

FFT-Based Analysis of Periodic Structures in Microacoustic Devices

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Abstract—Periodic structures utilized as transducer or reflector elements play an important role in microacoustic wave devices. Such structures can be described using approximate analytical models. However, to obtain the accuracy required for reliable device simulation, numerical methods have to be employed. In this contribution, we present an efficient numerical approach to calculate the dispersion curves associated with microacoustic modes propagating in periodic structures; the method is demonstrated for the case of Love wave modes. The computational efficiency is related to the utilization of the FFT algorithm in a hybrid Method of Moments (MoM) /Mode-Matching analysis. From the obtained dispersion curves, characteristic parameters such as the stopband width can be obtained which can be used in a coupling-of-modes (COM) model of the structure.

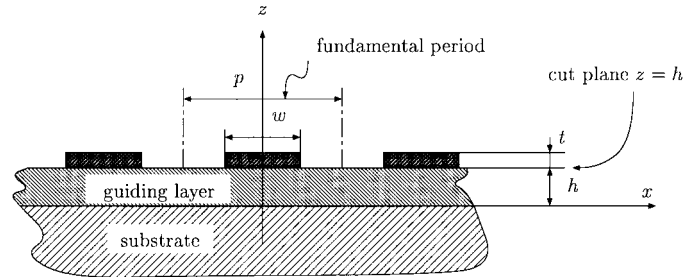


Fig. 1. Love wave guiding structures with periodic perturbations.

the FFT algorithm to obtain a computationally efficient method.

I. INTRODUCTION

IN THE ANALYSIS of periodic structures, so-called Floquet modes are frequently encountered [1]. In a wave guiding structure with periodic perturbations in the propagation direction (x), eigenmodes can be obtained in “Floquet-periodic” form:

$$\psi(x) = \psi_p(x)e^{-jk_0x} \quad (1)$$

where $\psi(x)$ stands for any of the field components associated with the mode, and $\psi_p(x)$ denotes a periodic function obeying the same period p as the perturbation: $\psi_p(x+p) = \psi_p(x)$. k_0 represents the characteristic wavenumber for the Floquet mode, which depends on the (angular) frequency ω . Because of the periodic function $\psi_p(x)$, a Floquet mode does not show a purely harmonic x dependence but represents a superposition of harmonic wave functions with wavenumbers $k_n = k_0 + n 2\pi/p$, where $n = -\infty, \dots, \infty$ as it can be perceived by expanding $\psi_p(x)$ in a Fourier series. Waves in periodic microacoustic structures have been analyzed utilizing the MoM together with the concept of a Floquet periodic Green’s function (see, e.g. [2]–[5]).

In this contribution, we present an approach employing a hybrid MoM/Mode-Matching technique that utilizes

II. THEORY

To illustrate the procedure, we outline the analysis method by considering Love waves propagating in a waveguide that is periodically loaded with elastic blocks (Fig. 1). Love waves are of interest for liquid sensor applications because they are shear polarized and do not couple with compressional acoustic wave modes in adjacent liquids [6], [7]. The structure is two-dimensional, showing no variations in the y direction; hence, $\partial/\partial y \equiv 0$. This geometry can also be interpreted as a model for reflector structures on a Love wave device. For the sake of simplicity, we demonstrate the approach for Love waves propagating on a nonpiezoelectric, isotropic substrate. (The generalization to more general cases will be illustrated later.)

For the following, we assume harmonic time dependence of all field quantities and suppress the common factor $\exp(j\omega t)$. We consider purely shear polarized Love modes for which the only non-vanishing displacement component is the displacement in y direction, u_y . Because $u_x = u_z = 0$ and $\partial/\partial y \equiv 0$, the only non-vanishing elements of the stress tensor T_{ij} [8] are $T_{xy}(=T_{yx})$ and $T_{yz}(=T_{zy})$. Because of the isotropy of the materials and because all material boundary planes are orthogonal to the xz plane, no coupling to differently polarized (sagittal) modes occurs. The interaction between the Love wave and the perturbing blocks occurs in the plane $z = h$. The boundary conditions in the fundamental period $[-p/2, p/2]$ are

$$T_{yz}|_{z=h} = 0 \text{ for } |x| \in]w/2, p/2[, \quad (2)$$

$$\left. \begin{aligned} T_{yz}|_{z=h^+} &= T_{yz}|_{z=h^-} \\ u_y|_{z=h^+} &= u_y|_{z=h^-} \end{aligned} \right\} \text{ for } x \in]-w/2, w/2[, \quad (3)$$

which, accordingly shifted, also holds in all other periods.

Manuscript received June 9, 1998; accepted November 9, 1999. This work was supported by the Brite-Euram project BE-95-1745:MIMICS.

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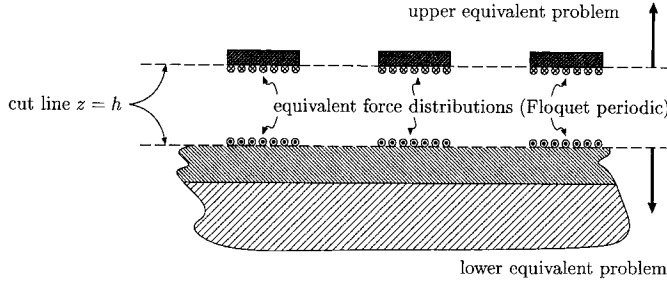


Fig. 2. Splitting the structure in two equivalent problems. Equivalent forces in the split plane represent the mechanical interaction between the two problems.

The regions $|x| \in]w/2, p/2[$ and $x \in]-w/2, w/2[$ characterize the free and the block-covered regions in the fundamental period, respectively.

For the analysis, we virtually cut the structure along $z = h$ to obtain two equivalent problems, where the interaction between the two is taken into account by oppositely directed but equally strong, $\pm y$ directed, “equivalent” surface force distributions in the block-covered regions of the cut planes (Fig. 2). These force distributions prescribe equal T_{yz} distributions in the cut plane of the two equivalent problems [in accordance with (3)]. The u_y distributions resulting from the impressed T_{yz} distributions in the two equivalent problems have to be equal in the block-covered regions, which completes the boundary condition (3).

A. Equivalent Problem for the Lower Half Space

The equivalent problem for the lower half space $z < h$ corresponds to the unloaded Love-wave waveguide excited by an impressed surface force distribution. Because the considered fields are Floquet-periodic, we can write the displacement $u_y(x)$ because of an impressed T_{yz} distribution in the cut plane $z = h$ as a convolution of a Floquet periodic Green’s function $G_p(x, k_0)$ [2], [3], [5] with the stress distribution in the fundamental period

$$u_y(x) = \int_{-\infty}^{+\infty} G_p(x - x', k_0) T_{yz}^0(x') dx'. \quad (4)$$

Here, and in the following, the superscript 0 indicates quantities in the fundamental period, and, for the sake of notational simplicity we use the convention that field quantities u_y and T_{yz} , are considered in the cut plane, $z = h$ if only one argument (x) is provided. For T_{yz}^0 we thus have $T_{yz}^0(x) = 0$ for $|x| > w/2$. The relationship with the T_{yz} distribution in the entire cut plane is given by

$$T_{yz}(x) = \sum_{n=-\infty}^{\infty} T_{yz}^0(x - np) \exp(-jnk_0p).$$

The Floquet-periodic Green’s function $G_p(x, k_0)$ is defined as the displacement u_y (in $z = h$) generated by a periodic

array of Floquet-periodic line forces creating a stress distribution $T_{yz}(x) = \sum_n \delta(x - np) \exp(-jnk_0p)$ in the plane $z = h$ of the unloaded structure [$\delta(x)$ denotes the Dirac delta function]. Because of the application of G_p , the resulting $u_y(x)$ includes the effects of the entire impressed stress distribution T_{yz} , where the boundary condition (2) has been considered as well.

B. Equivalent Problem for the Upper Half Space

In this case, a simple analytical solution for the fields in the block can be found in terms of a modal expansion. The fields of blocks in different periods are not coupled with each other, and, hence, it is sufficient to consider the fields in the fundamental period (T_{yz}^0 and u_y^0). We utilize the following modal functions for u_y ($n = 0, 1, 2, \dots$):

$$u_{y,n}(x, z) \propto \cos(k_{z,n}(z - h - t)) m_n(x), \quad (5)$$

where

$$m_n(x) = \begin{cases} \cos(x \frac{n\pi}{w}), & n = \text{even}, \\ \sin(x \frac{n\pi}{w}), & n = \text{odd}, \end{cases}$$

$$k_{z,n} = \sqrt{\frac{\omega^2 \rho_b}{\mu_b} - \left(\frac{n\pi}{w}\right)^2}.$$

Here, μ_b and ρ_b denote the shear modulus and the mass density of the block material, respectively. It can readily be verified that the corresponding stress tensor elements given by [8]

$$T_{yz} = \mu_b \frac{\partial u_y}{\partial z}, \quad T_{xy} = \mu_b \frac{\partial u_y}{\partial x}$$

fulfill the boundary conditions $T_{yz} = 0$ and $T_{xy} = 0$ at the block boundaries $z = h + t$ and $x = \pm w/2$, respectively. Using these modes, we can set up an expansion for T_{yz}^0 and u_y^0 in the cut plane $z = h$:

$$T_{yz}^0(x)|_{z=h} = \sum_{n=0}^{\infty} \tau_n m_n(x), \quad (6)$$

$$u_y^0(x)|_{z=h} = \sum_{n=0}^{\infty} \tau_n Z_n m_n(x). \quad (7)$$

τ_n are the expansion coefficients and

$$Z_n = \frac{\cot(k_{z,n}t)}{\mu_b k_{z,n}}$$

denotes the acoustic modal impedance giving the ratio u_y/T_{yz} at $z = h$ for mode n . Note that $k_{z,n}$ becomes imaginary from a certain value n onward; in this case, the trigonometric functions turn into the corresponding hyperbolic functions, and Z_n becomes purely imaginary. Truncating the previously mentioned modal expansion series would yield an approximation corresponding to a neglect of higher order modes.

C. *Joining the Equivalent Problems*

To join the field solutions, we have to match the T_{yx} distributions and the related u_y distributions in the cut plane, which formally corresponds to a problem in an infinite dimensional function space. To make the problem numerically accessible, we utilize a MoM approach and reduce the dimensionality of the function space by introducing a suitable approximation. This is done by expanding T_{yz}^0 into a finite sum of N rectangular pulse functions $P(x)$

$$T_{yz}^0(x) = \sum_{n=1}^N \alpha_n P(x - x_n), \tag{8}$$

where

$$P(x) = \begin{cases} 1, & |x| < w/(2N) \\ 0, & \text{elsewhere} \end{cases} \tag{9}$$

and

$$x_n = -w/2 + (n - 1/2)(w/N)$$

stands for the center point of pulse function number n . α_n are the expansion coefficients to be determined. The relationship of α_n with the expansion coefficients τ_n in (6) can simply be obtained by equating the right hand sides of (8) and (6), multiplying the resulting equation by

$P(x - x_m)$, and integrating with respect to x , which yields (using the orthogonality of the pulse functions $P(x - x_m)$)

$$\frac{w}{N} \alpha_m = A_{mn} \tau_n, \tag{10}$$

with

$$A_{mn} = \int_{-\infty}^{+\infty} P(x - x_m) m_n(x) dx.$$

Here and subsequently, we use Einstein's summation convention, which means that we sum over doubly occurring indices. The translation coefficients A_{mn} can be readily evaluated in closed form. It is near at hand to also truncate the modal expansion series (6) and (7) at $n = N - 1$, which makes the mapping (10) unique and invertible [A_{mn} then corresponds to a square matrix].

For matching the corresponding u_y distributions, we use a similar approach: equating the right-hand sides of (4) and (7), multiplying the so obtained equation with $P(x - x_m)$, and integrating with respect to x , we obtain

$$B_{mn} \alpha_n = A_{mn} Z_n \tau_n \tag{11}$$

with

$$B_{mn} = \int_{-\infty}^{+\infty} P(x - x_m) \int_{-\infty}^{+\infty} G_p(x - x', k_0) P(x - x_n) dx' dx. \tag{12}$$

We again note that it is sufficient to perform this matching in the fundamental period because we imposed Floquet-periodic fields by using G_p in (4). Once the matrix elements A_{mn} and B_{mn} have been determined, a homogeneous matrix equation can be derived from (10) and (11) by eliminating α_n :

$$\left(A_{mn} - \frac{N}{w} C_{mk} A_{kn} Z_n \right) \tau_n = 0 \tag{13}$$

where C is the inverse matrix of matrix B . To obtain a non-trivial solution for τ_n , the determinant of the system matrix in (13) has to vanish, which yields a condition for the Floquet wavenumber k_0 for a prescribed ω (or vice versa). The numerical search for zeros of this determinant yields the dispersion curve $k_0(\omega)$ for the Floquet modes in the structure.

III. COMPUTATIONAL PROCEDURE

The computational efficiency of this approach is mainly determined by the evaluation of the matrix elements B_{mn} . The expression for B_{mn} can be more conveniently calculated by introducing quantities in the spectral (Fourier) domain using the Fourier transform (spectral quantities are indicated by a tilde):

$$\text{FT}\{f(x)\} = \tilde{f}(\beta) = \int_{-\infty}^{+\infty} f(x) \exp(j\beta x) dx.$$

Using the convolution theorem and Parseval's theorem [9], we obtain

$$B_{mn} = \frac{1}{2\pi} \int_{-\infty}^{+\infty} |\tilde{P}(\beta)|^2 \tilde{G}_p(\beta, k_0) e^{-j\beta(x_m - x_n)} d\beta. \tag{14}$$

The Floquet-periodic Green's function in spectral domain, $\tilde{G}_p(\beta, k_0)$, can be simply given in terms of the associated "ordinary" (i.e., non-periodic) spectral Green's function $\tilde{G}(\beta)$ being sampled by a train of Dirac delta functions¹ [2]:

$$\tilde{G}_p(\beta, k_0) = \tilde{G}(\beta) \frac{2\pi}{p} \sum_{n=-\infty}^{\infty} \delta(\beta - k_0 - n \frac{2\pi}{p}). \tag{15}$$

The (non-periodic) spectral Green's function for the unloaded waveguide can be obtained by a straightforward analysis (similar to the one used for spectral electric Green's functions [10]) as

$$\tilde{G}(\beta) = \frac{1}{\beta_l \mu_l} \frac{\mu_s \alpha_s \tan(\beta_l h) + \mu_l \beta_l}{\mu_s \alpha_s - \mu_l \beta_l \tan(\beta_l h)} \tag{16}$$

¹The "ordinary" Green's function in spatial domain, $G(x)$, represents the fields $u_y(x)$ caused by a single, y -oriented unit line force at $x = 0$ and $z = h$.

where μ_s and μ_l denote the shear moduli of the substrate and the layer, respectively, and

$$\beta_l = \sqrt{\frac{\omega^2}{v_l^2} - \beta^2}, \quad \alpha_s = \begin{cases} \sqrt{\beta^2 - \frac{\omega^2}{v_s^2}}, & \beta^2 > \frac{\omega^2}{v_s^2} \\ j\sqrt{\frac{\omega^2}{v_s^2} - \beta^2}, & \beta^2 < \frac{\omega^2}{v_s^2} \end{cases}. \quad (17)$$

v_s and v_l denote the bulk shear velocities in the layer and the substrate material, respectively. Using (15) in (14) and considering the sampling property of the delta function, we finally arrive at

$$B_{mn} = \frac{1}{p} \sum_{k=-\infty}^{+\infty} |\tilde{P}(\beta_k)|^2 \tilde{G}(\beta_k) e^{-j\beta_k(x_m-x_n)} \quad (18)$$

where $\beta_k = k_0 + k \cdot 2\pi/p$. This series has to be truncated for numerical evaluation and can be effectively evaluated using an FFT if the number of considered series elements K equals a power of two. We can truncate the series as (using the abbreviation $f_k = |\tilde{P}(\beta_k)|^2 \tilde{G}(\beta_k)$)

$$B_{mn} \approx e^{-jk_0(x_m-x_n)} \sum_{k=-K/2}^{K/2-1} f_k e^{-jk \frac{2\pi}{p}(x_m-x_n)} = e^{-jk_0(x_m-x_n)} e^{j\pi\hat{x}} \sum_{k=0}^{K-1} f_{k-K/2} e^{-j \frac{2\pi}{K} k\hat{x}}$$

where the second sum representation has been obtained shifting the index variable k and using the definition

$$\hat{x} = (x_m - x_n) \frac{K}{p}. \quad (19)$$

This second sum represents the discrete Fourier transform $f_{k-K/2}$ provided that \hat{x} is interpreted as a discrete variable. A discrete Fourier transform can be evaluated effectively using the FFT algorithm [11], which then yields the sum for discrete values $\hat{x} = 0, 1, \dots, K-1$. Because of the periodicity property of the FFT, results for negative values of \hat{x} are equal to those for $K - \hat{x}$. Hence, utilizing a single FFT run, we obtain approximations for B_{mn} for a series of discrete $(x_m - x_n)$ values being equally spaced by p/K [see (19)]. Depending on the geometrical ratio w/p , it is often possible to choose the number of expansion functions N appropriately such that the actually needed spacing for the $(x_m - x_n)$ values, w/N , is an integer multiple of the spacing p/K provided by the FFT result. If that is the case, the needed B_{mn} elements are directly contained in the FFT output; otherwise, a simple interpolation procedure can be used to obtain the values for the desired relative distances $(x_m - x_n)$ from those that are delivered by the FFT [B_{mn} is a smooth function in $(x_m - x_n)$].

We remark that one could, in principle, also directly use the truncated modal series (6) and (7) as approximations for the interface distributions (without introducing the rectangular pulse approximation (8)). In that case, however, we could not evaluate the resulting B_{mn} elements using the FFT approach because the shape of the

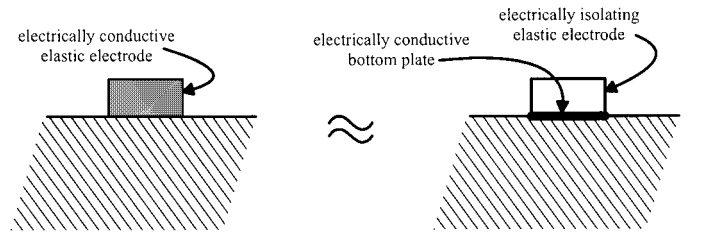


Fig. 3. Approximating a conducting electrode by a non-conductive one with conducting bottom.

expansion functions would vary and the used rectangular expansion functions differ only in their center position, which makes B_{mn} a function of the relative center distance $(x_m - x_n)$ [see (14)].

Finally, we note that the electric interaction in case of a piezoelectric substrate and electrically conducting blocks (electrodes) can be taken into account by using a set of Green's functions including piezoelectricity and thus, taking electromechanic interaction into account also. The conductive electrode can be modeled effectively as an elastic block featuring a perfectly conducting bottom but being otherwise electrically isolating (Fig. 3). Thus, electric charges appear at the electrically conducting bottom of the electrode only. These charges can be expanded similar to the stress distribution, and the corresponding electric boundary condition is given by requiring constant electric potential on the electrode bottom. This model generally represents a very good approximation and is discussed in [4] where a combined MoM/Finite-Element method has been introduced. For non-conductive but dielectric blocks, the simplest approach would be to neglect the contribution of the electric perturbation introduced by the blocks, which also represents a reasonable approximation (especially for low-coupling substrates such as quartz).

IV. NUMERICAL RESULTS

To illustrate the applicability of the approach, we calculated the dispersion diagram $k_0 = k_0(\omega)$ for a waveguide with an ST quartz substrate that is covered with a fused quartz layer. The ST-quartz substrate is modeled by an isotropic material with a mass density $\rho_s = 2650 \text{ kg/m}^3$ and a shear velocity $v_s = \sqrt{\mu_s/\rho_s} = 5060 \text{ m/s}$. For the layer material, we have $\rho_l = 2200 \text{ kg/m}^3$, $v_l = 3766 \text{ m/s}$. Calculations have been performed for gold ($\rho_b = 19300 \text{ kg/m}^3$, $v_b = 1245 \text{ m/s}$) and aluminum ($\rho_b = 2700 \text{ kg/m}^3$, $v_b = 3109 \text{ m/s}$) as block material.

Fig. 4 shows the dispersion characteristics for this structure. The width of the blocks was chosen such that they cover $1/8$ of the period: $w = 0.125 p$. The dispersion curve for the free surface and curves for different relative block heights t/p are shown in the vicinity of the boundary of the first Brillouin zone $k_0 = \pi/p$ [1] where a characteristic stop band occurs.

The shift of the center of the stopband with respect to the free surface dispersion curve ($\Delta\omega_c$) indicates the re-

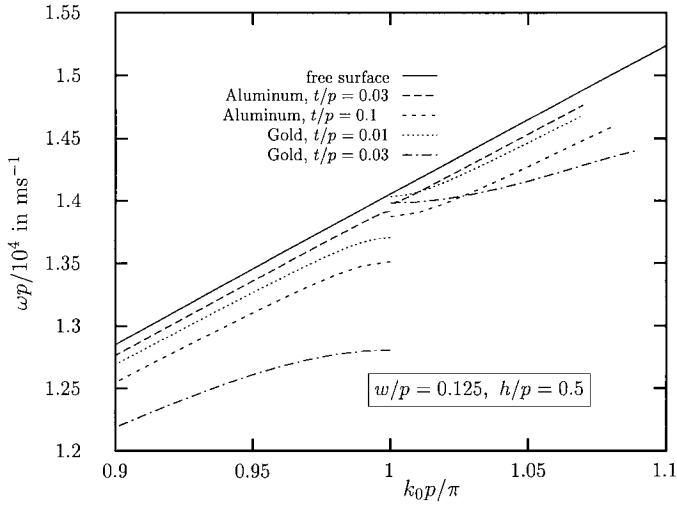


Fig. 4. Dispersion curves giving angular frequency ω vs the scaled Floquet wavenumber k_0p/π .

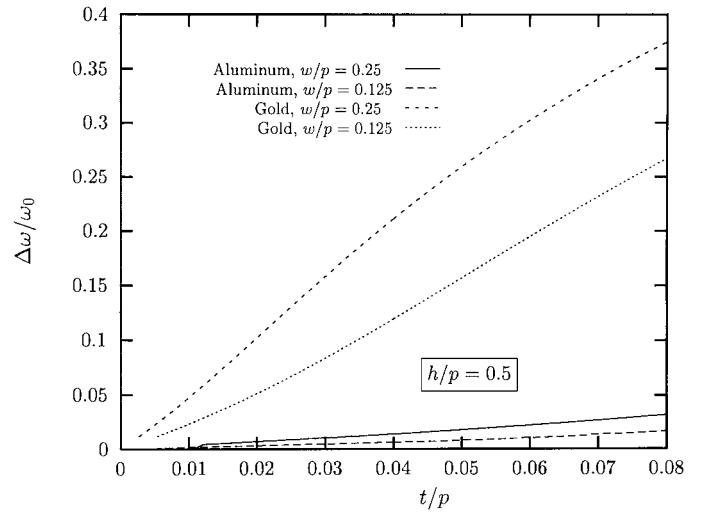


Fig. 6. Relative band gap $\Delta\omega/\omega_0$ vs relative block height t/p .

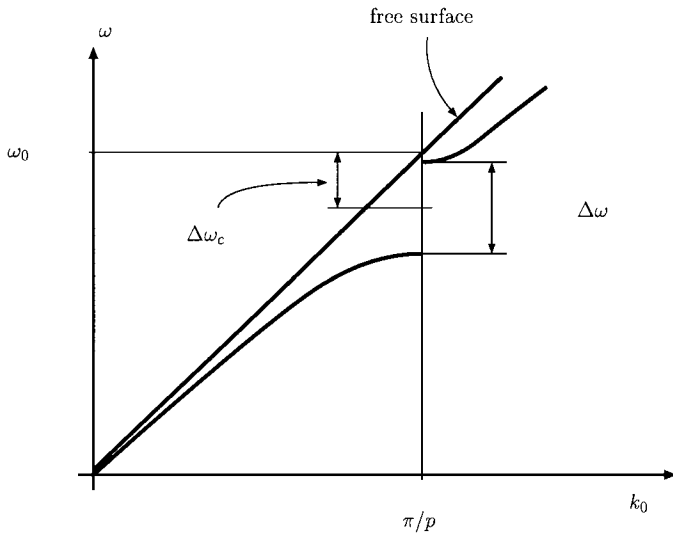


Fig. 5. Definition of band gap $\Delta\omega$ in the dispersion curve.

duction of the effective wave velocity compared with the unloaded case. The width of the stop band $\Delta\omega$ is a characteristic measure of the degree of the mechanical reflections caused by the blocks. These parameters can be used in a COM description of the periodic structure (see, e.g., [1], [5], [12], [13]). According to the COM theory, the expression $\pi\Delta\omega/2\omega_0$ can be interpreted as the reflection coefficient ρ for a single block (Fig. Fig. 5). This value can be used in the design of reflector arrays; a periodic arrangement of N reflecting strips yields a total reflection coefficient of $R = \tanh(N\rho)$ at the center frequency of the reflector [14].

It can be seen that, because of the much higher mass density, the gold blocks lead to larger band gaps compared with aluminum blocks. Note that the band gaps for gold and aluminum show about the same size for the cases $t/p = 0.01$ for gold and $t/p = 0.1$ for aluminum, which

corresponds to a difference in height by a factor of ten. This value reflects the difference in the mass densities for the two materials. The upper branches of the curves stop at certain points. Above those end points, the mode becomes damped because of leaky wave excitation in the substrate [1].

Fig. 6 shows the relative band gap width for two different widths w as a function of the block height t . We observe the effect that the band gap (corresponding to the reflection coefficient) increases for increasing electrode width. Again, the effect is roughly a factor ten greater for the gold blocks. Furthermore, the band gap increases for increasing block width, as can be seen by comparing the curves for different block widths.

V. CONCLUSIONS

We presented a numerical approach based on a hybrid MoM/Mode-Matching technique for the analysis of periodically loaded waveguides. The method has been outlined by considering the propagation of Love waves in a waveguide with periodic mass-loading. With appropriate modifications, the method is also applicable to other kinds of acoustic wave types. High computational efficiency has been achieved by utilizing the FFT for the calculation of the needed MoM interaction elements. As an example, we presented Brillouin dispersion diagrams that have been calculated for a sample structure. The results can be utilized to extract COM parameters for the structure.

ACKNOWLEDGMENTS

The authors thank Dr. Adrian Venema for many stimulating discussions and useful suggestions.

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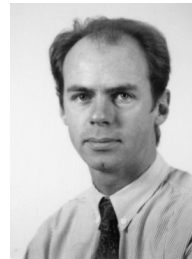


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