# Feature-Based Sequence-to-Sequence Matching\*

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Abstract. This paper studies the problem of matching two unsynchronized video sequences of the same dynamic scene, recorded by different stationary uncalibrated video cameras. The matching is done both in *time* and in *space*, where the spatial matching can be modeled by a homography (for 2D scenarios) or by a fundamental matrix (for 3D scenarios). Our approach is based on matching space-time *trajectories* of moving objects, in contrast to matching interest *points* (e.g., corners), as done in regular feature-based image-to-image matching techniques. The sequences are matched in space and time by enforcing consistent matching of all points along corresponding space-time trajectories.

By exploiting the dynamic properties of these space-time trajectories, we obtain sub-frame temporal correspondence (synchronization) between the two video sequences. Furthermore, using trajectories rather than feature-points significantly reduces the combinatorial complexity of the spatial point-matching problem when the search space is large. This benefit allows to match information across sensors in situations which are extremely difficult when only image-to-image matching is used, including: (a) matching under large scale (zoom) differences, (b) very wide base-line matching, and (c) matching across different sensing modalities (e.g., IR and visible-light cameras). We show examples of recovering homographies and fundamental matrices under such conditions.

**Keywords:** sequence-to-sequence matching, alignment in space and time, dynamic information, multi-sensor alignment, wide base-line matching, trajectory matching.

### 1. Introduction

Image-to-image matching methods, e.g., (Faugeras et al., 2001; Hartley and Zisserman, 2000; Xu and Zhang, 1996; Bergen et al., 1992; Szeliski and Shum, 1997; Zhang et al., 1995; Zoghlami et al., 1997), are inherently restricted to the information contained in individual images, i.e.,

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the spatial variations within image frames (which capture the scene appearance). But there are cases when there is not enough common spatial information within the two images to allow reliable image matching. One such example is illustrated in Fig. 1. The input images 1.a and 1.b contain a single object, but we want to match (or align) the entire frame. Alignment of image 1.a to image 1.b is not uniquely defined (see Fig. 1.c). However, a video sequence contains much more information than any individual frame does. In particular, a video sequence captures information about scene dynamics such as the trajectory of the moving object shown in Fig. 1.d and 1.e, which in this case provides enough information for unique alignment both in space and in time (see Fig. 1.f). The scene dynamics, exemplified here by trajectories of moving objects, is a property that is inherent to the scene, and is thus common to all sequences recording the same scene, even when taken from different video cameras. It therefore forms an additional or alternative powerful cue for matching video sequences.

The benefits of exploiting scene dynamics for matching sequences was noted before. Caspi and Irani (Caspi and Irani, 2000) described a direct (intensity-based) sequence-to-sequence alignment method. Their method is based on finding the space-time transformation which minimizes the intensity differences (SSD) between the two sequences, and was applied to cases where the spatial relation between the sequences could be modeled by a 2D parametric transformation (a homography). It was shown to be useful for addressing rigid as well as complex non-rigid changes in the scene (e.g., flowing water), and changes in illumination. However, that method does not apply when the two sequences have different appearance properties, such as with sensors of different sensing modalities, nor when the spatial transformation between the two sequences is very large, such as in wide base-line matching, or in large differences in zoom.

This paper illustrates a feature-based approach for space-time matching of video sequences. The "features" in our method are space-time trajectories constructed from moving objects. This approach can recover the 3D epipolar geometry between sequences recorded by widely separated video cameras, and can handle significant differences in appearance between the two sequences.

The advantage of this approach over using regular feature-based image-to-image matching is illustrated in Fig. 2. This figure shows two sequences recording several small moving objects. Each feature point in the image-frame of Fig. 2.a (denoted by A-E) can in principle be matched to any other feature point in the image-frame of Fig. 2.b. There is no sufficient information in any individual frame to uniquely resolve the point correspondences. Point trajectories, on the other hand, have

additional shape properties which simplify the *trajectory* correspondence problem (i.e., which trajectory corresponds to which trajectory) across the two sequences, as shown in Fig. 2.c and 2.d.

Stein (Stein, 1998) and Lee et.al. (Lee et al., 2000) described a method for estimating a time shift and a homography between two sequences based on alignment of centroids of moving objects. However, in (Stein, 1998; Lee et al., 2000) the centroids were treated as an unordered collection of feature points and not as trajectories. In contrast, we enforce correspondences between trajectories, thus avoiding the combinatorial complexity of establishing point matches of all points in all frames, resolving ambiguities in point correspondences, and allowing for temporal correspondences at sub-frame accuracy. This is not possible when the points are treated independently (i.e., as a "cloud of points").

Section 2 formulates the underlying problem, and Section 3 presents our sequence matching algorithm that is based on matching feature trajectories. The algorithm receives as input two unsynchronized video sequences and simultaneously estimates the parameters of the temporal and spatial transformation (relation) between the two sequences. Temporal misalignment (unsynchronization) occurs when the two input sequences have a time-shift (offset) between them (e.g., if the cameras were not activated simultaneously), and/or when they have different frame rates (e.g., PAL vs. NTSC). The *spatial* relation between the two sequences results from the camera setups. We have implemented two variants for the two following camera setups: (i) when the spatial relation between the two sequences is a 2D projective transformation (i.e., a homography), and (ii) when the spatial relation between the two sequences is expressed by epipolar geometry (i.e., a fundamental matrix).

Section 4 shows that by replacing point features with trajectories of moving points we can address several cases which are very difficult for regular image-to-image matching. We show that situations that are inherently ambiguous for image-to-image matching methods are often uniquely resolved by the sequence-to-sequence matching approach. In particular, these include situations where there is very little common appearance (spatial) information across the two sequences, such as in sequences of different sensing modalities (e.g., Infra-Red and Visible-light sensors), large scale differences, and wide base-lines between the cameras. We apply our method to such examples, and show that consistency of the scene dynamics (i.e., temporal cues across sequences) can become a major source of information for matching video sequences both in time and in space.

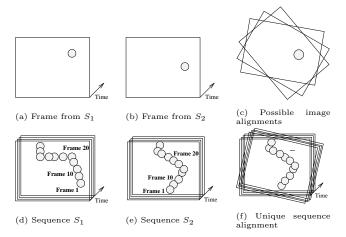


Figure 1. Spatial ambiguities in image-to-image alignment (a) and (b) show two temporally corresponding frames from two different video sequences viewing the same moving ball. There are infinitely many valid image alignments between the two frames, some of them shown in (c). (d) and (e) display the two sequences of the moving ball. There is only one valid alignment of the two trajectories of the ball. This uniquely defines the alignment both in time and in space between the two video sequences (f).

# 2. Problem Formulation

Let S and S' be two input image sequences, where S denotes the "reference" sequence, and S' denotes the second sequence. Let  $\vec{\mathbf{x}} = (x, y, t)$  be a  $space-time\ point$  in the reference sequence S (namely, a pixel (x, y) at frame (time) t) and let  $\vec{\mathbf{x}}' = (x', y', t')$  be the matching space-time point in sequence S'. The recorded scene can change dynamically, i.e., it can include moving objects. The cameras can be either stationary or jointly moving with fixed (but unknown) internal and relative external parameters. In this setup correspondences in time and in space between the video sequences can be described/modeled by a small set of parameters  $\vec{P} = (\vec{P}_{spatial}, \vec{P}_{temporal})$ . Our goal is to recover these parameters. The specific models that we address and their parameters are discussed next.

Temporal misalignment results when the two input sequences have a time-shift (offset) between them (e.g., if the cameras were not activated simultaneously), and/or when they have different frame rates (e.g., PAL vs. NTSC). Such temporal misalignments can be modeled by a 1-D affine transformation in time  $t' = s \cdot t + \Delta t$ , and is typically at subframe time units. Note that in most cases s is known – it is the ratio between the frame rates of the two cameras (e.g., for PAL and NTSC)

sequences, it is s = 25/30 = 5/6). Therefore, in such cases  $\vec{P}_{temporal}$  contains only one unknown parameter,  $\Delta t$ .

To model the spatial parameters let us look at the spatial part of a space-time point. Let  $\vec{p}(t) = (x, y, 1)^T$  denote the homogeneous coordinates of only the *spatial* component of a space-time point  $\vec{\mathbf{x}} = (x, y, t)$  in S. The *spatial misalignment* between two sequences results from the fact that the two cameras have different external and internal calibration parameters. We will consider two possible cases: the 2D case and the the 3D case:

(i) By the 2D case we refer to the case where the distance between the camera projection centers is negligible relative to the distances of the cameras to the scene, or else if the scene is roughly planar. In this 2D case the space-time relation between the two sequences is expressed by an unknown  $3 \times 3$  homography H and the unknown  $\Delta t$ :

$$H\vec{p}(t) \cong \vec{p}'(s \cdot t + \Delta t).$$

In this case the nine spatial parameters  $\vec{P}_{spatial} = [h_{11} \ h_{12} \ h_{13} \ h_{21} \ h_{22} \ h_{23} \ h_{31} \ h_{32} \ h_{33}]$  are defined up to a scale factor  $(h_{ij}$  are the 9 entries of  $H)^1$ , and  $\vec{P}_{temporal} = \Delta t$ .

(ii) By the 3D case we refer to the case where the cameras are disjoint and the scene contains observable 3D variations. In this case the spacetime relation between the two sequences is expressed by an unknown fundamental matrix F and the unknown  $\Delta t$ :

$$\vec{p}'(s \cdot t + \Delta t)^T F \vec{p} = 0,$$

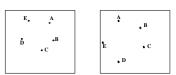
where  $[\cdot]^T$  denotes the transpose of a vector. In this case the spatial relation parameters are:  $\vec{P}_{spatial} = [f_{11} \ f_{12} \ f_{13} \ f_{21} \ f_{22} \ f_{23} \ f_{31} \ f_{32} \ f_{33}]$ , where  $f_{ij}$  are the 9 entries of the  $3 \times 3$  fundamental matrix F (up to a scale factor), and  $\vec{P}_{temporal} = \Delta t$ .

Note that in either case, F or H are shared by all temporally corresponding pairs of frames because the cameras are fixed relative to each other (both internal parameters and inter-camera external parameters are fixed).

#### 3. A Feature-Based Sequence Matching Algorithm

Typical feature-based *image* matching methods, e.g., (Faugeras et al., 2001; Hartley and Zisserman, 2000; Xu and Zhang, 1996), first apply

<sup>&</sup>lt;sup>1</sup> The modification to other 2D parametric models, such as translation, similarity or affine, is trivial (e.g., set  $h_{31}=h_{32}=0$  for a 2D affine model).







(a) Frame from  $S_1$  (b) Frame from  $S_2$ 

(c) Sequence  $S_1$  (d) Sequence  $S_2$ 

Figure 2. Point correspondences vs. trajectory correspondences. (a) and (b) display two frames out of two sequences recording five small moving objects (marked by A,B,C,D,E). (c) and (d) display the trajectories of these moving objects over time. When analyzing only single frames, it is difficult to determine the correct point correspondences across images. However, point trajectories have additional properties, which simplify the correspondence problem across two sequences (both in space and in time).

a local operator to detect interest points in a pair of images (e.g., the Harris corner detector (Harris and Stephens, 1988)). Once interest points are extracted in the two images, robust estimation methods, such as RANSAC (Fischler and Bolles, 1981), LMS (Hampel et al., 1986), etc., are used for finding corresponding points and recovering the spatial relation between the two images. In order to decrease the possible complexity of matching, a table of tentative matching is sometimes constructed. In general, this tentative matching table may be based on any property of a feature point, but usually it is based on brightness values of small neighborhoods of the feature points (e.g., in (Xu and Zhang, 1996) correlation was used).

Feature-based image matching can be generalized to feature-based sequence matching by extending the notion of features from feature points to feature trajectories. Let  $\gamma = \{\vec{x}_{t_0}, \vec{x}_{t_1}, \dots, \vec{x}_{t_n}\}$  be a space-time trajectory (remember that by  $\vec{x} = (x, y, t)$  we denote space-time points). Denote by  $\Gamma$  and  $\Gamma'$  the sets of all trajectories in sequences S and S' respectively, then spatio-temporal matching between the two sequences can be recovered by establishing correspondences between trajectories from the sets  $\Gamma$  and  $\Gamma'$ .

In particular, a single pair of (non-trivial) corresponding trajectories<sup>2</sup>  $\gamma$  and  $\gamma'$  can uniquely define: (i) the spatial relation, (ii) the temporal relation, (iii) can provide a convenient residual error measure:  $err(\vec{P}) = \sum_{\vec{x} \in \gamma} D(\vec{x}, \vec{x}') = \sum_{t \in [t_0, \dots, t_n]} d(\vec{p}(t), \vec{p}'(t'))$ , where  $[t_0, \dots, t_n]$  is

the temporal support of the space-time trajectory  $\gamma$ ,  $\vec{p}(t)$  is the spatial position (i.e., pixel coordinates) of the space-time point  $\vec{x}$  at time t (in

<sup>&</sup>lt;sup>2</sup> By a non-trivial trajectory we mean that it covers a large enough image region, and that its points do not all belong to a degenerate configuration (e.g, a straight line for a homography, or a plane for a fundamental matrix).

homogeneous coordinates), and  $\vec{p}'(t')$  is the spatial position of  $\vec{x}'$  in the other sequence at time  $t' = s \cdot t + \Delta t$ .

For the homography (2D) case the error measure is:  $d(\vec{p}, \vec{p}') = dist_H(H\vec{p}(t), \vec{p}'(s \cdot t + \Delta t))$ , where  $dist_H(q_1, q_2)$  is the distance between two points after normalizing each by its third coordinate. For the fundamental matrix (3D) case the error measure is:  $d(\vec{p}, \vec{p}') = dist_F(F\vec{p}(t), \vec{p}'(s \cdot t + \Delta t))$ , where  $dist_F(l, q)$  is the distance (in pixels) between a point q and a line l (an epipolar line).

We next outline the feature-based sequence-to-sequence alignment algorithm that we have used in our experiments (which is a RANSAC/MDS based algorithm). Each step of the algorithm is then explained in more detail below:

- (1) Construct feature trajectories (i.e., detect and track feature points for each sequence).
- (2) For each trajectory estimate its basic properties (e.g., dynamic vs. static, see more examples below).
- (3) Based on basic properties construct an initial table of tentative matching between trajectories.
- (4) Estimate candidate parameter vector  $\vec{P} = (P_{spatial}, P_{temporal})$  by repeatedly choosing (at random) a pair of possibly corresponding trajectories<sup>3</sup>. At each trial compute the set of parameters  $\vec{P}$  which minimizes the error function  $err(\vec{P})$  defined above.
- (5) Assign a score for each candidate set of parameters  $\vec{P}$  to be the number of corresponding pairs of trajectories whose residual error (or median residual error) is small.
- (6) Repeat steps (4) and (5) N times.
- (7) Choose  $\vec{P}$  which has the highest score.
- (8) Refine  $\vec{P}$  using all trajectory pairs that supported this candidate.

In our current implementation trajectories of moving objects were computed (Step 1) by tracking unique points on blobs of moving objects. This was done either by tracking the center of mass of moving objects, or the top point on the silhouettes of moving objects (the reliability of the center of mass to be used as a feature point is discussed in (Lee et al., 2000), and the reliability of extreme points on silhouettes is discussed in (Wong and Cipolla, 2001)). The KLT feature tracker (Lucas and Kanade, 1981; Tomasi and Kanade, 1991) may also be used to generate additional feature trajectories. In the presence of many trajectories, trajectory properties may be used to reduce the matching complexity (Step 2). For example, dynamic trajectories (of moving objects) in one sequence are matched only against dynamic trajectories in the other sequence. When the cameras are expected to have similar

<sup>&</sup>lt;sup>3</sup> If these are roughly along a straight line choose an additional pair.

photometric properties, the spatial properties of the features may also be used (e.g., the size or color distribution of the moving object). When we anticipate a significant change in appearance, shape properties of the *trajectories* could still be used (e.g., normalized length, average speed, curvature, 5-point projective invariance (Mundy and Zisserman, 1992)). Although some of these are not projective invariants, they are useful in an initial search for crude tentative matching (Step 3).

A matching of a *single* pair of trajectories across the two sequences induces *multiple* point correspondences across the camera views. These point correspondences are used for computing the spatial and temporal relation between the two sequences. To evaluate a candidate parameter vector  $\vec{P} = (h_{11}, \dots, h_{33}, \Delta t)$ , or  $\vec{P} = (f_{11}, \dots, f_{33}, \Delta t)$  (where  $h_{11}, \dots, h_{33}$  or  $f_{11}, \dots, f_{33}$  are the components of a homography H, or a fundamental matrix F, respectively), we minimize the following error function<sup>4</sup> (Step 4 and Step 8):

$$\vec{P} = \underset{\vec{P}}{\operatorname{argmin}} \sum_{\gamma \in \Gamma} \sum_{t \in support(\gamma)} d(\vec{p}(t), \vec{p}'(s \cdot t + \Delta t)) \tag{1}$$

where  $d(\cdot)$  is either  $dist_H(\cdot)$  or  $dist_F(\cdot)$ , depending on whether the scene is 2D or 3D. The minimization of Eq.(1) is performed by iterating the following two steps:

- (i) Fix  $\Delta t$  and approximate H (or F) using standard methods (e.g., (Hartley and Zisserman, 2000) Chapters 3 and 10, respectively).
- (ii) Fix H (or F) and refine  $\Delta t$ . Since  $t' = s \cdot t + \Delta t$  is not necessarily an integer value (allowing a sub-frame time shift), it is interpolated from the adjacent (integer time) point locations:  $t_1 = \lfloor t' \rfloor$  and  $t_2 = \lceil t' \rceil$ . We search for  $\alpha = t' t_1$  ( $1 \ge \alpha \ge 0$ ) that minimizes the following term:

$$\sum_{\gamma \in \Gamma} \sum_{t \in support(\gamma)} d(\vec{p}(t), \vec{p}'(t_1) \cdot (1 - \alpha) + \vec{p}'(t_2) \cdot \alpha)$$
 (2)

In our implementation we used a bounded number of refinement iterations (10 to 20), or stopped earlier if the residual error did not change. An initial (integer) approximation for  $\Delta t$  was derived using exhaustive search over a small fixed temporal interval (20-25 frames in our experiments).

Examples of applying the above algorithm to video sequences of different scenarios are found in Figs. 3,4,5,6, (see figure captions for further details).

<sup>&</sup>lt;sup>4</sup> In Step 4 the summation is only over the selected trajectory.

### 4. Benefits of Feature-Based Sequence Matching

When there are *no* dynamic changes in the scene, sequence-to-sequence matching provides no benefit over image-to-image matching. The increase in the data size (sequences vs. images) only increases the signal-to-noise ratio, but does not provide new information. On the contrary, some degenerate cases may result in space-time ambiguities, see (Caspi and Irani, 2000; Giese and Poggio, 2000; Stein, 1998). However, when the scene dynamics is rich enough, sequence matching is superior to image matching in multiple ways. Below we mention some of its benefits:

(i) **Resolving Spatial Ambiguities.** Inherent ambiguities in imageto-image matching occur, for example, when there is insufficient common appearance information across images. This can occur when there is not enough spatial information in the scene, such as in the case of the small ball against a uniform background in Fig. 1. Insufficient common appearance information across images can also occur when the two cameras record the scene at significantly different zooms (such as in Fig. 4.a. and 4.b), thus observing different features at different scales. It can also occur when the two cameras have different sensing modalities (such as the Infra-Red and visible-light cameras in Fig. 3.a and 3.b), thus sensing different features in the scene. In those cases the photometric properties of the two input sequences are very different. Yet, the trajectories of moving objects over time are independent of the sensor properties, thus form a powerful cue for matching across the two sequences. In other words, the need for consistent appearance information is replaced by consistent temporal behavior, as captured by trajectories of moving objects estimated within each sequence separately.

If the two cameras are known to observe similar features (e.g., when they have similar imaging properties and viewing direction), then a regular feature detector and tracker (e.g., KLT) may also be used (for static as well as for dynamic scene points). However, if the cameras have different sensing modalities or a wide base-line, we prefer to select "symbolic" features such as the center of gravity of the moving objects (e.g., the cars and the kite in Fig. 3) or the upper tip of the silhouettes of moving objects<sup>5</sup> (e.g., the moving people or the ball in Fig. 6) as the feature points.

(ii) Improved Accuracy for Unsynchronized Video. Even when there is sufficient spatial information within the images, and accurate frame correspondences is known between the two sequences, sequenceto-sequence matching may still provide higher accuracy in the estima-

 $<sup>^{5}</sup>$  Implicitly assuming that the cameras are horizontal, and the object tip is not occluded in one camera.

tion of the spatial transformation than image-to-image matching. This is true even when all the spatial constraints from all pairs of corresponding images across the two sequences are simultaneously used to solve for the spatial transformation. This is because image-to-image matching is restricted to matching of existing physical frames, whereas these may not have been recorded at exactly the same time due to sub-frame temporal misalignment between the two sequences. Sequence-to-sequence matching, on the other hand, is not restricted to physical ("integer") image frames. It can thus spatially match information across the two sequences at sub-frame temporal accuracy. This leads to higher sub-pixel accuracy in the spatial matching/alignment.

This phenomenon is mostly noticeable when the scene is highly dynamic. Fig. 7 shows such an example.

(iii) Reduced Combinatorial Complexity. When the search space for spatial correspondences is large (such as in wide base-line matching, under large image rotations, or under large zoom differences), sequence-to-sequence matching can be used to reduce the combinatorial complexity. First, correspondence of trajectories is less ambiguous than correspondence of feature points due to the added "shape" properties of feature trajectories. This is illustrated in Fig. 2 and discussed in Section 1. Second, in these cases the number of trials required by a RANSAC-like algorithm is significantly lower in sequence-to-sequence matching. We next analyze the difference between the number of trials in both cases (image-to-image vs. sequence-to-sequence matching).

Let m be the minimal number of correspondences required for computing a spatial transformation  $\vec{P}_{spatial}$  (e.g., m=4 for a homography; m=8 for a fundamental). Let  $\epsilon$  be the probability that a feature matching across the two images is correct (and therefore the probability of a mismatch or an outlier is  $(1-\epsilon)$ ). A RANSAC-like matching algorithm requires that at least one of the trials (i.e., one random sampling of m correspondences) will not contain any mismatches (outliers). Let N be the number of trials that are required to ensure with probability p (usually p=99%) that at least one random sample of m features is free from mismatches. Then N is given by the following formula (Rousseeuw, 1987; Hartley and Zisserman, 2000):

$$N \ge \frac{\log(1-p)}{\log(1-\epsilon^m)}. (3)$$

This formula emphasizes why in a standard image-to-image matching a limited search range for candidate feature correspondences is crucial: a bounded number of candidate correspondence points guarantees that  $\epsilon$  is large enough (e.g.,  $\epsilon > 0.5$ ), thus limiting the number of trials N to a reasonable number.

However, when there is a large base-line between the cameras, a large scale difference, or a large image rotation, then  $\epsilon \approx \frac{1}{\#features}$  (the probability to choose corresponding features at random).  $\epsilon$  may be even smaller if the two sets of features from the two images are inconsistent (i.e., different features are observed by the two cameras). In such cases the contribution of sequence-to-sequence matching is most prominent. Thus, for example, if we use image-to-image matching with 100 features (and without restricting the search range), then according to Eq. (3) the number of necessary trials for computing a homography  $(m=4,\epsilon=\frac{1}{100},p=99\%)$  is  $N>4.6\times10^8$  (which is obviously an unreasonable number of trials!). On the other hand, in the case of sequence-to-sequence matching, one pair of corresponding trajectories (m=1) provides the required number of point correspondences. Even if we do not exploit distinguishing shape properties of trajectories and assume that  $\epsilon=\frac{1}{\#trajectories}$ , we get a reasonable number of trials  $N\geq459$  (for  $m=1,\epsilon=\frac{1}{100},p=99\%$ ).

When dealing with unsynchronized video sequences we should also take into account the temporal ambiguity. Thus, for each pair of corresponding trajectories, we further have to verify T possible matches, where T is the range of possible temporal misalignments. Therefore, the number of trials for an unsynchronized pair of sequences is  $O(T \cdot N)$  (in our experiments we usually allow for T = 25 frames, i.e., we assume that the temporal offset between the two sequences is at most  $\Delta t = 1$  second).

When only trajectories of moving objects are used, the number of trajectories is usually very small, leading to an additional reduction in the complexity of trajectory matching. Furthermore, when moving objects appear at different times in the sequence, the complexity of trajectory matching is even further reduced. Note that a few such trajectory correspondences induce a high number of point correspondences, which enable robust recovery of spatial alignment/matching.

# 5. Applications and Results

The above mentioned benefits of sequence-to-sequence matching/alignment give rise to new video applications, that are very difficult or even impossible to obtain using existing image-to-image matching tools. Some of these are described in figures 3, 4, 5, 6 and briefly outlined below.

(i) Multi-sensor alignment. The same objects look different in visible and infra-red light, which often makes impossible to match them across the views relying on their appearance. For example, 200 features

were extracted in the multi-sensor image pair of Fig. 3.a and Fig. 3.b using Harris corner detector (Harris and Stephens, 1988), but only two out of the 200 turned out belonging to the same real world point. On the other hand, if we detect and track a moving object in both views, then its trajectory no longer depends on the sensing modality of the camera, and thus forms a powerful dynamic cue for alignment. An example of multi-sensor sequence-to-sequence alignment is presented in Fig. 3. (In this case a homography was computed).

- (ii) Matching across significant zoom differences. Fig. 4 shows an example of aligning sequences obtained at significantly different zooms. Due to the large scale difference (1:3) the search range for corresponding features is very large (the same features appear at distant locations in the images). Furthermore, the scene is captured at significantly different spatial resolutions, thus point neighborhoods look very different, making the matching of conventional (point) features problematic. The homography was accurately recovered using sequence-to-sequence alignment. See caption of Fig. 4 for more details.
- (iii) Wide base-line matching. Another difficult scenario for image matching is the wide base-line case. When cameras capture the scene from distant viewpoints, they see objects from different sides. We took extreme examples of two cameras, situated on the opposite sides of the scene (i.e., the cameras are facing each other; in fact each camera sees the other camera). The cameras observe the same objects, but can never see the same point.

Our algorithm succeeds to recover the fundamental matrix in this situation with reasonable accuracy, as shown in Figs. 5 and 6 (see figure captions for more information).

(iv) New video applications. Unsynchronized video sequences can be temporally matched (synchronized) at *sub-frame* accuracy. Such sub-frame synchronization gives rise to new video applications including super-resolution in time (Shechtman et al., 2002), where multiple video sequences with low temporal resolution (low frame-rate) are combined into a single high temporal resolution (high frame-rate) output sequences.

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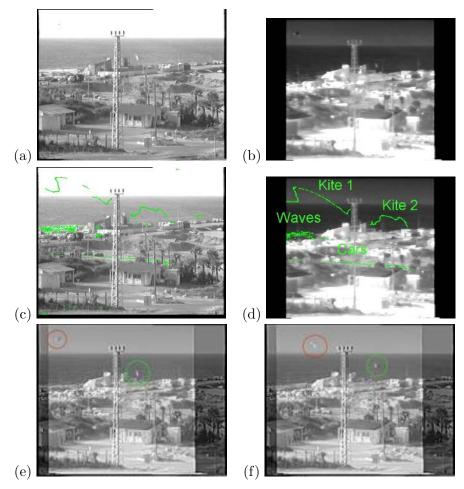


Figure 3. Multi-Sensor Alignment. (a) and (b) display representative frames from a PAL visible light sequence and an NTSC Infra-Red sequence, respectively. The scene contains several moving objects: 2 kites, 2 moving cars, and sea waves. The trajectories induced by tracking the moving objects are displayed in (c) and (d). The two camera centers were close to each other, therefore the spatial transformation was modeled by a homography. The output after spatio-temporal alignment via trajectories matching (Section 3) is displayed in (e) and (f). The recovered temporal misalignment was 1.31 sec. The results are displayed after fusing the two input sequences (using Burt's fusion algorithm (Burt and Kolczynski, 1993)). We can now observe spatial features from both sequences. In particular note the right kite which is more clearly visible in the visible-light sequence (circled in green), and the left kite which is more clearly visible in the IR sequence (circled in red).

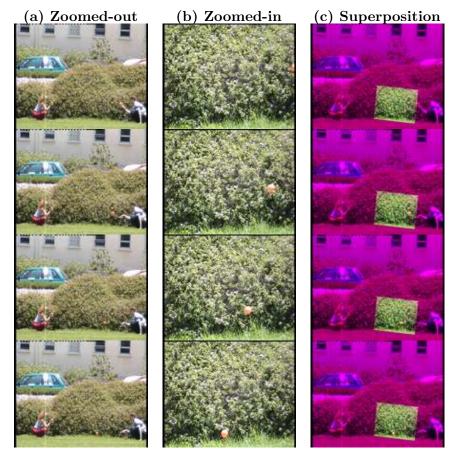


Figure 4. Alignment of sequences obtained at different zooms. Columns (a) and (b) display four representative frames from the reference sequence and second sequence, showing a ball thrown from side to side. The sequence in column (a) was captured by a wide field-of-view camera, while the sequence in column (b) was captured by a narrow field-of-view camera. The cameras where located next to each other (the spatial transformation was modeled by a homography) and the ratio in zooms was approximately 1: 3. The two sequences capture features at significantly different spatial resolutions, which makes the problem of inter-camera image-to-image alignment very difficult. The dynamic information (the trajectory of the ball's center of gravity), on the other hand, forms a powerful cue for alignment both in time and in space. Column (c) displays superposition of corresponding frames after spatio-temporal alignment, using the algorithm of Section 3 for estimating the homography and the temporal correspondence between the two sequences. The dark (pink) boundaries in (c) correspond to scene regions observed only by the reference (zoomed-out) camera.

# (a) First camera sequence:



# (b) Second camera sequence:







Figure 5. Wide Base-Line Matching Rows (a) and (b) display a few corresponding frames of one person (out of three that took part in the experiment) walking and sitting in a hall. The sequences were taken from two opposite sides of the hall. Each camera is visible by the other camera and is marked on the right-most frame by an arrow. Using background subtraction we extract moving objects (people), and select their head tips (the highest point on the silhouette) as feature points (this is illustrated for the second sequence in (b)). The recovered epipolar geometry is displayed in (c) and (d). Static points and their epipolar lines are displayed for verification only and were not used in the computation. Note that the recovered epipoles (the intersection of the epipolar lines) fall very close to their true locations (which is the position of the other camera, marked by a white cross). In this example only one person at a time enters the scene, thus the trajectory correspondence problem becomes simple. An initial temporal alignment with accuracy within one second (25 frames) was manually provided, and the final recovered temporal shift was -2.8 frames.

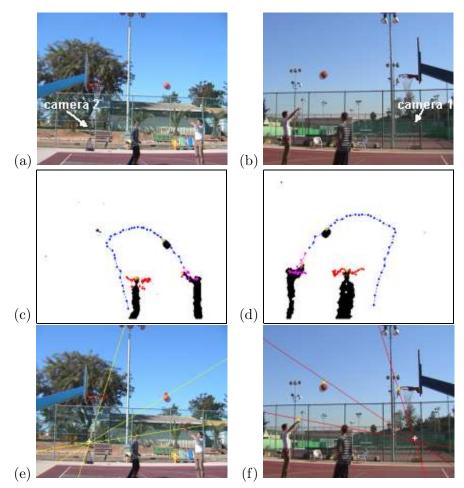


Figure 6. Wide Base-Line Matching (a) and (b) display two representative frames from two sequences of a basketball game taken from two opposite sides of the basket field (the cameras are facing each other). Each camera is visible by the other camera and is circled and marked by a white arrow. Space-time trajectories induced by moving objects (ball and players) are displayed in (c)-(d) in different colors for the different objects. The recovered epipolar geometry is displayed in (e) and (f). Points and their epipolar lines are displayed in each image for verification. Note, that the only static objects that are visible in both views are the basket ring and the board. Accuracy of the recovered spatial alignment can be appreciated by the closeness of each point to the epipolar line of its corresponding point, as well as by comparing the intersection of epipolar lines with the ground truth epipole marked by a cross (which is the other camera). In this example the relative blob size of the moving objects was used to provide initial correspondence between the trajectories across the two sequences. Two trajectories (instead of one) were used on each RANSAC iteration, as most trajectories are planar. An initial temporal alignment with accuracy within one second (25 frames) was manually provided, and the final recovered temporal shift was 3.7 frames.

(a) In sequence 1:



# (b) In sequence 2:

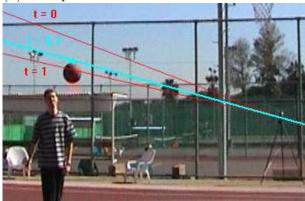


Figure 7. Subframe temporal synchronization (a) displays superposition of the moving ball position in two consecutive frames in sequence 1 (at t=0and t = 1). The ball is falling at a high speed, thus its displacement is quite noticeable. The feature point is the tip point of the ball in each frame (the highest point on the ball). The dashed blue circle displays the interpolated ball location at the correct time shift (i.e., the correct sub-frame time unit at which the corresponding frame was recorded in the other sequence – sequence 2). In this example it is 0.7 of a frame time, since the global temporal matching was 3.7 frames offset. (b) The red lines display the epipolar lines generated on the image plane of sequence 2 by the "physical" ball in sequence 1 (imaged at "integer" frames t = 0 and t = 1). The blue line displays the epipolar line corresponding to the interpolated location of the ball at t = 0.7. It can be clearly seen that the ball's feature point (its tip) in sequence 2 is on the epipolar line corresponding to the virtual point (its location at t = 0.7 in sequence 1). This example also shows that a large error can be introduced by matching only "integer" frames across two sequences (while ignoring the sub-frame temporal offset).