

Feature Unification in TAG Derivation Trees

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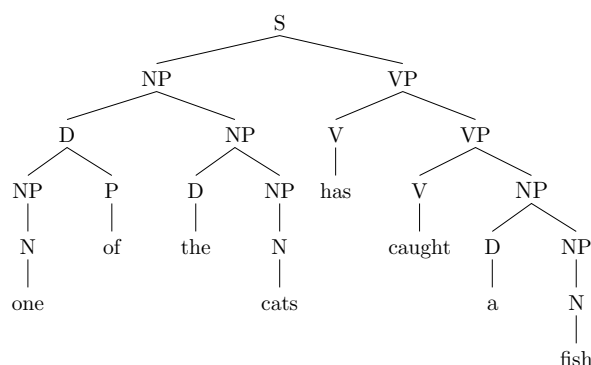
Abstract

The derivation trees of a tree adjoining grammar provide a first insight into the sentence semantics, and are thus prime targets for generation systems. We define a formalism, *feature-based regular tree grammars*, and a translation from feature based tree adjoining grammars into this new formalism. The translation preserves the derivation structures of the original grammar, and accounts for feature unification.

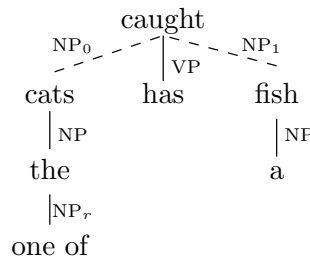
1 Introduction

Each sentence derivation in a tree adjoining grammar (Joshi and Schabes, 1997, TAG) results in two parse trees: a *derived tree* (Figure 1a), that represents the phrase structure of the sentence, and a *derivation tree* (Figure 1b), that records how the elementary trees of the grammar were combined. Each type of parse tree is better suited for a different set of language processing tasks: the derived tree is closely related to the lexical elements of the sentence, and the derivation tree offers a first insight into the sentence semantics (Candito and Kahane, 1998). Furthermore, the derivation tree language of a TAG, being a regular tree language, is much simpler to manipulate than the corresponding derived tree language.

Derivation trees are thus the cornerstone of several approaches to sentence generation (Koller and Striegnitz, 2002; Koller and Stone, 2007), that rely crucially on the ease of encoding regular tree grammars, as dependency grammars and planning problems respectively. Derivation trees also serve as intermediate representations from which both derived trees (and thus the linear order information) and semantics can be computed, e.g. with the abstract categorial grammars of de Groote (2002),



(a) Derived tree.



(b) Derivation tree.

Figure 1: Parse trees for “One of the cats has caught a fish.” using the grammar of Figure 2.

Pogodalla (2004), and Kanazawa (2007), or similarly with the bimorphisms of Shieber (2006).

Nevertheless, these results do not directly apply to many real-world grammars, which are expressed in a feature-based variant of TAGs (Vijay-Shanker, 1992). Each elementary tree node of these grammars carries two feature structures that constrain the allowed substitution or adjunction operations at this node (see for instance Figure 2). In theory, such structures are unproblematic, because the possible feature values are drawn from finite domains, and thus the number of grammar categories could be increased in order to account for all the possible structures. In practice, the sheer number of structures precludes such a naive im-

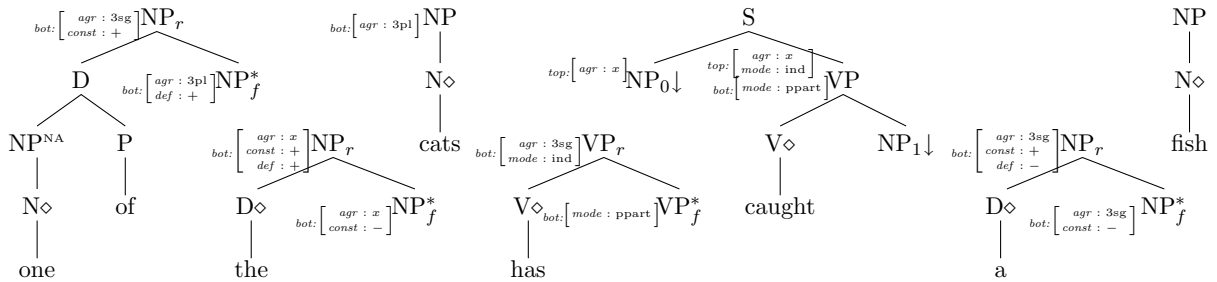


Figure 2: A feature-based tree adjoining grammar. For the sake of clarity, we identify elementary trees with their anchors in our examples.

plementation: for instance, the 50 features used in the XTAG English grammar (XTAG Research Group, 2001) together define a domain containing more than 10^{19} different structures. Furthermore, finiteness does not hold for some grammars, for instance with the semantic features of Gardent and Kallmeyer (2003).

Ignoring feature structures typically results in massive over-generation in derivation-centric systems. We define a formalism, *feature-based regular tree grammars*, that produces derivation trees that account for the feature structures found in a tree adjoining grammar. In more details,

- we recall how to generate the derivation trees of a tree adjoining grammar through a regular tree grammar (Section 2), then
- we define feature-based regular tree grammars and present the translation from feature-based TAG (Section 3); finally,
- we provide an improved translation inspired by left corner transformations (Section 4).

We assume the reader is familiar with the theory of tree-adjoining grammars (Joshi and Schabes, 1997), regular tree grammars (Comon et al., 2007), and feature unification (Robinson, 1965).

2 Regular Tree Grammars of Derivations

In this section, we define an encoding of the set of derivation trees of a tree adjoining grammar as the language of a regular tree grammar (RTG). Several encodings equivalent to regular tree grammars have been described in the literature; we follow here the one of de Groote (2002), but explicitly construct a regular tree grammar.

Formally, a tree adjoining grammar is a tuple $\langle \Sigma, N, I, A, S \rangle$ where Σ is a terminal alphabet, N

is a nonterminal alphabet, I is a set of initial trees α , A is a set of auxiliary trees β and S is a distinguished nonterminal from N . We note γ_r the root node of the elementary tree γ and β_f the foot node of the auxiliary tree β . Let us denote by $\gamma_1, \dots, \gamma_n$ the *active* nodes of an elementary tree γ , where a substitution or an adjunction can be performed;¹ we call n the *rank* of γ , denoted by $\text{rk}(\gamma)$. We set γ_1 to be the root node of γ , i.e. $\gamma_1 = \gamma_r$. Finally, $\text{lab}(\gamma_i)$ denotes the label of node γ_i .

Each elementary tree γ of the TAG will be converted into a single rule $X \rightarrow \gamma(Y_1, \dots, Y_n)$ of our RTG, such that $\text{rk}(\gamma) = n$ and each of the Y_i symbols represents the possible adjunctions or substitutions of node γ_i . We introduce accordingly two duplicates $N_A = \{X_A \mid X \in N\}$ and $N_S = \{X_S \mid X \in N\}$ of N , and a nonterminal labeling function defined for any active node γ_i with label $\text{lab}(\gamma_i) = X$ as

$$\text{nt}(\gamma_i) = \begin{cases} X_A & \text{if } \gamma_i \text{ is an adjunction site} \\ X_S & \text{if } \gamma_i \text{ is a substitution site} \end{cases} \quad (1)$$

The rule corresponding to the tree “one of” in Figure 2 is then $NP_A \rightarrow \text{one of}(NP_A, D_A, P_A, N_A)$, meaning that this tree adjoins into an NP labeled node, and expects adjunctions on its nodes NP_r , D , P , and N . Given our set of elementary TAG trees, only the first one of these four will be useful in a reduced RTG.

Definition 1. The *regular derivation tree grammar* $G = \langle S_S, \mathcal{N}, \mathcal{F}, R \rangle$ of a TAG $\langle \Sigma, N, I, A, S \rangle$ is a RTG with axiom S_S , nonterminal alphabet $\mathcal{N} = N_S \cup N_A$, terminal alphabet $\mathcal{F} = I \cup A \cup$

¹We consider in particular that no adjunction can occur at a foot node. We do not consider null adjunction constraints on root nodes and feature structures on null adjoining nodes, which would rather obscure the presentation, and we do not treat other adjunction constraints either.

$\{\varepsilon_A\}$ with ranks $\text{rk}(\gamma)$ for elementary trees γ in $I \cup A$ and rank 0 for ε_A , and with set of rules

$$\begin{aligned} R = & \{X_S \rightarrow \alpha(\text{nt}(\alpha_1), \dots, \text{nt}(\alpha_n)) \\ & \mid \alpha \in I, n = \text{rk}(\alpha), X = \text{lab}(\alpha_r)\} \\ \cup & \{X_A \rightarrow \beta(\text{nt}(\beta_1), \dots, \text{nt}(\beta_n)) \\ & \mid \beta \in A, n = \text{rk}(\beta), X = \text{lab}(\beta_r)\} \\ \cup & \{X_A \rightarrow \varepsilon_A \mid X_A \in N_A\} \end{aligned}$$

□

The ε -rules $X_A \rightarrow \varepsilon_A$ for each symbol X_A account for adjunction sites where no adjunction takes place. The RTG has the same size as the original TAG and the translation can be computed in linear time.

Example 2. The reduced regular tree grammar corresponding to the tree adjoining grammar of Figure 2 is then:

$$\begin{aligned} & \langle S_S, \{S_S, VP_S, VP_A, NP_S, NP_A\}, \\ & \{\text{one of, the, cats, has, caught, a, fish, } \varepsilon_A\}, \\ & \{ S_S \rightarrow \text{caught}(NP_S, VP_A, NP_S), \\ & \quad NP_S \rightarrow \text{cats}(NP_A), \\ & \quad NP_S \rightarrow \text{fish}(NP_A), \\ & \quad NP_A \rightarrow \text{the}(NP_A), \\ & \quad NP_A \rightarrow \text{a}(NP_A), \\ & \quad NP_A \rightarrow \text{one of}(NP_A), \\ & \quad NP_A \rightarrow \varepsilon_A, \\ & \quad VP_A \rightarrow \text{has}(VP_A), \\ & \quad VP_A \rightarrow \varepsilon_A \} \end{aligned}$$

□

Let us recall that the derivation relation induced by a regular tree grammar $G = \langle S_S, \mathcal{N}, \mathcal{F}, R \rangle$ relates terms² of $T(\mathcal{F}, \mathcal{N})$, so that $t \Rightarrow t'$ holds iff there exists a context³ C and a rule $A \rightarrow a(B_1, \dots, B_n)$ such that $t = C[A]$ and $t' = C[a(B_1, \dots, B_n)]$. The language of the RTG is $L(G) = \{t \in T(\mathcal{F}) \mid S_S \Rightarrow^* t\}$.

One can check that the grammar of Example 2 generates trees with a root labeled with “caught”, and three subtrees, the leftmost and rightmost of which labeled with “cats” or “fish” followed by an arbitrary long combination of nodes labeled with “one of”, “a” or “the”. The central subtree is an

²The set of *terms* over the alphabet \mathcal{F} and the set of variables \mathcal{X} is denoted by $T(\mathcal{F}, \mathcal{X})$; $T(\mathcal{F}, \emptyset) = T(\mathcal{F})$ is the set of trees over \mathcal{F} .

³A *context* C is a term of $T(\mathcal{F}, \mathcal{X} \cup \{x\})$, $x \notin \mathcal{X}$, which contains a single occurrence of x . The term $C[t]$ for some term t of $T(\mathcal{F}, \mathcal{X})$ is obtained by replacing this occurrence by t .

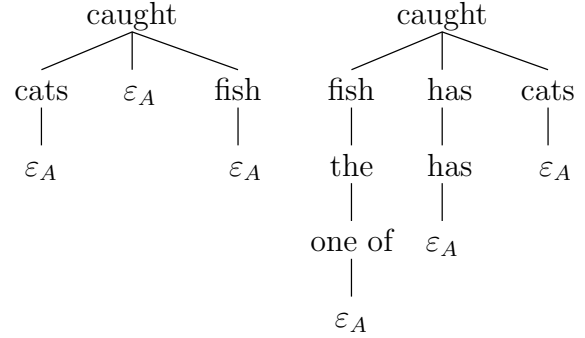


Figure 3: Some trees generated by the regular tree grammar of Example 2.

arbitrary long combination of nodes labeled with “has”. Each branch terminates with ε_A . Two of these trees can be seen on Figure 3. Our RTG generates the derivation trees of a version of the original TAG expunged from its feature structures.

3 Unification on TAG Derivation Trees

3.1 Feature-based Regular Tree Grammars

In order to extend the previous construction to feature-based TAGs, our RTGs use combinations of rewrites and unifications—also dubbed *narrowings* (Hanus, 1994)—of terms with variables in $\mathcal{N} \times \mathcal{D}$, where \mathcal{N} denotes the nonterminal alphabet and \mathcal{D} the set of feature structures.⁴

Definition 3. A *feature-based regular tree grammar* $\langle S, \mathcal{N}, \mathcal{F}, \mathcal{D}, R \rangle$ comprises an axiom S , a set \mathcal{N} of nonterminal symbols that includes S , a ranked terminal alphabet \mathcal{F} , a set \mathcal{D} of feature structures, and a set R of rules of form $(A, d) \rightarrow a((B_1, d'_1), \dots, (B_n, d'_n))$, where A, B_1, \dots, B_n are nonterminals, d, d'_1, \dots, d'_n are feature structures, and a is a terminal with rank n .

The *derivation* relation \Rightarrow for a feature-based RTG $G = \langle S, \mathcal{N}, \mathcal{F}, \mathcal{D}, R \rangle$ relates pairs of terms from $T(\mathcal{F}, \mathcal{N} \times \mathcal{D})$ and u -substitutions, such that $(s, e) \Rightarrow (t, e')$ iff there exist a context C , a rule $(A, d) \rightarrow a((B_1, d'_1), \dots, (B_n, d'_n))$ in R with fresh variables in the feature structures, a structure

⁴In order to differentiate TAG tree substitutions from term substitutions, we call the latter *u-substitutions*. Given two feature structures d and d' in \mathcal{D} , we denote by the u -substitution $\sigma = \text{mgu}(d, d')$ their *most general unifier* if it exists. We denote by \top the most general element of \mathcal{D} , and by *id* the identity.

d' , and an u-substitution σ verifying

$$s = C[(A, d')], \sigma = \text{mgu}(d, e(d')), e' = \sigma \circ e \\ \text{and } t = C[a((B_1, \sigma(d'_1)), \dots, (B_n, \sigma(d'_n)))].$$

The language of G is

$$L(G) = \{t \in T(\mathcal{F}) \mid \exists e, ((S, \top), id) \Rightarrow^* (t, e)\}.$$

□

Features percolate hierarchically through the computation of the most general unifier mgu at each derivation step, while the global u-substitution e acts as an environment that communicates unification results between the branches of our terms.

Feature-based RTGs with a finite domain \mathcal{D} are equivalent to regular tree grammars. Unrestricted feature-based RTGs can encode Turing machines just like unification grammars (Johnson, 1988), and thus we can reduce the halting problem on the empty input for Turing machines to the emptiness problem for feature-based RTGs, which is thereby undecidable.

3.2 Encoding Feature-based TAGs

For each tree γ with rank n , we now create a rule $P \rightarrow \gamma(P_1, \dots, P_n)$. A right-hand side pair $P_i = (\text{nt}(\gamma_i), d'_i)$ stands for an active node γ_i with feature structure $d'_i = \text{feats}(\gamma_i) = \begin{bmatrix} \text{top} : \text{top}(\gamma_i) \\ \text{bot} : \text{bot}(\gamma_i) \end{bmatrix}$, where $\text{top}(\gamma_i)$ and $\text{bot}(\gamma_i)$ denote respectively the top and bottom feature structures of γ_i .

The left-hand side pair $P = (A, d)$ carries the interface $d = \text{in}(\gamma)$ of γ with the rest of the grammar, such that d percolates the root top feature, and the foot bot feature for auxiliary trees. Formally, for each initial tree α in I and auxiliary tree β in A , using a fresh variable t , we define

$$\text{in}(\alpha) = \begin{bmatrix} \text{top} : t \\ \text{top} : \text{top}(\alpha_r) \end{bmatrix} \quad (2)$$

$$\text{in}(\beta) = \begin{bmatrix} \text{top} : t \\ \text{top} : \text{top}(\beta_r) \\ \text{bot} : \text{bot}(\beta_f) \end{bmatrix} \quad (3)$$

The interface thus uses the top features of the root node of an elementary tree, and we have to implement the fact that this top structure is the same as the top structure of the variable that embodies the root node in the rule right-hand side. With the same variable t , we define accordingly:

$$\text{feat}(\gamma_i) = \begin{cases} \begin{bmatrix} \text{top} : t \\ \text{bot} : \text{bot}(\gamma_r) \end{bmatrix} & \text{if } \gamma_i = \gamma_r \\ \begin{bmatrix} \text{top} : \text{top}(\gamma_i) \\ \text{bot} : \text{bot}(\gamma_i) \end{bmatrix} & \text{otherwise} \end{cases} \quad (4)$$

Finally, we add ε -rules $(X_A, \begin{bmatrix} \text{top} : v \\ \text{bot} : v \end{bmatrix}) \rightarrow \varepsilon_A$ for each symbol X_A in order to account for adjunction sites where no adjunction takes place. Let us denote by $\text{tr}(\gamma_i)$ the pair $(\text{nt}(\gamma_i), \text{feats}(\gamma_i))$.

Definition 4. The feature-based RTG $G = \langle S_S, N_S \cup N_A, \mathcal{F}, \mathcal{D}, R \rangle$ of a TAG $\langle \Sigma, N, I, A, S \rangle$ with feature structures in \mathcal{D} has terminal alphabet $\mathcal{F} = I \cup A \cup \{\varepsilon_A\}$ with respective ranks $\text{rk}(\alpha)$, $\text{rk}(\beta)$, and 0, and set of rules

$$R = \{ (X_S, \text{in}(\alpha)) \rightarrow \alpha(\text{tr}(\alpha_1), \dots, \text{tr}(\alpha_n)) \\ \mid \alpha \in I, n = \text{rk}(\alpha), X = \text{lab}(\alpha_r) \} \\ \cup \{ (X_A, \text{in}(\beta)) \rightarrow \beta(\text{tr}(\beta_1), \dots, \text{tr}(\beta_n)) \\ \mid \beta \in A, n = \text{rk}(\beta), X = \text{lab}(\beta_r) \} \\ \cup \{ X_A \begin{bmatrix} \text{top} : t \\ \text{bot} : t \end{bmatrix} \rightarrow \varepsilon_A \mid X_A \in N_A \}$$

□

Example 5. With the grammar of Figure 2, we obtain the following ruleset:

$$S_S \top \rightarrow \text{caught} \\ (NP_S \begin{bmatrix} \text{top} : [\text{agr} : x] \end{bmatrix}, VP_A \begin{bmatrix} \text{top} : \begin{bmatrix} \text{agr} : x \\ \text{mode} : \text{ind} \end{bmatrix} \\ \text{bot} : \begin{bmatrix} \text{mode} : \text{ppart} \end{bmatrix} \end{bmatrix}, NP_S \top) \\ NP_S \begin{bmatrix} \text{top} : t \end{bmatrix} \rightarrow \text{cats} (NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : [\text{agr} : 3\text{pl}] \end{bmatrix}) \\ NP_S \begin{bmatrix} \text{top} : t \end{bmatrix} \rightarrow \text{fish} (NP_A \begin{bmatrix} \text{top} : t \end{bmatrix}) \\ NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : x \\ \text{const} : - \end{bmatrix} \end{bmatrix} \rightarrow \text{the} (NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : x \\ \text{const} : + \\ \text{def} : + \end{bmatrix} \end{bmatrix}) \\ NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : 3\text{sg} \\ \text{const} : - \end{bmatrix} \end{bmatrix} \rightarrow \text{a} (NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : 3\text{sg} \\ \text{const} : + \\ \text{def} : - \end{bmatrix} \end{bmatrix}) \\ NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : 3\text{pl} \\ \text{def} : + \end{bmatrix} \end{bmatrix} \rightarrow \text{one of} (NP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : 3\text{sg} \\ \text{const} : + \end{bmatrix} \end{bmatrix}) \\ NP_A \begin{bmatrix} \text{top} : v \\ \text{bot} : v \end{bmatrix} \rightarrow \varepsilon_A \\ VP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{mode} : \text{ppart} \end{bmatrix} \end{bmatrix} \rightarrow \text{has} (VP_A \begin{bmatrix} \text{top} : t \\ \text{bot} : \begin{bmatrix} \text{agr} : 3\text{sg} \\ \text{mode} : \text{ind} \end{bmatrix} \end{bmatrix}) \\ VP_A \begin{bmatrix} \text{top} : v \\ \text{bot} : v \end{bmatrix} \rightarrow \varepsilon_A$$

□

With the grammar of Example 5, one can generate the derivation tree for “One of the cats has caught a fish.” This derivation is presented in Figure 4. Each node of the tree consists of a label and of a pair (t, e) where t is a term from $T(\mathcal{F}, \mathcal{N} \times \mathcal{D})$ and e is an environment.⁵ In order to obtain fresh variables, we rename variables from the RTG: we reuse the name of the variable in the grammar, prefixed by the Gorn address of the node where the rewrite step takes place. Labels indicate the chronological order of the narrowings in the derivation.

Labels in Figure 4 suggest that this derivation has been computed with a left to right strategy. Of course, other strategies would have led to the same

⁵Actually, we only write the change in the environment at each point of the derivation.

$$\begin{aligned}
NP_S [top : t] &\rightarrow \varepsilon_S (NP [top : t, bot : t]) \\
NP [bot : [agr : 3pl]] &\rightarrow \text{cats} \\
NP \top &\rightarrow \text{fish} \\
NP \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : x \\ const : + \\ def : + \end{array} \right] \end{array} \right] &\rightarrow \text{the} \left(NP \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : x \\ const : - \end{array} \right] \end{array} \right] \right) \\
NP \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : 3sg \\ const : + \\ def : - \end{array} \right] \end{array} \right] &\rightarrow \text{a} \left(NP \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : 3sg \\ const : - \end{array} \right] \end{array} \right] \right) \\
NP \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : 3sg \\ const : + \end{array} \right] \end{array} \right] &\rightarrow \text{one of} \left(NP \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : 3pl \\ def : + \end{array} \right] \end{array} \right] \right) \\
VP_A [top : t, mode : ppart] &\rightarrow \text{has} \left(VP_A \left[\begin{array}{l} top : t \\ bot : \left[\begin{array}{l} agr : 3sg \\ mode : ind \end{array} \right] \end{array} \right] \right) \\
VP_A [top : v, bot : v] &\rightarrow \varepsilon_A
\end{aligned}$$

□

Since we reversed the recursion of root adjunctions, the feature structures on the left-hand side and on the root node of the right-hand side of auxiliary rules are swapped in their transformed counterparts (e.g. in the rule for “one of”).

This version of a RTG for our example grammar is arguably much easier to read than the one described in Example 5: a derivation has to go through “one of” and “the” before adding “cats” as subject of “caught”.

The formal translation of a TAG into a transformed feature-based RTG requires the following variant tr_{lc} of the tr function: for any auxiliary tree β in A and any node γ_i of an elementary tree γ in $I \cup A$, and with t a fresh variable of \mathcal{D} :

$$\text{in}_{lc}(\beta) = \left[\begin{array}{l} top : t \\ bot : \text{bot}(\beta_f) \end{array} \right] \quad (5)$$

$$\text{feats}_{lc}(\gamma_i) = \begin{cases} \left[\begin{array}{l} top : t \\ top : \text{top}(\gamma_r) \\ bot : \text{bot}(\gamma_r) \end{array} \right] & \text{if } \gamma_i = \gamma_r \\ \text{feats}(\gamma_i) & \text{otherwise} \end{cases} \quad (6)$$

$$\text{tr}_{lc}(\gamma_i) = (\text{nt}(\gamma_i), \text{feats}_{lc}(\gamma_i)) \quad (7)$$

Definition 9. The *left-corner transformed* feature-based RTG $G_{lc} = \langle S_S, N \cup N_S \cup N_A, \mathcal{F}_{lc}, \mathcal{D}, R_{lc} \rangle$ of a TAG $\langle \Sigma, N, I, A, S \rangle$ with feature structures in \mathcal{D} has terminal alphabet $\mathcal{F}_{lc} = I \cup A \cup \{\varepsilon_A, \varepsilon_S\}$ with respective ranks $\text{rk}(\alpha) - 1$, $\text{rk}(\beta)$, 0, and 1, and set of rules

$$\begin{aligned}
R_{lc} = \{ & X_S [top : t] \rightarrow \varepsilon_S (X [top : t, bot : t]) \mid X_S \in N_S \} \\
& \cup \{ (X, \text{feats}(\alpha_1)) \rightarrow
\end{aligned}$$

$$\begin{aligned}
& \alpha(\text{tr}_{lc}(\alpha_2), \dots, \text{tr}_{lc}(\alpha_n)) \\
& \mid \alpha \in I, n = \text{rk}(\alpha), X = \text{lab}(\alpha_r) \}
\end{aligned}$$

$$\begin{aligned}
& \cup \{ (X, \text{feats}_{lc}(\beta_1)) \rightarrow \\
& \beta((X, \text{in}_{lc}(\beta)), \text{tr}_{lc}(\beta_2), \dots, \text{tr}_{lc}(\beta_n)) \\
& \mid \beta \in A, n = \text{rk}(\beta), X = \text{lab}(\beta_r) \}
\end{aligned}$$

$$\begin{aligned}
& \cup \{ (X_A, \text{in}(\beta)) \rightarrow \\
& \beta(\text{tr}(\beta_1), \text{tr}_{lc}(\beta_2), \dots, \text{tr}_{lc}(\beta_n)) \\
& \mid \beta \in A, n = \text{rk}(\beta), X = \text{lab}(\beta_r) \} \\
& \cup \{ X_A [top : t, bot : t] \rightarrow \varepsilon_A \mid X_A \in N_A \}
\end{aligned}$$

□

Again, the translation can be computed in linear time, and results in a grammar with at worst twice the size of the original TAG.

5 Conclusion

We have introduced in this paper feature-based regular tree grammars as an adequate representation for the derivation language of large coverage TAG grammars. Unlike the restricted unification computations on the derivation tree considered before by Kallmeyer and Romero (2004), feature-based RTGs accurately translate the full range of unification mechanisms employed in TAGs. Moreover, left-corner transformed grammars make derivations more predictable, thus avoiding some backtracking in top-down generation.

Among the potential applications of our results, let us further mention more accurate reachability computations between elementary trees, needed for instance in order to check whether a TAG complies with the tree insertion grammar (Schabes and Waters, 1995, TIG) or regular form (Rogers, 1994, RFTAG) conditions. In fact, among the formal checks one might wish to perform on grammars, many rely on the availability of reachability relations.

Let us finally note that we could consider the string language of a TAG encoded as a feature-based RTG—in a parser for instance—, if we extended the model with topological information, in the line of Kuhlmann (2007).

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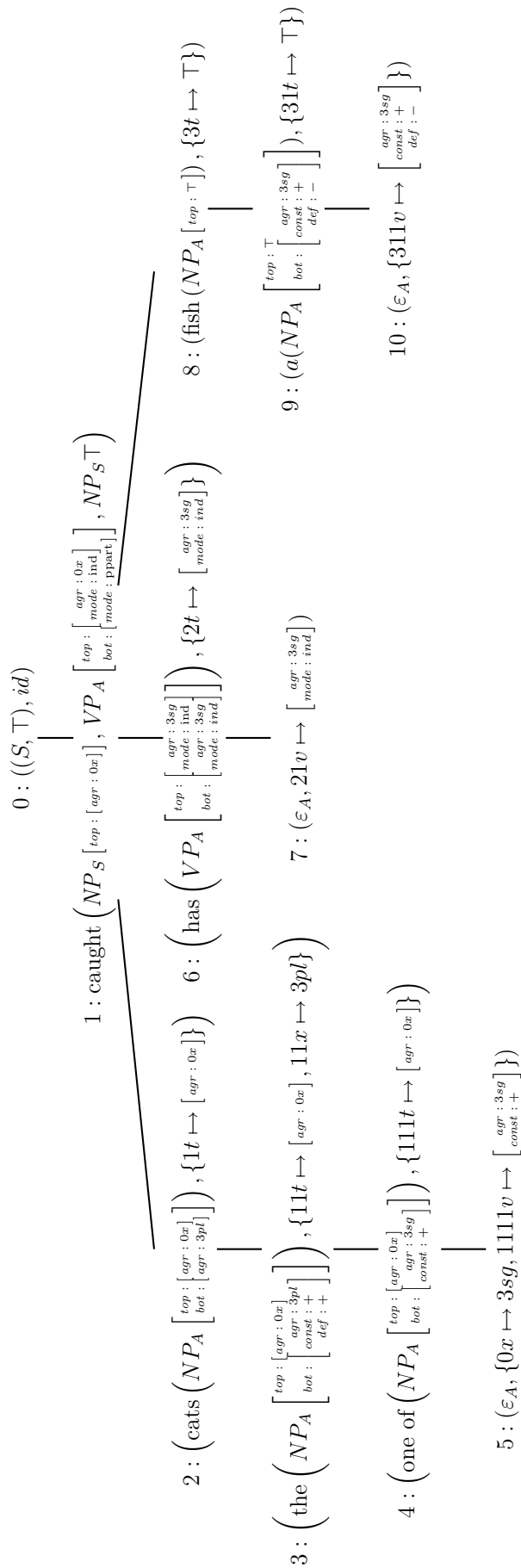


Figure 4: A rewrite sequence in the feature-based RTG for the sentence “One of the cats has caught a fish.”