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Jakub Bijak

# Forecasting International Migration in Europe: A Bayesian View

(with contribution by Arkadiusz Wiśniowski)

 Springer

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*To my Kasia*  
– JKB



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<sup>1</sup>See, for example, W. Bijak (1990) – I am especially grateful for mini-lectures on subjective probability around the time of publishing that paper.



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