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# Flat bands and emergent ferromagnetic ordering in $\text{Fe}_3\text{Sn}_2$ kagome lattices

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A flat band representing a highly degenerate and dispersionless manifold state of electrons may offer unique opportunities for emergence of exotic quantum phases. To date, definitive experimental demonstrations of flat bands remain to be accomplished in realistic materials. Here we present the first experimental observation of a striking flat band near the Fermi level in the layered  $\text{Fe}_3\text{Sn}_2$  crystal consisting of two Fe kagome lattices separated by an Sn spacing layer. The band flatness is attributed to the local destructive interferences of Bloch wave functions within the kagome lattices, as confirmed through theoretical calculations and modelings. We also establish high temperature ferromagnetic ordering in the system, and interpret the observed collective phenomenon as a consequence from the synergetic effect of electron correlation and the peculiar lattice geometry. Specifically, local spin moments formed by intramolecular exchange interaction are ferromagnetically coupled through a unique network of the hexagonal units in the kagome lattice. Our findings have important implications to exploit emergent flat-band physics in special lattice geometries.

In electronic band theory, the band structures of solids are determined by solving the one-electron Schrödinger equation for electrons in the periodic potential of the lattice [1]. The creation of various nontrivial band structures has been exploited by proper design of the lattice structures. For example, Dirac bands with linear dispersion are realized in the honeycomb lattice [2–4]. Contrasting with this linear Dirac band hosting massless quasiparticles, the dispersionless flat bands render electrons super heavy due to their localization [5–8]. In such flat bands, the kinetic energy of electrons is very quenched, while their mutual Coulomb repulsions prevail. Due to their intriguing electronic features, flat bands have been exploited to develop various emergent effects, including ferromagnetism [5–8], high-temperature fractional quantum Hall effect [9–12], Wigner crystallization [13], Bose-Einstein condensation [14], and high-temperature superconductivity [15, 16].

In principle, flat bands can be constructed by a delicate design of the lattice geometry that produces the destructive interference of Bloch wave functions [5–20]. Specifically, several lattice geometries have been proposed to generate flat bands [5–20], such as the kagome [5–7], side-centered square [8], and checkerboard [10] lattices.

In the kagome lattice composed of interlaced triangles where each lattice point interconnects two neighboring hexagons, self-localization of the electron wave functions can be realized by the destructive interference around each hexagon [19], as depicted in Fig. 1a, thereby leading to a dispersionless flat band. So far, despite many predicted intriguing physical aspects of such lattice-induced flat bands [5–20], flat bands have only been observed in artificially engineered systems such as assemblies of judiciously placed atoms on a two-dimensional (2D) surface and cold atomic systems [21–23]. The experimental observations of flat bands and their exotic electronic properties are still challenging in natural solid state materials. In the present study, we demonstrate how flat bands and ferromagnetism can be naturally materialized in a realistic layered 2D kagome compound,  $\text{Fe}_3\text{Sn}_2$ .

As shown in Figs. 1(b) and 1(c), the structure of  $\text{Fe}_3\text{Sn}_2$  is composed of two Fe-Sn layers separated by an Sn spacing layer, where the Fe atoms in each Fe-Sn layer form a kagome lattice [24]. The grown  $\text{Fe}_3\text{Sn}_2$  single crystal shows a hexagonal shape, whose lateral size amounts to about 3 mm: The X-ray diffraction (XRD) pattern (Fig. S1 in the Supplemental Material (SM) [25]) [24] and cross-sectional transmission electron microscopy (TEM)

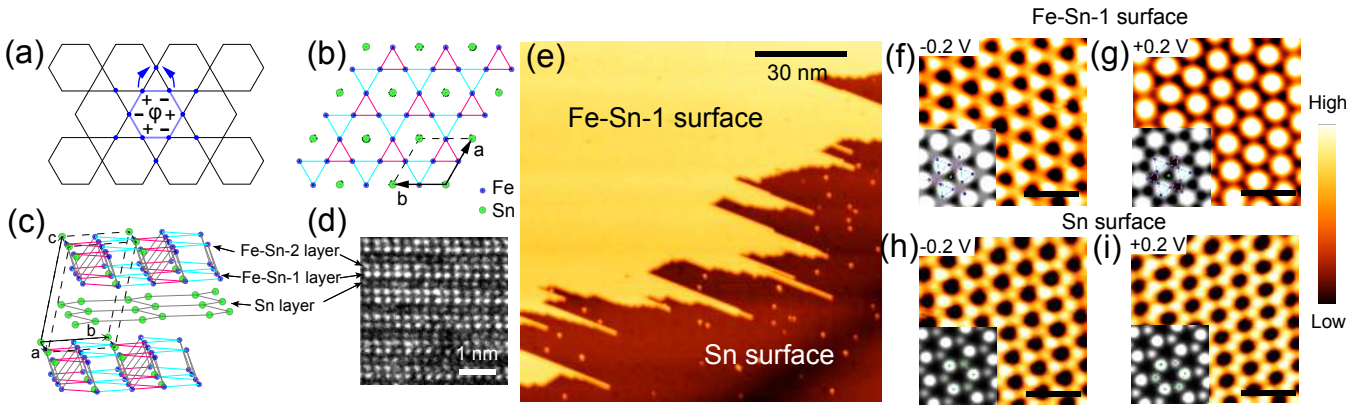


FIG. 1. Structural characterization of the  $\text{Fe}_3\text{Sn}_2$  bulk and surface. (a) Schematic diagram of wave function self-localization on the hexagons in the kagome lattice: Due to the special structure of the Kagome lattice, the wave function alternates its sign around the six vertices in each hexagon, leading to destructive interference outside of the hexagon and therefore electrons locally circulating around each hexagon. (b),(c) Top and perspective views of the optimized structure of bulk  $\text{Fe}_3\text{Sn}_2$ . The bond lengths in the red- and cyan-colored triangles are 2.54 and 2.77 Å, respectively. Three different layers are denoted as Fe-Sn-1, Fe-Sn-2 and Sn, respectively. (d) Cross-sectional TEM image with the atomic resolution of three different layers. (e) Large-scale STM image of a cleaved  $\text{Fe}_3\text{Sn}_2$  surface with two different surface layers. The sample bias was  $V_s = 0.4$  V. (f)-(i) Atomic-resolution STM images taken at  $V_s = 0.2$  V and  $-0.2$  V on the two different surface layers. The scale bars in (f-i) are 1 nm. The corresponding simulated STM images for the two surface layers are also given in the insets.

image (Fig. 1d) validate the high crystalline quality, and also reveal that the sample surface is parallel to the Fe-Sn layers.

Because of the layered structure of  $\text{Fe}_3\text{Sn}_2$ , there are three possible terminations at the surface [see Fig. 1(c)]: the Sn layer, the first Fe-Sn layer (hereafter denoted as Fe-Sn-1 layer) and the second Fe-Sn layer (Fe-Sn-2 layer). Figure 1(e) and Fig. S2(a) in the SM [25] show the large-scale scanning tunneling microscopy (STM) images, while Fig. S2(b) in the SM [25] displays the STM height profile, clearly demonstrating that the cleaved surface is composed of two different surface layers. In order to distinguish the structures of the two observed surface layers, we obtained zoom-in STM images at sample biases ( $V_s$ ) of  $-0.2$  V and  $0.2$  V [see Figs. 1(f)-1(i)]. It is found that the STM images [Figs. 1(f) and 1(g)] for the upper surface layer show bias-dependent features: i.e., buckled honeycomb pattern and hexagonally close packed bright spots at  $-0.2$  and  $0.2$  V, respectively. Meanwhile, the STM images for the lower surface layer [Figs. 1(h) and 1(i)] show a similar honeycomb pattern at both biases.

It is noted that the STM images mainly reflect the spatial variation of the local density of states (LDOS) at the surface, instead of a direct imaging of the surface atomic structure [33]. Therefore, it is usually difficult to determine the surface structure only from the experimental STM images, especially when the spatial distribution of the LDOS deviates from the atomic structure. In such cases, combinations of the experimental STM images and simulation ones is a powerful approach and has been widely adopted to identify the surface structures [34]. Therefore, to identify the two observed surface lay-

ers, we simulated the STM images of all three possible surface structures using the Tersoff-Hamann approximation [35, 36] (see more details in the “First-principles calculations” section of the SM [25]). The results for the Fe-Sn-1 and Sn structures are displayed in the insets of Figs. 1(f)-1(i), while that for the Fe-Sn-2 structure in Fig. S3 in the SM [25]. For the Fe-Sn-1 surface, the simulated filled- and empty-state STM images show strongly buckled honeycomb pattern and hexagonally close packed bright protrusions, respectively, arising from the two types of Fe triangles with different Fe-Fe bond lengths [see Fig. 1(b)]. On the other hand, for the Sn surface, the simulated filled- and empty-state STM images show a honeycomb pattern with three bright and three less-bright protrusions, representing a buckled honeycomb lattice of Sn. Here, the height difference between the buckled surface Sn atoms is calculated to be 0.152 Å. These features of the simulated STM images of the Fe-Sn-1 and Sn surface structures agree well with those of the experimental images [see Figs. 1(f)-1(i)]. Therefore, we conclude that the two observed surface layers are the Fe-Sn-1 and Sn layers. It is noted that the simulated STM images of the Fe-Sn-2 surface have similar patterns as those of Fe-Sn-1. However, the STM height-profile measurement at  $0.2$  V shows that the layers with hexagonally close packed bright spots are positioned at  $\sim 2$  Å higher or  $\sim 4$  Å lower than the other layer with the honeycomb pattern [see Fig. S2(b) in the SM [25]]. This result unambiguously indicates that the former layer is Fe-Sn-1, rather than Fe-Sn-2. Moreover, density-functional theory (DFT) total-energy calculations demonstrate that the order of the thermodynamic stability is  $\text{Sn} > \text{Fe-Sn-1}$

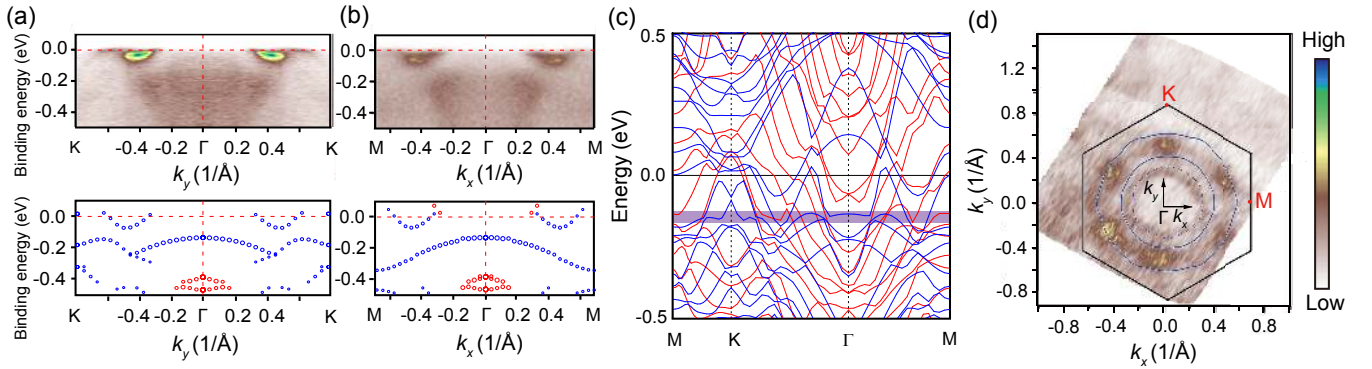


FIG. 2. Electronic band structure of the  $\text{Fe}_3\text{Sn}_2$  surface. (a),(b) (Top) ARPES results along the  $\Gamma$ -K and  $\Gamma$ -M lines, respectively. (Bottom) Calculated spin-polarized bands projected on to the top few layers of the Fe-Sn-1 surface structure. Here, the majority (minority) spin bands are drawn with the red (blue) circles whose sizes are proportional to the weights of the projected electrons. (c) Calculated spin-polarized band structure for the Fe-Sn-1 surface structure. Here the Fermi level  $E_F$  is set at zero energy, and the purple shaded stripe highlights the nearly-fat bands close to -0.2 eV. (d) Photoemission intensity map at the Fermi level superimposed with the calculated Fermi surfaces for the Fe-Sn-1 (solid circles) and Sn (dashed circle) surfaces.

> Fe-Sn-2 over a wide range of the Sn chemical potential (see Fig. S4 and more discussions in the SM [25]), consistent with the experimental observations of Sn and Fe-Sn-1. It is most likely that the Fe-Sn-2 surface layer decomposes during or very shortly after the cleaving process, because the cleavage temperature of about 80 K is not low enough to prevent the lattice relaxation. Indeed, high-density bright spots are clearly observed on the Sn surface [see Fig. 1(e) and Fig. S2(a) in the SM [25]], which could be the residues of the Fe-Sn-2 decomposition.

Next, we measured the low-energy electronic structure of the  $\text{Fe}_3\text{Sn}_2$  surface by angle-resolved photoemission spectroscopy (ARPES). Strikingly, the ARPES data along the  $\Gamma$ -K and  $\Gamma$ -M lines reveal a nearly dispersionless flat band at  $\sim 0.2$  eV below  $E_F$  [see Figs. 2(a) and 2(b)]. The presence of such a flat band can be more apparently seen in the second derivative ARPES data (see Fig. S5 in the SM [25]). Here, the flat dispersion extends more than half of the  $\Gamma$ -K and  $\Gamma$ -M lines. To quantitatively understand the observed flat band, we calculated the band structures for the bulk, Fe-Sn-1 and Sn surface structures. Their spin-polarized band structures are displayed in Fig. S6 in the SM [25] and Fig. 2(c), respectively, showing partially flat dispersions of some bands around  $\sim 0.2$  eV below  $E_F$ .

Since the ARPES measurement with photon energy of 35 eV is highly surface-sensitive, we projected the calculated bands on to the atoms near the surface up to the third subsurface layers to compare with the ARPES data. As shown in Figs. 2(a) and 2(b), the bands localized near the Fe-Sn-1 surface are in reasonably good agreement with the ARPES data. In particular, there exist narrow bands at  $\sim 0.2$  eV below  $E_F$  as well as the electron pockets along the  $\Gamma$ -K and  $\Gamma$ -M lines, consistent

with the ARPES measurements [see Figs. 2(a), 2(b), 2(d), and more discussions in the SM [25]]. Meanwhile, the surface-localized states at the Sn surface are much reduced in their intensity compared to the Fe-Sn-1 surface (Fig. S7 in the SM [25]), because the states originating from the Sn atoms are relatively weaker near  $E_F$ , as shown in Fig. S8 in the SM [25]. Therefore, the Sn surface states are likely too weak to be visible in ARPES, and the flat band observed near  $E_F$  is originated mostly from the Fe-Sn-1 surface.

There are some weak fuzzy features below the observed flat band in the experimental ARPES result [Fig. 2(a)], which may originate from the strongly dispersive bands farther away from the surface, as shown in the calculated band structure of the Fe-Sn-1 surface structure [Fig. 2(c)].

Using STM, we also obtained differential conductance ( $dI/dV$ ) spectra along the blue line on the Fe-Sn-1 surface [see Fig. 3(a)]. All the  $dI/dV$  spectra reflecting the local density of states (DOS) show a prominent peak at  $\sim -0.2$  V, due to the flat band observed by ARPES. As shown in Fig. 3(b), the charge character of the flat-band state at  $\sim 0.2$  eV below  $E_F$  represents quasilocated electrons originating from the Fe atoms, which encircle the hexagonal cells in the kagome lattice.

It is noteworthy that the ARPES spectra of  $\text{Fe}_3\text{Sn}_2$  show not only the strong intensity around the  $\Gamma$  point at  $\sim 0.2$  eV below  $E_F$ , but also a limitation of the band flatness within a finite region of the Brillouin zone. This feature deviates from that obtained using a single-orbital tight-binding model for the ideal 2D kagome lattice, where a perfectly flat band extends over the whole Brillouin zone [5–7, 19]. Figure 3(b) shows the charge character of the flat-band state, indicating a strong hybridization between Fe-Sn-1 and Fe-Sn-2 layers. Physically, such

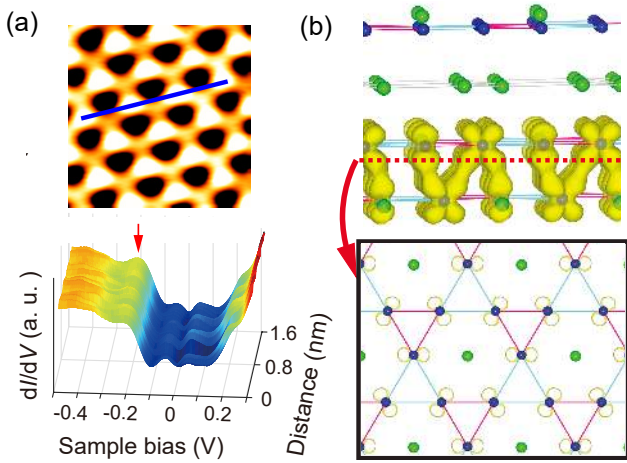


FIG. 3. Scanning tunneling spectroscopy of the Fe-Sn-1 surface. (a) Differential conductance ( $dI/dV$  spectra) scan (bottom) along the blue line on the STM image obtained at  $V_s = -0.2$  V (top). (b) (Top) Calculated charge character of the flat-band state at the  $\Gamma$  point obtained from the Fe-Sn-1 surface structure. Here, the charge density distribution is drawn with an isosurface of  $0.004 e/\text{bohr}^3$ . (Bottom) A cross-section view drawn parallel to the Fe-Sn layers.

interlayer hybridization associated with the multi  $d$  orbitals of Fe atoms is likely to violate the precise destructive interference of Bloch electrons, leading to weakened band flatness observed in  $\text{Fe}_3\text{Sn}_2$ . Based on these understandings, we develop a simple bilayer tight-binding model to explore the band evolution upon the strength of interlayer coupling (see details in the SM [25]). As depicted in Fig. S9(a) of the SM [25], bilayer kagome lattice belongs to the point group  $D_{3d}$  containing the symmetry operations of a three-fold rotation around the  $z$ -axis, inversion, and mirror reflection with respect to  $yz$ -plane. The calculated tight-binding band structures are shown in Figs. S9(b) and S9(c) of the SM [25], which unambiguously demonstrate that the interlayer coupling weakens the band flatness.

Long-range ferromagnetic order has been previously observed in  $\text{Fe}_3\text{Sn}_2$  [37–39]. Here we also observed the ferromagnetic behaviors with a saturation magnetic moment of about  $1.94 \mu_B$  per Fe atom at 2 K [Fig. 4(a)] and a Curie temperature  $T_c$  of  $\sim 610$  K [Fig. 4(b)], consistent with previous experiments [37–39]. Moreover, we performed magnetic force microscopy (MFM) measurements [40] (see more details in the SM [25]), which is more sensitive to surface magnetization. A striped magnetic domain pattern is clearly seen in Figs. S10(b) and S10(c) of the SM [25], further demonstrating the presence of long-range ferromagnetic order near the surface. It is noteworthy that the calculated surface band structure and simulated STM images of the nonmagnetic state of  $\text{Fe}_3\text{Sn}_2$  (see Figs. S11 and S12 in the SM [25]) substantially deviate from the experimental ARPES and STM results.

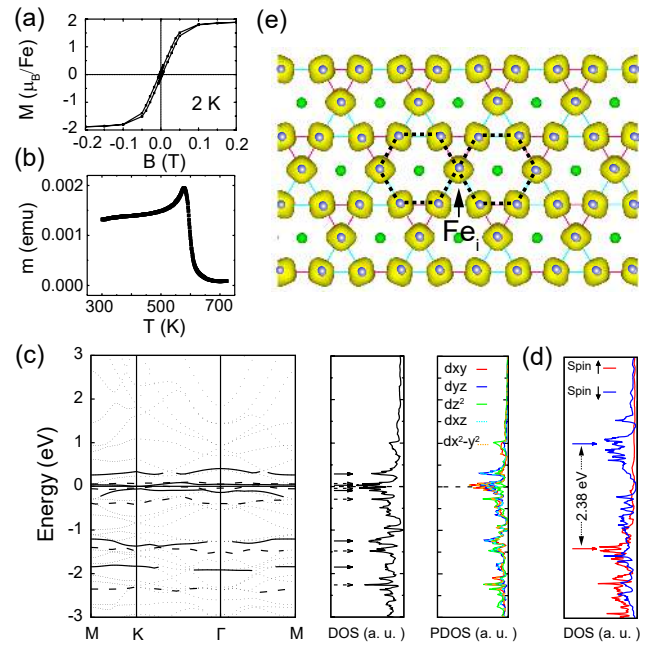


FIG. 4. Ferromagnetic order of  $\text{Fe}_3\text{Sn}_2$ . (a),(b) Hysteresis loop (obtained at 2 K) and temperature-dependent magnetic moment (applied field of 100 Oe) of an  $\text{Fe}_3\text{Sn}_2$  single crystal, respectively. Here, the magnetic field is applied parallel to the Fe-Sn layers. (c) Calculated band structure, DOS, and partial DOS for the nonmagnetic state of bulk  $\text{Fe}_3\text{Sn}_2$ . The ten flat bands with dispersion smaller than 0.2 eV are drawn by solid or heavy dashed lines. (d) Calculated DOS for the ferromagnetic state of bulk  $\text{Fe}_3\text{Sn}_2$ . (e) Spin density distribution of the ferromagnetic state. The spin density distribution is drawn with an isosurface of  $0.01 e/\text{bohr}^3$ .

Therefore, we can say that the presence of long-range ferromagnetic order is unambiguously validated even on the surface of  $\text{Fe}_3\text{Sn}_2$ .

The mechanism of such strong ferromagnetism in  $\text{Fe}_3\text{Sn}_2$ , however, still remains open. Earlier theoretical studies reported that the extremely high degeneracy inherently associated with flat bands would naturally give rise to ferromagnetism when taking into account nonvanishing on-site Coulomb interaction [5–8]. In order to reveal the microscopic nature of the flat-band ferromagnetism in  $\text{Fe}_3\text{Sn}_2$ , we calculated the band structure and partial DOS for the nonmagnetic bulk. We find that the DOS around the Fermi level mainly arise from the  $d$  orbitals of the Fe atoms [see Fig. 4(c)]. Here, the trigonal crystal field splits the five  $d$  orbitals into three categories, namely,  $d_{z^2}$ ,  $d_{xz, yz}$ , and  $d_{xy, x^2-y^2}$ , the partial DOS of which are drawn in different colored lines. Since all the  $d$  orbitals participate in hopping within the present bilayer kagome lattice, we expect ten flat bands in bulk  $\text{Fe}_3\text{Sn}_2$ , which can be identified from their narrow band dispersions and high DOS peaks [see Fig. 4(c)]. In particular, there are several nearly flat bands near  $E_F$ . Consequently, such high degenerate electronic states are

mostly susceptible to the ferromagnetic order even with a tiny on-site Coulomb interaction [5–8]. The present DFT calculations indeed confirm that the ferromagnetic configuration is more energetically stable than the non-magnetic one by 2.18 eV per unit cell. Figure 4(d) displays the spin-polarized DOS, showing a splitting of  $\sim 2.4$  eV between the majority- and minority-spin bands [see Fig. S6(a) in the SM [25]]. The calculated magnetic moment of  $2.04 \mu_B/\text{Fe}$  for bulk  $\text{Fe}_3\text{Sn}_2$  is close to the experimentally measured value of  $1.94 \mu_B/\text{Fe}$  at 2 K [see Fig. 4(a)].

So far we have shown that  $\text{Fe}_3\text{Sn}_2$  has two remarkable aspects: i.e., flat bands of localized electrons and a long-range ferromagnetic ordering over the kagome lattice. Both aspects are attributed to the geometric character of the kagome lattice, which produces not only the destructive interferences of Bloch wave functions but also a mutually interconnecting network of hexagonal cells through the Fe atoms, i.e.,  $\text{Fe}_i$  in Fig. 4(e). Thus,  $\text{Fe}_3\text{Sn}_2$  can possess the local spin polarization due to the intramolecular exchange of localized electrons around each hexagon, and such spin moments are in turn coupled with each other via the intermolecular correlation. In the present system, we note that the Stoner parameter  $I$  is equivalent to the effective on-site Coulomb interaction  $U$  within the hexagonal cell [41]. For bulk  $\text{Fe}_3\text{Sn}_2$ ,  $I$  is roughly 1.15 eV, estimated from dividing the exchange splitting by the magnetic moment [42, 43]. It is noticeable that the Hubbard model on the kagome lattice has offered the two mechanisms for ferromagnetism: one is Mielke’s flat-band ferromagnetism [5–7] that is an extreme case of the Stoner instability [44] reducing the potential energy of repulsive electron-electron interactions and the other is Nakaoka-type ferromagnetism [45] due to the gain in the kinetic energy of electrons [46]. Interestingly, our DFT calculations demonstrate that the present system possesses the two aspects of ferromagnetism, including not only a large value of on-site  $U$  and the high DOS at the Fermi level caused by the self-trapping effect in kagome lattices but also the nearest-neighbor hopping due to the above-mentioned interconnecting lattice networks. Therefore, the observed high-temperature ferromagnetism would be attributed to the synergetic effects of the potential and kinetic energies in the kagome lattice, which is distinct from the itinerant ferromagnetism of other 3d transition metal compounds.

In summary, the present study has demonstrated for the first time the presence of flat bands in the realistic quasi-2D kagome compound of  $\text{Fe}_3\text{Sn}_2$ , and further revealed that the flat bands attain the local spin polarization caused by an intramolecular exchange interaction as well as the long-range ferromagnetic order through a unique network of the hexagonal cells. This intriguing feature of flat-band ferromagnetism in the quasi-2D kagome lattice is quite distinctly contrasted with the recently observed ferromagnetism in 2D van der Waals crys-

tals, where magnetic atoms are ferromagnetically coupled with the interelectronic exchange  $J$  [47, 48]. Further control of the flat-band electronic structures, for example via charge doping, may enable realization of other versatile quantum phenomena [5–20].

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