

FIXED DISCS IN QUASI-METRIC SPACES

HASSEN AYDI*, NIHAL TAŞ**, NIHAL YILMAZ ÖZGÜR*** AND NABIL MLAIKI****

*Nonlinear Analysis Research Group, Ton Duc Thang University, Ho Chi Minh City, Vietnam
Faculty of Mathematics and Statistics, Ton Duc Thang University, Ho Chi Minh City, Vietnam
Université de Sousse, Institut Supérieur d'Informatique et des Techniques de Communication,
H. Sousse 4000, Tunisia

China Medical University Hospital, China Medical University, Taichung 40402, Taiwan
E-mail: hassen.aydi@tdtu.edu.vn

**Balıkesir University, Department of Mathematics, 10145 Balıkesir, Turkey
E-mail: nihaltas@balikesir.edu.tr

***Balıkesir University, Department of Mathematics, 10145 Balıkesir, Turkey
E-mail: nihal@balikesir.edu.tr

****Prince Sultan University, Department of Mathematics and General Sciences,
11586 Riyadh, Saudi Arabia
E-mail: nmlaiki@psu.edu.sa; nmlaiki2012@gmail.com

Abstract. In this paper, we present some results of fixed disc and common fixed disc in quasi-metric spaces, under some very interesting contractions. Obtained results are supported by illustrative examples.

Key Words and Phrases: Fixed disc, common fixed disc, quasi-metric space, contraction.

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