Flexo-photovoltaic effect

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It is highly desirable to discover photovoltaic mechanisms that enable a higher efficiency of solar cells. Here, we report that the bulk photovoltaic effect, which is free from the thermodynamic Shockley-Queisser limit but usually manifested only in noncentrosymmetric (piezoelectric or ferroelectric) materials, can be realized in any semiconductor, including silicon, by mediation of flexoelectric effect. We introduce strain gradients using either an atomic force microscope or a micron-scale indentation system, creating giant photovoltaic currents from centrosymmetric single crystals of SrTiO$_3$, TiO$_2$, and Si. This strain-gradient-induced bulk photovoltaic effect, which we call the flexo-photovoltaic effect, functions in the absence of a $p$–$n$ junction. This finding may extend present solar cell technologies by boosting the solar energy conversion efficiency from a wide pool of established semiconductors.

Since its first observation in the nineteenth century, the photovoltaic (PV) effect has been studied intensively for scientific interest and as a sustainable energy source to replace fossil fuels and reduce carbon emissions (1–3). In 1954, the first high-power modern silicon solar cells were invented in which the photoexcited carriers were separated by a built-in electrical field developed at a $p$–$n$ junction (4). By virtue of the appropriate bandgap energies of the semiconductors in a $p$–$n$ junction solar cell, sunlight is efficiently absorbed, resulting in considerable power conversion efficiency. Nowadays, silicon PV cells are the mainstay of the modern solar industry, contributing more than 1% of global electricity supply. Nevertheless, PV cells based on $p$–$n$ junctions have a photovoltage limited by the bandgap energy of the constituent semiconductors and an ultimate efficiency constrained by the Shockley-Queisser (S-Q) limit (5).

The ferroelectric materials exhibit a photovoltaic effect distinct from that of $p$–$n$ junctions, called the bulk photovoltaic (BPV) effect (6, 7). Under uniform illumination, a homogeneous ferroelectric material gives rise to a current under zero bias (short-circuit current; $I_{sc}$) that depends on the polarization state of the incident light and produces an anomalously large photovoltage well exceeding its bandgap energy. This peculiar PV effect originates from the asymmetric distribution of photoexcited nonequilibrium carriers in $k$-space caused by the absence of centrosymmetry in the material (7). Owing to its distinctive charge separation mechanism, solar cells based on the BPV effect can in principle exceed the S-Q limit (8). However, a substantial BPV effect is generally found in wide-bandgap noncentrosymmetric materials, such as ferroelectric BaTiO$_3$ (8) and BiFeO$_3$ (9), leading to an overall extremely low device efficiency under solar illumination. Hence, one way to enhance the efficiency may be to realize the BPV effect in semiconductors with more favorable bandgaps, regardless of their crystalline symmetry.

Flexoelectricity is an electromechanical property that reflects a coupling between an electric polarization and a strain gradient (10, 11). In centrosymmetric materials, a strain gradient breaks its inversion symmetry, resulting in a polarization with a preferred direction and enabling a piezoelectric composite containing no piezoelectric elements (11, 12). Likewise, one can hypothesize that a strain gradient allows the manifestation of the BPV effect in materials that are originally centrosymmetric. Here, we propose and demonstrate that the BPV effect can be induced in any semiconductor by mediation of the flexoelectric effect. Given that flexoelectricity is a universal property of all materials, ranging from biomaterials (13) to semiconductors and dielectrics (14) to 2D materials such as graphene (15), this strain-gradient-induced BPV effect, termed here the flexo-photovoltaic (FPV) effect, is allowed for all symmetry classes. Thus, the devices based on the FPV effect can be fabricated with silicon or any other semiconductors.

To demonstrate our idea, we explored the PV effect induced by a point force exerted onto the surface of centrosymmetric materials including a SrTiO$_3$ single crystal and a rutile TiO$_2$ single crystal (see section S1 of (16)). The point force was exerted by the tip of an atomic force microscope (AFM), inducing local inhomogeneous strain at the tip/surface contact area and, therefore, a local breaking of centrosymmetry (17, 18). In our experiments, we used a custom-made photoelectric atomic force microscope (Ph-AFM) consisting of an AFM-based system equipped with a customized current amplifier/filter system and an optical system (19). The optical system allows us to illuminate a sample surface with a 405-nm...
laser properly polarized by a half-wavelength plate. A conductive AFM tip applies a local force on a sample surface and simultaneously collects the resultant PV current. A brief schematic of the Ph-AFM setup is shown in Fig. 1, A and B.

SrTiO$_3$ single crystal is one of the ideal systems to study the flexoelectric effect thanks to its simple cubic centrosymmetric lattice and large dielectric permittivity (14, 20). Unlike its sister material BaTiO$_3$, ordinary SrTiO$_3$ crystals do not exhibit the BPV effect because they have a center of inversion symmetry. But, with illumination around the contact area on a (001)-face of SrTiO$_3$ crystal, we observed that $I_{SC}$ exhibits a large transient peak as the loading force is increased from 1 μN to 18 μN (Fig. 1C), which is reproducible, proven by repeated exertion/withdrawal of the loading force.

To show that the giant enhancement of $I_{SC}$ by the point force is not confined to SrTiO$_3$ crystals or a cubic structure, we investigated the force-induced PV current in a single crystal of rutile TiO$_2$, which is well-known for its photoelectric applications such as dye-sensitized photovoltaic cells and photocatalysis. As in the case of SrTiO$_3$, large negative $I_{SC}$ appears once a large force is exerted on a TiO$_2$ (100) face. Figure 1D shows a stable current under the 15 μN force, confirming that the force-induced PV effect is not a transient effect in this material. Although it depends on contact conditions and locations, the point force exerted by the AFM tip gives rise to a substantial current density up to about 1 A/cm$^2$ at the nanoscale contact area. This is over three orders of magnitude higher than $I_{SC}$ (0.3 mA/cm$^2$) obtained from a Schottky junction between TiO$_2$ and Pt under the same illumination condition (see section S6 of (16)).

The current density increases more than 100 times by simply increasing the loading force from 1 to 15 μN (Fig. 1E). This cannot be explained with an increase of the contact area with the loading force because a contact area increases at most ~6 times with a 15 times larger contact force in a simple elastic sphere contact model (see section S2 of (16)). Moreover, a 100 times increase of the contact area with an AFM tip is unphysical. It should be noted that $I_{SC}$ turns to a positive value when loading the conductive AFM tip on a (001)-face of the TiO$_2$ crystal in contrast to the negative value of $I_{SC}$ on its (100)-face (Fig. 1F). The fact that the direction of the PV current depends on the crystallographic orientation of the TiO$_2$ crystal indicates that the observed PV effect cannot be merely attributed to a probable Schottky contact formed by the TiO$_2$ surface and the Pt-coating of the AFM tip.

A potential origin of this PV current enhancement is the BPV effect. As hypothesized, it is likely that a point force exerted on a crystal surface generates a local strain gradient, resulting in local centrosymmetry breaking and, thus, a local BPV current under illumination, i.e., the FPV effect, in the absence of a p-n junction and an appropriate band alignment. Given that both the flexoelectric response and the BPV effect depend on the crystallographic orientation (19–21), our results suggest a predominant role of the strain gradient and the resultant FPV effect in the enhanced local PV current.

The strain gradient induced by a sphere contact has a complex spatial distribution with giant strain gradient values in an elastic material, as described in section S2 of (16). An AFM tip apex can be approximated as a hemisphere and the distribution of strain gradient induced by the AFM tip can be calculated analytically with the Hertzian model and the Boussinesq’s calculation (22). Figure 2 shows the spatial distributions of the z-component of the calculated strain and its derivative with respect to z under ~15.7 μN force with a 10-nm-radius contact area at the origin. The strain gradient is as large as 10$^7$ m$^{-1}$. Interestingly, we found that the $I_{SC}$ density and the volume beneath the AFM tip being subject to a strain gradient larger than 1 × 10$^6$ m$^{-1}$ show similar dependence on the exerted force (Fig. 1E); the detailed process to obtain the relative volume can be found in fig. S9 of (16). It is expected that the giant strain gradients induced by the AFM tip break local symmetry, leading to the manifestation of the BPV effect locally under illumination. However, a relationship between the complex distribution of the strain gradient and the BPV properties should be quite intricate and deep theoretical considerations are required.

The main characteristic of the BPV effect is a periodic dependence on the angle between the PV current and the light polarization, stemming from its tensorial nature (21). For the present case, this dependence is predicted to be

$$I_{FPV} = \frac{\pi}{2} I_0 (A_2 \cos 2\alpha + B_2 \cos 2\alpha)$$  

(1)

Where $I_{FPV}$ is the PV current, $I_0$ is a light intensity, $A_2$ and $B_2$ are effective BPV coefficients of the locally deformed crystal, and $\alpha$ is the polarization angle of the incident light with respect to the top surface edge as described in section S3 of (16). The FPV effect should inherit the distinctive feature of the BPV effect and exhibit a sinusoidal dependence on the incident light polarization angle with a period of 180°. Indeed, $I_{SC}$ measured by a conductive AFM tip in the configuration illustrated in Fig. 1B on the SrTiO$_3$ (010) and TiO$_2$ (001) surfaces exhibits a light polarization dependence in accord with Eq. 1, as seen in Fig. 3. The sinusoidal behavior upon rotating the light polarization provides strong evidence that the underlying mechanism of the force-induced PV effect is the BPV effect generated by local symmetry breaking due to inhomogeneous strain, namely the FPV effect.

The FPV effect should be neither confined to ionic crystals nor restricted to nanoscale geometries. First, we performed the same experiment (as in Fig. 1) on an HF-passivated surface of a commercial p-type Si (001) crystal. Similarly, $I_{SC}$ increased two orders of magnitude from ~5 pA with the 1 μN loading force to ~0.5 nA with the 15 μN loading force (Fig. 4A and section S7 of (16)). Secondly, the FPV effect could also be
demonstrated using a home-built indentation system that de-
forms a semiconductor using a conductive tungsten probe
needle with a radius of about 10 μm (fig. S1 of (16)). Figure
4B shows crystallographic orientation dependent photocur-
rent-voltage (I-V) characteristics of the SrTiO$_3$ crystal ac-
quired under 4 N mechanical force exerted by the probe
needle and 405 nm laser illumination directly to the probe
contact area as in Fig. 1A. These linear I-V characteristics
are similar to those of ferroelectrics under illumination (23).
The oscillating PV current with the rotating light polarization,
which is well fitted with Eq. 1 (Fig. 4C), demonstrates the FPV
effect under the indentation force in the micrometer scale.
The crystallographic orientation dependent PV current is also
observed on the TiO$_2$ crystal by the indentation system (fig.
S2 of (16)).

We emphasize here four main features of the FPV effect.
First, the separation of the photoexcited carriers in the FPV
effect is controlled by the local symmetry and the resultant
local BPV effect, in which the power conversion efficiency can
in principle exceed the S-Q limit (8). Second, to obtain a high
photocurrent from any semiconductor, only a strain gradient
generator, such as a sharp probe with a sufficient loading
force is necessary. This should be distinguished from the pre-
vious reports that a strain gradient modifies a bandgap, but
the charge separation in the photoelectric process still re-
quires a proper band alignment (26) or a nanostructure (27,
28). Third, whereas the BPV effect is allowed only in non-cen-
trosymmetric materials, the FPV effect is universal. It is
allowed by symmetry in all materials thanks to the universal
nature of the strain-gradient-induced centrosymmetry break-
ning. The FPV effect can be realized not only in ionic crystals
(SrTiO$_3$ and TiO$_2$) and covalent crystals (Si), but is also rele-
vant to any semiconductors ranging from organic-inorganic
hybrid perovskites to semiconducting polymers and even top-
ological insulators. For instance, the topological insulator
Bi$_2$Te$_3$ with a centrosymmetric structure exhibits the BPV
effect by means of the flexoelectric effect (29). Finally, given
that the BPV effect consists of asymmetric quantum mechan-
ical processes such as photoexcitation, relaxation, recombi-
nation, and scattering, we demonstrate that one can readily
control the quantum mechanical processes by macroscopic
tool such as an AFM tip and a probe needle.

The configuration of our photovoltaic indentation system
is very simple and the FPV effect can be increasingly signifi-
cant with material dimensions decreasing into the nanoscale
where flexoelectricity is more important (11). Thus, an im-
portant strain engineering route for improving the final per-
formance of solar cells and optoelectronic devices is now
open. For example, a tandem solar cell can be easily fabri-
cated by combining an array of indenters and a conventional
p-n junction, enabling a higher efficiency because the FPV ef-
fector can be designed to add to the existing PV current gen-
erated by the buried p-n junction. Given that the lattice
mismatch at the interfaces and crystallographic disorders in
epitaxial and polycrystalline thin film solar cells give rise to
substantial strain gradients (30–32), the associated FPV effect
would dramatically impact the performance of these solar
cells, which however remains largely unexplored. In addition
to inorganic solar cells, the FPV effect is also likely to play an
important role in flexible and stretchable electronics based
on organic and polymeric semiconductors. Not only the bend-
of flexible organic devices at a macroscopic level (33) but also
the folding and entanglement of the polymeric chains in
a nanoscale level would generate sizable strain gradients (34),
which redistribute the electron cloud of π-molecular orbits,
modifying the electronic transport and inducing the FPV ef-
fector under illumination (15, 35). The detailed effects of strain
gradient and FPV effect on the nanoscale electronic proper-
ties remain an open question.

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Fig. 1. Force-induced photovoltaic effect in centrosymmetric SrTiO$_3$ and TiO$_2$ single crystals. 

(A) Setup for illumination around the contact area. The tip loading force is controlled by the feedback loop of atomic force microscope. 

(B) Setup for illumination on the side surface. The sidewise illumination geometry has been chosen to avoid the effect of Fresnel reflection and have light absorption being independent of the light polarization. 

Evolution of the photocurrent induced and collected by a conductive AFM tip with a high loading force on (C) SrTiO$_3$ (001) face and (D) TiO$_2$ (100) face. 

(E) The loading force dependence of the induced photocurrent density and the relative volume subject to the strain gradient higher than 1 × 10$^6$ m$^{-1}$ (see fig. S9 of (16)). 

(F) Positive photocurrent measured on TiO$_2$ (001) face with a 15 µN force applied by the AFM tip.
Fig. 2. Spatial distributions of strain and strain gradient induced by an ideal spherical indenter. (A) The $z$-component of strain and (B) its partial derivative with respect to $z$. The contact area with a radius of 10 nm is centered at the origin, and the force is pointing upward. The positive (negative) value of the strain means a tensile (compressive) strain along the $z$-axis.

Fig. 3. Light polarization dependence of the force-induced photocurrent. The sinusoidal dependence of the photocurrent measured on (A) SrTiO$_3$ (010) face and (B) TiO$_2$ (001) face under 405 nm laser illumination. The red lines are the fits to Eq. 1.
Fig. 4. Flexo-photovoltaic effect extended to covalent crystal and to the micrometer scale. (A) Force-induced photocurrent on (001) Si crystal measured by Ph-AFM under illumination of the top intended surface. (B) Current-voltage characteristics measured on (001) and (111) faces of a SrTiO₃ crystal by the micro-indenter applying a 4 N force and illumination of the top intended surface. (C) The light polarization dependence of the photocurrent on a SrTiO₃ (010) face measured by the micro-indenter under illumination on the side surface. The red line is the fitting of experimental data with Eq. 1. Because the polarization angle origin of the micro-indenter is not coincident with the Ph-AFM setup, the oscillating $I_{sc}$ has a phase shift compared with Fig. 3B.