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Formation of ordered ice nanotubes inside carbon nanotubes

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Summary: Following their discovery¹, carbon nanotubes have attracted interest not only for their unusual electrical and mechanical properties, but also because their hollow interior can serve as a nanometre-sized capillary^{2, 3, 4, 5, 6, 7}, mould^{8, 9, 10, 11} or template^{12, 13, 14} in material fabrication. The ability to encapsulate a material in a nanotube also offers new possibilities for investigating dimensionally confined phase transitions¹⁵. Particularly intriguing is the conjecture¹⁶ that matter within the narrow confines of a carbon nanotube might exhibit a solid-liquid critical point¹⁷ beyond which the distinction between solid and liquid phases disappears. This unusual feature, which cannot occur in bulk material, would allow for the direct and continuous transformation of liquid matter into a solid. Here we report simulations of the behaviour of water encapsulated in carbon nanotubes that suggest the existence of a variety of new ice phases not seen in bulk ice, and of a solid-liquid critical point. Using carbon nanotubes with diameters ranging from 1.1 nm to 1.4 nm and applied axial pressures of 50 MPa to 500 MPa, we find that water can exhibit a first-order freezing transition to hexagonal and heptagonal ice nanotubes, and a continuous phase transformation into solid-like square or pentagonal ice nanotubes.

Carbon nanotubes can be wetted by liquids⁴ whose surface tension does not exceed about 200 mN m⁻¹. Thus, in principle, pure water can be drawn into open-ended nanotubes by capillary suction⁵. Once inside, water molecules are expected to form quasi-one-dimensional (Q1D) structures that might form new phases of ice, different from the 13 polymorphic phases of bulk ice identified experimentally thus far¹⁸. We carried out molecular dynamics (MD) simulations at constant temperature (T) and axial-pressure (P_{zz}) of water confined within 'armchair' (R,R) single-walled carbon nanotubes (SWCNs). We used nanotubes with indices $R = 14$ –18, corresponding to tubes with diameters of 11.1, 11.9, 12.6, 13.4 and 14.2 Å, respectively. The phase behaviour of the confined water was examined in several series of the MD simulations, each series corresponding to an isobaric path or an isothermal path in the P_{zz} - T phase diagram at a given R (see Methods for details).

The first series of simulations follows an isobaric path of 50 MPa. The temperature was lowered stepwise starting from 320 K or higher, where the system is in a liquid state, to 240 K or lower. The potential energy of water in each type of SWCN is plotted in Fig. 1. In the wide SWCNs (16,16) and (17,17), the potential energy drops abruptly (Fig. 1c and d) on cooling and jumps sharply on heating. This marked hysteresis-loop behaviour signifies a first-order phase transition. Structural analysis reveals that the low- T phase is a Q1D n -gonal 'ice nanotube' composed of orderly stacked n -membered water rings²⁰, where $n = 6$ (hexagonal) in (16,16) and $n = 7$ (heptagonal) in (17,17)

SWCNs. In both types of nanotube, the molar volume of water decreases during the liquid-to-ice nanotube transition; that is, the confined water shrinks on freezing. In the widest SWCN (18,18), however, crystallization was not observed within the timescale of simulation. In the narrower SWCNs (14,14) and (15,15), the potential energy also drops markedly on cooling below 300 K, but the change is not as sharp as in the wider nanotubes. Structural analysis shows that confined water has liquid-like disordered structure at high T but turns into solid-like ordered structure at low T —a square nanotube in (14,14) and a pentagonal nanotube in (15,15) SWCN. At 240 K, the calculated diffusion constants (along the axial direction) are $D = 3 \times 10^{-10}$ cm² s⁻¹ in the (14,14) SWCN, and $D < 1 \times 10^{-10}$ cm² s⁻¹ in the (15,15) SWCN, which are comparable to D of bulk ice²¹. At 300 K, $D = 1 \times 10^{-5}$ cm² s⁻¹ and $D = 2 \times 10^{-5}$ cm² s⁻¹ respectively. More interestingly, besides the less sharp change in the potential energy, the hysteresis loop was not observed in the cooling and heating process, a signature of continuous transformation from liquid-like to solid-like state of water.

In real-world experiments, the atomic structures of Q1D crystals can be determined by using transmission electron microscopy.¹¹ Simulations provide this information directly. Figure 2 displays snapshots of the Q1D n -gonal ($n = 4$ –6) ice nanotubes and the corresponding Q1D liquid phases inside

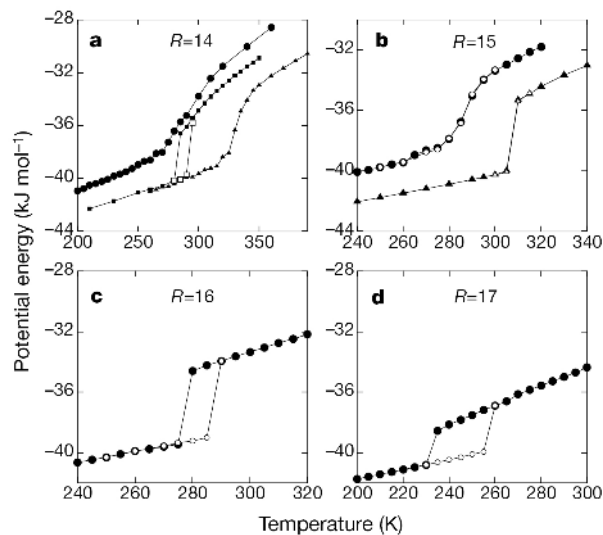


Figure 1: Potential energy against temperature for water confined in four types of single-walled carbon nanotube. The nanotubes are armchair (R,R) SWCNs, where $R = 14$ –17 (a–d, respectively). The potential energy is due to the water–water intermolecular interactions, and the water–SWCN interaction energy is excluded. The applied axial pressure is 50 MPa (circles), 200 MPa (squares), and 500 MPa (triangles). Filled and unfilled symbols indicate the cooling and heating process, respectively.

the (14,14), (15,15) and (16,16) SWCNs, showing that the disordered liquid-like structures are transformed at low T into distinct n -gonal nanotube structures with long-range order in the axial direction. The n -gonal ice nanotubes satisfy the 'bulk ice rule': every water molecule serves as a double donor and a double acceptor of hydrogen bonds, and every water molecule is hydrogen-bonded to exactly four nearest-neighbour molecules. However, a few residual defects might occur in the ice nanotubes, and this would result in interesting helical ice nanotube structure (shown in Fig. 2b). An independent chemical-potential calculation²² indicates that bulk water at a pressure of 83 MPa is in equilibrium with a hexagonal ice at $P_{zz} = 50$ MPa in the (16,16) SWCN at 260 K. The difference between external and internal pressures suggests that water can be easily drawn into the SWCNs^{4, 5} and, under moderate compression, form a hexagonal ice nanotube.

A comparison of the snapshot of the hexagonal ice nanotube with that of the liquid in the (16,16) SWCN (Fig. 2c and f) shows that the solid phase has a hollow-tube structure whereas the liquid phase has not. The radial density profile of water in the (16,16) SWCN accordingly has a distribution peak at $r = 0$ (axis of the SWCN) at higher T . This peak disappears abruptly between 275 and 280 K (Fig. 3a); that is, the system changes its 'symmetry' characteristics markedly on freezing. The abrupt symmetry change indicates that freezing in wider carbon nano-

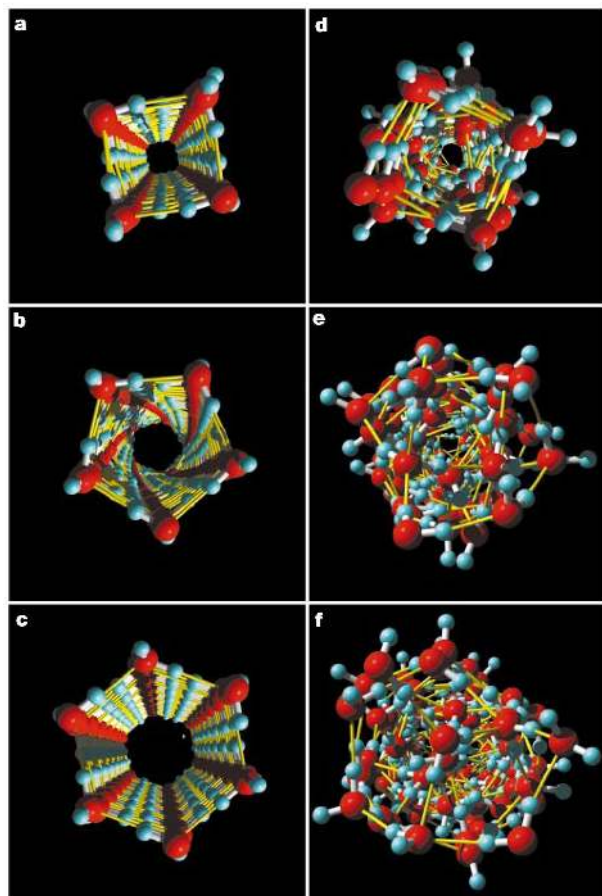


Figure 2: Snapshots of quenched molecular coordinates. a, Square; b, pentagonal; c, hexagonal ice nanotubes in (14,14), (15,15) and (16,16) SWCNs; d to f, the corresponding liquid phases. The ice nanotubes were formed on cooling under an axial pressure of 50 MPa in molecular dynamics simulations. The nearest-neighbour distances in both ice nanotube and encapsulated liquid water are fairly constant, about 2.7 to 2.8 Å, and this is in part responsible for the novel phase behaviour.

tubes is a first-order transition. This conclusion is supported by the curves of chemical potential against temperature for the confined liquid and hexagonal ice nanotube under 50 MPa, respectively (Fig. 3b). The two curves intersect at about 280 K, the melting point of the hexagonal ice nanotube, which falls within the region enclosed by the hysteresis loop shown in Fig. 1c. In the narrower (14,14) and (15,15) SWCNs, the liquid phase has a hollow-tube structure (Fig. 2d and e), in sharp contrast to the liquid phase in (16,16) SWCN. The 4-membered water-ring structure seen in the liquid phase in (14,14) SWCN resembles that of the square ice nanotube. This similarity in the structural characteristics (squareness and hollowness) of the two phases explains why the confined liquid water phase can transform continuously into the solid phase on cooling. Similar arguments apply to the pentagonal counterpart in (15,15) SWCN.

We also examined the phase behaviour at higher P_{zz} in the (14,14) SWCN. The potential energy on the 500 MPa isobar decreases smoothly with a distinct change between 320 and 340 K on cooling (Fig. 1a). On the 200 MPa isobar, however, the potential energy drops sharply at 280 K and a marked hysteresis appears on heating. On both high- P_{zz} isobars the low- T phase is the pentagonal nanotube. That is, liquid water undergoes a continuous transformation into the square-nanotube phase at 50 MPa and into the pentagonal-nanotube phase at 500 MPa, but undergoes a first-order transition to the pentagonal nanotube at 200 MPa. Figure 4a and b shows the axial and angular order parameters for square ($n = 4$) and pentagonal ($n = 5$) phases, defined by $\langle |\sum_i \exp(2\pi i N z_i / nl)|^2 / N^2 \rangle$ and $\langle |\sum_j \exp(in\theta_j)|^2 / N^2 \rangle$, where z_j and θ_j are the z -coordinate and the angle of j -th molecules in the cylindrical coordinate system, l is the length of the carbon nanotube, and $\langle \dots \rangle$ denotes the average. As expected, the two order parameters for the pentagonal phase show a sharp increase as T is lowered only when $P_{zz} = 200$ MPa.

The phase behavior of water in the (14,14) SWCN deserves special attention because it implies the possible existence of a solid-liquid critical point, which cannot occur in bulk systems¹⁷. To explore this possibility, we isothermally compressed the water stepwise from 50 to 900 MPa. In particular, long-time (200 ns) simulations were done for several P_{zz} from 250 to 330 MPa where all isotherms show a marked decline in potential energy and volume. The resulting potential-energy- P_{zz} and volume- P_{zz} isotherms are shown in Fig. 4c and d. On the 280 K isotherm, the potential energy and the volume show a sudden drop at 200 MPa on compression, and a sudden increase at 170 MPa on decompression; that is, a hysteresis loop appears. Structural analysis shows that the low-density phase

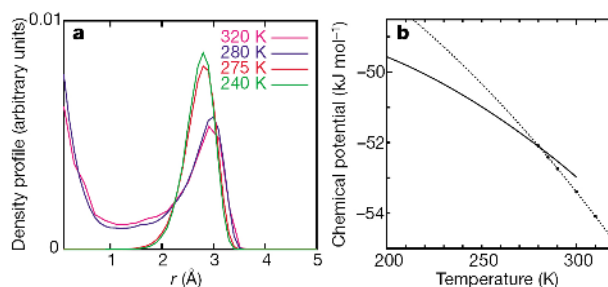


Figure 3: Properties associated with the first-order phase transition in the (16,16) SWCN at a fixed pressure of 50 MPa. a, Radial density profile of confined water at various temperatures. b, Chemical potential of liquid water (filled circles and dashed line) and the hexagonal ice nanotube (solid line) against temperature.

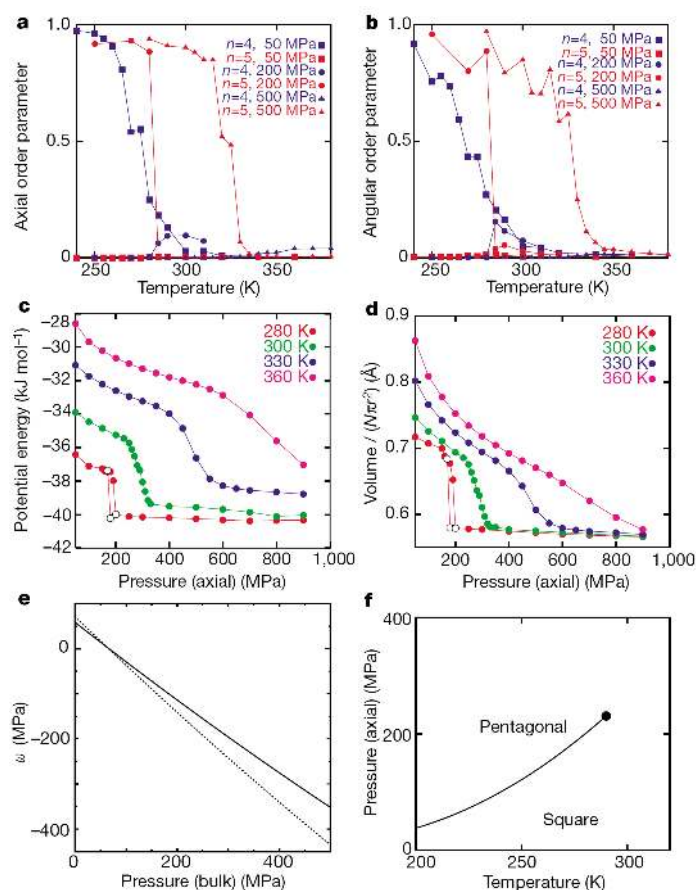


Figure 4: Properties associated with the phase transformation in the (14,14) SWCN. **a**, Axial; **b**, angular order parameters plotted against temperature for the square phase ($n = 4$) and pentagonal phase ($n = 5$). **c**, Curve of potential energy against pressure; **d**, volume against pressure. Filled and open marks indicate the compression and decompression process, respectively, **e**, Grand-potential density ω of the square ice nanotube (solid line) and pentagonal ice nanotube (dashed line) plotted against the pressure P of bulk liquid water at 260 K. **f**, Schematic temperature/axial pressure phase diagram of water. The first-order phase boundary (solid line) that divides the pentagonal-nanotube phase from the square-nanotube phase in the low- T range gradually turns into a boundary that separates the pentagonal-nanotube phase from the square-liquid phase at high T . The first-order phase boundary is terminated by a critical point (the filled circle).

is a square phase with a liquid-like disordered structure, whereas the high-density phase is a solid-like pentagonal-nanotube phase. The sudden changes in potential energy and volume evince a first-order transition between the two distinct phases. On the compressing path, the diffusion constant drops abruptly from $0.9 \times 10^{-6} \text{ cm}^2 \text{ s}^{-1}$ at 190 MPa to $1.0 \times 10^{-10} \text{ cm}^2 \text{ s}^{-1}$ at 200 MPa, which reinforces the idea that the pentagonal-nanotube phase is a solid whereas the square phase is a liquid. On the 300 K isotherm, however, the transformation seems to be continuous as no abrupt jumps in potential energy and volume are found. On the 330 K isotherm, the changes in potential energy and volume become much less abrupt, and finally on the 350 K isotherm the changes are essentially smooth.

The first-order transitions observed in the MD simulation on the 200 MPa isobar and 280 K isotherm in the (14,14) SWCN indicate that the square liquid and pentagonal ice-nanotube phases must be separated by a first-order phase boundary. The grand-potential densities (see Methods) of the square- and pentagonal-ice nanotube at 260 K have an intersection at about 65 MPa, as plotted in Fig. 4e against the pressure of bulk water. This free-energy result, independent of the MD simulation, supports the existence of a first-order phase boundary separating the square- and pentagonal-ice nanotube phase. Figure 4f is a schematic T - P_{zz} phase diagram derived from the results of MD simulations and free-energy calculations. The solid line denotes the boundary of the first-order transition. It is known that on a temperature–pressure phase diagram a first-order phase

boundary can go to infinity, intersect other phase boundaries, or end at a critical point. Here, it is most likely that the phase-boundary line is terminated by a solid–liquid critical point beyond which the pentagonal ice-nanotube and the square liquid lose their identities, because the square-to-pentagonal nanotube transformation is continuous in the high- T and high- P_{zz} region. It appears from the isotherms in Fig. 4c and d that this critical point lies between 280 and 300 K, and 200 and 300 MPa.

Methods

Molecular dynamics simulations

The TIP4P model²³ for water was used in the MD simulations, whose intermolecular potential energy is given by the sum of the long-range Coulomb potential and the short-range Lennard–Jones potential between the interaction sites. The force field of the model SWCN was taken to be a Lennard–Jones potential integrated over the cylindrical area of the SWCN using the area density of the carbon atoms and the potential parameters for graphite²⁴. A periodic boundary condition was applied in the axial direction of a tubule of length l containing 180 water molecules (182 when $R = 17$). The temperature T and the internal axial-pressure P_{zz} (the pressure tensor parallel to the axis) were maintained using a modified Nosé–Andersen’s method²⁵. The axial dimension l fluctuates to keep P_{zz} constant during a simulation; continuous change in l is possible because the force field of the model SWCN is smooth and structureless, and thus is independent of l . The simulation time at each state point (given T , P_{zz} , and R) was 10–40 ns, and at certain states was over 200 ns, which is one or two orders of magnitude longer than a typical simulation time for bulk water. Equilibra-

tion at each state point was assured by the absence of any steady drift in the properties of interest, and by reproducibility of these properties in heating and cooling (or compressing and decompressing) processes, except for the hystereses due to the first-order transitions.

Structural analysis

Instantaneous configurations generated in the MD simulations were mapped onto corresponding potential-energy local-minimum configurations via the constant-volume steepest-descent method. These configurations were used for structural analysis.

Grand-potential density

Phase equilibria of water confined in an open-ended carbon nanotube in contact with bulk water at fixed chemical potential μ and temperature T are determined from the minima of grand-potential density, $\omega = (F - \mu N)/V$, where F and V are the Helmholtz free energy and the volume of the interior. The stable phase has the lowest ω and two phases coexist if they have an identical minimum. The relation between P and μ of bulk water was obtained from the free-energy calculation for bulk water²².

Free-energy calculation

For ice inside a carbon nanotube of length l , the Helmholtz free energy, $F(T, l)$, at temperature T is calculated as a sum of four contributions: (1) the potential energy of the inherent structure, $U_0(l)$; (2) the harmonic vibrational free energy, $f_h(T, l) = k_B T \sum_{i=1}^{6(N-1)} \ln(h\nu_i/k_B T)$ where k_B and h are the Boltzmann and Planck constants, and ν_i is the frequency of the i th normal mode; (3) the anharmonic vibrational free energy, $f_a(T, l) = T \int_0^T [U_q(l) + 3Nk_B T' - U(T', l)/T'^2] dT'$, where $U(T', l)$ is the mean potential energy of ice at temperature T' ; and (4) the entropy term, TS_c where S_c is the configurational entropy arising from the disordered proton arrangement, given by $S_c = (N/n) k_B \ln 2$ for an n -gonal ice nanotube. Under a given internal axial-pressure, P_{zz} , the thermodynamic potential $G_{\text{ice}}(T, P_{zz}, l) = F(T, l) + P_{zz} A l$ has a minimum with respect to the variation of l for an arbitrarily defined inner area A . Thus, we can obtain the Gibbs free energy and the equilibrium length $\langle l \rangle$ as functions of P_{zz} , which generally differs from the pressure P of the bulk water. For liquid water in a SWCN, the interaction potential can be divided into the water-water interaction Φ_1 and the interaction of water molecules with carbon Φ_2 . The free energy is given by

$$F(T, l) = F_0(T, l) + \int_0^l d\lambda (4\lambda^3 \Phi_1)$$

where $\langle \dots \rangle$ stands for the ensemble average of the system interacting with the potential ($4\lambda^3 \Phi_1 + \Phi_2$) and $F_0(T, l)$ is the free energy of the ideal gas interacting only with carbon.

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