Research Article

Feedback Channel Suppression in Distributed Video Coding with Adaptive Rate Allocation and Quantization for Multiuser Applications

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We present a novel rate allocation technique for distributed multiuser video coding systems without the need for a permanent feedback channel. Based on analytical calculations, the system unequally distributes the available bandwidth among the different users, taking into account the actual amount of movement in the transmitted video as well as the transmission conditions of each user. On one hand, the quantization parameters are dynamically tuned in order to optimize the decoding quality. On the other hand, a frame dropping mechanism allows the system to avoid unnecessary channel use, when the analytical estimations show that the successful decoding of a given frame is not possible because of very high motion or bad channel conditions. A significant gain in the system performance is noticed compared with the case of equal allocation of channel resources and constant quantization parameters.

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1. INTRODUCTION

During the last decade, distributed source coding has made a tremendous progress, especially in the world of video communications [1–13]. In traditional video coding techniques such as MPEG or H.26x [14], motion estimation is performed at the encoder side in order to transmit motion information to the decoder, which yields very complex interframe encoders. At the decoder side, motion compensation is performed based on the received information, thus resulting in simple decoders. This configuration (i.e., complex encoders and simple decoders) is suitable for applications where a video scene is encoded once in a base station with sufficient resources, and decoded several times. Video broadcasting and video streaming on demand are the most common examples for this configuration; video sequences are compressed and stored on a server, and then streamed to multiple users, upon request for video on demand. A lowcomplexity decoder is desired in such applications in order to permit low-cost receivers for the end-users.

However, in other situations, a simple encoder is desired. Distributed video coding (DVC) was introduced [7, 8] to permit low-complexity encoding for small power-limited and memory-limited devices, such as camera-equipped mobile phones or wireless video sensors (see Figure 1), by moving the computation burden from the encoder side to decoder's. In such scenarios, the decoder is assumed to be located in a base station with sufficient resources.

It is known from information theory that, given two statistically dependent sources X and Y, each source can be independently compressed to its entropy limit H(X) and H(Y), respectively. However, by exploiting the correlation between the two sources, X and Y can be jointly compressed to the joint entropy H(X, Y). This results in a reduced total transmission rate since $H(X, Y) \leq H(X) + H(Y)$. The idea behind DVC goes back to the 1970's when Slepian and Wolf proved in [15] that, if Y is compressed to its entropy limit H(Y), X can be transmitted at a rate very close to the conditional entropy H(X | Y), provided that Y is perfectly recovered at the receiver as side information. Since H(X, Y) = H(Y) + H(X | Y), X and Y can be independently encoded and jointly decoded without any loss in the compression efficiency, compared to the case where both sources are jointly encoded and decoded. The application of this concept to lossy source coding is known as the Wyner-Ziv coding [16].

In practical DVC systems [6–9], a subset of frames, known as key frames, is usually compressed using traditional intracoding techniques. One or more frames following each key frame, known as Wyner-Ziv (WZ) frames, are then compressed by appropriate puncturing of the parity bits at the output of a channel coder. At the receiver side, key frames are interpolated to generate the necessary side information for the decoding process.

One of the first practical DVC systems proposed by Puri and Ramchandran [7] used syndrome encoding. In [8], Aaron et al. used turbo codes [17-19] for the compression of WZ frames. Later on, Ascenso et al. [10] proposed a refined motion compensation technique to generate more efficient side information for the system in [8]. One of the main drawbacks in all these systems is the use of a feedback channel (FC) [11] to allow flexible rate control and to ensure successful decoding of WZ frames. The FC is not suitable for real-time systems due to transmission delay constraints. Additionally, in multiuser applications with rate constraints, the application of WZ coding becomes impractical because of the difficulty of implementing appropriate rate allocation algorithms. Furthermore, since several decoding runs are required to successfully recover a WZ frame, the FC imposes instantaneous decoding in the receiver. For all these reasons, the introduction of new techniques for estimating the necessary bitrate to successfully decode each WZ frame becomes crucial. In fact, the problem of the return channel in DVC has rarely been targeted in the literature. A simple technique that allows the removal of the FC was proposed by Artigas and Torres in [12]. The necessary compression rate of a given frame was estimated based on empirical results. This estimation requires building performance tables for the channel code in use, for all possible compression rates and correlation levels between the side information and the WZ frames in a given sequence. Such tables can be built by running offline simulations. However, the influence of the transmission impairments on the decoding performance is not considered. In this case, performance tables should be built not only for all possible correlation levels and compression rates, but also for all possible channel states. This results in a significantly large (theoretically infinite) number of tables that cannot be stored in memory-limited devices. Thus, the proposed technique cannot be used in practical real-time applications with video sequences containing different levels of motion or transmitted over time-varying wireless channels. Morbee et al. [13] proposed another technique for the removal of the feedback channel in DVC. First, the correlation between a WZ frame and the corresponding side information is modeled by a binary symmetric channel (BSC) with a different transition probability for each bitplane. Then, the performances of the channel code in use are estimated offline as a function of the transition probabilities using random

binary sequences. The compression rate for a given frame is then determined based on the two previous estimations. This technique presents several disadvantages as well. First, it does not take into consideration the rate constraints in limited bandwidth applications. Besides, when the WZ frame is decoded with a high error rate, the decoded data is discarded in the receiver and replaced by the available side information, yielding wasted channel use. Furthermore, the influence of the channel impairments on the proposed rate allocation technique is not considered. Moreover, both techniques are designed for a single-user scenario; their implementation in a multiuser application would cause unoptimal distribution of the channel resources between the different users since each user tends to occupy the necessary bandwidth for its own transmission regardless of the total available bandwidth and of the needs of the other transmitting users.

In this paper, we present a novel technique for the removal of the feedback channel in DVC systems, using an analytical approach based on entropy calculations. Designed for a multiuser scenario, the proposed technique takes into account the amount of motion in the captured video scene as well as the transmission channel conditions for every user, in order to allocate unequal transmission rates among the different users. On the other hand, the total transmission rate for all users does not exceed a fixed, maximum allowable rate imposed by the limited available bandwidth in such systems. Furthermore, the quantization parameter (i.e., the number of quantization levels) is dynamically varied for each frame, at every user, in such a way to optimize the decoded video quality. A frame dropping mechanism is also used in order to avoid unnecessary channel use, when the analytical estimations show that successful decoding of a given WZ frame will not be possible in the receiver because of very high-motion and/or bad channel conditions.

This paper is organized as follows. In Section 2, we present a detailed description of the DVC codec. The theoretical compression bound for the distributed video coding system is then determined in Section 3. Modified turbo decoding metrics are derived in Section 4 and the proposed rate allocation technique is then presented in Section 5. Finally, simulation results are reported in Section 6.

2. DESCRIPTION OF THE MULTIUSER VIDEO CODING SYSTEM

Consider a network of *N* video users as shown in Figure 1. In practical applications, these users can be camera-equipped mobile phones, each capturing a different scene, or wireless surveillance cameras capturing the same scene from different viewpoints. Each user transmits the video data to a central base station through a different wireless channel. The base station performs rate control based on each user's transmission conditions and on the amount of movement in each video scene, as will be detailed later.

Figure 2 shows the block diagram of the distributed video coding system considered in this study. At each user, odd frames are compressed using traditional intracoding techniques, and are assumed to be perfectly recovered at the receiver. The side information of a particular even frame is



FIGURE 1: Network of wireless video sensors.

generated by motion-compensated interpolation of the two adjacent odd frames, with symmetric motion vectors [8]. As for the compression of the even frames, it starts by a uniform scalar quantization to obtain an *M*-bit representation of the eight-bit pixels, where $M \in \{1, 2, 4\}$. Quantized pixels are then serially concatenated and fed to the source-channel turbo encoder shown in Figure 3; it consists of a parallel concatenation of two 16-state quadri-binary convolutional encoders separated by an internal interleaver and resulting in a minimum global coding rate of 2/3. The generator polynomials in octal notation are (23, 35, 31, 37, 27)₈ from [20]. At the encoder output, systematic information is discarded, while parity information is punctured and transmitted to the decoder.

The amount of puncturing is determined by the desired compression rate for each frame. In case of error-free transmission, turbo coding and puncturing are performed only to achieve source compression. However, for a transmission through a noisy channel, error-protection is also desired, yielding joint source-channel coding. In this study, we model the transmission channel between each user and the base station by a binary symmetric channel (BSC) with a transition probability q. In fact, a different channel model (e.g., additive white Gaussian noise or Rayleigh fading) can also be used in our system by a mapping to a BSC [5, 6] using an equivalence of the stability functions as detailed in [21].

As stated earlier, quantized pixels of the even (WZ) frames are serially concatenated and fed to the turbo encoder. In other words, in our system, no bitplane extraction [8–13] is performed. Aaron et al. mentioned in [9] that both techniques (serial concatenation and bitplane extraction) yield similar results. However, we have noticed that bitplane coding presents a major disadvantage in case the FC is suppressed; since the necessary compression rate to successfully decode a given bitplane cannot be determined without a return channel, the compression of a certain bitplane cannot begin until the parity bits corresponding to the previous bitplane have all been transmitted. In fact, this procedure guarantees the least compression on the most significant bits (MSBs) in the quantized pixels, and the strongest

compression on the least significant bits (LSBs). However, in the absence of a return channel, a very strong compression on a bitplane can lead to a high decoding bit error rate (BER) and, consequently, a bad reconstructed output. If the compression was slightly stronger on the MSBs and softer on the LSBs, while keeping the same average compression rate per pixel, the system error correction capability would often yield a better result. This can be performed by directly feeding the quantized pixels to the turbo encoder instead of extracting bitplanes. Additionally, the use of a quadri-binary turbo codec, by a serial concatenation of the quantized pixels at the encoder input, allows for nonbinary turbo coding, which yields improved decoding performances compared to binary coding [4].

In the joint source-channel decoder, the conditional probabilities in the turbo decoding process must depend on the residual signal statistics between the even frames and the side information on one hand, and on the channel conditions on the other. In the sequel, we will derive the proper metric calculations for the turbo decoding process.

Finally, the reconstruction block is used to recover an eight-bit version of the even frames using the available side information [8].

3. THEORETICAL COMPRESSION BOUND OF THE JOINT SOURCE-CHANNEL DISTRIBUTED VIDEO CODEC

In case of error-free transmission, the Slepian-Wolf theorem states that a WZ frame can be compressed to a rate close to the conditional entropy H(X | Y) defined as

$$H(X \mid Y) = -\sum_{a=0}^{2^{M}-1} \sum_{b=0}^{2^{M}-1} P(Y = b) \times P(X = a \mid Y = b) \log_2(P(X = a \mid Y = b)),$$
(1)

where *M* is the number of quantization bits per pixel, *X* represents the quantized WZ frame, and *Y* represents the interpolated side information. The statistics of the residual error between the side information and the WZ frame are modeled by a Laplacian distribution [8] with parameter α :

$$P(X - Y = \Delta) = c\left(\frac{\alpha}{2}\right)e^{-\alpha|d_{\Delta}|},$$
(2)

where $d_{\Delta} = 2^{(8-M)}\Delta$ and *c* is a normalization factor such that $\sum_{\Delta} P(X - Y = \Delta) = 1$. Obviously, P(X - Y) = P(Y - X).

The parameter α can be approximately estimated on the receiver side using the available odd frames. It can also be estimated by the encoder and transmitted as side information to the receiver. In the latter case, no motion estimation is required at the encoder side; an average interpolation can be performed on the odd frames to approximate the side information generated at the receiver, and the variance σ^2 of the residual error between the current WZ frame and the estimated side information is then determined. It can be easily shown that $\alpha = 2/\sigma^2$.



FIGURE 2: Block diagram of the pixel-domain distributed video coding system.



FIGURE 3: Quadri-binary turbo encoder.

On the other hand,

$$P(X - Y = \Delta) = \sum_{b} P(X = a = \Delta + b \mid Y = b)P(Y = b).$$
(3)

The number of nonzero terms in (3) is equal to the number $L_{d_{a-b}}$ of couples (a, b) that yield the residual difference $\Delta = a - b$. Supposing an equiprobable source, these couples can be considered to be equally likely; for example, considering a two-bit quantization, the possible values of Δ are 0, ±1, ±2, and ±3 (i.e., $d_{\Delta} = 0, \pm 64, \pm 128, \text{ and } \pm 192$), with a decreasing order of probability of occurrence. For a particular value of the difference Δ , couples (a, b) that yield the difference Δ have the same probability to occur. For example, for $\Delta = 1$, the occurrences of (a = 1, b = 0), (a = 2, b = 1), and (a = 3, b = 2) are equally likely. Therefore, we can write

$$P(X = a \mid Y = b) = \frac{2^M}{L_{d_\Delta}} P(X - Y = \Delta), \qquad (4)$$

where $\Delta = a - b$. By calculating $L_{d_{\Delta}}$ for different values of Δ , we found that $L_{d_{\Delta}} = 2^M - |d_{\Delta}|$.

Besides, it can be easily shown that P(X | Y) = P(Y | X). In fact, since P(X - Y) = P(Y - X) (from (2)), $|d_{\Delta}| = |2^{(8-M)}\Delta| = |2^{(8-M)}(-\Delta)| = |d_{-\Delta}|$, and $L_{d_{\Delta}} = 2^M - |d_{\Delta}| =$

 $L_{d_{-\Delta}}$, we have

$$P(Y = b \mid X = a) = \frac{2^{M}}{L_{d_{b-a}}} P(Y - X = b - a)$$

= $\frac{2^{M}}{L_{d_{a-b}}} P(X - Y = a - b)$ (5)
= $P(X = a \mid Y = b)$

Finally, combining (1), (2), and (4) yields

$$H(X \mid Y) = -\sum_{a=0}^{2^{M}-1} \sum_{b=0}^{2^{M}-1} c \frac{\alpha}{2} \frac{e^{-\alpha |d_{a-b}|}}{L_{d_{a-b}}} \log_2 \left(c \frac{2^{M-1} \alpha e^{-\alpha |d_{a-b}|}}{L_{d_{a-b}}} \right).$$
(6)

Let $H_f(M)$ be the theoretical lower compression bound for a video frame f transmitted in the absence of noise, expressed as in (6). Since the transmission channel between a user and the base station is modeled by a BSC with a transition probability q, the overall theoretical compression bound becomes [1]

$$H'_f(M) = \frac{H_f(M)}{\mathcal{C}(q)},\tag{7}$$

where $\mathcal{C}(q)$ is the capacity of the BSC defined as

$$C(q) = 1 + q \log_2(q) + (1 - q) \log_2(1 - q).$$
 (8)

In the presence of transmission errors, the Wyner-Ziv codec performs joint source-channel coding. Equation (7) shows that, by considering channel impairments, the compression bound increases as the channel noise increases $(H'_f(M) \ge H_f(M)$ since $0 \le C(q) \le 1$). On the other hand, it can be verified that in the absence of channel errors, since no error protection is needed and C(q) = 1, (7) reduces to (6) as expected.

4. JOINT SOURCE-CHANNEL TURBO DECODING

Turbo decoding is realized by iterative soft-input soft-output (SISO) decoders based on the Max-Log-MAP (maximum a posteriori) algorithm [22]. However, since nonbinary codes are used in this work, we modified the metric calculations in order to take into account all possible transitions between any couple of trellis states. Moreover, the conditional probabilities in the turbo decoding process must rely on the residual signal statistics between the even frames and the side information on one hand, and on the channel conditions on the other.

As for the turbo decoding algorithm, we chose the Max-Log-MAP algorithm in order to reduce the decoding complexity. Note that the MAP or Log-MAP [22] algorithms could also be used. However, the gain in performance would be slight compared to the important increase in the decoding complexity.

Let $\{x_{1k}^s, x_{2k}^s, x_{3k}^s, x_{4k}^s\}$ be a group of four systematic bits at the input of the turbo encoder at time instant k, and $\{x_{1k}^p, x_{2k}^p\}$ the corresponding output parity bits from the first and second encoders, respectively (see Figure 3). Let $\{y_{1k}^p, y_{2k}^p\}$ be the received noisy versions of the parity bits at the output of the BSC with transition probability q. Since only parity bits are transmitted by the Slepian-Wolf encoder, the decoder replaces the missing systematic bits with their corresponding side information $\{y_{1k}^s, y_{2k}^s, y_{3k}^s, y_{4k}^s\}$ generated using the key (i.e., odd) frames.

During the turbo decoding process, each constituent convolutional decoder needs to determine the conditional probability:

$$P(y_k \mid x_k) = P(y_k^s \mid x_k^s) P(y_k^p \mid x_k^p)$$

= $P(y_{1k}^s, y_{2k}^s, y_{3k}^s, y_{4k}^s \mid x_{1k}^s, x_{2k}^s, x_{3k}^s, x_{4k}^s)$ (9)
 $\times P(y_{ik}^p \mid x_{ik}^p),$

where $y_k = \{y_k^s, y_{ik}^p\}$ and $y_k^s = \{y_{1k}^s, y_{2k}^s, y_{3k}^s, y_{4k}^s\}$. Similarly, $x_k = \{x_k^s, x_{ik}^p\}$ and $x_k^s = \{x_{1k}^s, x_{2k}^s, x_{3k}^s, x_{4k}^s\}$. The index *i* represents the order of the constituent encoder, i = 1 or 2.

In the case where the quantization parameter M = 4, the four systematic bits at the turbo decoder input correspond to one quantized pixel from the interpolated frame.

Let $X = 8x_{1k}^s + 4x_{2k}^s + 2x_{3k}^s + x_{4k}^s$ be the bin index of the quantized pixel in the WZ frame, and $Y = 8y_{1k}^s + 4y_{2k}^s + 4y_{$

 $2y_{3k}^s + y_{4k}^s$ the bin index of the corresponding quantized side information. Using (4), we can write

$$P(y_{1k}^{s}, y_{2k}^{s}, y_{3k}^{s}, y_{4k}^{s} \mid x_{1k}^{s}, x_{2k}^{s}, x_{3k}^{s}, x_{4k}^{s}) = P(Y \mid X)$$
$$= \frac{2^{M}}{L_{d_{Y-X}}} P(Y - X),$$
(10)

where P(Y - X) is defined in (2) and $L_{d_{Y-X}}$ is the number of couples (X, Y) that yield the residual difference $\Delta = Y - X$.

In the case where M = 2, the four systematic bits correspond to two quantized pixels.

Let $X_1 = 2x_{1k}^s + x_{2k}^s$ and $X_2 = 2x_{3k}^s + x_{4k}^s$ be the bins of the two WZ quantized pixels with their corresponding side information $Y_1 = 2y_{1k}^s + y_{2k}^s$ and $Y_2 = 2y_{3k}^s + y_{4k}^s$. Therefore,

$$P(y_{1k}^{s}, y_{2k}^{s}, y_{3k}^{s}, y_{4k}^{s} | x_{1k}^{s}, x_{2k}^{s}, x_{3k}^{s}, x_{4k}^{s})$$

$$= P(Y_{1} | X_{1})P(Y_{2} | X_{2})$$

$$= \frac{2^{2M}}{L_{d_{Y_{1}-X_{1}}}L_{d_{Y_{2}-X_{2}}}}P(Y_{1} - X_{1})P(Y_{2} - X_{2}).$$
(11)

When M = 1, each systematic bit corresponds to one pixel. Let $X_i = x_{ik}^s$ be the bin index of the quantized pixel i (i = 1, ..., 4), and $Y_i = y_{ik}^s$ the corresponding side information:

$$P(y_{1k}^{s}, y_{2k}^{s}, y_{3k}^{s}, y_{4k}^{s} | x_{1k}^{s}, x_{2k}^{s}, x_{3k}^{s}, x_{4k}^{s})$$

$$= \prod_{i=1}^{4} P(Y_{i} | X_{i}) \prod_{i=1}^{4} \frac{2^{M}}{L_{d_{Y_{i}-X_{i}}}} P(Y_{i} - X_{i}).$$
(12)

Now, as $P(y_k^s | x_k^s)$ has been determined for all possible values of *M*, we can proceed with the calculation of $P(y_k^p | x_k^p)$ in (9).

First, let $P_{\text{punct}}(\rho)$ be the probability of puncturing a parity bit expressed as a function of the compression rate ρ for the current WZ frame. ρ is defined as the ratio of the number N_p of remaining parity bits after puncturing over the total number of systematic bits N_s . Since the number of parity bits at the turbo encoder output is $N_s/2$ before puncturing, we get

$$P_{\text{punct}}(\rho) = \frac{(N_s/2) - N_p}{N_s/2} = 1 - 2\rho.$$
(13)

Two cases have to be considered for the calculation of $P(y_k^p | x_k^p)$ at the decoder.

Case 1. x_k^p has been punctured at the output of the turbo encoder. In this case, y_k^p has no value $(y_k^p = n)$. Therefore,

$$P(y_k^p \mid x_k^p, x_k^p \text{ is punctured}) = \begin{cases} 1 & \text{if } y_k^p = n, \\ 0 & \text{if } y_k^p \neq n. \end{cases}$$
(14)

Case 2. x_k^p has not been punctured at the output of the turbo encoder. In this case, y_k^p can take two possible values: 0 or 1. Therefore,

$$P(y_{k}^{p} | x_{k}^{p}, x_{k}^{p} \text{ is not punctured})$$

$$= \begin{cases} 0 & \text{if } y_{k}^{p} = n, \\ \begin{cases} q & \text{if } y_{k}^{p} \neq x_{k}^{p}, \\ 1 - q & \text{if } y_{k}^{p} = x_{k}^{p}, \end{cases} \text{ if } y_{k}^{p} = 0 \text{ or } 1, \\ = \begin{cases} 0 & \text{if } y_{k}^{p} = n, \\ q[1 - \delta(y_{k}^{p} - x_{k}^{p})] + (1 - q)\delta(y_{k}^{p} - x_{k}^{p}) & \text{if } y_{k}^{p} = 0 \text{ or } 1, \end{cases}$$
(15)

where

$$\delta(k) = \begin{cases} 1 & \text{if } k = 0, \\ 0 & \text{otherwise.} \end{cases}$$
(16)

On the other hand,

$$P(y_k^p \mid x_k^p)$$

$$= P(y_k^p \mid x_k^p, x_k^p \text{ is punctured})P(x_k^p \text{ is punctured})$$

$$+ P(y_k^p \mid x_k^p, x_k^p \text{ is not punctured})$$

$$\times P(x_k^p \text{ is not punctured}).$$
(17)

Thus, $P(y_k^p | x_k^p)$ will be calculated by

$$P(y_k^p = 0, 1 | x_k^p)$$

$$= P(y_k^p = 0, 1 | x_k^p, x_k^p \text{ is not punctured})$$

$$\times P(x_k^p \text{ is not punctured})$$

$$= P(y_k^p = 0, 1 | x_k^p, x_k^p \text{ is not punctured}) \cdot (1 - P_{\text{punct}}(\rho))$$

$$= (q[1 - \delta(y_k^p - x_k^p)] + (1 - q)\delta(y_k^p - x_k^p)) \cdot 2\rho,$$

$$P(y_k^p = n | x_k^p)$$

$$= P(y_k^p = n | x_k^p, x_k^p \text{ is punctured})P(x_k^p \text{ is punctured})$$

$$= P(y_k^p = n | x_k^p, x_k^p \text{ is punctured}) \cdot P_{\text{punct}}(\rho) = 1 - 2\rho.$$

On the other hand, the extrinsic information on a symbol $d_k = x_k^s$ is given by

$$L_i(d_k) = \ln \frac{P(d_k = i)}{P(d_k = 0)}, \quad i = 1, 2, 3, \dots, 15.$$
 (19)

(18)

Therefore, it is easy to prove that [23]

$$\ln P(d_k = 0) = -\max_{i=1,\dots,15} \{0, L_i(d_k)\},\$$

$$\ln P(d_k = i) = L_i(d_k) - \max_{i=1,\dots,15} \{0, L_i(d_k)\},\ i = 1, 2, 3, \dots, 15.$$
(20)

On the other side, the logarithmic branch metric from state *s* to state *s'*, in the code trellis at time *k*, can be calculated by

$$\overline{\gamma}_{k}(s',s) = \ln P(d_{k}) + \ln P(y_{k}^{s} \mid d_{k}) + \ln P(y_{k}^{p} \mid x_{k}^{p}).$$
(21)

As for the forward and backward state metrics, they are given by

$$\overline{\alpha}_{k}(s) = \max_{s'} [\overline{\gamma}_{k}(s',s) + \overline{\alpha}_{k-1}(s')],$$

$$\overline{\beta}_{k-1}(s') = \max_{s} [\overline{\gamma}_{k}(s',s) + \overline{\beta}_{k}(s)].$$
(22)

On the other hand, the log-likelihood ratio of symbol d_k is calculated using

$$\operatorname{LLR}_{i=1,2,\dots,15}_{i=1,2,\dots,15} = \max_{\substack{(s',s)\\d_k=i}} [\overline{\gamma}_k(s',s) + \overline{\alpha}_{k-1}(s') + \overline{\beta}_k(s)] \\ - \max_{\substack{(s',s)\\d_k=0}} [\overline{\gamma}_k(s',s) + \overline{\alpha}_{k-1}(s') + \overline{\beta}_k(s)].$$
(23)

Finally, the extrinsic information used as a priori information to the next decoder is calculated by

$$L_i^a(d_k) = \text{LLR}_i(d_k) - L_i(d_k) - L_i^c(d_k), \qquad (24)$$

where $L_i^c(d_k) = \ln(P(y_k^s \mid d_k = i)/P(y_k^s \mid d_k = 0))$ is a measure of the channel reliability [18].

At the end of each decoding iteration, 15 LLRs are calculated for each symbol d_k . At the last iteration, d_k is decoded as

$$\widetilde{d}_{k} = \begin{cases} \arg\max \ \text{LLR}_{i}(d_{k}) & \text{if } \max_{i} \ \text{LLR}_{i}(d_{k}) > 0, \\ 0 & \text{otherwise.} \end{cases}$$
(25)

5. ADAPTIVE RATE ALLOCATION AND QUANTIZATION TECHNIQUE

Consider a system of *N* users sharing the same wireless medium to transmit video data to a base station at a total bitrate of *R* bits per second (bps). Let $\rho_{f,n}$ be the compression rate for frame *f* at node *n* defined as in Section 4, $M_{f,n}$ the quantization parameter for this frame, and $A_{f,n} = M_{f,n} \cdot \rho_{f,n}$ its average number of bits per pixel. In our joint sourcechannel codec, if no parity bits are transmitted, $\rho_{f,n} = 0$. On the other side, if all parity bits are transmitted without any puncturing, $\rho_{f,n} = 1/2$. As a result, the compression rate can be varied between these two extreme cases: $0 \le \rho_{f,n} \le 1/2$. Our aim is to determine, for each frame *f* at every user *n*, the couple $(M_{f,n}, \rho_{f,n})$ that optimizes the average system performance. In other words,

$$\{(M_{f,n}, \rho_{f,n}); n = 1, \dots, N\} = \underset{\substack{M_{f,n} \in \{1,2,4\}\\0 \le \rho_{f,n} \le 1/2}}{\operatorname{arg\,max}} \left(\frac{1}{N} \sum_{n=1}^{N} \operatorname{PSNR}_{f,n}\right),$$
(26)

where $\text{PSNR}_{f,n}$ is the peak signal-to-noise ratio obtained after the decoding and reconstruction of the frame f

encoded at the user *n*. PSNR_{*f*,*n*} depends not only on the parameters $M_{f,n}$ and $\rho_{f,n}$, but also on the transmission conditions, the accuracy of the side information, and the rate constraint:

$$\sum_{n=1}^{N} R_{f,n} \le R,\tag{27}$$

where $R_{f,n}$ is the transmission rate assigned for the frame f at the user n. As a result, it is difficult to solve analytically (26) for the set { $(M_{f,n}, \rho_{f,n})$; n = 1, ..., N}. For this reason, we proceed with the optimization process in two stages. First, we determine the transmission rate for each user, and then we choose the couples $(M_{f,n}, \rho_{f,n})$ that yield the best reconstructed output at the specified bitrates.

In the first stage, instead of assigning R/N bps for each user, the base station first determines the compression bound for each frame as in (7), based on its content (parameter α) and on the user transmission conditions (channel crossover probability q). Since the optimal quantization parameter has not been determined yet, (7) is calculated for M = 8, assuming eight-bit raw video data before compression. Then, in a proportionally fair attribution, the user n is assigned the rate

$$R_{f,n} = \frac{H'_{f,n}(8)}{\sum_{n=1}^{N} H'_{f,n}(8)} R,$$
(28)

where $H'_{f,n}(8)$ represents the entropy in (7) calculated for frame *f* at node *n* with M = 8.

The average number of bits per pixel $A_{f,n}$ is related to $R_{f,n}$ by

$$A_{f,n} = \frac{R_{f,n}}{m \cdot n \cdot r},\tag{29}$$

where (m, n) represent the dimensions of a given frame, and r the WZ frame rate (in fps).

In the second stage, the base station needs to determine, for each frame f at every node n, the couple $(M_{f,n}, \rho_{f,n})$ that yields the best video output after reconstruction, at the specified rate $R_{f,n}$. In fact, this is equivalent to optimizing the individual rate-distortion performance for each user since, for a given bitrate, the parameters are chosen in such a way to maximize PSNR_{*f,n*}.

After a thorough analysis of the system performance observed for different values of $M_{f,n}$, we noticed that in most cases, for a given target bitrate, choosing the lowest allowable value of $M_{f,n}$ yields the best video quality at the decoder output. Indeed, by reducing the number of quantization levels, the system is able to transmit a greater amount of parity bits to protect the quantized bitstream from channel errors, especially when q increases. However, in some cases, the assigned bitrate is sufficient enough to permit efficient error protection when a greater value of $M_{f,n}$ is selected; thus, a better reconstructed output can be obtained. In all cases, we noticed that the system behavior for different configurations of the couples $(M_{f,n}, \rho_{f,n})$ is directly related to the ratio between $A_{f,n}$ and the theoretical compression bound defined as

$$C_{f,n}(M_{f,n}) = \frac{A_{f,n}}{H'_{f,n}(M_{f,n})}.$$
(30)

Therefore, we define the thresholds T_1 , T_2 , and T_4 which indicate the average value of the ratio $C_{f,n}(M_{f,n})$ that permits a correct decoding of a transmitted frame for $M_{f,n} =$ 1, 2, and 4, respectively. These thresholds are determined experimentally by observing the system performance for different values of the ratio $C_{f,n}(M_{f,n})$, as will be detailed in Section 6. Our proposed algorithm then proceeds with the dynamic quantization (see Figure 4) as follows.

Step 1. Initially, set $M_{f,n}$ to the lowest value that permits to reach $A_{f,n}$. This will allow for the maximum error protection for a given $A_{f,n}$.

Step 2. Calculate $C_{f,n}(1)$, $C_{f,n}(2)$, and $C_{f,n}(4)$.

Step 3. If M = 4 and $C_{f,n}(4) \leq T_4$, set $M_{f,n} = 2$ and $\rho_{f,n} = 1/2$. In other words, if $A_{f,n}$ could not be reached for $M_{f,n} < 4$ (i.e., $A_{f,n} > 1$) and the amount of error protection transmitted with $M_{f,n} = 4$ does not yield an acceptable decoding error rate, set $M_{f,n}$ to the next lower value and transmit all parity bits. In this case, the given frame is transmitted at a rate lower than the target bitrate since the target $A_{f,n}$ could not be reached exactly. Similarly, if $M_{f,n} = 2$ and $C_{f,n}(2) \leq T_2$, set $M_{f,n} = 1$ and $\rho_{f,n} = 1/2$.

Step 4. If $M_{f,n} = 1$ and $C_{f,n}(1) \le T_1$, drop the frame (set $M_{f,n} = 0$). In this case, the amount of transmitted bits will not permit efficient decoding even if the number of quantization levels is reduced to its minimum. At the decoder, the dropped frame is replaced by the corresponding side information. Note that other error concealment techniques can also be envisaged in the receiver.

Step 5. If $M_{f,n} = 1$ and $C_{f,n}(2) > T_2$, set $M_{f,n} = 2$. In other words, if $A_{f,n}$ is reachable with $M_{f,n} = 1$ and 2, and it is possible to send a sufficient amount of parity bits to correctly decode the frame with $M_{f,n} = 2$, set $M_{f,n} = 2$ since it yields a better reconstructed output. Similarly, if $M_{f,n} = 2$ and $C_{f,n}(4) > T_4$, set $M_{f,n} = 4$.

Step 6. If the frame was not dropped and $\rho_{f,n}$ was not already set to 1/2, set $\rho_{f,n} = A_{f,n}/M_{f,n}$.

Step 7. Transmit the couple $(M_{f,n}, \rho_{f,n})$ to the corresponding user.

As it can be seen from the proposed algorithm, control information is sent only once from the base station to the users. Moreover, instantaneous decoding at the receiver is no more required, and only one decoding run is performed for each frame. As a result, all the disadvantages related to the return channel in traditional Wyner-Ziv applications are eliminated.



FIGURE 4: Dynamic quantization algorithm with a frame dropping mechanism.



FIGURE 5: R-D curves obtained with a TRD system and with the ARA technique.

6. EXPERIMENTAL RESULTS

In our simulation setup, we consider a set of three mobile users (N = 3) capturing different scenes and transmitting the resulting video to a central base station. These scenes are assumed to be the Foreman, Carphone, and Mother-Daughter QCIF video sequences. They are sampled at a rate of 15 WZ frames per second (fps), which corresponds to an overall sampling rate of 30 fps. For example, this can be seen as a network of surveillance cameras in a building, each located in a different floor, or a network of mobile users positioned at different locations in a cell. We consider the first 100 frames of each sequence repeated in 50 simulations. The side information is generated by motion-compensated interpolation with symmetric motion vectors as described in [8]. The time-varying nature of the transmission channel between a video user and the base station is modeled by a uniform random variation of the crossover probability q between 0.001 and 0.02, independently for each user.

In Figure 5, we first show the rate-distortion (R-D) curves obtained with a traditional (TRD) system where all users are assigned an equal bandwidth. The quantization parameter M is fixed and is the same for all users. The results are presented in terms of the PSNR averaged over the three video scenes as a function of the total WZ bitrate occupied by all the users. We also show the results obtained with our adaptive rate allocation (ARA) technique (see (28) and (29)), but with a constant quantization parameter. We can clearly see that when the rate regions overlap for different values of *M*, the best performance, in both ARA and TRD systems, is obtained when the lowest value of M is used. For example, at 570 kbps, the use of a one-bit quantizer yields a performance gain of nearly 1 dB, compared to the case with a two-bit quantizer. A similar effect is noticed at 1 Mbps, where the system with a two-bit quantizer outperforms the one with a four-bit quantizer by 0.8 dB.



FIGURE 6: Individual PSNR as a function of the total bitrate, for the Carphone (C), Foreman (F), and Mother-Dauther (D) sequences, with M = 4.

In some cases, the performance of a TRD system can be better than that of ARA. In Figure 6, we present the individual PSNR of the different video sequences, for the case where M = 4. In fact, a similar behavior is observed for different values of M. We notice that at a total bitrate of 1 Mbps, the performance loss for the Mother-Daughter (D) sequence is relatively high, which degrades the average ARA system performance, compared to the TRD system, as also shown in Figure 5. The remedy for this problem is to reduce the number of quantization levels for the transmission at this bitrate, as was explained earlier. We also notice that the ARA technique significantly improves the PSNR of the Carphone (C) and Foreman (F) sequences at the expense of a reduced performance for Mother-Daughter. This can be explained by the fact that the Mother-Daughter sequence contains low-motion scenes, while Carphone and Foreman are characterized by average and high-motion scenes. In fact, the ARA technique allocates the lowest rates for videos with low motion and/or experiencing good channel conditions, while the highest rates are assigned to video users capturing high-motion scenes and/or suffering from a bad channel. This results in an improved average system performance, especially at medium and high total transmission rates.

The analysis of the individual PSNR as a function of the total bitrate (as in Figure 6) can sometimes be misleading. In Figure 7, the PSNR of each video sequence is represented as a function of the effective WZ bitrate assigned for each user, for the case where M = 4. Figure 7 clearly shows that the R-D curves obtained with the ARA technique are above those obtained with a TRD system. This implies that the ARA technique improves not only the average system performance, but the individual R-D performance for each user as well, especially at medium and high bitrates.

This effect can be further explained by Table 1 which shows the average bitrates (in kbps) assigned for each user with the ARA technique. In the TRD system, all users operate



FIGURE 7: Individual R-D curves for the Carphone (C), Foreman (F), and Mother-Dauther (D) sequences obtained with M = 4.

at the same bitrate. Indeed, we notice that in all cases, for a certain total bitrate, the ARA technique assigns the Mother-Daughter sequence the lowest bitrate compared to the two other sequences. For example, at a total rate of 1.5 Mbps, the bitrate assigned for Mother-Daughter is almost half the one assigned for Carphone. Moreover, the bitrate assigned for the Mother-Daughter sequence by the ARA technique is less than the one assigned by the TRD system. This allows the assignment of higher bitrates to the two other sequences, and leads to an improvement in the overall system performance.

In order to apply the dynamic quantization algorithm and the frame dropping mechanism, it is necessary to determine suitable values for the thresholds T_1 , T_2 , and T_4 defined in Section 5. For this purpose, we show, in Figure 8, the BER obtained after source-channel decoding, as a function of the ratio $C_{f,n}$ defined in (30). For each value of M, the transmission of 22500 frames from different video sequences was simulated with variable channel conditions. In general, a BER close to 10^{-3} is desired to yield a good reconstructed output [8]. When M = 1, only the most significant bit in each pixel is coded and transmitted, which greatly affects the performance of the reconstruction function. For this reason, we chose a threshold $T_1 = 6$ to guarantee a BER less than 10^{-3} in this case. Similarly, we chose $T_2 = 4$ for a BER of 10^{-3} when M = 2. For the case where M = 4, a higher BER can be tolerated since the two least significant bits in the quantized pixel are less important than the two most significant bits. Therefore, we chose $T_4 =$ 2.4. In the sequel, we will show the system performances for these selected values of the thresholds, and compare them to the ones obtained with other values of T_2 and T_4 .

In Figure 9, it can be seen that the problem of overlapping rate regions is avoided by applying dynamic quantization (curves labeled "ARAQ" and "ARAQ-D"), in addition to adaptive rate allocation. When no frame dropping is performed (ARAQ: Step 4 in the dynamic quantization

	Total	TRD	ARA (C)	ARA (F)	ARA (D)
	249.5	83.16	80.1	95.5	73.9
<i>M</i> = 1	320.8	106.92	103.2	124.4	93.2
	392	130.68	127.6	150.5	113.9
	499	166.32	212.9	168.3	117.7
<i>M</i> = 2	641.5	213.84	274.2	219.9	147.4
	784.1	261.36	331.1	274.4	178.6
	997.9	332.64	405.4	353.4	239.2
M = 4	1283	427.68	520.3	461.9	300.8
	1568.2	522.72	636.5	568.5	363.1

TABLE 1: Average individual bitrates in kbps for the Carphone (C), Foreman (F), and Mother-Dauther (D) sequences.



FIGURE 8: Performance curves showing the BER as a function of the ratio in (30) for M = 1, 2, and 4.

algorithm is skipped), a performance gain towards the TRD system is observed only at high rates, for $T_2 = T_4 = 2.7$. The reason for this behavior is that, at low rates, M takes the values 1 or 2 most of the time and $T_2 = 2.7$ does not guarantee a good BER when M = 2, as shown in Figure 8, whereas for M = 4 (mostly at high rates), $T_4 = 2.7$ yields acceptable performance. Compared to the TRD system, very close performances are obtained at low rates by setting $T_2 =$ 4 and $T_4 = 2.4$, while an important enhancement is noticed at medium and high rates. In fact, at very low rates, the available bandwidth to be allocated for the different users is barely sufficient to protect the transmitted bitstreams. At a rate near 200 kbps, we notice a performance loss of 0.5 dB, whereas a gain of 1.5 dB is observed with the frame dropping mechanism (ARAQ-D curves) for $T_1 = 6$. When the bitrate increases, less frames are dropped. Starting from 600 kbps, the R-D curves are the same with or without frame dropping. This is expected since frames are only dropped when the assigned bitrate is not sufficient to guarantee a correct decoding of the transmitted WZ frame. On the other hand, at 500 kbps, our proposed algorithm yields similar performance compared to the TRD system with M = 1, but



FIGURE 9: R-D Curves obtained with a TRD system and with the ARAQ and ARAQ-D techniques.

a gain of 1.4 dB is observed towards the case where M = 2. At 1 Mbps, the gain reaches 0.6 dB compared to M = 2 and 1.5 dB to M = 4.

It is important to note that when M is fixed (TRD and ARA systems), the transmission bitrate for the WZ codec is limited to a narrow range. For example, a traditional system with N = 3 cannot transmit at a total rate greater than 570 kbps when M = 1, and 1140 kbps when M = 2 (assuming QCIF video sequences sampled at 15 WZ-fps). Our proposed algorithm with the ARAQ and ARAQ-D techniques allows the system to transmit video data at a wider range of transmission rates and with an optimized decoding quality.

Figures 10, 11, and 12 show the individual R-D performance for the Carphone (C), Foreman (F), and Mother-Daughter (D) sequences, respectively, obtained with our ARAQ-D technique with $T_1 = 6$, $T_2 = 4$, and $T_4 = 2.4$. Compared to the TRD system, it can be seen, as explained in Section 5, that the R-D performance for each user is improved, especially at high rates. At an individual rate of 430 kbps, the gain reaches 1.5 dB for Carphone, 1.2 dB for Foreman, and 0.6 dB for Mother-Daughter. Again, it can be seen that Mother-Daughter is assigned the lowest bitrates. The maximum bitrate allocated to the Mother-Daughter sequence is 430 kbps, while Carphone and Foreman are



FIGURE 10: R-D curves for the Carphone (C) sequence obtained with the ARAQ-D technique, compared to the performance of a TRD system.



FIGURE 11: R-D curves for the Foreman (F) sequence obtained with the ARAQ-D technique, compared to the performance of a TRD system.

assigned a maximum of 615 kbps and 610 kbps, respectively. The unequal assignment of channel resources with the proposed rate allocation techniques (ARA, ARAQ, and ARAQ-D) results in an improvement in the overall system performance.

In our simulations, key frames were assumed to be perfectly recovered at the receiver. The case where key frames are subject to degradations due to lossy source coding or channel impairments can be easily taken into account in our study by modifying the entropy calculations in Section 3 accordingly. However, it should be noted that, in this case, all studied systems (TRD, ARA, ARAQ, and ARAQ-D) would be subject to a similar performance degradation. As a result, the performance analysis presented earlier would still hold.



FIGURE 12: R-D curves for the Mother-Daughter (D) sequence obtained with the ARAQ-D technique, compared to the performance of a TRD system.

In Figure 13, we show a snapshot from the Carphone video sequence (7th WZ frame) obtained with both the TRD (Figures Figure 13(b) and Figure 13(c)) and ARAQ-D (Figures 13(d) and 13(e)) systems, for the same transmission conditions ($R_{f,n} = 332.64$ kbps and $q = 6.4 \cdot 10^{-3}$). The middle column shows the turbo decoded images before reconstruction, and the right column shows the final reconstructed outputs. In the TRD system, the quantization parameter was set to $M_{f,n} = 4$ and the compression rate to $\rho_{f,n} = 0.21875$, whereas the ARAQ-D system determined that $M_{f,n} = 2$ and $\rho_{f,n} = 0.4375$ would yield a better result, even though in both cases $A_{f,n} = 0.875$. In fact, when $M_{f,n} = 4$, more details about the transmitted image are available at the receiver, as shown in Figure 13(b) compared to Figure 13(d). This is supposed to help the reconstruction function in improving the output video quality. However, the received frame was decoded with BER = 0.09 in the TRD system, giving a noiselike visual effect (see Figure 13(b)), whereas in the ARAQ-D system, the frame was perfectly recovered (BER ≈ 0) with $M_{f,n} = 2$ (see Figure 13(d)). This is due to the fact that, in the latter case, the choice of $\rho_{f,n} = 0.4375$ leads to a better protection of the transmitted bitstream. The superior performance of the ARAQ-D system can be observed by comparing Figures 13(c) and 13(e). A visual inspection of both images shows that the reconstruction function was not able to completely remove the noise-like effect from the decoded image in the TRD system, whereas in the ARAQ-D system, the reconstructed image is visually better. This performance gain can be further observed in the output PSNR: 31.5 dB in Figure 13(c) and 34 dB in Figure 13(e), resulting in a 2.5 dB gain. However, in both cases, the PSNR for this frame is below the average PSNR obtained at the same bitrate and presented in Figure 10. This is due to a higher level of motion in this particular frame, compared to the average motion level in the sequence.

Finally, we show in Figure 14 the 40th WZ frame from the Foreman sequence. In the ARAQ system, the original





(d) ARAQ-D decoded image



(e) ARAQ-D reconstructed image

FIGURE 13: Snapshot from the Carphone sequence. (a) Original image. (b) TRD turbo decoded image with M = 4 and $\rho = 0.21875$. (c) Reconstructed image from (b). (d) ARAQ-D turbo decoded image with M = 2 and $\rho = 0.4375$. (e) Reconstructed image from (d).



(a) Original image

(b) ARAQ reconstructed image



FIGURE 14: Snapshot from the Foreman sequence. (a) Original image. (b) ARAQ reconstructed image with M = 1 and $\rho = 0.25$. (c) ARAQ-D output image obtained by replacing the frame with its corresponding side information.

WZ frame was quantized with M = 1, compressed with $\rho = 0.25$, and transmitted at 95 kbps over a BSC with q = $9 \cdot 10^{-3}$. As in the previous example, the image was decoded with a high BER (0.02) which caused undesirable noise in the reconstructed output (Figure 14(b)). The ARAO-D system determined that under these conditions, it is not possible to recover an acceptable version of the transmitted frame. Therefore, the frame was dropped in the transmitter and replaced by the corresponding side information at the receiver side (Figure 14(c)). It can be clearly seen that the resulting image has a smoother visual effect. The PSNR in Figure 14(b) is 30.65 dB compared to 32.61 in Figure 14(c), resulting in a 2 dB gain. However, in both images, we notice a deformation of the mouth (compared to Figure 14(a)). In fact, this frame was captured from a fast mouth opening and closing scene (high-motion of the lips), which yielded less accurate side information for this region. In general, when the available transmission rate permits an error-free decoding of the WZ frame, the influence of inaccurate side information on the final output is reduced to a large extent.

7. CONCLUSION

In this paper, we introduced a novel rate allocation technique for distributed multiuser Wyner-Ziv video coding systems. Using entropy calculations, the available system bandwidth is unequally distributed among several users transmitting data to a central base station without the need for a permanent feedback channel. The proposed rate allocation technique allows the system to adapt to the random variations of the wireless channel and to different amounts of motion captured by the different users. The quantization parameters are dynamically varied to optimize the decoding quality, and a frame dropping mechanism allows the system to avoid unnecessary channel use. Our results obtained by simulating a network of multiple users show a significant improvement in the average system performance, as well as in the individual R-D performance of each user. The gain in the average PSNR can reach 1.5 dB compared to a traditional system where the available bandwidth is equally shared by all the users and the quantization parameters are fixed.

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