μm to avoid saturation and a long-wavelength cutoff at 2.5 μm to avoid spectral contamination (Greene et al. 2016). We then used the Near Infrared Camera (NIRCam) using the long-wavelength (LW) channel and the F322W2 and F444W filters, covering the 2.5–3.9 μm and 3.9–5.0 μm spectral ranges, respectively (Greene et al. 2007). An alternative could be the use of the Near-Infrared Spectrograph (NIRSpec) in its high-resolution mode with the two instrumental configurations: F170LP/G235H (1.7–3.1 μm) and F290LP/G395H (2.9–5.2 μm) (Ferruit et al. 2014). Finally, we use the Mid-Infrared Instrument (MIRI) to cover the 5.0–10.0 μm wavelength range. We use MIRI in slitless mode, using the Low Resolution Spectrometer (LRS), and we apply a long-wavelength cutoff of 10 μm due to the degrading signal-to-noise ratio at longer wavelengths (Kendrew et al. 2015). Each observation covering the full wavelength range of 1–10 μm will therefore require four separate observations. We have considered a 1 hr effective integration time during the transit and the same amount of time on the star alone. For each mode, the same amount of time was used. Table 1 summarizes the instrument modes considered in this study.

The noise in the spectra was calculated taking into account the star photon noise, the zodiacal and telescope background noise (integrated over the entire band pass of the spectrometer for the slitless mode), and the detector dark current and noise. We assumed a star similar to HD 189733. The star spectrum used was generated using the PHOENIX atmosphere star code (Husser et al. 2013). For NIRISS and NIRCAM, we have binned the spectra to a constant spectral resolution of $R = 100$. For such a bright star we realized that we are in fact very close to the limitation from systematics of the *JWST*. Such systematics are difficult to assess, but we can reasonably assume that they will be lower than *HST*. Given the latest performances achieved with *HST* (e.g., Tsiaras et al. 2016), we can anticipate that the systematics for NIRISS and NIRCAM will be better than about 20 ppm. For MIRI, Greene et al. (2016) adopted a value of 50 ppm, and Beichman et al. (2014) took a value of 30 ppm; we have adopted an intermediate value of 40 ppm. An example of a final spectrum is shown in Figure 2.

2.4. Atmospheric Retrieval

The analysis and interpretation of the simulated observed spectra were carried out using TauREx (Waldmann et al. 2015b). Recently, TauREx has been used to model the spectra obtained with the Wide Field Camera 3 on board *HST* for HD 209458b and 55 Cnc e (Tsiaras et al. 2015, 2016).

Two retrieval approaches were used as part of the current study. Both approaches did not assume any prior knowledge on the chemistry, i.e., the absolute abundance of all gases taken into account is fitted independently. The only difference between the two approaches is in the parameterization of the temperature profile:

1. In the first case we assumed an isothermal TP profile. We will refer to this method as "TP-ISO." This approach is the most commonly used when fitting transmission spectra (Irwin et al. 2008; Benneke & Seager 2012; Line et al. 2012) and includes a parameterization of the atmosphere assuming constant-with-altitude mixing ratio and temperature profiles. Crucially, it does not assume any prior on the chemistry of the atmosphere. The free parameters of the retrieval were the absolute abundance of each atmospheric constituent taken into account, the isothermal temperature, the cloud parameters, and the 10 bar pressure radius. The mean molecular weight is coupled to the fitted composition, and we assumed the bulk atmosphere to be formed by a mixture of hydrogen and helium, whose ratio is fixed to the solar value (85% H_2 and 15% He). We assumed uniform priors in log space for the absolute abundances, ranging from 10^{-12} to 1. We assumed uniform priors for the temperature (1300–2500 K) and for the 10 bar radius (1.05–1.28 R_{Jup}). The prior width of the 10 bar radius was determined by assuming a relative uncertainty on R_p of 20% ($R_p = 1.162\ R_J$). Lastly, we fitted the cloud top pressure with a uniform prior in log space (10^{-5}–10 bars). This parameterization resulted in 10 free variables.

2. In the second case, we assumed a more complex TP profile described by five separate parameters. We will refer to this method as "TP-PARAM." Since the
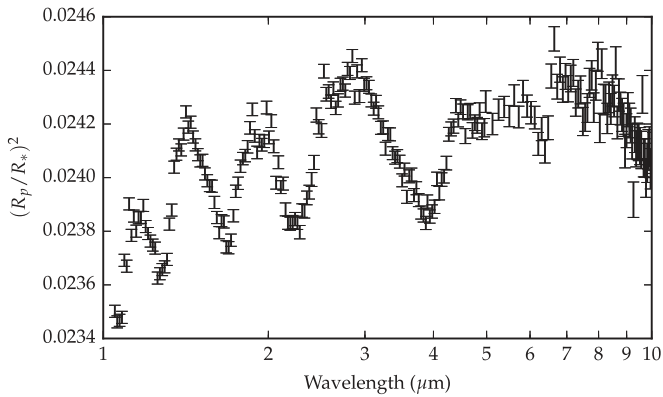
Figure 2. Simulated *JWST* observation for C/O = 0.5. The spectrum was obtained combining four separate synthetic observations obtained with NIRISS, NIRCam, and MIRI to cover the 1–10 μm spectral range. This spectrum would therefore require observing a total of four transits.

Table 1
JWST Instrument Modes

Instrument	Mode	Wavelength Range (μm)
NIRISS	SOSS/GR700XD	1.0–2.5 μm
NIRCam	LW grism/F322W2	2.5–3.9 μm
NIRCam	LW grism/F444W	3.9–5.0 μm
MIRI	Slitless/LRS prism	5.0–10.0 μm

3. RESULTS

3.1. Chemical Models and Transmission Spectra

Figure 3 shows the vertical abundance profiles of seven molecules for all C/O ratios considered in this study, and Figure 4 shows the synthetic transmission spectra and contributions of the major opacity sources for the same C/O values. It can be clearly seen that the chemistry and the resulting spectra change significantly between C/O < 1, C/O = 1, and C/O > 1.

First, we note that while the transmission spectra of an oxygen-rich atmosphere are dominated almost entirely by H_2O, with additional features from CO at 4.6 μm and from CO_2 at 4.3 μm, a carbon-rich atmosphere is dominated by HCN and CH_4, with additional features from CO at 4.6 μm and C_2H_2 at 1.7, 3.0, and 7.5 μm. At the C/O = 1.0 threshold the transmission spectrum is dominated by H_2O and HCN and exhibits strong features of CO at 2.3 and 4.6 μm. Weak features from CH_4 are also seen at 3.4 and 7.6 μm. Tight constraints on the abundances of all these molecules are therefore paramount to constrain the chemistry and C/O of these atmospheres.

Between C/O = 0.5 and 0.9 we see a gradual decrease in the molar fractions of H_2O and CO_2 and a slight increase in the CH_4, HCN, and C_2H_2 abundances, while CO remains relatively constant. The resulting transmission spectra in this C/O range show the progressive decrease in the absorption of H_2O (which remains the dominant absorber across this C/O range) and the resulting emergence of CO, while all the other molecules remain hidden. It is only at C/O > 1.0 that HCN is sufficiently abundant to be clearly seen in the transmission spectrum. We note that at this threshold we see the minimum average absorption from active gases across most of the spectrum, so that in some regions we can also see the emergence of the collision-induced absorption from H_2–H_2 and H_2–He pairs.

At C/O = 1.1 the H_2O and CO_2 content drastically drops, while the abundances of CH_4, HCN, and C_2H_2 increase significantly. The corresponding transmission spectra show features of CH_4, HCN, CO, and C_2H_2. At progressively higher C/O ratios we see the increase in abundance of CH_4, HCN, and C_2H_2 and the progressive decrease of CO abundance. However, we note that the resulting spectra are very similar to each other. The only differences in the spectra are the weakening of CO at 4.6 μm and the strengthening of C_2H_2 at 3 and 7.5 μm.

Finally, we note that C_2H_2 might actually have additional and much stronger features than those seen here. This is because the line list used for this molecule comes from HITRAN and has been computed experimentally at Earth-like temperatures. It is therefore suboptimal to use this line list for such high temperatures (>1500 K). As an appropriate hot line list would include many more transitions resulting from the population of higher vibrational levels, additional spectral features (i.e., "hot bands") are expected, together with the strengthening of the features that can already be seen at lower

temperature profile of the atmospheres under study is highly nonisothermal for pressures greater than 1 mbar (see Figure 1), fitting an isothermal profile might lead to biases. We therefore investigated the effectiveness of fitting a more complex profile using this second method. We used the parameterization of Guillot (2010) modified by Line et al. (2013) and Parmentier & Guillot (2014). There are five parameters that define the temperature profile: the planet internal heat flux (T_{int}), the stellar irradiation flux (T_{irr}), the opacities in the optical and infrared ($\kappa_{\nu1}$, $\kappa_{\nu2}$), and a weighting factor between optical opacities (α). For a full description of this model we refer the reader to Section 3.1 of Line et al. (2013). These five parameters replace the single parameter used for the isothermal profile in the first method. This model only differs from the first one for the type of TP profile used. This parameterization resulted in 14 free variables.

The parameterized profile described above is commonly used in the retrieval of emission spectra, where the spectral features are more sensitive to temperature gradients than in transmission. It has received little attention in the retrieval of transmission spectra, as it is assumed that transmission spectra are much less sensitive to temperature gradients, and therefore isothermal profiles, thought to represent the "average" atmospheric temperature, have always been used. Previous studies have addressed the potential bias of the isothermal assumption (Barstow et al. 2013) and found that some information on the temperature profile could be retrieved in transmission only in the highest signal-to-noise ratio and broad wavelength coverage cases.

We used these two approaches to interpret the synthetic *JWST* observations in a range of C/O. In all cases we used the MultiNest sampling algorithm (Feroz & Hobson 2008) to finely sample the parameter space and obtain the posterior distributions of the model parameters. We chose this method instead of a more classical MCMC, as MultiNest can better map the likelihood of highly degenerate parameter spaces. Table 2 summarizes the free parameters and the corresponding prior widths used in the two retrieval methods.

Table 2
Free Parameters of the Two Retrieval Approaches Used in This Study

Approach	Parameter	Prior	Description
TP-ISO (10 free parameters)	log H_2O, log CO, log CO_2, log CH_4 log NH_3, log HCN, log C_2H_2	$-12 \dots 1$	Molecular abundances
	T_{iso} (K)	$1300 \dots 2600$	Isothermal temperature
	R_p (R_{Jup})	$1.05 \dots 1.28$	Planetary radius at 10 bars
	$\log(P_{top}$ (Pa))	$0 \dots 6$	Cloud top pressure
TP-PARAM (14 free parameters)	log H_2O, log CO, log CO_2, log CH_4 log NH_3, log HCN, log C_2H_2	$-12 \dots 1$	Molecular abundances
	T_{irr} (K)	$1300 \dots 2600$	Stellar flux at the top of the atmosphere
	$\log \kappa_{IR}$	$-4 \dots 1$	Mean infrared opacity
	$\log \kappa_{\nu 1}$, $\log \kappa_{\nu 2}$	$-4 \dots 1$	Optical opacity sources
	α	$0 \dots 1$	Weighting factor for $\kappa_{\nu 1}$ and $\kappa_{\nu 2}$
	R_p (R_{Jup})	$1.05 \dots 1.28$	Planetary radius at 10 bars
	$\log(P_{top}$ (Pa))	$0 \dots 6$	Cloud top pressure

Note. The TP-ISO approach refers to the retrieval using an isothermal TP profile, while the TP-PARAM refers to the retrieval using a parameterized TP profile.
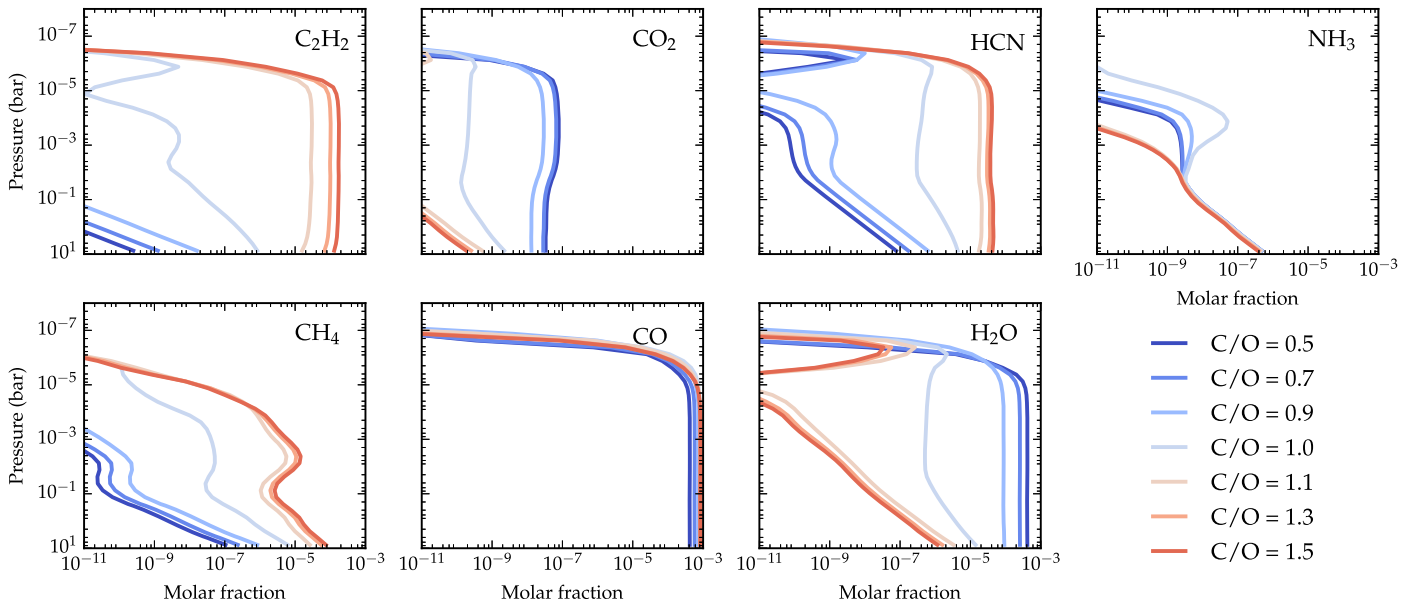

Figure 3. Vertical abundance profiles for different molecules for a range of C/O. The different colored lines show the molar fraction profiles at different C/O, as shown by the legend.

temperatures. Such a list is under development at ExoMol[5] (private communication).

3.2. Retrieval of Temperature Profiles

Figure 5 shows the retrieved temperature profiles using the two approaches for all C/O values. It can be clearly seen that in most cases the retrieved TP profile is within 1σ of the input profile using the TP-PARAM method, while using the TP-ISO method the input profile is almost entirely outside the 1σ retrieved error bars.

For C/O > 1 (first three panels), it can be seen how the TP-PARAM method fits both the upper atmosphere temperature and the lower-altitude part of the atmosphere. We found that the upper atmospheric temperature could be well fitted within about 1σ–3σ using the parameterized TP profile in all cases.

The high-altitude temperature was found to be $T = 1502 \pm 66$ K, $T = 1425 \pm 27$ K, and $T = 1433 \pm 50$ K for C/O = 0.5, 0.7, and 0.9, respectively. Using the TP-ISO method, the retrieved temperatures for the same C/O values were $T = 1572 \pm 14$ K, $T = 1610 \pm 17$ K, and $T = 1716 \pm 24$ K, respectively. In all cases, the input profile has a high-altitude temperature of 1500 K.

From these plots we can also appreciate that the non-isothermal part of the profile could be fitted within 1σ for C/O = 0.5, 0.7, and 0.9. Interestingly, we also note that for C/O < 1 the constraint of the low-altitude temperature ($P > 10^{-3}$ bars) improves for higher C/O, while the fit of the high-altitude part of the profile ($P > 10^{-3}$ bars) improves for lower C/O.

The last three panels in Figure 5 show the retrieved temperature profiles using both approaches for C/O > 1. We can see that the TP-ISO approach retrieves a temperature of
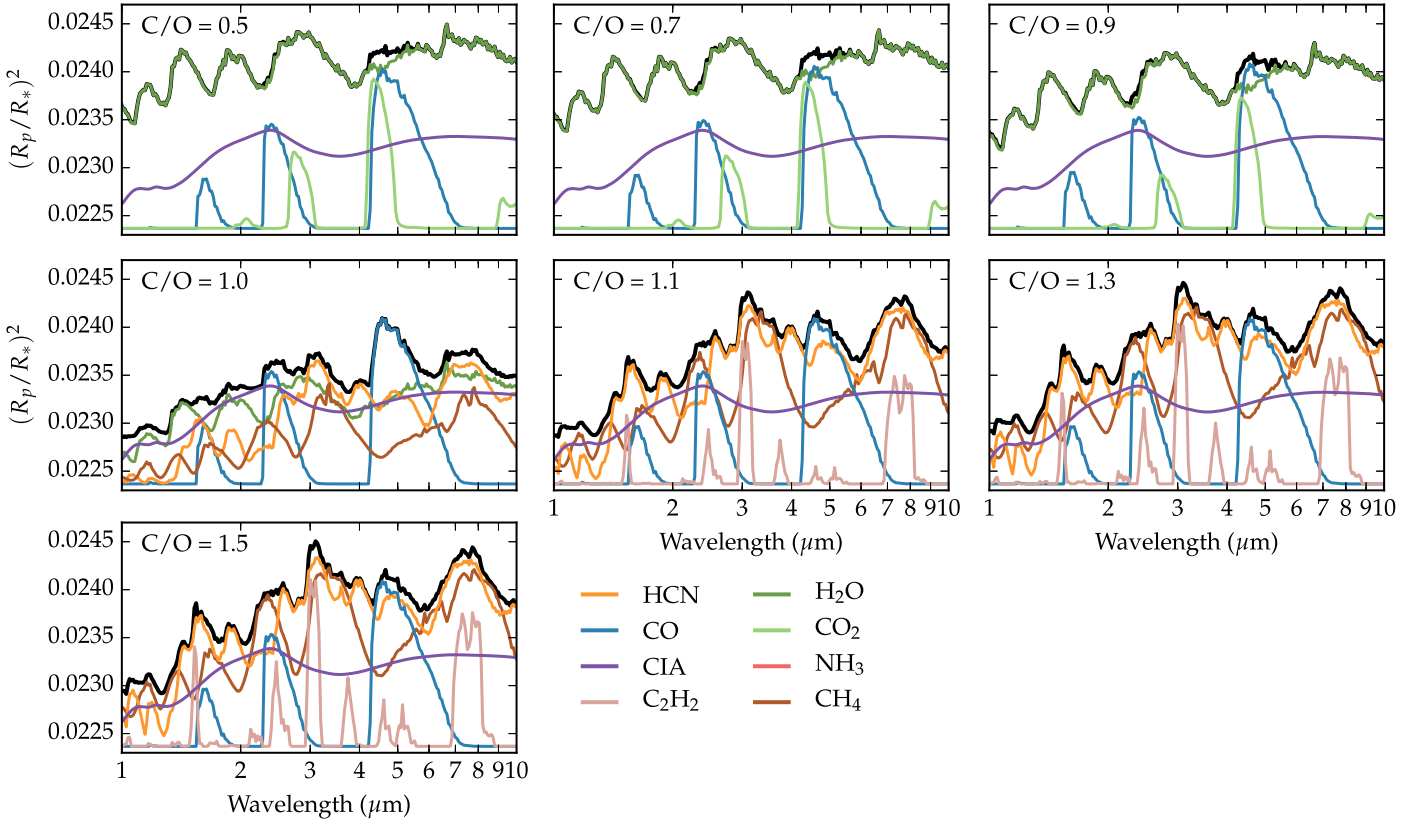
Figure 4. Synthetic transmission spectra (black lines) and contributions of the major opacity sources (colored lines; see legend) for the atmospheres whose chemistry is shown in Figure 3, for different C/O values. The opacity sources include the seven molecules considered in this study and the collision-induced absorption (CIA) from H_2–H_2 and H_2–He pairs. Note that for each plot we only show the major opacity contributors to the spectrum, and we hide the molecules that do not significantly contribute to the transmission spectrum features.
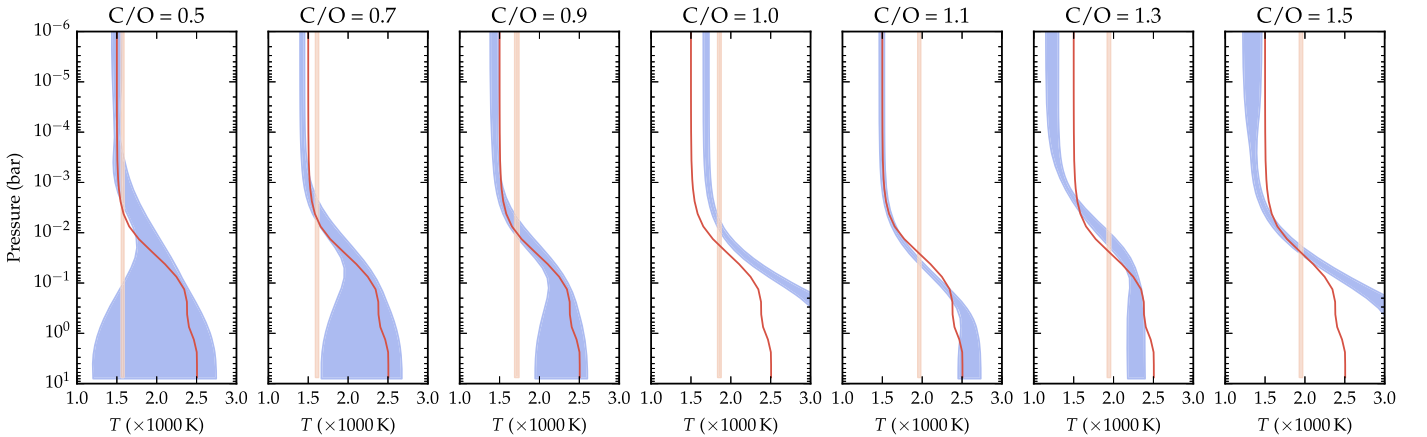

Figure 5. Retrieved temperature profiles for the approach with isothermal profile (pink) and parameterized profile (blue) for different C/O. The red line shows the input profile. The shaded areas show the 1σ confidence level.

$\approx$2000 K, with an uncertainty of $\approx$20 K in all cases. Using the parameterized approach, we could fit the high-altitude temperature within about 1σ for C/O = 1.1 and 1.5 and within 3.4σ for C/O = 1.3. We also note that while the low-altitude part of the TP profile for C/O = 1.1 and 1.3 is well constrained within about 1σ, for C/O = 1.5 the fit is poor for pressures higher than 0.1 bars.

For C/O = 1 we note that the TP profile is poorly retrieved, with the TP-PARAM method giving slightly better results. In both cases, however, the input profile cannot be retrieved within several sigma: the retrieved upper atmosphere

temperature is 6σ and 18σ away from the true state using the TP-PARAM and TP-ISO methods, respectively. Additionally, the lower atmosphere temperature ($P < 0.1$ bars) is not retrieved in both cases.

3.3. Retrieval of Atmospheric Abundances

The atmospheric retrieval results for the atmospheric abundances of H_2O, CO, CO_2, CH_4, HCN, C_2H_2, and NH_3 are shown in Table 3 and in Figures 6 and 7. In these plots, the input mixing ratios for each molecule at each C/O are also shown with solid lines as a function of pressure. We note again

Table 3
Retrieved Absolute Abundances with 1σ Uncertainty for the Seven Molecules and Seven C/O Values Considered in This Study

Parameter	C/O	Input Value (at 0.1 bars)	Retrieved Value	
			TP-ISO	TP-PARAM
H_2O	0.5	4.08×10^{-4}	4.66×10^{-3}–6.53×10^{-3} (15.4)	3.73×10^{-4}–1.98×10^{-2} (1.0)
	0.7	2.52×10^{-4}	2.98×10^{-3}–4.12×10^{-3} (16.2)	1.82×10^{-4}–5.37×10^{-4} (0.4)
	0.9	8.63×10^{-5}	6.61×10^{-4}–8.18×10^{-4} (20.1)	4.84×10^{-5}–9.75×10^{-5} (0.3)
	1.0	1.20×10^{-6}	1.63×10^{-6}–1.94×10^{-6} (4.6)	1.43×10^{-6}–1.62×10^{-6} (4.0)
	1.1	4.56×10^{-8}	$<1.04 \times 10^{-8}$ (1.4)	$<5.44 \times 10^{-12}$ (6.2)
	1.3	2.44×10^{-8}	$<5.13 \times 10^{-9}$ (1.5)	$<2.58 \times 10^{-8}$ (1.1)
	1.5	1.85×10^{-8}	$<5.74 \times 10^{-9}$ (1.3)	$<1.49 \times 10^{-8}$ (0.8)
CO	0.5	4.13×10^{-4}	8.74×10^{-3}–1.10×10^{-2} (28.0)	3.64×10^{-4}–5.33×10^{-2} (0.9)
	0.7	5.70×10^{-4}	9.46×10^{-3}–1.17×10^{-2} (27.0)	2.69×10^{-4}–1.17×10^{-3} (0.0)
	0.9	7.34×10^{-4}	1.15×10^{-2}–1.44×10^{-2} (25.4)	2.90×10^{-4}–7.79×10^{-4} (0.4)
	1.0	8.22×10^{-4}	2.24×10^{-3}–3.38×10^{-3} (5.9)	2.44×10^{-3}–3.40×10^{-3} (7.5)
	1.1	8.24×10^{-4}	7.39×10^{-3}–9.62×10^{-3} (17.6)	1.01×10^{-3}–1.01×10^{-3} (799.1)
	1.3	8.24×10^{-4}	8.35×10^{-3}–1.06×10^{-2} (20.7)	6.33×10^{-4}–1.67×10^{-3} (0.5)
	1.5	8.24×10^{-4}	8.17×10^{-3}–1.03×10^{-2} (20.9)	8.91×10^{-4}–1.26×10^{-3} (1.4)
CO_2	0.5	3.60×10^{-8}	9.46×10^{-7}–1.82×10^{-6} (11.0)	8.63×10^{-8}–4.13×10^{-6} (1.5)
	0.7	3.07×10^{-8}	5.95×10^{-7}–1.14×10^{-6} (10.2)	4.13×10^{-8}–1.27×10^{-7} (1.5)
	0.9	1.35×10^{-8}	1.57×10^{-7}–2.77×10^{-7} (9.6)	1.41×10^{-8}–2.87×10^{-8} (1.1)
	1.0	2.10×10^{-10}	$<2.78 \times 10^{-9}$ (1.1)	$<3.24 \times 10^{-9}$ (0.3)
	1.1	8.01×10^{-12}	$<3.32 \times 10^{-10}$ (0.6)	$<7.64 \times 10^{-10}$ (2.5)
	1.3	4.28×10^{-12}	$<7.23 \times 10^{-10}$ (0.9)	$<8.56 \times 10^{-12}$ (0.4)
	1.5	3.25×10^{-12}	$<4.05 \times 10^{-10}$ (1.0)	$<4.51 \times 10^{-7}$ (1.3)
CH_4	0.5	6.43×10^{-11}	$<1.85 \times 10^{-7}$ (0.6)	$<1.30 \times 10^{-7}$ (0.7)
	0.7	1.44×10^{-10}	$<2.86 \times 10^{-7}$ (0.5)	$<1.97 \times 10^{-8}$ (0.3)
	0.9	5.39×10^{-10}	$<2.03 \times 10^{-8}$ (0.1)	$<7.50 \times 10^{-10}$ (0.5)
	1.0	4.36×10^{-8}	8.48×10^{-8}–1.13×10^{-7} (5.6)	4.61×10^{-8}–6.35×10^{-8} (1.4)
	1.1	1.16×10^{-6}	9.23×10^{-6}–1.15×10^{-5} (20.0)	3.06×10^{-6}–3.06×10^{-6} (43189.6)
	1.3	2.20×10^{-6}	2.03×10^{-5}–2.55×10^{-5} (20.4)	4.85×10^{-6}–8.79×10^{-6} (3.6)
	1.5	2.92×10^{-6}	1.80×10^{-5}–2.22×10^{-5} (18.6)	5.66×10^{-6}–6.57×10^{-6} (10.0)
HCN	0.5	1.32×10^{-9}	$<2.15 \times 10^{-5}$ (0.4)	$<1.15 \times 10^{-7}$ (0.0)
	0.7	2.94×10^{-9}	$<2.94 \times 10^{-7}$ (0.1)	$<2.68 \times 10^{-8}$ (0.4)
	0.9	1.10×10^{-8}	$<5.54 \times 10^{-7}$ (0.3)	$<3.03 \times 10^{-8}$ (0.9)
	1.0	8.84×10^{-7}	6.60×10^{-7}–8.20×10^{-7} (1.7)	5.18×10^{-7}–6.14×10^{-7} (5.3)
	1.1	2.09×10^{-5}	5.53×10^{-5}–6.74×10^{-5} (10.8)	2.18×10^{-5}–2.18×10^{-5} (1355.8)
	1.3	3.58×10^{-5}	1.20×10^{-4}–1.49×10^{-4} (12.1)	3.00×10^{-5}–5.79×10^{-5} (0.5)
	1.5	4.42×10^{-5}	1.01×10^{-4}–1.23×10^{-4} (9.2)	3.47×10^{-5}–4.26×10^{-5} (0.3)
C_2H_2	0.5	8.54×10^{-14}	$<4.18 \times 10^{-7}$ (2.0)	$<9.43 \times 10^{-8}$ (2.2)
	0.7	4.26×10^{-13}	$<5.26 \times 10^{-7}$ (1.6)	$<1.03 \times 10^{-7}$ (1.8)
	0.9	5.96×10^{-12}	$<2.97 \times 10^{-7}$ (1.1)	$<5.24 \times 10^{-7}$ (1.3)
	1.0	3.88×10^{-8}	$<4.08 \times 10^{-9}$ (1.6)	$<4.77 \times 10^{-9}$ (1.6)
	1.1	2.72×10^{-5}	1.66×10^{-4}–2.88×10^{-4} (7.5)	2.51×10^{-5}–2.51×10^{-5} (0.1)
	1.3	9.66×10^{-5}	7.19×10^{-4}–1.17×10^{-3} (9.2)	5.76×10^{-5}–4.44×10^{-4} (0.5)
	1.5	1.68×10^{-4}	9.42×10^{-4}–1.47×10^{-3} (8.7)	1.64×10^{-4}–2.86×10^{-4} (0.9)
NH_3	0.5	9.73×10^{-9}	$<1.04 \times 10^{-7}$ (0.5)	9.74×10^{-12}–3.33×10^{-8} (0.7)
	0.7	9.73×10^{-9}	$<4.43 \times 10^{-7}$ (0.3)	$<1.11 \times 10^{-8}$ (0.9)
	0.9	9.65×10^{-9}	$<3.53 \times 10^{-6}$ (10.9)	$<9.63 \times 10^{-8}$ (0.5)
	1.0	9.62×10^{-9}	$<3.76 \times 10^{-7}$ (1.4)	$<9.12 \times 10^{-8}$ (3.2)
	1.1	8.70×10^{-9}	$<1.80 \times 10^{-6}$ (36.4)	$<2.89 \times 10^{-7}$ (4651.3)
	1.3	7.97×10^{-9}	$<2.02 \times 10^{-6}$ (29.5)	$<5.93 \times 10^{-7}$ (5.6)
	1.5	7.51×10^{-9}	$<2.15 \times 10^{-6}$ (35.7)	$<1.76 \times 10^{-7}$ (1452.3)

Note. For each retrieved parameter, we show in parentheses how many sigma away the retrieved value is from the true state.

that the retrieved abundances are constant with altitude, so that a single parameter is retrieved for each molecule using both the TP-ISO (left panels) and TP-PARAM (right panels) retrieval methods. Moreover, we found that NH_3 is never well retrieved; hence, we do not show its retrieved values in these figures. This is not surprising given that NH_3 is never seen in the simulated transmission spectra (Figure 4).

In general, we found that the TP-ISO method retrieves higher abundances by about one order of magnitude and significantly underestimates the error bars, causing strong biases, while the

TP-PARAM method retrieves the correct true state within 1σ for all atmospheres with C/O greater and less than 1, but not for C/O = 1. This is also because the retrieved error bars are significantly larger.

Looking at the transmission spectra for C/O < 1 in Figure 4, it can be seen that H_2O has multiple features across the entire wavelength range and is therefore the dominant molecule. Indeed, we found that, for these C/O values, the retrieved abundance of H_2O has the smallest uncertainties, but only the approach using the parameterized TP profile gives unbiased
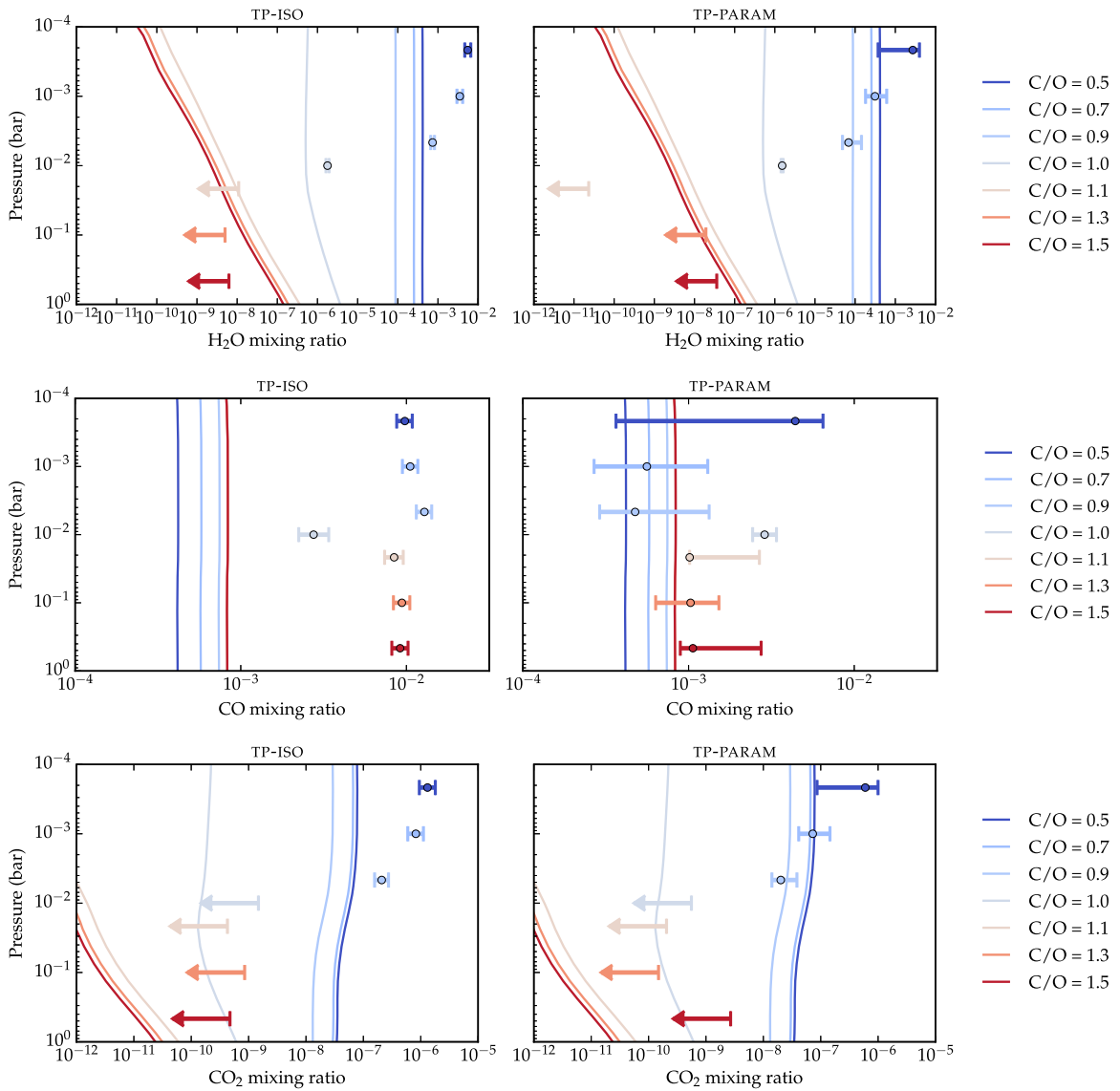
Figure 6. Retrieved H_2O (top), CO (middle), and CO_2 (bottom) abundance for C/O = 0.5–1.5 using the approach with an isothermal profile (left) and that with a parameterized TP profile (right). The solid lines show the input mixing ratio profiles for different C/O, with different colors corresponding to different C/O, as shown by the legend. The retrieved absolute mixing ratios for the different C/O are shown with error bars. Note that we retrieve constant-with-altitude mixing ratio profiles. Note also that the vertical position of the retrieved values is arbitrary.

results. Interestingly, the retrieval method using the isothermal approximation was found to bias the results significantly. For example, for C/O = 0.7 the true abundance for H_2O at 0.1 bars is 2.5×10^{-4} and is relatively constant with altitude. The retrieved abundance using the isothermal approximation was found to be $(3–4) \times 10^{-3}$, and 16σ away from the true value. On the contrary, the retrieved abundance using the parameterized TP profile is $(1.8–6.3) \times 10^{-4}$ and well within 1σ from the true value. For C/O = 0.5 and 0.9 we see similar results: using the TP-PARAM method, the true state is within 1σ–2σ of the retrieved values, but if we use the TP-ISO method, the same retrieved values are 15σ and 20σ away, respectively, from the true state.

The two other molecules that contribute to the spectrum, CO and CO_2, were found to be highly degenerate, but could be retrieved within 1σ–2σ using the TP-PARAM method. Using the TP-ISO method, abundances were, however, overestimated. For CO_2 we found that, using the parameterized TP profile, the true state is within 2σ of the retrieved state for C/O = 0.5 and

within 1.5σ and 1.1σ for C/O = 0.7 and 0.9, respectively. Using the isothermal profile, we obtain retrieved values that are significantly overestimated and are 11.0σ, 10.2σ, and 9.6σ away from the true state for C/O = 0.5, 0.7, and 0.9, respectively. In these hot oxygen-rich atmospheres the retrieved abundances of CO and CO_2 must, however, be interpreted with caution, as both molecules have the only detectable feature in the same wavelength range (≈ 4.0–5.5 μm). From Figure 8, showing the posterior distribution of CO and CO_2 for C/O = 0.7 using the parameterized TP profile, it can be appreciated that the retrieved absolute abundances for these two molecules are highly degenerate. For C/O < 1 no other molecules could be retrieved, and only upper limits could be obtained.

The transmission spectra of these atmospheres with C/O > 1 show that the dominant molecules are CH_4, HCN, C_2H_2, and CO, while all other molecules remain hidden below these stronger absorbers (Figure 4). Only these dominant absorbers could be retrieved, while for all other molecules only
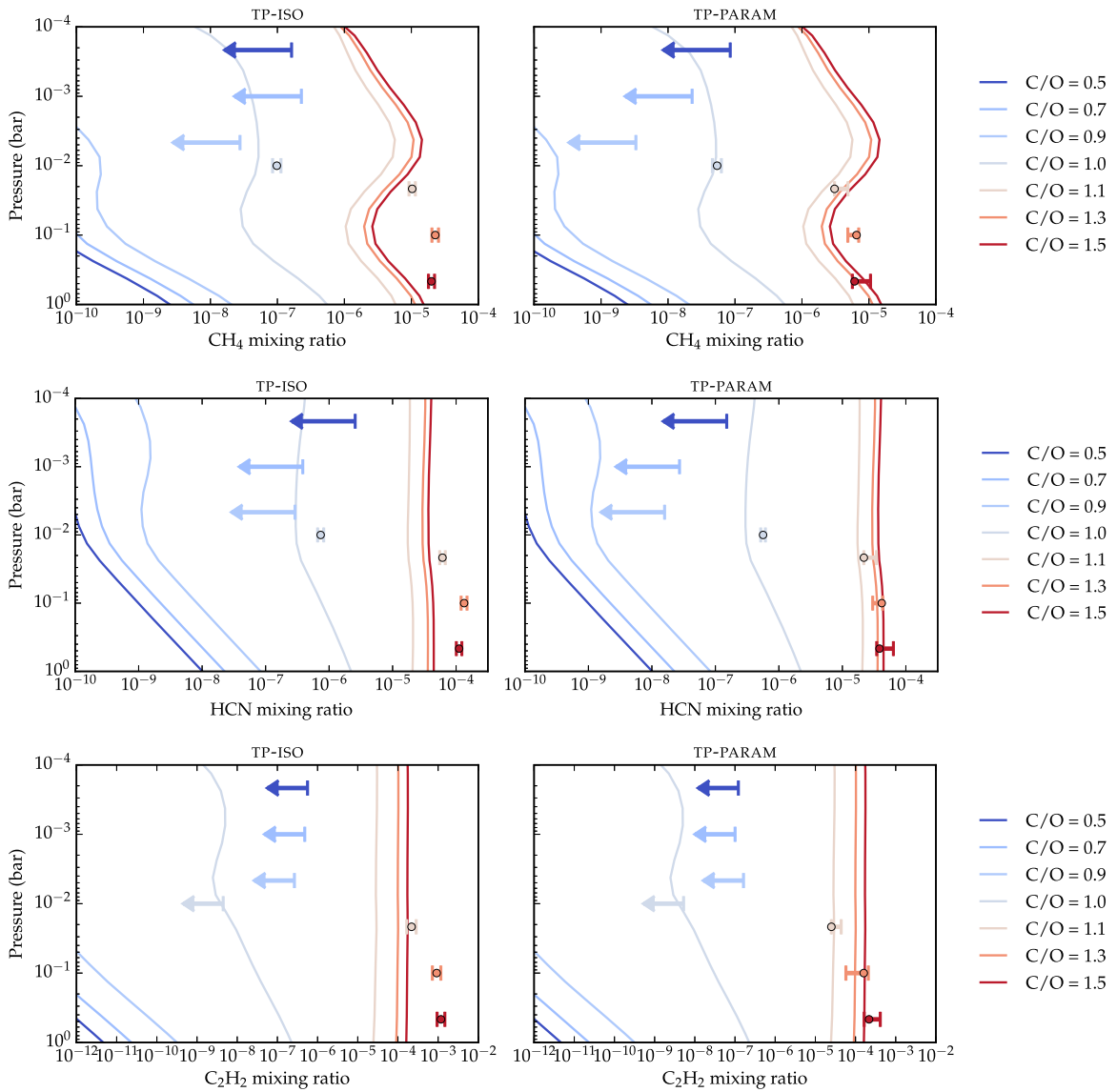
Figure 7. Retrieved CH_4 (top), HCN (middle), and C_2H_2 (bottom) abundance for C/O = 0.5–1.5. Caption as in Figure 6.

upper limits could be placed. We found that also for these carbon-rich atmospheres the TP-PARAM retrieval method gives considerably better results.

Figure 7 shows the retrieved CH_4, HCN, and C_2H_2 abundances. For C/O > 1 we can see that the input abundance profiles change significantly as a function of pressure, especially for CH_4. In the case of CH_4 we found that the TP-ISO method significantly overestimates the abundances. For all C/O > 1 the retrieved abundances are higher than the true abundances at all pressures in the atmosphere. More reasonable results are obtained with the TP-PARAM method, where the retrieved abundances are always between the maximum and minimum true abundance.

For the same carbon-rich atmospheres, the retrieved abundances of HCN and C_2H_2 using the TP-PARAM approach are all within 1σ–2σ of the input abundance, while the values obtained with the TP-ISO are always overestimated by about one order of magnitude and are 8σ–11σ away from the true state. Lastly, we note that the retrieved abundances of CO were within 1σ of the true state using the TP-PARAM method, while the same values are an order of magnitude higher than the true

state and have underestimated error bars when using the TP-ISO method.

This case with C/O = 1 is the most peculiar as many molecules are visible in the spectrum, and their abundance varies significantly as a function of altitude. In the case of H_2O, CO_2, and CH_4 the true abundance profile changes by about one order of magnitude at the typical pressures probed by transmission spectra (10^{-1}–10^{-4} bars; see Figure 3). For H_2O, small differences are seen between the TP-PARAM and TP-ISO methods. The retrieved abundances are $(1.4–1.6) \times 10^{-6}$ in the first case and $(1.6–1.9) \times 10^{-6}$ in the second case, while the input profile varies between 5×10^{-7} and 4×10^{-6} for pressures between 1 and 10^{-4} bars. For carbon monoxide, in both cases the retrieved abundances are overestimated by about one order of magnitude, with values 6σ–7.5σ away from the true state. This is somewhat surprising, considering that the input profile is constant with altitude. For CO_2 the retrieved abundance is within 1σ using the TP-PARAM method and within 2σ using the TP-ISO approach. Finally, for CH_4 and HCN the retrieved abundances are very similar using both methods and are found to be within the maximum and minimum abundances
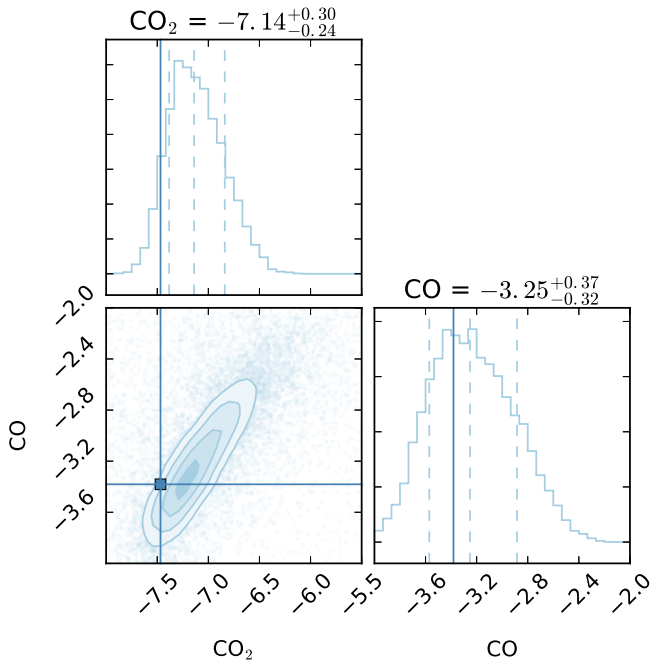
Figure 8. Posterior distributions of CO and CO_2 for C/O = 0.7 for the retrieval approach with a parameterized TP profile. Dashed lines in the histogram plots show the 1σ confidence intervals. The true state (absolute input abundance at 0.1 bars) is shown with a blue square box and straight blue lines. Note that the mixing ratios of these two molecules are approximately constant with altitude in this case, as seen in Figure 3.

of the input profiles, which both vary significantly as a function of altitude.

4. DISCUSSION

4.1. The Impact of Common Approximations

The results presented in the previous section highlight how common assumptions used in current retrieval methods for exoplanets can potentially lead to wrong conclusions.

Strong biases are seen for all C/O ratios, where we see that the isothermal approximation causes in general an over-estimation of the absolute abundances by one order of magnitude and significantly underestimates error bars.

The strongest biases are seen for H_2O, CO, and CO_2 in the C/O < 1 atmospheres, and for HCN, CH_4, and C_2H_2 in the C/O > 1 atmospheres. This is not surprising, given that these are the strongest absorbers for these C/O ranges, and therefore those with the smallest retrieved uncertainties.

For all these atmospheres, excluding C/O = 1, the retrieval method assuming a parameterized TP profile was found to describe the more complex temperature structure of the atmosphere, leading to retrieved values in general agreement with the true state within 1σ on average. This finding opens even new prospects for the use of this technique to characterize exoplanetary atmospheres, showing how high signal-to-noise ratio and broad wavelength coverage transmission spectra can lead to significant constraints on the temperature profiles of the terminator region of hot Jupiter atmospheres.

In general, the retrieval of constant-with-altitude mixing ratio profiles seems sufficient to describe the more complex real profiles when the TP-PARAM approach is used, and it is therefore a fair approximation in most cases. This is especially true for the C/O < 1 atmospheres, where the true profiles of

the most abundant molecules are constant, but it is also true for the C/O > 1 atmospheres, where one of the most abundance molecules, CH_4, has a profile that varies significantly with altitude. The retrieved abundance of this molecule falls within the minimum and maximum true abundance, indicating that the features seen in the transmission spectra at 3.4 and 7.6 μm probe similar pressure regions in the atmosphere.

Retrieved parameters are more strongly affected for the C/O = 1 case, where the biases introduced by assuming a constant-with-altitude abundance profile dominate. Small differences in the retrieved values are seen using the TP-PARAM and TP-ISO methods, and the retrieved results are in both cases several sigma away from the true state. Interestingly, the TP profile retrieved using the TP-PARAM method is also several sigma away from the input profile. This indicates that the biases are driven by the assumption that the abundance profiles are constant with altitude, which is clearly wrong for most molecules. In this case, the different features of the same molecules seen at different wavelengths (e.g., H_2O and CO) probe different regions of the atmosphere, where the abundances can vary significantly. Trying to fit these features using the same abundances throughout the entire atmosphere clearly leads to strong biases. We did not explore here the possibility of fitting a more complex abundance profile for the molecules, but future work in this direction will be required.

The retrieved abundances obtained with the TP-PARAM method will enable placing some limits on the C/O values of the observed atmospheres. First, it will be clearly possible to differentiate between C/O greater or less than unity and C/O = 1, as the spectrum signatures change dramatically at this threshold. Tighter constraints on C/O can be obtained by linking the retrieved absolute abundances with atmospheric chemical models. However, our results indicate that it will be difficult. For C/O < 1, the strongest tracer for C/O is water. Increasingly lower H_2O abundances are expected at increasing C/O, but the differences seen here are rather small and comparable with the retrieved uncertainties (see Figure 6). Similarly, for C/O > 1, the strongest tracers are HCN and C_2H_2 (and, to a lesser extent, CH_4, which has, however, a nonuniform abundance profile). However, even in this case the difference in absolute abundance is quite small and comparable with the error bars of the retrieved values. This is not totally surprising, given that the simulated transmission spectra show very little variation between similar C/O in both the oxygen- and carbon-rich regimes. Higher signal-to-noise ratio observations might further decrease these uncertainties and therefore improve the inferred C/O, but we note that we are already very close to the systematic uncertainties. Other techniques might prove more effective at constraining the C/O ratio, such as emission spectra through secondary eclipse measurements and/ or using chemically consistent retrieval approaches (see, e.g., Greene et al. 2016).

4.2. Understanding the Biases

In order to understand why, and in which scenarios, a nonisothermal profile and constant-with-altitude abundance profiles might lead to strong biases, it is instructive to look at the spectral transmittance as a function of pressure for the atmospheres under study. Figure 9 shows the spectral transmittance integrated over the path parallel to the line of sight as a function of pressure, together with the temperature and scale height profiles. It can be seen that different spectral
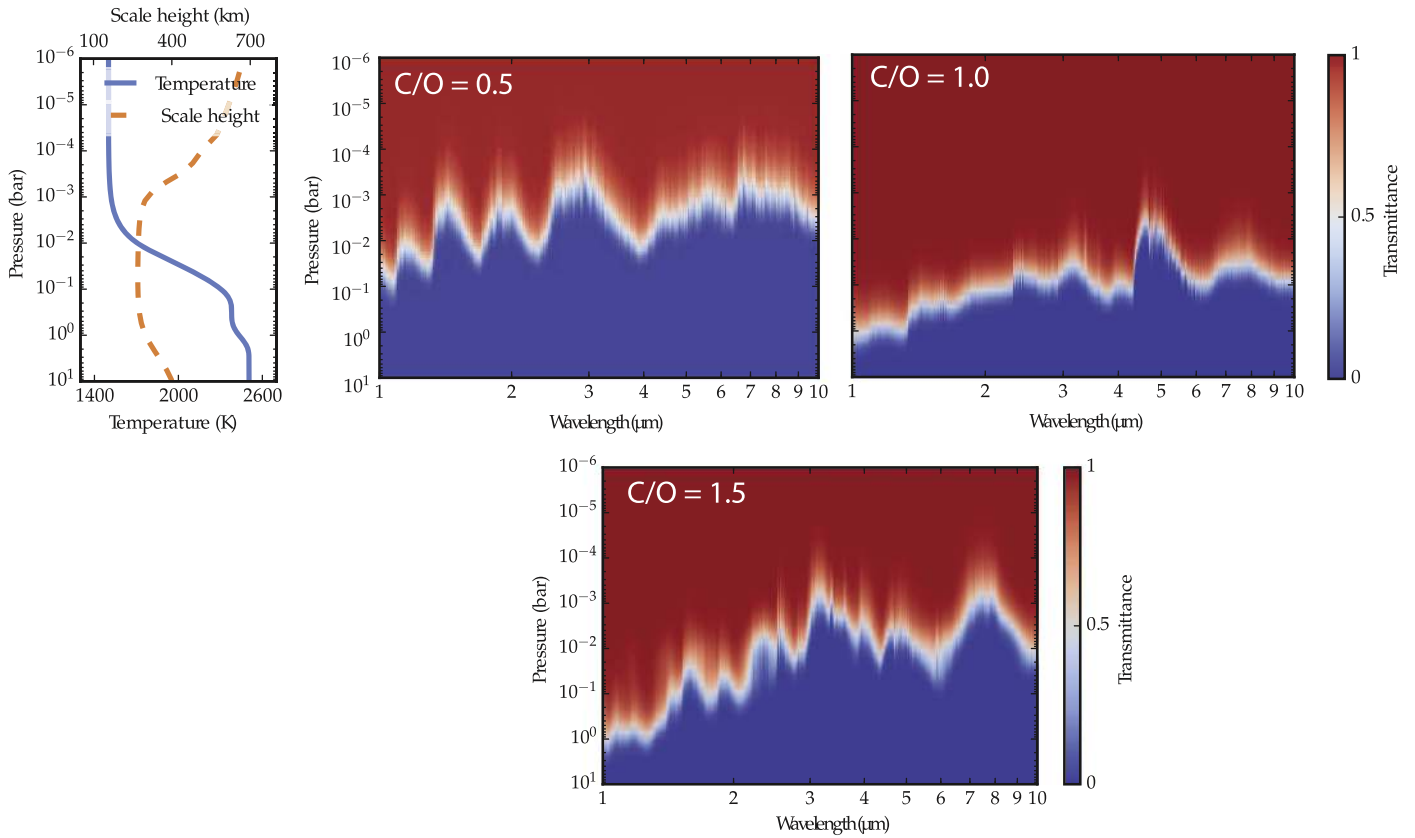
Figure 9. The first plot on the left shows the temperature profile (blue line) and scale height profile (dashed orange line) as a function of pressure. The other panels show the spectral transmittance as a function of pressure for the models with C/O of 0.5, 1.0, and 1.5. Note that the pressure axis is the same as in the first panel. The transmittance is integrated over the path parallel to the line of sight. The transmittance plots allow us to see the pressures (and therefore the temperature and scale height) probed at different wavelengths for different C/O regimes.

regions probe different pressure ranges and therefore different temperatures and scale heights. First, we note that the scale height does not increase exponentially with altitude between 10^{-3} and 1 bar, as one would expect in a purely isothermal atmosphere. On the contrary, the strong temperature gradient seen at these pressures causes the scale height to stay relatively constant at $\approx$200 km. For the atmosphere with C/O = 0.5 we see that most of the absorption occurs between 10^{-4} and 10^{-1} bar, while for the C/O = 1.1 case the transmission spectrum probes higher-pressure regions, from 1 bar to 10^{-3} bars. At these pressures the temperature varies from 1500 to about 2500 K. We also note that the peak of the absorption features probes the higher-altitude and lower-temperature part of the atmospheres, while the troughs probe the regions of the atmosphere that are almost 1000 K hotter.

An isothermal approximation will clearly lead to several problems. First, as we noted before, the scale height of an isothermal atmosphere will increase exponentially, while in this case it is roughly constant with pressure up to 1 mbar. Spectral features that probe different pressures, such as the strong water features seen for C/O < 1, will therefore vary considerably if the scale height is constant with pressure or not. A second, equally important effect is caused by the very different temperatures probed. Molecular opacity cross sections vary considerably between the temperature regions probed here (1500–2500 K), and therefore assuming a single temperature will obviously lead to further biases.

Additionally, Figure 9 helps to explain why for the retrievals of the atmospheres with C/O < 1 we found that the fit of the

low-altitude temperature improves for higher C/O, while that for the high-altitude part of the TP profile improves for lower C/O. As the C/O value increases from 0.5 to 0.9, we see that the water abundance decreases from about 4×10^{-4} to 1×10^{-4}. The effect in the transmission spectrum is a vertical shift toward lower absorption, which also translates into a vertical shift in the transmissivity plot. This means that as the water content drops, we probe increasingly higher pressure regions of the atmospheres, meaning that we increasingly lose information from the upper-altitude part of the atmosphere. This easily explains why the uncertainty on the retrieved upper-altitude temperature of these atmospheres progressively increases, while the constraint of the temperature in the bottom layers improves for higher C/O.

So far we have only considered cloud-free, broad wavelength range observations. This is the case where common approximations are most likely to break down. Shorter wavelength ranges will, for example, tend to probe specific regions of the TP profiles. For instance, an atmosphere with C/O = 1.1 observed between 1 and 3 μm will only probe pressures between 1 and 0.1 bars, where the temperature is roughly constant at $\approx$2400 K. In this scenario, we expect the isothermal approximation to be sufficiently good. However, this is not always the case. If the atmosphere with C/O = 0.5 is observed between 2.5 and 4 μm, we will see a strong water feature with a peak absorption coming from a region with a temperature of about 1500 K, and with wings probing increasingly higher temperatures. Clearly, even in this case an isothermal approximation would give biased results, and our
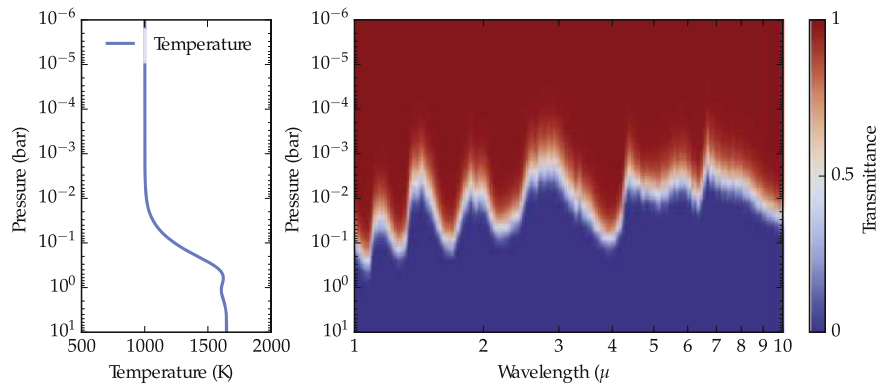
Figure 10. TP profile and spectral transmittance for a planet with a cooler TP profile. Caption as in Figure 9.

study indicates that the retrieved uncertainty of the abundance will be likely underestimated.

The presence of uniform clouds will increase the degeneracy of model parameters, somewhat hiding the underlying biases, as the effect of a cloud deck is that of making the atmosphere opaque. A cloud deck extending to 10 mbars would, for example, make the atmosphere opaque to incoming radiation for pressures higher than 10 mbars. This also means that it will be impossible to probe the temperature and mixing ratio profiles in this pressure regime. In the case under study, the TP profile for pressure lower than 10 mbars is relatively isothermal, and in the presence of clouds, an isothermal approximation would therefore be appropriate. Note, however, that cloud models commonly used in current retrievals were found to cause significant degeneracies. Line & Parmentier (2016) investigated the biases of retrieving a uniform cloud cover in the presence of patchy clouds and found significant degeneracies in the retrieved mean molecular weight.

We also note that similar biases are expected for cooler planets. Figure 10 shows the spectral transmittance as a function of pressure for an atmosphere with a cooler TP profile, with high-altitude temperature of 1000 K. The spectrum was computed from a chemical model with C/O = 0.5 and assuming the same hot Jupiter used in this work. It can be seen that the spectrum probes the range of pressures (10^{-3}–1 bar) where the TP profile changes more significantly. We therefore expect that the use of an isothermal profile to retrieve this spectrum will lead to similar biases to those found for the hotter planet case.

Lastly, we note that this study focused on two specific common assumptions in current retrieval methods, constant mixing ratio and temperature profiles, and the biases that these approximations can lead to. However, other strong assumptions are likely to bias our retrievals. One of the most important ones is to neglect 3D dynamical effects. The simulated observations have in fact been generated using 1D chemical models and assume a uniform chemistry and atmospheric temperature at the terminator region. Further studies that compare transmission spectra obtained with general circulation models and retrieved with the simpler 1D models are needed to address the biases of this assumption. A recent study in this direction is presented in Feng et al. (2016).

5. CONCLUSIONS

In this paper we investigated the biases caused by two common assumptions in the forward models used by current retrieval methods of transmission spectra of hot Jupiter atmospheres: the use of an isothermal profile and constant-with-altitude abundances. We investigated whether these assumptions will still be valid for high signal-to-noise ratio, broad wavelength coverage spectra such as those expected by *JWST*. In order to do this, we simulated high-quality observations using a chemical scheme developed by Venot et al. (2012), which include detailed temperature and abundance profiles, and we retrieved them using two simpler forward models: the first one assumes an isothermal profile (TP-ISO), while the second one assumes a parameterized temperature profile (TP-PARAM). In both cases, constant-with-altitude abundances were retrieved. We found the following:

1. The nonuniform temperature profile could be well retrieved within about 1σ for all cases but C/O = 1 using the TP-PARAM method. This is an important result, opening the possibility to obtain detailed temperature structure information about the terminator region of a hot Jupiter.

2. The retrieval approach that assumes an isothermal profile led to strong biases. We found that, on average, the retrieved abundances using this method are overestimated by about one order of magnitude and the error bars are underestimated. The TP-PARAM approach leads to much improved constraints, with retrieved abundances within 1σ–2σ of the input values in most cases. This is also because the retrieved uncertainties are generally larger.

3. The retrieval assumption that abundance profiles are constant with altitude was found to be a good approximation for C/O < 1 and C/O > 1 atmospheres, but not for C/O = 1. In the latter case, most of the abundance profiles have strong variations, and a uniform abundance profile is a poor approximation that leads to significant biases. Future work will therefore be needed to address the feasibility of fitting more complex abundance profiles.

4. Although we found that differentiating between C/O < 1, C/O = 1, and C/O > 1 was straightforward, we also found that tighter constraints are more difficult to obtain as the differences between the transmission spectra are relatively small. Higher signal-to-noise ratio observations might lead to better constraints, but other biases, due to systematic uncertainties, for example, might become more dominant. Emission spectra observations, possibly combined with transmission spectra, might give better constraints than transmission spectra alone.

These results show that when broad wavelength ranges and high signal-to-noise ratio observations are used, the forward models used in our retrieval approaches need to allow for larger flexibility. One very simple solution is to adopt a parameterization of the TP profile, as the one used here, but other techniques, such as the two-stage approach used in Waldmann et al. (2015a), could be considered in the future.

APPENDIX

REFERENCES

Agúndez, M., Venot, O., Selsis, F., & Iro, N. 2014, ApJ, 781, 68
Ali-Dib, M., Mousis, O., Petit, J.-M., & Lunine, J. I. 2014, ApJ, 785, 125
Anderlohr, J. M., Pires da Cruz, A., Bounaceur, R., & Battin-Leclerc, F. 2010, CST, 182, 39
Barber, R. J., Strange, J. K., Hill, C., et al. 2014, MNRAS, 437, 1828
Barber, R. J., Tennyson, J., Harris, G. J., & Tolchenov, R. N. 2006, MNRAS, 368, 1087
Barstow, J. K., Aigrain, S., Irwin, P. G. J., et al. 2013, MNRAS, 430, 1188
Barstow, J. K., Aigrain, S., Irwin, P. G. J., Kendrew, S., & Fletcher, L. N. 2015, MNRAS, 448, 2546
Barstow, J. K., & Irwin, P. G. J. 2016, MNRAS, 461, L92
Batalha, N., Kalirai, J., Lunine, J., Clampin, M., & Lindler, D. 2015, arXiv:1507.02655
Battin-Leclerc, F., Bounaceur, R., Glaude, P.-A., & Belmekki, N. 2006, arXiv:physics/0603102
Bean, J. L., Desert, J.-M., Seifahrt, A., et al. 2013, ApJ, 771, 108
Beaulieu, J. P., Kipping, D., Batista, V., et al. 2010, MNRAS, 409, 963
Beichman, C., Benneke, B., Knutson, H. A., et al. 2014, PASP, 126, 1134
Benneke, B., & Seager, S. 2012, ApJL, 753, 100
Benneke, B., & Seager, S. 2013, ApJ, 778, 153
Bounaceur, R., Glaude, P. A., Fournet, R., et al. 2007, Int. J. Veh. Des., 44, 1
Brogi, M., de Kok, R. J., Birkby, J. L., Schwarz, H., & Snellen, I. A. G. 2014, A&A, 565, A124
Brown, T. M. 2001, ApJL, 553, 1006
Cavalié, T., Moreno, R., Lellouch, E., et al. 2014, A&A, 562, A33
Charbonneau, D., Brown, T. M., Noyes, R. W., & Gilliland, R. L. 2002, ApJL, 568, 377
Charbonneau, D., Knutson, H. A., Barman, T. S., et al. 2008, ApJ, 686, 1341
Cowan, N. B., Greene, T., Angerhausen, D., et al. 2015, PASP, 127, 311
Danielski, C., Deroo, P., Waldmann, I., et al. 2014, ApJ, 785, 35
Deming, D., Knutson, H. A., Agol, E., et al. 2011, ApJ, 726, 95
de Wit, J., & Seager, S. 2013, Sci, 342, 1473
Doyon, R., Hutchings, J. B., Beaulieu, M., et al. 2012, Proc. SPIE, 8442, 84422R
Feng, Y. K., Line, M. R., Fortney, J., et al. 2016, ApJ, 829, 52
Feroz, F., & Hobson, M. P. 2008, MNRAS, 384, 449
Ferruit, P., Birkmann, S., Böker, T., et al. 2014, Proc. SPIE, 9143, 91430A
Greene, T., Beichman, C., Eisenstein, D., et al. 2007, Proc. SPIE, 6693, 66930G
Greene, T. P., Line, M. R., Montero, C., et al. 2016, ApJ, 817, 17
Grillmair, C. J., Charbonneau, D., Burrows, A., et al. 2007, ApJL, 658, L115
Guillot, T. 2010, A&A, 520, A27
Harris, G. J., Tennyson, J., Kaminsky, B. M., Pavlenko, Y. V., & Jones, H. R. A. 2006, MNRAS, 367, 400

Hollis, M. D. J., Tessenyi, M., & Tinetti, G. 2013, CoPhC, 184, 2351
Husser, T. O., Wende-von Berg, S., Dreizler, S., et al. 2013, A&A, 553, 6
Irwin, P. G. J., Teanby, N. A., De Kok, R., et al. 2008, JQSRT, 109, 1136
Kendrew, S., Scheithauer, S., Bouchet, P., et al. 2015, PASP, 127, 623
Knutson, H. A., Charbonneau, D., Allen, L. E., et al. 2007, Natur, 447, 183
Knutson, H. A., Madhusudhan, N., Cowan, N. B., et al. 2011, ApJ, 735, 27
Kreidberg, L., Bean, J. L., Desert, J.-M., et al. 2014, Natur, 505, 69
Lee, J. M., Fletcher, L. N., & Irwin, P. G. J. 2011, MNRAS, 420, 170
Lewis, N. K., Showman, A. P., Fortney, J., et al. 2010, ApJ, 720, 344
Line, M. R., Fortney, J., Marley, M. S., & Sorahana, S. 2014, ApJ, 793, 33
Line, M. R., & Parmentier, V. 2016, ApJ, 820, 78
Line, M. R., Vasisht, G., Chen, P., Angerhausen, D., & Yung, Y. L. 2011, ApJ, 738, 32
Line, M. R., Wolf, A. S., Zhang, X., et al. 2013, ApJ, 775, 137
Line, M. R., Zhang, X., Vasisht, G., et al. 2012, ApJ, 749, 93
Liou, K. N. 2002, An Introduction to Atmospheric Radiation (New York: Academic Press)
Madhusudhan, N. 2012, ApJ, 758, 36
Madhusudhan, N., Burrows, A., & Currie, T. 2011a, ApJ, 737, 34
Madhusudhan, N., Harrington, J., Stevenson, K. B., et al. 2011b, Natur, 469, 64
Madhusudhan, N., & Seager, S. 2009, ApJ, 707, 24
Moses, J. I., Line, M. R., Visscher, C., et al. 2013a, ApJ, 777, 34
Moses, J. I., Madhusudhan, N., Visscher, C., & Freedman, R. S. 2013b, ApJ, 763, 25
Moses, J. I., Visscher, C., Fortney, J., et al. 2011, ApJL, 737, 15
Mousis, O., Fletcher, L. N., Lebreton, J. P., et al. 2014, P&SS, 104, 29
Öberg, K. I., Murray-Clay, R., & Bergin, E. A. 2011, ApJL, 743, L16
Parmentier, V., & Guillot, T. 2014, A&A, 562, A133
Parmentier, V., Guillot, T., Fortney, J., & Marley, M. S. 2015, A&A, 574, A35
Parmentier, V., Showman, A. P., & Lian, Y. 2013, A&A, 558, A91
Redfield, S., Endl, M., Cochran, W. D., & Koesterke, L. 2008, ApJL, 673, L87
Richard, C., Gordon, I. E., Rothman, L. S., et al. 2012, JQSRT, 113, 1276
Rothman, L. S., Gordon, I. E., Babikov, Y., et al. 2013, JQSRT, 130, 4
Rothman, L. S., Gordon, I. E., Barber, R. J., et al. 2010, JQSRT, 111, 2139
Seager, S. 2011, ConPh, 52, 602
Sing, D. K., Fortney, J., Nikolov, N., et al. 2016, Natur, 529, 59
Snellen, I. A. G., Albrecht, S., de Mooij, E. J. W., & Le Poole, R. S. 2008, A&A, 487, 357
Stevenson, K. B., Harrington, J., Nymeyer, S., et al. 2010, Natur, 464, 1161
Swain, M., Deroo, P., Griffith, C. A., et al. 2010, Natur, 463, 637
Swain, M., Deroo, P., Tinetti, G., et al. 2013, Icar, 225, 432
Tennyson, J., & Yurchenko, S. N. 2012, MNRAS, 425, 21
Thiabaud, A., Marboeuf, U., Alibert, Y., Leya, I., & Mezger, K. 2015, A&A, 580, A30
Tinetti, G., Deroo, P., Swain, M., et al. 2010, ApJL, 712, L139
Tinetti, G., Tennyson, J., Griffith, C. A., & Waldmann, I. 2012, RSPTA, 370, 2749
Tinetti, G., Vidal-Madjar, A., Liang, M.-C., et al. 2007, Natur, 448, 169
Todorov, K. O., Deming, D., Knutson, H. A., et al. 2013, ApJ, 770, 102
Tsiaras, A., Rocchetto, M., Waldmann, I., et al. 2016, ApJ, 820, 99
Tsiaras, A., Waldmann, I., Rocchetto, M., et al. 2015, arXiv:1511.07796
Valencia, D., Guillot, T., Parmentier, V., & Freedman, R. S. 2013, ApJ, 775, 10
Venot, O., & Agúndez, M. 2015, ExA, 40, 469
Venot, O., Agúndez, M., Selsis, F., Tessenyi, M., & Iro, N. 2014, A&A, 562, 51
Venot, O., Fray, N., Bénilan, Y., et al. 2013, A&A, 551, A131
Venot, O., Hébrard, E., Agúndez, M., et al. 2012, A&A, 546, A43
Venot, O., Hébrard, E., Agúndez, M., Decin, L., & Bounaceur, R. 2015, A&A, 577, A33
Waldmann, I., Rocchetto, M., Tinetti, G., et al. 2015b, ApJ, 813, 13
Waldmann, I., Tinetti, G., Drossart, P., et al. 2012, ApJL, 744, 35
Waldmann, I., Tinetti, G., Rocchetto, M., et al. 2015a, ApJ, 802, 107
Wang, H., Warner, S. J., Oehlschlaeger, M. A., et al. 2010, CoFl, 157, 1976
Yurchenko, S. N., Barber, R. J., & Tennyson, J. 2011, MNRAS, 413, 1828
Yurchenko, S. N., Tennyson, J., Barber, R. J., & Thiel, W. 2013, JMoSp, 291, 69
Zellem, R. T., Griffith, C. A., Deroo, P., Swain, M., & Waldmann, I. 2014, ApJ, 796, 48