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Authors

Heckman, H.H. Greiner, D.E. Lindstrom, P.J. <u>et al.</u>

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LBL-3656

FRAGMENTATION OF 4 He, 12 C, 14 N, and 16 O NUCLEI IN

NUCLEAR EMULSION AT 2.1 GeV/NUCLEON

H. H. Heckman, D. E. Greiner, P. J. Lindstrom, and H. Shwe

Lawrence Berkeley Laboratory and Space Sciences Laboratory University of California, Berkeley, California 94720

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ABSTRACT

A comparative study of the fragmentation of ⁴He, ¹²C, ¹⁴N, and ¹⁶O nuclei, E=2.1 GeV/nucleon, has been made by using nuclear emulsion detectors. The interaction mean-free paths (cm) for these nuclei in emulsion are 21.8 ± 0.7 , 13.8 ± 0.5 , 13.1 ± 0.5 , and 13.0 ± 0.5 , respectively. These data are discussed in terms of optical models and geometrical theories. Fragmentation reactions initiated by ¹²C, ¹⁴N, and ¹⁶O projectiles that exhibit no target excitation, i.e., that possess no low-energy particle emission, are selected for special study of projectile fragmentation. The projected angular distributions of Z=1 and 2 secondaries from these interactions are reported, as are the prong-number and charge-multiplicity distributions. The angular distributions are independent of the projectile and exhibit features of limiting fragmentation.

KEY WORDS

NUCLEAR REACTIONS Emulsion exp., ⁴He, ¹²C, ¹⁴N, and ¹⁶O at 2.1 GeV/A; measured mean-free-path lengths; projectile fragmentation reactions; angular, number and charge multiplicity distributions. Optical and geometrical models; limiting fragmentation.

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I. INTRODUCTION

With the discovery of heavy nuclei in primary cosmic rays in 1948,¹ studies of the nucleus-nucleus interaction at high energies became possible. Early work was concerned with interaction mean-free paths and the production of fragments, as these data were most pertinent to the physics of cosmic rays.² Although encumbered by the low intensities and uncertainties in charge and energy determination of the heavy nuclei, later cosmic-ray experiments have revealed many of the general features of the nucleus-nucleus interaction, e.g., production of shower particles, alpha-particle production from both target and projectile nuclei, production of heavy nuclei.³⁻⁹ In these experiments, as in the present one, the nuclear research emulsion was used as the target and detector.

In this paper we present experimental results on the interactions in nuclear research emulsions of ⁴He, ¹²C, ¹⁴N, and ¹⁶O nuclei accelerated to 2.1 GeV/nucleon at the Bevatron. The interaction mean-free paths measured for these ions are compared with optical-model calculations, and are also presented in terms of a two-parameter expression for the geometrical cross section (Sec. III-A). These parameters are r_0 , the constant of proportionality defined by the expression for the nuclear radius $r_i = r_0 A_i^{1/3}$, and b, the overlap parameter. The quantity b is equal to $\Delta r/r_0$, where Δr is the geometrical overlap between the colliding nuclei. In this experiment we find that about 12 percent of the interactions of ¹²C, ¹⁴N, and ¹⁶O beam particles with emulsion nuclei lead to "pure" projectile fragmentation, characterized by no detectable target fragmentation, i.e. no low-energy, charged-particle emission in the interaction. We have selected these interactions for specific study of the projected angular distribution for charge Z=1 and 2 secondary fragments (Sec. III-B) and of the topological features

of the fragmentation of ${}^{12}C$, ${}^{14}N$, and ${}^{16}O$ nuclei, presented in terms of the prong-number and charge-multiplicity distributions (Sec. III-C).

An interesting aspect of this experiment is the possibility for interpreting the angular distribution measurements in terms of the hypothesis of limiting fragmentation.¹⁰ Because of the large separation in rapidity $(y=tanh^{-1}\beta_1)$ between the projectile and target fragments at relativistic energies, limiting fragmentation dictates that no correlations exist between the projectile and target fragments. Bevatron experiments on the 0° fragmentation of relativistic heavy-ion projectiles at E=1.05 and 2.1 GeV/nucleon have shown that the modes of fragmentation are independent of the mass of the target nucleus, 11-13 a result that is compatible with the principle of limiting fragmentation. Consequently, the fragmentation cross sections for the reaction $B+T\rightarrow F+--$ can be factored according to $\sigma_{BT}^F = \gamma_B^F \gamma_T$, where γ_B^F is a function of the beam B and fragment F nuclei; and γ_{T} , the target factor, is a function of target T. Exceptions of strict factorization have been observed for fragmentation reactions in hydrogen (where $\gamma_{\rm T}$ exhibits a weak dependence on the mass of fragment F),¹³ in helium,¹⁴ and for heavy targets where single-nucleon stripping is enhanced by the Coulomb dissociation of ^{12}C and ^{16}O projectiles in the virtual photon field of the target nucleus.^{13,15} By selecting interactions in emulsion with no visible target fragmentation, we have defined a subset of interactions where the nature of the reaction is specified in the lowrapidity region. Thus, a comparison of the angular distribution of the high-rapidity projectile fragments measured in this experiment with the results of the single-particle inclusive experiments of Greiner et al., where there were no restrictions on the fragmentation of the target, provides for a more stringent test of the limiting fragmentation hypothesis.

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II. PROCEDURE

The emulsion stacks used in this experiment were fabricated from Ilford G.5 pellicles, 600 microns thick. The stacks were exposed to beams of 2.1-GeV/nucleon ⁴He, ¹²C, ¹⁴N, and ¹⁶O nuclei parallel to the emulsion planes. The scanning technique for each beam was to select an incident ion 1 to 2mm from the entrance edge and scan along the track until the ion interacted or left the pellicle. The beginning and terminal points of each track segment were recorded by three-coordinate digitized microscopes with one micron read-out accuracy. Recorded for each interaction were beam type, the event number, the emulsion plate number and grid coordinate (a 1mm grid system was photographed on the emulsion glass interface of each pellicle), the number, and, for relativistic secondaries, the charges of the secondary fragments. The interactions were qualitatively classified as to type, depending upon their visual characteristics.

- Type 1 Projectile fragmentation only. No visible target fragmentation. Also denoted as $n_h=0$ events, where n_h is the number of non-relativistic particles emitted from the interaction.
- Type 2 Projectile fragmentation with target breakup, $n_h \ge 1$.
- Type 3 Catastrophic destruction of projectile and target nuclei. No forward-cone fragments from the projectile are evident.

Type 4 Target fragmentation only. No detectable change in charge of projectiles, i.e., the inverse of Type 1.

We have selected events of Type 1 for special examination in that they represent the "cleanest" examples of projectile fragmentation. These events were intensively examined for all secondary fragments. Because the velocities of nuclear fragments of the beam projectile are near the velocity of the beam, $\beta = 0.95$, the grain densities of the secondary tracks are related to Z^2 of the fragment. Charge estimates for ionizing tracks $Z \leq 3$ were thus greatly simplified, requiring only rudimentary grain-density measurements. All secondary tracks with $Z \geq 4$ were grouped together, and no systematic attempt was made to resolve these higher charges. However, although not fundamental to the analysis of the data, charge estimates of all tracks were made by the scanner-measurer by inspecting the relative ionization rates of the incident beam and secondary particles.

The spatial configuration of each event was reconstructed by measuring a pair of x, y, z coordinates separated by at least 500 microns, on each of the primary and secondary tracks. These coordinate data were digitally recorded on magnetic tape accompanied by pertinent indicative information. The projected angular resolutions between two track segments attained in these measurements was $\pm 0.16^{\circ}$ (S.D.) in the horizontal plane and $\pm 0.39^{\circ}$ in the vertical plane,

III. RESULTS AND DISCUSSION

A. Interaction mean-free-path lengths

The path length followed for each species of beam was sufficient to obtain at least 10^3 interactions. Table I presents a breakdown of these interactions into the numbers observed for Types 1-4, N₁ through N₄, and their sum, N_{obs}. An analysis of the data obtained from the original scanning led us to conclude that the scanning efficiency was near 100% for events in which the difference between the charges of the beam and principal fragment is $\Delta Z=Z_B-Z_F \ge 2$. However, events for which $\Delta Z=0$ or 1, e.g. when the projectile undergoes neutron or proton stripping, tend to be missed.

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Of particular concern are those fragmentation events that exhibit little or no evidence for excitation of the target nucleus. Clearly, events of Type 1 in which the projectile undergoes neutron loss are undetectable in the emulsion. Also, Type 1 events that involve the loss of a single charge by the projectile, where the resulting fragment proceeds with no noticeable change in direction (whether or not it is accompanied by a minimally ionizing Z=1 particle), become progressively more difficult to detect as the charge of the projectile increases. These conjectures were confirmed upon rescanning about one-third of the ${}^{12}C$, ${}^{14}N$, and ${}^{16}O$ track data. Out of 1059 events, the rescanning contributed 16 new events, all of which were Types 1 or 4, having $\Delta Z=0,1$ only. No new Type 2 or 3 events were detected.

To correct N_{obs} for these scanning biases we have used the isotope production cross sections of Lindstrom <u>et al.</u>^{13,17} to compute the probabilities for $\Delta Z=0$ and 1 fragmentation events for ¹²C and ¹⁶O ions in emulsion at 2.1 GeV/nucleon. These probabilities are 16.1% and 16.4%, respectively. The final corrections to N_{obs} are summarized in Table II. The largest correction for missed $\Delta Z=0,1$ events is for ¹⁶O, where 39% (or about 4% of N_{total}) of these types of events are undetected. Owing to improved detection efficiency for these events as Z decreases, this fraction decreases to 1% for ¹²C, indicating that the loss of $\Delta Z=0,1$ events for ⁴He beams is also small. We have, therefore, made no corrections to the ⁴He data.

Listed in Table I are the numbers of events, $N_{\Delta Z} \ge 1$, for which the charge of the principal fragment differs from that of the incident ion by $\Delta Z \ge 1$. The mean-free path derived therefrom can be directly compared with experiments that rely on the differences in $\frac{dE}{dx}$, hence charge, between the incident and fragment nuclei to signify an interaction.¹⁸ Table I concludes

with the measured interaction mean-free paths, $\lambda_{total}(cm)$ and $\lambda_{\Delta Z \ge 1}(cm)$ in nuclear emulsion for ⁴He, ¹²C, ¹⁴N, and ¹⁶O nuclei, E=2.1 GeV/nucleon.

The C, N, and O data confirm, within the accuracies of the cosmic-ray experiments, the mean values of the interaction mean-free paths for cosmicray M-nuclei (6 \leq Z \leq 9) in emulsion as summarized by Cleghorn,¹⁹ and Waddington.²⁰ The average of all measurements of $\lambda(M)$ cited in Refs. 19,20 gives an energy-independent interaction mean-free path of 13.3 ± 0.6 cm. Recent measurements of the mean-free path of Bevatron-accelerated 2.0 GeV/ nucleon 16 O ions in emulsion, have been made by Jakobsson et al. 21 (13.7 ± 1.1 cm) and Judek²² (12.6 ± 0.5 cm). Our measured value of λ (He) = 21.8 ± 0.7 cm is 15 ± 5% greater than the average value of λ (He) = 18.9 ± 0.8 cm evaluated from the summary given by Lohrmann and Teucher²³ for the interactions of cosmic-ray primary and secondary α -particles (the latter from the fragmentation of heavy nuclei) in emulsion at kinetic energies E > 6 GeV/nucleon. Neither the cosmic-ray results nor the individual contributions from our five scanners to our α data showed any significant anomalies that could account for the differences between the respective values of λ (He). In view of possible differences in scanning and selection criteria, uncertainties in the identification of cosmic-ray alpha nuclei, and the provocative evidences that the interaction path lengths of light secondary nuclei exhibit anomalously short mean-free paths,^{19,22} a resolution of this difference must await further experimental inquiry.

An empirical expression for the interaction cross section that traditionally has been used to interpret the data given in Table I is the geometrical formula first proposed by Bradt and Peters²⁴

$$\sigma_{\rm BT} = \pi r_{\rm o}^2 (A_{\rm B}^{1/3} + A_{\rm T}^{1/3} - b)^2, \qquad (1)$$

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where A_{B} and A_{T} are the mass numbers of the beam and target nuclei respectively; b is the overlap parameter, and r_0 is the constant of proportionality in the expression for the geometrical nuclear radius $r_i =$ r_A , ^{1/3}. Consistent fits to heavy-ion reaction cross-section data have been reported for r and b in the ranges $1.15 \le r_0 \le 1.45$ fm and $0 \le b \le 1.45$ 1.5, 19,24,25 owing to the fact that the parameters r and b are coupled. This is exemplified in the present experiment where, with an assumed constant overlap parameter b for all elements in emulsion, the mean-free path data can be fitted, by using Eq. 1, to confidence levels < 25% ($\chi^2 \leq$ 2.7 for two degrees of freedom) when r_0 and b are in the range $1.44 \leq r_0$ \leq 1.72 fm and 1.28 \leq b \leq 1.92. The calculated mean-free path lengths are given by the expression $\lambda_{calc} = (\Sigma_i n_i (T) \sigma_{BT})^{-1}$, where $n_i(T)$ is the number of target nuclei T per milliliter in emulsion, 26 and $\sigma_{\rm BT}$ is the interaction cross section--taken to be Eq. 1 in this case. However, the transmutation cross sections ($\Delta Z \ge 1$) measured by Lindstrom et al,¹⁷ for ¹²C and ¹⁶O, E=2.1 GeV/nucleon, give evidence that the overlap b is not constant, but depends upon the mass, i.e., radius, of the beam nucleus. From any geometrical description of nuclei, one can intuitively argue that the b parameter should be dependent on the radii of colliding nuclei. We have found that the theoretical results of Barshay, Dover, and $Vary^{27}$ and Karol²⁸ are particularly useful in addressing this problem.

In their investigation on the question of the validity of factorization of total cross sections in nucleus-nucleus collisions, Barshay <u>et al.</u>²⁷ calculated the total reaction cross sections using a geometrical nuclear model and an impact parameter representation of the scattering amplitude, which can be considered to be the optical limit of the Glauber theory. In the same limit, Karol has derived an analytical approximation for the total nucleus-nucleus reaction cross section²⁸ that gives values in good agreement with those given by Barshay <u>et al</u>. Karol's "soft-spheres model" utilizes the experimentally-measured density distribution parameters (i.e., half-central-density radius and the 90%-10% surface-skin-thickness parameter) and energy-dependent nucleon-nucleon cross sections.

To fit the measured mean-free path data to the optical model, we employ Karol's analytical expression for the reaction cross section, σ_{BT} , taking the average nucleon-nucleon cross section, $\overline{\sigma}$, to be given by $K\overline{\sigma}(\ell.1)$ where $\sigma(2.1)$ is the average nucleon-nucleon cross section at 2.1 GeV, and K is an adjustable parameter. The best fit to the experimental data is obtained when K = 0.52 ± 0.06 , which corresponds to effective proton-proton (neutron-neutron) and proton-neutron inelastic cross sections of 23.1 ± 1.3 mb and 22.2 ± 1.3 mb, respectively.

Using the effective nucleon-nucleon cross section $\overline{\sigma}$ thus determined, we now examine the possibility of presenting the calculated reaction cross section of Karol and Barshay <u>et al</u>. in the form of the Bradt-Peters relation, Eq. 1. We find that the calculated nucleus-nucleus reaction cross sections do exhibit the form of Eq. 1, to excellent approximation, when the cross sections are ordered to A_{min} , the lighter of the beam and target nuclei. In Fig. 1 we plot $\sigma_{BT}^{1/2}$ versus $A_B^{1/3} + A_T^{1/3}$, where σ_{BT} is computed for a large variety of nuclei, using the effective nucleon-nucleon cross section $\overline{\sigma} = 0.52 \ \overline{\sigma}(2.1)$. The computational results display a family of approximately parallel lines, each identified with a given A_{min} , whose slope is r_0 and intercept with the abscissa is the mass-dependent overlap parameter $b(A_{min})$. In Fig. 2ab we present the results of a least-squares fit to a number of sets of computed cross sections, each designated by $A_{min} (\subseteq A_B)$ with $A_T \ge A_{min}$, from which we have deduced r_0 and b (A_{min}) as

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a function of A_{min} . The fits to the calculated cross sections reveal that r_o , Fig. 2a, is insensitive to A_{min} , with the systematic variations in r_o being less than the typical statistical error for r_o . The mean value of r_o for all A_{min} , $1 < A_{min} < 60$ is $\overline{r}_o = 1.36 \pm 0.02$ fm. The overlap parameters $b(A_{min})$, Fig. 2b, are all positive, which indicates that a finite overlap of the colliding nuclei, hence, nuclear transparency, is necessary to produce visually detectable reactions in nuclear emulsion. Qualitatively, the overlap parameter is largest for the light nuclei. It decreases approximately linearly until $A_{min} \approx 30$, then becomes constant for $A_{min} \gtrsim 30$. Thus, for heavy nuclei the cross sections approach those characteristics of the geometric cross section $\sigma = \pi r_o^2 (A_B^{1/3} + A_T^{1/3})^2$.

Vary²⁹ has shown that Glauber (nucleus-nucleus scattering) amplitudes lead to a total nucleus-nucleus reaction cross section that can be expressed in the Bradt-Peters form, given by

$$\sigma = \pi r_0^2 \left[A_B^{1/3} + A_T^{1/3} - b_0 (A_B^{-1/3} + A_T^{-1/3}) \right]^2 fm^2, \qquad (2)$$

where $r_0 = 1.36$ fm and $b_0 = 0.75$. In the overlap term $b = b_0 (A_B^{-1/3} + A_T^{-1/3})$, the quantities $A^{-1/3} \propto r^{-1}$ are identified with effects due to the curvature of the nuclear surfaces. Although Vary's expression for b includes contributions from both interacting nuclei, the general feature of b is that its value is dominated by the smaller nuclear mass, and becomes insensitive to changes in A_B and A_T when they are large, a behavior qualitatively similar to that illustrated in Fig. 2b.

To relate the mean-free path data of this experiment to Vary's expression, Eq. 2, we take the following approach: i) because of the insensitivity of r_0 to both A_{min} , Fig. 2a, and the average nucleon-nucleon cross

section $\overline{\sigma}(\Delta r_o/r_o \approx -0.03 \text{ when K increases from 0.4 to 1.0})$, we assume r_o is constant, equal to 1.36 fm, and ii) because changes in $\overline{\sigma}$ are therefore principally contained in the overlap parameter b, we take b_o as an adjustable parameter in Eq. 2 to fit the mean-free-path lengths, Table I. In Table III we give the results of this analysis, and list the measured and computed mean-free-path lengths using the cross sections σ_{BT} evaluated with the fitted parameters K = 0.52 in the soft-sphere model and $b_o = 1.11$ in Eq. 2.

Finally, having determined the parameters K and b_0 from our measured path lengths in emulsion, we are able to compare directly the nucleusnucleus cross sections implied by the emulsion data with those measured by Lindstrom <u>et al.</u>¹⁷ for several target nuclei. This is done in Table IV.

Thus, we find that, by using as adjustable parameters the average nucleon-nucleon cross section $\overline{\sigma}$ in the soft-sphere model and b_o in Vary's expression, the mean-free-path theories of ⁴He, ¹²C, ¹⁴N, and ¹⁶O can be well accounted for by the respective therories. However, the one-parameter approach we have taken to fit the emulsion data clearly fails for hydrogen targets, as indicated in Table IV. Because the emulsion data require an effective nucleon-nucleon cross section that is about 50 percent of the free nucleon-nucleon cross section at 2.1 GeV, we are led to the conclusion that the effective nucleon-nucleon cross section for nucleon removal, i.e., transmutation, in heavy-ion collisions (the only type of reaction detectable in emulsion) is significantly suppressed in nucleus-nucleus collisions. This argument is supported by the agreement between the cross sections deduced from this experiment and those measured by Lindstrom et al.,¹⁷ Table IV. The notable disagreement for hydrogen targets implies that, for this case, the effective nucleon-nucleon cross section is within about 10%

of nucleon-nucleon inelastic cross section. The dichotomy between the $\overline{\sigma}_{\rm NN}$'s to account for the nucleon-nucleus and nucleus-nucleus transmutation reactions appears to be real, and one that requires further theoretical and experimental investigation.

We find it provocative that the reaction cross sections given by Karol²⁸ and Barshay <u>et al.</u>,²⁷ exhibit the form of the Bradt-Peters relation, albeit modified in that the overlap parameter b is now a function of A_{min} . Although the representation of the theoretical cross sections in such a geometrical model may not be entirely valid, the parameters r_0 and b deduced from the optical-model theories are physically realistic.

B. <u>Angular distributions of Z=1 and 2 secondaries from projectile</u> fragmentation

The measurements of single-particle inclusive spectra by Greiner <u>et</u> <u>a1</u>.¹⁶ have shown that the longitudinal momentum distributions of secondary nuclei produced by the fragmentation of ¹²C and ¹⁶O beam projectiles are typically Gaussian-shaped in the projectile rest frame, and have widths (S.D.) from about 50 to 200 MeV/c that depend only on the fragment and beam nuclei. To about 10% accuracy, these characteristics of the momentum distributions are independent of the target. Our present study of projectile fragmentation in nuclear emulsion uses a sample of ($n_h = 0$) events in which no low-energy charged particles were produced in the interaction. Because these particular events show no visual evidence of target excitation, they are taken to represent nuclear collisions that occur at large impact parameters.

Figure 3 is an example of a "pure" projectile-fragmentation event in emulsion, typical of the interactions selected for this investigation.

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Here, a 2.1-GeV/nucleon ¹⁴N nucleus fragments into three Z=2 secondaries and one Z=1 secondary. Approximately 100 fragmentation events of the type illustrated were observed for each of the ¹²C, ¹⁴N, and ¹⁶O beams. Note that the absence of any low-energy target-associated prongs precludes target identification. Under this criterion, most, if not all, hydrogen target events are excluded, because such interactions would be classified as n_h =1 events owing to the recoil of the target. In fact, several examples of hydrogen-target-induced fragmentations were kinematically identified.

Figures 4, 5, and 6 present, respectively, the composite projected angular distribution for Z=1 and Z=2 secondaries from the fragmentation of ¹²C, ¹⁴N, and ¹⁶O nuclei at 2.1 GeV/nucleon. The angular distribution data were combined because we observed no statistically significant difference between them, and, based on the results of Greiner et al.¹⁶ and Lepore and Riddell,³⁰ we expected none. Because the nuclear fragments of the projectile proceed with velocities nearly equal to that of the incident ion, the secondary nuclei have energies ≈ 2.1 GeV/nucleon, hence ionization-loss rates $\approx Z^2 (dE/dx)_{min}$. The Z=1 and Z=2 secondary nuclei are thus easily identified by their differences in grain density (see Fig. 3). The composition of Z=1 secondaries includes, in fact, all singly-charged particles (p, d, π , etc.) having grain densities $g \leq 1.4$ Low-velocity Z=1 secondaries with grain densities about 4 g_{min} g_{min}. can, in principle, be included in the Z=2 data. However, such tracks tend to display large multiple scattering that would affect their elimination from the sample. The Z=2 data are therefore predominantly He nuclei.

The projected angular distribution for Z=1 particles, Fig. 4,

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shows a peaked distribution at 0° with respect to the beam direction. with about 99% of all secondaries restricted to the forward hemisphere. In Fig. 5 we show the structure of the Z=1 distribution for $\theta_{proj} \leq 16^{\circ}$. The projected angular distribution has a narrow central peak, superimposed upon, and distinct from, a broader distribution. The observed projected angular distribution for Z=2 secondaries is given in Fig. 6. This distribution is dominated by a narrow forward peak, having a characteristic width $\approx 1^{\circ}$. There is evidence for production angles significantly greater than can be associated with the central distribution, although all Z=2 secondaries are confined to $\theta_{\text{proj}} < 7^{\circ}$.

To interpret the Z=1,2 angular distributions (Figs. 5 and 6), we refer to the experiments of Greiner $\underline{et} \underline{al}$, $\frac{16}{}$ and to the work of Lepore and Riddell.³⁰ The latter authors have treated the fragmentation of highenergy nuclei by a quantum mechanical calculation using the sudden approximation and shell-model functions and have shown that a) the projected momentum distributions in the projectile frame are, to good approximation, Gaussian, with equal standard deviations, and b) the standard deviation widths of these distributions are to first order given by:

$$\sigma = \left[m_{p} \omega A_{F} (A_{B} - A_{F}) / 2A_{B} \right]^{1/2} \text{ MeV},$$

where $A_{\mathbf{B}} = \text{mass number of beam}$ $A_{\rm F}$ = mass number of fragment $m_p = mass of proton, and$ $\omega = 45 A_{\rm B}^{-1/3} - 25 A_{\rm B}^{-2/3}$

(3)

In Table V we tabulate the average momentum-widths $\sigma(S.D.)$ for the CNO group, as measured by Greiner et al. and evaluated from Eq. 3, and the corresponding angular widths $\sigma(\theta_{proj})$ for the Z=1,2 isotopes. To intercompare the data in Table V, one must bear in mind that the longitudinal momentum data of Greiner et al.¹⁶ are based only on production angles less than 0.72°. Within this acceptance angle the longitudinal momentum spectra for all isotopes were Gaussian shaped (in the projectile frame), with the exception of the spectrum for protons, which was consistently exponential in shape. For purposes of Table V, however, we have taken all momentum widths to be $\sigma(S.D.)$. From the isotopic production cross-section data of Lindstrom \underline{et} al., 13 we estimate the production ratios in nuclear emulsion for the hydrogen isotopes to be p:d:t = 1:0.25:0.1; and for the helium isotopes 4 He: 3 He = 1:0.31, Included in Table V are the resultant weighted values of $\sigma(\theta_{proj})$ for the Z=1,2 isotopes, denoted as $\sigma_{Z=1}$ and $\sigma_{Z=2}$, which are the standard deviations of the projected angular distribution of Z=1 and 2 secondary nuclei produced by the fragmentation of 2.1-GeV/nucleon ^{12}C , ^{14}N , and 16 O projectiles that are to be compared with the experimental results (Figs. 5 and 6).

Referring to Fig. 5 we find that the narrow, forward peak of Z=1 fragments can be fitted by a Gaussian distribution, having a width consistent with the values $\sigma_{Z=1}$ of 1.35-1.45 given in Table V, provided the large-angle background events can be described by a Gaussian distribution, $\sigma \approx 7.5$, whose amplitude is about 1/3 that of the central peak. The large-angle events are primarily pions, although nucleons with high transverse momenta, as suggested by the fireball model,³¹ may be present. Specifically, if we use the temperature and velocity of the projectile-

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fireball estimated by Westfall et al.,³¹ i.e., $\beta=0.91$ and $\tau=66$ MeV, the width of the momentum distribution, assumed to be Maxwellian, is $\sigma \sqrt{m \pi}$ = 250 MeV/c. The corresponding width of the projected angular distribution for protons is $\sigma(\theta) {\sim} 7^\circ$, compatible with the 7.5° S.D. of the observed background. Drawn through the data points in Fig. 5 are curves of the form N(θ)=A exp $\left[-\frac{\theta^2}{(2\sigma_1^2)}\right]$ + B exp $\left[-\frac{\theta^2}{(2\sigma_2^2)}\right]$, calculated for two values of σ_1 , 1.3° and 1.5°, and $\sigma_2 = 7.5^\circ$. The amplitudes B of the large-angle background distribution illustrated in Fig. 5 are 0.065 and 0.073, and are indicative of the sensitivity of $\sigma_1 \approx \sigma_{Z=1}$ upon background subtraction. Thus, although an accurate estimate of the width of the central peak is not possible, owing to the uncertainty in the spectral shape of the large-angle component, this analysis does lead to the conclusion that the central peak in the Z=1 projected angular distribution is due to the hydrogen isotopes produced in the fragmentation of the projectile. The distribution is consistent with being a Gaussian, whose σ width is in satisfactory agreement with the experiments of Greiner et al.¹⁶ and the first-order theory of Lepore and Riddell.³⁰

Figure 6 shows the projected angular distribution for the He isotopes from the fragmentation of ¹²C, ¹⁴N, and ¹⁶O nuclei in emulsion projected in the emulsion plane (actually in the <u>x-y</u> plane, where <u>x</u> is along the incident beam track and <u>y</u> is in the plane of the emulsion). Drawn through the distribution is a Gaussian curve whose standard deviation σ is evaluated from data restricted to $\sigma_{\text{proj}} \leq 1.5^{\circ}$. Correcting the measured widths for measurement error ($\Delta \theta = 0.16 \pm 0.03^{\circ}$), we obtain $\sigma_{Z=2}$ (horiz) = 0.65 ± 0.02^{\circ}. A similar analysis for the vertical plane gives $\sigma_{Z=2}$ (vert) = 0.61 ± 0.05^{\circ}, the increase in the error being attributable to the vertical shrinkage of the processed emulsion. Thus, within the errors of this experiment, the transverse momentum distributions for He nuclei projected onto orthogonal planes in the emulsion are equal. The weighted average is $\sigma_{Z=2} = 0.64 \pm 0.02^{\circ}$.

This measurement of the standard deviation of the projected angular distribution for Z=2 fragments appears to be slightly less than that expected from the longitudinal momentum distribution measured by Greiner et al. and given by Lepore and Riddell, i.e., $\sigma_{Z=2} = 0.73^{\circ}$, Table V. Because the value $\sigma_{Z=2} \approx 0.64^{\circ}$ was obtained for angles $\theta_{\text{proj}} \leq 1.5^{\circ}$, hence for angles $\leq 2\sigma_{Z=2}$, the contributions of large, non-Gaussian production angles to the standard deviation are suppressed. Thus, the quoted result properly represents a lower limit of $\sigma_{Z=2}$. We therefore argue that the projected angular distributions of hydrogen and helium nuclei produced by the fragmentation of 12 C, 14 N, and 16 O projectiles at 2.1 GeV/ nucleon observed in this experiment are in agreement with those expected from the p - distributions measured by Greiner et al., and that to about a 10% level, the momentum distributions of Z=1 and 2 nuclei in the projectile frame are consistent with isotropy.

The principal conclusion we come to, then, is that the projected angular distributions for both Z=1 and Z=2 fragments emitted from $n_h=0$ type events in emulsion are in agreement with the single-particle inclusive spectra.¹⁶ Thus, when we compare the momentum distributions of fragments measured in single-particle inclusive experiments--fragments that are selected only on the basis of their high rapidity (without knowledge of the low-rapidity region)--with the momentum distributions of fragments produced in interactions selected on the bases of the presence of high-rapidity fragments and knowledge of the state of the target-

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rapidity region, we find no difference between them. This result is a characteristic feature of the hypothesis of limiting fragmentation.

The general features of the angular distribution for Z=1 and 2 secondaries that are portrayed in Figs. 4-6 have been well documented in cosmic-ray heavy-ion experiments. The low intensity of heavy nuclei in the cosmic rays has limited these experiments to studies of the nucleus-nucleus interaction averaged over all impact parameters and Pertinent to this discussion is the work of Andersson et al., energy. who examined the angular distribution of shower particles, i.e., highenergy Z=1 particles produced in nucleus-nucleus collisions in emulsions by cosmic-ray heavy ions, $3 \le Z \le 26$, $E \ge 1.7$ GeV/nucleon, as a function of n_{h} . They found that as n_{h} increased from the interval $2 \leq n_{h} \leq 6$ to $n_{\rm h} \geqslant 20$, the probability for a Z=1 fragment from the incident projectile to appear within the "proton" peak ($\theta \leq 2.2^{\circ}$) decreased from 0.40 ± 0.08 to approximately zero (no signal above background). To compare this result with the $(n_{h}=0)$ events examined in this experiment, we find that 0.40 ± 0.02 of the Z=1 particles from CNO projectiles are within θ_{proj} $\leq 2.0^{\circ}$. Thus, the amplitude of the Z=1 fragments produced within $\sim 2^{\circ}$ of the direction of the incident heavy ions does not depend critically on the n_h for $n_h \leq 6$. The results of Andersson <u>et al.</u>, therefore, allow us to extend the application of the concept of limiting fragmentation to target-projectile interactions that exhibit a small, but finite number of target prongs in the low-rapidity region. Thus, there is evidence that projectile fragmentation distributions remain uncorrelated with target fragmentation for $n_h \approx 6$.

C. Prong number and prong multiplicity distributions

To demonstrate some of the topological features of the fragmentation process for the $n_h=0$ type interactions, we plot in Fig. 7 the chargedprong number (n), and in Fig. 8 the charge-multiplicity (Z*) distributions of the secondary fragments as a function of Z_{max} , the charge of the principal fragment, i.e., highest Z produced in the fragmentation of ¹²C, $n^{14}N$, and ¹⁶O projectiles. The quantity $Z^{*=\Sigma}_{=\Sigma} |Z_i|$, is the sum of the (absolute) charges of the n secondary particles. Table VI presents the production frequency of events also categorized according to Z_{max} . These data have been corrected for scanning losses for events $Z_{max} \ge 4$ (Table II). Because of the small number of events observed to have $Z_{max} \ge 4$ and the cited difficulties in their detection, we shall limit our discussion to fragmentation events that have $1 \le Z_{max} \le 3$ only; events for which scanning losses are negligible.

Before discussing some of the details presented in Figs. 7 and 8, we wish to point out that in no case, out of 1000 observed interactions for each of the ${}^{12}C_{,}$ ${}^{14}N$, and ${}^{16}O$ beam projectiles, did we observe a fragmentation event that yielded two or more secondaries with z > 2, irrespective of the amount of target excitation. Thus, two-product fragmentation events, such as ${}^{14}N \rightarrow {}^{7}Be + {}^{7}Li$ were not observed. The cross section for their production is therefore $\approx 10^{-3}$ of the total reaction cross section.

Notable features of the data presented in Figs. 7 and 8 are:

i) For Z_{max} =1 events (where all fragments are singly charged, hence, include only the hydrogen isotopes and mesons of both charges) the number of prongs (Fig. 7) are in all cases equal to, or greater than, the atomic number of the projectile. The largest number of prongs detected

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in this sample is a ¹⁴N, Z_{max}=1 fragmentation that has 15 minimallyionizing secondaries. The excess of 8 charged particles, if we assume 7 of the charges are due to hydrogen isotopes from the ¹⁴N projectile, implies that multiple-pion production can occur in nucleus-nucleus collisions, even though the target nucleus (if it is not hydrogen) does not receive sufficient excitation energy to emit particles.

ii) Fragmentations in which $Z_{max}=2$, i.e., no fragments with charge $Z \ge 2$, is a highly probable configuration for all projectiles. The ${}^{12}C \Rightarrow 3\alpha$ reaction is the only contributor to the 3-prong, $Z_{max}=2$ events for carbon, as is the ${}^{14}N \Rightarrow 3$ He + H reaction to the 4-prong events in nitrogen, each comprising about 10% of their respective $n_h=0$ events. The 4-alpha breakup of ${}^{16}O$ is considerably less probable than the ${}^{12}C \Rightarrow 3\alpha$ reaction, occurring in only about 1% of the $n_h=0$ ${}^{16}O$ events. We note also that complete breakup into Z=1 fragments is less probable for ${}^{16}O$ than it is for ${}^{12}C$ and ${}^{14}N$.

iii) The topologies of ¹²C and ¹⁶O fragmentations are the same--the differences between them being attributable primarily to the differences in the masses of these projectiles. The $\langle n \rangle$ values for ¹²C and ¹⁶O show the same trends for each Z_{max} ; for example, within the errors of the data, $\langle n \rangle (^{16}O) \approx \langle n \rangle (^{12}C) + 2$. Also, the excess of charge Z^*-Z_B observed in the fragmentation products of ¹²C (0.7 \pm 0.1) and ¹⁶O (0.9 \pm 0.1) is approximately 10% of the charge of the incident ion,

iv) Three events were observed in which the net charge emitted from the interaction (12 C and 16 O) is one unit of charge less than the charge of projectile. Although undetected singly-charged tracks could account for them, the number of such events can be accounted for by charge-exchange (p \rightarrow n) reactions between the projectile and target nucleons, provided the cross section is the order of 100 µb.

v) The fragmentation of ¹⁴N nuclei shows differences when compared with the ¹²C and ¹⁶O data: these are the high probability for complete fragmentation of ¹⁴N into Z=1 particles (11 ± 4% versus 7 ± 2% and 2 ± 2% for ¹²C and ¹⁶O, respectively) and the high multiplicity of these events, 9.2 ± 0.6. The (Z*) for ¹⁴N is 8.5 ± 0.1₄ for the 1 \leq Z_{max} \leq 3 events, giving a charge excess of 1.5 ± 0.1-about twice that observed for ¹²C and ¹⁶O. The elimination of the two highest values of Z*=13 and 15 from the ¹⁴N spectrum reduces the charges excess to 1.3 ± 0.1, illustrating that this quantity is not significantly influenced by the tail of the ¹⁴N Z*-distribution,

vi) Whereas the modes of the Z*-histograms, Fig. 8, for $^{12}\mathrm{C}$ and $^{16}\mathrm{O}$ occur at Z*=Z_B, the atomic number of the incident ion, the mode of the Z*-distribution for incident $^{14}\mathrm{N}$ is Z_B+1.

That the most probable value for Z^* for ¹⁴N fragmentation is $Z^{*=8}$ may be statistical in nature, particularly because of the small number of events. It leads, however, to the question of whether there was ¹⁶O contamination of the ¹⁴N beam. From an analysis of the interactions and beam tracks themselves in the emulsion, we found no direct, or indirect, evidence for beam impurities in the ¹⁴N data. For example, the fragmentation of ¹⁶O \rightarrow 4He (with or without accompanying shower particles) is a reaction unique to ¹⁶O, and its detection in the ¹⁴N data would unequivocally indicate the presence of ¹⁶O. No such event was observed in this experiment, nor in the study of a comparable number of ¹⁴N interactions by Judek, ³² who has analyzed several plates from our emulsion stack, as well as emulsions exposed to the same ¹⁴N beam. Specifically, no 4He events were observed in a sample of 91 ¹⁴N interactions

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for which $Z_{max} = 2$ and $n_h = 0$. Based on the ¹⁶O data from this experiment and Ref. 22, the probability for the reaction ¹⁶O \rightarrow 4He (for the type $Z_{max} = 2$, $n_h = 0$) is ~ 9%, i.e., 7 events in 81 interactions. Given this probability, we would expect a 50% chance of observing at least one 4He event in the ¹⁴N data had there existed a 12% ¹⁶O background in the ¹⁴N beam. If we take 12% as an upper limit to the ¹⁶O background, a maximum of eight ¹⁶O events could contribute to the Z* histogram for ¹⁴N (Fig. 8). If we assume that the Z* values of these events would be distributed the same as those observed for ¹⁶O, then the corrections to the ¹⁴N data would be less than the statistical errors at all values of Z*. Thus, an upper limit of ¹⁶O background events, derived statistically from the lack of 4He events in the ¹⁴N data, could not, if present, alter significantly the Z* distributions for ¹⁴N as observed.

If we choose to consider the differences between the fragmentation topologies of ¹⁴N relative to ¹²C and ¹⁶O as real, then they must be a manifestation of the differences in the nuclear structure of the projectile nuclei. As an example, ¹⁴N is an odd-odd, I = 1 nucleus, while ¹²C and ¹⁶O are both even-even (α -particle) nuclei with I = 0. In evidence, therefore, is that nuclear structure of the projectile may play an important role in the fragmentation process. This observation complements the results of Greiner <u>et al.</u>¹⁶ and Lindstrom <u>et al.</u>¹³ where effects attributable to the structure of fragment nuclei are apparent in the systematics of the longitudinal momentum distributions and isotope production cross sections. Of particular interest is the indication that ¹⁴N produces, on the average, a net charge excess per fragmentation that is about 0.7e greater than that observed for ¹²C and ¹⁶O. Because this increase in charge multiplicity is most likely due to pions, an implication is that the pion-production cross section by $2.1-\text{GeV/n}^{14}\text{N}$ is greater than those by ^{12}C and ^{16}O on nuclei for the particular class of fragmentation reactions we have examined, i.e., those with no visible target fragmentation. Whether or not this possible enhancement of pion production by ^{14}N is limited to peripheral collisions, where nuclear structure effects become important, can only be conjectured at this time. The revelation of any impact-parameter dependence (e.g., as indicated by the number of evaporation and knock-on fragments from target nuclei) on pion-production cross sections in heavy-ion collisions necessarily requires further experimentation.

IV. SUMMARY

In this comparative study on the interactions of relativistic nuclei in nuclear research emulsion we have measured the mean-free-path lengths of ⁴He, ¹²C, ¹⁴N, and ¹⁶O nuclei at 2.1 GeV/nucleon, and have examined the topological features of the projectile fragmentation of ¹²C, ¹⁴N, and ¹⁶O nuclei, with specific attention to the angular distributions of the Z=1 and 2 fragments and the prong and charge-multiplicity distributions.

By fitting the mean-free-path data to Karol's soft-spheres (optical) model,²⁸ we are able to determine the effective, mean nucleon-nucleon cross section, $\overline{\sigma}$, that accounts for the experimental observations. Our finding is that the effective nucleon-nucleon cross section is 0.52 ± 0.06 (=K) of the average, free nucleon-nucleon cross section at 2.1 GeV. Our conclusion, therefore, is that the mean-free-path measurements in emulsion do not constitute a measure of the total reaction cross section (one which corresponds to K \approx 1), but determine a cross section that involves greater inelasticity and increased energy transfer more properly

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identified with nucleus transmutation reactions.

We have pointed out that the optical model calculations of Karol²⁸ and Barshay <u>et al</u>.²⁷ can be ordered in terms of A_{min} , the smaller mass number of the interacting nuclei, to exhibit the traditional form of the Bradt-Peters relation (Fig. 1). The dependences of the parameters r_0 and b on A_{min} , appropriate for K = 0.52, are illustrated in Fig. 2. Whereas r_0 is quite insensitive to A_{min} , the overlap parameter b decreases monotonically with A_{min} to an $A_{min} \approx 30$, becoming approximately constant thereafter. Such behavior is consistent with the diminution of nuclear transparency with increasing mass of the interacting nuclei.

The projected angular distributions for Z=1 (corrected for background of large P_{\perp} fragments) and Z=2 fragments emitted from $n_h=0$ type events in emulsion are found to be in agreement with those expected from the longitudinal momentum distributions observed in single-particle inclusive experiments. The angular distribution data thus indicate that the momentum distributions are consistent with isotropy in the projectile frame, and serve to demonstrate the validity of the limiting fragmentation process when heavy-ion interactions are selected on the basis that the states are specified in both the high-and low-rapidity regions.

We concluded this experiment with an exposition of the prong and charge-multiplicity distributions of high-rapidity (projectile) fragments produced in $n_h = 0$ type events. The notable feature of these data is the observation that the (absolute) charge multiplicities are, on the average, about 10% greater than the charge of the incident nucleus. That the chargeexcess produced in ¹⁴N interactions is greater than that produced by either ¹²C or ¹⁶O projectiles is suggested by the data. Complementing this result is the observation that $n_h=0$ type events with the largest charge excess occurred in the fragmentation of 14 N projectiles, where Z*'s up to 13 and 15, all high-velocity, Z=1 particles were detected--suggesting that significant pion production can take place, albeit with very low target excitation.

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REFERENCES

- 1. P. Frier, E.J. Lofgren, E.P. Ney, F. Oppenheimer, H.L. Brandt, and B. Peters, Phys. Rev. <u>74</u>, 213 (1948).
- 2. C.J. Waddington, Prog. Nucl. Phys. 8, 1 (1960).
- 3. B. Andersson, I. Otterlund, and K. Kristiannson, Ark. Fys. <u>31</u>, 527 (1966).
- 4. I. Otterlund, Ark. Fys. 38, 467 (1968).
- 5. R. Kullberg and I. Otterlund, Z. Phys. 259, 245 (1973).
- 6. I. Otterlund and B. Andersson, Ark. Fys. 35, 133 (1967).
- 7. R. Kullberg, I. Otterlund, and R. Resman, Phys. Scr. 5, 5 (1972).
- 8. R. Resman and I. Otterlund, Phys. Scr. 4, 183 (1971).
- 9. I. Otterlund and R. Resman, Ark, Fys. 39, 265 (1969).
- 10. W.R. Frazer, L. Ingber, C.H. Mehta, C.H. Poon, D. Silverman, K. Stowe, P.D. Ting, and H.J. Yesian, Rev. Mod. Phys. 44, 284 (1972).
- 11. H.H. Heckman, D.E. Greiner, P.J. Lindstrom, and F.S. Bieser, Phys. Rev. Lett. 28, 926 (1972).
- 12. H.H. Heckman, in Proceedings of the Fifth International Conference on <u>High Energy Physics and Nuclear Structure</u>, Upsala, Sweden, 1973, edited by G. Tibbell (Elsevier, New York, 1974).
- P.J. Lindstrom, D.E. Greiner, H.H. Heckman, Bruce Cork, and F.S. Bieser, Lawrence Berkeley Laboratory Report No. LBL-3650, February 1975.
- 14. G.M. Raisbeck and F. Yiou, Phys. Rev. Lett. 35, 155 (1975).
- 15. H.H. Heckman and P.J. Lindstrom, Phys. Rev. Lett. 37, 56 (1976).
- 16. D.E. Greiner, P.J. Lindstrom, H.H. Heckman, B. Cork, and F.S. Bieser, Phys. Rev. Lett. 35, 152 (1975).
- P.J. Lindstrom, D.E. Greiner, and H.H. Heckman, Bull. Am. Phys. Soc. 17, 488 (1972). Also H.H. Heckman, Relativistic Heavy Ion Seminar, Internal LBL Report, 1973 (unpublished).
- P.J. Lindstrom, D.E. Greiner, H.H. Heckman, B. Cork, and F.S. Bieser, 14th International Cosmic Ray Conference, München, Conference Papers, Vol. 7, 2315 (1975).
- 19. T.F. Cleghorn, The Energy Dependence of the Fragmentation Parameters and Mean Free Paths in Nuclear Emulsion for Heavy Cosmic Ray Nuclei, Thesis, University of Minnesota (1967).

- 20. C.J. Waddington, Prog. Nucl. Phys. 8, 1 (1960).
- B. Jakobsson, R. Kullberg, and I. Otterlund, 14th International Cosmic Ray Conference, München, Conference Papers, Vol. 7, 2353 (1975).
- 22. B. Judek, 14th International Cosmic Ray Conference, München, Conference Papers, Vol. 7, 2342 (1975).
- 23. E. Lohrmann and M.W. Teucher, Phys. Rev. 115, 636 (1959).
- 24. H.C. Bradt and B. Peters, Phys. Rev. 77, 54 (1950).
- D.L. Cheshire, R.W. Huggett, D.P. Johnson, W.V. Jones, S.P. Rountree, S.D. Verma, W.K.H. Schmidt, R.J. Kurz, T. Bowen, and E.P. Krider, Phys. Rev. D10, 25 (1974).
- 26. W.H. Barkas, <u>Nuclear Research Emulsions</u>, Vol. 1 (Academic Press, 1963).
- 27. S. Barshay, C.B. Dover, and J.P. Vary, Phys. Rev. C11, 360 (1975). Also private communication, J.P. Vary (April 23, 1975).
- 28. P.J. Karol, Phys. Rev. C11, 1203 (1975).
- 29. J.P. Vary, private communication, 1977.
- 30. J.V. Lepore and R.J. Riddell, Jr., Lawrence Berkeley Laboratory Report No. LBL-3086, 1974 (unpublished).
- 31. G.D. Westfall, J. Gosset, P.J. Johansen, A.M. Poskanzer, W.G. Meyer, H.H. Gutbrod, A. Sandoval, and R. Stock, Phys. Rev. Lett. <u>37</u>, 1202 (1976).
- 32. B. Judek, private communication, April 1975.

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TABLE I.

Interaction mean-free-path length data. Tabulated are: N_i , the number of observed interactions of Type i, $N_{obs} = \Sigma_i N_i$, $N_{total} = N_{obs}$ corrected for scanning losses of $\Delta Z = 0$ and 1 events, and $N_{\Delta Z} \ge 1$, the number of charge-changing ($\Delta Z \ge 1$ events). The interaction lengths evaluated from N_{total} and $N_{\Delta Z} \ge 1$ are λ_{total} and $\lambda_{\Delta Z} \ge 1$, respectively.

Measurements		Beam		
·····	⁴ He	12 _C	14 _N	¹⁶ 0
N ₁	104	149	123	119
N ₂	500	533	506	600
N ₃	353	325	376	249
N ₄	54	88	54	55
Nobs	1011	1095	1059	1023
N _{total}	1011	1111 ± 39	1090 ± 47	1092 ± 38
$^{N}\Delta Z \ge 1$	957	1044 ± 39	1031 ± 45	1040 ± 36
Path length (cm)	22080	15302	14895	14174
λ_{total} (cm)	21.8 ± 0.5	13.8 ± 0.5	13.7 ± 0.6	13.0 ± 0.5
$^{\lambda}\Delta Z \ge 1^{(\mathrm{cm})}$	23.1 ± 0.8	14.7 ± 0.6	14.5 ± 0.6	13.6 ± 0.5
	1			

	Ве		
$\frac{N}{\Delta Z} = 0, 1$	¹² C	14 _N	16 ₀
Observed	163 ± 17	146 ± 28	110 ± 12
Expected ^a	179 ± 18	177 ± 17^{b}	179 ± 17
Correction to N _{obs}	16 ± 25	31 ± 33	69 $\pm \sqrt{21}$
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TABLE II. Corrections to N_{obs} for undetected $\Delta Z = 0$ and 1 events.

- a Expected number of $N_{\Delta Z} = 0$, 1 events were computed by using the cross sections given in Refs. 13 and 17.
- b Evaluated with the average of the ^{12}C and ^{16}O fragmentation cross sections.

TABLE III.	Interaction	mean-f	free-pa	th ler	ngths	s (cm)	in Il:	ford	emulsion	calculated	by	using
	parameters	K and b	o that	best	fit	experi	menta	l dat	a. The	composition	of	Ilford

1	Beam				
	Fitted Parameters	⁴ He	- ¹² C	¹⁴ N	160
Experiment		21.8 ± 0.7	13.8 ± 0.5	13.7 ± 0.6	13.0 ± 0.5
Karol (Ref. 28)	$K = 0.52 \pm 0.06$	22.5	14.1	13.2	12.4
Vary (Eq. 2)	$b_0 = 1.11 \pm 0.05$	22.2	14.2	13.2	12.5

G.5 emulsion used for the calculations is given in Ref. 26.

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TABLE IV.	Comparison of measured cross sections by Lindstrom <u>et al</u> . ¹⁷ with computed cross
•. *.	sections using parameters K and b_0 obtained from the emulsion data. The cross
	sections are given in mb.

Beam			Target		
12 _C	Н	С	S	Cu	РЪ
Lindstrom (exp)	258 ± 21	826 ± 23	1250 ± 51	1730 ± 36	2960 ± 65
Karol $(K = 0.52)$	181	788	1320	1800	3190
Vary (b _o = 1.11)	167	757	1250	1770	3300
			· ·	,	
<u>160</u>	Н	С	S	Cu	РЪ
Lindstrom (exp)	361 ± 24	1022 ± 25	1420 ± 51	1950 ± 41	3270 ± 82
Karol	230	918	1500	2000	3470
Vary	225	877	1400	1950	3540
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TABLE V. Standard deviation widths of the momentum and projected angular distributions for the Z=1 and 2 secondary isotopes from the fragmentation of the CNO group at E = 2.1GeV/nucleon. The production-weighted angular widths of Z=1 and Z=2 fragments are $\sigma^{}_{Z=1}$ and $\sigma^{}_{Z=2},$ respectively. Experimental data are based upon $n^{}_{h}$ =0 type interactions.

	Greiner <u>et al</u> . ¹⁶	Lepore and Riddell, ³⁰ Eq. 3 This experiment					Greiner <u>et al.</u> ¹⁶ Lepore and Riddell, ³⁰ Eq. 3		
Fragment (wt)	σ(p) σ(θproj) (MeV/c) (deg)	σ(p) σ(θproj) (MeV/c) (deg)	exp. (deg)						
p (0.74)	69 ± 6 1.38 ± 0.11	79 1.58							
d (0.19)	134 ± 4 1.34 ± 0.04	107 1.07							
t (0.07)	144 ± 6 0.96 ± 0.04	126 0.84							
	$\sigma_{Z=1} = 1.35 \pm 0.11$	1,45	1.3 - 1,5						
³ He (0.24)	150 ± 6 1.00 \pm 0.04	126 0.84							
⁴ He (0.76)	130 ± 1 0.65 \pm 0.005	138 0.69							
	$\sigma_{Z=2} = 0.73 \pm 0.06$	0.73	0.64 ± 0.02						

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TABLE VI.	Production frequency, in percent, of events in emulsion as a					
	function of Z_{max} , the highest charged projectile fragment					
	produced in interaction. Corrections for scanning losses for					
	events for $Z \ge 4$ are included.					

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Projectile Z max	1	2	3	≥4
. ¹² C	7 ± 2	59 ± 10	8 ± 3	26 ± 12
14 _N	11 ± 4	49 ± 13	8 ± 3	32 ± 17
¹⁶ 0	2 ± 1	33 ± 5	9 ± 2	55 ± 6

events for $Z_{\text{max}} \ge 4$ are included.

FIGURE CAPTIONS

- Fig. 1 Reaction cross sections computed from soft-sphere model, Ref. 28, by using nucleon-nucleon cross sections adjusted to fit the emulsion mean-free-path data. Cross sections are ordered by A_{min} , the mass of the lighter of the two interacting nuclei, in terms of the Bradt-Peters relation, Eq. 1. Least-squares fits to the computed cross sections are indicated for $A_{min} = 4$, 12, 20, 40, and 56.
- Fig. 2 a) The radius r_o and b) overlap b parameter deduced from the leastsquares fits of soft-sphere model calculations versus A_{min}.
- Fig. 3 Photomicrograph of the fragmentation of a 2.1-GeV/n ¹⁴N nucleus in nuclear emulsion. The point of interaction is indicated by the arrow. The ¹⁴N enters from the left, fragments into 3 He + H, with no emission of low-energy, heavily ionizing tracks.
- Fig. 4 Projected angular distribution for Z=1 fragments, produced in the forward hemisphere by the fragmentation of ^{12}C , ^{14}N , and ^{16}O projectiles. All interactions are of the $n_h=0$ type, as illustrated in Fig. 3. Beam energy is 2.1 GeV/n.
- Fig. 5 The combined projected angular distribution for Z=1 fragments, C, N, and O projectiles, $\theta_{\text{proj}} \leq 16^{\circ}$. The curves drawn through the data are the sums of two Gaussian distributions, $\sigma = 1.3^{\circ}$ (1.5°), and 7.5°, normalized to unit areas,
- Fig. 6 Angular distribution, projected onto the emulsion plane, for He (Z=2) fragments from the fragmentation of ¹²C, ¹⁴N, and ¹⁶O projectiles. All interactions are of type $n_h=0$. Curve is a Gaussian distribution, $\sigma = 0.65^{\circ}$, fitted to the data for $\theta_{proj} \leq 1.5^{\circ}$ and corrected for measurement error.

Fig. 7 Histograms of the prong-number distributions for the fragmentation

of a) ¹²C, b) ¹⁴N, and c) ¹⁶O nuclei in nuclear emulsion, $n_h=0$ type interactions. Data are ordered as to the maximum charge, Z_{max} , emitted in the fragmentation for $1 \le Z_{max} \le 3$ only. The mean prong number (n) is indicated for each distribution.

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Fig. 8 Histograms of the charge multiplicity distributions for the fragmentation of a) 12 C, b) 14 N, and c) 16 O. The quantity Z* = ${}^{n}_{\Sigma} |Z_{i}|$, where $|Z_{i}|$ is the absolute charge of the n^{th} prong. The i=1 histograms are based upon the same events used for Fig. 7, and are also ordered as to Z_{max} . The mean-charge multiplicity is indicated for each distribution.





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Fig. 2











Fig. 4



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Fig. 5



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TECHNICAL INFORMATION DEPARTMENT LAWRENCE BERKELEY LABORATORY UNIVERSITY OF CALIFORNIA BERKELEY, CALIFORNIA 94720