

## EXTENSIONAL FLOW OF HYALURONIC ACID SOLUTIONS IN AN OPTIMIZED MICROFLUIDIC CROSS-SLOT DEVICE

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### KEY WORDS

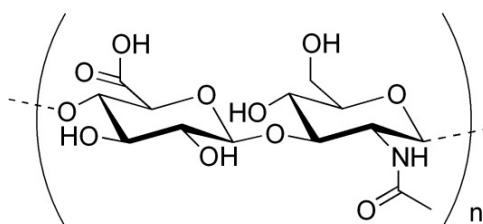
Synovial fluid, non-Newtonian fluid flow, extensional rheology, birefringence, flow velocimetry.

### ABSTRACT

We utilize a recently-developed microfluidic device, the Optimized Shape Cross-slot Extensional Rheometer (OSCER), to study the rheological properties and flow behavior of hyaluronic acid (HA) solutions representative of the synovial fluid (SF) found in the knee joint. The OSCER geometry is a stagnation point device that imposes a planar extensional flow with a homogenous extension rate over a significant length of the inlet and outlet channel axes. Due to the compressive nature of the flow generated along the inlet channels, and the planar elongational flow along the outlet channels, the flow field in the OSCER device is representative of that occurring between the articular cartilage of knee joints during running or jumping movements. Full-field birefringence microscopy measurements demonstrate a high degree of localized macromolecular orientation along streamlines passing close to the stagnation point of the OSCER device, while micro-particle image velocimetry is used to quantify the flow kinematics. The stress-optical rule is used to assess the local extensional viscosity in the elongating fluid elements as a function of the measured deformation rate. The large limiting values of the dimensionless Trouton ratio,  $Tr \sim O(50)$ , demonstrate that these fluids are highly extensional-thickening, providing a clear mechanism for the load-dampening properties of SF. The results also indicate the potential for utilizing the OSCER in screening of physiological SF samples, which will lead to improved understanding of, and therapies for, disease progression in arthritis sufferers.

### 1. INTRODUCTION

Hyaluronic acid (HA) is a naturally occurring linear polysaccharide composed of D-glucuronic acid and N-acetyl-D-glucosamine disaccharide units linked by alternating  $\beta$  1 $\rightarrow$ 3 and  $\beta$  1 $\rightarrow$ 4 glycosidic bonds (see Figure 1) [1, 2].



**Figure 1:** Chemical structure of the hyaluronic acid (HA) molecule.

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Hyaluronic acid is found abundantly in many biological systems and occurs in particularly high concentrations in the vitreous humour of the eyes, umbilical cord, cockerel comb and the synovial fluid (SF) of the joints [3]. In healthy human synovial fluid a broad range of values for the concentration of HA has been measured, ranging generally between around 0.05 and 0.4 wt % [4-6]. The molecular weight of HA in healthy SF can be extremely high and has been reported as reaching more than 7 MDa [7]. The high concentration and molecular weight of the HA in SF confers strong viscoelastic properties to the fluid [8, 9]. Synovial fluid is highly viscous (on the order of 10's to 100's of Pa s) and is strongly shear thinning [10, 11]; a property which contributes to the highly effective lubrication of joints undergoing flexion. Synovial fluid is also highly elastic and it has been suggested that this may be the key to the shock-absorbing properties of SF that protects joints from sudden high-load impacts [12, 13].

Compression of the synovial fluid in the joint cavities (e.g. between the femur and tibia in the knee, when running or landing after a jump) can be considered (in a simplified sense) as essentially a biaxial extensional flow between two compressing disks, with a stagnation point located at the midpoint of the symmetry axis. At the stagnation point the flow velocity is zero, so the residence time in the flow is (in principle) infinite, and under such circumstances macromolecules such as HA can become stretched to a considerable fraction of their contour length providing the extension rate ( $\dot{\epsilon}$ ) exceeds the reciprocal of the longest molecular relaxation time ( $1/\lambda$ ). This condition defines a critical value for the dimensionless flow strength or Weissenberg number,  $Wi = \dot{\epsilon}\lambda = 1$ , above which macromolecules will stretch [14]. This behavior has been demonstrated experimentally in many systems including by observations of fluorescently-labeled DNA [15, 16] and measurements of flow-induced birefringence in synthetic and biological polymer solutions [17, 18]. Due to the very small gaps ( $< 100 \mu\text{m}$ ) between the articular cartilage layers and the short time scales involved in sudden joint impacts, only small deformations are required to generate high values of  $\dot{\epsilon}$ , estimated to range between 1 and  $1000 \text{ s}^{-1}$  in the knee [19]. On the other hand, the high molecular weight of HA and the high viscosity of synovial fluid means the relaxation time,  $\lambda$ , of the HA in SF can be very long ( $0.1 \leq \lambda \leq 1 \text{ s}$ ) [11]. Hence it is highly likely that biologically relevant deformation rates generated within joints can result in high Weissenberg numbers [12, 13]. The stretching of macromolecules in solution can result in orders of magnitude increases in elastic stresses and extensional viscosity [20-22], which presents a mechanism whereby the HA could dramatically thicken the synovial fluid as it compresses, helping to prevent contact between cartilage layers.

In osteo- and rheumatoid arthritis patients, the properties of synovial fluid become degraded, with both the concentration and molecular weight of the HA being significantly altered [4, 6, 7, 23-25] and the viscoelasticity significantly reduced. Monitoring the concentration and molecular weight of HA in SF therefore has potential as a marker for diagnosis of such joint diseases [23]. An important application of commercially produced HA (normally isolated from cockerel combs or produced by bacterial fermentation) is in viscosupplementation of arthritic joints in order to enhance the properties of the diseased SF [3, 26, 27]. Characterizing and understanding the rheological properties of HA in solution is therefore vital for the optimization of this form of therapy and may lead to alternative methods of diagnosis in joint disease. While such rheological studies are numerous for simple shearing flows that are relevant to joint flexion [11, 28-31], detailed studies of extensional flows of HA solutions that are relevant to SF function during joint compression remain very few [11-13, 32].

Backus et al. [13] used an opposed-jets device, in "blowing mode", in order to apply a biaxial extensional flow to solutions of two different high molecular weight HA samples (one linear and one cross-linked) used in viscosupplementation therapy. The fluids displayed a disk of birefringent material situated between the blowing jets, clearly demonstrating the extension of HA molecules in the flow field. Fluids were also tested in a custom-made compression cell, and showed a significant non-linear increase in the normal force response as the compression rate was increased. A cross-slot device was used to obtain a measure of the extensional viscosities of the test fluids, initially showing an increase with deformation rate for  $\dot{\epsilon} \leq 40 \text{ s}^{-1}$ , followed by a reduction in extensional viscosity at higher rates. The reduction in extensional viscosity was attributed to the likely modification of the flow field by the stretching molecules and the consequent loss of the purely extensional flow field in the cross-slot device. The authors did not confirm this hypothesis directly but noted that full visualization of the flow field would have been a highly desirable complementary experiment.

In a very recent study, Bingöl et al. [11] performed comprehensive experiments on HA solutions in a physiological phosphate buffered saline (PBS) using both steady shear in a cone-and-plate rheometer and uniaxial extensional flow in a capillary thinning (CaBER) device. Hyaluronic acid solutions of two molecular weights (1.6 and 4.6 MDa) and a range of concentrations spanning  $0.09 \text{ wt } \% \leq c \leq 0.88 \text{ wt } \%$  were tested, along with 'model' synovial fluid systems consisting of HA mixtures with bovine serum albumin (BSA) and  $\gamma$ -globulin. It has been suggested that complexes formed between HA and the proteins present in SF could play an important role in influencing SF rheological properties [33, 34]. However, Bingöl et al. [11] found no significant differences between the shear and extensional rheological properties of HA solutions with and without the proteins present, and concluded that it is the HA alone that is predominantly responsible for the functional properties of SF. In addition to HA solutions, Bingöl et al. [11] also examined samples of real human SF in shear and extensional flow. They found that a 4.6 MDa HA at a concentration of  $c = 0.3 \text{ wt } \%$  in PBS had shear and extensional rheological properties that compared well with the native SF samples.

A potential limitation of the work of Bingöl et al. [11] is the use of a capillary thinning rheometer to study the extensional properties of HA solutions. In the CaBER device it is not possible to impose a controlled deformation rate to a fluid sample; the fluid simply drains, necks down and eventually breaks up according to its own timescale, determined by a balance between viscous, capillary and elastic stresses [35]. Also, since the CaBER is a free-surface

instrument, hydrophobic molecules can be drawn to the air-liquid interface in the device, modifying the interfacial rheology and potentially affecting measurements by stabilizing the eventual breakup of the fluid filament [36, 37].

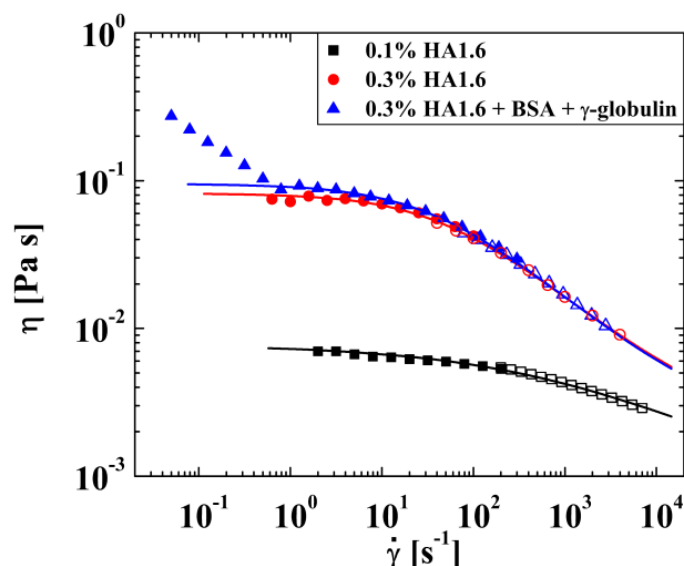
In the present work we examine HA solutions and protein mixtures similar to those studied by Bingöl et al. [11]. However we employ a recently developed microfluidic extensional rheometry device to deduce fluid relaxation times and extensional viscosity behavior as a function of the deformation rate. The microfluidic extensional rheometer is similar to a cross-slot device, but has a profile that has been numerically optimized in order to generate a large region of homogenous pure planar extensional flow [38, 39]. This device allows fluid extensional rheological properties to be measured as a function of the flow strength in a clean and enclosed environment, with no complicating effects due to free-surfaces and using small volumes of fluid ( $O(10 \text{ nL})$ ). Our aim is to understand the extensional properties of HA and its role in joint protection within synovial fluid. This may lead to improved prosthetic fluids and therapies for joint disease, and potentially to a novel disease diagnostic technique. The remainder of the article is organized as follows: in Section 2 we present details of our test fluids and their characterization using standard cone-and-plate rheometric methods as well as high shear rate microfluidic rheometry. In Section 3 we describe our microfluidic extensional flow device and give details of the experimental techniques used to determine fluid relaxation times and extensional viscosities of the HA solutions. In Section 4 we present our results and in Section 5 we summarize our main conclusions.

## 2. TEST FLUIDS AND THEIR RHEOLOGICAL CHARACTERIZATION

The high molecular weight (MW = 1.63 MDa) HA sample used in the study was obtained from Sigma Aldrich and was produced by fermentation of *Streptococcus equi*. For convenience we refer to it as HA1.6 in the remainder of the article. HA solutions were prepared at concentrations of 0.1 wt % and 0.3 wt % in a physiological phosphate buffered saline (PBS, 0.01 M, pH 7.4, obtained from Sigma Aldrich). We also prepared a model synovial fluid formed from a solution of 0.3 wt % HA combined with 1.1 wt % BSA and 0.7 wt %  $\gamma$ -globulin [34]. Light scattering experiments indicate an overlap concentration of  $c^* \approx 0.01 \text{ wt } \%$  for this HA molecule in PBS solution, suggesting that our solutions are in the semi-dilute regime [30].

All of the test solutions were prepared by weighing the HA and protein powders into a glass container and adding the appropriate volume of PBS solution. In order to avoid mechanical degradation of the HA during dissolution, magnetic stirring was avoided; rather occasional gentle manual agitation was applied to the containing vessel until the solution appeared completely transparent and homogenous. This typically took around 36 hours. Following complete dissolution of the sample in the PBS, the fluid was tested without delay (i.e. within the subsequent 12 hours) to determine the rheological and extensional flow properties.

The test solutions were characterized by steady shear experiments in an AR-G2 stress-controlled rheometer with a 40 mm diameter 2° cone-and-plate fixture. To access higher shear rates ( $100 \text{ s}^{-1} < \dot{\gamma} < 10000 \text{ s}^{-1}$ ) a microfluidic shear rheometer was used (m-VROC, Rheosense Inc, CA [40]). The results of the experiments are presented in Figure 2.



**Figure 2:** Steady shear viscosity of HA/PBS solutions measured using an AR-G2 stress-controlled cone-and-plate rheometer (closed symbols) and an m-VROC microfluidic rheometer (open symbols). The viscosity is well-described by a Carreau-Yasuda model (solid lines), except for the fluid containing BSA and  $\gamma$ -globulin at low shear rates.

In the absence of added protein, the steady shear rheology presented in Figure 2 is in good agreement with that of previous authors using microbial HA solutions of comparable molecular weight and concentration under equivalent solvent conditions [11, 29, 30]. The fluids display a zero-shear-rate viscosity plateau ( $\eta_0$ ) and are shear-thinning.

Increasing the HA concentration from 0.1 wt % to 0.3 wt % results in a significant increase in  $\eta_0$  and in a more pronounced shear-thinning behavior. Addition of 1.1 wt % BSA and 0.7 wt %  $\gamma$ -globulin to the 0.3 wt % HA solution, appears to have little effect on the fluid rheology except at low shear rates, where an additional region of strong shear-thinning is observed. Such behavior was also reported by Oates et al. [33] using a concentric cylinder geometry and was attributed to complexation between the HA and protein resulting in the formation of a weak gel. However, Bingöl et al. [11] observed no such phenomenon in a 60 mm diameter 1° cone-and-plate geometry. The fact that the observation of this phenomenon depends on the flow geometry employed suggests that it may be due to an interfacial, as opposed to a bulk, property of the fluid [37, 41] and we intend to investigate this possibility further in future work. In general, the fluid steady shear viscosity is well described by the Carreau-Yasuda model [42]:

$$\eta = \eta_\infty + (\eta_0 - \eta_\infty) \left[ 1 + (\dot{\gamma}/\dot{\gamma}^*)^a \right]^{(n-1)/a}, \quad (1)$$

where  $\eta_\infty$  is the infinite-shear-rate viscosity,  $\eta_0$  is the zero-shear-rate viscosity,  $\dot{\gamma}^*$  is the characteristic shear rate for the onset of shear-thinning,  $n$  is the “power-law exponent” and  $a$  is a dimensionless fitting parameter that influences the sharpness of the transition from a constant shear viscosity at low shear rates to the power-law region. The values of these parameters determined for all the test fluids are provided in Table 1.

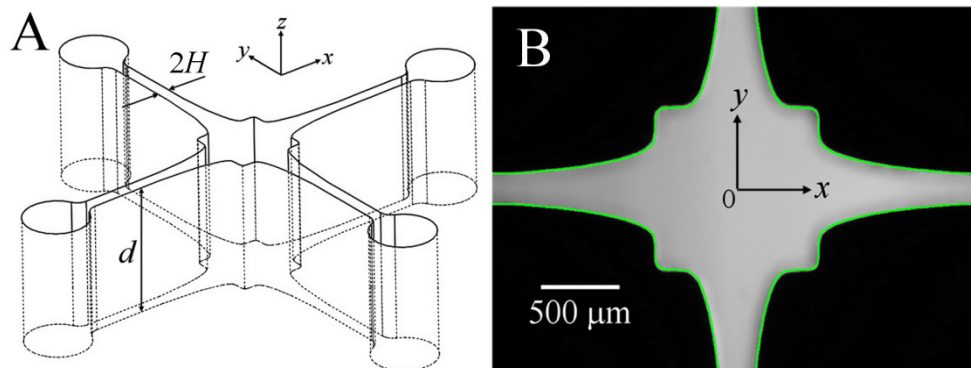
HA1.6 Concentration (wt %)	$\eta_0$ (Pa s)	$\eta_\infty$ (Pa s)	$\dot{\gamma}^*$ ( $s^{-1}$ )	$n$	$a$
0.1	0.0073	0.001	200	0.68	0.60
0.3	0.082	0.002	50	0.45	0.75
0.3 + BSA + $\gamma$ -globulin	0.097	0.0021	45	0.42	0.72

**Table 1:** Parameters used to fit the Carreau-Yasuda model to the steady shear rheology data.

### 3. EXPERIMENTAL METHODS

#### 3.1 Extensional Flow Apparatus

We refer to the microfluidic device used to generate the extensional flow field as the Optimized Shape Cross-slot Extensional Rheometer (OSCER). The OSCER geometry operates on principles similar to traditional cross-slots (i.e. with opposed inlets and outlets to generate a stagnation point [15, 18]), but has an optimized shape that achieves a homogeneous strain rate along a significant portion of the inlet and outlet channel axes [38, 39]. A 3D drawing and a photograph of the actual flow geometry are provided in Figure 3.



**Figure 3:** (A) 3D view of the OSCER geometry showing the upstream and downstream characteristic channel dimension  $H$  and the uniform depth  $d$ . (B) Light micrograph of the actual OSCER geometry. The inflow is along the  $y$ - and the outflow along the  $x$ -direction. At the center of the geometry there is a stagnation point, here marked as the origin of coordinates. The superimposed green line represents the prescribed profile determined from numerical optimization.

The OSCER device was precision micro-machined from stainless steel using the technique of wire electrical discharge machining (EDM). It has initially parallel channels upstream and downstream of the stagnation point, with a characteristic dimension of  $H = 100 \mu\text{m}$ , and a uniform depth of  $d = 2100 \mu\text{m}$ , providing a high aspect ratio of  $\alpha = 10.5$  and hence a good approximation to a 2D flow. The geometry is optimized over the central  $3 \text{ mm}$  ( $30H$ ) section of the device, i.e.  $\pm 15H$  either side of the stagnation point in both the  $x$ - and  $y$  directions. The extensional deformation rate (or strain rate,  $\dot{\epsilon}$ ) has been shown to be nominally constant over this optimized region in both Newtonian fluids and viscoelastic polymer solutions [39].

Experiments were conducted at controlled total volume flow rates ( $Q$ ) using a Harvard PHD-Ultra syringe pump to drive the flow from a single syringe into both opposing inlets of the OSCER device. We define the superficial flow velocity ( $U$ ) as the average flow velocity in the upstream and downstream parallel sections of channel:  $U = Q/(4Hd)$ .

The homogenous strain rate,  $\dot{\epsilon}$ , on the flow axes depends on the imposed flow velocity and was measured experimentally using micro-particle image velocimetry ( $\mu$ -PIV), see Section 3.2 below.

We define the dimensionless flow strength, or Weissenberg number as:

$$Wi = \dot{\epsilon}\lambda, \quad (2)$$

where  $\lambda$  is the fluid relaxation time, which will be assessed from measurements of flow-induced birefringence in the extensional flow field (see Section 3.3).

The Reynolds number is used to characterize inertial contributions to the flow and is defined as:

$$Re = \frac{\rho U D_h}{\eta(\dot{\gamma})}, \quad (3)$$

where  $\rho \approx 1000 \text{ kg m}^{-3}$  is the fluid density,  $D_h = 4Hd/(2H + d)$  is the hydraulic diameter and  $\eta(\dot{\gamma})$  is the shear-rate dependent viscosity (see Figure 2 and Table 1), evaluated at the characteristic shear rate  $\dot{\gamma} = \sqrt{\text{II}(\dot{\boldsymbol{\gamma}})/2} = 2\dot{\epsilon}$  where  $\text{II}(\dot{\boldsymbol{\gamma}})$  is the second invariant of the shear rate tensor  $\dot{\boldsymbol{\gamma}} = \nabla\mathbf{v} + \nabla\mathbf{v}^T$ . This is valid assuming an ideal planar extensional flow,  $\mathbf{v} = [\dot{\epsilon}x, -\dot{\epsilon}y, 0]$ , within the OSCER device.

## 3.2 Flow Field

### 3.2.1 Flow visualization

To obtain a qualitative impression of the flow field within the OSCER device, the fluid was seeded with 8  $\mu\text{m}$  diameter fluorescent spheres (excitation:emission 520:580 nm,  $c = 0.02 \text{ wt } \%$ ). The flow geometry was placed on the imaging stage of a Nikon Eclipse TE2000-S inverted microscope and was continuously illuminated with a mercury lamp at 532 nm. A  $2 \times 0.06\text{NA}$  objective lens was used to focus on the mid-plane of the flow geometry and streak images were captured using an MV Bluefox  $640 \times 480$  pixel CCD camera set to a long exposure time of 0.25 s.

### 3.2.2 Micro-PIV

For quantitative measurements of the flow kinematics, micro-particle image velocimetry ( $\mu$ -PIV) was performed on test fluid seeded with 1.1  $\mu\text{m}$  diameter fluorescent spheres (excitation:emission 520:580 nm,  $c = 0.02 \text{ wt } \%$ ). A  $4 \times 0.13\text{NA}$  objective was used to focus on the mid-plane of the flow cell. The resulting measurement depth over which microparticles contribute to the determination of the velocity field is approximately 150  $\mu\text{m}$ , or 7 % of the channel depth [43]. The fluid was illuminated by a double-pulsed 532 nm Nd:YAG laser with pulse width  $\delta t = 5 \text{ ns}$ . The fluorescent seed particles absorb the laser light and emit at a longer wavelength. The laser light was filtered out with a G-2A epifluorescent filter, so that only the light emitted by fluorescing particles was transmitted onto a CCD array. A 1.4 megapixel, frame-straddling CCD camera (TSI Instruments, PIV-Cam) was used to capture image pairs with a time separation ( $10 \mu\text{s} < \Delta t < 320 \mu\text{s}$ , depending on the flow rate) chosen to achieve an average particle displacement of approximately four pixels, optimal for subsequent PIV analysis. Image pairs were captured at a rate of approximately four pairs per second. The standard cross-correlation PIV algorithm (TSI insight software), with interrogation areas of  $32 \times 32$  pixels and Nyquist criterion, was used to analyze each image pair. Twenty image pairs were captured and ensemble-averaged in order to obtain full-field velocity maps in the vicinity of the stagnation point. Tecplot 10 software (Amtec Eng. Inc.) was used to extract velocity profiles and hence deformation rates,  $\dot{\epsilon}$ , from the resulting vector fields.

## 3.3 Flow-Induced Birefringence Measurement

The spatial distribution of flow-induced birefringence in the central region of the OSCER device was measured using an ABRIO birefringence imaging system (CRi Inc., MA). Briefly, the cross-slot flow cell is placed on the imaging stage of an inverted microscope (Nikon Eclipse TE 2000-S) and the mid-plane of the flow cell is brought into focus using a  $4 \times 0.13 \text{ NA}$  objective lens. Circularly polarized monochromatic light (wavelength 546 nm) is passed first through the sample, then through a liquid crystal compensator optic and finally onto a CCD array. The CCD camera records five individual frames with the liquid crystal compensator configured in a specific polarization state for each frame. Data processing algorithms described by Shribak and Oldenbourg [44] combine the five individual frames into a single full-field map of retardation and orientation angle. The system can measure the retardation ( $R$ ) to a nominal resolution of approximately 0.02 nm, and has an excellent spatial resolution (projected pixel size approximately 2  $\mu\text{m}$  with a  $4 \times$  objective lens). Assuming 2D flow, the relationship between retardation and birefringence is given by:

$$R = d\Delta n, \quad (4)$$

where  $d$  is the depth of the flow cell and  $\Delta n$  is the birefringence.

The birefringence intensity measured along the stagnation point streamline of the OSCER device can then be used to determine the local extensional viscosity of the fluid ( $\eta_e$ ) using the stress-optical rule (SOR). The SOR states that, for a range of microstructural deformations, the magnitude of the birefringence ( $\Delta n$ ) is directly proportional to the principal stress difference in the fluid ( $\Delta\sigma = \sigma_{xx} - \sigma_{yy}$ ), i.e.:

$$\Delta n = C\Delta\sigma, \quad (5)$$

where the constant of proportionality,  $C$ , is the stress-optical coefficient. For solutions of 1.6 MDa HA in PBS over a concentration range of  $0.22 \text{ wt} \% \leq c \leq 0.88 \text{ wt} \%$ , the stress-optical coefficient has been determined rheo-optically to be  $C = 1.82 \times 10^{-8} \text{ Pa}^{-1}$  [30].

The apparent extensional viscosity follows directly from:

$$\eta_E = \frac{\Delta\sigma}{\dot{\epsilon}} = \frac{\Delta n}{C\dot{\epsilon}}. \quad (6)$$

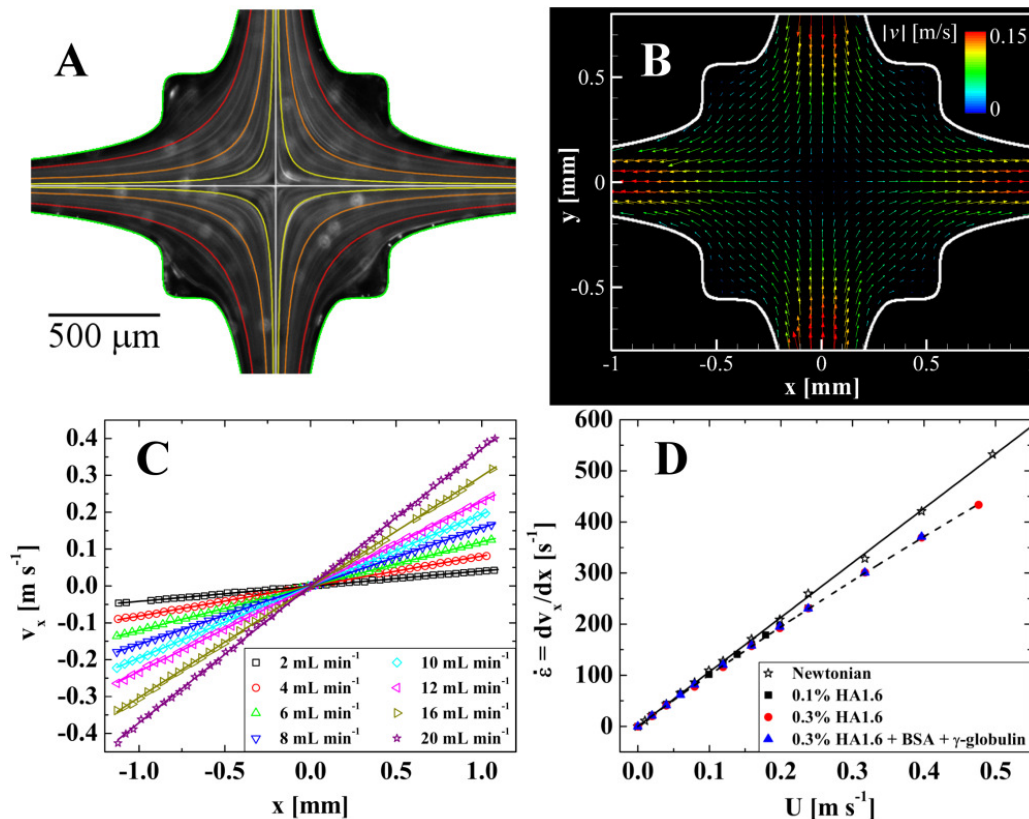
We define the dimensionless Trouton ratio,  $\text{Tr}$ , as the ratio of extensional viscosity to shear viscosity, i.e.:

$$\text{Tr} = \frac{\eta_E(\dot{\epsilon})}{\eta(\dot{\gamma})}, \quad (7)$$

where the shear viscosity,  $\eta$ , is evaluated using the Carreau-Yasuda model fits to the steady shear rheology, evaluated at the characteristic shear rate,  $\dot{\gamma} = 2\dot{\epsilon}$ .

## 4. RESULTS AND DISCUSSION

In Figure 4 we present a detailed experimental analysis of the flow field within the OSCER device. In Figure 4A we show streak imaging performed with a Newtonian fluid consisting of 66 wt% glycerol in water. The fluid viscosity was approximately 13 mPa s and the volume flow rate was  $Q = 0.5 \text{ mL min}^{-1}$ , equivalent to  $U = 0.01 \text{ m s}^{-1}$  and  $\text{Re} \approx 0.1$ . Superimposed in color on the streak image are hyperbolic streamlines (defined by  $y = k/x$ , for a range of  $k$  values) expected for an ideal homogeneous extensional flow, and it is clear that the experimental streamlines broadly follow these hyperbolae. Superimposed in white are the  $x$  and  $y$  axes of symmetry, which clearly converge at the hyperbolic singularity (the stagnation point) at the center of the OSCER geometry.



**Figure 4:** (A) Streak imaging showing the nature of the flow field in the OSCER with a Newtonian fluid at  $U = 0.01 \text{ m s}^{-1}$  ( $\text{Re} \approx 0.1$ ), with superimposed colored hyperbolae for comparison. The superimposed white lines indicate the symmetry axes of the geometry, which coincide at the stagnation point. Flow enters through the top and bottom channels and exits through the left- and right-hand channels. (B) Experimental flow velocity vector field, measured using  $\mu$ -PIV, for an analogue synovial fluid at  $U = 0.2 \text{ m s}^{-1}$  ( $\text{Re} = 2.8$ ,  $\text{Wi} = 3.1$ ). (C) Outflow velocity  $v_x(x)$  measured along  $y = 0$  for the analogue synovial fluid. At any given flow rate  $v_x$  varies linearly with  $x$  and the slope of the straight line provides the elongation rate  $\dot{\epsilon} = \partial v_x / \partial x$  along the exit channel centerline. (D) Elongation rate as a function of superficial flow velocity for HA1.6 solutions in the OSCER, compared with the result for a Newtonian fluid.



In Figure 4B we show a velocity vector field measured using  $\mu$ -PIV in a model synovial fluid consisting of 0.3 wt % HA1.6 with 1.1 wt % BSA and 0.7 wt %  $\gamma$ -globulin. The superficial flow velocity was  $U = 0.2 \text{ m s}^{-1}$  ( $Re = 2.8$ ,  $Wi = 3.1$ ). Here we can see quantitatively how the flow velocity approaches zero at the center of the OSCER device and how fluid elements are stretched continuously as they flow outwards along the  $x$ -direction. Taking a line profile along the  $y = 0$  axis, we can extract  $v_x$  as a function of  $x$ , as shown in Figure 4C for the model synovial fluid over a range of volume flow rates. It is clear that, at each volume flow rate,  $v_x$  varies linearly with  $x$  providing a nominally constant velocity gradient  $\dot{\epsilon} = \partial v_x / \partial x$  along the  $x$ -axis. Such measurements have been made for the Newtonian fluid and all three HA1.6-based test solutions and the results of strain rate,  $\dot{\epsilon}$ , as a function of bulk flow velocity,  $U$ , are shown in Figure 4D. In the Newtonian fluid the strain rate increases linearly with  $U$  as  $\dot{\epsilon} = 1066U$  (with  $U$  in  $\text{m s}^{-1}$ , as shown by the solid line). In the HA solutions at low flow rates the Newtonian trend is obeyed, however at higher flow rates a weak power-law dependency is observed and the strain rate drops slightly, but progressively, below the Newtonian expectation. Consequently, in the HA solutions, the extension rate is better described by  $\dot{\epsilon} = 1066U - 236U^{1.58}$  (shown by the dashed line). Similar behavior was reported by Haward et al. [39] with dilute poly(ethylene oxide) (PEO) solutions and was attributed to the formation of a birefringent elastic strand localized along the outflowing axis. Such flow-induced structures can act as stress boundary layers, causing perturbations to the local flow velocity field and modifying local velocity gradients [45]. However, it is important and interesting to note that this flow perturbation apparently does not affect the spatial homogeneity of the deformation rate measured along the outflow ( $y = 0$ ) axis, as is evident from Figure 4c.

As was seen in PEO solutions, for the HA1.6 solutions we also observe the formation of a localized birefringent strand along the outflowing stagnation point streamline, as shown in Figure 5.

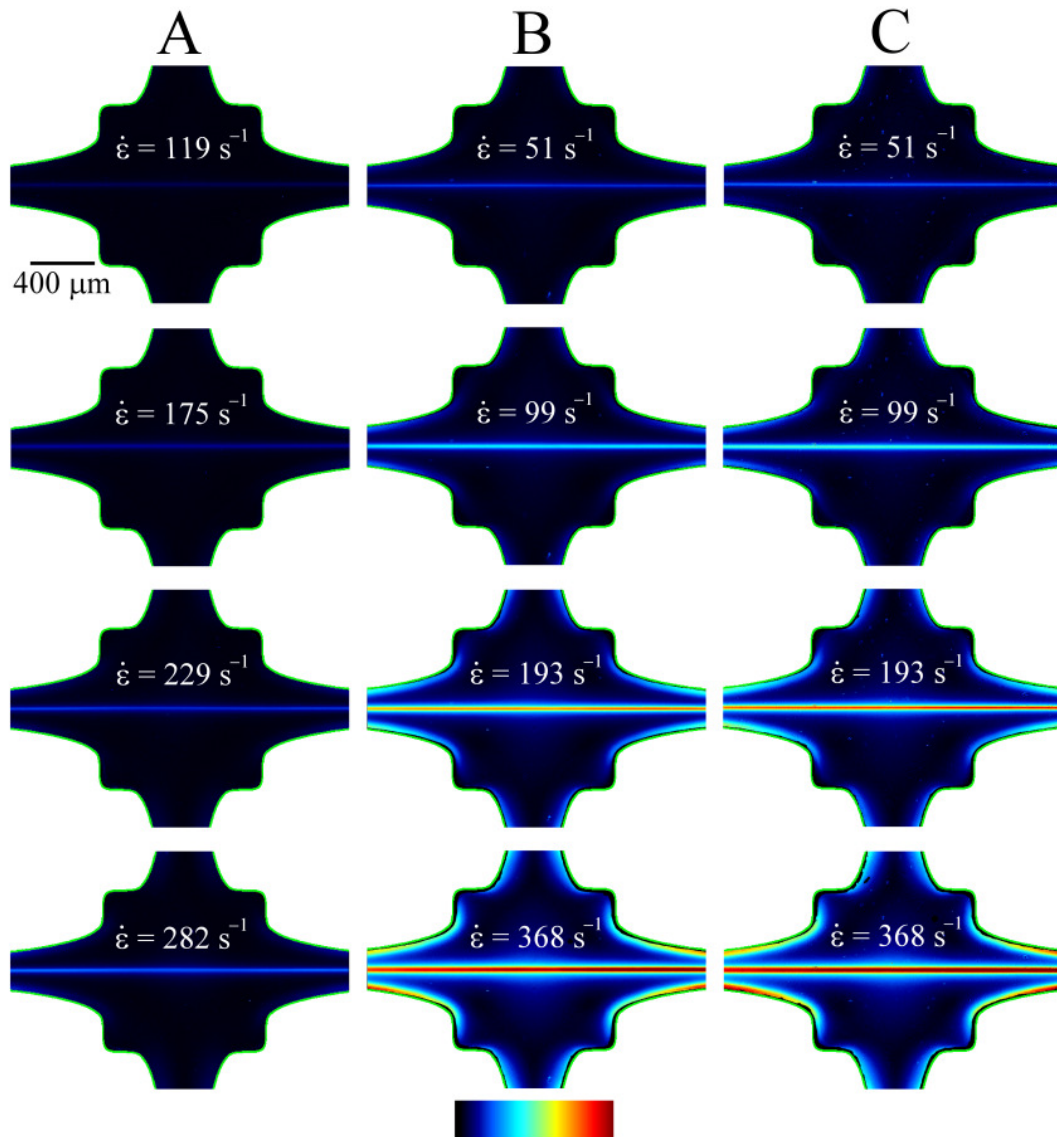
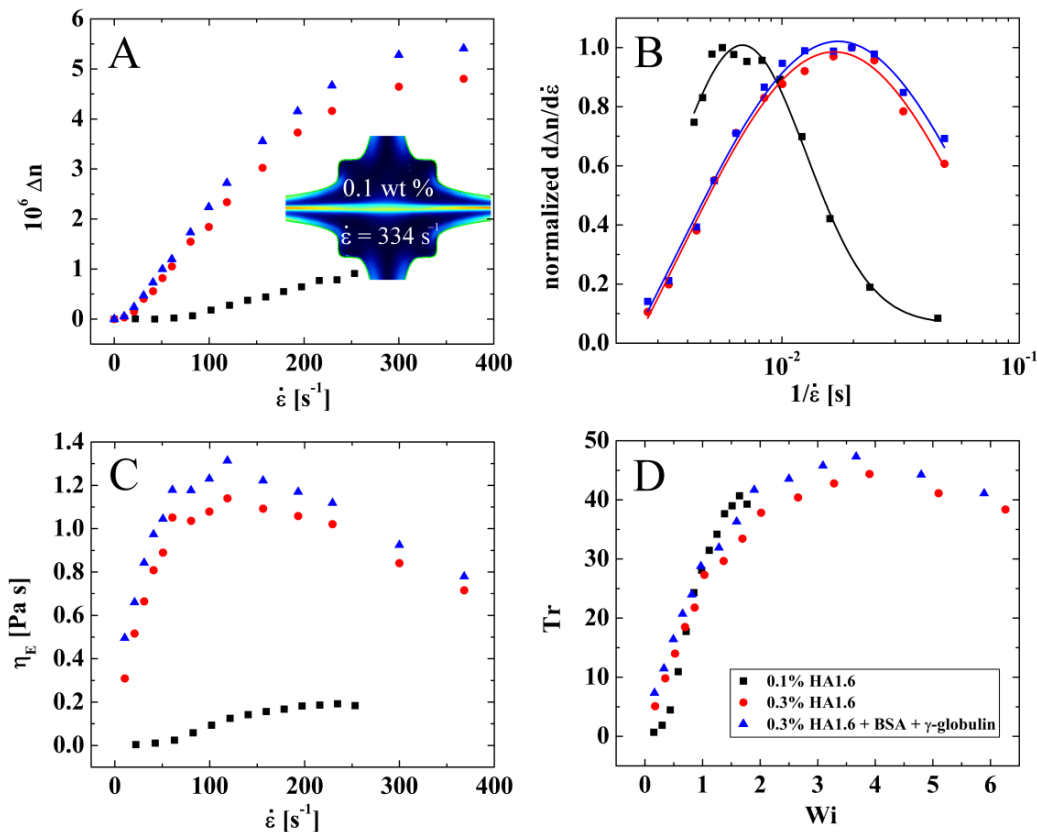


FIG. 5. Flow induced birefringence measured over a range of extension rates in solutions of HA1.6: (A) 0.1 wt %, (B) 0.3 wt %, (C) 0.3 wt % + BSA +  $\gamma$ -globulin. The color scale bar represents retardation in the range  $R = 0 - 10 \text{ nm}$ .

The birefringence microscopy images indicate that significant macromolecular stretching and orientation takes place only along streamlines that pass close to the stagnation point, where the residence times in the high velocity gradient are maximal. The intensity of the birefringence along the  $x$ -axis can be seen to be almost constant, which is a result of the homogenous strain rate along the  $x$ -axis and provides a clear visual demonstration of the strong extensional flow field generated in the OSCER device. The birefringent strands shown in Figure 5 become observable at low strain rates, and increase in intensity as the imposed strain rate is incrementally increased. The fluids with the higher concentration of HA (Figure 5B, C) are significantly more birefringent than the low concentration fluid (Figure 5A), as expected. Qualitatively, for a given strain rate, we observe little difference between the behavior of the two 0.3 wt % HA1.6 fluids with and without added protein.

By measuring the birefringence on the  $x$ -axis (averaging along sections of strands close to the stagnation point), we obtain the birefringence,  $\Delta n$ , as a function of the strain rate for the three HA1.6 solutions, as shown in Figure 6A. In the two 0.3 wt % HA1.6 fluids, with and without added protein, we observe an initial increase in the birefringence at a strain rate of  $\dot{\epsilon} \approx 10 \text{ s}^{-1}$ , up to similar plateau values of  $\Delta n \approx 5 \times 10^{-6}$  at strain rates of  $\dot{\epsilon} \approx 370 \text{ s}^{-1}$ . In the 0.1 wt % HA1.6 solution the initial increase in  $\Delta n$  occurs at a higher value of  $\dot{\epsilon} \approx 80 \text{ s}^{-1}$ , and we are not able to reach a plateau value of birefringence due to the onset of an inertio-elastic instability that distorts the birefringent strand (as shown by the inset birefringence field image in Figure 6A captured at  $\dot{\epsilon} \approx 334 \text{ s}^{-1}$ ).

Since we broadly expect macromolecules to stretch when the characteristic Weissenberg number,  $Wi = \dot{\epsilon} \lambda$ , exceeds unity, i.e.  $Wi_{crit} = \dot{\epsilon}_{crit} \lambda = 1$  [14], it is apparent that we can obtain a characteristic macromolecular relaxation time (or Zimm coil→stretch characteristic time) from the birefringence data by measuring the rate of increase in the birefringence with strain rate and considering  $\lambda = 1/\dot{\epsilon}_{crit}$ . However, this approach is made more complex due to the molecular weight distribution of the HA sample, which results in different molecular weight species within the sample stretching at different values of  $\dot{\epsilon}_{crit}$ , hence the gradual increase of  $\Delta n$ , with strain rate observed in Figure 6A [46]. In fact the birefringence versus strain rate curve can be considered as a cumulative molecular weight distribution.



**Figure 6:** (A) Measured birefringence ( $\Delta n$ ) as a function of the strain rate ( $\dot{\epsilon}$ ) for HA1.6 solutions in the OSCER. In the 0.1 wt % solution the experiment is curtailed at lower  $\dot{\epsilon}$  due to the onset of an inertio-elastic instability that distorts the birefringent strand (as illustrated by the inserted image for  $U = 0.36 \text{ m s}^{-1}$ ,  $Re = 29$ ,  $Wi = 2.4$ ). (B) Derivatives of the curves shown in part (A) (i.e.  $d\Delta n/d\dot{\epsilon}$ , normalized by their maximum values) plotted against  $1/\dot{\epsilon}$ . The data is fitted with log-normal distributions, the peak of which can be used as a measure of the fluid relaxation time ( $\lambda$ ). (C) Extensional viscosity ( $\eta_E$ ) as a function of  $\dot{\epsilon}$ , determined from birefringence measurements using the stress-optical rule. (D) Trouton ratio ( $Tr = \eta_E/\eta$ ) as a function of the Weissenberg number ( $Wi = \dot{\epsilon}\lambda$ ).



By differentiating the curves shown in Figure 6A with respect to  $\dot{\epsilon}$ , and plotting the results as a function of  $1/\dot{\epsilon}$ , we obtain curves which are well described by log-normal distribution functions (see Figure 6B). The variance of the log-normal distributions is indicative of the polydispersity in molecular weight of the HA sample and the peak of the distributions occurs at the critical strain rate at which the peak molecular weight fraction begins to stretch. Therefore we can take the reciprocal strain rate at the peak of the log-normal distribution function as a characteristic relaxation time for the HA1.6 molecule. In the 0.1 wt % HA1.6 solution we find  $\lambda_{0.1} \approx 6.8$  ms, while at the higher concentration of 0.3 wt % HA1.6 we find  $\lambda_{0.3} \approx 16.8$  ms. With the additional protein in the 0.3 wt % HA1.6 solution, we find the relaxation time remains essentially unchanged ( $\lambda_{0.3+BSA} \approx 17.2$  ms). These relaxation times are in excellent agreement with those reported by Bingöl et al. [11] for similar HA solutions using a capillary breakup (CaBER) device. Bingöl et al. [11] reported the relaxation time for HA solutions with added BSA and  $\gamma$ -globulin increased by approximately 20 %; an effect that they attributed to the protein causing a reduction in the surface tension of the fluid. The fact that, in our interface-free microfluidic device, we observe a negligible change in relaxation time on addition of protein to the solution lends support to this hypothesis. The increase in relaxation time from approximately 7 to 17 ms between the 0.1 wt % and 0.3 wt % HA1.6 solutions is consistent with the increase in fluid viscosity and an expected increase in intermolecular interactions, since these fluids are in the semi-dilute regime.

Using the stress-optical rule to convert from birefringence to an extensional viscosity (Equations 5 and 6), we obtain the extensional viscosity versus strain rate curves shown in Figure 6C. In the 0.1 wt % HA1.6 solution, the extensional viscosity increases at a strain rate of approximately  $50 \text{ s}^{-1}$  and rises to a plateau value of around 0.2 Pa s. In the more concentrated HA1.6 solutions, the extensional viscosity begins to increase even from the lowest applied strain rates and rises very rapidly to a maximum value of  $\eta_e \approx 1.2 \text{ Pa s}$  for  $\dot{\epsilon} \approx 120 \text{ s}^{-1}$ , before gradually thinning with further increases in the strain rate. When the extensional viscosity is compared with the steady shear viscosity to obtain the dimensionless Trouton ratio (Equation 7) as a function of  $Wi$ , we find that the data essentially collapse onto a single curve, as shown in Figure 6D. The Trouton ratio reaches a maximum value of  $Tr \approx 50$  for a Weissenberg number of  $Wi \approx 4$ . This is of similar magnitude to the Trouton ratio reported by Bingöl et al. [11] using similar fluids in a CaBER device. Also in agreement with Bingöl et al. [11], in our microfluidic extensional rheometer we find there is only a marginal difference in the extensional response of the fluids with and without added protein, which strongly indicates that it is the hyaluronic acid alone that confers functional viscoelastic properties to synovial fluid.

## 5. CONCLUSIONS

In this work we have demonstrated the application of a recently-developed numerically-optimized microfluidic cross-slot (OSCER) device to test the extensional response of biologically-relevant hyaluronic acid solutions. Analogous formulations of fluids are used for viscosupplementation of the degraded synovial fluid in patients with joint disease, especially in the articular cavity of the knees. Our microfluidic device provides a good model of the flow field within the knee joint as it undergoes compressional and extensional deformations (e.g. during running and jumping activities), in which the synovial fluid is squeezed at high deformation rates (and thus at  $Wi \gg 1$ ). Our birefringence observations and measurements with semi-dilute HA solutions clearly demonstrate that these high molecular weight polysaccharides stretch significantly under such conditions of high flow strength, resulting in a significant increase in the extensional viscosity and in the corresponding dimensionless Trouton ratio. This is likely to represent an important functional aspect of synovial fluid, which allows it to resist compression under high loading rates at short time scales, thus preventing damaging contact from occurring between articular cartilage layers.

In future work, we intend to use the OSCER device to examine HA solutions over a range of molecular weight and concentration, allowing us to obtain the molecular weight dependency of the coil→stretch relaxation time and the concentration dependency of the birefringence. This will lead to the possibility of screening small samples of native synovial fluid in order to assess the molecular weight distribution and concentration of the HA, providing minimally-invasive diagnostic techniques for joint diseases.

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