

Research Article

Frequency-Domain Block Signal Detection with QRM-MLD for Training Sequence-Aided Single-Carrier Transmission

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A frequency-domain block signal detection (FDBD) using QR decomposition with M-algorithm maximum likelihood detection (QRM-MLD) can significantly improve the bit error rate (BER) performance of the cyclic prefix inserted single-carrier (CP-SC) block transmission in a frequency-selective fading channel. However, the use of a fairly large number of the surviving paths is required in the M-algorithm, leading to high computational complexity. In this paper, we propose the use of the training sequence-aided SC (TA-SC) block transmission instead of CP-SC block transmission. We show that TA-SC using FDBD with QRM-MLD can achieve the BER performance close to the matched-filter (MF) bound while reducing the computational complexity compared to CP-SC.

1. Introduction

In next-generation mobile communication systems, broadband data services are demanded. Since the mobile wireless channel is composed of many propagation paths with different time delays, the channel becomes severely frequency selective as the transmission data rate increases. When the single-carrier (SC) transmission without any equalization technique is used, the bit error rate (BER) performance significantly degrades due to strong intersymbol interference (ISI) [1]. The computational complexity of the maximum likelihood- (ML-) based equalization, that is, ML sequence estimation (MLSE), depends on the number of propagation paths and becomes extremely high in a severely frequency-selective channel [2]. Therefore, several suboptimal linear detection schemes, such as time-domain and frequency-domain linear equalization schemes, have been proposed to reduce the computational complexity [3–5]. A simple one-tap frequency-domain equalization based on the minimum mean square error criterion (MMSE-FDE) can significantly improve the BER performance of cyclic prefix inserted SC (CP-SC) block transmission in a frequency-selective fading

channel. However, a big performance gap from the matched-filter (MF) bound still exists due to the presence of residual ISI after FDE. To narrow the performance gap, an MMSE-FDE combined with iterative ISI cancellation was proposed [6–8]. However, the achievable BER performance is still a few dB away from the MF bound, particularly when high-level data modulation (e.g., 16QAM and 64QAM) is used. Near ML-based reduced complexity time-domain equalization schemes have been proposed in [9, 10].

Recently, we proposed a near ML-based reduced complexity frequency-domain equalization scheme, which is called frequency-domain block signal detection (FDBD) using QR decomposition with M-algorithm ML detection (QRM-MLD), for the reception of CP-SC signals transmitted over a frequency-selective channel [11]. QRM-MLD was originally proposed as a signal detection scheme for the multi-input multi-output (MIMO) spatial multiplexing in [12]. In FDBD with QRM-MLD, QR decomposition is applied to a concatenation of the propagation channel and discrete Fourier transform (DFT). We showed [11] that FDBD with QRM-MLD can significantly improve the BER performance when compared to the MMSE-FDE and achieve

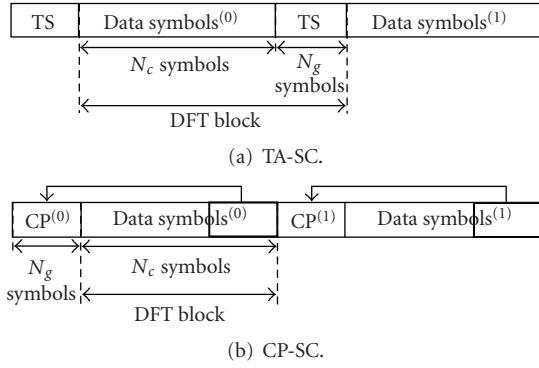


FIGURE 1: Block structure.

the BER performance close to the MF bound even if high level data modulation is used. However, the use of a fairly large number M of surviving paths in the M-algorithm is required, leading to high computational complexity. If smaller M is used, the achievable BER performance degrades because of increased probability of removing the correct path at early stages. This probability greatly affects the achievable BER performance of FDBD with QRM-MLD.

In this paper, we will show that the use of training sequence-aided SC (TA-SC) block transmission [13, 14] instead of CP-SC block transmission can significantly reduce the probability of removing the correct path at early stages in QRM-MLD and hence improve the achievable BER performance of FDBD with QRM-MLD. In TA-SC, CP is replaced by a known training sequence (TS), which is a part of DFT block at the receiver, and TS in the previous block acts as CP in the present block. When TA-SC is used, since the symbols to be detected at early stages belong to the known TS, the achievable BER performance of FDBD with QRM-MLD can be improved. The performance improvement of TA-SC over CP-SC when using FDBD with QRM-MLD is confirmed by computer simulation.

The remainder of this paper is organized as follows. In Section 2, TA-SC using FDBD with QRM-MLD is presented. In Section 3, we will show by computer simulation that TA-SC transmission using FDBD with QRM-MLD can achieve BER performance close to the MF bound while reducing the number of surviving paths when compared to CP-SC. We will also discuss the computational complexity of FDBD with QRM-MLD and show that TA-SC can reduce the overall complexity of FDBD with QRM-MLD to achieve almost the same performance as CP-SC. Section 4 offers some concluding remarks.

2. TA-SC Using FDBD with QRM-MLD

2.1. TA-SC versus CP-SC. The TA-SC block structure is illustrated and compared to CP-SC transmission in Figure 1. CP is replaced by TS. In order to let TS to play the role of CP, DFT size at the receiver must be the sum of number of useful data symbols and the TS length. In the case of CP-SC, the data symbol block length and the CP length are, respectively, denoted by N_c and N_g . For TA-SC, to keep the

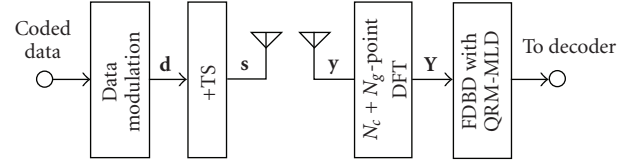
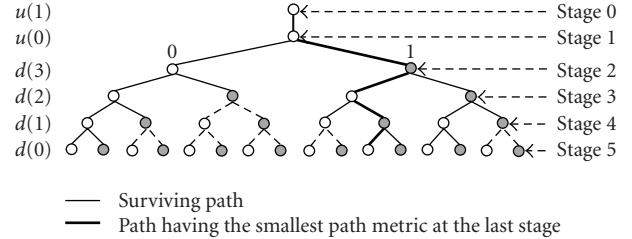


FIGURE 2: TA-SC transmission system model.

FIGURE 3: An example of QRM-MLD ($M = 3$) with BPSK when $N_c = 4$ and $N_g = 2$.

same data rate as CP-SC, the data symbol block length and the TS length need to be set to N_c and N_g , respectively. The difference between TA-SC and CP-SC is the size of DFT to be used at the receiver; the DFT size is $N_c + N_g$ symbols for TA-SC while it is N_c symbols for CP-SC.

2.2. TA-SC Signal Transmission Model. The TA-SC transmission model using FDBD with QRM-MLD is illustrated in Figure 2. Throughout the paper, the symbol-spaced discrete time representation is used. At the transmitter, a binary information sequence to be transmitted is data-modulated, and then the data-modulated symbol sequence is divided into a sequence of symbol blocks of N_c symbols each. The data symbol block can be expressed using the vector form as $\mathbf{d} = [d(0), \dots, d(n), \dots, d(N_c - 1)]^T$. Before the transmission, the TS of length N_g symbols is appended at the end of each block. The block \mathbf{s} to be transmitted is expressed using the vector form as

$$\begin{aligned} \mathbf{s} &= [s(0), \dots, s(N_c + N_g - 1)]^T \\ &= [d(0), \dots, d(N_c - 1), u(0), \dots, u(N_g - 1)]^T \\ &= \begin{bmatrix} \mathbf{d} \\ \mathbf{u} \end{bmatrix}, \end{aligned} \quad (1)$$

where $\mathbf{u} = [u(0), \dots, u(n), \dots, u(N_g - 1)]^T$ denotes the TS vector which is identical for all blocks.

We assume a symbol-spaced frequency-selective fading channel composed of L propagation paths with different time delays. The channel impulse response $h(\tau)$ is given by

$$h(\tau) = \sum_{l=0}^{L-1} h_l \delta(\tau - \tau_l), \quad (2)$$

where h_l and τ_l are, respectively, the complex-valued path gain with $E[\sum_{l=0}^{L-1} |h_l|^2] = 1$ and the time delay of the l th

all symbols in a block, and hence no ordering is necessary in the QR decomposition. First, the QR decomposition is applied to the equivalent channel matrix $\bar{\mathbf{H}}^{(\text{TA})}$ to obtain $\bar{\mathbf{H}}^{(\text{TA})} = \mathbf{Q}^{(\text{TA})}\mathbf{R}^{(\text{TA})}$, where $\mathbf{Q}^{(\text{TA})}$ is an $(N_c + N_g) \times (N_c + N_g)$ matrix satisfying $\mathbf{Q}^{(\text{TA})H}\mathbf{Q}^{(\text{TA})} = \mathbf{I}$ (\mathbf{I} is the identity matrix) and $\mathbf{R}^{(\text{TA})}$ is an $(N_c + N_g) \times (N_c + N_g)$ upper triangular matrix. The transformed frequency-domain received signal $\hat{\mathbf{Y}}^{(\text{TA})} = [\hat{Y}^{(\text{TA})}(0), \dots, \hat{Y}^{(\text{TA})}(m), \dots, \hat{Y}^{(\text{TA})}(N_c + N_g - 1)]^T$ is obtained as

$$\begin{aligned} & \hat{\mathbf{Y}}^{(\text{TA})} \\ &= \mathbf{Q}^{(\text{TA})H}\mathbf{Y}^{(\text{TA})} = \sqrt{\frac{2E_s}{T_s}}\mathbf{R}^{(\text{TA})}\mathbf{s} + \mathbf{Q}^{(\text{TA})H}\mathbf{N}^{(\text{TA})} \\ &= \sqrt{\frac{2E_s}{T_s}} \\ & \times \begin{bmatrix} R_{0,0}^{(\text{TA})} & \cdots & R_{0,N_c-1}^{(\text{TA})} & R_{0,N_c}^{(\text{TA})} & \cdots & R_{0,N_c+N_g-1}^{(\text{TA})} \\ & \ddots & \vdots & \vdots & \ddots & \vdots \\ & & R_{N_c-1,N_c-1}^{(\text{TA})} & R_{N_c-1,N_c}^{(\text{TA})} & \cdots & R_{N_c-1,N_c+N_g-1}^{(\text{TA})} \\ & & & R_{N_c,N_c}^{(\text{TA})} & \cdots & R_{N_c,N_c+N_g-1}^{(\text{TA})} \\ \mathbf{0} & & & & \ddots & \vdots \\ & & & & & R_{N_c+N_g-1,N_c+N_g-1}^{(\text{TA})} \end{bmatrix} \\ & \times \begin{bmatrix} d(0) \\ \vdots \\ d(N_c - 1) \\ u(0) \\ \vdots \\ u(N_g - 1) \end{bmatrix} + \mathbf{Q}^{(\text{TA})H}\mathbf{N}^{(\text{TA})}. \end{aligned} \quad (12)$$

From (12), the ML solution $\hat{\mathbf{d}}^{(\text{TA})}$ can be obtained by searching for the best path having the minimum Euclidean distance in the tree diagram composed of $N_c + N_g$ stages. However, in TA-SC, the $N_c, N_c + 1, \dots, (N_c + N_g - 1)$ th elements of $\hat{\mathbf{Y}}^{(\text{TA})}$ contain the training symbols only, and therefore only one path exists at the $n = 0, 1, \dots, (N_g - 1)$ th stages and the M-algorithm [16] can be started from the $n = N_g$ stage.

An example of the QRM-MLD is shown in Figure 3 assuming $N_c = 4$ and $N_g = 2$, binary phase shift keying (BPSK) modulation, and $M = 3$. In the $n = N_g$ th stage, all possible symbol-candidates for the last symbol $d(N_c - 1)$ in a data symbol block are generated (the number of all possible symbol-candidates is X for X -QAM). The path metric based on the squared Euclidean distance between $\hat{Y}^{(\text{TA})}(N_c - 1)$ and each symbol-candidate is calculated as

$$\begin{aligned} e_{n=N_g} &= \left| \hat{Y}^{(\text{TA})}(N_c - 1) - \sqrt{\frac{2E_s}{T_s}}R_{N_c-1,N_c-1}^{(\text{TA})}\bar{d}(N_c - 1) \right. \\ & \left. - \sqrt{\frac{2E_s}{T_s}}\sum_{i=0}^{N_g-1}R_{N_c-1,N_c+i}^{(\text{TA})}u(i) \right|^2, \end{aligned} \quad (13)$$

where $\bar{d}(N_c - 1)$ is the symbol-candidate for $d(N_c - 1)$. Next, M ($M \leq X$) paths having the smallest path metric are selected as surviving paths. In the next stage ($n = N_g + 1$), there are a total of X branches for $d(N_c - 2)$ leaving from each selected surviving path. Therefore, there are totally $M \cdot X$ possible paths for the two symbol sequence of $d(N_c - 1)$ and $d(N_c - 2)$. The path metrics are calculated for all possible $M \cdot X$ paths using

$$\begin{aligned} & e_{n=N_g+1} \\ &= \left| \hat{Y}^{(\text{TA})}(N_c - 2) - \sqrt{\frac{2E_s}{T_s}} \right. \\ & \quad \times \left\{ R_{N_c-2,N_c-2}^{(\text{TA})}\bar{d}(N_c - 2) + R_{N_c-2,N_c-1}^{(\text{TA})}\bar{d}(N_c - 1) \right\} \\ & \quad \left. - \sqrt{\frac{2E_s}{T_s}}\sum_{i=0}^{N_g-1}R_{N_c-2,N_c+i}^{(\text{TA})}u(i) \right|^2 \\ & + \left| \hat{Y}^{(\text{TA})}(N_c - 1) - \sqrt{\frac{2E_s}{T_s}}R_{N_c-1,N_c-1}^{(\text{TA})}\bar{d}(N_c - 1) \right. \\ & \quad \left. - \sqrt{\frac{2E_s}{T_s}}\sum_{i=0}^{N_g-1}R_{N_c-1,N_c+i}^{(\text{TA})}u(i) \right|^2. \end{aligned} \quad (14)$$

Similar to the $n = N_g$ th stage, M surviving paths are selected from $M \cdot X$ paths. This procedure is repeated until the last stage ($n = N_c + N_g - 1$). The path metric at the n th stage ($n = N_g, N_g + 1, \dots, N_c + N_g - 1$) is calculated using

$$\begin{aligned} & e_n = \sum_{n'=0}^{n-N_g} \left| \hat{Y}^{(\text{TA})}(N_c - 1 - n') \right. \\ & \quad \left. - \sqrt{\frac{2E_s}{T_s}}\sum_{i=0}^{n'}R_{N_c-1-n',N_c-1-i}^{(\text{TA})}\bar{d}(N_c - 1 - i) \right. \\ & \quad \left. - \sqrt{\frac{2E_s}{T_s}}\sum_{i=0}^{N_g-1}R_{N_c-1-n',N_c+i}^{(\text{TA})}u(i) \right|^2. \end{aligned} \quad (15)$$

The most possible transmitted symbol sequence is found by tracing back the path with the smallest path metric at the last stage ($n = N_c + N_g - 1$). QRM-MLD requires $X\{1 + M(N_c - 1)\}$ times squared Euclidean distance calculation, which is significantly smaller than the original MLD that requires X^{N_c} times squared Euclidean distance calculation.

2.4. Advantage of TA-SC over CP-SC. The received signal power associated with the symbol $d(N_c - 1 - i)$ at the n th stage ($n - N_g \geq i$, $n = N_g, N_g + 1, \dots, N_c + N_g - 1$) is the sum of the squared values of the $(N_c - 1), (N_c - 2), \dots, (N_c - 1 - i)$ th elements in the $(N_c - 1 - i)$ th column of \mathbf{R} . In the case of SC transmission, the channel impulse response matrix is circulant, and therefore the magnitude of a lower right element of \mathbf{R} drops with large probability [17]. Therefore, the probability of removing the correct path is greater at early stages.

In the case of CP-SC transmission, the transformed frequency-domain received signal vector $\hat{\mathbf{Y}}^{(\text{CP})} = [\hat{Y}^{(\text{CP})}(0), \dots, \hat{Y}^{(\text{CP})}(N_c - 1)]^T$ is obtained as [11]

$$\begin{aligned} \hat{\mathbf{Y}}^{(\text{CP})} &= \sqrt{\frac{2E_s}{T_s}} \mathbf{R}^{(\text{CP})} \mathbf{d} + \mathbf{Q}^{(\text{CP})H} \mathbf{N}^{(\text{CP})} \\ &= \sqrt{\frac{2E_s}{T_s}} \begin{bmatrix} R_{0,0}^{(\text{CP})} & R_{0,1}^{(\text{CP})} & \cdots & R_{0,N_c-1}^{(\text{CP})} \\ & R_{1,1}^{(\text{CP})} & \cdots & R_{1,N_c-1}^{(\text{CP})} \\ & & \ddots & \vdots \\ & & & R_{N_c-1,N_c-1}^{(\text{CP})} \end{bmatrix} \\ &\quad \times \begin{bmatrix} d(0) \\ d(1) \\ \vdots \\ d(N_c - 1) \end{bmatrix} + \mathbf{Q}^{(\text{CP})H} \mathbf{N}^{(\text{CP})}. \end{aligned} \quad (16)$$

The lower right elements of $\mathbf{R}^{(\text{CP})}$ are relevant to the selection of the surviving path. Since the received signal power is lower at early stages, the probability of removing the correct path at early stages may increase when smaller M is used. The probability of removing the correct path at early stages affects significantly the achievable BER performance of FDBD with QRM-MLD. A fairly large M must be used to achieve the BER performance close to the MF bound. For example, $M = 256$ is necessary for the case of $N_c = 64$ and 16QAM data modulation [11]. The use of larger M increases the computational complexity.

In the case of TA-SC, it can be understood from (12) that the lower right elements of $\mathbf{R}^{(\text{TA})}$ are associated with TS, and therefore they are not relevant to the selection of the surviving path. The M-algorithm can start from the $n = N_g$ th stage and therefore, the probability of removing the correct path at early stages can be significantly reduced even if small M is used. This suggests that smaller M can be used for TA-SC than CP-SC.

3. Computer Simulation

The simulation condition is summarized in Table 1. The data symbol block length is $N_c = 64$ for both TA- and CP-SC and the TS length of TA-SC is $N_g = 16$ which is equal to the CP length of CP-SC. A partial sequence taken from a PN sequence with a repetition period of 4095 bits is used as TS. The same data modulation is used for TS and useful data. The channel is assumed to be a frequency-selective block Rayleigh fading channel having symbol-spaced L -path uniform power delay profile. Ideal channel estimation is assumed.

3.1. Average BER Performance. The BER performance of TA-SC using FDBD with QRM-MLD is plotted in Figure 4 as a function of average received bit energy-to-noise power spectrum density ratio $E_b/N_0 (= (E_s/N_0)(1 + N_g/N_c) / \log_2 X)$ for $M = 1, 4, \text{ and } 16$. For comparison, the BER performance of CP-SC [11] and the MF bound [18] are also plotted. It can be seen from Figure 4 that when small M is used,

TABLE 1: Computer simulation condition.

| | Channel code | Turbo code ($R = 1/2, 3/4, 8/9, 1$) |
|-------------|--------------------------|--|
| Transmitter | Data modulation | QPSK, 16QAM, 64QAM |
| | Data symbol block length | $N_c = 64$ |
| | TS and CP lengths | $N_g = 16$ |
| | Fading type | Frequency-selective block Rayleigh |
| Channel | Power delay profile | $L = 2 \sim 16$ path uniform power delay profile |
| | Time delay | $\tau_l = l$ ($l = 0 \sim L - 1$) |
| | Receiver | Channel estimation |

the achievable BER performance of CP-SC degrades. On the other hand, TA-SC can achieve better BER performance even if small M is used. The required value of M in TA-SC is 16, 16, and 4 for QPSK, 16QAM, and 64QAM, respectively, to achieve the BER performance similar to CP-SC using $M = 256$. The reason for this is discussed in the following.

Figure 5 shows the pdf of the received signal power $P_{N_c-1,n}$ associated with the symbol $d(N_c - 1)$ at the n th stage, where $P_{N_c-1,n}$ is given by

$$P_{N_c-1,n} = \begin{cases} \sum_{i=0}^{n-N_g} \left| R_{N_c-1-i, N_c-1}^{(\text{TA})} \right|^2 & \text{for TA-SC} \\ \sum_{i=0}^n \left| R_{N_c-1-i, N_c-1}^{(\text{CP})} \right|^2 & \text{for CP-SC.} \end{cases} \quad (17)$$

It is seen from Figure 5(a) that when CP-SC is used, the probability that the received signal power drops is high at early stages. Therefore, the probability of removing the correct path at early stages increases when smaller M is used. This is shown in Figure 6 which plots the probability of removing the correct path at the n th stage ($n = N_g, N_g + 1, N_g + 2$ for TA-SC and $n = 0, 1, 2$ for CP-SC) when $E_b/N_0 = 10$ dB and 16QAM is used. The use of larger M can reduce the probability of removing the correct path and hence improve the achievable BER performance; however, the computational complexity increases. The computational complexity of FDBD with QRM-MLD will be discussed in the next subsection.

In the case of TA-SC, the lower right elements of \mathbf{R} are not used in QRM-MLD. Therefore, the probability that the received signal power at early stages drops is very low (see Figure 5(b)). As a consequence, the probability of removing the correct path at early stages is reduced. This is clearly seen in Figure 6.

Figure 7 plots the required E_b/N_0 for achieving BER = 10^{-4} as a function of M . For comparison, the required E_b/N_0 for the MF bound is also plotted. In the case of CP-SC, the required value of M to achieve the BER performance close to the MF bound is 64 for QPSK and 256 for 16QAM and 64QAM. However, in the case of TA-SC, much smaller M is required, that is, $M = 8$ for QPSK and 16 for 16QAM and

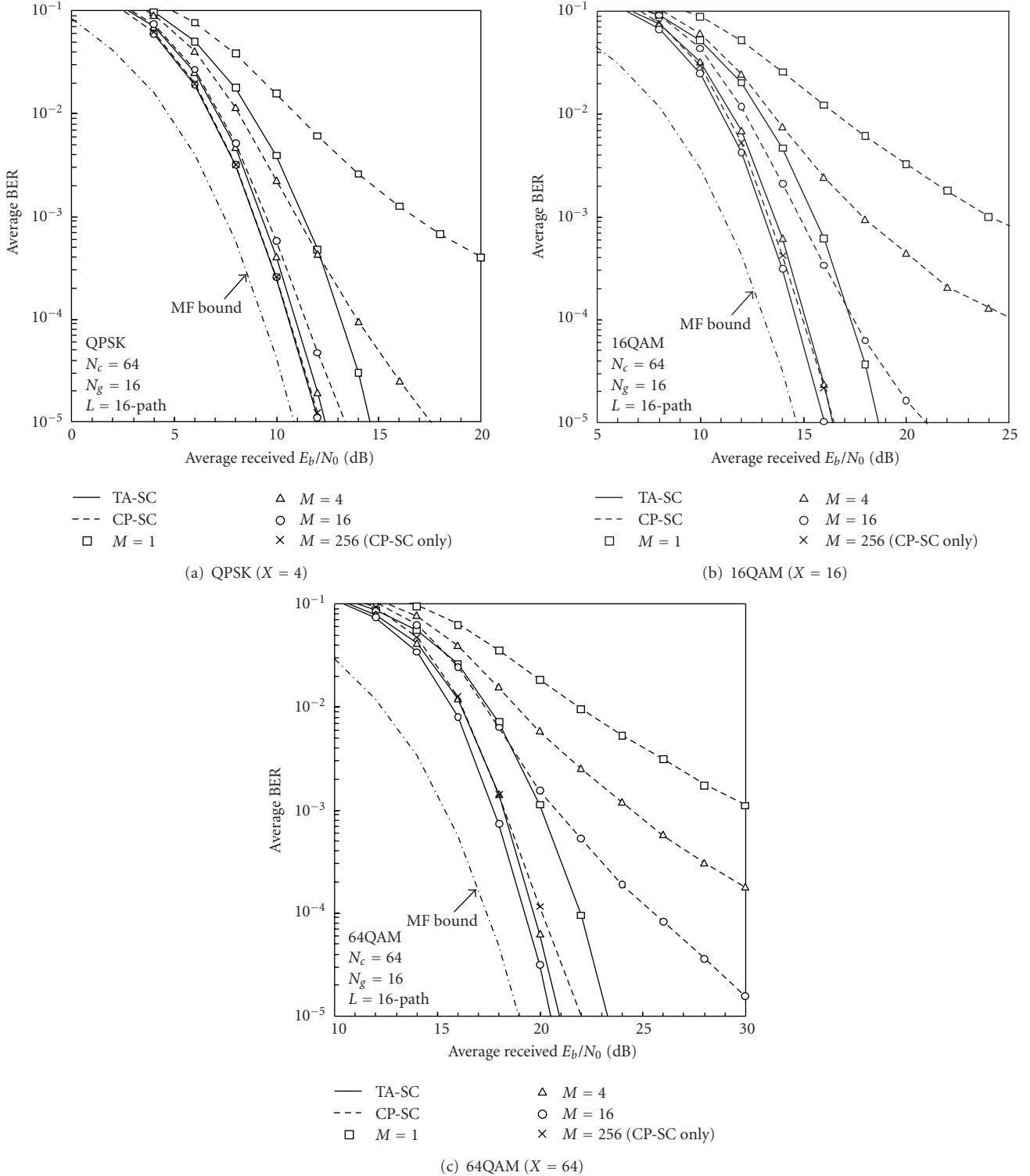


FIGURE 4: Average BER performance (uncoded).

64QAM. The performance gap of 1 dB from the MF bound is owing to the insertion of TS and CP.

Figure 8 shows the influence of the number L of propagation paths on the required M to reduce the E_b/N_0 gap from the MF bound for achieving BER = 10^{-4} to 1.5, 2.5,

and 3.0 dB for QPSK, 16QAM, and 64QAM, respectively. It can be seen from Figure 8 that the required M increases with L in the case of CP-SC. This is because the number of elements (whose magnitudes likely drop) of \mathbf{R} in the lower right positions increases with L [17], and therefore the

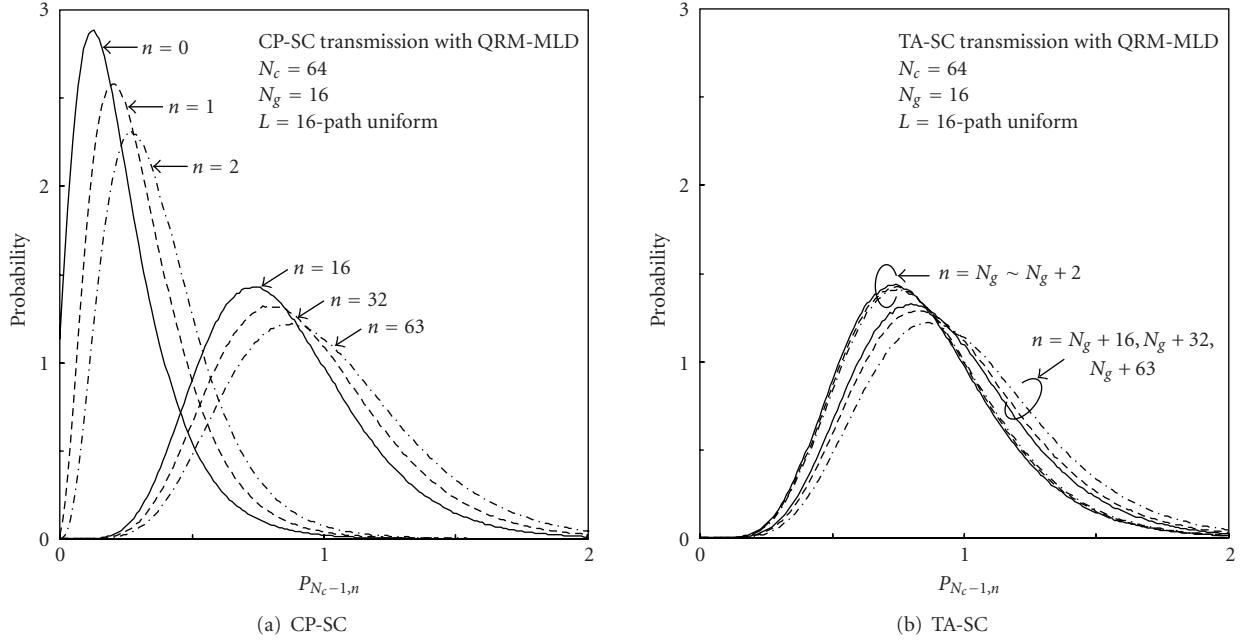


FIGURE 5: Pdf of the received signal power associated with the symbol $d(N_c - 1)$ at the n th stage.

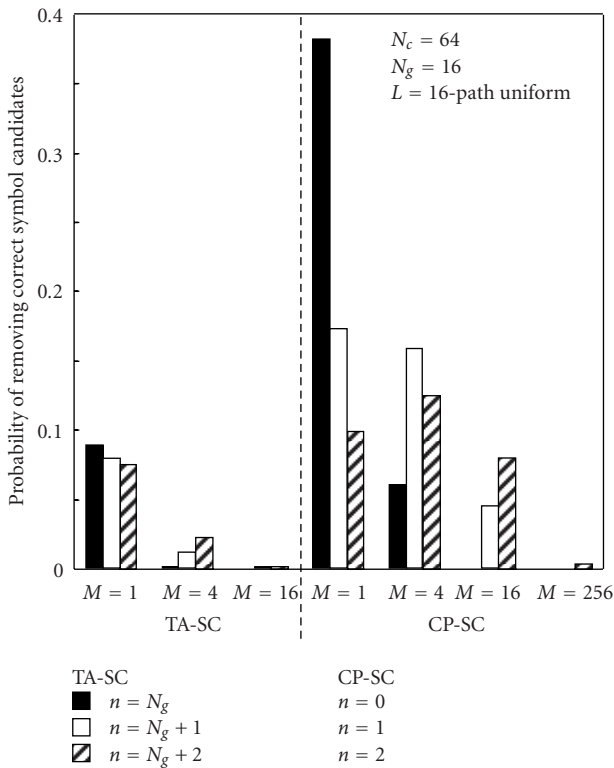


FIGURE 6: Probability of removing correct path at n th stage ($n = 0 \sim 2$). 16QAM.

probability of removing the correct path at early stages also increases. However, in the case of TA-SC, required M does not almost depend on the number of L .

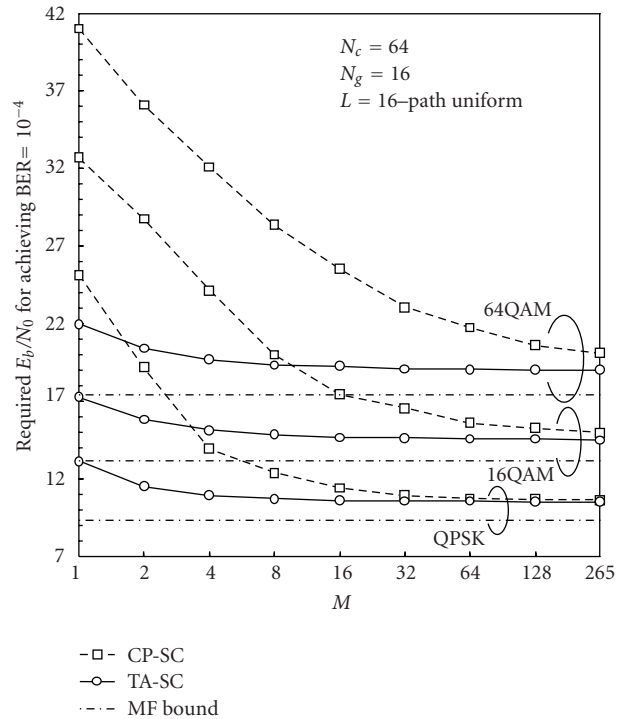


FIGURE 7: Required E_b/N_0 for achieving $BER = 10^{-4}$.

Below, we examine the transmission performances of coded CP-SC and TA-SC systems. 16QAM is assumed as the data modulation scheme. We employ a rate 1/3 turbo encoder using two (13, 15) recursive systematic convolutional (RSC) component encoders. The two parity sequences from the turbo encoder are punctured to obtain rate-1/2, 3/4,

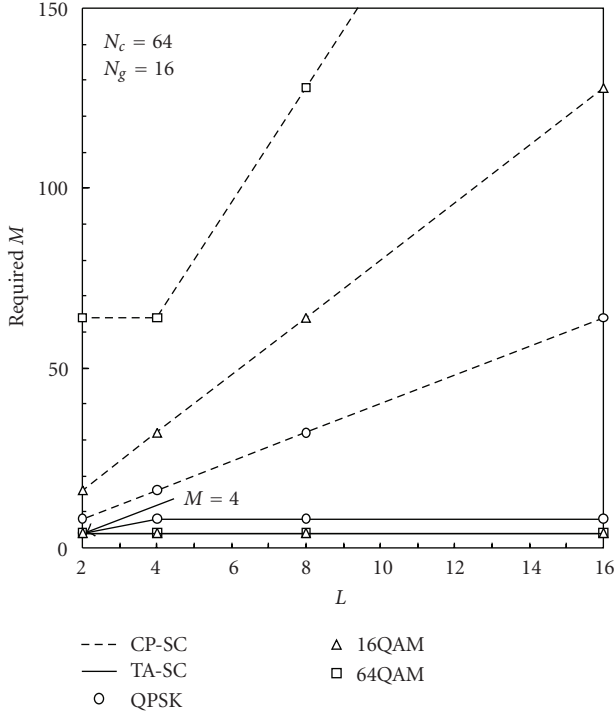


FIGURE 8: Required M as a function of the number L of propagation paths.

and 8/9 turbo codes. Log-MAP decoding with 6 iterations is assumed. The packet length is set to 8 blocks ($8N_c$ symbols) in all simulations. The log likelihood ratio (LLR) is used as the soft-input in the turbo decoder. When FDBD with QRM-MLD is used, however, the LLR values cannot be directly computed, since surviving paths at the last stage do not necessarily contain both 1 and 0 for every coded bit. Therefore, how to estimate reliable LLR values is an important issue for FDBD with QRM-MLD. In our paper, we applied the LLR estimation scheme proposed in [19]. The BER performance of turbo coded TA-SC using FDBD with QRM-MLD is plotted in Figure 9 as a function of average received $E_b/N_0 (= R(E_s/N_0) (1 + N_g/N_c)/\log_2 X)$ for $M = 1, 4, \text{ and } 16$. For comparison, the BER performance of CP-SC is also plotted. It can be seen from Figure 9 that when small M is used, the achievable BER performance of CP-SC degrades. On the other hand, TA-SC can achieve better BER performance even if small M is used. The required value of M in TA-SC is 1, 16, and 16 for $R = 1/2, 3/4, \text{ and } 8/9$, respectively, to achieve the BER performance similar to CP-SC using $M = 256$.

3.2. Complexity. The computational complexities of FDBD with QRM-MLD required for TA-SC and CP-SC are discussed. The complexity here is defined as the number of complex multiply operations. The required number of multiplications is shown in Table 2. First, we discuss the number of multiplications required for the squared Euclidean distance calculations. In FDBD with QRM-MLD, the number of multiplications required for the squared Euclidean distance

TABLE 2: Number of multiplications (uncoded with $N_c = 64$ and $L = 16$).

| | QPSK | 16QAM | 64QAM |
|---|---------|---------|----------|
| CP-SC | | | |
| DFT [20] | | 384 | |
| QR decomposition | | 266240 | |
| Multiplication of \mathbf{Q}^H | | 4096 | |
| Squared Euclidian distance calculations ($M = 256$) | 218271 | 876214 | 3505779 |
| Total | 2453432 | 9032864 | 35328512 |
| TA-SC | | | |
| DFT [20] | | 800 | |
| QR decomposition | | 518400 | |
| Multiplication of \mathbf{Q}^H | | 6400 | |
| Squared Euclidian distance calculations ($M = 8$) | 68504 | 137120 | 274304 |
| Total | 594104 | 662720 | 799904 |

calculations is $2X + XM \sum_{n=1}^{N_c-1} (n+2)$, when $M \leq X$. When $M > X$, it is a bit different from the case of $M \leq X$. For example, when $M = X^2$, the number of multiplications is $(n+2)X + (n+3)X^2 + MX \sum_{n=2}^{N_c-1} (n+2)$. It can be seen from Figure 7 that the required value of M in TA-SC is 8, 4, and 2 for QPSK, 16QAM, and 64QAM, respectively, to achieve the BER performance similar to CP-SC with $M = 256$ when $L = 16$ (uncoded case). Therefore, the computational complexity required for the squared Euclidean distance calculations in TA-SC is reduced to about 3.1, 1.6, and 0.8% of that of in CP-SC.

Next, we discuss the overall computational complexity, which is the sum of the complexity required for DFT, QR decomposition, multiplication of \mathbf{Q}^H , and the squared Euclidean distance calculation. When the DFT size at a receiver is J , the number of complex multiplications is J^2 for DFT in general (There are also efficient algorithms for DFT [20]), $J^3 + J^2$ for QR decomposition, and J^2 for the multiplication of \mathbf{Q}^H . In TA-SC, CP is replaced by a known TS, which is a part of DFT block at the receiver, and TS in the previous block acts as CP in the present block as shown in Figure 1. In order to let TS to play the role of CP, DFT size at the receiver must be the sum of data symbol block length and the TS length. In this paper, for TA-SC to keep the same data rate as CP-SC, we have set the data symbol block length and the TS length to be N_c and N_g , respectively. Therefore, DFT requires $(N_c + N_g)^2$ multiplications for the TA-SC case. Furthermore, it also requires large size of equivalent channel matrix \mathbf{H} than that of CP-SC (resulting in higher complexity for QR decomposition and multiplication of \mathbf{Q}^H). However, TA-SC can reduce significantly the computational complexity required for the squared Euclidean distance calculations as mentioned above. As a result, the overall computational complexity for TA-SC is smaller than that of CP-SC. The overall computational complexity in TA-SC is about 24, 7.4, and 2.3% of that in CP-SC for QPSK, 16QAM, and 64QAM, respectively, when $L = 16$ (uncoded case).

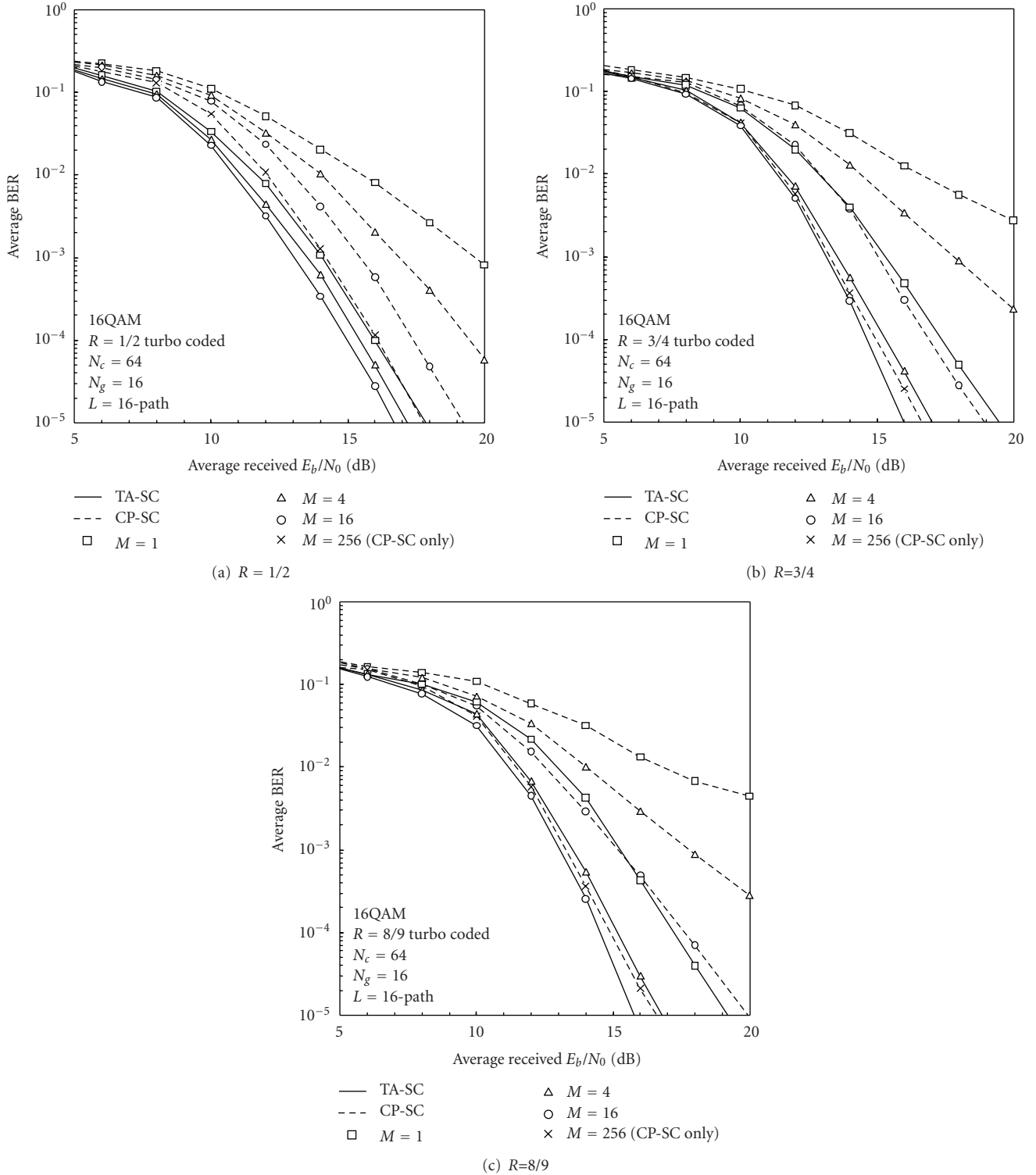


FIGURE 9: Average BER performance (turbo coded).

3.3. BER Performance Comparison between FDBD with QRM-MLD, MMSE-FDE, and FDISIC. Figure 10 compares the BER performances achieved by FDBD with QRM-MLD, MMSE-FDE, and frequency-domain iterative ISI cancellation (FDISIC) [6] when uncoded TA-SC is used. For FDISIC,

the use of three iterations is sufficient (i.e., $i = 3$) and therefore, only the BER performance curve with $i = 3$ is plotted. It can be seen from Figure 10 that when 16QAM is used, FDBD with QRM-MLD using $M \geq 2$ provides better BER performance than FDISIC using $i = 3$. When

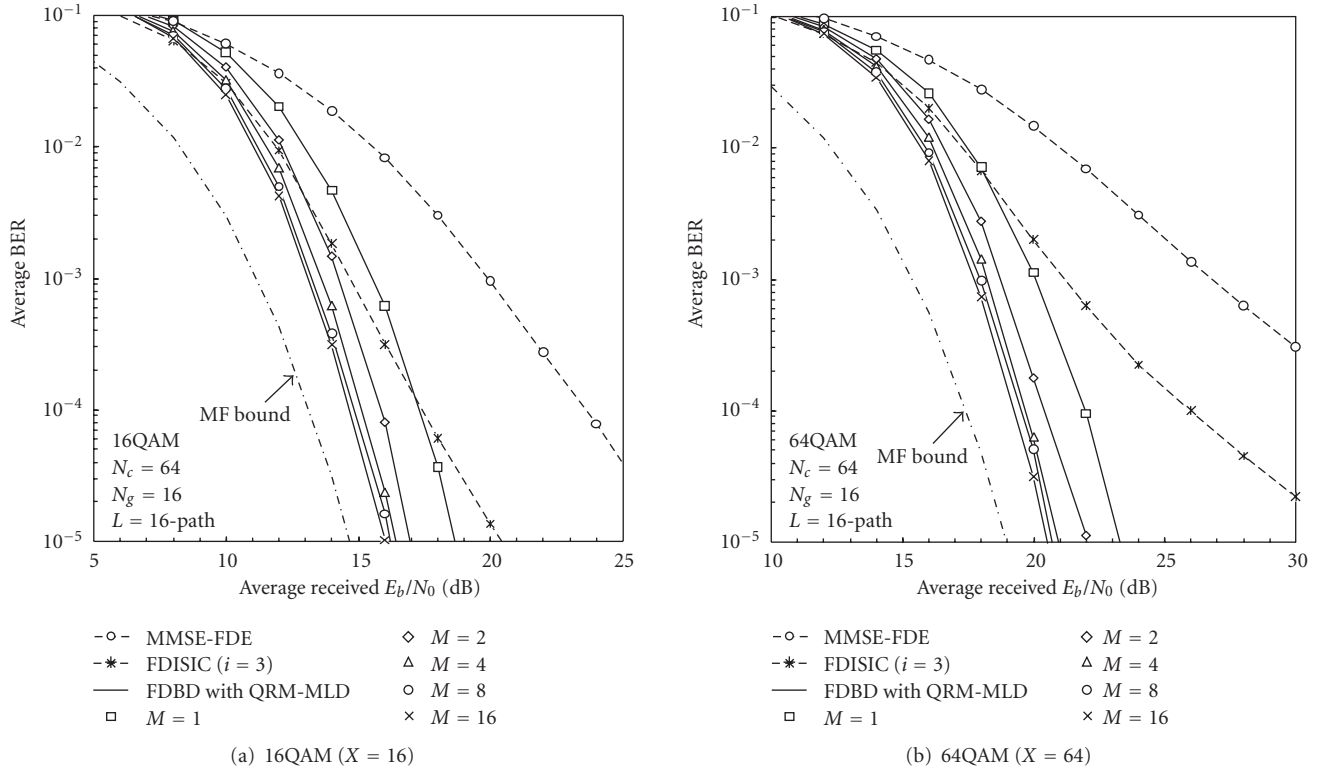


FIGURE 10: BER performance comparison between FDBD with QRM-MLD, MMSE-FDE, and FDISIC in uncoded TA-SC.

64QAM is used, FDBD with QRM-MLD can achieve better BER than FDISIC even if $M = 1$ is used. When 16 (64) QAM is used, FDBD with QRM-MLD using $M = 16$ can reduce the required E_b/N_0 for an average BER = 10^{-4} by about 2.8(6.8) dB compared to FDISIC using $i = 3$. FDBD with QRM-MLD requires about 20(80) times higher computational complexity than FDISIC for $N_c = 64$ and 16(64) QAM. FDBD with QRM-MLD can improve the BER performance at the cost of increased complexity. FDBD with QRM-MLD significantly reduces the complexity compared to the MLD. However, the computational complexity of FDBD with QRM-MLD is still much higher than MMSE-FDE and MMSE-FDE with iterative ISI cancellation. This is because QR decomposition and path selection using M-algorithm require high computational complexity. Therefore, further complexity reduction is necessary. This is left as an interesting future research topic. In the case of path selection using M-algorithm, the complexity can be reduced by using adaptive M algorithm [21], which adapts the value of M for each stage based on the respective channel condition. Quadrant detection scheme [22, 23] also can reduce the complexity required for the M-algorithm.

In Figure 11, we compare the BER performances of turbo-coded TA-SC using FDBD with QRM-MLD and also using MMSE-FDE. Turbo decoding with 6 iterations is performed after FDBD with QRM-MLD and also after MMSE-FDE. It can be seen from Figure 11 that when $R = 3/4$ and $8/9$, FDBD with QRM-MLD provides much better BER performance than MMSE-FDE. When $R = 3/4(8/9)$,

FDBD with QRM-MLD using $M = 16$ can reduce the required E_b/N_0 for an average BER = 10^{-4} by about 2.5(4.8) dB when compared to MMSE-FDE. However, when $R = 1/2$, a fairly large M ($M \geq 512$) must be used to achieve better BER performance than MMSE-FDE even if TA-SC is used. When smaller M than 256 is used, the LLR estimation error increases and hence, the achievable BER performance of FDBD with QRM-MLD is inferior to that of MMSE-FDE.

Joint channel decoding and QRM-MLD can be performed in an iterative fashion (called FDBD with iterative QRM-MLD in this paper) to improve the BER performance of low-rate turbo-coded TA-SC system. However, this paper is intended to show that when using FDBD with QRM-MLD, TA-SC system is superior to the well-known CP-SC system. FDBD with iterative QRM-MLD for coded TA-SC system is left as an interesting future study.

4. Conclusion

In this paper, we presented the application of FDBD with QRM-MLD to TA-SC, in which the known TS in the previous block acts as CP in the present block. The known TS is exploited in the M-algorithm to reduce the probability of removing the correct path at an early stages. We showed by computer simulation that the required number of surviving paths in the M-algorithm is greatly reduced in TA-SC. Therefore, the computational complexity required for FDBD with QRM-MLD is greatly reduced. The overall complexity required for FDBD with QRM-MLD in TA-SC is reduced

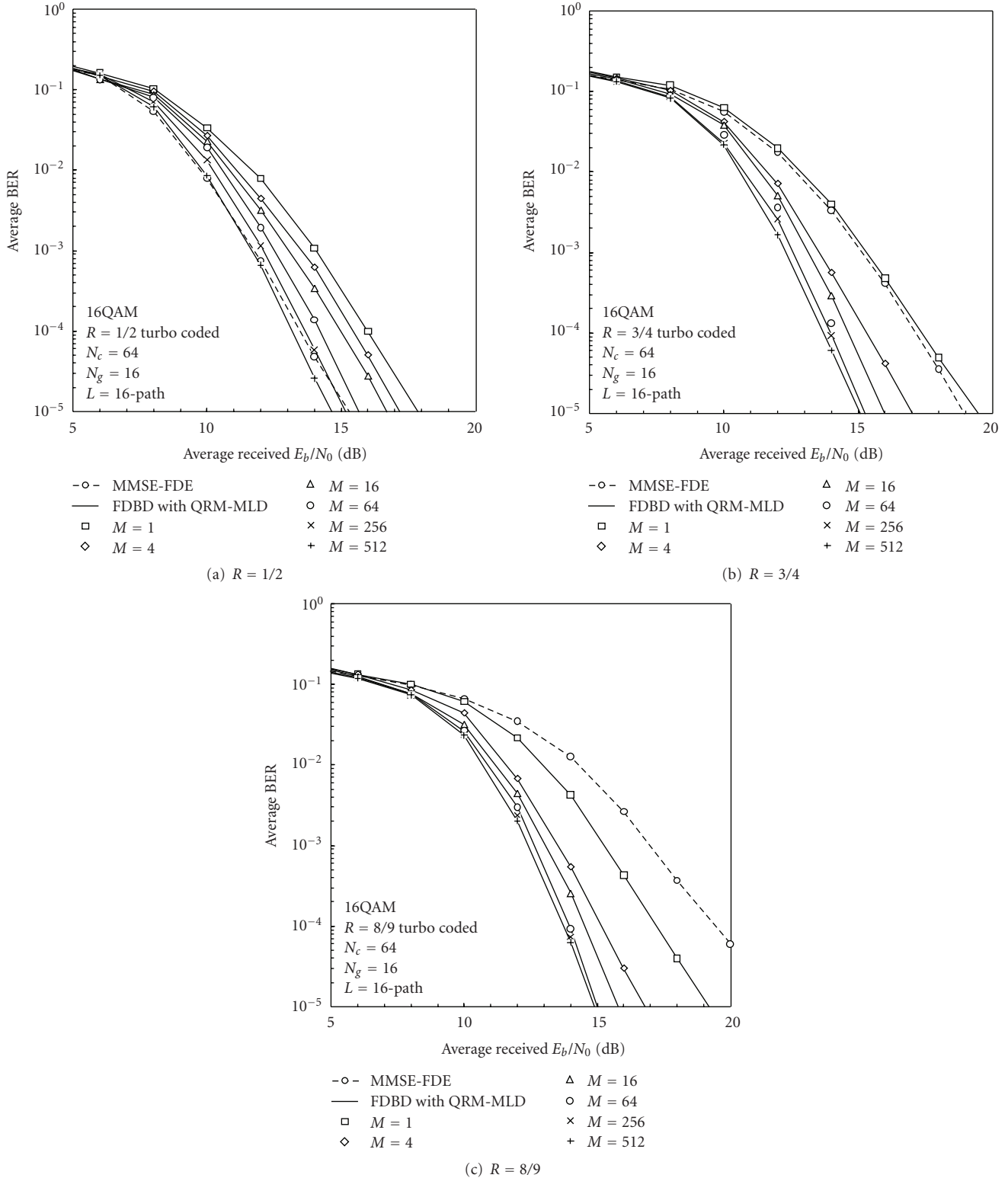


FIGURE 11: BER performance comparison between FDBD with QRM-MLD and MMSE-FDE in turbo-coded TA-SC.

to about 24%, 7.4%, and 2.3% of that in CP-SC for QPSK, 16QAM, and 64QAM, respectively, when $N_c = 64$ and $L = 16$ (uncoded case). We also showed that FDBD with QRM-MLD provides better BER performance than FDISIC

when uncoded TA-SC is used, but, at the cost of increased complexity.

We showed that when high-rate ($R \geq 3/4$) turbo-code is used, FDBD with QRM-MLD provides better BER

performance than MMSE-FDE. However, when low-rate ($R = 1/2$) turbo-code is used, a fairly large M ($M \geq 512$) must be used to achieve better BER performance than MMSE-FDE even if TA-SC is used. FDBD with iterative QRM-MLD may significantly improve the achievable BER performance. FDBD with iterative QRM-MLD for low-rate turbo-coded TA-SC system is left as an interesting future study. The use of TA-SC can reduce the computational complexity required for the M-algorithm, but still requires high computational complexity in the QR decomposition of the equivalent channel matrix. Another important future study is the further complexity reduction of FDBD with QRM-MLD.

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