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### F<sup>2</sup>Dock: Fast Fourier Protein-Protein Docking

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### Abstract

The functions of proteins is often realized through their mutual interactions. Determining a relative transformation for a pair of proteins and their conformations which form a stable complex, reproducible in nature, is known as docking. It is an important step in drug design, structure determination and understanding function and structure relationships. In this paper we extend our non-uniform fast Fourier transform docking algorithm to include an adaptive search phase (both translational and rotational) and thereby speed up its execution. We have also implemented a multithreaded version of the adaptive docking algorithm for even faster execution on multicore machines. We call this protein-protein docking code F<sup>2</sup>Dock ( $F^2 = Fast Fourier$ ). We have calibrated F<sup>2</sup>Dock based on an extensive experimental study on a list of benchmark complexes and conclude that F<sup>2</sup>Dock works very well in practice. Though all docking results reported in this paper use shape complementarity and Coulombic potential based scores only, F<sup>2</sup>Dock is structured to incorporate Lennard-Jones potential and re-ranking docking solutions based on desolvation energy.

#### **Index Terms**

Computational Structural Biology; Protein-Protein Interactions; Fast Fourier Methods; Algorithms; Docking; Redocking

### **1** Introduction

Proteins are stable, folded chains of amino acid polymers, and together with lipids (fats and oils), carbohydrates (e.g., sugars) and nucleic acids (DNA and RNA) form the structural and functional building blocks in our cells. Functions of these building blocks, and particularly those of proteins are expressed through their mutual structural interactions. For example, inhibitors bind to enzymes to limit their rate of reaction. Another example is the attachment of immunoglobins to antigens like viruses, in order to signal that these antigens are foreign objects in our cells. Hence the study of protein-protein interactions plays an important role in uderstanding the processes of life [1]. In particular, as the two preceding examples suggest, protein-protein interaction is at the core of structure-based drug design. Though advancements in X-ray crystallography and other imaging techniques have lead to the extraction of near atomic resolution information for numerous individual proteins, the creation, crystallization and imaging of macromolecular complexes, as extensively required for drug design, still remains a difficult task. Flexibility of proteins makes the search for the required conformation through experimentation even more difficult. Hence, the need for fast and robust computational approaches to predicting the structures of protein-protein

interactions is growing[2]. An important step towards understanding protein-protein interactions is *protein-protein docking* which can be defined as computationally finding the best relative transformation and conformation of two proteins that results in a stable complex, reproducible in nature (if one exists). If only large, fairly inflexible proteins are involved, *rigid protein-protein docking* can be performed as an initial step. Rigid docking based on structure alone has shown to be adequate for a range of proteins[3].

There are two main aspects of a docking algorithm:

- 1. scoring or measuring the quality of any given docked complex, and
- 2. searching for the highest scoring or a pool of high quality docking conformations

Shape complementarity along the docked interface is seen to one of the primary measure of docking quality. Other factors which contribute to the formation of stable complexes include electrostatics, hydrophobicity, hydrogen bonds, solvation energy etc. [2], [4]. These, together with shape complementarity are known as *affinity functions*. The docking problem can be viewed as the search for stable minimum energy complexes. The energy function has several major terms.

i.

The *Lennard-Jones* 12-6 dispersion-repulsion potential is given by  $\sum_{i,j} \left( \frac{a_{ij}}{r_{ij}^{1/2}} - \frac{b_{ij}}{r_{ij}^{6}} \right)$ , where  $r_{ij}$  is the distance between two given atoms, and  $a_{ij}$  and  $b_{ij}$  are constants based on atom types.

ii.

The *electrostatic potential* is given by  $\sum_{i,j} \frac{q_i q_j}{\epsilon(r_i)r_i}$ , where  $q_i$  and  $q_j$  are Coulombic charges, and  $\epsilon(r_{ij})$  is a distance dependant dielectric constant. Electrostatics plays a role in long range interaction due to partially charged protein and solvent atoms.

iii. Desolvation energy is defined as the change in energy due to the displacement of solvent molecules from the interface. The desolvation free energy for moving an atom of charge q and radius r from a region of dielectric  $\varepsilon_1$  to a region of dielectric

 $\varepsilon_2$ , is given by  $\frac{q^2}{r} \left( \frac{1}{\varepsilon_1} - \frac{1}{\varepsilon_2} \right)$ . The total desolvation energy is the sum of desolvation energies of individual atoms involved.

**iv.** Docking energy computations also involve change in energy due to hydrophobicity, hydrogen bond formation and conformational changes. Given the affinity functions, and a scoring method, a search is performed over all of transformation and conformation spaces to find where the two given proteins fit best.

Shape based complementarity, coupled with electrostatic compatibility is typically used as an initial step to obtain possible docking sites. These sites are further ranked using other energy terms. The few remaining potential docking sites are then tested using energy minimization routines.

In [5] we described a Non-equispaced Fast Fourier (NFFT) based algorithm for efficiently performing the initial docking search (based on shape and electrostatics complementarity). We presented a sum of Gaussians based model for proteins, and described a new specification of the rigid protein-protein docking problem. Given two proteins *A* and *B* with  $M_A$  and  $M_B$  atoms, respectively, our algorithm spends  $O(max(M_A, M_B) + n^3 \log n + \rho n^3)$  time to find the top  $\rho$  peaks in the docking profile, and *n* is a parameter chosen to satisfy a user required accuracy in the docking profile. We showed that for a summation of Gaussians model for the molecule where atoms are represented as Gaussian kernels,  $n^3$  varies as  $O(max(M_A, M_B))$ . Compared to traditional grid based Fourier docking algorithms, the algorithm was shown to have lower computational complexity and memory requirement.

In this paper we extend our non-uniform fast Fourier transform(NFFT) based docking algorithm to include an adaptive search phase (both translational and rotational) and thus speed up its execution. We have also implemented a multithreaded version of the adaptive docking algorithm for even faster execution on multicore machines. We call this proteinprotein docking code  $F^2$ Dock ( $F^2$  = Fast Fourier). We have calibrated  $F^2$ Dock based on an extensive experimental study on a list of benchmark complexes and conclude that F<sup>2</sup>Dock works very well in practice. Though all docking results reported in this paper use shape complementarity and Coulombic potential based scores only,  $F^2$ Dock is structured to incorporate Lennard-Jones potential and re-ranking docking solutions based on desolvation energy. In our consider three scenarios of pairwise rigid protein-protein docking. The first is known as redocking, where a given complex of two proteins, are first separated, randomly rotated and translated, and then redocked. In this case the top docking solutions are compared with the original complex, and the RMSD (root mean square deviation) error measure computed. The second scenario is known as bound-unbound docking, where one of the two proteins is in the same conformation as in a complex, while the conformation of the second protein is independent and unknown from the one in the complex. Again the RMSD of the solution dockings are computed with respect to the original complex. The third and final docking scenario is the unbound-unbound case, where both proteins are in unknown conformations with respect to those in the complex. All three docking scenarios have the same computational complexity.

The rest of the paper is organized as follows. In Section 2 we include a review of prior work on rigid protein-protein docking. In Section 3 we describe our new algorithm with adaptive translational and rotational search. We include our experimental results with  $F^2$ Dock on ZDock Benchmark Suite 2.0 [6] in Section 4. Finally, in Section 5 we include some concluding remarks and plans for future research.

#### 2 Related Work

There have been a wide range of work on both flexible and rigid-body docking. In this Section we discuss some relevant prior work on rigid-body docking. Please see the technical report on our flexible docking algorithm F<sup>3</sup>Dock [7] for a review of known techniques for docking flexible molecules.

Graph theory based docking methods [8], [9], [10] reduce the shape complementarity based molecular fitting problems into combinatorial search that have well developed algorithms. However, some good potential matches may be ignored during search due to the use of pruning for reducing the cost of combinatorial search. Geometry-based docking methods use a first level assumption that molecules will 'dock' if the receptor and the ligand exhibit very high shape (surface and volume) complementarity. Point-wise spherical approximations, surface normals, etc. have also been considered in characterizing shape complementarity. In [11], [12] spheres are used to represent grooves in one protein and the density of the other. It was later used in a geometric hashing scheme [13], [14], [15], [16], [17], [18] where a search strategy based on matching pairs of consistent spheres, one from each protein was used, instead of a full combinatorial search. In [19] the combinatorial search was reduced to a clique finding problem by considering pairwise distances among atoms. A knob and hole detection and matching algorithm was used in [20], [21] where an optimization is performed using a grid-based double skin layer approach in 2D. We shall further discuss this double skin layer approach later as we use a variation of it in our algorithm. A full 6D grid based search was used in [22] which also provides a method to uniformly sample 3D rotational space. Using geometric features such as pockets, holes, and surface normals, these methods attempt to constrain the search areas to relatively small portions of the receptor's surface. Geometric signatures/feature points were also used in earlier geometry-based docking

methods [13], [23]. However, geometric signature based approaches often have difficulties in dealing with molecular surfaces without notable features such as flat regions. These methods are also quite sensitive to small geometric feature changes, and a large amount of hashing of storage space is needed for complicated ligand/receptor geometries. Some relatively recent surface and 3-D shape matching methods could be customized to improve the efficiency of geometric surface-surface docking. For example, including molecular properties into the scoring function would necessarily move the geometry matching problem to higher than three dimensions. Belongie et al. [24] calculate shape matches by using shape contexts to describe the relation of the shape to a certain point on the shape. Since corresponding points on two similar shapes will have similar shape contexts, the matching problem is reduced to an optimal point pair assignment problem between two shapes. This technique has reduced sensitivity to small variations in the two shapes.

Using some representation of molecular surface boundary (skin), and a correlation/scoring function based on cumulative overlap of characteristic (electron density) functions of molecular shape, rigid docking can be performed by conducting a combinatorial search in a six dimensional parameter space of all possible translations and orientations of a rigid protein relative to another rigid protein. In [25] coarse grids and rotational angles are used to reduce the combinatorics of the search. The combinatorics of possible relative conformations can be reduced by using a priori knowledge of suitable binding site locations on the proteins [3]. Fast Fourier Transforms can be used to speed up the cumulative scoring function computations [25], [3], [26]. The grid based double skin layer approach became the base of many variations and software, e.g., DOT [27], ZDOCK [28], [29], [30] and RDOCK [31]. Hydrogen bonds were used in [32] to reduce the rotational sampling space and improve the scoring function. Spherical harmonics based approached were studied in [33], [34], [26], [35], [36], [37], [38]. We have compared our algorithm to previous grid based Fourier transform and Spherical harmonics approaches in [5].

There have also been other approaches including building webs over the surfaces and matching them using least squares fit [39], a slice based matching scheme [40], mapping surfaces to 2D matrices and detection of matching sub matrices [41] and fixing anchors and searching over other degrees of freedom (TreeDock [42]). A simulated annealing method, by choosing angles in discrete 45 degree steps and translations of 2Å is used in [43] to perform a random walk and dock proteins. In [44], a coarse approximation of the protein is obtained by approximating each residue by a single spheres, and furthermore the 6D docking search space is parameterized by 5 rotations and 1 translation. The 5D rotational space is further sampled using simulated annealing techniques.

#### 3 Algorithm Details

Consider two proteins A and B, with  $M_A$  and  $M_B$  atoms respectively. We represent the molecules using Gaussian kernels, construct double skin layers used for complementary space docking and derive a new model for docking.

#### 3.1 Affinity Functions

The affinity functions are modeled as Radial Basis Functions (RBFs) to facilitate using Fourier transforms to efficiently solve the docking problem.

We use the sum of Gaussian's representation to model our proteins. An atom centered at  $\mathbf{x}_c$ , with a van der Waal's radius of r, is modeled as an isotropic Gaussian kernel:

 $g(\mathbf{x} - \mathbf{x}_c) = e^{-\beta \left(\frac{(\mathbf{x} - \mathbf{x}_c)^2}{r^2} - 1\right)}$ . The decay rate of the kernel is controlled by the blobbiness parameter  $\beta$ . A value of 2.3 is used in the literature [45] to approximate the solvent excluded surface at

an isovalue of 1. By lowering this parameter, we can model molecules at lower resolutions [46].

**3.1.1 Shape Complementarity**—For shape based docking we maximize the overlap of the surface of protein *B* with the complementary space of *A*. The *double skin layer* approach is used here. It was introduced in [21] for 2D, [22] for 3D, sped up using Fast Fourier Transforms in [47], and extended to complex space in [29]. We define two *skin regions*:

- 1. The complementary region of *A*, defined by a *grown skin region*, by introducing a 1-layer of pseudo-atoms on the surface of *A*. Typically each pseudo-atoms has the same radius which is chosen to make its size comparable to that of a solvent molecule.
- 2. The surface skin of B, which is the density function of the set of surface atoms of B.

The atoms of *A* and the inner atoms of *B* form *core regions*. These regions are shown in Figure 1. We use an adaptive grid based algorithm to construct these regions [5].

To maximize skin overlaps and to minimize overlaps of the cores, we assign positive imaginary weights to the core atoms and positive real weights to the skin atoms/pseudoatoms (see Figure 2). An integral of the superposition of the molecules has two real contributions: the core overlaps contribute negatively and the skin overlaps contribute positively. The magnitude of the imaginary part of the integral due to skin-core clashes (caused by psuedo-atom vs atom overlaps) are also non-desirable and assigned a 'smaller' negative weight in the accumulated score.

The weighted sum of Gaussians function definition of a molecule  $P \in \{A,B\}$  with  $M_P$  atoms be expressed as follows:

$$f_p^{SC}(\mathbf{x}) = \sum_{k \in skin(P)} c^{Re} g_k(\mathbf{x} - \mathbf{x}_k) + \sum_{k \in core(P)} c^{Im} g_k(\mathbf{x} - \mathbf{x}_k)$$
$$= \sum_{k=1}^{M_p} c_k g_k(\mathbf{x} - \mathbf{x}_k),$$

where, g is the Gaussian function located at each atom (or pseudo atom) and (SC) stands for shape complementarity. The weights  $\{c_k \in \{c^{Im}, c^{Re}\}, k = 1, ..., M_P\}$  are either positive imaginary or positive real. See also [30] for an extension of shape complementarity to pairwise shape complementarity.

**3.1.2 Electrostatics Interactions**—Similar to the procedure used for shape complementarity, Gabb et. al. [3] have shown how to introduce the electrostatics term. The first protein's electric potential is computed and matched against the charges in the other. This can also be sped up using a Fourier based algorithm. Charge assignments are made

using PDB2PQR [48]). We define two new affinity functions  $f_A^E$  and  $f_B^E$  for molecule A and B, respectively.

$$f_A^E(\mathbf{x}) = \sum_{k=1}^{M_A} q_k \frac{1}{E(\mathbf{x} - \mathbf{x}_k)(\mathbf{x} - \mathbf{x}_k)}$$
  
and  $f_B^E(\mathbf{x}) = \sum_{k=1}^{M_B} q_k \delta(\mathbf{x} - \mathbf{x}_k),$ 

where,  $q_k$  is the Coulombic charge on atom k,  $\delta(\mathbf{x})$  is the Kronecker delta function with value 1 at  $||\mathbf{x}|| = 0$ , and 0 everywhere else, and  $E(\mathbf{x})$  is the distance dependent dielectric constant [3] as given below.

$$E(\mathbf{x}) = \begin{cases} 4 & \text{if } \|\mathbf{x}\| \le 6\text{\AA}, \\ 80 & \text{if } \|\mathbf{x}\| > 8\text{\AA}, \\ 38 \cdot \|\mathbf{x}\| - 224 & \text{otherwise.} \end{cases}$$

#### 3.2 Rigid Docking Model Specification

Let *T* and  $\Delta$  denote the translational and the rotational operators, respectively. If the user considers a potential docking site as one where the overlap potential (plus electrostatics potential if electrostatics interactions are used) is over a threshold  $\tau$ , then the rigid protein-protein docking solution, using our affinity functions definition, is expressed as the set of triplets:

$$\left\{ (\mathbf{t}, \mathbf{r}, s): \left( \begin{array}{c} s = Re\left(F_{A,B}^{SC}(\mathbf{t}, \mathbf{r}) - w_{E} \cdot F_{A,B}^{E}(\mathbf{t}, \mathbf{r})\right) \\ -\frac{w_{EC}}{\sqrt{w_{SS}, w_{CC}}} \cdot Im\left(F_{A,B}^{SC}(\mathbf{t}, \mathbf{r})\right) \end{array} \right) \geq \tau \right\}$$

where,

$$F_{A,B}^{SC}(\mathbf{t},\mathbf{r}) = \int_{\mathbf{x}} f_A^{SC}(\mathbf{x}) T_{\mathbf{t}}(\Delta_{\mathbf{r}}(f_B^{SC}(\mathbf{x}))) d\mathbf{x},$$
  
$$F_{A,B}^{E}(\mathbf{t},\mathbf{r}) = \int_{\mathbf{x}} f_A^{E}(\mathbf{x}) T_{\mathbf{t}}(\Delta_{\mathbf{r}}(f_B^{E}(\mathbf{x}))) d\mathbf{x},$$

 $w_{ss}$  = reward for (unit) skin-skin overlap,

 $w_{cc}$  = penalty for (unit) core-core overlap,

 $w_{sc}$  = penalty for (unit) skin-core overlap, and

 $w_E$  = reward for (unit) charge-complementarity.

This model assumes that each skin atom is assigned a positive real weight of  $c^{Re} = \sqrt{w_{ss}}$ , and each core atom is assigned a positive imaginary weight of  $c^{Im} = \sqrt{w_{cc}}$  (see Figure 2).

#### 3.3 Search

We solve Equation 1 using Fourier series expansions. Shape complementarity scores and electrostatics scores are computed separately, and then combined. For simplicity of exposition, we describe below our search algorithm for the following simpler case where both  $w_{sc}$  and  $w_E$  are set to 0. Generalization to Equation 1 is straight-forward.

$$\left\{ (\mathbf{t}, \mathbf{r}, s) : \left( s = Re\left( F_{A,B}^{SC}(\mathbf{t}, \mathbf{r}) \right) \right) \ge \tau \right\}$$

We express the integral as a sum of compactly supported radial basis functions and provide an adaptive algorithm to search for regions where the scoring function exceeds the threshold provided by the user.

**3.3.1 Fourier Series Expansions**—Any periodic integrable function can be expanded as a Fourier series. For example, a periodic function in [-1/2, 1/2] can be expressed as:

 $q(x) = \sum_{j=-\infty}^{\infty} \omega_j e^{2\pi i j x}, \text{ where the coefficients } \omega_j = \int_{-1/2}^{1/2} q(x) e^{-2\pi i j x} dx. \text{ Let } I_n \text{ denote a 3D grid of integer indices: } \{k: [-n/2..n/2)^3, k \in \mathcal{K}^3\}. \text{ Let us expand the kernel function in its Fourier}$ 

series form:  $g(\mathbf{x} - \mathbf{x}_{k}) = \sum_{\omega \in I_{\infty}} G_{\omega} e^{2\pi i (\mathbf{x} - \mathbf{x}_{k}) \cdot \omega}$ Hence, the affinity function  $f_{p}^{SC}(\mathbf{x}) = \sum_{k=1}^{M_{p}} c_{k}g(\mathbf{x} - \mathbf{x}_{k})$ can be expressed as  $f_{p}^{SC}(\mathbf{x}) = \sum_{k=1}^{M_{p}} c_{k}(\sum_{\omega \in I_{\infty}} G_{\omega} e^{2\pi i (\mathbf{x} - \mathbf{x}_{k}) \cdot \omega})$ . Rearranging terms, we obtain:  $f_{p}^{SC}(\mathbf{x}) = \sum_{\omega \in I_{\infty}} G_{\omega} e^{2\pi i \mathbf{x} \cdot \omega} \sum_{k=1}^{M_{p}} c_{k} e^{-2\pi i \mathbf{x}_{k} \cdot \omega}$ . Let us denote the second terms by  $C_{\omega}$ . Hence,  $f_{p}^{SC}(\mathbf{x}) = \sum_{\omega \in I_{\infty}} G_{\omega} C_{\omega} e^{2\pi i \mathbf{x} \cdot \omega}$ . Similarly:  $f_{p}^{SC}(\mathbf{x} - \mathbf{y}) = \sum_{\omega \in I_{\infty}} G_{\omega} C_{\omega} e^{2\pi i (\mathbf{x} - \mathbf{y}) \cdot \omega}$ .

Expanding  $f_A^{SC}$  and  $f_B^{SC}$  using the above series, for a given rotation **r**, with the molecules scaled to lie in  $\pi^3 = (-0.5..0.5]^3$  for simpler mathematical notation, the scoring integral in Equation 2 reduces to

$$\forall \mathbf{x}: \int_{\mathbf{y} \in \pi^3} f_A^{SC}(\mathbf{y}) (\Delta_{\mathbf{r}}(f_B^{SC}))(\mathbf{x} - \mathbf{y}) d\mathbf{y}$$

$$= \int_{\mathbf{y} \in \pi^3} \sum_{\omega_A \in I_{\infty}} G_{\omega_A} C_{\omega_A} e^{2\pi i \mathbf{y} \cdot \omega_A} \sum_{\omega_B \in I_{\infty}} G_{\omega_B} C'_{\omega_B} e^{2\pi i (\mathbf{x} - \mathbf{y}) \cdot \omega_B} d\mathbf{y}$$

 $\int_{\omega \in I_{\infty}}^{1/2} e^{2\pi i y(a-b)} = 1$ Since -1/2 if a = b and 0 otherwise, the integral reduces to  $\sum_{\omega \in I_{\infty}} G_{\omega}^2 C_{\omega} C'_{\omega} e^{2\pi i x \cdot \omega}$ .

**3.3.2 Approximations**—We make three approximations in computing the above coefficients. Since the truncated Gaussian is a decaying kernel, we choose to compute only the first  $(-n/2..n/2]^3$  Fourier coefficients. The parameter *n* is chosen to satisfy a user required accuracy in the docking profile. If we include electrostatics, the decay should be even slower, and hence, the same bounds derived for shape complementarity should be sufficient. The current analysis, though, is based on shape complementarity. The Fourier

coefficients of the atoms centers,  $C_{\omega}$ ,  $C'_{\omega}$  are approximated as  $\hat{C}_{\omega}$ ,  $\hat{C}'_{\omega}$ , computed using a Nonequispaced Fast Fourier Transform (NFFT) algorithm given in [49] (Very briefly, the NFFT algorithm computes an approximation to Fourier coefficients when input data is not uniformly sampled). The truncated Gaussian is a tensor product kernel. The Fourier coefficients of the truncated Gaussians are now approximated as the tensor product  $\hat{G}_{\omega}$ .

Hence, we approximate the scoring integral as  $\sum_{\omega \in I_n} \widehat{G}_{\omega}^2 \widehat{C}_{\omega} \widehat{C}_{\omega} e^{2\pi i \mathbf{x} \cdot \omega} = \sum_{\omega \in I_n} \widehat{F}_{\omega} e^{2\pi i \mathbf{x} \cdot \omega}$ .

**3.3.3 Inverse Peak Search**—Given the function  $\widehat{f}(\mathbf{x}) = \sum_{\omega \in I_n} \widehat{F}_{\omega} e^{2\pi i \mathbf{x} \cdot \omega}$ , we are required to compute  $\{(\mathbf{x},s): s = Re(\widehat{f}(\mathbf{x})) \ge \tau\}$ . A 3D IFFT (Inverse nonequispaced fast Fourier transform) of  $\widehat{F}_{\omega}$  yields the docking profile  $\widehat{f}(\mathbf{x})$  at a uniform sampling. If we have prior knowledge on the smoothness of the profile, we can zero pad  $\widehat{F}_{\omega}$  (if necessary) and obtain the profile at a sufficient sampling. This would generally lead to higher computational and memory requirements. Instead, we perform an adaptive computation of  $\widehat{F}_{\omega}$ , progressively zooming in on regions where the threshold  $\tau$  is satisfied. Using the NFFT algorithm in [49], we make the

 $\widehat{f}(\mathbf{x}) \approx \widehat{g}(\mathbf{x}) = \sum_{\mathbf{k} \in I_{\widehat{n},m}(\omega_{\mathbf{j}})} g_{k}\varphi(\omega_{\mathbf{j}} - \mathbf{k}/\widehat{n}), \quad (\mathbf{j} \in I_{n}, \, \widehat{n} = an, \, a \approx 2, \, I_{\widehat{n},m}(\omega_{\mathbf{j}}) = \{\mathbf{l} \in I_{\widehat{n}}: \, \widehat{n}\omega_{\mathbf{j}} - m \le \mathbf{l} \le \widehat{n}\omega_{\mathbf{j}} + m\} ).$  This is schematically represented in 1D in Figure 4. Obtaining regions which are above a certain threshold is now reduced to finding roots of the polynomial  $Re(\hat{g}(\mathbf{x})) = \tau$  If we use a cubic Bspline function for  $\varphi$  with a support width of 5, it requires the root of a  $7 \times 7 \times 7$  system of degree 5 equations. We instead adaptively compute regions which satisfy our docking threshold using an adaptive search algorithm. We initially start with the  $\hat{n}^3$  grid of  $\varphi$  as a set of intervals. We determine using a simple procedure if any interval can potentially contain a value greater than the docking threshold and, if so, subdivide and recursively search the sub intervals. Consider any interval I. There are multiple  $\varphi$  functions whose summation determine the function in I. If we change these  $\varphi$ , such that positive ones centered outside I come closer by one interval width, negative ones shift away from I by one interval width and positive ones centered inside I are given its maximum value, the sum of the new function (called  $\psi$ ) at the interval endpoints defines an upper bound for the original function  $\varphi$  and  $\hat{g}(\mathbf{x})$  inside *I*. This upper bound function yields an approximate profile to our score  $\hat{f}(\mathbf{x})$  and provides us with a test function for determining where to further subdivide and refine an interval as we locate the positive peaks of the scoring function.

The docking score profile is usually large in a thin closed region (as skin-skin overlaps occur in a relatively small subset of 3D space) with zeros on the outside and large negatives on the inside. Hence, in the very first step of the algorithm, a large number of regions are removed from further consideration. We are able to reduce the full 3D inverse FFT of  $\hat{F}_{\omega}$  which yields the docking profile  $\hat{f}(\mathbf{x})$  in the first step of our adaptive search into an inverse FFT of size  $\hat{n}^3$ . This is an efficient way of speeding up the overall inverse peak search algorithm 1. We provide an analysis in 1D, which can be easily extended to 3D. Consider an interval [*i*,*i* + 1], with B-spline functions  $\varphi_k$ , where  $i - m \le k \le i + 1 + m$ , capturing both positive and negative peaks of  $\hat{F}_{\omega}$ . Let the extent of the  $\varphi_k$  be *m* on each side of *k*. We construct a new upper bound function  $\psi_k$  (to construct an approximate scoring profile, by raising the value of  $\varphi_k$  to  $max(\varphi_k, \varphi_{k+1}, \varphi_{k-1})$  on the  $\hat{n}^3$  grid. This gives us the following simple observation:

**Lemma 3.1:** The summation of  $\psi$  values at a point k in the low resolution grid of the Gaussian centers is always greater than the summation of  $\varphi$  values at any point in any interval which includes k.

 $\widehat{f(\mathbf{x})} \approx \widehat{g(\mathbf{x})} = \sum_{\mathbf{k} \in I_{\overline{n},m}(\omega_{\mathbf{j}})} g_k \psi(\omega_{\mathbf{j}} - \mathbf{k}/\widehat{n})$ is a summation of smooth functions, and is now computed over a uniform interval of  $n^3$  points. This summation of smooth functions is equivalent to a convolution of a discretely sampled kernel function  $\psi$  with discrete values of g, namely  $g_k$ . The convolution of  $\psi$  and g is, as is well known, equivalent to the inverse Fourier transform, of the product of the Fourier transforms of  $\psi$  and g respectively and hence computable using 3D FFT in  $O(n^3 \log n)$  as the first step of our algorithm. This initial uniform coarse approximation of the docking profile eliminates most regions outside the overlap of skin and core clashes. Hence, our adaptive search is then

limited to a narrower region where the skin-skin overlaps occur, which yield the maximum positive values to the docking profile.

Figure 3 gives an overview of the adaptive translation search phase of F<sup>2</sup>Dock.

**3.3.4 Rotational Sampling**—For the orientational degrees of freedom we use the optimized and uniform sampling described in [27]. The sampling is based on Euler angles, and the rotations are applied on molecule *B*. Each rotational step is followed by a 3D translational search as described in preceding sections. For 20° of mean rotational spacing the number of samples obtained is 1,800, while for 6° there are 54,000 sample rotations. Rotational search can also be made adaptive as follows. We first perform a low resolution rotational search, say, of mean rotational spacing of  $R_1$ , and retain only those rotations for which translational search yield solutions above a user-specified threshold. Then for each of these retained coarse rotations we perform a finer rotational search, say, of mean rotational spacing of  $R_2 < R_1/4$ , within a cone of angular radius  $R_1/2$  around the coarse rotational space the given threshold during translational search. Such adaptive refinement steps can be repeated with finer and finer rotational samplings until some given level of accuracy is reached.

#### **4 Experimental Results**

We have computed docking predictions for a set of 84 complexes obtained from the ZDock Benchmark Suite 2.0 [6]. For soft docking we first use shape complementarity (i.e. van der Waal's interactions) as the affinity function in scoring. Then we investigate the effects of introducing electrostatics interactions.

We performed three types of docking experiments:

**Bound-bound** (**Redocking**). Both molecules *A* and *B* are taken from the bound complex involving *A* and *B*, and they are then computationally redocked.

**Bound-unbound.** One molecule, say *A*, is taken from the bound complex involving *A* and *B*, and the other one, i.e., *B*, is taken from another known independent structure of *B*.

**Unbound-unbound.** Neither *A* nor *B* is taken from the bound complex involving *A* and *B*, that is, each of them comes from an independent structure that does not include the other molecule.

In all experiments, we measured the quality of our docking solution based on its RMSD distance from the known bound structure of the two molecules involved. RMSD was calculated using the  $C_a$  atoms within 5Å of the interface of the bound structure. We used Kabsch's optimal vector alignment algorithm [50], [51] for aligning the two sets of interface atoms during RMSD computation. We had F<sup>2</sup>Dock output the top 50,000 solutions ranked based on the score it assigns to each solution. We claimed a 'hit' if there was a solution with RMSD less than 5 Å among the top 2,000 solutions returned by F<sup>2</sup>Dock. A rotational sampling of 6 degrees was used, and unless specified otherwise, the number of frequencies extracted by FFT is  $32^3$ . Adaptive search was not used for obtaining the results reported in this section.

#### 4.1 Unbound-unbound Docking

Tables 1 and 2 shows the results of running  $F^2$ Dock on the 84 complexes of ZDock Benchmark Suite 2.0 [6] for unbound-unbound docking using shape complementarity only. We used four different sets of weight values given to the skin-skin ( $w_{ss}$ ), core-core ( $w_{cc}$ ) and

skin-core ( $w_{sc}$ ) overlap costs. In the tables 'Rank' is the best rank among all predicted positions whose RMSD from the known bound structure was less than 5Å. 'Good Peaks' is the number of peaks in the predicted set which were less than 5Å RMSD from the known position. In the 'RMSD' column in the tables we report the lowest RMSD among all peaks that were retained. We also list the ZDock results in the last column. ZDock used 6° rotational sampling like F<sup>2</sup>Dock, but retained 54,000 peaks. The RMSD computation procedure is also based on  $C_{\alpha}$  atoms within 5Å of the interface.

We observe from Tables 1 and 2 that the number of hits slightly increased as  $w_{cc}$  is increased from 5 to 10 (with  $w_{ss}$  and  $w_{sc}$  held constant at 1.0 and 0.5, respectively), and increased even further if  $w_{sc}$  is increased from 0.5 to 1.0. However, increasing  $w_{cc}$  further to 20 did not seem to increase the number of hits anymore. Moreover, increasing  $w_{cc}$  from 5 to 10 generally improved the lowest RMSD value of the predictions, but increasing  $w_{cc}$  even further or increasing  $w_{sc}$  from 0.5 to 1.0 generally worsened the lowest RMSD. We also observe that ZDock performed better than F<sup>2</sup>Dock in most cases under these parameter settings.

In Figure 5 we show the best docking positions we obtained during unbound-unbound docking of the following four complexes: (a) Ribonuclease A complexed with Rnase inhibitor, (b) Epstein-Barr virus receptor CR2 complexed with Complement C3, (c) Cyt C peroxidase complexed with Cytochrome C, and (d) Colicin E7 nuclease complexed with Im7 immunity protein.

In Table 3 we report the results of incorporating the approximate electrostatics interactions score computed by our method into the docking score. We used 1.0, 10.0 and 1.0 as skinskin  $(w_{ss})$ , core-core  $(w_{cc})$  and skin-core  $(w_{sc})$  weights, respectively. Electrostatics based affinity function is defined using a model by Gabb [3]. The dielectric value is set to 4 for distances less than 6 Å from the center of atoms, 80 for greater than 8 Å and a linear interpolation in between. The electrostatics weight  $(w_F)$  was set to an empirically determined value of 350 which seems to improve the 'Rank' for the largest number of complexes when  $w_{ss}$ ,  $w_{cc}$  and  $w_{sc}$  are set to 1.0, 10.0 and 1.0, respectively. We observe that adding the electrostatics score improved the 'Rank' of 45 out of 84 complexes ( $\approx 53\%$ ), while for 24 complexes ( $\approx 29\%$ ) solutions actually degraded. Among the complexes with improved 'Rank' values, 42 had their 'Rank' improved by at least 10, 30 by at least 100, and 15 by at least 1,000. There are 2 complexes ((1) 1K5D: Ran GTPase complexed with Ran GAP, and (2) 1ML0: Viral chemokine binding p.M3 complexed with Chemokine Mcp1) for which we did not have a single solution with RMSD less than 5 Å in the top 50,000 without electrostatics, but with  $w_F$  set to 350 we had several such solutions for each. For one of the complexes (2PCC: Cyt C peroxidase complexed with Cytochrome C) while we did not have a hit (i.e., at least one solution with RMSD less than 5 Å in the top 2,000) when electrostatics was not used, it was a hit when  $w_E$  was set to 350. On the other hand, for 1FC2 (i.e., Staphylococcus protein A complexed with Human Fc fragment) we had a solution with RMSD less than 5 Å in the top 50,000 when  $w_E$  was set to 0, but lost it when  $w_E$  was set to 350. Electrostatics scores did not seem to have as much impact on the minimum RMSD value as they had on 'Rank'. For only 16 complexes the minimum RMSD improved by at least 0.05 Å, while for 9 it degraded by at least 0.05 Å. For 52 complexes the minimum RMSD did not change. Overall, electrostatics was most effective on inhibitors or enzymesubstrate and antigen-bound antibody complexes (improving results in more than 60% of the 35 cases), and least effective on antibody-antigens (marginally improving results for only 3 out of 10 complexes). For the remaining 39 complexes, however, electrostatics was effective in more than 70% of the cases.

#### 4.2 Bound-unbound Docking

Table 4 shows the results of increasing the number of frquencies extracted by FFT from  $32^3$  to  $64^3$  when performing bound-unbound docking on the complexes of the ZDock benchmark suite. The weight values are the same as in Table 3, and electrostatics interactions were not considered. We observe that increasing the number of frequencies generally improved the lowest RMSD considerably. For 45 complexes the lowest RMSD improved by at least 0.05 Å.

In Figure 6(b) we show our docking of chains A & B (nuclear transport factor 2) obtained from 10UN.pdb on chain C (Ran GTPase) of 1A2K.pdb (i.e., docking the unbound nuclear transport factor 2 from 10UN.pdb instead of the same protein already docked on Ran GTPase of 1A2K.pdb). In Figure 6(d) we show the docking of PSTI obtained from 1HPT.pdb on chain E (Bovine chymotrypsinogen) of 1CGI.pdb replacing the PSTI (chain I) already docked there.

#### 4.3 Bound-bound Docking or Redocking

In Table 5 we report our bound-bound docking results on ZDock benchmark 2.0 [6]. We use the same weight values as in Table 4, and show results both with and without electrostatics. We did not move molecule *B* (the moving molecule) to a random location at the beginning of the experiment since  $F^2$ Dock initially centers both molecules at the origin anyway. We also did not rotate molecule *B* by a random amount initially since we are using rotations sampled uniformly at random and the identity matrix (i.e., 0° rotation) was not included as a rotation matrix separately. For 27 complexes the lowest RMSD was less than 1 Å, and for 47 it was less than 1.5 Å. The impact of including electrostatics was almost similar to the unbound-unbound case. For example, electrostatics improved the 'Rank' value for around 54% of the complexes, while for around 34% of the complexes 'Rank' degraded.

Figure 6(a) shows our redocking of chains A & B (nuclear transport factor 2) of 1A2K.pdb on its chain C (Ran GTPase), while Figure 6(c) shows our redocking of chain I (PSTI) of 1CGI.pdb on its chain E (Bovine chymotrypsinogen).

Figure 7 shows the distribution of electrostatics potential on the molecular surfaces of Ran GTPase and Ran GAP, and also how the distribution changes when they form a complex (1K5D.pdb). In Figure 8 we show the electrostatics complementarity at the interface when Ran GTPase and Ran GAP dock at three different locations and orientations. The electrostatics potential for all of these examples, were computed using our CVC in-house software called PBEM3D (Molecular Poisson Boltzmann Boundary Element Electrostatics Potential calculation in 3D [52]). Figures (visualization) were created using CVC software TexMol.

#### **5 CONCLUSION**

We have presented a fast, and practical adaptive algorithm for rigid protein-protein docking. Our algorithm is based on representing affinity functions in a multi-resolution radial basis function format. The smoothed particle protein representation, together with nonequispaced Fast Fourier transforms allows us several advantages of efficiency and accuracy tradeoffs visavis traditional FFT based docking approaches. Our contributions are also in scoring of docked conformations as a convolution of complex affinity functions, and providing approximation algorithms to detect peaks in the docking scoring profiles. Both shape complementarity and electrostatics are used for scoring and to obtain the top docking conformations. Our implementation of  $F^2$ Dock speeds up computation even further by executing multiple concurrent threads on multicore machines. The rotation matrices are evenly distributed among the threads. When electrostatics is not used we use on the average,

around 15 mins for computing docking positions (with 6° rotational sampling and  $32^3$  frequencies) per typical protein complex on a quad-core linux desktop (3.0GHz) with 4GB RAM. The running time approximately doubles when electrostatics is used. We used the FFTW package [53] for computing FFT and the inverse FFT. We are also working on an MPI [54] based distributed implementation of F<sup>2</sup>Dock capable of running on Linux clusters. This implementation will be available as a web-based docking server. Jobs can also be launched on the server from our in-house molecular modeling and visualization client software tool, called TexMol [55]. The TexMol client tool is in the public domain and can be freely downloaded from our center's software website (http://www.ices.utexas.edu/CVC/software/).

We are also in the process of extending  $F^2Dock$  to  $F^3Dock$  which is capable of handling flexible molecules. Some preliminary results on  $F^3Dock$  are available as a technical report [7].

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#### Fig. 1.

(a) Skin and Core regions for complementary space docking. Atoms are drawn as solid circles. The skins regions are colored green while the core regions are red. The skin volume of molecule A is obtained by rolling a solvent ball over its surface. (b) A possible docking of the molecules show a large overlap between the grown layer of molecule A and the surface atoms of molecule B.



#### Fig. 2.

For shape-complementarity scoring skin atoms are assigned a weight of  $c^{Re} = \sqrt{w_{ss}}$ , and core atoms are assigned weight  $c^{Im} = i \cdot \sqrt{w_{cc}}$ , where  $w_{ss}$  is the reward factor for skin-skin overlaps, and  $w_{cc}$  is the penalty factor for core-core overlaps.



#### Fig. 3.

Overview of the translational search phase of the F<sup>2</sup>Dock algorithm. Here  $f_A$  and  $f_B$  are affinity functions of molecule A and B, respectively. We assume that a given rotation has already been applied on molecule B.

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#### Fig. 4.

The docking peak search can be represented as finding the peak positions and values in a grid of overlapping splines.



#### Fig. 5.

Unbound-unbound docking: (a) (1DFJ: Ribonuclease A complexed with Rnase inhibitor) Docking the unmarked chain of 2BNH.pdb (Rnase inhibitor) on chain B (Ribonuclease A) of 9RSA.pdb, (b) (1GHQ: Epstein-Barr virus receptor CR2 complexed with Complement C3) Docking chain A (Complement C3) of 1LY2.pdb on the unmarked chain (Epstein-Barr virus receptor CR2) of 1C3D.pdb, (c) (2PCC: Cyt C peroxidase complexed with Cytochrome C) Docking the unmarked chain (Cytochrome C) of 1YCC.pdb on the unmarked chain (Cyt C peroxidase) of 1CCP.pdb, and (d) (7CEI: Colicin E7 nuclease complexed with Im7 immunity protein) Docking chain B (Im7 immunity protein) of 1M08.pdb on chain D (Colicin E7 nuclease) of 1UNK.pdb. In all cases the first chain is static (colored yellow), and the other chain is moved around for docking. The position of the moving molecule shown in pink corresponds to the true solution (obtained by the best superimposition of each molecule on the corresponding molecule in the bound structure) while red is our final docked position.



#### Fig. 6.

(a & b) Docking 1A2K (Ran GTPase complexed with nuclear transport factor 2): (a) (Bound-Bound) Redocking chains A & B (nuclear transport factor 2) of 1A2K.pdb on it's chain C (Ran GTPase), (b) (Bound-Unbound) Docking chains A & B (nuclear transport factor 2) of 1OUN.pdb on chain C of 1A2K.pdb. (c & d) Docking 1CGI (Bovine chymotrypsinogen complxed with PSTI):: (c) (Bound-Bound) Redocking chain I (PSTI) of 1CGI.pdb on it's chain E (Bovine chymotrypsinogen), (d) (Bound-Unbound) Docking the unmarked chain (PSTI) of 1HPT.pdb on chain E of 1CGI.pdb. In (a) & (b) chain C is static (colored yellow), and in (c) & (d) chain E is static, and in all cases the other chain(s) is (are) moved around for docking (the true position in the bound complex is pink, and our final docked position is red).



#### Fig. 7.

Poisson-Boltzmann electrostatics potential on the surface of (a) Ran GTPase, (b) Ran GAP, and (c) complex of Ran GTPase and Ran GAP (1K5D.pdb). The potential ranges from  $-3.8 k_b T/e_c$  (red) to  $+3.8 k_b T/e_c$  (blue).



#### Fig. 8.

Figures (a) and (b) show Poisson-Boltzmann electrostatics potential on the surface of Ran GTPase and Ran GAP, respectively. The potential ranges from  $-3.8 k_b T/e_c$  (red) to  $+3.8 k_b T/e_c$  (blue). Figures (c) and (d) show the bound complex of Ran GTPase and Ran GAP (1K5D.pdb). In (c) Ran GAP is drawn semi-transparent while in (d) Ran GTPase is drawn semi-transparent in order to show the electrostatics complementarity at the interface. Figures (e) and (f) show the solution with the lowest RMSD (1.66 Å) from the bound complex among the top 2,000 solutions returned by F<sup>2</sup>Dock when electrostatics weight was set to 350. Figures (g) and (h) show the solution with the lowest RMSD (2.90 Å) from the bound complex among the top 2,000 solutions returned by F<sup>2</sup>Dock when electrostatics weight was set to 350. Figures (g) and (h) show the solution seturned by F<sup>2</sup>Dock when electrostatics weight was set to 0.

1 F<sup>2</sup>Dock and ZDgck use 6° rotational sampling. F<sup>2</sup>Dock and ZDock retained 50,000 and 54,000 peaks, respectively. RMSD was calculated using the ound-unbound docking results using shape complementarity only, where we use four different sets of skin-skin ( $w_{ss}$ ), core-core ( $w_{cc}$ ) and skin-core in the predicted set which were less than 5Å RMSD from the known position. 'RMSD' is the lowest RMSD among all peaks that were retained. ) weight values for  $F^2Dock$ . 'Rank' is the best rank among all predicted positions whose RMSD was less than 5Å. 'Good Peaks' is the number of toms near the interface of the known bound conformation (within  $5\text{\AA}$  of the interface for F<sup>2</sup>Dock).

		ZDock Results	RMSD (Å)	1.61	2.54	0.89	2.01	1.24	3.87	0.76	1.08	2.05	5.69	0.87	1.00	1.49	1.00	2.08	2.61	2.65	1.35	1.63	1.18
			RMSD (Å)	3.19	3.08	1.65	3.49	1.45	4.72	1.88	1.04	2.18	6.57	4.45	0.87	2.21	1.62	2.57	1.49	2.81	1.15	2.83	3.84
		$c_{cc} = 20.0$ $v_{sc} = 1.0$	Rank	5,565	1,282	3,844	207	62	32,962	870	360	1431		49,034	20	234	117	4	164	1,059	1,093	17,605	4,953
		# -	Good Peaks	29	328	44	95	381	1	198	237	77	ı	1	3,825	173	442	1,167	2,252	81	112	50	61
			RMSD (Å)	3.02	3.08	1.65	3.49	1.45	4.72	1.75	0.87	1.96	6.54	6.81	0.75	2.21	1.58	2.55	1.45	2.81	1.15	5.80	3.38
	:= 32 <sup>3</sup> )	$v_{cc} = 10.0$ $w_{sc} = 1.0$	Rank	8,100	803	6,516	160	102	19,423	1,769	94	1,862			65	801	72	39	177	607	243		12,176
	.0, frequencies	2	Good Peaks	36	569	36	110	679	4	339	303	127			4,505	139	685	1,859	2,419	110	318		47
	Results ( $w_{ss} = 1$		RMSD (Å)	3.02	2.89	1.65	3.49	1.45	4.68	1.58	0.69	1.70	6.03	7.31	0.97	2.88	1.58	2.53	1.43	2.81	1.07	6.67	2.26
	F <sup>2</sup> Dock ]	$c_{cc} = 10.0$ $w_{sc} = 0.5$	Rank	19,083	480	13,916	91	165	3,889	723	100	1,844			107	3,692	6	14	477	34,372	75		5,428
		2	Good Peaks	29	1,117	23	248	961	8	470	420	157			5,244	61	1,087	2,736	2,858	40	640		141
			RMSD (Å)	4.37	2.55	4.77	3.43	1.54	4.68	1.58	0.80	1.70	4.54	7.31	1.04	3.97	1.58	2.53	1.45	2.98	1.07	8.78	2.15
		$w_{cc} = 5.0$ $w_{sc} = 0.5$	Rank	15,258	361	46,475	84	16	8,017	408	156	3,278	21,434		154	18,274	1	29	48	4,182	154	-	9,817
			Good Peaks	2	1,913	1	604	1,412	8	725	491	166	3		6,060	6	1,566	3,533	3,923	131	1,198		136
			Unbound Mol 2	10UN_AB	1EGL_	1TFH_A	1E6J_P	1CD8_AB	3DNI_	1BA7_B	1A19_B	1IAS_A	1CMW_A	2VPF_GH	1DKS_A	$3LZT_{-}$	1HOE_	$1$ HPT_	1K9B_A	1CX8_AB	$2BNH_{-}$	$3LZT_{-}$	1CJE_D
40	'M Tr	ans Goi	Unbound Mol 1	1004_A	209 BOGBA_B	1FON_LH	$\frac{2K}{2}$ PL	2CBR_DE	1 HU_B	1000 A	1RCH_B #GH_B	11260_A	1AA1_HL ii	TH_ IBH_H		1BTL_BA	Ite DIG_	2ŒA_B	$2 T G T_{-}$	1A6Z_AB	9RSA_B	1DQQ_CD	1E1N_A
			ind Complex	A2K_C:AB	IACB_E:I	AHW_AB:C	AK4_A:D	vKJ_AB:DE	ATN_A:D	AVX_A:B	AY7_A:B	[B6C_A:B	BGX_HL:T	J1_HL:VW	BUH_A:B	BVK_DE:F	BVN_P:T	1CGI_E:I	1D6R_A:I	DE4_AB:CF	1DFJ_E:I	DQJ_AB:C	IE6E_A:B

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							F <sup>2</sup> Dock	Results ( $w_{ss} =$	1.0, frequencies	s = 32 <sup>3</sup> )					
	Data			$w_{cc} = 5.0$ $w_{sc} = 0.5$		4	$v_{cc} = 10.0$ $w_{sc} = 0.5$		-	$v_{cc} = 10.0$ $w_{sc} = 1.0$		4	$v_{cc} = 20.0$ $w_{sc} = 1.0$		ZDock Results
ind Complex	Unbound Mol 1	Unbound Mol 2	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	RMSD (Å)
E6J_HL:P	1E60_HL	$1A43_{-}$			9.85		ı	8.31		ı	7.03	36	32,782	3.05	1.28
1E96_A:B		1HH8_A	104	768	2.08	196	725	1.79	175	300	1.79	195	684	1.50	1.68
EAW_A:B	1EAX_A	_IT40	1,088	35	1.22	1,146	478	1.22	913	517	1.70	636	760	2.40	0.66
EER_A:BC	1BDY_A	1ERN_AB	512	20	2.47	250	L	2.47	112	4	2.80	33	2	3.11	3.24
EWY_A:C	$1^{cu}_{OR_A}$	1CZP_A	3,055	172	1.08	2,608	30	1.08	1,567	4	1.21	162	2	1.27	1.49
EZU_C:AB	A_M∰D	1ECZ_AB	266	630	2.48	86	412	2.94	42	826	3.40	21	2,762	3.81	1.35
1F34_A:B	uter ter	1F32_A	972	484	1.23	783	156	1.23	570	98	1.34	396	35	1.90	1.23
F51_AB:E	11X	1SRR_C		-		,						-			0.83
FAK_HL:T	100K_HL	1TFH_B		-	8.30	,		8.26			8.43	-		8.67	6.85
IFC2_C:D	1BDD_	1FC1_AB			5.95		-	5.86	1	45,800	4.98	20	13,678	4.16	2.23
IFQ1_A:B	$1$ $H_{\rm PZ}$	$1B39_A$	62	652	4.01	53	90 <i>L</i>	3.89	42	026	4.01	20	2,950	4.03	3.52
IFQJ_A:B	11 BD_C	1FQI_A	558	62	1.90	345	20	1.90	288	27	2.12	162	179	2.14	2.75
FSK_BC:A	1Far BC	1BV1_		ı	8.58	8	38,144	2.88	39	14,829	2.19	58	5,874	2.19	0.66
GCQ_B:C	1GRI_B	1GCP_B		ı	14.19			14.19		ı	14.19			14.19	1.17
GHQ_A:B	183D_	1LY2_A	159	1,253	2.75	211	181	3.05	245	101	2.85	226	58	2.85	3.60
GP2_A:BG	I BIA_	1TBG_DH			7.05		-	7.05	-	-	7.05	-	-	7.38	2.02
GRN_A:B	1/GHR_A	1RGP_	486	1,600	2.26	357	1,418	2.26	349	1,264	2.23	297	1,605	2.23	1.62
H1V_A:G	1∰J_B	1D0N_B			13.45		-	13.46	-	-	13.47	-	-	13.48	9.58
IHE1_C:A	<sup>-1</sup> H21	1HE9_A	3,492	25	1.12	1,866	3	1.12	1,116	1	1.12	592	5	1.12	1.16
HE8_B:A	_dI⊠a	1E8Z_A	64	11,791	2.98	4	41,665	4.60	-	-	5.14	-	-	5.40	3.24
HIA_AB:I	2PEA_XY	1BXB_	749	88	3.09	590	103	3.09	488	453	3.10	284	570	3.35	2.60
II2M_A:B	1QG4_A	1A12_A	210	574	2.74	181	1,133	2.86	137	1,352	3.06	02	1,411	3.51	2.31

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ound-unbound docking results using shape complementarity only (continued), where we use four different sets of skin-skin (w<sub>ss</sub>), core-core (w<sub>cc</sub>) and ned. Both F<sup>2</sup>Dock and ZDock use 6° rotational sampling. F<sup>2</sup>Dock and ZDock retained 50,000 and 54,000 peaks, respectively. RMSD was calculated ber of peaks in the predicted set which were less than 5Å RMSD from the known position. 'RMSD' is the lowest RMSD among all peaks that were -core ( $w_{sc}$ ) weight values for F<sup>2</sup>Dock. 'Rank' is the best rank among all predicted positions whose RMSD was less than 5Å. 'Good Peaks' is the g the  $C_{\alpha}$  atoms negative interface of the known bound conformation (within 5Å of the interface for F<sup>2</sup>Dock).

		ZDock Results	Å) RMSD (Å)	1.74	1.49	3.97	4.71	1.11	0.75	0.86	0.64	1.81	1.34	2.35	0.87	0.76	1.58	0.85	4.29	0.86	1.25	0.83	3.03
			RMSD (		1.51	5.19	6.78	2.55	1.34	1.21	3.02	4.49	1.67	5.02	3.45	4.78	2.01	1.36	3.67	2.07	3.38	5.12	'
		$w_{cc} = 20.0$ $w_{sc} = 1.0$	Rank		842		'	3,036	3,551	66L	1,569	27,117	431		6,464	14,660	70	302	6,232	2,628	48,211		
			Good Peaks	1	149			113	53	322	55	3	341	-	22	14	82	263	37	77	1	ı	i
			RMSD (Å)	3.41	1.51	3.66	68.9	2.54	1.34	1.24	3.02	5.06	1.67	6.07	4.36	4.89	2.01	1.36	3.36	2.07	5.22	5.12	4.82
	s = 32 <sup>3</sup> )	$v_{cc} = 10.0$ $w_{sc} = 1.0$	Rank	6,940	2,739	20,918	-	2,221	8,909	484	64	-	747	-	20,914	26,751	306	646	7,365	6,598	-	-	16,076
	l.0, frequencies		Good Peaks	96	129	18	-	197	31	265	115		380	-	8	3	138	303	42	39	-	-	2
	Results ( $w_{ss} = 1$		RMSD (Å)		1.60	3.66	7.38	2.54	1.34	1.29	3.02	4.34	1.42	5.62	4.31	4.89	2.01	1.36	2.99	2.16	3.57	5.48	İ
	F <sup>2</sup> Dock	$v_{cc} = 10.0$ $w_{sc} = 0.5$	Rank		4043	13,593	1	3,514	33,186	1,733	13	18,833	941	-	3,276	33,047	226	2,270	3,593	30,532	9,643		
		-	Good Peaks		109	54		228	6	174	147	9	375		19	2	178	279	90	7	40	-	I
			RMSD (Å)	3.58	2.31	3.66	4.41	2.54	8.65	3.25	3.02	4.52	1.42	5.75	4.09	5.03	1.59	1.36	2.99	5.50	2.62	96.6	3.70
		$w_{cc} = 5.0$ $w_{sc} = 0.5$	Rank	6,391	13,814	18,213	13,885	3,414		5,846	74	1,203	2,005	-	2,582	-	418	1,502	3,412		4,634	-	11,739
			Good Peaks	42	13	99	9	289		71	167	13	301	-	47	-	223	160	146		186		6
			Unbound Mol 2	1149_AB	1ALY_ABC	1KUY_A	1F59_A	IAUQ_	1D7P_M	1TFH_B	1JVM_ABCD	1YRG_B	1F5W_B	2HPR_	$1STE_{-}$	1M9Z_A	1KW2_B	1PPI_	1MOZ_B	$1$ FSC_	1DOL_	$3LZT_{-}$	2NIP_AB
40	M Tr	ans 🛱	Unbound Mol 1		TH <sup>−</sup> ti BH	10gB_AB	$1064_A$	1FBU_AB	11(HD_AB	1JPT_HL	1K#C_AB	1RRP_AB	11 NOB_F	1JBABC	1HQ5_AB	1 TECK_	1∰J_B	1KH O_H	1AUQ_	$1J06_B$	1MKF_AB	1MLB_AB	3MIN_ABCD
			ind Complex	[4D_D:AB	R_HL:ABC	IB1_AB:E	IBR_A:B	IJK_BC:A	IQD_AB:C	JPS_HL:T	K4C_AB:C	X5D_AB:C	KAC_A:B	KL_ABC:H	KLU_AB:D	KTZ_A:B	KXP_A:D	KXQ_H:A	M10_A:B	MAH_A:F	ML0_AB:D	ALC_AB:E	C_ABCD:EF

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							F <sup>2</sup> Dock	Results ( $w_{ss} =$	1.0, frequencie	$s = 32^3$					
Data	-			$w_{cc} = 5.0$ $w_{sc} = 0.5$			$w_{cc} = 10.0$ $w_{sc} = 0.5$			$v_{cc} = 10.0$ $w_{sc} = 1.0$		-	$v_{cc} = 20.0$ $w_{sc} = 1.0$		ZDock Results
x Unbound	Mol 1	Unbound Mol 2	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	RMSD (Å)
INCA	HL	_eNN7	2	46,528	4.50	32	7,060	1.50	37	7,406	1.50	51	3,765	0.86	09.0
	HL	1KDC_	29	29,539	2.31	90	9,501	2.13	69	7,846	2.09	31	4,773	2.09	0.94
A CAN		1LU0_A	3,425	118	1.12	2,574	210	1.12	1,634	355	1.12	1,007	165	1.12	0.58
t ∰ara	Ľ	1CCZ_A	4	35,505	4.45	11	12,385	3.37	23	9,957	3.37	49	6,689	2.03	1.38
B IQ <sup>w</sup>	IM	1HRP_AB	12	34,831	2.43	27	5,651	1.34	35	1,372	1.34	46	391	1.34	1.13
E 2PABEA	(BCD	1HBP_	25	7,151	3.53	35	19,653	4.29	26	6,480	3.82	33	3,088	2.85	1.11
ut <b>B</b> EC	UL C	1SE4_			5.43	4	25,893	4.80	19	6,270	4.06	8	3,717	4.34	1.36
EVE ABI	ار ريا	1B1U_A	564	6	1.63	379	18	1.63	233	247	1.63	175	1,652	1.97	1.43
1 TEDH	H	2UGI_B	352	5,597	1.46	236	3,693	1.60	113	5,438	1.98	121	1,817	1.99	1.24
1V <sup>1</sup> A	AB	BLYZ_	20	4,533	3.26	135	863	0.75	243	310	0.75	259	96	0.75	1.42
	НК	1HRC_	-	-	6.91		-	7.03	-	-	6.44	4	44,648	3.24	0.51
6021_	D	1WER_	1,039	327	1.58	809	132	1.95	203	96	1.95	392	52	2.01	1.55
1 I I I	B	1PNE_	1	41,750	2.96	13	13,803	2.31	L	17,075	2.31	8	5,799	2.96	0.88
	CD	1S6P_AB	L	18,636	3.73	13	4,480	3.73	10	884	4.15	10	303	4.15	2.58
2J <u>B</u> L_I	HL	1POH_	-	ı	10.62	ı		-	-	-	1	-	-	I	0.72
2BBK_	JM	2RAC_A	358	882	2.35	434	1,489	2.25	384	1,378	1.58	619	304	1.58	0.74
1ÉCP	P	1YCC_	245	5,259	1.55	88	8,369	1.64	73	19,509	1.10	79	8,413	1.60	1.46
в 10ğw_	HL	1HRP_AB	113	6,453	1.75	193	1,308	1.18	239	525	1.18	223	595	1.18	1.48
40 <b>5</b> 1		3SSI_	352	1,978	2.35	293	936	1.79	226	1,072	1.79	213	773	1.79	0.43
N 2011	I_A	2CI2_I	827	291	1.63	421	359	1.63	257	362	1.92	168	1,739	2.28	1.05
10 <sup>2</sup> 6_1	LH	2VIU_ACE	-	I	8.07	I	ı	ı	-	I	7.74	-	-	I	1.24
IUNK	D	1M08_B	622	1,182	1.22	262	845	0.95	318	1,188	1.04	378	516	1.04	0.80

shape-complementarity-based unbound-unbound docking with  $F^2Dock$ . 'Rank' is the best rank among all predicted than 5Å. 'Good Peaks' is the number of peaks in the predicted set which were less than 5Å RMSD from the known tMSD among all peaks that were retained. In both cases we used  $6^\circ$  rotational sampling, and retained 50,000. RMSD was ar the interface of the known bound conformation (within 5Å of the interface).

	El														
	EE/A		F <sup>2</sup> Dock	Results								F <sup>2</sup> Dock	Results		
	CM 1	Weig	hts: wss = 1.0,	$w_{cc} = 10.0, w_{sc} =$	: 1.0						Weigł	its: $w_{ss} = 1.0$ , $v$	$v_{cc} = 10.0, w_{sc} =$	1.0	
	rans		Frequenc	cies = $32^3$								Frequenc	ies = 32 <sup>3</sup>		
	Without E	lectrostati	ics $w_E = 0$	With Elect	trostatics 1	$v_E = 350$		Data		Without E	lectrostatic	S $w_E = 0$	With Elec	trostatics )	$v_{E} = 350$
Unbound Mol 2	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Bound	Unbound	Unbound	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)
10UN_AB	92 Biol I	8,100	3.02	75	4,374	3.02	114D_D:AB	1MH1_	1149_AB	96	6,940	3.41	94	7,033	3.41
1EGL_	99 Biôin	803	3.08	501	849	3.20	119R_HL:ABC	119R_HL	1ALY_ABC	129	2,739	1.51	185	2,090	1.51
1TFH_A	90 form	6,516	1.65	36	5,396	1.65	11B1_AB:E	1QJB_AB	1KUY_A	18	20,918	3.66	13	22,719	3.73
1E6J_P	9 . Au	160	3.49	139	128	3.48	11BR_A:B	1QG4_A	1F59_A			6.89	1		6.26
1CD8_AB	629 thor	102	1.45	706	46	1.45	11JK_BC:A	1FVU_AB	1AUQ_	197	2,221	2.54	299	1,426	2.43
3DNI_	+ manı	19,423	4.72	4	14,779	4.72	1IQD_AB:C	1IQD_AB	1D7P_M	31	8,909	1.34	50	6,412	1.34
1BA7_B	6£ Iscrij	1,769	1.75	326	1,909	1.75	1JPS_HL:T	1JPT_HL	1TFH_B	265	484	1.24	265	702	1.17
1A19_B	50 pt; av	94	0.87	474	32	96.0	1K4C_AB:C	1K4C_AB	1JVM_ABCD	115	64	3.02	114	87	3.02
1IAS_A	LZ ailat	1,862	1.96	144	1,687	1.96	1K5D_AB:C	IRRP_AB	1YRG_B			5.06	64	8,013	2.79
1CMW_A	ole ir		6.54			6.54	1KAC_A:B	INOB_F	1F5W_B	380	747	1.67	377	672	1.67
2VPF_GH	PM		6.81			7.19	1KKL_ABC:H	1JB1_ABC	2HPR_			6.07	1		6.07
1DKS_A	0 6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	65	0.75	4,569	64	0.75	1KLU_AB:D	1H15_AB	1STE_	8	20,914	4.36	6	33,414	4.36
$3LZT_{-}$	6£ 1⊥v	801	2.21	LL1	560	2.21	1KTZ_A:B	1TGK_	1M9Z_A	3	26,751	4.89	4	20,866	4.89
1HOE_	S80 larch	72	1.58	809	54	1.58	1KXP_A:D	11JJ_B	1KW2_B	138	306	2.01	168	157	2.01
1HPT_	£859	39	2.55	1,762	45	2.55	1KXQ_H:A	1KXQ_H	1PPI_	303	646	1.36	353	528	1.39
1K9B_A	2,419	177	1.45	2,480	170	1.45	1M10_A:B	1AUQ_	1MOZ_B	42	7,365	3.36	115	3,138	2.99
1CX8_AB	110	607	2.81	131	589	2.81	1MAH_A:F	1J06_B	1FSC_	39	6,598	2.07	89	3,327	2.07
2BNH_	318	243	1.15	881	22	1.14	1ML0_AB:D	1MKF_AB	1DOL_	I		5.22	3	33,027	4.50
$3LZT_{-}$	1	-	5.80	-		5.80	1MLC_AB:E	1MLB_AB	3LZT_	I		5.12	I	-	5.33
1CJE_D	47	12,176	3.38	210	3,526	2.41	1N2C_ABCD:EF	3MIN_ABCD	2NIP_AB	2	16,076	4.82	2	8,637	4.82

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			F <sup>2</sup> Dock	c Results								F <sup>2</sup> Dock	Results		
		Weig	ghts: wss = 1.0,	$w_{cc} = 10.0, w_{sc} =$	: 1.0						Weigł	its: $w_{ss} = 1.0$ , $u_{ss} = 1.0$	$v_{cc} = 10.0, w_{sc} =$	1.0	
			Frequen	cies = $32^3$								Frequenc	ies = 32 <sup>3</sup>		
	Without E	Jectrostat	ics $w_E = 0$	With Elect	trostatics y	$v_E = 350$		Data		Without El	lectrostatic	$\cos w_E = 0$	With Elect	trostatics 4	$v_E = 350$
Unbound Mol 2	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Bound	Unbound	Unbound	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)
1A43_	E/A		7.03			7.00	INCA_HL:N	1NCA_HL	ONN7	37	7,406	1.50	29	8,944	1.65
1HH8_A	M75	300	1.79	218	193	1.79	1NSN_HL:S	1H_NSN1	1KDC_	69	7,846	2.09	68	8,340	2.09
_IT40	EI Trâns	517	1.70	1,265	454	1.52	1PPE_E:I	1BTP_	1LU0_A	1,634	355	1.12	1,450	392	1.12
1ERN_AB	21 Con	4	2.80	142	-	2.84	1QA9_A:B	1HNF_	1CCZ_A	23	9,957	3.37	24	9,730	3.37
1CZP_A	म्स् 195,567	4	1.21	2,308	4	1.17	1QFW_IM:AB	1QFW_IM	1HRP_AB	35	1,372	1.34	45	1,212	1.34
1ECZ_AB	Biol	826	3.40	42	763	3.40	1RLB_ABCD:E	2PAB_ABCD	1HBP_	26	6,480	3.82	28	4,843	3.77
1F32_A	02 Biloin	86	1.34	625	09	1.34	1SBB_A:B	1BEC_	1SE4_	19	6,270	4.06	19	6,146	4.06
1SRR_C	ıforn		ı	-	-		1TMQ_A:B	$1JAE_{-}$	1B1U_A	233	247	1.63	238	241	1.63
1TFH_B	ı. At		8.43	-	-	8.43	1UDI_E:I	1UDH_	2UGL_B	113	5,438	1.98	217	3,043	1.74
1FC1_AB	thor	45,800	4.98		1	5.12	1VFB_AB:C	1VFA_AB	BLYZ_	243	310	0.75	269	213	0.75
1B39_A	man man	026	4.01	-	-		1WEJ_HL:F	1QBL_HK	1HRC_	-	1	6.44	'		6.44
1FQI_A	88 uscri	27	2.12	326	30	2.10	1WQ1_R:G	6Q21_D	1WER_	503	96	1.95	608	62	1.95
$1BV1_{-}$	68 pt; a	14,829	2.19	37	14,873	2.19	2BTF_A:P	11JJ_B	1PNE_	L	17,075	2.31	8	13,957	2.31
1GCP_B	vaila	ı	14.19	ı	I	14.19	2HMI_CD:AB	2HMI_CD	1S6P_AB	10	884	4.15	10	836	4.15
1LY2_A	i a245	101	2.85	190	431	2.85	2JEL_HL:P	2JEL_HL	1POH_	I	ı	1	57	11,932	2.58
1TBG_DH	n PM	I	7.05	I	I	6.97	2MTA_HL:A	2BBK_JM	2RAC_A	384	1,378	1.58	811	1,124	1.58
IRGP_	64 C 2(	1,264	2.23	504	674	2.23	2PCC_A:B	1CCP_	1YCC_	73	19,509	1.10	1,574	843	0.66
1D0N_B	)11 N	ı	13.47	ı	I	13.47	2QFW_HL:AB	1QFW_HL	1HRP_AB	239	525	1.18	307	427	1.18
1HE9_A	116 ס#נר	1	1.12	1,253	1	1.12	2SIC_E:I	1SUP_	3SSI_	226	1,072	1.79	180	1,429	2.35
1E8Z_A	1 16.	ı	5.14	ı	I	5.14	2SNI_E:I	1UBN_A	2CI2_I	257	362	1.92	246	377	1.92
1BXB_	488	453	3.10	718	220	2.98	2VIS_AB:C	1GIG_LH	2VIU_ACE			7.74			7.74
1A12_A	137	1,352	3.06	349	381	2.86	7CEI_A:B	1UNK_D	1M08_B	318	1,188	1.04	958	598	0.85

of changing the number of frequencies extracted by FFT during Bound-unbound docking with F<sup>2</sup>Dock. 'Rank' is the best rank among all predicted ons whose RMSD was less than 5Å. 'Good Peaks' is the number of peaks in the predicted set which were less than 5Å RMSD from the known on. 'RMSD' is the lowest RMSD among all peaks that were retained. F<sup>2</sup>Dock used 6° rotational sampling, and retained 50,000 peaks. RMSD was uted using the  $C_{\alpha}$  atoms near the interface of the known bound conformation (within 5Å of the interface).

				64 <sup>3</sup>	RMSD (Å)	2.68	0.84	1.35	3.43	1.77	1.74	0.75	2.84	4.73	1.73	2.27	4.30	5.05	1.16	0.65	3.65	1.58	1.86	5.11	4.41
				uencies = (	Rank	353	1,782	3,166	31,965	7,958	25,042	1,195	31	7,478	804	7,376	11,638		126	1,758	5,628	3,508	621		2,936
	Results	hts	10.0, $w_{sc} = 1.0$	Freq	Good Peaks	227	123	107	3	18	6	142	357	3	319	94	6	-	345	295	26	73	34		10
	F <sup>2</sup> Dock	Weig	$v_{ss} = 1.0, w_{cc} =$	32 <sup>3</sup>	RMSD (Å)	4.08	0.85	1.79	4.98	1.72	1.34	0.93	3.02	1.80	1.53	2.09	4.04	5.15	1.35	1.69	3.09	3.39	5.34	5.43	4.44
			×	uencies = 3	Rank	4,657	3,983	589	49,336	2,647	8,909	1,689	64	34,601	340	30,156	7,312		102	1,020	5,622	16,095	ı		797
				Frequ	Good Peaks	35	108	75	1	56	31	178	115	7	465	24	31	-	221	249	91	25	-	-	13
				-	Unbound Mol 2	1149_AB	1ALY_ABC	1KUY_A	1F59_A	1AUQ_	1D7P_M	1TFH_B	1JVM_ABCD	1YRG_B	1F5W_B	2HPR_	1STE_	A_Z9M1	1KW2_B	1PPI_	1MOZ_B	1FSC_	1DOL_	3LZT_	2NIP_AB
				Dat	Bound Complex	1I4D_D:AB	119R_HL:ABC	1IB1_AB:E	1IBR_A:B	11JK_BC:A	1IQD_AB:C	1JPS_HL:T	1K4C_AB:C	1K5D_AB:C	1KAC_A:B	1KKL_ABC:H	1KLU_AB:D	1KTZ_A:B	1KXP_A:D	1KXQ_H:A	1M10_A:B	1MAH_A:F	1ML0_AB:D	1MLC_AB:E	1N2C_ABCD:EF
				643	RMSD (Å)	3.17	1.93	1.27	3.97	1.26	1.57	1.40	1.41	1.56	3.51	6.02	0.22	1.72	1.03	1.20	1.10	2.09	0.64	2.24	1.29
				uencies =	Rank	2,329	50	1,001	3,480	286	25,273	176	45	7,647	2,049		6	842	14	14	200	878	732	18,100	175
	Results	hts	10.0, $w_{sc} = 1.0$	Freq	Good Peaks	26	594	94	82	532	1	781	109	66	12		5,723	61	1,255	4,752	2,469	113	637	16	319
	F <sup>2</sup> Dock ]	Weig	$v_{ss} = 1.0, w_{cc} = 1.0$	32 <sup>3</sup>	RMSD (Å)	3.01	1.90	1.24	4.09	1.26	4.61	1.70	1.48	2.08	5.21	4.69	0.46	1.58	1.27	0.75	1.11	1.61	0.86	3.15	2.27
			•	uencies = .	Rank	5,240	130	5,742	785	320	17,662	262	2,607	2,059	-	43,036	8	3,687	36	5	170	1,296	65	3,5060	4,586
				Freq	Good Peaks	40	581	42	58	427	3	588	121	92	-	2	6,041	<i>L</i> 6	719	3,289	2,508	206	512	8	212
EE	E/AC	CM T	Trans	Com	Unbound Mol 2	10UP AB	1EQL	$1 \text{TF}_{u-A}^{\mathcal{D}}$	1EQ	1CD&AB	3DMI_	1BAGs Tu <sup>7</sup> B	1A ISO_B	aidat 114	1CM	2VPH GH	1DKS_A	3LZT-	1HaE_	1HFFT_	1K9B_A	1CX8_AB	2BNH_	3LZT_	1CJE_D
				Data	d Complex	tK_C:AB	CB_E:I	W_AB:C	K4_A:D	J_AB:DE	TN_A:D	VX_A:B	Y7_A:B	6C_A:B	JX_HL:T	HL:VW	UH_A:B	/K_DE:F	VN_P:T	GI_E:I	6R_A:I	4_AB:CF	DFJ_E:I	QJ_AB:C	6E_A:B

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				F <sup>2</sup> Dock	Results							F <sup>2</sup> Dock	Results		
				Wei	ghts							Weig	ghts		
				$w_{ss} = 1.0, w_{cc} =$	10.0, $w_{sc} = 1.0$						Ŧ	$v_{ss} = 1.0, w_{cc} =$	10.0, $w_{sc} = 1.0$		
D	ıta	Freq	juencies =	: 32 <sup>3</sup>	Freq	uencies =	64 <sup>3</sup>	Da	ta	Freq	uencies =	32 <sup>3</sup>	Freq	uencies = (	643
d Complex	Unbound Mol 2	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Bound Complex	Unbound Mol 2	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)
6J_HL:P	1A53	-		6.99	23	23,314	1.93	INCA_HL:N	_ennt	37	7,406	1.50	67	3,133	0.91
96_A:B	A_MHI	252	514	1.62	150	2,084	1.74	S: TH_NSN1	1KDC_	69	7,846	2.09	106	1,996	2.09
AW_A:B		837	203	2.21	1,460	149	1.54	1PPE_E:I	ILU0_A	2,994	205	1.68	3,171	18	1.27
3R_A:BC	1ERN AB	112	29	2.86	534	47	1.79	1QA9_A:B	1CCZ_A	26	15,078	2.59	40	4,334	1.57
WY_A:C	1CZ <sup>u</sup> tr_A	2,253	129	1.14	2,160	1	1.04	1QFW_IM:AB	1HRP_AB	35	1,371	1.34	11	4,852	1.57
TU_C:AB	1EC AB	61	24	3.23	113	51	3.36	1RLB_ABCD:E	1HBP_	30	10,452	2.20	10	16,389	2.16
34_A:B	1F3 <b>8</b> 197	528	65	1.28	875	15	1.13	1SBB_A:B	1SE4_	6	30,808	4.24	4	18,560	4.07
51_AB:E	1SRAC	168	2,553	3.05	351	499	1.63	1TMQ_A:B	1B1U_A	309	6	1.60	504	12	1.33
NK_HL:T	1TF <u>y</u> B	39	1,391	2.41	58	2,184	2.72	1UDI_E:I	2UGI_B	398	1,071	1.51	509	192	1.06
C2_C:D	1FC FAB	ı	1	5.61	1	1	6.04	1VFB_AB:C	$^{-}ZX^{-}8$	129	8,387	2.53	96	2,511	1.84
Q1_A:B	$1B3 \vec{B}_{-}A$	15	4,591	4.23	1	28,985	4.87	1WEJ_HL:F	1HRC_	I	ı	6.57	4	27,001	3.62
QJ_A:B	1FQFA	325	21	1.75	277	124	1.99	1WQ1_R:G	1WER_	868	379	1.40	1,080	93	1.44
K_BC:A	1B菜1	39	14,829	2.19	27	8,442	1.75	2BTF_A:P	1PNE_	126	7,748	1.57	89	3,769	0.87
cQ_B:C	1GC# B	1,280	20	1.18	1,263	2	1.30	2HMI_CD:AB	1S6P_AB	I	ı	5.73		ı	5.97
HQ_A:B	1LYAA	239	11	2.90	368	190	2.77	2JEL_HL:P	1POH_	46	14,110	2.76	6	25,303	3.29
2_A:BG	1TBG DH	42	1,990	1.35	14	10,191	1.61	2MTA_HL:A	2RAC_A	171	6,357	3.36	333	1,273	1.09
RN_A:B	-422 18∰1	171	3,286	1.59	239	708	1.23	2PCC_A:B	1YCC_	200	9,587	0.62	85	5,616	1.56
1V_A:G	1D0M_B	ı	ı	13.33	1	ı	13.49	2QFW_HL:AB	1HRP_AB	239	525	1.18	209	3,715	1.06
E1_C:A	1HHA	1,134	27	0.88	1,400	40	0.91	2SIC_E:I	3SSI_	328	550	1.59	207	838	2.39
E8_B:A	$1E8\overline{Z}$ A	6	28,558	3.50	62	4,239	2.14	2SNI_E:I	2CI2_I	234	855	2.53	262	2,688	1.87
IA_AB:I	1BXB_	454	90	2.61	641	1	2.20	2VIS_AB:C	2VIU_ACE	I	ı	7.02		ı	7.01
2M_A:B	1A12_A	532	48	0.84	576	27	0.87	7CEI_A:B	1M08_B	582	67	1.25	725	19	1.56

position. 'RMSD' is the lowest RMSD among all peaks that were shortlisted.  $F^2$ Dock used use 6° rotational sampling, and retained 50,000 peaks. RMSD was calculated using the  $C_{\alpha}$  atoms near the interface of the known bound conformation (within 5Å of the interface). Shape-complementarity-based bound-bound docking results with and without electrostatics using F<sup>2</sup>Dock. 'Rank' is the best rank among all predicted positions whose RMSD was less than 5Å. 'Good Peaks' is the number of peaks in the predicted set which were less than 5Å RMSD from the known

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			$v_E = 350$	RMSD (Å)	2.16	1.69	0.91	1.74	3.09	0.99	0.85	1.31	0.69	0.55	1.38	1.13	0.61	96.0	1.69	0.84	2.74	2.67	3.31	6.71
F <sup>2</sup> Dock Results	1.0		trostatics 1	Rank	26,792	1,189	56	166	8,490	81	666	5,984	42	341	297	1,558	190	54	563	11	768	4,134	31,822	,
	$w_{cc} = 10.0, w_{sc} =$	cies = 32 <sup>3</sup>	With Elec	Good Peaks	8	79	190	289	38	315	458	49	324	311	437	41	1,323	84	238	726	634	180	5	,
	ghts: $w_{ss} = 1.0$ ,	Frequenc	ics $w_E = 0$	RMSD (Å)	1.75	1.69	0.91	1.87	1.00	66.0	1.51	1.31	0.83	0.55	1.38	1.13	0.80	0.98	1.70	0.93	3.48	3.56	1.04	6.71
	Weig		lectrostat	Rank	25,200	2,794	181	398	277	772	1,414	4,338	1,370	1,018	1,097	424	2,965	203	1,511	197	6,719	17,851	27,310	1
			Without E	Good Peaks	12	37	141	120	194	85	346	53	79	187	322	43	64	70	104	81	58	26	12	
	<u>.</u>		Data	Bound Complex	114D_D:AB	119R_HL:ABC	1IB1_AB:E	11BR_A:B	1IJK_BC:A	11QD_AB:C	1JPS_HL:T	1K4C_AB:C	1K5D_AB:C	1KAC_A:B	1KKL_ABC:H	1KLU_AB:D	1KTZ_A:B	1KXP_A:D	1KXQ_H:A	1M10_A:B	1MAH_A:F	1ML0_AB:D	1MLC_AB:E	1N2C_ABCD:EF
			$w_E = 350$	RMSD (Å)	0.60	0.45	0.79	0.34	0.93	3.81	0.64	0.55	0.94	1.40	7.47	0.26	0.41	96.0	0.40	0.35	1.36	0.61	3.16	1.02
F <sup>2</sup> Dock Results	1.0		trostatics	Rank	50	1	5,542	5	12	12,168	10	941	1,588	44		2	310	44	1	41	38	1	10,128	3
	$w_{cc} = 10.0, w_{sc} =$	cies = 32 <sup>3</sup>	With Elec	Good Peaks	440	2,731	46	2,665	607	16	1,114	145	86	29		3,106	279	154	2,132	1,947	299	3,156	31	873
	Weights: $w_{ss} = 1.0$ , y	Frequen	$\log w_E = 0$	RMSD (Å)	09:0	0.45	0.79	0.34	0.93	3.81	0.64	0.55	0.94	1.40	7.39	0.33	0.66	86.0	0.40	0.35	1.36	0.61	2.23	1.18
			ectrostatic	Rank	232	-	5,807	13	32	11,589	46	1,867	911	35		8	1,831	3	1	40	51	1	3,336	34
			Without E	Good Peaks	240	2,005	29	1,417	286	10	729	111	108	33		3,367	72	552	1,622	2,086	282	248	112	251
			Data	Bound Complex	1A2K_C:AB	1ACB_E:I	1AHW_AB:C	1AK4_A:D	1AKJ_AB:DE	1ATN_A:D	1AVX_A:B	1AY7_A:B	1B6C_A:B	1BGX_HL:T	1BJ1_HL:VW	1BUH_A:B	1BVK_DE:F	1BVN_P:T	1CGI_E:I	1D6R_A:I	1DE4_AB:CF	1DFJ_E:I	1DQJ_AB:C	1E6E_A:B

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Veriphics $\mu_{\mu} = IA, \eta_{\nu,\mu} = IA, \eta_{\mu,\mu} = IA,$				F <sup>2</sup> Dock	Results						F <sup>2</sup> Dock	Results		
Formericand matrix from the first from the fi			Weig	thts: $w_{ss} = 1.0, w_{ss}$	$v_{cc} = 10.0, w_{sc} =$	1.0				Weig	hts: $w_{ss} = 1.0$ ,	$v_{cc} = 10.0, w_{sc} =$	1.0	
Mithous Flactronatices $y_{a} = 340$ With Electronatices $y_{a} = 340$ With Electronatices $y_{a} = 340$ (2012)     Sub				Frequenc	ies = 32 <sup>3</sup>						Frequenc	ies = 32 <sup>3</sup>		
Good Peaks         RMSD (Å)		Without E	lectrostati	$\operatorname{ics} w_E = 0$	With Elect	trostatics	$w_E = 350$	Data	Without E	lectrostati	$\cos w_E = 0$	With Elect	trostatics 1	$v_E = 350$
9         6,805         6,435         18         4,873         16,5         16,7         16,5         16,7         1		Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)	Bound Complex	Good Peaks	Rank	RMSD (Å)	Good Peaks	Rank	RMSD (Å)
(3)         (3)         (13)         (	-	6	6,805	4.35	18	4,873	4.15	1NCA_HL:N	40	6,351	1.57	25	8,636	1.57
4516901141.8511001.141.8711.076.001.4716.001.410.72935.7271.561.591.5371.5371.5371.5371.5371.4712.291.4712.291.4712.2965777190.731.2371.2371.2371.2371.2371.2471.2471.2471.2471.2471.24757711.11.1352.9711.131.1371.1371.1371.1371.1371.1371.13720441.11.1372.1471.1371.1371.1371.1471.1371.1471.14720411.131.1371.1371.1371.1371.1471.1471.1471.1471.14720411.1371.1371.1371.1471.1471.1471.1471.1471.14720411.1371.1371.1471.1471.1471.1471.1471.1471.14720411.131.1371.1471.1471.1471.1471.1471.1471.14720411.141.1471.1471.1471.1471.1471.1471.1471.14720411.141.1471.1471.1471.1471.1471.1471.1471.14720411.141.1471.1471.1471.1471.1471.1471.1471.14720411.141.1471.147		139	946	1.26	174	1,053	1.26	S:'TH <sup>¬</sup> NSN1	42	5,504	2.85	19	8,735	3.15
295.771.561.995311.551.641.551.641.551.4712251.4712251.4712251.4712251.4712261.4712271.4712291.4712291.4712291.4712291.4712291.4712291.4712391.4712391.4712391.4712391.4712391.4712391.4372341.4352341.4372341.4372341.4372341.4372341.4372341.4372341.4372341.4372341.4372341.4372341.4372341.4372342341.4372342		451	59	1.14	1,851	10	1.14	1PPE_E:I	1,767	1	0.77	630	1	0.77
657         779         0.73         1.285         447         0.62         10FW_MAB         256         433         647         7351         147         793         147         193           148         1         1.03         247         1         1.03         11.3         7351         174         103         7351         174         103         174           264         1         1.05         271         112         782         118         174         103         216         174         103         174         103           264         125         112         782         113         114         115         147         103         216         174         103         174         103           264         126         127         783         118         112         783         118         116 </td <td>_</td> <td>29</td> <td>5,727</td> <td>1.56</td> <td>159</td> <td>531</td> <td>1.55</td> <td>1QA9_A:B</td> <td>701</td> <td>77</td> <td>1.25</td> <td>1,471</td> <td>22</td> <td>0.84</td>	_	29	5,727	1.56	159	531	1.55	1QA9_A:B	701	77	1.25	1,471	22	0.84
$148$ $24$ $1.00$ $145$ $9$ $100$ $101$ $100$ $7951$ $791$ $791$ $791$ $777$ $1$ $1.33$ $297$ $1$ $1.33$ $1.38$ $1.88$ $1.42$ $1.92$ $214$ $1.92$ $264$ $642$ $2.21$ $112$ $782$ $2.51$ $11MQ_{ABB}$ $55$ $302$ $1.02$ $294$ $108$ $294$ $1.89$ $2.31$ $1.89$ $1.89$ $1.89$ $1.89$ $1.1MQ_{ABB}$ $55$ $324$ $1.15$ $271$ $197$ $307$ $2.530$ $0.49$ $1.30$ $3.749$ $1.18$ $1.1MQ_{ABB}$ $574$ $1.15$ $274$ $1.92$ $307$ $1.89$ $2.78$ $1.89$ $1.7MQ_{ABB}$ $1.89$ $1.1MQ_{ABB}$ $1.96$ $2.78$ $1.97$ $307$ $1.89$ $2.79$ $1.30$ $1.74$ $1.89$ $1.97$ $1.97$ $2.99$ $2.78$ $1.97$ $2.50$ $1.90$ $1.20$ $1.74$ $1.90$ $1.97$ $2.94$ $1.96$ $2.78$ $1.96$ $1.10$ $2.20$ $1.20$ $1.20$ $1.20$ $1.20$ $1.20$ $2.78$ $1.97$ $2.78$ $2.70$ $1.90$ $2.79$ $1.74$ $2.96$ $1.47$ $1.06$ $2.96$ $1.29$ $2.78$ $2.70$ $1.20$ $1.20$ $1.20$ $1.20$ $1.20$ $1.20$ $1.20$ $2.78$ $2.78$ $2.70$ $1.90$ $1.20$ $1.20$ $1.20$ $1.20$ $1.20$ $1.20$		657	<i>6LT</i>	0.73	1,285	447	0.62	1QFW_IM:AB	226	433	0.89	332	147	0.89
$577$ $1$ $1.35$ $297$ $1$ $1.35$ $1.8B_{\rm A}.B$ $64$ $9,509$ $1.42$ $013$ $91,56$ $1.26$ $264$ $642$ $2.21$ $112$ $782$ $2.51$ $11MO_{\rm A}.B$ $55$ $302$ $106$ $597$ $247$ $108$ $297$ $974$ $1.89$ $2.81$ $818$ $1.89$ $1.18$ $1VPB_{\rm A}B.C$ $156$ $374$ $11.5$ $977$ $18$ $097$ $307$ $2530$ $0.49$ $1.30$ $3749$ $1.87$ $1.87$ $2.76$ $1.97$ $1.97$ $1.97$ $317$ $2.70$ $1.30$ $2.79$ $1.81$ $1.90$ $1.90$ $3.749$ $1.97$ $1.97$ $317$ $2.90$ $1.30$ $1.72$ $2.90$ $1.78$ $1.97$ $1.97$ $2.78$ $1.92$ $317$ $1.90$ $2.91$ $1.90$ $1.90$ $1.90$ $1.90$ $1.90$ $1.97$ $1.97$ $1.97$ $206$ $1.90$ $1.90$ $1.90$ $2.78$ $1.91$ $2.76$ $1.90$ $2.78$ $1.92$ $1.149$ $1.90$ $1.90$ $2.91$ $1.90$ $2.76$ $1.90$ $2.78$ $1.92$ $1.92$ $2014$ $1.90$ $2.91$ $1.90$ $2.78$ $1.91$ $2.96$ $1.97$ $2.96$ $1.92$ $2114$ $1.90$ $1.90$ $1.91$ $2.91$ $1.91$ $2.92$ $1.91$ $1.92$ $1.92$ $2114$ $1.91$ $2.91$ $1.91$ $2.91$ $1.91$ $2.92$ $1$		148	24	1.09	145	6	1.09	1RLB_ABCD:E	24	5,651	1.74	10	7,951	1.74
$264$ $642$ $2.21$ $112$ $782$ $2.51$ $1TMQ_AB$ $55$ $302$ $106$ $59$ $254$ $1.8$ $27$ $974$ $189$ $28$ $818$ $189$ $101P_{121}$ $135$ $324$ $115$ $977$ $18$ $070$ $370$ $530$ $049$ $130$ $3.749$ $118$ $1VB_AB:C$ $156$ $349$ $0.59$ $271$ $18$ $073$ $310$ $187$ $0.73$ $2.90$ $130$ $3.749$ $118$ $1VB_AB:C$ $156$ $349$ $0.59$ $271$ $199$ $073$ $1143$ $187$ $0.73$ $220$ $1.376$ $2.742$ $1.844$ $2.266$ $1.47$ $869$ $1.72$ $0.43$ $1149$ $110$ $0.49$ $311$ $232$ $094$ $1.89$ $2BT_APP$ $244$ $147$ $869$ $1.727$ $0.72$ $1149$ $110$ $0.49$ $311$ $232$ $0.43$ $2BT_APP$ $244$ $147$ $869$ $1.727$ $0.72$ $1149$ $110$ $0.40$ $311$ $232$ $0.43$ $2BT_APP$ $244$ $147$ $896$ $0.79$ $0.72$ $1149$ $110$ $0.40$ $311$ $232$ $0.43$ $211-142$ $2142$ $2162$ $1147$ $869$ $1.72$ $0.72$ $1149$ $110$ $110$ $0.40$ $113$ $0.40$ $1142$ $0.72$ $0.72$ $0.72$ $0.72$ $1149$ $110$ $110$ $0.412$ $1120$ $0.72$ <td< td=""><td></td><td>577</td><td>-</td><td>1.35</td><td>297</td><td></td><td>1.35</td><td>1SBB_A:B</td><td>64</td><td>9,509</td><td>1.42</td><td>103</td><td>9,156</td><td>1.42</td></td<>		577	-	1.35	297		1.35	1SBB_A:B	64	9,509	1.42	103	9,156	1.42
29 $914$ $1.89$ $28$ $818$ $1.89$ $1.89$ $1.89$ $1.89$ $0.71$ $0.77$ $18$ $0.79$ $307$ $2.530$ $0.49$ $130$ $3.749$ $1.18$ $1.78$ $1.79$ $2.78$ $1.99$ $2.78$ $1.99$ $0.59$ $143$ $187$ $0.73$ $2.79$ $1.376$ $1.376$ $1.78$ $1.78$ $2.78$ $1.78$ $1.78$ $711$ $2.220$ $3.22$ $2.20$ $1.376$ $2.76$ $1.76$ $2.47$ $1.69$ $2.78$ $1.78$ $2.06$ $1.030$ $1.89$ $2.231$ $0.94$ $1.89$ $2.76$ $1.78$ $2.96$ $1.79$ $2.78$ $1.78$ $2.06$ $1.030$ $1.89$ $2.231$ $2.94$ $1.89$ $2.74$ $1.79$ $2.79$ $2.78$ $1.78$ $1.149$ $11$ $0.40$ $1.31$ $2.32$ $2.94$ $1.89$ $2.74$ $1.79$ $2.76$ $2.78$ $2.78$ $1.149$ $11$ $0.40$ $2.11$ $2.74$ $2.74$ $2.47$ $1.47$ $8.94$ $1.79$ $2.74$ $1.149$ $11$ $0.40$ $2.12$ $2.74$ $1.47$ $2.90$ $1.74$ $2.92$ $1.41$ $1.147$ $2.94$ $1.88$ $1.21$ $3.71$ $1.42$ $2.76$ $1.78$ $2.92$ $1.41$ $1.147$ $3.29$ $1.21$ $3.71$ $1.42$ $2.76$ $1.78$ $2.92$ $1.41$ $1.147$ $3.29$ $1.21$ $3.71$ $1.42$ $2.76$ <t< td=""><td></td><td>264</td><td>642</td><td>2.21</td><td>112</td><td>782</td><td>2.51</td><td>1TMQ_A:B</td><td>55</td><td>302</td><td>1.06</td><td>59</td><td>254</td><td>1.08</td></t<>		264	642	2.21	112	782	2.51	1TMQ_A:B	55	302	1.06	59	254	1.08
$307$ $2,530$ $0.49$ $130$ $3,749$ $1.18$ $1VFE_AB:C$ $156$ $349$ $0.59$ $271$ $159$ $0.59$ $143$ $187$ $0.73$ $$ $  1WE_1H:F$ $484$ $2.266$ $1.36$ $389$ $2.778$ $1.36$ $71$ $2,220$ $3.22$ $2.20$ $1.376$ $2.76$ $1WQ_1EG$ $447$ $10$ $0.49$ $1,127$ $2$ $0.44$ $206$ $1.30$ $2.32$ $994$ $1.89$ $2.76$ $1WQ_1EG$ $447$ $10$ $0.49$ $1,127$ $2.78$ $1.31$ $1,149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HF_A:P$ $244$ $1.47$ $866$ $9.529$ $1.31$ $1,149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HF_A:P$ $244$ $1.47$ $866$ $9.539$ $1.31$ $1,149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HF_A:P$ $244$ $3.02$ $1.47$ $866$ $9.539$ $1.31$ $1,149$ $11$ $0.40$ $311$ $2.32$ $2312$ $241$ $44$ $3.02$ $1.67$ $2.97$ $2.97$ $1,149$ $126$ $1.23$ $1.23$ $1.24$ $1.23$ $214$ $1.47$ $3.02$ $1.67$ $2.94$ $1.64$ $1,17$ $16$ $2.24$ $1.23$ $212$ $1.24$ $2.06$ $1.23$ $2.94$ $1.64$ $1.41$ $129$ $129$ $1.21$ $1.23$ $1.21$ $1.24$ $1.24$		29	974	1.89	28	818	1.89	1UDI_E:I	135	324	1.15	779	18	0.94
$143$ $187$ $0.73$ $\cdot$ $\cdot$ $\cdot$ $\mathbf{WEJ-HL:F$ $484$ $2.26$ $1.36$ $389$ $2.778$ $1.73$ $71$ $2.220$ $3.22$ $220$ $1.376$ $2.76$ $1WQI_R:G$ $447$ $10$ $0.49$ $1.127$ $22$ $0.49$ $206$ $1.930$ $1.89$ $2.33$ $994$ $1.89$ $2.81F_{-}EP$ $244$ $18,464$ $1.47$ $866$ $9.529$ $1.31$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HT_{-}EP$ $244$ $18,464$ $1.47$ $86$ $9.529$ $1.31$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HT_{-}EP$ $244$ $1.47$ $86$ $9.529$ $1.31$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HT_{-}EP$ $2HL_{-}P$ $244$ $814$ $816$ $9.529$ $1.147$ $16$ $2.84$ $1.33$ $2174$ $1.42$ $2MT_{-}HL:P$ $3.02$ $1.69$ $3.124$ $2.69$ $1.17$ $16$ $2.84$ $1.33$ $2174$ $1.42$ $3.30$ $269$ $1.67$ $89$ $3.124$ $1.17$ $329$ $1.21$ $377$ $392$ $2174$ $1.44$ $3.02$ $1.696$ $1.696$ $1.696$ $1.17$ $106$ $1.23$ $1.21$ $1.27$ $1.27$ $2.142$ $3.23$ $2.141$ $1.26$ $1.29$ $1.24$ $1.24$ $1.29$ $1.29$ $1.28$ $1.29$ $1.28$ $1.29$ $1.29$ <td></td> <td>307</td> <td>2,530</td> <td>0.49</td> <td>130</td> <td>3,749</td> <td>1.18</td> <td>1VFB_AB:C</td> <td>156</td> <td>349</td> <td>0.59</td> <td>271</td> <td>159</td> <td>0.59</td>		307	2,530	0.49	130	3,749	1.18	1VFB_AB:C	156	349	0.59	271	159	0.59
$71$ $2.220$ $3.22$ $220$ $1.376$ $2.76$ $IWQLR:G$ $447$ $10$ $0.49$ $1.127$ $2$ $0$ $0.13$ $206$ $1.030$ $1.89$ $2.33$ $994$ $1.89$ $2.81T_A:P$ $244$ $1.47$ $86$ $9.529$ $1.31$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HL-HL:P$ $244$ $1.47$ $86$ $9.52$ $5.34$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HL-HL:P$ $444$ $3.02$ $1.67$ $894$ $3.12$ $1.71$ $16$ $2.84$ $337$ $2.742$ $3.83$ $2.1EL-HL:P$ $444$ $3.029$ $1.07$ $894$ $3.65$ $1.71$ $16$ $2.24$ $1.85$ $1.21$ $3.77$ $1.42$ $2.742$ $3.30$ $2169$ $1.58$ $894$ $305$ $1.44$ $1.77$ $1.29$ $2.742$ $3.83$ $2.1EL-HL:P$ $3.30$ $269$ $1.67$ $894$ $3.65$ $1.44$ $1.77$ $3.29$ $1.21$ $3.77$ $1.42$ $2.742$ $3.30$ $269$ $1.69$ $3.74$ $0.66$ $1.77$ $3.29$ $1.21$ $3.77$ $1.22$ $2.742$ $3.74$ $2.67$ $894$ $305$ $1.44$ $1.77$ $3.29$ $1.21$ $3.74$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ $1.79$ $0.59$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ $1.21$ <		143	187	0.73	1		I	1WEJ_HL:F	484	2,266	1.36	389	2,778	1.36
$206$ $1.030$ $1.89$ $233$ $994$ $1.89$ $2BTF_A:P$ $24$ $18,464$ $1.47$ $86$ $9.529$ $1.31$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $2HM_LCD:AB$ $$ $ 5.91$ $86$ $9.52$ $1.34$ $1.149$ $11$ $0.40$ $311$ $328$ $0.43$ $21BL_HL:P$ $44$ $3.02$ $1.05$ $89$ $3.124$ $0.86$ $1.71$ $16$ $2.244$ $185$ $1.27$ $1.277$ $1.42$ $2MT_AHL:A$ $330$ $269$ $1.58$ $834$ $305$ $1.41$ $1.47$ $329$ $1.21$ $377$ $39$ $1.202$ $2NT_AHL:A$ $330$ $269$ $1.58$ $834$ $305$ $1.41$ $1.47$ $329$ $1.21$ $377$ $39$ $1.202$ $2PC_A:B$ $216$ $503$ $1.56$ $305$ $1.41$ $1.47$ $329$ $1.21$ $377$ $39$ $1.202$ $2PC_A:B$ $216$ $503$ $1.58$ $344$ $305$ $1.47$ $329$ $1.21$ $377$ $392$ $217$ $207$ $216$ $503$ $1.36$ $243$ $366$ $9.69$ $1.99$ $1.91$ $1.92$ $1.38$ $1.20$ $216$ $503$ $1.96$ $1.63$ $9.69$ $1.79$ $0.99$ $1.38$ $1.12$ $0.59$ $1.28$ $216$ $1.28$ $1.26$ $9.69$ $1.28$ $1.98$ $0.99$ $1.38$ $1.98$ $1.28$ $216$ $216$		71	2,220	3.22	220	1,376	2.76	1WQ1_R:G	447	10	0.49	1,127	2	0.49
1,149         11         0.40         311         328         0.43         2HMLCD:AB         -         5,91         -         5,91         -         5,91         -         5,91         -         5,91         0.312         0.313           171         16         2.84         33         2.742         3.83         2.16L_HL:P         44         3,029         1.05         89         3,124         0.36           6         1.247         1.37         1.42         2.47         3.30         269         1.58         83.4         305         1.41           147         329         1.217         1.42         2.47         3.30         269         1.58         83.4         305         1.41           147         329         1.21         377         39         1.20         269         1.58         83.4         305         1.41           147         329         1.21         371         1.20         2.26         216         503         1.56         305         1.41           1.08         310         1.10         1.10         1.10         1.20         2.13         1.40         1.41         1.40         1.40         1.41         1.41<		206	1,030	1.89	233	994	1.89	2BTF_A:P	24	18,464	1.47	86	9,529	1.31
$171$ $16$ $2.84$ $33$ $2.742$ $3.83$ $2.1EL_HL.P$ $44$ $3.029$ $1.05$ $89$ $3.124$ $0.36$ $6$ $2.224$ $1.85$ $1.2$ $1.277$ $1.42$ $2.MT_ALL.A$ $330$ $269$ $1.58$ $834$ $305$ $1.41$ $147$ $329$ $1.21$ $377$ $39$ $1.20$ $2.26C_A.B$ $2.30$ $269$ $1.58$ $834$ $305$ $1.41$ $233$ $6.904$ $1.38$ $11$ $16,219$ $1.38$ $2.26FW_LH.AB$ $170$ $1.106$ $0.91$ $243$ $364$ $0.91$ $233$ $6.904$ $1.38$ $11$ $16,219$ $1.38$ $2.20FW_LH.AB$ $170$ $1.106$ $0.91$ $243$ $364$ $0.91$ $1.008$ $33$ $0.59$ $1.438$ $1$ $0.59$ $1.38$ $2.16$ $889$ $1$ $0.64$ $173$ $7$ $0.64$ $1.008$ $3$ $0.517$ $0.51$ $0.51$ $0.51$ $0.51$ $0.51$ $0.51$ $0.94$ $173$ $7$ $0.64$ $1.008$ $10$ $0.52$ $3.731$ $0.59$ $2.17$ $889$ $1$ $0.64$ $173$ $7$ $0.67$ $1.853$ $1$ $0.52$ $3.731$ $1$ $0.52$ $2.116$ $809$ $1$ $0.809$ $1$ $0.809$ $1$ $0.81$ $1.853$ $1$ $0.99$ $1.633$ $2$ $0.98$ $10$ $0.91$ $0.94$ $10$ $1.17$ $1.17$ $1.853$ $0.99$ <		1,149	11	0.40	311	328	0.43	2HMI_CD:AB	1	ı	5.91	I	I	5.34
6 $2,224$ $1.85$ $12$ $1,277$ $1.42$ $2MTA_HL:A$ $330$ $269$ $1.58$ $834$ $305$ $1.41$ $147$ $329$ $1.21$ $377$ $39$ $1.20$ $2PCC_A:B$ $216$ $503$ $1.36$ $4,634$ $16$ $0.60$ $233$ $6,904$ $1.38$ $11$ $16,219$ $1.38$ $21.20$ $2PCL_A:B$ $170$ $1,106$ $243$ $243$ $7$ $0.64$ $1,098$ $3$ $0.59$ $1,438$ $1$ $0.59$ $2.312$ $2.517$ $2SNL_E:1$ $570$ $1$ $0.64$ $173$ $7$ $0.64$ $1,098$ $3$ $0.59$ $1,438$ $1$ $0.59$ $2.517$ $2.517$ $889$ $1$ $0.64$ $173$ $7$ $0.64$ $1,038$ $1$ $0.52$ $5.17$ $2.517$ $2SNL_E:1$ $889$ $1$ $0.64$ $173$ $7$ $0.64$ $1,833$ $1$ $0.52$ $3.731$ $1$ $0.52$ $2.17$ $889$ $1$ $0.89$ $1$ $0.89$ $1$ $0.89$ $1,833$ $1$ $0.52$ $3.731$ $1$ $0.52$ $2VL_A:B$ $8$ $12,239$ $2.17$ $8$ $2.676$ $2.668$ $2.17$ $1,833$ $1$ $0.99$ $1.633$ $2$ $0.99$ $1$ $0.54$ $2.17$ $0.94$ $2.68$ $2.17$ $1,934$ $0.99$ $1.633$ $2$ $0.98$ $1.62$ $0.24$ $0.24$ $0.24$ $10.26$ $0.24$ $1,934$		171	16	2.84	33	2,742	3.83	2JEL_HL:P	44	3,029	1.05	89	3,124	0.86
147         329         1.21         377         39         1.20         2PCC_A:B         216         503         1.36         4.634         16         0.60           233         6,904         1.38         11         16,219         1.38         2QFW_HI:AB         170         1,106         0.91         243         364         0.91           1,098         3         0.59         1,438         1         0.59         2.517         570         1         0.64         173         7         0.64           1,098         3         0.59         1,438         1         0.59         2.517         281L_E:1         570         1         0.64         173         7         0.64           1,038         1         0.59         1,438         1         0.59         2.17         2.67         2.67         2.67         2.67         2.67         2.67         2.67         2.64         1.7         0.64           1,038         3         0.59         1,438         1         0.59         2.17         2.67         2.67         2.67         2.67         2.67         2.64         2.67         2.64         2.64         2.64         2.64         2.64         <		9	2,224	1.85	12	1,277	1.42	2MTA_HL:A	330	269	1.58	834	305	1.41
23         6,04         1.38         11         16,219         1.38         2QFW_HL:AB         170         1,106         0.91         243         364         0.91           1,098         3         0.59         1,438         1         0.59         2SIC_E:1         570         1         0.64         173         7         0.64           1,098         3         0.59         1,438         1         0.59         2SIC_E:1         570         1         0.64         173         7         0.64           1,081         0.51         -         5.17         2SIL_E:1         889         1         0.89         1         0.81         0.64         1         0.64         1         0.64         0.71         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         0.64         1         1         0.64         1         1         0.64         1         1         0.64         1 <td></td> <td>147</td> <td>329</td> <td>1.21</td> <td>377</td> <td>39</td> <td>1.20</td> <td>2PCC_A:B</td> <td>216</td> <td>503</td> <td>1.36</td> <td>4,634</td> <td>16</td> <td>0.60</td>		147	329	1.21	377	39	1.20	2PCC_A:B	216	503	1.36	4,634	16	0.60
1,098         3         0.59         1,438         1         0.59         2SIC_E:1         570         1         0.64         173         7         0.64           -         -         5.17         -         -         5.17         2SNLE:1         889         1         0.81         809         1         0.81           1,853         1         0.52         5.17         2SNLE:1         889         1         0.81         809         1         0.81           1,853         1         0.52         2VIS_AB:C         8         12.239         2.17         8         12.678         2.17           129         433         0.99         1.633         2         0.94         2.468         58         0.34		23	6,904	1.38	11	16,219	1.38	2QFW_HL:AB	170	1,106	0.91	243	364	0.91
-         5.17         -         -         5.17         2.5.17         2.5.17         889         1         0.81         809         1         0.81         809         1         0.81           1.853         1         0.52         3.731         1         0.52         2VIS_AB:C         8         12,239         2.17         8         12,678         2.17           129         433         0.99         1,633         2         0.98         7CEL_A:B         518         162         0.34         2.468         58         0.34		1,098	3	0.59	1,438	1	0.59	2SIC_E:I	570	1	0.64	173	7	0.64
1.853         1         0.52         3.731         1         0.52         2VIS_AB:C         8         12,239         2.17         8         12,678         2.17           129         433         0.99         1,633         2         0.98         7CEL_A:B         518         162         0.34         2.468         58         0.34		-	1	5.17	1		5.17	2SNI_E:I	889	1	0.81	809	1	0.81
129 433 0.99 1,633 2 0.98 7CEL_A:B 518 162 0.34 2,468 58 0.34		1,853		0.52	3,731	1	0.52	2VIS_AB:C	8	12,239	2.17	8	12,678	2.17
		129	433	0.99	1,633	2	0.98	7CEI_A:B	518	162	0.34	2,468	58	0.34

### Algorithm 1

#### Inverse adaptive peak search

1:	Inputs:
2:	$-n^3$ : number of frequencies
3:	-h: accuracy of peak position
4:	- e: Compactly supported smooth decaying function
5:	[] at each $k \in I_{\hat{n}}$
6:	-τ: threshold for docking score
7:	-{(val, pos)}: Current output peak regions and
8:	[] scores
9:	Preprocessing: [Interval set: <i>I</i> = <i>intervals</i> ( <i>k</i> )]
10:	while $I \neq \emptyset$ do
11:	<i>interval</i> ← <i>I.next</i> ()
12:	if interval.isLowRes() then
13:	$t \leftarrow 0, \{\varphi\} \leftarrow interval.overlapping\varphi()$
14:	for $\varphi \in \{\varphi\}$ do
15:	if $\varphi > 0$ then
16:	<b>if</b> <i>interval.isOutside</i> ( $\phi$ ) <b>then</b>
17:	$t \leftarrow t + \varphi(interval.fIdx(\varphi.center))$
18:	else
19:	$t \leftarrow t + \varphi_{max}$
20:	end if
21:	else
22:	$t \leftarrow t - \varphi$ (interval.fldx( $\varphi$ .center))
23:	end if
24:	end for
25:	if $(t > \tau)$ then
26:	$I \leftarrow I \cup interval.subIntervals()$
27:	[] [midpoint subdivision based on h]
28:	end if
29:	else
30:	update({(val, pos)},interval)
31:	end if
32:	end while
33:	Output: [{(val, pos)}]