Flux distributions in anaerobic, glucose-limited continuous cultures of *Saccharomyces cerevisiae*

Torben L. Nissen, Ulrik Schulze, Jens Nielsen and John Villadsen

Author for correspondence: Torben L. Nissen. Tel: +45 45 25 26 70. Fax: +45 45 88 41 48.

Department of Biotechnology, Technical University of Denmark, 2800 Lyngby, Denmark

A stoichiometric model describing the anaerobic metabolism of Saccharomyces cerevisiae during growth on a defined medium was derived. The model was used to calculate intracellular fluxes based on measurements of the uptake of substrates from the medium, the secretion of products from the cells, and of the rate of biomass formation. Furthermore, measurements of the biomass composition and of the activity of key enzymes were used in the calculations. The stoichiometric network consists of 37 pathway reactions involving 43 compounds of which 13 were measured (acetate, CO₂, ethanol, glucose, glycerol, NH^{*}, pyruvate, succinate, carbohydrates, DNA, lipids, proteins and RNA). The model was used to calculate the production rates of malate and fumarate and the ethanol measurement was used to validate the model. All rate measurements were performed on glucose-limited continuous cultures in a high-performance bioreactor. Carbon balances closed within 98%. The calculations comprised flux distributions at specific growth rates of 0.10 and 0.30 h⁻¹. The fluxes through reactions located around important branch points of the metabolism were compared, i.e. the split between the pentose phosphate and the Embden-Meyerhoff-Parnas pathways. Also the model was used to show the probable existence of a redox shunt across the inner mitochondrial membrane consisting of the reactions catalysed by the mitochondrial and the cytosolic alcohol dehydrogenase. Finally it was concluded that cytosolic isocitrate dehydrogenase is probably not present during growth on glucose. The importance of basing the flux analysis on accurate measurements was demonstrated through a sensitivity analysis. It was found that the accuracy of the measurements of CO₂, ethanol, glucose, glycerol and protein was critical for the correct calculation of the flux distribution.

Keywords: anaerobic growth, Saccharomyces cerevisiae, stoichiometric model, continuous culture, flux distribution

INTRODUCTION

Quantification of metabolic fluxes is one of the most important aspects of physiological studies, especially in connection with studies of metabolite production where the aim is to direct as much carbon as possible from the substrate into the metabolic product. A powerful technique for determination of the fluxes through various pathways is Metabolic Flux Analysis (MFA), where the intracellular fluxes are calculated using a stoichiometric model for all the major intracellular reactions. As input to the calculations a set of measured fluxes, typically the uptake rates of substrates and secretion rates of metabolites, is used (Vallino & Stephanopoulus, 1993; Jørgensen *et al.*, 1995). Apart from flux calculations leading to determination of the carbon flows inside the cell, MFA is useful for:

(1) Calculation of non-measured extracellular fluxes. Normally the number of fluxes that can be measured is larger than what is needed for the calculation of the

Abbreviations: EMP, Embden–Meyerhoff–Parnas; MFA, metabolic flux analysis; PP, pentose phosphate; RSD, relative standard deviation.

intracellular fluxes. In this case it is possible to calculate some of the extracellular fluxes, e.g. the production of various by-products, by use of the stoichiometric model and the measured rates.

(2) Calculation of maximum theoretical yields. Based on a stoichiometric model it is possible to calculate the maximum theoretical yield of a given metabolite if a set of constraints is specified. This has been illustrated by Stephanopoulos & Vallino (1991) who calculated the maximum theoretical yield of lysine on glucose in *Corynebacterium glutamicum* and by Jørgensen *et al.* (1995) who calculated the maximum theoretical the maximum theoretical the maximum theoretical the maximum theoretical yield of penicillin on glucose in *Penicillium chrysogenum* under the assumption of no growth.

(3) Identification of the existence of different pathways. Formulation of the stoichiometric matrix, which is the basis for MFA, requires detailed information on the biochemistry. However, for many micro-organisms certain details about the pathway stoichiometries are not known, and it may not be known whether a given pathway is active. Furthermore, there may be several isoenzymes with functions which are not known in detail. By calculating the metabolic fluxes with different sets of cellular pathways it may be possible to identify the set of pathways which is most likely to be active, or get indications of the function of different isoenzymes and/or pathways. This approach is illustrated in one of the first applications of MFA, where Aiba & Matsuoka (1979) examined various anaplerotic pathways in citrate-producing Candida lipolytica.

(4) Examination of the influence of alternative pathways on the distribution of fluxes. In connection with optimization of metabolite production it may be possible to identify one or several constraints for increasing the yield of a particular metabolite on the substrate or for increasing the flux leading to the desired metabolite. Here various scenarios can be compared to examine whether insertion of a new pathway or an isoenzyme (or perhaps deletion of an isoenzyme) can help to remove the constraint, and thereby lead to an increased flux towards the desired metabolite. This approach is especially of value in connection with metabolic engineering of microorganisms, where rational changes in the gene base are introduced with the aim of improving the performance of the micro-organism (Bailey, 1991).

(5) Identification of possible rigid branch points (or nodes) in the cellular pathways. Through comparison of the distribution of fluxes at different operating conditions it is possible to identify whether a pathway node is rigid or flexible (Stephanopoulos & Vallino, 1991). Thus in lysine-producing corynebacterium it is found that the nodes at glucose-6-phosphate, pyruvate and oxaloacetate are flexible, whereas the phosphoenolpyruvate node is rigid (Stephanopoulos & Sinskey, 1993; Vallino & Stephanopoulos, 1993).

In this paper we will use MFA for several of the abovementioned purposes. The metabolic fluxes in *Saccharomyces cerevisiae* will be calculated at different dilution rates in an anaerobic, glucose-limited continuous cultures providing a basis for the analysis of differences in the metabolism between the wild-type strain and genetically modified strains derived from the wild-type strain. Furthermore, the MFA is used in the study of various isoenzymes, which are active during anaerobic growth of *S. cerevisiae*, e.g. alcohol dehydrogenase (ADH) and isocitrate dehydrogenase, providing new information about the distribution and role of these enzymes during anaerobiosis.

Theory of MFA

The basis of MFA is a stoichiometric model describing the biochemistry of the micro-organism (Papoutsakis, 1984; Vallino & Stephanopoulos, 1990, 1993; Jørgensen et al., 1995). The stoichiometry of the considered intracellular reactions is specified in a stoichiometric matrix. From mass balancing around the intracellular metabolites, the reaction rates (or metabolic fluxes) are calculated based on an assumption of pseudosteady state in the intracellular concentrations of the metabolites and measurement of a few reaction rates, e.g. glucose uptake rate (Vallino & Stephanopoulos, 1993). Furthermore, to quantify the drain of metabolites for biomass synthesis it is nessesary to know the macromolecular composition of the biomass (Jørgensen et al., 1995).

If the stoichiometric matrix is singular, two or more reactions are linearly dependent and a unique solution of the set of mass balances cannot be determined. A typical singularity appears when the three reactions of ammonia assimilation catalysed by glutamate dehydrogenase II, glutamine synthase (GOGAT) and glutamine synthetase (GS) all are included in the stoichiometric matrix. Singularities can only be eliminated by changing the metabolic network, e.g. by adding or removing reactions. However, this must be done with due respect to the underlying biochemistry. *In vitro* enzyme assays can be used as a tool to determine the presence or absence of reactions and may also add a constraint to the model, e.g. an estimate of the ratio between two fluxes can be obtained.

Any stoichiometric model should be subjected to a sensitivity analysis to detect if the calculated rates are sensitive to errors in the measurements. For this purpose the sensitivity analysis described by Vallino & Stephanopoulos (1990) is useful.

Finally, it should be mentioned that compartmentation of the cell can be achieved simply by treating a given compound found in more than one compartment as different compounds in the model.

A stoichiometric model for S. cerevisiae

The general biochemistry of the primary and secondary metabolism in *S. cerevisiae* is well known. Detailed information concerning the reactions in the stoichio-

	Table 1.	References us	sed in the formu	ulation of the sto	ichiometric model
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Reaction	Reference		
Uptake			
Glucose	Bisson & Fraenkel (1983); McClellan & Bisson (1988)		
Ammonia	Roon et al. (1975); Cooper (1982); Cartwright et al. (1989)		
Sulphate	Breton & Surdin-Kerjan (1977); Roomans et al. (1979)		
Phosphate	Cockburn et al. (1975)		
Catabolism			
EMP pathway, PP pathway	Sols et al. (1971); Gancedo & Serrano (1989)		
Anabolism			
TCA cycle	Schatzmann (1975); Wales <i>et al</i> . (1980); Gancedo & Serrano (1989); Visser <i>et al</i> . (1994)		
Anaplerotic reaction	Haarasilta & Taskinen (1977)		
Amino acid synthesis	Jones & Fink (1982)		
Polymerization of amino acids	Tuite (1989)		
Nucleotide synthesis	Jones & Fink (1982)		
Lipid synthesis	Stryer (1988)		
Carbohydrate synthesis	Farkas (1989)		
Product formation			
Ethanol	Lutsdorf & Megnet (1968); von Jagow & Klingenberg (1970); Ciriacy (1979); Danielsson & Moseley (1986)		
Glycerol	Gancedo et al. (1968); Oura (1977)		
Acetate	Seegmiller (1955); Tamaki & Hama (1982)		
Product secretion	Gancedo <i>et al.</i> (1968); Jones & Greenfield (1982); Cartwright <i>et al.</i> (1989); Jones (1989); Stanley & Pamment (1993)		

metric model can be obtained in the references listed in Table 1.

The composition of protein, DNA, RNA and lipids is assumed to be constant under all growth conditions. This assumption is supported by measurements of the amino acid composition of the protein under various growth conditions. Whereas the amino acid composition of the protein was measured (data not shown), we use the composition of nucleotides in RNA and DNA obtained by de Robichon-Szulmajster & Surdin-Kerjan (1971) and the lipid composition described by Rattray (1988). The unsaturated fatty acids and the sterols are assumed to be supplied by respectively the Tween 80 and the ergosterol content of the medium. Specific properties of the stoichiometric model are described in the following.

Isoenzymes. Three isoenzymes of ADH (ADH I, ADH II and ADH III) have been identified in *S. cerevisiae* (Lutstorf & Megnet, 1968; Danielsson & Moseley, 1986). The cytosolic ADH I is constitutively expressed during anaerobic growth on glucose and is responsible for the formation of ethanol. ADH II is mainly associated with growth on ethanol (Ciriacy, 1979), and is therefore not active under the conditions applied in this work. The function of the mitochondrial ADH III is not known but it has been postulated to function as a shuttle of redox equivalents between mitochondria and the cytosol (von Jagow & Klingenberg, 1970). Measurements carried out in this work have shown that ADH III is active during anaerobic growth on glucose (see Results). Hence, the model includes two reactions where acetaldehyde is reduced to ethanol but localized in different compartments (reactions 9 and 37).

Two isoenzymes of aldehyde dehydrogenase exist (Seegmiller, 1955; Tamaki & Hama, 1982). The mitochondrial enzyme is repressed by glucose and can use both NAD⁺ and NADP⁺ as cofactors whereas the other is localized in the cytosol and is specific for NADP⁺. The formation of acetate by these two enzymes has been pooled into one reaction (reaction 10) in which the stoichiometric values for NADH and NADPH has been determined from measured *in vitro* activities of the enzymes (see Results). If both enzymic reactions are included a singularity in the stoichiometric matrix arises. This singularity is avoided by the chosen procedure.

Three isoenzymes of isocitrate dehydrogenase have been isolated (IDH, IDP1 and IDP2) (Keys & McAlister-Henn, 1990; Cupp & McAlister-Henn, 1991, 1992; Haselbeck & McAlister-Henn, 1991; Loftus *et al.*, 1994). The NAD⁺-dependent IDH is localized in the mitochondria and is important for the function of the TCA cycle whereas the function of the two NADP⁺-dependent isoenzymes IDP1 and IDP2 localized in the mitochondria and cytosol, respectively, have not yet been clearly established. The role of IDP1 may be in the formation of NADPH in the mitochondria for the synthesis of amino acids in this compartment. Furthermore, speculations have been made whether the two enzymes may play a role in the transfer of redox equivalents between cytosol and mitochondria (Lupiañez *et al.*, 1974; Machado *et al.*, 1975). Recent studies have suggested that IDP2 is not active during growth on glucose. Consequently only IDH and IDP1 are included in the model (reactions 17 and 22) although the consequences of including IDP2 in the model will be analysed (see Results).

Synthesis of cytosolic acetyl-CoA. Synthesis of cytosolic acetyl-CoA can occur in three ways in yeasts: (1) from acetate in a reaction catalysed by acetyl-CoA synthetase (Frenkel & Kitchens, 1977; Klein & Jahnkle, 1979; van der Berg & Steensma, 1995), (2) by hydrolysis of citrate to oxaloacetate and acetyl-CoA in a reaction catalysed by ATP: citrate lyase (Boulton & Ratledge, 1981), and (3) by transport of mitochondrial acetyl-CoA to the cytosol in the form of acetylcarnitine in a reaction catalysed by carnitine acetyltransferase (Kohlhaw & Tan-Wilson, 1977). Since a thorough study of the activity of ATP: citrate lyase in a large number of yeasts failed to find any activity of the enzyme in S. cerevisiae (Boulton & Ratledge, 1981), and since measurements of the activity of carnitine acetyltransferase carried out in this study showed no activity under the present growth conditions (see Results) only the reaction catalysed by acetyl-CoA synthetase has been included in the model (reaction 21).

Ammonia assimilation. Glutamate can be synthesized by two systems in S. cerevisiae: (1) glutamate dehydrogenase; (2) a two-step pathway catalysed by GS and GOGAT (Roon et al., 1974; Mitchell & Magasanik, 1983; Holmes et al., 1991). Measurements of the specific activities of both the NADPH-dependent and the NADH-dependent glutamate dehydrogenase and GOGAT carried out in this work (see Results) showed that the activity of the former enzyme exceeds the activities of the two other enzymes by a factor of 40 while no activity of GS could be detected. Hence, only the reaction catalysed by the NADPH-dependent glutamate dehydrogenase is included in the model.

ATP consumption. ATP is included as a metabolite in the stoichiometric matrix. To account for maintenance and futile cycles, a reaction is included to dissipate excess ATP (reaction 35). Furthermore, it is assumed that ATP and GTP can be interconverted by means of nucleoside diphosphokinases (Stryer, 1988).

Compartmentation. To obtain a realistic description of the redox levels in both the mitochondria and the cytosol, compartmentation is considered in the model. This compartmentation is achieved by treating compounds unable to cross the inner mitochondrial membrane as two different compounds, one present in the cytosol and the other in the mitochondria. This has been done for NADH, NADPH and fumarate since no transport systems for these compounds exist (LaNoue & Schoolwerth, 1979; Krämer & Palmieri, 1992). A compartmentation is also made for acetyl-CoA since no activity could be determined for carnitine acetyltransferase (see Results). This compartmentation implies that reactions consuming and producing the four compounds must balance in each compartment. S. cerevisiae has a number of carriers for di- and tricarboxylic acids that allows exchange of the TCA-cycle intermediates between the two compartments. The function of these carriers has been established in anaerobically grown cells (Perkins et al., 1973). Carriers for all intermediates of the TCA cycle, except for succinyl-CoA, have been reported, which implies that no compartmentation of these compounds is included in the model. Furthermore, a number of amino acids are partly synthesized in the mitochondria (Jones & Fink, 1981), and it is assumed that the intermediates of these reactions can be transported across the inner mitochondrial membrane.

Summary of the model description

The model contains 43 compounds and 37 pathway reactions. A zero volumetric production rate (pseudosteady state) is assumed for 27 compounds resulting in a model with 10 degrees of freedom. Thirteen compounds are measured: acetate, CO₂, ethanol, glucose, glycerol, NH₄⁺, pyruvate, succinate, carbohydrates, DNA, lipids, proteins and RNA. The remaining three compounds are not measured: cytosolic fumarate, malate and SO_4^{2-} . We have chosen to exclude ethanol and NH⁺₄ from the list of measured compounds which are used to calculate the metabolic fluxes. Thus, the calculated fluxes of ethanol and NH₄⁺ can be used to validate the flux model. The condition number of the stoichiometric matrix (Vallino & Stephanopoulos, 1990) is 22, implying that the model is numerically robust. All reactions and compounds of the stoichiometric matrix are listed in Appendix A.

METHODS

Micro-organism and its maintenance. S. cerevisiae CBS 8066 was obtained from the Centraal Bureau voor Schimmelcultures (Delft, The Netherlands). The strain was maintained at 4 °C on YPG agar plates, monthly prepared from a lyophilized stock kept at -80 °C. The bioreactor was inoculated to an initial biomass concentration of 1 mg l⁻¹ with a pre-culture grown in unbaffled shake flasks at 30 °C and 100 r.p.m. for 24 h.

Media. The yeast was cultivated in a mineral medium prepared according to the method of Verduyn *et al.* (1990). Vitamins were added by sterile filtration following heat-sterilization of the medium. The feed concentration of glucose and $(NH_4)_2SO_4$ was 25 g l⁻¹ and 7·5 g l⁻¹, respectively. Growth of *S. cerevisiae* under anaerobic conditions requires the supplementary addition to the medium of ergosterol and unsaturated fatty acids, typically in the form of Tween 80 (Andreasen & Stier, 1953; Libudzisz *et al.*, 1986). Ergosterol and Tween 80 were dissolved in 96% (v/v) ethanol and the solution was autoclaved at 121 °C for 5 min. The final concentrations of ergosterol and Tween 80 in the medium were 4·2 mg (g dry weight)⁻¹ and 175 mg (g dry weight)⁻¹, respectively. To prevent foaming, 75 µl antifoam l⁻¹ (Sigma) was added to the medium.

Cultivation conditions. Anaerobic continuous cultivations were performed at 30 °C and at a stirring speed of 1000 r.p.m. in an in-house-manufactured bioreactor with a working volume of 1 l. pH was kept constant at 5.00 by addition of 2 M KOH. The bioreactor was equipped with an off-gas condenser cooled to 2 °C. The bioreactor was continuously sparged with N_2 containing less than 5 p.p.m. O_2 , obtained by passing N_2 of a technical quality (AGA 3.8), containing less than 100 p.p.m. O_2 , through a column (250 × 30 mm) filled with copper flakes and heated to 400 °C. The column was regenerated daily by sparging it with H_o (AGA 3.6). A mass-flow controller (Bronkhorst HiTec F201C) was used to keep the gas flow into the bioreactor constant at 0.50 l min⁻¹. The medium reservoir was extensively sparged with N₂ containing less than 5 p.p.m. O2 and was then sealed. To avoid formation of a vacuum when withdrawing medium from the reservoir, it was connected to a gas-impermeable bag filled with N₂ containing less than 5 p.p.m. O₂. Norprene tubing (Cole-Parmer Instruments) was used throughout to minimize diffusion of oxygen into the bioreactor

Determination of dry weight. Dry weight was determined gravimetrically using nitrocellulose filters (pore size 0.45 μ m; Gelman Sciences). The filters were pre-dried in a microwave oven (Moulinex FM B 935Q) for 10 min. A known volume of culture liquid was filtered and the filter was washed with an equal volume of demineralized water followed by drying in a microwave oven for 15 min. The relative standard deviation (RSD) of the determinations was less than 1.5% based on triplicate determinations (n = 3).

Analysis of medium compounds. Cell-free samples were withdrawn directly from the bioreactor through a capillary connected to a 0.45 µm filter. Samples were subsequently stored at -40 °C. Glucose, ethanol, glycerol, acetic acid, pyruvic acid and succinic acid were determined by HPLC using an HPX-87H Aminex ion-exclusion column (RSD < 0.6%, n = 3). The column was eluted at 60 °C with 5 mM H_2SO_4 at a flow rate of 0.6 ml min⁻¹. Pyruvic acid and acetic acid were determined with a Waters 486 UV meter at 210 nm, whereas the other compounds were determined with a Waters 410 refractive index detector. The two detectors were connected in series with the UV detector first. The glycerol measurement was verified by measuring the concentration of the compound with a kit purchased from Boehringer Mannheim, while the glucose measurement was verified using a flow-injection analyser (Benthin et al., 1994). Ammonium was determined using a flow-injection analyser as described by Christensen et al. (1991) (RSD = 1.0%, n=3). The CO₂ concentration in the off-gas was determined using a Brüel & Kjær 1308 acoustic gas analyser (RSD = 0.02%) (Christensen et al., 1995). In a separate experiment, the off-gas from the bioreactor was bubbled through liquid nitrogen and the ethanol concentration in the frozen mixture of water, ethanol and acetaldehyde was determined by HPLC after evaporation of the N₂. Hereby the loss of ethanol through the reflux condenser of the bioreactor was determined to be between 4 and 9% of the ethanol formed by the bioreaction depending on the dilution rate (Schulze, 1995). In the carbon balances (Table 2), the measured ethanol fluxes were corrected for this loss through evaporation.

Analysis of intracellular compounds. Culture liquid was withdrawn from the bioreactor into an ice-cooled beaker. For each analysis, an adequate amount of sample was centrifuged, washed twice with 0.9% (w/w) NaCl and resuspended in buffer. Samples were immediately frozen in liquid nitrogen and subsequently stored at -40 °C. The protein content of whole cells was determined by a modified Biuret method

according to Verduyn et al. (1990) (RSD = 2.5%, n = 3). RNA measurements were determined as described by Benthin et al. (1991) (RSD = 2.0%, n = 3). Trehalose and glycogen were determined enzymically as described by Schulze et al. (1995) (RSD = 2.5%, n = 3). The total carbohydrate content was determined using the phenol method as described by Herbert et al. (1971). DNA measurement was by Burton's method as described by Herbert et al. (1971). Mannan and glucan were extracted by treating cells with hot acid (75 °C, 1 M HCl) for 6 h, whereafter mannan was precipitated with Fehling's reagent. After washing the precipitate with ethanol containing HCl, the content of mannan was quantified by the phenol method. Lipid was extracted from the cells using a mixture of chloroform and methanol (2:1 w/w) followed by washing with 0.9% NaCl. Subsequently, the solvents were removed by sparging the samples with N_2 whereafter the amount of lipid was quantified gravimetrically. The amino acid composition of the protein was determined as described by Barkholt & Jensen (1989) (RSD = 1.8%, n = 3). The intracellular pool of free amino acids was extracted by boiling cells in H₂O for 15 min (Malaney et al., 1989). The amino acid content of the extract was determined as described for the protein composition.

Preparation of cell-free extracts. Culture liquid was withdrawn from the bioreactor into an ice-cooled beaker, centrifuged and washed twice with 10 mM potassium phosphate buffer (pH 7·5, 2 °C) containing 2 mM EDTA. Subsequently the cells were resuspended in 4·2 ml 100 mM potassium phosphate buffer (pH 7·5, 2 °C) containing 2 mM MgCl₂, followed by immediate freezing in liquid nitrogen and storage at -40 °C. Prior to analysis, 0·22 ml 20 mM DTT was added to the samples, whereafter they were distributed into precooled 2 ml Eppendorf tubes containing 0·75 ml glass beads (size 0·25–0·50 mm). The cells were disrupted in a bead mill for 12·5 min (0 °C). The test tubes were centrifuged (20000 r.p.m., 20 min, 0 °C), whereafter the supernatants were pooled in one test tube. During the following analyses the extract was kept on ice.

Analysis of in vitro enzyme activities. Enzyme assays were performed at 30 °C using a Shimadzu UV-260 spectrophotometer at 30 °C. Reaction rates, corrected for endogenous rates, were proportional to the amount of extract added. All enzyme activities are expressed as µmol substrate converted min⁻¹ (mg protein)⁻¹ as determined by the Lowry method. Alcohol dehydrogenases I and III (EC 1.1.1.1) were assayed as described by Verduyn et al. (1992). Acetyl-CoA synthetase (EC 6.2.1.1), hexokinase (EC 2.7.1.1), glucose-6-phosphate 1-dehydrogenase (EC 1.1.1.49) and aldehyde dehydrogenase [NAD(P)⁺ and NADP⁺] (EC 1.2.1.5 and EC 1.2.1.4, respectively) were assayed as described by Postma et al. (1989). Glutamate dehydrogenase (NAD⁺ and NADP⁺) (EC 1.4.1.5 and EC 1.4.1.4, respectively) were assayed as described by Bruinenberg et al. (1983). Glutamine synthetase (EC 6.3.1.2) and glutamate synthase (GOGAT) (EC 1.4.1.14) were assayed as described by Holmes et al. (1989). The functionality of the GS assay was verified with GS purchased from Sigma. The assay of carnitine acetyltransferase (EC 2.3.1.7) was performed essentially as the acetyl-CoA synthetase assay except that acetyl carnitine was used instead of acetate as substrate. MgSO₄ was not added to the assay due to the inhibitory effect of magnesium ions on the enzyme. The functionality of the assay was verified with a carnitine acetyltransferase purchased from Sigma. For one dilution rate $(D = 0.1 \text{ h}^{-1})$, the assay for carnitine acetyltransferase was compared with the assay described by Fritz & Schulz (1965).

RESULTS AND DISCUSSION

Formation of biomass and products

Table 2 summarizes the yields on glucose of the most important products in the anaerobic, glucose-limited continuous cultures. It is seen that about 80% (w/w) of the consumed glucose is converted into ethanol and carbon dioxide and that these yields are virtually independent of the specific growth rate. On a molar basis Y_{sc} (1.63 mol mol⁻¹) is slightly higher than Y_{setoh} (1.49 mol mol⁻¹) since CO₂ is formed not only in the synthesis of ethanol but also in a number of anabolic reactions. A little less than 10% (w/w) of the glucose is converted into biomass and another 10% (w/w) ends up as glycerol whereas approximately 1% (w/w) is converted into various organic acids. Y_{sx} decreases slighty with increasing dilution rate whereas Y_{sgly} increases. Y_{ssuc} is practically unaffected by the dilution rate whereas Y_{spyr} and especially Y_{sace} increase when the dilution rate is increased from 0.1 to 0.4 h⁻¹. It is seen that the measured compounds can account for about 98% (w/w) of the consumed glucose (c.f. Table 2). The specific rates of glucose uptake and ethanol formation (Fig. 1) were found to be linear functions of the specific growth rate in analogy with the maintenance model of Pirt (1965):

$$r_{\rm i} = \gamma_{\rm xi} \cdot \mu + m_{\rm i} \tag{1}$$

The equation ascribes the consumption of a given substrate (or the formation of a product) to two processes, a growth associated and a non-growth associated. For $D < 0.2 \text{ h}^{-1}$ the specific rate of glycerol formation also follows the linear relation in equation (1) but for $D > 0.2 \text{ h}^{-1}$ the glycerol production increases more than linearly with μ (Fig. 1). Table 3 lists the stoichiometric and the maintenance coefficients for ethanol, glucose and glycerol. It is observed that all the maintenance coefficients are very close to zero.

The data obtained in this study are qualitatively in accordance with previously reported results for S.

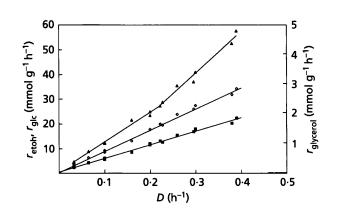


Fig. 1. The specific uptake rate of glucose (\blacksquare) and the specific production rates of ethanol (\blacklozenge) and glycerol (▲) as functions of the dilution rate.

Table 3. Stoichiometric (γ) and maintenance (*m*) coefficients for the glucose-limited continuous culture

Coefficient	mmol (g dry weight) ⁻¹	Coefficient	mmol (g dry weight) ⁻¹ h ⁻¹
γ _{xetoh}	85·05	m _{etob}	0.15 ± 0.27
γ_{xgle}	54.32	m_{glc}	0.45 ± 0.52
γ _{xgly} *	10.01	m_{gly}	0.02 ± 0.07

* Only valid for $D < 0.2 \text{ h}^{-1}$.

cerevisiae CBS 8066 (Verduyn et al., 1990; Lidén et al., 1995). All the reported results indicate that Y_{setoh} is independent of D and that Y_{sgly} and Y_{sace} increase with increasing D. However, Verduyn et al. (1990) do not find the linear relationships between r_{etoh} , r_{glc} and μ that are shown in Fig. 1 – the reason being that they measure a decreasing biomass concentration and hence a decreasing Y_{sx} (from 0.103 to 0.086 g g⁻¹) when D

Table 2. Yields on glucose for an anaerobic, glucose-limited continuous culture at various dilution rates

 Y_{sx} was calculated using molecular masses calculated from the measured biomass compositions. These values varied between 28.0 g C-mol⁻¹ at D = 0.1 h⁻¹ and 27.1 g C-mol⁻¹ at D = 0.4 h⁻¹.

Compound	Yield on glucose [C-mol (C-mol glucose) ⁻¹]			
	$D = 0.10 \text{ h}^{-1}$	$D = 0.50 \text{ h}^{-1}$	$D = 0.30 \text{ h}^{-1}$	$D = 0.40 \text{ h}^{-1}$
Carbon dioxide (Y _{sc})	0.272	0.273	0.267	0.261
Ethanol (Y _{setob})	0.497	0.496	0.494	0.497
Biomass (Y _{sx})	0.107	0.105	0.105	0.104
Glycerol (Y _{sgly})	0.086	0.091	0.095	0.109
Succinic acid (Y _{ssuc})	0.003	0.003	0.002	0.002
Acetic acid (Y _{sace})	0.002	0.003	0.006	0.010
Pyruvic acid (Y_{snyr})	0.001	0.002	0.003	0.004
Total	0.968	0.973	0.972	0.987

increases from 0·10 to 0·27 h⁻¹. Since the value of Y_{sx} at D = 0.10 h⁻¹ obtained in this study is virtually identical to the value observed by Verduyn *et al.* (1990), it is unlikely that the present culture has been limited by unsaturated fatty acids. The decrease in Y_{sx} observed by Verduyn *et al.* (1990) may be due to excess residual medium concentration of unsaturated fatty acids at high dilution rates which could lead to uncoupling of anabolic and catabolic processes (Viegas *et al.*, 1989) and thus, a decrease in Y_{sx} . However, the γ values listed in Table 3 are in good accordance with the values observed by Verduyn *et al.* (1990) at dilution rates lower than 0·20 h⁻¹. Lidén *et al.* (1995) reports similar values although the maximum value of Y_{sx} is found to be 0·09 g g⁻¹ indicating that the culture may have been fed with a suboptimal concentration of unsaturated fatty acids

Cellular composition

Measurements of the cellular composition are necessary to structure the flux of carbon to biomass, and especially if the cellular composition changes with the operating conditions it is important to consider the differences in fluxes to the different macromolecular pools. In this study, the cellular composition was therefore determined at four different dilution rates (see Table 4). The most important variation in the cellular composition is that the amount of active machinery, i.e. protein and RNA, increases linearly with increasing dilution rate at the expense of carbohydrates. The cellular content of other components is virtually independent of the dilution rate. From Table 4 it is seen that the measurements can account for approximately 100% of the cell mass, but since the pool of e.g. glycolytic intermediates has not been measured, some of the analyses have a small overlap. However, the results indicate that no major cellular component has been left out. The values listed in Table 4 are in good accordance with previously reported values for the cellular composition of S. cerevisiae (Küenzi & Fiechter, 1972; Oura, 1972; Watson, 1976; Waldron, 1977; Furukawa et al., 1983; Verduyn et al., 1990).

Enzyme activities

In vitro activities of 12 enzymes were measured to clarify ambiguities with respect to the presence or absence of an enzyme and the cofactor-specificity of certain enzymes at various growth conditions.

Fig. 2(a) illustrates the *in vitro* enzyme activities of key enzymes involved in formation and consumption of acetate. The activities of the two isoenzymes of aldehyde dehydrogenase were assayed to determine in which conditions the enzymes were active. From Fig. 2(a) it is apparent that the NAD(P)⁺-dependent enzyme is not active at D > 0.3 h⁻¹. Thus, the model includes both enzymes in the ratio determined by the enzyme assay except at D > 0.3 h⁻¹ where only the NADP⁺-dependent enzyme is included. No activity of carnitine acetyltransferase could be detected in the applied growth conditions indicating that cytosolic acetyl-CoA does not originate from the mitochondria. The activity of acetyl-CoA synthetase increased with the dilution rate, indicating that this enzyme is involved in synthesis of cytosolic acetyl-CoA.

Fig. 2(b) shows the *in vitro* activities of the enzymes involved in the assimilation of ammonia. It is apparent that at all tested dilution rates the activity of the NADPH-dependent glutamate dehydrogenase is more than 30-fold higher than the activity of GOGAT and the NADH-dependent glutamate dehydrogenase. Thus, it seems reasonable to include only the NADPH-dependent enzyme in the model. No activity of GS could be detected, indicating that the enzyme is labile and therefore lost in the preparation of the cell-free extract.

The specific enzyme activities of the two isoenzymes of alcohol dehydrogenase, ADH I and ADH III, are shown in Fig. 2(c). It is seen that both isoenzymes exhibit activity although the activity of ADH III is very low. The activity of this enzyme is nevertheless important since ADH III is localized in the mitochondria and may function as a shuttle of redox equivalents between the cytosol and the mitochondria (von Jagow & Klingenberg, 1970).

Finally, the activities of hexokinase and glucose-6phosphate dehydrogenase were determined in an attempt to verify the split between the PP and the EMP pathway predicted by the model. Fig. 2(d) shows the ratio between the activities of the two enzymes as a function of the dilution rate.

Flux distributions

Figs 3 and 4 show the flux distributions at D = 0.1 and $0.3 h^{-1}$, respectively. The fluxes are expressed in C-mol (g dry wt)⁻¹ h⁻¹ and have been normalized with respect to the glucose uptake. It is seen that the split between the PP and the EMP pathways increases with increasing specific growth rate. This can be explained by an increased demand for NADPH which is the result of an increase in the cellular content of especially protein but also of RNA. Also the flux from acetaldehyde to acetate, which is the second source of NADPH production in the cytosol, increases with increasing dilution rate.

Based on the measured enzyme activities, the split between the PP and the EMP pathways is 1:10 independent of dilution rate (Fig. 2d). The calculated split between the two pathways vary between 1:16 at a low dilution rate and 1:13 at a high dilution rate. The difference between the measured and the calculated split is likely to be caused by the differences between *in vitro* and *in vivo* conditions.

The flux to glycerol is observed to increase with μ as a result of an increasing drain of intermediates from the catabolic pathways (and hence an increasing production of surplus NADH) to support the higher levels of protein and RNA. The total flux into the TCA cycle through the reaction catalysed by pyruvate dehydro-

Metabolite	Cellular content (%, w/w)				
	$D = 0.10 \text{ h}^{-1}$	$D = 0.20 \text{ h}^{-1}$	$D = 0.30 \text{ h}^{-1}$	$D = 0.40 \text{ h}^{-1}$	
Protein	45.0	50.0	55.5	60·1	
Glycogen	8.4	4 ·2	0.6	0.0	
Trehalose	0.8	0.5	0.0	0.0	
Mannan	13·1	12.9	12.0	13·3	
Other carbohydrates	18.4	15.4	12.6	3.7	
RNA	6.3	8.2	10.1	12.1	
DNA	0.4	0.4	0.2	0.6	
Free amino acids	1.1	1.3	1.1	2.0	
Lipid	2.9	3.0	3.8	3.4	
Ash	5.0	5.0	5.0	5.0	
Total	101 ·4	100 ·6	101·2	100·2	

Table 4. Cellular composition of *S. cerevisiae* as a function of the dilution rate in a glucose-limited culture

genase and the transport of oxaloacetate from the cytosol into the mitochondria decreases from 3.6 to 2.6% of the glucose uptake when the specific growth rate increases from 0.1 to 0.3 h⁻¹. This drop is almost exclusively due to the decrease in the succinate production with increasing specific growth rate and is only reflected in the influx of oxaloacetate to the mitochondria, while the flux through the reaction catalysed by pyruvate dehydrogenase is almost constant. A split in the TCA cycle into an oxidative (clockwise) and a reductive branch is observed at both specific growth rates. It should be noted that the reductive branch is thermodynamically feasible and has been proposed to operate in S. cerevisiae (Lupiañez et al., 1974; Machado et al., 1975). The reductive branch and the ADH I/ADH III shunt are two possible routes for oxidation of surplus NADH produced in the mitochondria by the oxidative TCA branch and in the synthesis of amino acids. It is seen that the flux through the reductive branch decreases to a very low level while the flux through the shunt increases slightly when the specific growth rate increases. This indicates that the ADH I/ADH III shunt is the primary route in the regeneration of NAD⁺ in the mitochondria while the reductive branch is primarily involved in the formation of succinate.

The rates of malate and of cytosolic fumarate formation were not measured in the present study, but were calculated from the model assuming that the two compounds are secreted into the medium without being further metabolized. The calculated specific production rates correspond reasonably well with measurements of both these compounds in anaerobic, glucose-limited continuous cultures of *S. cerevisiae* CBS 8066 (Verduyn *et al.*, 1990).

The specific production rate of ethanol was calculated by the model to be 0.0176 and 0.0551 C-mol (g dry weight)⁻¹ h⁻¹ at D = 0.1 and 0.3 h⁻¹, respectively. This corresponds to ethanol yields on glucose of 0.405 g g⁻¹ at D = 0.1 h⁻¹ and 0.406 g g⁻¹ at D = 0.3 h⁻¹, i.e. about 6% higher than the measured yield of 0.381 g g⁻¹ (Table 2). A possible explanation for this discrepancy is that more ethanol evaporates than accounted for (see Methods).

The metabolic flux model is an excellent tool for examining the presence and localization of reactions in the metabolism. This was tested by deleting the reaction catalysed by ADH III from the model, whereby the redox shunt across the mitochondrial membranes is no longer present. The calculated fluxes are shown in Fig. 4 (italic numbers). As the basis for the calculation the data from the dilution rate $0.3 h^{-1}$ was used. It is seen that the flux through the reductive branch of the TCA cycle increases when compared to the calculated fluxes at $D = 0.3 \text{ h}^{-1}$ where the redox shunt is included (bold numbers in Fig. 4), and that the branch also includes the reactions from succinate to 2-oxoglutarate. Since this last reaction (which is the sum of two reactions with succinyl-CoA as an intermediate) is thermodynamically favourable in the opposite direction ($\Delta G^{\circ} = -7.2 \text{ kJ}$ mol⁻¹ in the reaction from 2-oxoglutarate to succinyl-CoA), the calculated fluxes in the model without the reaction catalysed by ADH III are probably incorrect, and this indicates that the redox shunt has a role in the regulation of the redox level in the mitochondria. Similarly, the presence of an NADPH-dependent isocitrate dehydrogenase (IDP2) in the cytosol was tested since it has been proposed that this enzyme has an important role in the production of NADPH in this compartment (Bruinenberg, 1983). This was done by including the reaction in the model and calculating the fluxes using the data obtained at $D = 0.3 \text{ h}^{-1}$ (italic numbers in Fig. 5). It is seen that the presence of the reaction has a significant effect on the calculated fluxes. The origin of this effect is the occurrence of another redox shunt across the mitochondrial membrane where NADH is consumed in the mitochondria by the NADHdependent isocitrate dehydrogenase (IDH) leading to a substantial formation of isocitrate which is transported

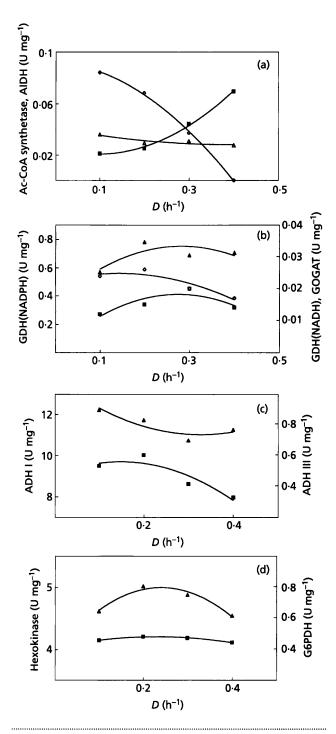
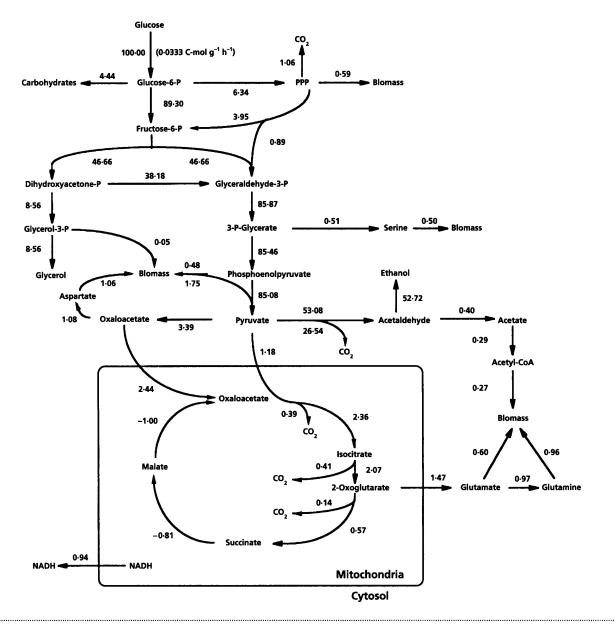


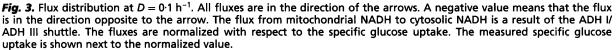
Fig. 2. In vitro specific enzyme activities as functions of dilution rate. (a) acetyl-CoA synthetase (\blacktriangle) and NAD(P)⁺- and NADP⁺- dependent aldehyde dehydrogenase (\diamondsuit , \blacksquare); (b) NADH- and NADPH-dependent glutamate dehydrogenase (\blacksquare , \blacktriangle) and GOGAT (\diamond); (c) mitochondrial (ADH III) and cytosolic (ADH I) alcohol dehydrogenase (\blacksquare , \blacktriangle); (d) glucose-6-phosphate 1-dehydrogenase (\blacksquare) and hexokinase (\bigstar).

to the cytosol and converted back to 2-oxoglutarate with an accompanying large production of NADPH in this compartment. In order to remove the pool of NADPH the model calculates negative fluxes through the PP pathway, and this is thermodynamically unfeasible since the reaction from glucose-6-phosphate to ribose-5-phosphate is practically irreversible ($\Delta G^{\circ} =$ $-47.04 \text{ kJ mol}^{-1}$). The high amount of NADH which is consumed when converting 2-oxoglutarate to isocitrate in the mitochondria is produced in the remaining part of the TCA cycle and by reversing the direction of the reaction catalysed by ADH III. The calculated flux pattern indicates that IDP2 is absent under the growth condition used in this study. Instead, the enzyme might play a role in the production of NADPH during growth on other carbon sources. This hypothesis is supported by a recent study where no activity of the enzyme could be detected when growing S. cerevisiae on glucose whereas the enzyme was active in cells grown on ethanol or glycerol (Loftus et al., 1994). It should also be noted that when using data obtained from dilution rates different from $D = 0.3 h^{-1}$, most reasonable results are obtained by including the reaction catalysed by ADH III and excluding the reaction catalysed by IDP2.

Sensitivity analysis

To determine the sensitivity of the flux calculations towards measurement errors a sensitivity analysis was carried out as described above. In the analysis, the RSD values described in Methods were used. The analysis showed that accurate measurements of the specific glucose uptake rate and the specific production rates of ethanol, glycerol, CO₂ and protein are critical for calculating the correct fluxes while an error in the measurement of any other compound only leads to incorrect fluxes through the last two or three reactions at the end of the biosynthesis of the given compound. The measurement of the ethanol concentration in the medium is very accurate, but systematic errors arise due to evaporation of the compound from the bioreactor. As previously discussed the correction procedure by which evaporated ethanol is captured in liquid N₂ does not recover all ethanol lost from the reactor. Therefore, ethanol was not included in the vector of measured rates, and the calculated ethanol flux can possibly be used to improve the correction procedure. The measurements of CO₂ and glucose are critical for the correct calculation of the fluxes through the PP and the EMP pathway (a relative error of 0.6% leads to relative errors of 1.4% in the fluxes), in the TCA cycle (relative errors of 3.0 to 6.0%) and to ethanol, RNA and DNA (relative errors of 2.4 to 3.6%). The glycerol measurement has a significant effect on the fluxes in certain mitochondrial reactions (in most TCA cycle reactions one obtains relative deviations from 3.0 to 6.0% while flux 18 and 37 are particularly sensitive with relative errors of respectively 18.0 and 9.0%). Similarly, the error of 2.5% in the protein measurement leads to a 1.2% change in the fluxes through the PP pathway and a 5.0% change in the fluxes 17 and 18. It should be noted that the protein content increases by far more than the 2.5% used in the sensitivity analysis when the specific growth rate is increased from 0.1 to $0.3 h^{-1}$. This means that an assumption of a constant protein content under different





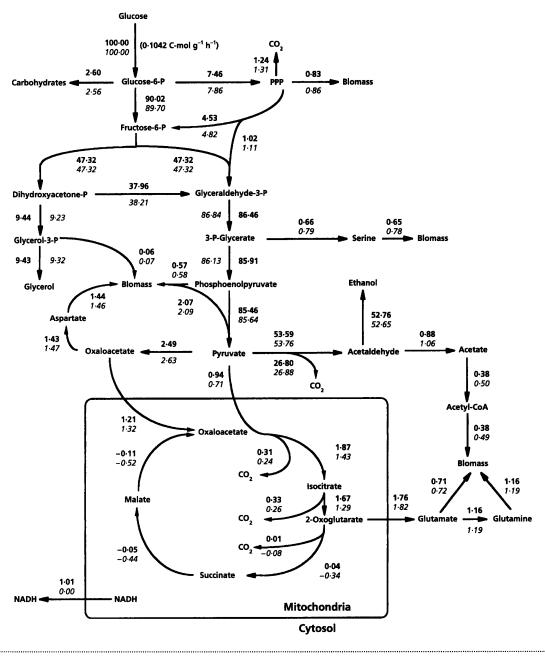
growth conditions leads to a significant error in the calculation of the flux distributions. This might also be true for other macromolecules under aerobic conditions where the amount of carbon going from glucose to biomass is fivefold higher.

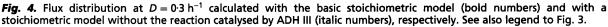
Conclusions

In conclusion, three obvious applications exist for the MFA:

(1) Data from physiological studies can easily be analysed and information concerning intracellular flux distributions under various growth conditions can be evaluated. In the present study, calculations of the split between the PP and the EMP pathways, and of the flux into the mitochondria at various growth rates, were used to illustrate how further insight into the growth physiology may be obtained through flux analysis.

(2) It is possible to test for the presence or absence of single reactions or whole pathways in the metabolism. This application was demonstrated with the reactions catalysed by ADH localized in the mitochondria and isocitrate dehydrogenase localized in the cytosol. It was concluded that during anaerobic growth ADH III together with the reductive branch of the TCA cycle



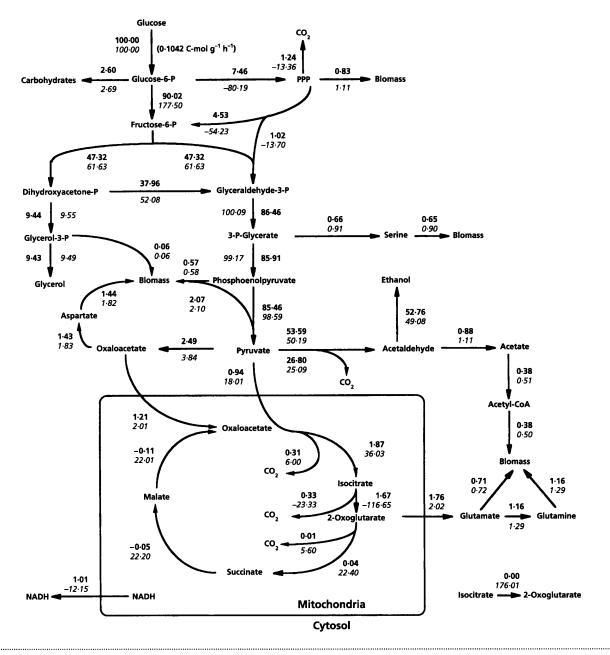


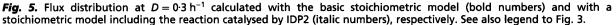
regenerates the mitochondrial pool of NAD⁺ that is consumed in the synthesis of amino acids and compounds in the TCA cycle. It was also shown that IDP2 probably does not serve as a source of NADPH in the cytosol during anaerobic growth on glucose. The consequences of deletions or insertions of pathways in the central metabolism through genetic engineering can be evaluated in the same way. The MFA is consequently a simple and powerful tool when deciding a strategy for metabolic engineering of a given micro-organism.

(3) The MFA can in general be applied to calculate yields of compounds which are not measured if the degrees of

freedom in the model exceeds the number necessary for determining the fluxes. Here the fluxes of malate and cytosolic fumarate were calculated and a possible systematic error in the ethanol measurement was indicated.

To calculate correct fluxes it is necessary to have precise measurements of the specific consumption rates of the substrates and of the specific production rates of the products which form the basis for the flux analysis. In this work, the physiological studies were carried out using steady state continuous cultures where the rates were determined from a single but well-established





measurement of the substrates and the products at any given specific growth rate. Furthermore, carbon and redox balances of the measurements were set up leading to the conclusion that no major product was ignored in the flux analysis. When using other cultivation strategies, e.g. batch or fed batch cultivations, estimation of the specific rates to be used for the flux calculations is difficult, since it requires information on the time derivatives of the concentrations in the medium.

In the evaluation of the outcome of MFA, a sensitivity analysis determines the influence of each measurement on the calculations, and this creates a quantitative basis on which the required precision of the measurements can be determined. In this work a sensitivity analysis showed that the measurement of the specific consumption rate of glucose and the specific production rates of ethanol, glycerol, protein and CO_2 were important for the calculation of the correct fluxes. Ethanol was, however, not included in the stoichiometric matrix since there might be a small, but systematic, error in its determination. The accuracy in the measurements of the remaining four compounds was sufficient to ensure that accurate fluxes were calculated – and hence that the calculated ethanol flux might be more accurate than the measured flux.

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 $(CH_{11/6}OP_{1/6})$

 $(CH_{11/6}OP_{1/6})$

 $(CH_{5/3}OP_{1/3})$

 $(CH_{7/3}OP_{1/3})$

 $(CH_{1/2}O_{5/4})$

 $(CH_{2/3}^{-}OP_{1/3})$

 $(CH_{9/5}OP_{1/5})$

 $(CH_{7/3}ON_{1/3})$

 $(CH_{5/6}O_{7/6})$

('H')

('H')

('H')

('H')

 $(CH_{5/8}O_{4/5}N_{1/5})$ $(CH_2O_{3/5})$

 $(CHO_{3/2})$

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APPENDIX A: Compounds and reactions in the stoichiometric matrix

Compounds

1. Acetate	(CH _{3/2} O)
2. Ethanol	$(CH_3O_{1/2})$
3. Glycerol	$(CH_{8/3})^{1/2^{1}}$
4. Pyruvate	(CHO)
5. Succinate	(CHO)
6. RNA	$(CH_{1\cdot 2457}O_{0\cdot 4653}N_{0\cdot 4074}$
	$P_{0.1048}$)
7. CO ₂	(CO_2)
8. Glucose	$(CH_{2}^{\tilde{U}}O)$
9. NH4 (extracellular)	(NH_4^+)
10. Carbohydrate	$(CH_{11/6}^{4}O)$
11. DNA	$(CH_{1.5577}^{11/6}O_{0.4925}N_{0.3740}^{-}$
	$P_{0.1018}$
12. Protein	$(CH_{1.5651}^{0.1010}O_{0.4639}N_{0.2722}S_{0.0083}$
	$P_{0.021}$
13. Lipid	$(CH_{1.9507}^{0.0217}O_{0.1579}N_{0.0221}^{-}$
L	$P_{0.0337}$
14. Sulphate	(SO_4^{2})
15. 5-AICAR	$(CH_{13/9}^*O_{5/9}N_{1/9}P_{1/9})$
16. 2-Oxoglutarate	$(CH_{4/5}O)$
17. 3-Phosphoglycerate	$(CH_{4/3}^{4/3}O_{4/3}P_{1/3})$
18. Methyl-THF	('CH ₃ ')
19. Acetaldehyde	$(CH_2O_{1/2})$
20. Acetyl-CoA	$(CH_{3/2}^2O_{1/2}^2(CoA)_{1/2})$
21. NH_4^+ (intracellular)	(NH_4^+)
22. Aspartate	$(CH_{6/4}ON_{1/4})$
23. Diĥydroxyacetone-	$(CH_{5/3}^{3}OP_{1/3}^{1/3})$
phosphate	-,,-
24. Erythrose-4-phosphate	$(CH_{4/7}OP_{1/4})$
	-, • • •, •

- 25. Fructose-6-phosphate
- 26. Malate 27. Glucose-6-phosphate
- 28. Glutamate
- 29. Glutamine
- 30. Glyceraldehyde-3phosphate
- 31. Glycerol-3-phosphate
- 32. NADPH_{mit}
- 33. NADPH_{evt}
- 34. NADH_{mit}
- 35. NADH_{evt}
- 36. Oxaloacetate_{mit}
- 37. Phosphoenolpyruvate 38. Ribose-5-phosphate
- 39. Serine 40. ATP
- 41. Isocitrate
- 42. Oxaloacetate_{evt} $(CH_{1/2}O_{5/4})$
- 43. Fumarate_{evt} $(CH_{1/2}O)$

Reactions

Compounds in bold letters are included in the stoichiometric matrix.

- 1. Glucose + $1/6ATP \rightarrow Glucose-6-P + 1/6ADP +$ $1/6H^{+}$
- 2. Glucose-6-P \rightarrow Fructose-6-P
- 3. Fructose-6-P + $1/6ATP \rightarrow 1/2Glyceraldehyde +$ 1/2Dihydroxyacetone-P + 1/6ADP + 1/6H⁺
- 4. Dihydroxyacetone-P \rightarrow Glyceraldehyde-3-P
- 5. Glyceraldehyde-3-P+1/3NAD⁺+1/3ADP+1/3P₁ \rightarrow 3-P-glycerate + 1/3ATP + 1/3NADH_{evt} + $1/3H^{+}$
- 6. **3-P-Glycerate** \rightarrow Phosphoenolpyruvate $+ 1/3H_{0}O$
- 7. Phosphoenolpyruvate $+ 1/3ADP + 1/3H^+ \rightarrow Pyru$ vate + 1/3ATP
- 8. Pyruvate + $1/3H^+ \rightarrow 2/3$ Acetaldehyde + $1/3CO_2$
- 9. Acetaldehyde + 1/2NADH_{cvt} + 1/2H⁺ \rightarrow Ethanol $+ 1/2NAD^+$
- 10. Acetaldehyde + 1/2NADP⁺ + 1/2H₂O \rightarrow Acetate- $+1/2NADPH_{cvt} + 1/2H^{+}$
- Dihydroxyacetone-P + 1/3NADH_{cvt} + 1/3H⁺ \rightarrow 11. Glycerol-3-P + 1/3NAD⁺
- 12. Glycerol-3-P + $1/3H^+ \rightarrow$ Glycerol + $1/3P_i$
- 13. Glucose-6-P+1/3NADP⁺+1/2H₂O \rightarrow 5/6Ribose-5-P + 1/3NADPH_{cvt} + $1/3H^{+}+1/6CO_{2}$
- 14. Ribose-5-P $\rightarrow 2/5$ Erythrose-4-P+3/5Fructose-6-P
- 15. 5/9Ribose-5-P+4/9Erythrose-4-P $\rightarrow 6/9$ Fructose-6-P+3/9Glyceraldehyde-3-P
- 16. 3/7Pyruvate + 4/7Oxaloacetate_{mit} + 1/7NAD⁺ + $1/7H_2O \rightarrow 6/7Isocitrate + 1/7CO_2 +$ $1/7H^{4} + 1/7NADH_{mit}$ 17. Isocitrate + $1/6NAD^{+} \rightarrow 5/62$ -Oxoglutarate +
- $1/6CO_2 + 1/6NADH_{mit}$ 18. **2-Oxoglutarate** + $1/5NAD^+ + 1/5ADP + 1/5P_i +$ $1/5H_2O \rightarrow 4/5Succinate + 1/5ATP +$ $1/5CO_2 + 1/5NADH_{mit} + 1/5H^+$
- 19. Succinate + $1/4FAD \rightarrow Malate + 1/4FADH2$

- 20. Malate + $1/4H_{2}O + 1/4NAD^{+} \rightarrow$ $Oxaloacetate_{mit} + 1/4NADH_{mit} + 1/4H^+$
- 21. Acetate + $1/2CoA + ATP \rightarrow Acetyl CoA + ADP + P_i$
- 22. Isocitrate + $1/6NADP^+ \rightarrow 5/62$ -Oxoglutarate + $1/6CO_2 + 1/6NADPH_{mit}$
- 23. 3/4Pyruvate + 1/4CO₂ + 1/4H₂O + 1/4ATP \rightarrow
- Oxaloacetate_{cyt} + $1/4ADP + 1/4P_i + 1/4H^+$ 24. Glucose-6-P + $1/6ATP \rightarrow Carbohydrate +$ $1/6ADP + 1/3P_{i}$
- 25. 2-Oxoglutarate $+ 1/5NH_4^+ + 1/5NADPH_{cvt} +$ $1/5H^+ \rightarrow \text{Glutamate} + 1/5H_2O + 1/5NADP^+$
- 26. Glutamate + $1/5NH_4^+$ + $1/5ATP \rightarrow$ Glutamine $+ 1/5ADP + 1/5P_{1} + 1/5H^{+}$
- 27. $4/9Oxaloacetate_{cyt} + 5/9Glutamate \rightarrow 4/9Aspartate + 5/92-Oxoglutarate$
- 28. 3/83-P-Glycerate + 5/8Glutamate + 1/8NAD⁺ \rightarrow 3/8Serine + 5/82-Oxoglutarate + $1/8P_i$ + $\frac{1/8\text{NADH}_{cyt}}{29. \text{ NH}_4^+(\text{ex}) + \text{ATP} \rightarrow \text{NH}_4^+(\text{int}) + \text{ADP} + P_i}$
- 30. 5/23Ribose-5-P+10/23Glutamine+3/23Serine+ 4/23Aspartate + 1/23CO₂ + 1/23H₂O + 6/23ATP + 1/23NADP_{eyt}⁺ $\rightarrow 9/235$ -AICAR + 10/23Glutamate + 4/23Fumarate + 1/23NADPH_{cvt} + $1/23H^{+}+6/23ADP+6/23P_{1}$
- 31. 0.45795-AICAR + 0.4371Glutamine + 0.0842 Methyl-FH₄ + 0.3313 Aspartate + 0.2544**Ribose-5-P**+0.4625**ATP**+ 0.0509NADPH_{cvt} + 0.3301H₂O + 0.1540NAD⁺ \rightarrow DNA + 0.4371Glutamate + 0.1278Fumarate +0.1540 NADH_{cvt} + 0.0509 NADP⁺ + 0.5166H⁺ + $0.4625 \text{ADP} + 0.4625 \text{P}_{1}$

- 32. 0.51125-AICAR + 0.5271Glutamine + 0.0568 Methyl-FH₄ + 0.2993 Aspartate + 0.2400 Ribose-5-P + 0.4890 ATP + 0.3427 H₂O + 0.0568NADP⁺ + 0.1348NAD⁺ \rightarrow RNA + 0.5271Glutamate + 0.1073Fumarate + 0.1348NADH_{cvt} + 0.0568NADPH_{evt} + 0.7080H⁺ + 0.4890ADP + 0.4890P
- 33. 0.0404 Ribose-5-P + 0.6090 Glutamate + 0.2078Glutamine + 0.2153Aspartate + 0.3380Pyruvate + 0.1182Serine + 0.0623Erythrose-4-P+0.0935Phosphoenolpyruvate+1.0396ATP+ 0.0495NADPH_{mit} + 0.0742NAD⁺_{mit} + 0.0017NADH_{cyt} + 0.1084NADPH_{cyt} + $0.0053SO_4^{2-}$ $+0.7685H_{\odot}O \rightarrow Protein + 0.49272$ -**Oxoglutarate** + 0.0413 Fumarate + 0.0117 Glyceraldehyde-3-P+ $0.1054CO_2$ + $0.0100 \text{NH}_{4}^{+} + 0.0165 \text{Methyl-FH}_{4} +$ 0.0742NADH_{mit} + 0.01885-AICAR + 1.0617H⁺ + $\begin{array}{c} 0.0495 \text{NADP}^+_{\text{mit}} + 0.0017 \text{NAD}^+_{\text{cyt}} + \\ 0.1084 \text{NADP}^+_{\text{cyt}} + 1.0396 \text{ADP} + 1.0396 \text{P}_{i} \\ 34. 0.8326 \text{Acetyl-CoA}_{\text{cyt}} + 0.0662 \text{Glycerol-3-} \\ \end{array}$
- P + 0.1012Serine + 0.4000ATP +0.7111NADPH_{cvt} + 0.0259H⁺ \rightarrow Lipid + $0.0258H_{2}O + 0.4000ADP + 0.4000P_{i} + 0.4163CoA$
- 35. ATP \rightarrow 'Maintenance'
- 36. Oxaloacetate_{cvt} + 1/4ATP \rightarrow Oxaloacetate_{mit} + 1- $/4ADP + 1/4P_{i} + 1/4H^{+}$
- 37. Acetaldehyde + 1/2NADH_{mit} + 1/2H⁺ \rightarrow Ethanol $+1/2NAD^{+}$

Received 13 May 1996; revised 23 July 1996; accepted 23 August 1996.