# Feedback Control of Dynamic Bipedal Robot Locomotion <br> Eric R. Westervelt, Jessy W. Grizzle, <br> Christine Chevallereau, Jun Ho Choi, and Benjamin Morris 

## Errata

Known errors and correction as of January 28, 2014.

- Page 58 (Submitted by Kaveh Akbari Hamed): Equation (3.31) should be the following.

$$
\mathcal{S}:=\left\{\left(q_{\mathrm{s}}, \dot{q}_{\mathrm{s}}\right) \in T \mathcal{Q}_{\mathrm{s}} \mid p_{2}^{\mathrm{v}}\left(q_{\mathrm{s}}\right)=0, p_{2}^{\mathrm{h}}\left(q_{\mathrm{s}}\right)>0\right\} .
$$

- Page 63 (Submitted by Kaveh Akbari Hamed): Equation (3.57) should be the following.

$$
\tilde{\Sigma}:\left\{\begin{aligned}
\dot{\tilde{x}} & =\tilde{f}_{\mathrm{s}}(\tilde{x})+\tilde{g}_{\mathrm{s}}(\tilde{x}) v & & \tilde{x}^{-} \notin \mathcal{S} \\
\tilde{x}^{+} & =\tilde{\Delta}\left(\tilde{x}^{-}\right) & & \tilde{x}^{-} \in \mathcal{S},
\end{aligned}\right.
$$

- Page 67 (Submitted by Hae Won Park): Equation (3.67) should be the following.

$$
\begin{aligned}
\left(C_{\mathrm{s}}(q, \dot{q})\right)_{1,2} & =-\frac{1}{2} m r^{2} \sin \left(\theta_{1}-\theta_{2}\right) \dot{\theta}_{2} \\
\left(C_{\mathrm{s}}(q, \dot{q})\right)_{1,3} & =M_{T} r \ell \sin \left(\theta_{1}-\theta_{3}\right) \dot{\theta}_{3} \\
\left(C_{\mathrm{s}}(q, \dot{q})\right)_{2,1} & =\frac{1}{2} m r^{2} \sin \left(\theta_{1}-\theta_{2}\right) \dot{\theta}_{1} \\
\left(C_{\mathrm{s}}(q, \dot{q})\right)_{3,1} & =-M_{T} r \ell \sin \left(\theta_{1}-\theta_{3}\right) \dot{\theta}_{1}
\end{aligned}
$$

- Page 93 (Submitted by Kaveh Akbari Hamed): In item (e), " $\varphi^{+}(t):=\lim _{\tau} \gamma_{t} \varphi(\tau)$ " should be " $\varphi^{-}(t):=\lim _{\tau}{ }_{t t} \varphi(\tau)$ ".
- Page 95 (Submitted by Kaveh Akbari Hamed): On the first line, " $\mathcal{X}_{2}$ " should be " $\mathcal{X}_{1}$ ".
- Page 107 (Submitted by Kaveh Akbari Hamed): The following hypothesis should be added to list of hypotheses for Proposition 4.3:

5. $\mathcal{Z}_{(\alpha \rightarrow \beta)}$ is forward invariant and continuously finite-time attractive under $f_{(\alpha \rightarrow \beta)}$.

- Page 147 (Submitted by Kaveh Akbari Hamed): In Table 6.1, " 0.813 " should be " 0.662 ".
- Pages 153,154: NEC2, NEC4, and NEC5 should be NIC4, NIC5, and NIC6, respectively.
- Page 158 (Submitted by Thomas Schauss): Equation (6.67) should be the following.

$$
\left[L_{\tilde{g}} L_{\tilde{f}} h(\tilde{q})\right]^{-1}=\mathrm{I}_{(N-1) \times(N-1)}-\frac{1}{\operatorname{det}\left(L_{\tilde{g}} L_{\tilde{f}} h\right)(\tilde{q})} \frac{\partial h_{d}(\theta)}{\partial \theta} \tilde{J}^{\mathrm{norm}}\left(q_{\mathrm{b}}\right) .
$$

- Page 158 (Submitted by Thomas Schauss): Equation (6.68) should be the following.

$$
\begin{aligned}
{\left[L_{\tilde{g}} L_{\tilde{f}} h(\tilde{q})\right]^{-1}=} & \mathrm{I}_{(N-1) \times(N-1)} \\
& -\left(\frac{1}{\tilde{d}_{N, N}\left(q_{\mathrm{b}}\right)+\left[\tilde{d}_{N, 1}\left(q_{\mathrm{b}}\right), \cdots, \tilde{d}_{N,(N-1)}\left(q_{\mathrm{b}}\right)\right] \frac{\partial h_{d}(\theta)}{\partial \theta}}\right) \\
& \left(\frac{\partial h_{d}(\theta)}{\partial \theta}\left[\tilde{d}_{N, 1}\left(q_{\mathrm{b}}\right), \cdots, \tilde{d}_{N,(N-1)}\left(q_{\mathrm{b}}\right)\right]\right) .
\end{aligned}
$$

- Page 195 (Submitted by Amine Kamel): Equation (7.9) should be the following.

$$
\left[\begin{array}{l}
\alpha_{0} \\
\theta_{\alpha}^{+}
\end{array}\right]=H R H^{-1}\left[\begin{array}{c}
\alpha_{M} \\
\theta_{\alpha}^{-}
\end{array}\right]
$$

- Page 242: "10.1 W" should be " 40.4 W "
- Page 245: "8.9 W" should be " 35.6 W "
- Page 271 (Submitted by Ulrich Romer): Equation (9.51) should be the following.

$$
\dot{q}^{\mathrm{f}-}=A^{-1}\left(A+m_{\mathrm{tot}} \frac{\partial \mathbf{f}_{2}^{\prime}}{\partial q} \frac{\partial \mathbf{f}_{2}}{\partial q}\right) R^{-1} \dot{q}_{0}^{\mathrm{s+}} \delta\left(\sigma_{1}^{\mathrm{s}-}\right)-m_{\mathrm{tot}} A^{-1} \frac{\partial \mathbf{f}_{2}^{\prime}}{\partial q}\left[\begin{array}{c}
\dot{\mathbf{x}}_{\mathrm{cm}}^{f-} \\
\dot{\mathbf{y}}_{\mathrm{cm}}^{f-}
\end{array}\right] .
$$

(In the book, there is a $+\operatorname{sign}$ in front of $m_{\mathrm{tot}} A^{-1}$ )

- Page 398 (Submitted by Kaveh Akbari Hamed): Equation (B.83) should be the following.

$$
\tilde{f}^{*}(\eta, z)=\left[\begin{array}{c}
\tilde{f}_{1}^{*}\left(\eta_{1}\right) \\
\vdots \\
\tilde{f}_{m}^{*}\left(\eta_{m}\right) \\
\tilde{f}_{r+1}(\eta, z) \\
\vdots \\
\tilde{f}_{n}(\eta, z)
\end{array}\right]
$$

- Page 398 (Submitted by Kaveh Akbari Hamed): Equation (B.85) should be the following.

$$
\left.\tilde{f}^{*}\right|_{\mathcal{Z}}(z)=\left[\begin{array}{c}
\tilde{f}_{r+1}(0, z) \\
\vdots \\
\tilde{f}_{n}(0, z)
\end{array}\right]
$$

- Page 431 (Submitted by Hae Won Park): Equation (B.204) should be the following.

$$
\bar{D}(\bar{q})=\left.\left(\frac{\partial F(q)^{\prime}}{\partial q}\right)^{-1} D(q)\left(\frac{\partial F(q)}{\partial q}\right)^{-1}\right|_{q=F^{-1}(\bar{q})}
$$

- Page 432 (Submitted by Noah Cowan): Equation (B.211) should be the following.

$$
\Gamma=\left[\begin{array}{c}
-\left(\frac{\partial \lambda\left(q_{1}\right)}{\partial q_{1}}\right)^{\prime} \\
\mathrm{I}
\end{array}\right] u^{*}(q, \dot{q}),
$$

- Page 432 (Submitted by Noah Cowan): Equation (B.212) should be the following.

$$
\left[\begin{array}{c}
\dot{x}_{1} \\
\dot{x}_{2}
\end{array}\right]=\left[\begin{array}{c}
x_{2} \\
\left.D^{-1}\left(x_{1}\right)\left(-C\left(x_{1}, x_{2}\right) x_{2}-G\left(x_{1}\right)+\left[\begin{array}{c}
-\left(\frac{\partial \lambda\left(q_{1}\right)}{\partial q_{1}}\right)^{\prime} \\
\mathrm{I}
\end{array}\right] u^{*}\left(x_{1}, x_{2}\right)\right)\right] . . . ~ . ~ . ~
\end{array}\right.
$$

- Page 432 (Submitted by Kaveh Akbari Hamed): Equation (B.214) should be the following.

$$
D\left(q_{1}, q_{2}\right)=\left[\begin{array}{ll}
D_{11}\left(q_{1}, q_{2}\right) & D_{12}\left(q_{1}, q_{2}\right) \\
D_{12}^{\prime}\left(q_{1}, q_{2}\right) & D_{22}\left(q_{1}, q_{2}\right)
\end{array}\right]
$$

- Page 432 (Submitted by Noah Cowan): Equation (B.216) should be the following.

$$
\Gamma \cdot \dot{q}=\left(\left[\begin{array}{c}
-\left(\frac{\partial \lambda\left(q_{1}\right)}{\partial q_{1}}\right)^{\prime} \\
\mathrm{I}
\end{array}\right] u^{*}\right)^{\prime} \dot{q}=\left(u^{*}\right)^{\prime} \frac{d}{d t}\left(q_{2}-\lambda\left(q_{1}\right)\right)
$$

- Page 438 (Submitted by Oscar E. Ramos Ponce): Equation (B.234b) should be the following.

$$
\left(G_{\mathrm{s}}\left(q_{1}, q_{2}\right)\right)_{2}=\left(m_{1} g_{0} L_{2}+m_{2} g_{0} \ell_{\mathrm{cm}, 2}^{\mathrm{h}}\right) \cos \left(q_{2}\right)+m_{1} g_{0} \ell_{\mathrm{cm}, 1}^{\mathrm{h}} \cos \left(q_{1}+q_{2}\right)
$$

- Page 441 (Submitted by Kaveh Akbari Hamed): On the second line of Section C.1.4, " $T_{I}(x)<\infty$ " should be " $T_{I}(\Delta(x))<\infty$ ".
- Page 445 (Submitted by Kaveh Akbari Hamed): Equation (C.25) should be the following.

$$
\mathcal{D} T_{I}^{\epsilon}\left(\hat{\Delta}\left(z_{2: k}^{*}, \eta^{*}\right)\right)=-\left(L_{f^{\epsilon}} H\left(x^{*}\right)\right)^{-1} \frac{\partial H}{\partial x}\left(x^{*}\right) \Phi^{\epsilon}\left(t^{*}, \hat{\Delta}\left(z_{2: k}^{*}, \eta^{*}\right)\right)
$$

