

Fully differential NNLO computations with MATRIX

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Abstract We present the computational framework MATRIX (<http://matrix.hepforge.org/>) which allows us to evaluate fully differential cross sections for a wide class of processes at hadron colliders in next-to-next-to-leading order (NNLO) QCD. The processes we consider are $2 \rightarrow 1$ and $2 \rightarrow 2$ hadronic reactions involving Higgs and vector bosons in the final state. All possible leptonic decay channels of the vector bosons are included for the first time in the calculations, by consistently accounting for all resonant and non-resonant diagrams, off-shell effects and spin correlations. We briefly introduce the theoretical framework MATRIX is based on, discuss its relevant features and provide a detailed description of how to use MATRIX to obtain NNLO accurate results for the various processes. We report reference predictions for inclusive and fiducial cross sections of all the physics processes considered here and discuss their corresponding uncertainties. MATRIX features an automatic extrapolation procedure that allows us, for the first time, to control the systematic uncertainties inherent to the applied NNLO subtraction procedure down to the few permille level (or better).

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1 Introduction

Precision computations for standard model (SM) processes are vital for the rich physics programme at the LHC. The increasing amount of collected data pushes the experimental uncertainties down to the percent level, thereby demanding accurate predictions for many relevant physics processes. This holds not only for SM measurements. Also new-physics searches rely on a precise modelling of the SM backgrounds. In particular, the sensitivity to small deviations from the SM predictions directly depends on the size of theoretical uncertainties. Besides single vector-boson and Higgs boson production processes, vector-boson pair production is particularly important in that respect since anomalous triple gauge couplings would be first uncovered in cross sections and distributions of the diboson processes.

Precise SM computations require, in particular, the inclusion of QCD radiative corrections at the next-to-leading order (NLO), and if possible at the next-to-next-to-leading order (NNLO). NNLO QCD predictions for the simplest hadronic reactions have been available for quite some time. The pioneering computation of the inclusive cross section for vector-boson production was carried out in the 1990s [2]. The corresponding computation for Higgs boson production was performed about ten years later [3–5]. They were followed by the calculation of the rapidity distribution of vector bosons [6]. Shortly after, fully differential calculations for Higgs and vector-boson production started to appear [7–12]. This further step was essential to obtain realistic predictions since fully differential computations allow us to apply selection cuts on the produced boson and on its decay products, and to directly address all the relevant kinematic distributions. The last decade has seen a revolution in the field of NNLO computations for hadron collider processes: the calculations for associated production of a Higgs boson with a vector boson [13–16], Higgs boson production in bottom-quark annihilation [17–20], top-mass effects in Higgs boson production [21–25], HH [26,27], $\gamma\gamma$ [28,29], $Z\gamma$ [30–32], $W\gamma$ [31], ZZ [33–35], W^+W^- [36,37] and $W^\pm Z$ [38,39] production have been completed. NNLO results have been achieved also for further important processes like top-quark pair [40,41] and single top [42,43] production, dijet production [44], Higgs production through vector-boson fusion [45], $H + \text{jet}$ [46–48], $\gamma + \text{jet}$ [49], $Z + \text{jet}$ [50,51] and $W + \text{jet}$ [52]. Despite this tremendous progress, at present, publicly available NNLO programs typically carry out fully differential NNLO computations for a limited set of specific processes. Examples are FEWZ [53] and DYNNLO [12] for vector-boson production, FEHipro [7,54] and HNNLO [9,11] for Higgs boson production, and 2 γ NNLO [28] for diphoton production. A notable exception is MCFM [55], which in its current release features an NNLO implementation of single vector-boson and Higgs boson production, associated pro-

duction of a Higgs boson with a vector-boson, and diphoton production.

In this paper, we present the computational framework MATRIX,¹ which features a parton-level Monte Carlo generator capable of computing fiducial cross sections and distributions for Higgs boson, vector-boson and vector-boson pair production processes up to NNLO in QCD. For the first time, we consider all possible leptonic decay channels of the vector bosons, and we include spin correlations and off-shell effects by accounting for all resonant and non-resonant diagrams, thereby allowing the user to apply realistic fiducial cuts directly on the phase-space of the respective leptonic final state. MATRIX achieves NNLO accuracy by using a process-independent implementation of the q_T -subtraction formalism [9] in combination with a fully automated implementation of the Catani–Seymour dipole subtraction method [56,57] within the Monte Carlo program MUNICH.² All (spin- and colour-correlated) tree-level and one-loop amplitudes are obtained from OPENLOOPS [58,59]. Early versions of MATRIX have been used, in combination with the two-loop scattering amplitudes of Refs. [60–62], for the NNLO calculations of $Z\gamma$ [30,31], $W^\pm\gamma$ [31] ZZ [33,34], W^+W^- [36,37], $W^\pm Z$ [38,39] and HH [27] production³ and the importance of including NNLO corrections for these processes is evident for both total rates and differential distributions. MATRIX provides a fully automated extrapolation procedure that allows us, for the first time, to control the systematic uncertainties inherent to the q_T -subtraction procedure down to the few permille level (or better) for all NNLO predictions of inclusive or fiducial cross sections. The MATRIX framework offers a simple interface to a powerful code to carry out such computations in a relatively straightforward way, and its first public version is now available for download [1].

The manuscript is organized as follows: In Sect. 2 we give a general introduction into the MATRIX framework, where we review the q_T -subtraction formalism and describe the organization of the computations. Section 3 provides the list of processes available in MATRIX. We then provide detailed instructions on how to use the code: This involves the generation, compilation and running of a process to compute LO, NLO and NNLO cross sections in Sect. 4, and a detailed description of the relevant input files and parameters in Sect. 5. In Sect. 6 we provide benchmark predictions for total and fiducial rates, respectively, for all processes, including the results of our

¹ MATRIX is the abbreviation of “MUNICH Automates q_T subtraction and Resummation to Integrate X-sections”.

² MUNICH is the abbreviation of “MULTI-chaNnel Integrator at Swiss (CH) precision” – an automated parton-level NLO generator by S. Kallweit.

³ A first application of the code to the resummed transverse-momentum spectra of ZZ and W^+W^- pairs has been presented in Ref. [63] at NNLL+NNLO.

novel extrapolation procedure, and we discuss the relevant physics features of each process. A discussion of the systematic uncertainties of NNLO cross sections computed with q_T subtraction for a representative set of processes and details on the extrapolation procedure are presented in Sect. 7. In Sect. 8 we summarize our results. All predefined phase-space cuts are listed in Appendix A. How to extend the predefined set of cuts, distributions and dynamic scales by modifying the underlying C++ code is sketched in Appendix B. Finally, Appendix C provides a loose selection of solutions on compilation and running issues, which have been encountered in the testing phase of MATRIX and are expected to be potentially helpful for the user.

2 NNLO computations in the MATRIX framework

The computation of a QCD cross section at NNLO requires the evaluation of tree-level contributions with up to two additional unresolved partons, of one-loop contributions with one unresolved parton and of purely virtual contributions. The implementation of the corresponding scattering amplitudes in a complete NNLO calculation at the fully differential (exclusive) level is a highly non-trivial task because of the presence of infrared (IR) divergences at intermediate stages of the calculation. In particular, since the divergences affect real and virtual contributions in a different way, a straightforward combination of these components is not possible. Various methods have been proposed and used to overcome these issues at NNLO [9, 52, 64–76]. The method applied by MATRIX is transverse-momentum (q_T) subtraction [9], and it is briefly described below.

2.1 The q_T -subtraction formalism

The q_T -subtraction formalism [9] is a method to handle and cancel IR divergences at NLO and NNLO. The method exploits the fact that for the production of a colourless final-state system (i.e. a system composed of particles without QCD interactions) the behaviour of the q_T distribution⁴ at small q_T has a universal (process-independent) structure that is explicitly known up to NNLO through the formalism of transverse-momentum resummation [77, 78]. This knowledge is sufficient to fully determine the q_T dependence of the cross section at small q_T and to construct a non-local, but process-independent IR subtraction counterterm for this entire class of processes.⁵

⁴ Here and in the following, q_T always refers to the transverse momentum of the colourless final-state system under consideration.

⁵ The extension to heavy-quark production has been discussed in Ref. [79].

In the q_T -subtraction method, the cross section for a generic process $pp \rightarrow F + X$, where F is a colourless system as specified above, can be written up to (N)NLO as

$$d\sigma_{(N)NLO}^F = \mathcal{H}_{(N)NLO}^F \otimes d\sigma_{LO}^F + \left[d\sigma_{(N)LO}^{F+jet} - d\sigma_{(N)NLO}^{CT} \right]. \quad (1)$$

The term $d\sigma_{(N)LO}^{F+jet}$ represents the cross section for the production of the system $F+jet$ at (N)LO accuracy. If Eq. (1) is applied at NLO, the LO cross section $d\sigma_{LO}^{F+jet}$ can be obtained by direct integration of the corresponding tree-level amplitudes. If Eq. (1) is applied at NNLO, the NLO cross section $d\sigma_{NLO}^{F+jet}$ can be evaluated by using any available NLO subtraction method [56, 57, 80, 81] to handle and cancel the corresponding IR divergencies. Therefore, $d\sigma_{NLO}^{F+jet}$ is finite provided that $q_T \neq 0$, but it diverges in the limit $q_T \rightarrow 0$. The process-independent counterterm $d\sigma_{(N)NLO}^{CT}$ guarantees the cancellation of this divergence of the $F+jet$ cross section, and its general expression is provided in Ref. [78]. The numerical implementation of the contribution in the square bracket in Eq. (1), which is by construction finite in the limit $q_T \rightarrow 0$, is discussed in detail in Sect. 2.2. The computation is completed by evaluating the first term on the right-hand side of Eq. (1), which depends on the hard-collinear coefficients \mathcal{H}_{NLO}^F and \mathcal{H}_{NNLO}^F , respectively, at NLO and NNLO. The structure of the NLO coefficient \mathcal{H}_{NLO}^F has been obtained in a universal way from the one-loop corrections to the respective Born subprocess [82]. The general form of \mathcal{H}_{NNLO}^F is also known [83]: it has been derived from the explicit results for Higgs [84] and vector-boson [85] production in terms of the suitably subtracted two-loop corrections to the respective Born subprocesses. Thus, if the $q\bar{q} \rightarrow F$ (or $gg \rightarrow F$) two-loop amplitude is available, the coefficient \mathcal{H}_{NNLO}^F can be straightforwardly extracted.

2.2 Implementation within the MATRIX framework

MATRIX provides a process library for the computation of colour-singlet processes at NNLO QCD. The core of the MATRIX framework is the Monte Carlo program MUNICH, which is capable of computing both QCD and EW [86, 87] corrections to any SM process at NLO accuracy. MUNICH employs an automated implementation of the Catani–Seymour dipole-subtraction method for massless [56, 57] and massive [88] partons, and contains a general implementation of a very efficient, multi-channel based phase-space integration. All amplitudes up to one-loop level are supplied by OPENLOOPS⁶ [58] through an automated interface.

⁶ OPENLOOPS relies on the fast and stable tensor reduction of COLLIER [89, 90], supported by a rescue system based on quad-precision CUTTOOLS [91] with ONELOOP [92] to deal with exceptional phase-space points.

With this functionality inherited from MUNICH, MATRIX is immediately able to perform in principle any SM calculation up to NLO accuracy. To promote MUNICH to a Monte Carlo integrator at NNLO QCD, the F +jet cross section at NLO ($d\sigma_{\text{NLO}}^{\text{F+jet}}$) is combined with a process-independent implementation of the q_T -subtraction formalism for both gg - and $q\bar{q}$ -initiated processes within the MATRIX framework. The universal nature of the counterterm $d\sigma_{\text{NNLO}}^{\text{CT}}$ and the hard-collinear coefficients $\mathcal{H}_{\text{NNLO}}^{\text{F}}$ in Eq. (1) allows us to perform NNLO QCD computations⁷ for the hadroproduction of an arbitrary set of colourless final-state particles, provided that the corresponding two-loop virtual amplitudes for the Born-level subprocesses are available.

To this end, MATRIX includes the hard-collinear coefficients of Ref. [84,85], relevant for single Higgs and vector-boson production, and employs own implementations of the two-loop amplitudes for the associated production of a W/Z boson with a photon [60] and $\gamma\gamma$ [94] production, whereas external codes are used for on-shell ZZ [33] and W^+W^- [36] production.⁸ The two-loop amplitudes for off-shell production of massive vector-boson pairs[61] are taken from the publicly available code VVAMP [95]. Any new production process of colour singlets can be supplemented to the MATRIX library upon implementation of the corresponding two-loop amplitudes, since all remaining process-dependent ingredients are available in MUNICH + OPENLOOPS and the implementation of the q_T -subtraction formalism is fully general.

While the idea behind the q_T -subtraction formalism has been outlined in the previous section, one point deserves some additional discussion. The contribution in the square bracket in Eq. (1) is formally finite in the limit $q_T \rightarrow 0$, but both $d\sigma_{(\text{N})\text{LO}}^{\text{F+jet}}$ and $d\sigma_{(\text{N})\text{NLO}}^{\text{CT}}$ are separately divergent. Since the subtraction is non-local, we introduce a technical cut-off r_{cut} on the dimensionless quantity $r = q_T/M$ (M being the invariant mass of the colourless system) which renders both terms separately finite. Below this cut-off, $d\sigma_{(\text{N})\text{LO}}^{\text{F+jet}}$ and $d\sigma_{(\text{N})\text{NLO}}^{\text{CT}}$ are assumed to be identical, which is correct up to power-suppressed contributions. The latter vanish in the limit $r_{\text{cut}} \rightarrow 0$ and can be controlled by monitoring the r_{cut} dependence of the cross section. The absence of any residual logarithmic dependence on r_{cut} thus provides strong evidence of the correctness of the computation since any mismatch between the contributions would result in a divergence of the cross section for $r_{\text{cut}} \rightarrow 0$. The cut-off on r acts as a slicing parameter, and, correspondingly, the q_T -subtraction

method as implemented in MATRIX works very similar to a phase-space slicing method.

To monitor the r_{cut} dependence without the need of repeated CPU-intensive runs, MATRIX simultaneously computes the cross section at several r_{cut} values. The numerical information on the r_{cut} dependence is used to address the limit $r_{\text{cut}} \rightarrow 0$ by using a fit based on the results at finite r_{cut} values. The extrapolated result, including an estimate of the uncertainty of the extrapolation procedure, is provided at the end of each run. Details on the $r_{\text{cut}} \rightarrow 0$ extrapolation and its uncertainty estimate are presented in Sect. 7, where we also discuss the r_{cut} dependence of a representative set of the processes available in the first release of MATRIX.

3 Available processes in MATRIX

The list of the available processes in MATRIX is provided in Table 1: it includes Higgs boson, vector-boson and vector-boson pair production with all the possible leptonic decay channels of the vector bosons.

4 How to use MATRIX

The code is engineered in a way that guides the user from the very first execution of MATRIX to the very end of a run of a specific process, obtaining all relevant results. In-between there are certain steps/decisions to make (such as choosing the process, inputs, parameters, ...), which will be described in more detail throughout this and the next section.

The only thing we require the user of MATRIX to provide on the machine where the code is executed is a working installation of LHAPDF, which is a well-known standard code by now, such that `lhpdf-config` is recognized as a terminal command, or that the path to the `lhpdf-config` executable is specified in the file `MATRIX_configuration` (see Sect. 4.5 for more details on the configuration of MATRIX).⁹

4.1 Compilation and setup of a process

Assuming that the `MATRIX_v1.0.0.tar.gz` package is extracted and LHAPDF is installed, the simple command¹⁰

```
$ ./matrix
```

executed from the folder `MATRIX_v1.0.0` opens the MATRIX shell, an interactive steering interface for the compilation and the setup of a certain process. In principle, one can

⁷ On the same basis MATRIX automates also the small- q_T resummation of logarithmically enhanced terms at NNLL accuracy (see Ref. [63], and Ref. [93] for more details), which, however, is not yet included in the first release.

⁸ Private code provided by T. Gehrmann, A. von Manteuffel and L. Tancredi.

⁹ MATRIX has been tested to work with LHAPDF versions 5 and 6.

¹⁰ Note that global compilation settings (if necessary) must be set before starting the code; for options see Sect. 4.5.

Table 1 Available processes in MATRIX

$\{\text{process_id}\}$	Process	Description
pph21	$pp/p\bar{p} \rightarrow H$	On-shell Higgs-boson production
ppz01	$pp/p\bar{p} \rightarrow Z$	On-shell Z production
ppw01	$pp/p\bar{p} \rightarrow W^-$	On-shell W^- production with CKM
ppwx01	$pp/p\bar{p} \rightarrow W^+$	On-shell W^+ production with CKM
ppeex02	$pp/p\bar{p} \rightarrow e^-e^+$	Z production with decay
ppnenex02	$pp/p\bar{p} \rightarrow \nu_e\bar{\nu}_e$	Z production with decay
ppenex02	$pp/p\bar{p} \rightarrow e^-\bar{\nu}_e$	W^- production with decay and CKM
ppexne02	$pp/p\bar{p} \rightarrow e^+\nu_e$	W^+ production with decay and CKM
ppaa02	$pp/p\bar{p} \rightarrow \gamma\gamma$	$\gamma\gamma$ production
ppeexa03	$pp/p\bar{p} \rightarrow e^-e^+\gamma$	$Z\gamma$ production with decay
ppnenexa03	$pp/p\bar{p} \rightarrow \nu_e\bar{\nu}_e\gamma$	$Z\gamma$ production with decay
ppenexa03	$pp/p\bar{p} \rightarrow e^-\bar{\nu}_e\gamma$	$W^-\gamma$ with decay
ppexnea03	$pp/p\bar{p} \rightarrow e^+\nu_e\gamma$	$W^+\gamma$ with decay
ppzz02	$pp/p\bar{p} \rightarrow ZZ$	On-shell ZZ production
ppwxw02	$pp/p\bar{p} \rightarrow W^+W^-$	On-shell W^+W^- production
ppemexmx04	$pp/p\bar{p} \rightarrow e^-\mu^-e^+\mu^+$	ZZ production with decay
ppeexex04	$pp/p\bar{p} \rightarrow e^-e^-e^+e^+$	ZZ production with decay
ppeexnmnm04	$pp/p\bar{p} \rightarrow e^-e^+\nu_\mu\bar{\nu}_\mu$	ZZ production with decay
ppemxnmn04	$pp/p\bar{p} \rightarrow e^-\mu^+\nu_e\bar{\nu}_e$	W^+W^- production with decay
ppeexnenex04	$pp/p\bar{p} \rightarrow e^-e^+\nu_e\bar{\nu}_e$	ZZ / W^+W^- production with decay
ppemexnm04	$pp/p\bar{p} \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$	W^-Z production with decay
ppeexnex04	$pp/p\bar{p} \rightarrow e^-e^-e^+\bar{\nu}_e$	W^-Z production with decay
ppeexmxnm04	$pp/p\bar{p} \rightarrow e^-e^+\mu^+\nu_\mu$	W^+Z production with decay
ppeexexne04	$pp/p\bar{p} \rightarrow e^-e^+e^+\nu_e$	W^+Z production with decay

always follow the on-screen instructions; auto-completion of commands should work in all the MATRIX-related shells. The first thing to do is to choose the desired process that should be created and compiled, by typing the respective $\{\text{process_id}\}$, e.g.

```
|====> ppz01
```

for on-shell Z-Boson production. To find a certain $\{\text{process_id}\}$, the command

```
|====> list
```

will print a list of all available processes on screen, in the same format as given in Table 1. After entering the process, you will be asked to agree with the terms to use MATRIX. They require you to acknowledge the work of various groups that went into the computation of the present MATRIX process by citing the references provided in the file CITATION.bib. This file is provided with the results in every MATRIX run. In particular, a separate dialog appears for external computations if the implementation of a process is based on them. Simply type

```
|====> y
```

for each of these dialogs. Once agreed to the usage terms of MATRIX, the compilation script will automatically pursue the following steps:

- linking to LHAPDF [96];
- download and installation of OPENLOOPS [58,97] (skipped if already installed);
- installation of CLN [98] (skipped if already installed);
- installation of GINAC [98] (skipped if already installed);
- download of the relevant tree-level and one-loop amplitudes through OPENLOOPS (skipped if they already exist);
- compilation of MATRIX process (asked for recompilation if executable exists);
- setting up of the MATRIX process folder under the path $\text{run}/\{\text{process_id}\}_{\text{MATRIX}}$.

Thereafter, the MATRIX shell exits and the process is ready to be run from the created process folder. As instructed on screen, enter that folder,

```
$ cd run/{process_id}_MATRIX
```

and start a run for this process by continuing with the instructions given in Sect. 4.4.

We note that a process folder created by MATRIX may be moved to and used from essentially any location on the present machine. Moreover, a MATRIX process folder can be shipped to another system that contains a working installation of the respective process in MATRIX. This requires, however, to change the soft links for `bin/run_process` and `input/MATRIX_configuration` inside the process folder to the correct files of the MATRIX installation on the new system.

4.2 Compilation with arguments

The MATRIX script also features compilation directly via arguments: Type

```
$ ./matrix --help
```

in order to see the available options.

We summarize a few useful examples in the following:

1. To directly compile some specific process with ID `{process_id}`, simply use the following command:

```
$ ./matrix {process_id}
```

2. To clean the process before compiling (remove object files and executable), add the following option:

```
$ ./matrix {process_id} --clean_process
```

3. One can force the code to download the latest OPENLOOPS version even if there is an OPENLOOPS version found on the system, by using

```
$ ./matrix {process_id} --install_openloops
```

4. The command

```
$ ./matrix {process_id}
  --folder_name_extension _my_process_extension
```

will add an extension to the created process folder such that the default name will be changed to `run/{process_id}_MATRIX_my_process_extension`.

4.3 General structure of a process folder

Before providing details on how to actually start the run in a MATRIX process folder, it is useful to understand the essential parts of the general folder structure the code uses and produces while running. This will significantly simplify the comprehension of the code behaviour in the upcoming section. Figure 1 visualizes the general structure: The folders relevant to a user are `input`, `log` and `result`. They will be discussed in detail below, while the others should not be touched/are not of interest (especially for an unexperienced user); the folder `bin` contains the executable and will only be used to start the MATRIX run shell; the folder

`default.MATRIX` is the default folder for a run of this process, which is copied upon creation of each new run; the run folders denoted by `run_XX` contain the actual runs started by the user, where `XX` stands for the name given by the user, or an increasing number starting with 01 in case no name is given (see Sect. 4.4 for more details).

The folders `input`, `log` and `result` all follow the same structure: They contain subfolders of the form `run_XX` that correspond to each run started by the user, so that the relevant information is kept strictly separated between those different runs. The organization of these subfolders is identical for each run up to differences controlled by the inputs. We note that parts of the folder structure are created in the course of running. Figure 1 shows the folder structure at the very end of a complete run of the most complex type (i.e. including LO, NLO and NNLO with separate PDF choices). In the following we discuss the purpose and the organization of the relevant folders for such a run:

- `input`:
 - Three different cards can be modified in order to adjust all the run settings (of physics-related and technical kind), model parameters and distributions to be generated in the run. The respective files can be accessed directly or through the interface of the MATRIX run shell; see Sect. 5 for details on the input cards.
 - * The file `parameter.dat` controls the physics-related run settings, such as collider type, machine energy, PDFs, etc., but also technical parameters, such as which orders in perturbation theory should be computed, which precision is to be achieved in the run, if distributions are computed, if the loop-induced `gg` contribution is included, etc.
 - * The file `model.dat` sets all relevant model parameters, such as masses, widths, etc.
 - * The file `distribution.dat` gives the possibility to define distributions from the final-state particles with certain ranges, bin sizes, etc. (only effective if distributions are turned on in the file `parameter.dat`).
 - The process-specific file `MATRIX_configuration` for general MATRIX configurations inside the folder `input` is the same for all runs of this process and can be modified to use an individual configuration for this process (by default it is a soft link to the global file `MATRIX_configuration` inside the folder `MATRIX_v1.0.0/config`, but may be replaced by a copy of this file, see Sect. 4.5)
- `log`:
 - This folder is for debugging purposes only. Log files (`*.log` files) are saved for every single job that is

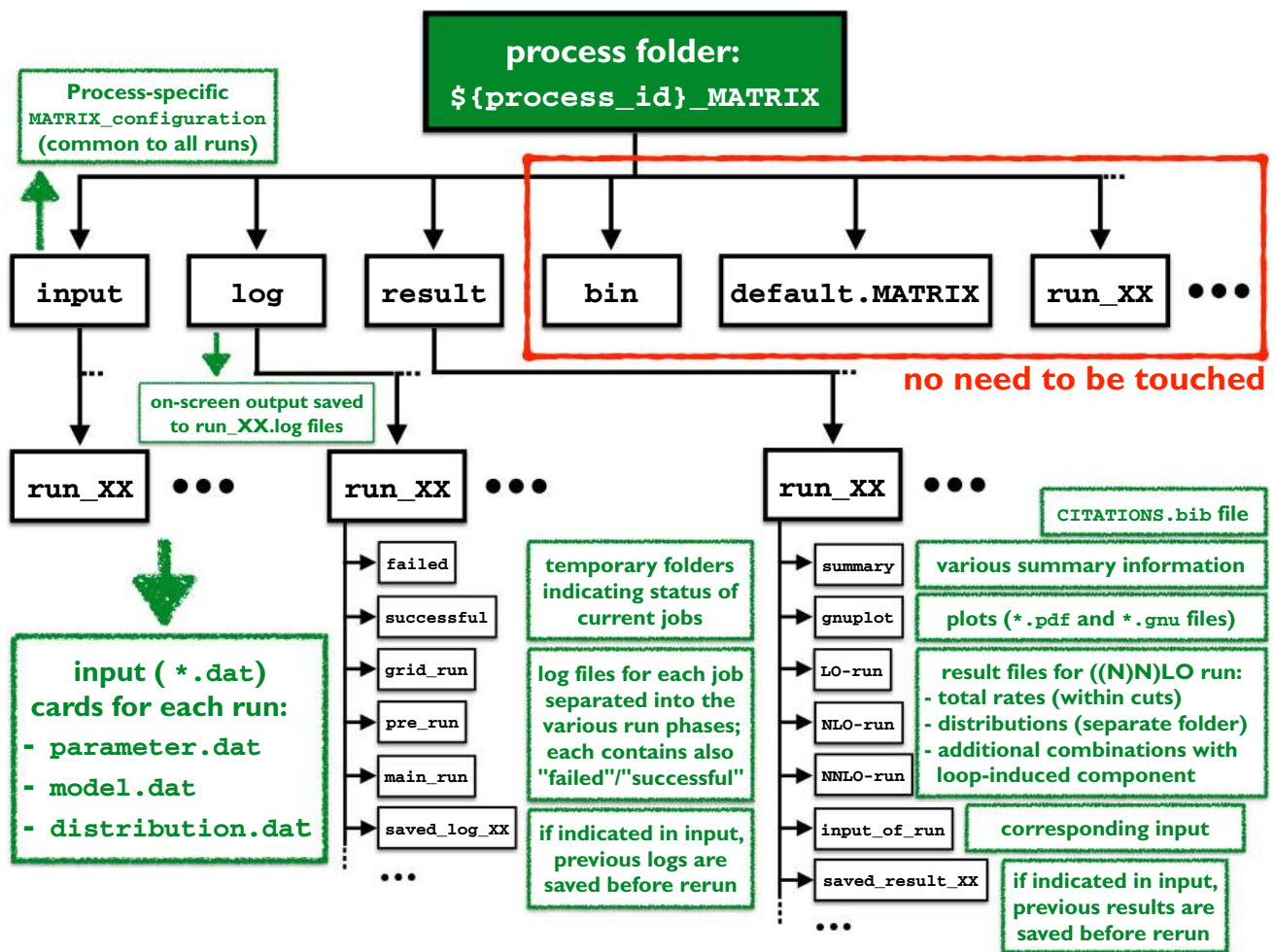


Fig. 1 Overview of the folder structure inside a MATRIX process folder

started during a run. Once a job has finished successfully, this is indicated by a file created in the successful folder. If a job fails (even after a certain number of retries) a corresponding file will be added to the failed folder.

- At the end of each running phase (*grid-run*, *pre-run*, *main-run*; see Sect. 4.4.1) the respective log files (including the successful and failed folders) are moved into the folders *grid_run*, *pre_run* and *main_run*, respectively.
- If an existing run, which has already created log files in the respective log folder, is picked up and started again, those log files are saved into a subfolder *saved_log_XX*, where XX is an increasing number starting at 01 (only working if the respective switch in the file *parameter.dat* is turned on; default: turned off).
- The on-screen output of the MATRIX run script is saved for each run to a file *run_XX.log*.

• result:

- This folder contains all relevant results that are generated during and collected at the end of a run.
- A file *CITATIONS.bib* is created with every run, which contains the citation keys for all publications that were relevant for the specific run. Please cite these papers if you use the results of MATRIX to acknowledge the efforts that have been made to obtain these results with MATRIX.
- The folder *summary* contains information on the respective run. In particular, the summary of all total rates (possibly within cuts), which are also printed on screen at the end of each run, is saved to the file *result_summary.dat* (currently the only file there).
- In the folder *gnuplot* one finds (automatically generated) *.gnu and *.pdf files for every distribution created during the run. Its *histogram* subfolder contains the data prepared and used for these plots.

Additionally, all pdf files are combined into a single file `all_plots.pdf` using the `pdfunite` binary. If either `gnuplot` or `pdfunite` do not exist on the system, the corresponding `*.pdf` files are not created.

- The total rates and distributions are saved to plain text files in the folders `LO-run`, `NLO-run` and `NNLO-run`. This separation reflects the different PDF sets that can be chosen for each of the three runs (in the file `parameter.dat`; see Sect. 5.1.1.3). Total rates (possibly within cuts) are saved to the files `rate_XX.dat` (including scale variations if turned on in the file `parameter.dat`; see Sect. 5.1.1.2), where, depending on the considered order, `XX` can be `LO`, `NLO_QCD`, `NNLO_QCD` and `loop-induced_QCD`. Additional files `rate_extrapolated_XX` are created for total rates, which are computed with the q_T -subtraction method (NNLO, and possibly NLO): They provide extrapolated results for $r_{\text{cut}} \rightarrow 0$ as the final results, see Sect. 7, while the original rate files contain only the cross sections calculated at a finite r_{cut} value. Inside each of the `*-run` folders the distributions are saved to a folder `distributions` (including minimum and maximum results of the scale variations). There is an extra distribution folder `distributions_NLO_plus_loop-induced` inside the folder `NLO-run`, which contains the results of the NLO distributions combined with the loop-induced contribution (if turned on). Besides, there are folders `distributions_NLO_prime_plus_loop-induced` and `distributions_only_loop-induced` inside the folder `NNLO-run` which contain the combined $\text{NLO}' + gg$ contribution¹¹ and the pure gg contribution, respectively.
- The folder `input_of_run` contains the three input cards (`parameter.dat`, `model.dat`, `distribution.dat`), which were copied at the beginning of the respective run.
- If an existing run, which has already created results in the respective result folder, is picked up and started again, those results are saved into a subfolder `saved_result_XX`, where `XX` is an increasing number, starting with 01 (only working if the respective switch in the file `parameter.dat` is turned on; default: turned on).

¹¹ $\text{NLO}' + gg$ refers to the sum of the NLO and gg contributions, where both are computed with NNLO PDFs. This can generally be regarded as the best prediction before the full NNLO became available.

4.4 Running a process

4.4.1 Running with interactive shell

From the MATRIX process folder (default: `run/${process_id}_MATRIX`) the command¹²

```
$ ./bin/run_process
```

opens the MATRIX run shell, an interactive steering interface for handling all run-related settings, inputs and options.¹³ From here on one can simply follow the on-screen instructions of the MATRIX run shell; we thus only summarize the most relevant steps in the following.

First, one must choose a name,

```
|===>> ${run_name}
```

for the run, which has to begin with `run_`, to generate a new run. Alternatively, one can also list and choose one of the runs which already exist (have been created before). As in all MATRIX shells, auto-complete should work here. The general idea is that each run is separate, i.e. each of these runs will create its own run folder (`${run_name}`) and the corresponding subfolders inside `input`, `log` and `result`. An old run can only be picked up when the previous one is not running any more. One should, however, be careful with this option since all data of the old run will be overwritten (except for possibly the results and the log files, see Sect. 4.3).

Next, we can choose from a list of several commands printed on screen. These commands are divided into three groups: general commands, input to modify, run modes. Information on each individual command (`${command}`) can be received through the help menu by typing

```
|===>> help ${command}
```

In order to directly modify the input cards from the shell (opened in the default editor¹⁴), one can simply type the name of the input file

```
|===>> ${name_input_file}
```

where `${name_input_file}` can be either `parameter`, `model` or `distribution`. Changes will be done directly to the respective files `parameter.dat`, `model.dat` or `distribution.dat` inside the folder `input/${run_name}` (see Sect. 4.3). Details on the

¹² Note that the global configuration (if necessary) must be set in the file `input/MATRIX_configuration` before starting the run; see Sect. 4.5 for a description of the general options.

¹³ The script can also be started with certain arguments, see Sect. 4.4.2.

¹⁴ The default editor can be set through the `default_editor` variable of the file `MATRIX_configuration`, or by exporting directly the `EDITOR` environment variable on the system, e.g. `export EDITOR=emacs`, where the respective editor (here: `emacs`) must be installed and recognized as a terminal command.

impact of the various parameters, which can be accessed through the input files, are described in Sect. 5.¹⁵

After adjusting the input cards to obtain the desired results, we can start the run by typing

```
|====>> run
```

This will start a complete run, no human intervention is needed from now on. Once the run is finished the results from the run are collected in the respective folder `result/${run_name}` as printed on screen (see Sect. 4.3 for details on the result-folder structure), the most relevant results, which are the total rates, are also printed on screen at the very end of the run.¹⁶ We emphasize that for every run a `CITATION.bib` file is created and provided inside the folder `result/${run_name}`. Please cite these papers if you use the results of `MATRIX` to acknowledge the efforts that have been made to obtain these results with `MATRIX`.

When performing a time-extensive (NNLO) run, we recommend to start `MATRIX` from a window manager (e.g. `screen` or `tmux`) in order to be able to logout from the present machine during the run. An alternative is to start `MATRIX` with `nohup` as explained in the second example of Sect. 4.4.2.

Running phases of a complete run

A complete run is divided into various stages (*running phases*), each of which may be started directly from the run shell by typing the name of the respective run mode (`${run_mode}`). One must bear in mind, however, that every run stage depends on all previous run stages and will fail in case one of the previous ones has not finished successfully. The order of the run stages is as follows:

- *grid-run*: First, the integration grids are created in the warm-up phase (`run_grid`).
- *pre-run*: Next, the expected runtimes for the *main-run* are extrapolated from a quick pre-run phase (`run_pre`); some preliminary results are already printed on screen.
- *main-run*: Then, the main run is started, computing all results to the desired precision (`run_main`).
- *result-collection*: Finally, the results are collected, and all distributions are automatically plotted if `gnuplot` is installed (`run_results`).

¹⁵ By default the inputs are already set to use reasonable cuts and parameters for each process; the default run (without changing the cards) computes a simple LO cross section with 1% precision, which we recommend to use when running for the first time in order to test whether everything is working properly. As this run should be very quick (a few minutes), this test can be done in local mode (see Sect. 4.5 for the settings in the file `input/MATRIX_configuration`).

¹⁶ Note that `MATRIX` provides the extrapolated cross section for $r_{\text{cut}} \rightarrow 0$ as a final result at NNLO (and at NLO if the q_T -subtraction procedure is used also at NLO) including an extrapolation uncertainty, see Sect. 7, which is printed on screen after the cross section with a fixed r_{cut} value.

Note that the *result-collection* will always be started automatically after a successful *main-run*. Furthermore, if the run mode `run_pre_and_main` is used, the code will start from the *pre-run* (assuming a successful *grid-run*) and automatically continue with the *main-run* and *result-collection*.

Starting from one of these intermediate stages can be useful in many respects. One example is the continuation of a run after some unwanted behaviour, if some stages have already passed successfully and one would like to restart from one of the later stages. Note that all jobs in the requested run stage are removed and started from scratch. To continue a run while keeping already successfully finished jobs of the requested run stage, or to run with increased precision, the `--continue` command can be used, see example seven of Sect. 4.4.2. Another example is running again with a modified set of inputs. In the latter case it is sufficient to only restart the *main-run* as follows:

```
$ ./bin/run_process
```

to start the script,

```
|====>> ${run_name}
```

to pick up the old run with name `${run_name}`, and

```
|====>> parameter
```

to change, e.g., the PDF set in the file `parameter.dat` (if not done by hand before). It is essential to also uncomment `include_pre_in_results = 0` in the same file in order to avoid mixing of the different settings in *pre-run* and *main-run* in the result combination. After that, the *main-run* is started by

```
|====>> run_main
```

Other run modes to be selected involve different behaviour of the code, such as only setting up the folder `${run_name}` and the corresponding subfolders inside `input`, `log` and `result` (`setup_run`) without starting the run (this is helpful if one wants to change the inputs by hand, but not through the interface, e.g. by copying the input files from somewhere else); deleting a given run including its respective subfolders inside `input`, `log` and `result` (`delete_run`); etc.

4.4.2 Running with arguments

The run script allows some of the various settings, which are typically controlled interactively, to be controlled directly by arguments in its shell command. This enables, e.g., the possibility to directly start a certain run without having to interact with the interface. Type

```
$ ./bin/run_process --help
```

in order to see all available options.

We summarize a few useful examples in the following:

1. The command

```
$ ./bin/run_process ${run_name}
  --run_mode run
```

will create (pick up, if `${run_name}` exists) the run with name `${run_name}`, and directly start a complete run (due to `--run_mode run`), with the default inputs (or the ones already set in `${run_name}`).¹⁷ The `${run_mode}` may be chosen as any of the various commands outlined at the end of the previous section, e.g. `--run_mode run_pre_and_main` to start the run directly from the *pre-run* (assuming a successful *grid-run* has already been done).

2. The same command can be used in combination with `nohup`

```
$ nohup ./bin/run_process ${run_name}
  --run_mode run > run.out &
```

to run MATRIX in the background while one is still able to logout from the present machine. The on-screen output of MATRIX in this example is written to the file `run.out`.

3. The command

```
$ ./bin/run_process ${run_name}
  --delete_run
```

will delete the run with name `${run_name}`, including its respective subfolders inside `input`, `log` and `result`.

4. The command

```
$ ./bin/run_process ${run_name} --setup_run
```

will create a run with name `${run_name}` including its respective subfolders inside `input`, `log` and `result` without starting the run. One may then modify the input files directly by hand (without using the MATRIX shell) and continue with starting the run as described under 1.).

5. One may want to copy, e.g. as a backup, some existing (possibly finished) run. The command

```
$ ./bin/run_process ${run_name}
  --copy_run_from ${run_another_name}
```

allows to make a complete copy of an existing run with name `${run_another_name}` to a new run with name `${run_name}`. This may take quite a while in case a finished run is copied, as the run folder could have a rather large size.

6. In certain situations it may be helpful to use inputs other than the default inputs when creating a new run. The command

```
$ ./bin/run_process ${run_name}
  --input_dir ${any_folder_inside_input}
```

will create a run with name `${run_name}`, and the three input files will be copied from the folder `${any_folder_inside_input}` inside the folder `input`. This may, of course, also be the name of another run whose inputs should be used. The only requirement is that a folder with the given name exists inside the folder `input` and contains the files `parameter.dat`, `model.dat` and `distribution.dat`.

7. MATRIX provides the possibility to continue a run, while deleting only the content of later run stages, but not of the current run stage. This is very useful in two situations: First, a run has crashed in the middle or at the end of a run stage, but several jobs have already finished successfully. Second, the precision of a run should be improved by adding more statistics to a previous run. In both cases the command

```
$ ./bin/run_process ${run_name}
  --run_mode run_main --continue
```

will continue the run with name `${run_name}` and not delete any job that has already finished successfully. Note that it is absolutely required not to change any of the inputs, except for a possibly increased precision, with respect to the previous run if the flag `--continue` is used. Any other `${run_mode}` may be chosen to be continued in this way.

4.5 Configuration file

Before turning to physics-related and technical settings relevant for a specific MATRIX run in Sect. 5, we discuss the global parameters that steer the general behaviour of the code. The file `MATRIX_configuration` controls various global settings for both the compilation and the running of the code. The general idea is that these configurations can be made once and for all, depending on the respective environment one is working on: one can, e.g., set the relevant paths for the compilation (if not found automatically), choose local running or specify the cluster scheduler available on the present machine, etc. The global settings that affect the running of a process may still be altered at a later stage (before starting the respective run) and can be chosen different for different process folders. The main file `MATRIX_configuration` can be found in the folder `config` inside the MATRIX main folder. This file is linked during each setup of a process (see Sect. 4.1) into the folder `input` of the respective process folder. This soft link may be replaced by the actual file such that each process can have its own configuration file. This allows for process-specific run settings, and one can, e.g., change from cluster to local

¹⁷ Note that in the default inputs only a simple LO run is enabled.

Table 2 Parameters to be set in the file `MATRIX_configuration`

Variable	Description
<code>default_editor</code>	Sets the editor to be used for interactive access to input files. Alternatively, the default editor may be configured directly by exporting the <code>EDITOR</code> environment variable on the system
<code>mode</code>	Switch to choose local (multicore) run mode or cluster mode
<code>cluster_name</code>	Name of the cluster; currently supported: Slurm, LSF (e.g. <code>lxplus</code>), Condor, HTCondor (e.g. <code>lxplus</code>), PBS, Torque, SGE.
<code>cluster_queue</code>	Queue/Partition of the cluster to be used for cluster submit; not required in most cases
<code>cluster_runtime</code>	Runtime of jobs in cluster submit; not required in most cases
<code>cluster_submit_line[1-99]</code>	Lines in cluster submit file to add cluster-specific options
<code>max_nr_parallel_jobs</code>	Number of cores to be used in multicore mode; maximal number of available cores on cluster
<code>parallel_job_limit</code>	Upper threshold for number of parallel jobs; if exceeded, user intervention required to continue.
<code>max_jobs_in_cluster_queue</code>	If cluster queue contains more jobs than this value, <code>MATRIX</code> will wait until jobs finish before submitting further jobs
<code>path_to_executable</code>	This path can be set to the folder that contains the executables of the processes (usually <code>bin</code> in the <code>MATRIX</code> main folder), and provides the possibility to use an executable from a different <code>MATRIX</code> installation; not required in most cases
<code>max_restarts</code>	If there are still jobs left that failed after all jobs finished, <code>MATRIX</code> will restart all failed jobs n times when this parameter is set to n
<code>nr_cores</code>	Number of cores to be used for the compilation; determined automatically by the number of available cores on the machine if not set
<code>path_to_lhapdf</code>	Path to <code>lhpdf-config</code> ; not required in most cases
<code>path_to_openloops</code>	Path to the <code>openloops</code> executable; not required in most cases
<code>path_to_ginac</code>	Path to the <code>ginac</code> installation; not required in most cases
<code>path_to_cln</code>	Path to the <code>cln</code> installation; not required in most cases
<code>path_to_libgfortran</code>	Path to the <code>libgfortran</code> library; not required in most cases. This path can also be used if the <code>libquadmath</code> library is not found, to be set to the respective <code>lib</code> folder
<code>path_to_gsl</code>	Path to <code>gsl-config</code> ; not required in most cases

run mode for a specific process (or even only for a dedicated run and change it back after having started the run).¹⁸

The options controlled by the file `MATRIX_configuration` are listed in Table 2.

5 Settings of a `MATRIX` run

In this section all relevant input settings are discussed. Most of them are directly physics-related, but there are also a few more technical parameters.

5.1 Process-independent settings

Every run of a process contains three input files in its respective subfolder inside `input`, which can be modified by the user. The generic inputs in the files `parameter.dat`, `model.dat` and `distribution.dat` of each `MATRIX` run are described in the following.

¹⁸ Since the file `MATRIX_configuration` is read only at the beginning of a run, any change done after that has no effect.

5.1.1 Settings in `parameter.dat`

All main parameters, related to the run itself or the behaviour of the code, are specified in the file `parameter.dat`. Most of them should be completely self-explanatory, and we will focus our discussion on the essential ones. The settings can be organized into certain groups and are discussed in the order they appear in the file `parameter.dat` for the sample case of $Z\gamma$ production (where applicable).

5.1.1.1 General run settings

```
process_class = pp-emepa+X # process id
E             = 6500.      # energy per beam
coll_choice  = 1          # (1) PP collider;
                        (2) PPbar collider
```

`process_class` A unique identifier for the process under consideration; it should never be touched by the user; in particular, no other process can be chosen at this stage. Its sole purpose is to identify which process the respective parameter file belongs to.

`E` Value of the energy per beam; assumed to be identical for both initial hadrons, i.e. equal to half of the collider energy. Here and in what follows, all input parameters with energy dimension are understood in units of GeV.

5.1.1.2 Scale settings

```

scale_ren      = 91.1876      # renormalization (muR) scale
scale_fact     = 91.1876      # factorization (muF) scale
dynamic_scale  = 6            # dynamic ren./fac. scale
                                # 0: fixed scale above
                                # 1: invariant mass (Q) of system (of the colourless final states)
                                # 2: transverse mass (mT^2=Q^2+pT^2) of the colourless system
                                # 3: transverse mass of photon (note: mT_photon=pT_photon)
                                # 4: transverse mass of Z boson (lepton system, mT_lep1+lep2)
                                # 5: geometric average of mT of photon and mT of Z boson
                                # 6: quadratic sum of Z mass and mT of the photon (mu^2=m_Z^2+mT_photon^2)
factor_central_scale = 1.      # relative factor for central scale
scale_variation = 1            # switch for muR/muF variation (0) off; (1) 7-point; (2) 9-point
variation_factor = 2          # symmetric scale variation factor up and down

```

`dynamic_scale` This parameter allows the user to choose between the specified fixed renormalization and factorization scales (`scale_ren/scale_fact`) and dynamic ones. A dynamic scale must be implemented individually for the process under consideration. For all processes two dynamic scales are provided by default: the invari-

`variation_factor` This (integer) value determines by which factor with respect to the central scale the scale variation is performed.

5.1.1.3 Order-dependent run settings

```

# LO
run_LO         = 1            # switch for LO cross section (1) on; (0) off
LHAPDF_LO      = NNPDF30_lo_as_0118 # LO LHAPDF set
PDFsubset_LO   = 0            # member of LO PDF set
precision_LO   = 1.e-2       # precision of LO cross section

# NLO
run_NLO        = 0            # switch for NLO cross section (1) on; (0) off
LHAPDF_NLO     = NNPDF30_nlo_as_0118 # NLO LHAPDF set
PDFsubset_NLO  = 0            # member of NLO PDF set
precision_NLO  = 1.e-2       # precision of NLO cross section
NLO_subtraction_method = 1    # switch for (1) Catani-Seymour (2) qT subtraction at NLO

# NNLO
run_NNLO       = 0            # switch for NNLO cross section (1) on; (0) off
LHAPDF_NNLO    = NNPDF30_nnlo_as_0118 # NNLO LHAPDF set
PDFsubset_NNLO = 0            # member of NNLO PDF set
precision_NNLO = 1.e-2       # precision of NNLO cross section
loop_induced   = 1            # switch to turn on (1) and off (0) loop-induced gg channel

switch_qT_accuracy = 0        # switch to improve qT-subtraction accuracy (slower numerical convergence)

```

ant mass (`dynamic_scale = 1`) and the transverse mass (`dynamic_scale = 2`) of the colourless final-state system. The relevant file of the C++ code is `prc/${process_id}/user/specify.scales.cxx` in the MATRIX main folder (recompilation needed if modified!). All additional dynamic scale choices for each process are discussed in Sect. 5.2. A user interested in setting a specific dynamic scale which has not been implemented yet for this process is advised to contact the authors.¹⁹

`factor_central_scale` A relative factor that multiplies the central scale; particularly useful for dynamic scales.

A single run of a process in MATRIX involves up to three different orders (`order`), namely LO, NLO and NNLO. For each of these orders we may choose the following inputs:

`run_order` Switch to turn on and off the order `order` in the run.

`LHAPDF_order` LHAPDF string that determines the PDF set used at this order with the respective member `PDFsubset_order`.

`precision_order` Desired numerical precision of the cross section (within cuts) of this run.

`NLO_subtraction_method` Switch to choose the NLO subtraction scheme: For the NLO part of the computation two different subtraction schemes are available. The default is the Catani–Seymour dipole subtraction, which comes with the advantage of being fully local and thus does

¹⁹ A short description on how to add user-specified scales, cuts and distributions to the C++ code is given in Appendix B for the advanced user.

not lead to any r_{cut} dependence. The NLO computation can also be performed by means of the q_T -subtraction method. The option to use both subtraction schemes in the same run is currently not supported.

`loop_induced` For certain processes (such as ZZ , W^+W^- , ...) a loop-induced gg contribution enters at the NNLO; this contribution is separately finite and can be included or excluded by this switch; if a process has no loop-induced gg component, the switch is absent.

`switch_qT_accuracy` Switch specific to processes with large r_{cut} dependence (in particular processes with final-state photons). The lowest calculated value of r_{cut} is changed from $r_{\text{cut}} = 0.15\%$ (`switch_qT_accuracy = 0`) to $r_{\text{cut}} = 0.05\%$ (`switch_qT_accuracy = 1`) in order to improve the accuracy of the q_T -subtracted NNLO cross section, at the cost of numerical convergence. We refer to Sect. 5.2 for further information.

5.1.1.4 Settings for fiducial cuts

We first note that certain settings, such as photon isolation, naturally only affect dedicated processes. The default input files are adapted such that they only contain options that are of relevance for the respective process. It is not recommended to add any new blocks to the input files in order to avoid unwanted behaviour, although such additional settings would usually just not have any impact on the run.

Jet algorithm

```
jet_algorithm = 3           # (1) Cambridge-Aachen (2) kT (3) anti-kT
jet_R_definition = 0       # (0) pseudo-rapidity (1) rapidity
jet_R = 0.4                # DeltaR
```

`jet_algorithm` Switch to choose between three pre-defined jet-clustering algorithms: Cambridge-Aachen [99, 100], k_T [101] or anti- k_T [102].²⁰

```
frixione_isolation = 1     # switch for Frixione isolation (0) off;
                           # (1) with frixione_epsilon, used by ATLAS;
                           # (2) with frixione_fixed_ET_max, used by CMS
frixione_n = 1             # exponent of delta-term
frixione_delta_0 = 0.4     # maximal cone size
frixione_epsilon = 0.5     # photon momentum fraction
#frixione_fixed_ET_max = 5 # fixed maximal pT inside cone
```

`jet_R_definition` According to the setting of this switch, the distance ΔR of jets is defined either via pseudo-rapidity or rapidity,

²⁰ We note that, for the processes considered in the first release of MATRIX, the three algorithms are actually equivalent, since the final state contains at most two partons. Also parameter `jet_R_definition` has no impact for final states with at most two partons, as the pseudo-rapidity and rapidity of massless partons is identical.

$$\Delta R_{jj} = \sqrt{\Delta\eta_{jj}^2 + \Delta\phi_{jj}^2} \quad \text{or} \quad \Delta R_{jj} = \sqrt{\Delta y_{jj}^2 + \Delta\phi_{jj}^2}. \tag{2}$$

`jet_R` Value of the jet radius used for the jet definition.

This sets the relevant parameters for the jet algorithm. Selection cuts on jets, including the setting for their minimal transverse momenta and maximal (pseudo-)rapidity, are described below under the paragraph *Particle definition and generic cuts*.

Photon isolation

For all processes involving identified final-state photons, MATRIX relies on the smooth-cone photon isolation procedure from Ref. [103], which works as follows: For every cone of radius $\delta = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} < \delta_0$ around a final-state photon, the total amount of hadronic (partonic) transverse energy E_T inside the cone has to be smaller than $E_T^{\text{max}}(\delta)$,

$$\sum_{i=\text{hadrons(partons)}} p_{T,i} \Theta(\delta - \delta_{i\gamma}) \leq E_T^{\text{max}}(\delta) = E_T^{\text{ref}} \left(\frac{1 - \cos \delta}{1 - \cos \delta_0} \right)^n \quad \forall \delta \leq \delta_0, \tag{3}$$

where E_T^{ref} is a reference transverse-momentum scale that can be chosen to be either a fraction ϵ_γ of the transverse momentum of the respective photon ($p_{T,\gamma}$) or a fixed value (p_T^0),

$$E_T^{\text{ref}} = \epsilon_\gamma p_{T,\gamma} \quad \text{or} \quad E_T^{\text{ref}} = p_T^0. \tag{4}$$

`frixione_isolation` Switch for smooth-cone photon isolation with three possible settings: turned off; using one or the other alternative in Eq. (4).

`frixione_n` Value of n in Eq. (3).

`frixione_delta_0` Value of δ_0 in Eq. (3).

`frixione_epsilon` Value of ϵ_γ in Eq. (4). Only used for `frixione_isolation = 1`, and must be commented if `frixione_isolation = 2`.

`frixione_fixed_ET_max` Value of p_T^0 in Eq. (4). Only used for `frixione_isolation` = 2, and must be commented if `frixione_isolation` = 1.

Selection cuts on photons, including the setting for their minimal transverse momenta and maximal (pseudo-)rapidity, are described in the following paragraph.

Particle definition and generic cuts

Some fiducial cuts are defined in a general, i.e. process-independent, way by requiring a minimum and maximum multiplicity of a certain (group of) particle(s) with given requirements (such as minimal transverse momentum or maximal rapidity). For that purpose, the user can define which requirements (clustered) parton-level objects need to fulfil in order to be considered particles that can be accessed in scale definitions, phase-space cuts and distributions. Table 3 summarizes the content of all relevant predefined particle groups. All objects entering these groups will be ordered by their transverse momenta, starting with the hardest one.

The parameters `define_y` $\{\text{particle_group}\}$ and `define_eta` $\{\text{particle_group}\}$ set the geometric range for the acceptance of particles in $\{\text{particle_group}\}$, in terms of upper limits on the absolute value of rapidity and/or pseudo-rapidity, respectively, in the hadronic frame. Objects that do not fulfil these requirements are discarded in the respective particle group. For example, `define_eta lepton = 2.5` defines all leptons in the respective group with a maximal absolute pseudo-rapidity of 2.5.

The parameter `define_pT` $\{\text{particle_group}\}$ sets a threshold on the transverse momentum of particles in $\{\text{particle_group}\}$. Objects below that threshold are not discarded, but they do not increase the multiplicity counter of accepted particles in the respective $\{\text{particle_group}\}$. They enter the respective (p_T -ordered) particle groups at the very end of the group.

Setting only the above parameters does not result in selection cuts yet. To define requirements on the multiplicity counter of accepted particles of that $\{\text{particle_group}\}$, the parameters `n_observed_min` $\{\text{particle_group}\}$, and `n_observed_max` $\{\text{particle_group}\}$ are used: They define how many particles of that group must be observed at least and at most, respectively, in the final state for an event to be accepted. No cut is applied here if the minimum and maximum requirements do not impose an actual restriction.

These parameters are organized in blocks for each $\{\text{particle_group}\}$ in the file `parameter.dat` with the following general structure:

```
define_eta  $\{\text{particle\_group}\}$ 
define_y  $\{\text{particle\_group}\}$ 
```

Table 3 All relevant particle groups predefined in MATRIX. Each group is ordered by the transverse momenta of the respective particles, starting with the hardest one. These groups are most important to recognize by the user in two situations: when using the predefined blocks for fiducial cuts and when defining distributions (see Sect. 5.1.3). Furthermore, they can be accessed directly in the C++ code which is essential to the advanced user when defining user-specified scales, cuts and distributions, see Appendix B

Identifier	Description
<code>jet</code>	Parton-level jets, 5 light quarks+gluons, clustered according to jet algorithm
<code>ljet</code>	Light jets: same as <code>jet</code> , but without bottom jets
<code>bjjet</code>	Bottom jets: jets with a bottom charge (see main text)
<code>photon</code>	Photons, isolated according to chosen smooth-cone isolation
<code>lep</code>	Charged leptons, i.e. electrons and muons, including particles and anti-particles
<code>lm</code>	Negatively charged leptons, i.e. electrons and muons
<code>lp</code>	Positively charged leptons, i.e. positrons and anti-muons
<code>e</code>	Electrons and positrons
<code>em</code>	Electrons
<code>ep</code>	Positrons
<code>mu</code>	Muons and anti-muons
<code>mum</code>	Muons
<code>mup</code>	Anti-muons
<code>z</code>	Z bosons
<code>w</code>	W^+ and W^- bosons
<code>wp</code>	W^+ bosons
<code>wm</code>	W^- bosons
<code>h</code>	Higgs bosons
<code>nua</code>	Neutrinos and anti-neutrinos
<code>nu</code>	Neutrinos
<code>nux</code>	Anti-neutrinos
<code>nea</code>	Electron-neutrinos and anti-electron-neutrinos
<code>ne</code>	Electron-neutrinos
<code>nex</code>	Anti-electron-neutrinos
<code>nma</code>	Muon-neutrinos and anti-muon-neutrinos
<code>nm</code>	Muon-neutrinos
<code>nmx</code>	Anti-muon-neutrinos
<code>missing</code>	Sum of all neutrino momenta, containing only one entry (special group)

```
define_pT  $\{\text{particle\_group}\}$ 
n_observed_min  $\{\text{particle\_group}\}$ 
n_observed_max  $\{\text{particle\_group}\}$ 
```

Such blocks are predefined for the relevant particle groups of each process in the respective file `parameter.dat`. They should be sufficient for most practical purposes, and it is generally recommended to stick to the predefined blocks. Nevertheless, it is possible to add additional blocks also for the other particle groups using the structure above. In this case, care has to be taken to avoid unwanted behaviour. In

particular, requiring a certain number of particles which actually do not exist in the final state of a given process must

Lepton cuts

```
define_pT lep = 25.           # requirement on lepton transverse momentum (lower cut)
define_eta lep = 2.47        # requirement on lepton pseudo-rapidity (upper cut)
define_y lep = 1.e99         # requirement on lepton rapidity (upper cut)
n_observed_min lep = 2       # minimal number of observed leptons (with cuts above)
n_observed_max lep = 99     # maximal number of observed leptons (with cuts above)
```

be avoided. Below, we provide examples of the respective blocks available in various processes.

Jet cuts

```
define_pT jet = 30.          # requirement on jet transverse momentum (lower cut)
define_eta jet = 4.4        # requirement on jet pseudo-rapidity (upper cut)
define_y jet = 1.e99        # requirement on jet rapidity (upper cut)
n_observed_min jet = 0      # minimal number of observed jets (with cuts above)
n_observed_max jet = 99    # maximal number of observed jets (with cuts above)
```

This defines the particle group `jet` with a minimal transverse momentum of 30 GeV and a maximal absolute pseudo-rapidity of 4.4, using the jet-clustering algorithm specified above. No phase-space cut is effective, since this process has a maximum of two jets in the final state at NNLO, and neither a minimal (> 0) nor a maximal number (< 2) of observed jets is required.²¹ However, the particle group `jet` with the

This block defines each lepton in the particle group `lep` to have a minimal transverse momentum of 25 GeV and a maximal absolute pseudo-rapidity of 2.47. It further requires the

presence of at least two such leptons. All events not passing this criterion are discarded from the fiducial phase space.²³

Analogous blocks are available for other particle groups of charged leptons, namely `lm`, `lp`, `e`, `mu`, `em`, `ep`, `mum` and `mup`.

Photon cuts

```
define_pT photon = 15.      # requirement on photon transverse momentum (lower cut)
define_eta photon = 2.37    # requirement on photon pseudo-rapidity (upper cut)
define_y photon = 1.e99     # requirement on photon rapidity (upper cut)
n_observed_min photon = 1   # minimal number of observed photons (with cuts above)
n_observed_max photon = 99  # maximal number of observed photons (with cuts above)
```

requirements defined here can be accessed in the definition of distributions, see Sect. 5.1.3.²²

Analogous blocks can be processed by MATRIX for the particle groups `bjet` and `ljet`, which denote bottom jets and light jets (i.e. all jets, but the bottom jets), respectively. Note that a computation with bottom quarks treated as massless requires a jet involving a $b\bar{b}$ pair from a $g \rightarrow b\bar{b}$ splitting to be considered as a light jet, to guarantee observables to be IR safe. We thus define our b -jets by assigning bottom-charges to the partons: jets that contain a net bottom charge are considered bottom jets, whereas jets containing a $b\bar{b}$ pair are treated as light jets.

Similarly, due to this block the photons in the particle group `photon`, which have passed the isolation criterion defined above, have a transverse momentum greater than 15 GeV and absolute pseudo-rapidity smaller than 2.37, and the presence of at least one such isolated photon is required. Note that for the cross section to be IR finite, the number of identified photons in the final state must be equal to the total number of photons in the final state of a process.

²¹ Note that setting `n_observed_min jet = 1` would effectively reduce any (N)NLO calculation for the production of a final state F in MATRIX to be only a (N)LO accurate calculation for the production of $F+\text{jet}$. On the other hand, setting `n_observed_max jet = 0` would impose a veto against events that contain any jets that fulfil the defined requirements on jets.

²² Accordingly, the defined particle group is also accessible within the C++ code as discussed for the definition of new dynamic scales, cuts and observables for distributions by the advanced user in Appendix B.

²³ We stress again that any lepton in the particle group `lep` fulfils the defined (rapidity) requirements, irrespective of whether `n_observed_min lep` or `n_observed_max lep` require the presence of a minimal or maximal number of such leptons in the event. This is important to bear in mind when using `lep` to define distributions in Sect. 5.1.3. Even in a fully inclusive phase space without fiducial cuts, any distribution using `lep` will be affected by the defined (rapidity) requirements in the file `parameter.dat` on the leptons. Of course, the equivalent is true for any of the other particle groups.

Heavy-boson cuts

```
define_pT w = 0.           # requirement on W-boson transverse momentum (lower cut)
define_eta w = 1.e99      # requirement on W-boson pseudo-rapidity (upper cut)
define_y w = 1.e99       # requirement on W-boson rapidity (upper cut)
n_observed_min w = 0     # minimal number of observed W-bosons (with cuts above)
n_observed_max w = 99    # maximal number of observed W-bosons (with cuts above)
```

Equivalent blocks are available for the particle groups of heavy bosons, namely w , wm , wP , z and h . The above example does not impose any requirements on W bosons, as needed for a fully inclusive cross section.

Neutrino cuts

```
define_pT missing = 30.    # requirement on pT of sum of all neutrinos (lower cut)
```

The particle group `missing` contains only the missing energy vector, given by the sum of all neutrino momenta. In processes with neutrinos this particle group can be used to impose a minimum requirement on the total missing transverse momentum in the event. The example above sets $p_T^{\text{miss}} > 30 \text{ GeV}$.

In particular for technical checks it might be useful to access neutrinos also as individual particles. To do so, MATRIX can process blocks for the particle groups `nua`, `nu`, `nux`, `nea`, `nma`, `ne`, `nex`, `nm` and `nmx`.

Process-specific cuts

A number of cuts are defined individually for each process. They enable a realistic definition of fiducial phase

spaces as used in experimental measurements. For every process-specific cut there is usually one integer-valued switch (`user_switch`) to either turn on and off a certain cut or to choose between different options. Moreover, each switch typically comes with one or more real-valued parameters (`user_cut`) which are only active

if the respective switch is turned on. There are a number of predefined process-specific cuts for each process, all of which are defined directly inside the C++ code in the file `MATRIX_v1.0.0/prc/${process_id}/user/specify.cuts.cxx`; the list of predefined (process-specific) cuts for each process is documented in Sect. 5.2. A user interested in setting a specific cut which has not been implemented yet for a certain process is advised to contact the authors.²⁴

For $Z\gamma$ production, e.g., the following predefined cuts are accessible in the file `parameter.dat`.

```
user_switch M_leplep = 1   # switch to turn on (1) and off (0) cuts on lepton-lepton invariant mass
user_cut min_M_leplep = 40. # requirement on lepton-lepton invariant mass (lower cut)
user_cut max_M_leplep = 1.e99 # requirement on lepton-lepton invariant mass (upper cut)

user_switch M_lepgam = 0   # switch to turn on (1) and off (0) cuts on lepton-photon invariant mass
user_cut min_M_lepgam = 40. # requirement on lepton-photon invariant mass (lower cut)

user_switch R_leplep = 0   # switch to turn on (1) and off (0) cuts on lepton-lepton separation
user_cut min_R_leplep = 0.5 # requirement on lepton-photon separation in y-phi-plane (lower cut)

user_switch R_lepgam = 1   # switch to turn on (1) and off (0) cuts on lepton-photon separation
user_cut min_R_lepgam = 0.7 # requirement on lepton-photon separation in y-phi-plane (lower cut)

user_switch R_lepjet = 1   # switch to turn on (1) and off (0) cuts on lepton-jet separation
user_cut min_R_lepjet = 0.3 # requirement on lepton-jet separation in y-phi-plane (lower cut)

user_switch R_gamjet = 1   # switch to turn on (1) and off (0) cuts on photon-jet separation
user_cut min_R_gamjet = 0.3 # requirement on photon-jet separation in y-phi-plane (lower cut)

user_switch pT_lep_1st = 0 # switch to turn on (1) and off (0) cuts on pT of hardest lepton
user_cut min_pT_lep_1st = 25 # requirement on pT of hardest lepton (lower cut)
```

²⁴ A short description on how to add user-specified scales, cuts and distributions to the C++ code is given in Appendix B for the advanced user.

They should be rather self-explanatory and enable standard invariant-mass and $R = \sqrt{y^2 + \phi^2}$ -separation cuts on the final-state leptons, photons and jets, as well as a lower transverse-momentum cut on the hardest lepton.

5.1.1.5 MATRIX behaviour

```

max_time_per_job = 12      # very rough time (in hours) one main-run job shall take
switch_distribution = 1    # switch to turn on (1) and off (0) distributions
save_previous_result = 1  # switch to save previous result if rerun
save_previous_log = 0     # switch to save previous log if rerun
#include_pre_in_results = 0 # switch to include (0) main-run (1) main+pre-run in results
reduce_workload = 0      # switch to keep full output (0) or reduce the workload (1)
random_seed = 0          # specify integer value between 0-100 (grid-/pre-run reproducible)

```

`max_time_per_job` Essential (real-valued) parameter to control the parallelization of the jobs in the *main-run* (the *grid-run* and *pre-run* are unaffected, i.e. they will always run the same number of jobs). The given value sets a very rough requirement on the time (in hours) a single job in the *main-run* may take. It should be regarded as a tuning parameter rather than an exact measure; the actual runtime of the jobs may deviate significantly (factor of $\sim [0.5, 2]$) in certain cases. Together with the precision that can be set individually for each order (see Sect. 5.1.1.2) `max_time_per_job` determines the level of parallelization; clearly, the higher the precision (with constant `max_time_per_job`), the higher the level of parallelization. One must bear in mind that too small values of `max_time_per_job` (below ~ 1 h for a NNLO run) become unreliable, i.e. the jobs would take significantly longer than specified in that case. For heavy NNLO runs ($\lesssim 0.1\%$ precision for one of the most complicated processes) we recommend not to use values $\lesssim 5$ h, as too small values lead to a huge parallelization which may have a negative effect on the result combination. Also note that this parameter becomes ineffective as soon as the number of jobs is larger than `max_nr_parallel_jobs`, which can be set in the file `MATRIX_configuration` (see Sect. 4.5), or the number of cores in local mode.

`switch_distribution` Switch to control whether distributions are generated during the run.

`save_previous_result` This switch is effective when rerunning in a run folder which already contained a full run including results. If the switch is turned on, the previous results are saved into a subfolder `saved_result_XX` of the result folder for the respective run, where `XX` is an increasing number starting at 01 for each time an old result is saved; default: turned on.

`save_previous_log` This switch is effective when rerunning in a run folder which already contained a run

with written log files. If the switch is turned on, the previous log files are saved into a subfolder `saved_log_XX` of the log folder for the respective run, where `XX` is an increasing number starting at 01 for each time old log files are saved; default: turned off.

`include_pre_in_results` This switch affects the result combination. It allows the user to include/exclude the results of the *pre-run* into/from the *result-collection*, which always includes the *main-run*. If the switch is absent, i.e. commented (default), this decision is made internally in the MATRIX code independently for each contribution by a certain algorithm which is designed to optimize the total precision, while excluding irrelevant low-statistic runs of the *pre-run* phase. Excluding the *pre-run* from the *result-collection* is particularly useful if the *main-run* is restarted with a slightly modified setup, in order to avoid mixing of the two setups.

`reduce_workload` Switch to reduce the output of the jobs to a minimum. May be used to improve the speed on clusters with slow access to the file system.

`random_seed` Sets starting seed for run. *grid-* and *pre-run* for same seed are reproducible.

5.1.2 Settings in `model.dat`

All model-related parameters are set in the file `model.dat`. We adopt the SUSY Les Houches accord (SLHA) format [104]. This standard format is used in many codes and thus simplifies the settings of common model parameters. In the SLHA format inputs are organized in blocks which have different entries characterized by a number. For simplicity, we introduce the following short-hand notation: `Block example[i]` corresponds to entry `i` in `Block example`. For example, entry 25 of `Block mass` (`Block mass[25]`) in the SLHA format corresponds to the Higgs mass in the SM, which is required as an input in the file `model.dat`. Only the format for decay widths is slightly different and not organized in a `Block`, but defined by the keyword `DECAY`, followed by a number which specifies the respective particle. A typical model file is shown below.

```
#####
# MATRIX model parameter #
#####

#-----\
# masses |
#-----/
Block MASS
1 0.000000 # M_d
2 0.000000 # M_u
3 0.000000 # M_s
4 0.000000 # M_c
5 0.000000 # M_b
6 1.732000e+02 # M_t
11 0.000000 # M_e
12 0.000000 # M_νe
13 0.000000 # M_μ
14 0.000000 # M_νμ
15 1.777000e+00 # M_τ
16 0.000000 # M_ντ
23 9.118760e+01 # M_Z
24 8.038500e+01 # M_W
25 1.250000e+02 # M_H

#-----\
# inputs for the SM #
#-----/
Block SMINPUTS
2 1.166390e-05 # G_F

#-----\
# Yukawa couplings |
#-----/
#Block YUKAWA
# 5 4.750000e+00 # M_ΥB
# 6 1.730000e+02 # M_ΥT
# 15 1.777000e+00 # M_ΥTAU

#-----\
# decays widths |
#-----/
DECAY 6 1.442620e+00 # WT
DECAY 23 2.495200e+00 # WZ
DECAY 24 2.085400e+00 # WW
DECAY 25 4.070000e-03 # WH
```

The Block Yukawa is currently not used, which is why it is commented.

In the first release of MATRIX, only on- and off-shell W -boson production allow for a non-trivial CKM matrix. This feature will be added also for other processes like $W\gamma$ and $W^\pm Z$ production in a future update. The CKM parameters are controlled in the file `model.dat` of these processes through additional Blocks. The user may choose between three different setups. The default is a complete CKM matrix, where each of the entries may be set individually using Block CKM as defined below.

```
#-----\
# CKM matrix |
#-----/
Block CKM
11 0.974170e+00 # V_ud
12 0.224800e+00 # V_us
13 0.004090e+00 # V_ub
21 0.220000e+00 # V_cd
22 0.995000e+00 # V_cs
23 0.040500e+00 # V_cb
31 0.008200e+00 # V_td
32 0.040000e+00 # V_ts
33 1.009000e+00 # V_tb
```

The default values are chosen according to the SM CKM matrix as reported by the PDG in Ref. [105]. Note that any

top-related CKM entry has no effect on the processes considered in MATRIX.

A second option to use a non-trivial CKM matrix is through the Cabibbo angle θ_c , by adding the Block VCKMIN as follows:

```
#-----\
# Cabibbo angle |
#-----/
Block VCKMIN
1 0.227000e+00 # Cabibbo angle
```

This enables mixing only between the first two generations, while turning off any mixing with the third generation, i.e. by setting internally $V_{ud} = \cos(\theta_c)$, $V_{us} = \sin(\theta_c)$, $V_{cd} = -\sin(\theta_c)$, $V_{cs} = \cos(\theta_c)$, $V_{tb} = 1$, and $V_{ub} = V_{cb} = V_{td} = V_{ts} = 0$. Note that only Block CKM or Block VCKMIN may be present in the file `model.dat` at the same time.

Finally, if both blocks are absent, a trivial CKM matrix (no mixing) is used.

5.1.3 Settings in `distribution.dat`

5.1.3.1 General structure

In the file `distribution.dat` the user can define histograms for distributions which are filled during the run. Each distribution is represented by one block containing the following parameters:

`distributionname` Unique user-defined label (string) of the distribution for identification at the end of the run; every `distributionname` starts a new block. Code will stop if the same distribution identifier is used twice.

`distributiontype` Type identifier (string) of the observable to be binned. MATRIX has a number of predefined observables, which are summarized in Table 4. A user interested in a specific distribution which has not been implemented yet is advised to contact the authors.²⁵

`particle j` Specification of particles entering the definition of the observable to be binned. Several final-states particles may be grouped into one `particle`. The general form is as follows:

```
particle 1 = ${particle_group_1} ${position_in_pT_ordering_1}
particle 1 = ${particle_group_2} ${position_in_pT_ordering_2}
particle 1 = ${particle_group_3} ${position_in_pT_ordering_3}
...
particle 2 = ${particle_group_4} ${position_in_pT_ordering_4}
particle 2 = ${particle_group_5} ${position_in_pT_ordering_5}
particle 2 = ${particle_group_6} ${position_in_pT_ordering_6}
...
particle 3 = ${particle_group_7} ${position_in_pT_ordering_7}
particle 3 = ${particle_group_8} ${position_in_pT_ordering_8}
particle 3 = ${particle_group_9} ${position_in_pT_ordering_9}
...
```

²⁵ A short description on how to add user-specified scales, cuts and distributions to the C++ code is given in Appendix B for the advanced user.

Each $\{\text{particle_group_i}\}$ is given by one of the particle groups defined in Table 3, and $\{\text{position_in_pT_ordering_i}\}$ is an integer which determines the desired position in the p_T -ordering of the respective group. For instance, lep 2 corresponds to the second-hardest lepton in the final state. If particle j has several entries, the respective 4-momenta are summed to define the momentum of particle j .²⁶ How many particles ($j = 1, 2, 3, \dots$) are allowed or required depends on the observable under consideration. Many observables use only one particle entry, i.e. only particle 1, others that determine the distance or angle between two particles require two particles, i.e. particle 1 and particle 2. Table 4 specifies this behaviour for each of the predefined observables.

binning_type Defines how the binning is performed. It may be set to linear, logarithmic or irregular (if not specified, linear is used as default):

- The setting **linear** requires the definition of three inputs out of **startpoint**, **endpoint**, **binnumber** and **binwidth**. The fourth one is uniquely defined then. Defining all four parameters results in a stop of the C++ code if they are inconsistent.
- The setting **logarithmic** requires the definition of **startpoint**, **endpoint** and **binnumber**. The widths of the resulting bins are determined equidistantly on a logarithmic scale from this input.
- The setting **irregular** facilitates the definition of an arbitrary (not necessarily equidistant) binning, which is specified by the input parameter **edges**.

startpoint Left endpoint of the first bin (real number).

endpoint Right endpoint of the last bin (real number).

binnumber Number of bins in the histogram (integer).

binwidth Width of each bin in the histogram (real number).

edges Edges (real numbers) of an irregular histogram, specified by $a_0 : a_1 : \dots : a_n$ for n bins.

5.1.3.2 Examples

We give a few examples on how proper distributions may be defined for the sample process of $Z\gamma$ production (examples

²⁶ This provides a simple way to access distributions of combined particles, such as a Z boson determined by its two decay leptons. We note that combined (reconstructed) particles are defined for certain processes (see, e.g., Sect. 5.2.4.4) as additional particle groups via user-defined particles. This is particularly useful if the definition of such particle requires a certain pairing prescription, e.g. the reconstruction of a Z boson in a same-flavour channel with more than two leptons. An advanced user may use this concept to define his own particle groups, see Appendix B.2.

can be found also in the file `distribution.dat` of each process).

- Transverse momentum of the hardest lepton, regularly binned in 200 bins from 0 – 1000 GeV (i.e. in 5 GeV steps):

```
distributionname = pT_lep1
distributiontype = pT
particle 1       = lep 1
startpoint      = 0.
endpoint        = 1000.
binnumber       = 200
```

- Transverse momentum of the second-hardest lepton, regularly binned from 0 – 1000 GeV in 5 GeV steps (i.e. in 200 bins):

```
distributionname = pT_lep2
distributiontype = pT
particle 1       = lep 2
startpoint      = 0.
endpoint        = 1000.
binwidth        = 5.
```

- Transverse momentum of the hardest photon with irregular edges (as used by ATLAS in the 7 TeV analysis for $Z\gamma$ [106]):

```
distributionname = pT_gamma_ATLAS
distributiontype = pT
particle 1       = photon 1
binningtype     = irregular
edges           = 0.:15.:20.:30.:40.:60.:100.:1000.:3500.
```

- Invariant mass of the pair formed by the hardest and the second-hardest lepton, binned from 0 – 1000 GeV in 10 GeV steps:

```
distributionname = m_lep1_lep2
distributiontype = m
particle 1       = lep 1
particle 2       = lep 2
startpoint      = 0.
endpoint        = 1000.
binwidth        = 10.
```

- Distance in y - ϕ plane between the hardest electron and the hardest positron, binned from 0 – 10 in 0.1 steps:

```
distributionname = dR_em1_ep1
distributiontype = dR
particle 1       = em 1
particle 2       = ep 1
startpoint      = 0.
endpoint        = 10.
binwidth        = 0.1
```

The default file `distribution.dat` contains further examples and information, as well as instructions on how to define distributions in this format.

5.2 Process-specific settings

In this section we provide information specific to the individual processes. Below we list all processes available in MATRIX by their respective $\{\text{process_id}\}$, summarize

Table 4 Predefined distributions available in MATRIX. These distributions can be used in a distribution block of the file `distribution.dat` and require to specify the parameter(s) particle j , $j = 1, \dots, m$ ($m \geq 1$). Some observables behave differently for a different number of defined particles m : In these cases

the respective options are given in separate rows. We use the shorthand notation p^j for the momentum of particle j . Note that, if particle j has several entries of particles, p^j is the sum of their momenta, which provides a straightforward way to access trivially reconstructed particles (e.g. a single Z boson from its decay leptons)

Identifier	Binned variable	Description
pT	$\sum_{j=1}^m p_T^j$	Scalar sum of transverse momenta of particle 1 to particle m
m	$m(p^1)$	Invariant mass of particle 1
dm	$m(p^1) - m(p^2)$	Invariant-mass difference between particle 1 and particle 2
absdm	$ m(p^1) - m(p^2) $	Absolute invariant-mass difference between particle 1 and particle 2
mmin	$\min(m(p^1), m(p^2))$	Minimal invariant-mass of particle 1 and particle 2
mmax	$\max(m(p^1), m(p^2))$	Maximal invariant-mass of particle 1 and particle 2
y	$y(p^1)$	Rapidity of particle 1
absy	$ y(p^1) $	Absolute rapidity of particle 1
dy	$y(p^1) - y(p^2)$	Rapidity difference between particle 1 and particle 2
absdy	$ y(p^1) - y(p^2) $	Absolute rapidity difference between particle 1 and particle 2
dabsy	$ y(p^1) - y(p^2) $	Difference between absolute rapidities of particle 1 and particle 2
absdabsy	$ y(p^1) - y(p^2) $	Absolute difference between absolute rapidities of particle 1 and particle 2
eta	$\eta(p^1)$	Pseudo-rapidity of particle 1
abseta	$ \eta(p^1) $	Absolute pseudo-rapidity of particle 1
deta	$\eta(p^1) - \eta(p^2)$	Pseudo-rapidity difference between particle 1 and particle 2
absdeta	$ \eta(p^1) - \eta(p^2) $	Absolute pseudo-rapidity difference between particle 1 and particle 2
dabseta	$ \eta(p^1) - \eta(p^2) $	Difference between absolute pseudo-rapidities of particle 1 and particle 2
absdabseta	$ \eta(p^1) - \eta(p^2) $	Absolute difference between absolute pseudo-rapidities of particle 1 and particle 2
phi	$\phi(p^1)$	Azimuthal angle of particle 1
phi	$\Delta\phi(p^1, p^2)$	Difference in azimuthal angle between particle 1 and particle 2
dR	$\sqrt{[\Delta y(p^1, p^2)]^2 + [\Delta\phi(p^1, p^2)]^2}$	Distance in y - ϕ -plane between particle 1 and particle 2
dReta	$\sqrt{[\Delta\eta(p^1, p^2)]^2 + [\Delta\phi(p^1, p^2)]^2}$	Distance in η - ϕ -plane between particle 1 and particle 2
ET	$\sum_{j=1}^m E_T(p^j) \equiv \sum_{j=1}^m \sqrt{[m(p^j)]^2 + [p_T^j]^2}$	Scalar sum of transverse masses of particle 1 to particle m
mT	$E_T(p^1)$	Transverse mass of particle 1
mT	$\sqrt{[\sum_{j=1}^m E_T(p^j)]^2 - [p_T(\sum_{j=1}^m p^j)]^2}$	Transverse mass, defined with all neutrinos in particle 1 and all other particles in particle 2 to particle m
pTveto	$\sigma(p_T^1 < p_{T,\text{veto}})$	Cumulative cross section with a veto on p_T of particle 1 as a function of $p_{T,\text{veto}}$
multiplicity	N	Distribution in number of identified objects of type particle 1
muR	μ_R	Distribution in renormalization scale (no particle j definition)
muF	μ_F	Distribution in factorization scale (no particle j definition)

the predefined process-specific cuts and dynamic scales, and, where applicable, we give additional process-specific information.

In addition to the standard cuts on particle groups, discussed in Sect. 5.1.1.4, process-specific fiducial cuts are predefined via an integer-valued parameter `user_switch` in

combination with none, one or more real-valued parameters `user_cut`. For a `user_switch XXX` together with corresponding `user_cut XXX_A`, `user_cut XXX_B`, and so forth, we adopt the notation

XXX: XXX_A,
 XXX_B,
 ...

to list all available predefined cuts in the respective file `parameter.dat` of each process. A detailed explanation for each of these cuts is given in Appendix A.²⁷

As outlined in Sect. 5.1.1.2, dynamic scales are set by the switch `dynamic_scale` in the file `parameter.dat`, and there are two default scales for all processes: the invariant and the transverse mass of the colourless system. Any additional predefined scale implemented for a process is stated below, and the adopted nomenclature is summarized in Table 5.

We note that all leptons are considered massless throughout all computations. This implies that, e.g., electrons may be considered as muons and vice versa in order to get results for other lepton flavours. Thus, a process like $pp/p\bar{p} \rightarrow e^-e^+$ is fully equivalent to $pp/p\bar{p} \rightarrow \mu^-\mu^+$, and only the former is provided in MATRIX. The same holds for more involved processes such as $pp/p\bar{p} \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$ and $pp/p\bar{p} \rightarrow \mu^-e^-\mu^+\bar{\nu}_e$ if the cuts do not depend on the lepton flavour. Since we provide only the $pp/p\bar{p} \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$ channel, $pp/p\bar{p} \rightarrow \mu^-e^-\mu^+\bar{\nu}_e$ for different muon and electron cuts can be simply computed by using $pp/p\bar{p} \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$ with muon cuts implemented for electrons and vice versa.

An alternative which will be supported in a future release is an exchange of electrons and muons by means of the parameter `process_class`. For every process where this is relevant, a separate file `parameter.dat` will be provided inside its folder `input`, which can be used instead of the original file `parameter.dat` of the process to run with exchanged electrons and muons. For example, for different-flavour $W^\pm Z$ production (`{process_id} = ppemexnmx04`) an additional file with `process_class = ppemexnmx04` instead of `process_class = ppemexnmx04` will be used to calculate the process $pp/p\bar{p} \rightarrow \mu^-e^-\mu^+\bar{\nu}_e$ instead of $pp/p\bar{p} \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$, and all scales, cuts, distributions, etc. are to be formulated directly for the actual particles of this new process.

All processes available in MATRIX are discussed in the following, grouped into Higgs boson production (Sect. 5.2.1), vector-boson production (Sect. 5.2.2), diphoton and vector-boson plus photon production (Sect. 5.2.3), and vector-boson pair production (Sect. 5.2.4). The process-specific cuts are explained in detail in Appendix A.

Table 5 Symbols used in the definition of dynamic scales throughout this section. The transverse mass of a particle, or a sum of particle momenta, X is defined as $m_{T,X} = \sqrt{m_X^2 + p_{T,X}^2}$, with $p_{T,X}$ and m_X^2 being its transverse momentum and invariant mass, respectively

m_Z :	Mass of the Z boson
m_W :	Mass of the W boson
p_{T,e^-e^+} :	Transverse momentum of the reconstructed Z boson (electron pair)
$p_{T,\mu^-\mu^+}$:	Transverse momentum of the reconstructed Z boson (muon pair)
$p_{T,\nu_\mu\bar{\nu}_\mu}$:	Transverse momentum of the reconstructed Z boson (neutrino pair)
$p_{T,Z_{rec}}$:	Transverse momentum of the reconstructed Z boson (see main text)
$p_{T,Z_{i,rec}}$:	Transverse momentum of the respective reconstructed Z boson (see main text)
$p_{T,e^\pm\nu_e}$:	Transverse momentum of the reconstructed W boson (electron–neutrino pair)
$p_{T,\mu^\pm\nu_\mu}$:	Transverse momentum of the reconstructed W boson (muon–neutrino pair)
p_{T,W_{rec}^\pm} :	Transverse momentum of the reconstructed W boson (see main text)
m_{T,e^-e^+} :	Transverse mass of the reconstructed Z boson (electron pair)
$m_{T,\mu^-\mu^+}$:	Transverse mass of the reconstructed Z boson (muon pair)
$m_{T,\nu_e\bar{\nu}_e}$:	Transverse mass of the reconstructed Z boson (neutrino pair)
$m_{Z_{rec}}$:	Transverse mass of the reconstructed Z boson (see main text)
$m_{T,Z_{i,rec}}$:	Transverse mass of the respective reconstructed Z boson (see main text)
$m_{T,e^\pm\nu_e}$:	Transverse mass of the reconstructed W boson (electron–neutrino pair)
$m_{T,\mu^\pm\nu_\mu}$:	Transverse mass of the reconstructed W boson (muon–neutrino pair)
m_{T,W_{rec}^\pm} :	Transverse mass of the reconstructed W boson (see main text)
$m_{T,\gamma}(p_{T,\gamma})$:	Transverse mass (momentum) of the photon

5.2.1 Higgs boson production

5.2.1.1 $pp\bar{p}\bar{p} \rightarrow H$

On-shell Higgs boson production has no process-specific cuts or dynamic scales. The process is computed in the infinite-top-mass approximation by using an effective field theory where the top quark is integrated out.

5.2.2 Vector-boson production

This group contains both the on-shell and the off-shell production of a single vector boson. Whereas the former processes feature cuts and distributions only with respect to the

²⁷ The links embedded in the arXiv version of this paper for each cut in this section can be used to jump to the corresponding explanation in Appendix A, if supported by the PDF viewer in use.

on-shell final state, the off-shell processes give access to, in principle, arbitrary phase-space selection cuts and distributions of the leptons. The phenomenologically irrelevant process of $pp/p\bar{p} \rightarrow \nu_e \bar{\nu}_e$ production has been added as it might be useful for technical checks.

5.2.2.1 $ppz01$ ($pp/p\bar{p} \rightarrow Z$)

On-shell Z-boson production has no process-specific cuts or dynamic scales.

5.2.2.2 $ppw01$ ($pp/p\bar{p} \rightarrow W^-$), $ppwx01$ ($pp/p\bar{p} \rightarrow W^+$)

On-shell W^\pm -boson production has no process-specific cuts or dynamic scales. The process includes a non-trivial CKM matrix, which the user may modify, see Sect. 5.1.2.

5.2.2.3 $ppeex02$ ($pp/p\bar{p} \rightarrow e^-e^+$)

Off-shell Z-boson production²⁸ with decay to leptons includes the following predefined cuts:

```
M_leplep: min_M_leplep,
           max_M_leplep
R_leplep: min_R_leplep
lepton_cuts: min_pT_lep_1st,
             min_pT_lep_2nd
```

No process-specific dynamic scales are implemented.

If cuts are applied, this process may feature a peculiarly strong dependence on the value of r_{cut} in the q_T -subtraction procedure, see Sect. 7. The $pp/p\bar{p} \rightarrow e^-e^+$ process therefore features a switch `switch_qT_accuracy` in the file `parameter.dat`, which allows the user to decrease the uncertainty induced by the q_T -subtraction procedure at NNLO, at the cost of a slower numerical convergence:

```
switch_qT_accuracy = 0 Uses the default value
r_cut = 0.15% with fast numerical convergence.
switch_qT_accuracy = 1 Uses r_cut = 0.05% with
reduced uncertainty, but longer runtime.
```

We recommend to use `switch_qT_accuracy = 0` if the targeted precision of the extrapolated cross-section prediction ($r_{\text{cut}} \rightarrow 0$) is of the order of 0.5% – 1%. To achieve results with numerical precision of 0.1% – 0.5%, `switch_qT_accuracy = 1` should be used.

5.2.2.4 $ppnenex02$ ($pp/p\bar{p} \rightarrow \nu_e \bar{\nu}_e$)

Off-shell Z-boson production with decay to neutrinos has no process-specific cuts or dynamic scales.

5.2.2.5 $ppenex02$ ($pp/p\bar{p} \rightarrow e^- \bar{\nu}_e$), $ppexne02$ ($pp/p\bar{p} \rightarrow e^+ \nu_e$)

Off-shell W^\pm -boson production has no process-specific cuts or dynamic scales. The process includes a non-trivial CKM matrix, which the user may modify, see Sect. 5.1.2.

5.2.3 Diphoton and vector-boson plus photon production

This group contains both the diphoton process and the $V\gamma$ processes with off-shell leptonic decays of the heavy vector bosons V .

All processes with isolated photons in the final state have a peculiarly strong dependence on the value of r_{cut} in the q_T -subtraction procedure, see Sect. 7. For this reason the estimated uncertainty induced by finite r_{cut} values is particularly large in these processes. The photon processes therefore feature a switch `switch_qT_accuracy` in the file `parameter.dat`, which allows the user to decrease the uncertainty induced by the q_T -subtraction procedure at NNLO, at the cost of a slower numerical convergence:

```
switch_qT_accuracy = 0 Uses the default value
r_cut = 0.15% with fast numerical convergence.
switch_qT_accuracy = 1 Uses r_cut = 0.05% with
reduced uncertainty, but longer runtime.
```

We recommend to use `switch_qT_accuracy = 0` if the targeted precision of the extrapolated cross-section prediction ($r_{\text{cut}} \rightarrow 0$) is of the order of 0.5% – 1%. To achieve results with numerical precision of 0.1% – 0.5%, `switch_qT_accuracy = 1` should be used.

5.2.3.1 $ppaa02$ ($pp/p\bar{p} \rightarrow \gamma\gamma$)

Diphoton production includes the following predefined cuts:

```
M_gamgam: min_M_gamgam,
           max_M_gamgam
pT_gam_1st: min_pT_gam_1st
gap_eta_gam: gap_min_eta_gam,
             gap_max_eta_gam
R_gamgam: min_R_gamgam
```

No process-specific dynamic scales are implemented.

5.2.3.2 $ppeexa03$ ($pp/p\bar{p} \rightarrow e^-e^+\gamma$)

$Z\gamma$ production [30,31] with Z-boson decay to charged leptons²⁹ includes the following predefined cuts:

²⁸ Note that this process includes also off-shell photon contributions.

²⁹ Note that this process includes also $\gamma^*\gamma$ contributions, where one photon is off-shell and decays to leptons, and Z/γ^* production with a subsequent decay $Z/\gamma^* \rightarrow e^-e^+\gamma$.

M_leplep: min_M_leplep
 M_lepgam: min_M_lepgam
 R_leplep: min_R_leplep
 R_lepgam: min_R_lepgam
 R_lepjet: min_R_lepjet
 R_gamjet: min_R_gamjet
 pT_lep_1st: min_pT_lep_1st

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

dynamic_scale = 3:	$\mu = m_{T,\gamma} \equiv p_{T,\gamma}$
dynamic_scale = 4:	$\mu = m_{T,e^-e^+}$
dynamic_scale = 5:	$\mu = \sqrt{m_{T,\gamma} \cdot m_{T,e^-e^+}}$
dynamic_scale = 6:	$\mu = \sqrt{m_Z^2 + m_{T,\gamma}^2}$

5.2.3.3 ppnenexa03 ($pp/p\bar{p} \rightarrow \nu_e \bar{\nu}_e \gamma$)

Z γ production [31] with Z-boson decay to neutrinos includes the following predefined cuts:

R_gamjet: min_R_gamjet

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

dynamic_scale = 3:	$\mu = m_{T,\gamma} \equiv p_{T,\gamma}$
dynamic_scale = 4:	$\mu = m_{T,\nu_e \bar{\nu}_e}$
dynamic_scale = 5:	$\mu = \sqrt{m_{T,\gamma} \cdot m_{T,\nu_e \bar{\nu}_e}}$
dynamic_scale = 6:	$\mu = \sqrt{m_Z^2 + m_{T,\gamma}^2}$

5.2.3.4 ppenexa03 ($pp/p\bar{p} \rightarrow e^- \bar{\nu}_e \gamma$), ppexnea03 ($pp/p\bar{p} \rightarrow e^+ \nu_e \gamma$)

$W^\pm \gamma$ production [31] with leptonic W-boson decay³⁰ includes the following predefined cuts:

R_lepgam: min_R_lepgam
 R_lepjet: min_R_lepjet
 R_gamjet: min_R_gamjet
 mT_CMS: min_mT_CMS
 gap_eta_gam: gap_min_eta_gam,
 gap_max_eta_gam

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

³⁰ Note that this process includes also contributions from W^\pm production with a subsequent decay $W^+ \rightarrow e^+ \nu_e \gamma$ or $W^- \rightarrow e^- \bar{\nu}_e \gamma$, respectively.

dynamic_scale = 3:	$\mu = m_{T,\gamma} \equiv p_{T,\gamma}$
dynamic_scale = 4:	$\mu = m_{T,e^\pm \nu_e}$
dynamic_scale = 5:	$\mu = \sqrt{m_{T,\gamma} \cdot m_{T,e^\pm \nu_e}}$
dynamic_scale = 6:	$\mu = \sqrt{m_W^2 + m_{T,\gamma}^2}$

5.2.4 Vector-boson pair production

This group contains both the on-shell and the off-shell production of a vector-boson pair. The on-shell production of a $W^+ W^-$ or a ZZ pair allows selection cuts to be applied only on the vector bosons, and distributions in the vector-boson kinematics can be studied. The off-shell processes, on the other hand, give access to the full leptonic final states, i.e. they allow in principle arbitrary IR safe selection cuts on the leptons to be applied, and distributions in the kinematics of these leptons can be computed. Off-shell vector-boson pair production includes processes with different-flavour (DF) and same-flavour (SF) leptons in the final state. For the processes with two neutrinos and two leptons in the final state, the separation of DF ($e^- e^+ \nu_\mu \bar{\nu}_\mu$) and SF ($e^- e^+ \nu_e \bar{\nu}_e$) channels is done according to the underlying calculation, not to the experimental signature: For any analysis of two leptons plus missing transverse energy the predictions must be obtained by (incoherently) combining the DF and SF processes, i.e.

$$\begin{aligned} \sigma(e^- e^+ + p_{T,\text{miss}}) &= \sigma(e^- e^+ \nu_e \bar{\nu}_e) + \sigma(e^- e^+ \nu_\mu \bar{\nu}_\mu) \\ &\quad + \sigma(e^- e^+ \nu_\tau \bar{\nu}_\tau) \\ &= \sigma(e^- e^+ \nu_e \bar{\nu}_e) + 2 \times \sigma(e^- e^+ \nu_\mu \bar{\nu}_\mu). \end{aligned} \tag{5}$$

Flavour-scheme choice and top-quark contamination in WW production

All processes including a pair of on- or off-shell W bosons are subject to a contamination by off-shell top-quark contributions with $t \rightarrow Wb$ decays. Such contributions enter radiative corrections in both the four-flavour scheme (4FS), where bottom quarks are treated as massive, and the five-flavour scheme (5FS), where the bottom-quark mass is set to zero as all other light-quark masses. In case of $W^+ W^-$ production, the 4FS has the advantage that the bottom quark appears only in the final state, and that the bottom-quark mass renders all partonic subprocesses with bottom quarks in the final state separately finite. Thus, the top-quark contamination is easily avoided by omitting bottom-quark emission subprocesses in this scheme, which are considered part of the (off-shell) top-pair background. Consequently, we use this 4FS approach as the default for any process that features an on- or off-shell $W^+ W^-$ pair, namely by setting `flavour_scheme = 0` in the file `parameter.dat` in combination with $m_b \neq 0$ in the file `model.dat`. We note

that this approach requires the use of consistent PDF sets with $n_f = 4$ light parton flavours.

Alternatively, one can use the 5FS by setting `flavour_scheme = 1`, $m_b = 0$ and choosing $n_f = 5$ PDF sets. In this case, however, the top-quark contamination is not removed from the results. A numerical procedure to achieve a definition of the W^+W^- cross section without top-quark contamination in the 5FS, which has been used in Refs. [36,37], requires the repeated computation of the cross section for varying top-quark widths in order to approach the limit $\Gamma_t \rightarrow 0$ and thereby to isolate the contributions from single-top and top-pair production. As it has been shown in these references, the resulting top-subtracted W^+W^- cross sections calculated in the 4FS and the 5FS prescription, respectively, agree within 1–2%, both at the inclusive level and with different sets of fiducial cuts applied. This justifies the use of the simpler 4FS computation for such processes.

Off-shell Z bosons in ZZ production

For off-shell ZZ-production processes the cuts may be arranged in a way that at least one of the Z bosons is forced to be far in the off-shell region. For such cases these processes include an additional switch `switch_off_shell` in the file `parameter.dat` to improve the convergence of the computation in this phase-space region. This is relevant, e.g., when studying the ZZ background in Higgs boson measurements. The default choice `switch_off_shell = 0` uses the standard setup for the grid generation (*grid-run*, see Sect. 4.4.1), which is suitable if both Z bosons can simultaneously become resonant. Using `switch_off_shell = 1` adapts the settings of the *grid-run* for cases where at least one Z boson is off-shell.

5.2.4.1 ppzz02 ($pp/p\bar{p} \rightarrow ZZ$)

On-shell ZZ production [33] has no process-specific cuts or dynamic scales.

5.2.4.2 ppwxw02 ($pp/p\bar{p} \rightarrow W^+W^-$)

On-shell W^+W^- production [36,37] has no process-specific cuts or dynamic scales.

By default (`flavour_scheme = 0`) this process is computed in the 4FS, dropping all diagrams with final-state bottom quarks to remove the top-quark contamination. The 5FS can be chosen by setting `flavour_scheme = 1`, where, however, the top-quark contamination is not removed from the results, since the recommended procedure is much more involved and requires several runs for the 5FS, see introduction of Sect. 5.2.4 for further details.

5.2.4.3 ppemexmx04 ($pp/p\bar{p} \rightarrow e^- \mu^- e^+ \mu^+$)

Off-shell ZZ production [34] with Z-boson decays to DF leptons³¹ includes the following predefined cuts:

```
M_leplep_OSSF: min_M_leplep_OSSF,
                max_M_leplep_OSSF,
                min_M_Z1_OSSF,
                max_M_Z1_OSSF
R_leplep: min_R_leplep
pT_lep_1st: min_pT_lep_1st
pT_lep_2nd: min_pT_lep_2nd
M_4lep: min_delta_M_4lep,
        max_delta_M_4lep,
        min_M_4lep,
        max_M_4lep
lep_iso: lep_iso_delta_0,
        lep_iso_epsilon
```

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

$$\text{dynamic_scale} = 3: \mu = \sqrt{m_{T,e^-e^+} \cdot m_{T,\mu^-\mu^+}}$$

$$\text{dynamic_scale} = 4: \mu = \sqrt{m_Z^2 + p_{T,e^-e^+}^2 + \sqrt{m_Z^2 + p_{T,\mu^-\mu^+}^2}}$$

This process provides an additional switch `switch_off_shell` to speed up the grid-generation phase when considering at least one of the Z bosons to be far off-shell; it should not be used otherwise, see introduction of Sect. 5.2.4 for further details.

5.2.4.4 ppeeexex04 ($pp/p\bar{p} \rightarrow e^- e^- e^+ e^+$)

Off-shell ZZ production [34] with Z-boson decays to SF leptons³² includes the following predefined cuts:

```
lepton_identification
M_Zrec: min_M_Zrec,
        max_M_Zrec
M_leplep_OSSF: min_M_leplep_OSSF
R_leplep: min_R_leplep
pT_lep_1st: min_pT_lep_1st
pT_lep_2nd: min_pT_lep_2nd
M_4lep: min_delta_M_4lep,
        max_delta_M_4lep,
        min_M_4lep,
        max_M_4lep
lep_iso: lep_iso_delta_0,
        lep_iso_epsilon
```

³¹ Note that this process includes also $Z\gamma^*$ and $\gamma^*\gamma^*$ contributions with off-shell photons decaying to leptons, as well as Z/γ^* production with a subsequent decay $Z/\gamma^* \rightarrow e^- \mu^- e^+ \mu^+$.

³² Note that this process includes also $Z\gamma^*$ and $\gamma^*\gamma^*$ contributions with off-shell photons decaying to leptons, as well as Z/γ^* production with a subsequent decay $Z/\gamma^* \rightarrow e^- e^- e^+ e^+$.

Since this process features four SF leptons, two of which are positively and two negatively charged, the leptons cannot be unambiguously associated with the two parent Z bosons as in the DF case. However, the experimental analyses often rely on cuts specific to (reconstructed) Z bosons. Hence, in the SF channel an identification procedure is required to assign one opposite-charge same-flavour (OSSF) lepton pair to each of the Z bosons. The parameter `lepton_identification` switches between such identification procedures of the Z bosons as used by ATLAS and CMS. In both cases seven new particle groups are defined (see Sect. 5.1.1.4 and the related Table 3 for the standard particle groups), which makes them available in the definition of cuts, scales and distributions: Particle group `Z1rec` contains the Z boson reconstructed from the OSSF lepton pair with its invariant mass closer to the Z -boson mass, labelled as $Z_{1,rec}$, and particle group `Z2rec` contains the remaining OSSF lepton pair, labelled as $Z_{2,rec}$. Particle group `Zrec` is filled with both reconstructed Z bosons in the standard p_T -ordering. The particle groups `lmZ1`, `lmZ2`, `lpZ1` and `lpZ2` contain the negatively and positively charged leptons that belong to the corresponding reconstructed Z bosons, respectively, i.e. each of these groups has by definition only a single entry. Examples of the usage of these particle groups can be found in the file `distribution.dat` of this process. Furthermore, the predefined cut `M_Zrec: min_M_Zrec, max_M_Zrec` uses the respective particle groups identified corresponding to the setting of the switch `lepton_identification`.³³

If `lepton_identification = 0` is set, the respective particle groups are not filled and thus cannot be used to define distributions. Also cuts and dynamic scales depending on the identification must not be used in this case, such as `M_Zrec: min_M_Zrec, max_M_Zrec`. In the following we outline the predefined pairing prescriptions.

The ATLAS pairing (`lepton_identification = 1`) considers all possible (two, in the theoretical computation) combinations to associate two OSSF lepton pairs with $Z_1 = e^-e^+$ and $Z_2 = e'^-e'^+$. The criterion to decide on the pairing is the sum of the absolute differences of their invariant masses to the Z -boson mass, i.e. $|m_{e^-e^+} - m_Z| + |m_{e'^-e'^+} - m_Z|$, and the assignment that minimizes this sum is associated with the reconstructed Z bosons $Z_{1,rec} = Z_1$ and $Z_{2,rec} = Z_2$. The respective particle groups are filled accordingly.

The CMS pairing (`lepton_identification = 2`) selects the OSSF lepton pair among all possible pairings (four, in the theoretical computation) that minimizes the invariant-mass difference to the Z -boson mass, $|m_{e^-e^+} - m_Z|$. This pair is always identified as $Z_{1,rec}$, while the remaining pair is defined as $Z_{2,rec}$.

³³ Note that the respective particle groups are also available within the C++ code, see Appendix B.

This process provides an additional switch `switch_off_shell` to speed up the grid-generation phase when considering at least one of the Z bosons to be far off-shell; it should not be used otherwise, see introduction of Sect. 5.2.4 for further details.

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

$$\text{dynamic_scale} = 3: \mu = \sqrt{m_{T,Z_{1,rec}} \cdot m_{T,Z_{2,rec}}}$$

$$\text{dynamic_scale} = 4: \mu = \sqrt{m_Z^2 + p_{T,Z_{1,rec}}^2} + \sqrt{m_Z^2 + p_{T,Z_{2,rec}}^2}$$

5.2.4.5 *ppexnmnm04* ($pp/p\bar{p} \rightarrow e^-e^+v_\mu\bar{v}_\mu$)

Off-shell ZZ production with Z -boson decays to leptons and neutrinos of different flavour³⁴ includes the following predefined cuts:

```
M_leplep: min_M_leplep,
           max_M_leplep
M_leplepnu: min_M_leplepnu,
            max_M_leplepnu,
            min_delta_M_leplepnu,
            max_delta_M_leplepnu
```

The process facilitates the following additional predefined dynamic scale (symbols in Table 5):

$$\text{dynamic_scale} = 3: \mu = \sqrt{m_Z^2 + p_{T,e^-e^+}^2} + \sqrt{m_Z^2 + p_{T,v_\mu\bar{v}_\mu}^2}$$

This process provides an additional switch `switch_off_shell` to speed up the grid-generation phase when considering at least one of the Z bosons to be far off-shell; it should not be used otherwise, see introduction of Sect. 5.2.4 for further details.

5.2.4.6 *ppemxnmnex04* ($pp/p\bar{p} \rightarrow e^- \mu^+ v_\mu \bar{v}_e$)

Off-shell W^+W^- production [36,37] with W -boson decays to DF leptons and the corresponding neutrinos³⁵ includes the following predefined cuts:

```
M_leplep: min_M_leplep,
           max_M_leplep
R_leplep: min_R_leplep
R_ejet: min_R_ejet
```

³⁴ Note that this process includes also $Z\gamma^*$ contributions with the off-shell photon decaying to leptons, and Z/γ^* production with a subsequent decay $Z/\gamma^* \rightarrow e^-e^+v_\mu\bar{v}_\mu$.

³⁵ Note that this process includes also Z/γ^* production with a subsequent decay $Z/\gamma^* \rightarrow e^- \mu^+ v_\mu \bar{v}_e$.

```

pT_leplep: min_pT_leplep
pT_lep_1st: min_pT_lep_1st
M_leplepnunu: min_M_leplepnunu,
               max_M_leplepnunu,
               min_delta_M_leplepnunu,
               max_delta_M_leplepnunu
gap_eta_e: gap_min_eta_e,
            gap_max_eta_e
rel_pT_miss: min_rel_pT_miss
phi_leplep: max_phi_leplep
phi_leplep_nunu: min_phi_leplep_nunu
pT_W: min_pT_W,
       max_pT_W

```

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

$$\text{dynamic_scale} = 3: \mu = \sqrt{m_W^2 + p_{T,e^- \bar{\nu}_e}^2} + \sqrt{m_W^2 + p_{T,\mu^+ \nu_\mu}^2}$$

$$\text{dynamic_scale} = 4: \mu = m_{T,e^- \bar{\nu}_e} + m_{T,\mu^+ \nu_\mu}$$

By default (flavour_scheme = 0) this process is computed in the 4FS, dropping all diagrams with final-state bottom quarks to remove the top-quark contamination. The 5FS can be chosen by setting flavour_scheme = 1, where, however, the top-quark contamination is not removed from the results, since the recommended procedure is much more involved and requires several runs for the 5FS, see introduction of Sect. 5.2.4 for further details.

5.2.4.7 ppeexnenex04 ($pp/p\bar{p} \rightarrow e^- e^+ \nu_e \bar{\nu}_e$)

Off-shell W^+W^- and ZZ production with decays to SF leptons and the corresponding neutrinos³⁶ includes the following predefined cuts:

```

M_leplep: min_M_leplep,
           max_M_leplep
R_leplep: min_R_leplep
R_ejet: min_R_ejet
pT_leplep: min_pT_leplep
pT_lep_1st: min_pT_lep_1st
M_leplepnunu: min_M_leplepnunu,
               max_M_leplepnunu,
               min_delta_M_leplepnunu,
               max_delta_M_leplepnunu
gap_eta_e: gap_min_eta_e,
            gap_max_eta_e
rel_pT_miss: min_rel_pT_miss
phi_leplep: max_phi_leplep
phi_leplep_nunu: min_phi_leplep_nunu

```

³⁶ Note that this process includes also $Z\gamma^*$ contributions with the off-shell photon decaying to leptons, and Z/γ^* production with a subsequent decay $Z/\gamma^* \rightarrow e^- e^+ \nu_e \bar{\nu}_e$.

```

pT_W: min_pT_W,
       max_pT_W

```

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

$$\text{dynamic_scale} = 3: \mu = \sqrt{m_W^2 + p_{T,e^- \bar{\nu}_e}^2} + \sqrt{m_W^2 + p_{T,e^+ \nu_e}^2}$$

$$\text{dynamic_scale} = 4: \mu = m_{T,e^- \bar{\nu}_e} + m_{T,e^+ \nu_e}$$

By default (flavour_scheme = 0) this process is computed in the 4FS, dropping all diagrams with final-state bottom quarks to remove the top-quark contamination. The 5FS can be chosen by setting flavour_scheme = 1, where, however, the top-quark contamination is not removed from the results, since the recommended procedure is much more involved and requires several runs for the 5FS, see introduction of Sect. 5.2.4 for further details.

This process includes an additional switch switch_off_shell to speed up the grid-generation phase when considering at least one of the Z bosons to be far off-shell; it should not be used otherwise, see introduction of Sect. 5.2.4 for further details.

5.2.4.8 ppemexnm04 ($pp/p\bar{p} \rightarrow e^- \mu^- e^+ \bar{\nu}_\mu$), ppeeexnm04 ($pp/p\bar{p} \rightarrow e^- e^+ \mu^+ \nu_\mu$)

Off-shell $W^\pm Z$ production [38, 39] with decays to one OSSF lepton pair, one DF lepton and one corresponding neutrino³⁷ (DF channel) includes the following predefined cuts:

```

M_Zrec: min_M_Zrec,
         max_M_Zrec
delta_M_Zrec_MZ: max_delta_M_Zrec_MZ
delta_M_leplelep_MZ: min_delta_M_leplelep_MZ
R_leplep: min_R_leplep
R_lepZlepZ: min_R_lepZlepZ
R_lepZlepW: min_R_lepZlepW
electron_cuts: min_pT_e_1st,
                min_pT_e_2nd
muon_cuts: min_pT_mu_1st,
            min_pT_mu_2nd
lepton_cuts: min_pT_lep_1st,
              min_pT_lep_2nd
leading_lepton_cuts: min_pT_lep_1st_if_e,
                     min_pT_lep_1st_if_mu
MT_Wrec: min_MT_Wrec

```

In the DF channel W and Z bosons can be unambiguously identified. In analogy to the SF case we define the following particle groups which can be accessed, e.g., in distributions:

³⁷ Note that this process includes also W^-/W^+ production with a subsequent decay $W \rightarrow e^- e^+ \mu \nu_\mu$.

Particle group `Zrec` contains the Z boson, reconstructed by the two electrons, and `Wrec` the W boson, defined by the muon and the neutrino. `lepZ` contains the corresponding leptons of the Z boson, ordered in their transverse momentum, and `lepW` the lepton of the W boson.

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

$$\begin{aligned} \text{dynamic_scale} = 3: \mu &= \frac{1}{2} \left(\sqrt{m_Z^2 + p_{T,Zrec}^2} + \sqrt{m_W^2 + p_{T,Wrec}^2} \right) \\ \text{dynamic_scale} = 4: \mu &= \frac{1}{2} \left(m_{T,Zrec} + m_{T,Wrec} \right) \end{aligned}$$

5.2.4.9 `ppeeexn04` ($pp/p\bar{p} \rightarrow e^-e^-e^+\bar{\nu}_e$),
`ppeexn04` ($pp/p\bar{p} \rightarrow e^-e^+e^+\nu_e$)

Off-shell $W^\pm Z$ production [38,39] with decays to three SF leptons and one corresponding neutrino³⁸ (SF channel) includes the following predefined cuts:

```
lepton_identification
M_Zrec: min_M_Zrec,
      max_M_Zrec
M_leplep_OSSF: min_M_leplep_OSSF
delta_M_Zrec_MZ: max_delta_M_Zrec_MZ
delta_M_lepleplep_MZ: min_delta_M_lepleplep_MZ
R_leplep: min_R_leplep
R_lepZlepZ: min_R_lepZlepZ
R_lepZlepW: min_R_lepZlepW
lepW_cuts: min_pT_lepW,
           max_eta_lepW
lepZ_cuts: min_pT_lepZ_1st,
           min_pT_lepZ_2nd
lepton_cuts: min_pT_lep_1st,
            min_pT_lep_2nd
MT_Wrec: min_MT_Wrec
```

Since this process features three SF leptons, two of which have the same charge, and one neutrino, a-priori the leptons are not unambiguously associated with the decays of the Z and W bosons. However, the experimental analyses often rely on cuts specific to (reconstructed) Z and W bosons. Hence, in the SF channel an identification procedure is required to unambiguously assign one OSSF lepton pair to the Z boson as well as the remaining lepton and the neutrino to the W boson. The parameter `lepton_identification` switches between two such predefined identification procedures, as used by ATLAS and CMS. In both cases four new particle groups are defined (see Sect. 5.1.1.4 and the

³⁸ Note that this process includes also W^-/W^+ production with a subsequent decay $W \rightarrow e^-e^+\nu_e$.

related Table 3 for the standard particle groups) to make them accessible in cuts, scales and distributions: Particle group `Zrec` contains the OSSF lepton pair that is reconstructed as a Z boson, labelled `Zrec`. `Wrec` contains the lepton and the neutrino that are reconstructed as a W boson, labelled `Wrec`. `lepZ` is filled with the leptons corresponding to the reconstructed Z boson in the standard p_T -ordering, and `lepW` with the lepton assigned to the W boson. By definition each of the other particle groups effectively contains only one particle, whereas `lepZ` contains two particles. Examples for the usage of these particle groups can be found in the file `distribution.dat` of this process. Furthermore, many of the predefined cuts, e.g. `delta_M_Zrec_MZ`: `max_delta_M_Zrec_MZ`, `MT_Wrec`: `min_MT_Wrec` or `R_lepZlepW`: `min_R_lepZlepW`, use the respective particle groups, which are filled according to the chosen value of the switch `lepton_identification`.³⁹

If `lepton_identification = 0` is set, the respective particle groups are not filled and thus cannot be used to define distributions. Also dynamic scales and cuts depending on the identification must not be used in this case. Finally, we outline the predefined pairing prescriptions:

ATLAS applies the so-called resonant-shape procedure [107] (`lepton_identification = 1`), where the assignment that maximizes the estimator

$$P = \left| \frac{1}{m_{e^-e^+}^2 - m_Z^2 + i \Gamma_Z m_Z} \right|^2 \cdot \left| \frac{1}{m_{e^\pm\nu_e}^2 - m_W^2 + i \Gamma_W m_W} \right|^2 \tag{6}$$

is chosen to identify $Z_{rec} = Z$ and $W_{rec} = W$, and the respective particles groups are filled accordingly.⁴⁰

The CMS pairing (`lepton_identification = 2`) simply chooses the OSSF lepton pair that minimizes the invariant-mass difference to the Z -boson mass, i.e. $|m_{e^-e^+} - m_Z|$. This pair is identified as `Zrec`, and `Wrec` and the other particle groups are assigned accordingly.

The process facilitates the following additional predefined dynamic scales (symbols in Table 5):

$$\begin{aligned} \text{dynamic_scale} = 3: \mu &= \frac{1}{2} \left(\sqrt{m_Z^2 + p_{T,Zrec}^2} + \sqrt{m_W^2 + p_{T,Wrec}^2} \right) \\ \text{dynamic_scale} = 4: \mu &= \frac{1}{2} \left(m_{T,Zrec} + m_{T,Wrec} \right) \end{aligned}$$

³⁹ Note that the respective particle groups are also available within the C++ code, see Appendix B.

⁴⁰ We note that this definition requires the knowledge of the complete momentum of the neutrino. This variable can, of course, be used in the theoretical calculation, but cannot be directly extracted in the experimental analysis, where it must be reconstructed with the Monte Carlo.

6 Phenomenological results

In this section we present results on integrated cross sections for all processes available in the first MATRIX release. They are reported at LO, NLO and NNLO to study the impact of QCD radiative corrections. We also discuss the impact of the loop-induced gg contribution on the NNLO cross section, if applicable. The results in this section are obtained with the MATRIX default setup for each of these processes. Their purpose is both to provide benchmark numbers for all processes that can be evaluated with MATRIX, and to give a reference for the user: These benchmark results can be reproduced (on a statistical level) if no changes are applied to the default input cards (except for turning on the corresponding perturbative orders and the targeted precision the user is interested in).

6.1 Settings

We consider proton–proton collisions at the 13 TeV LHC. In terms of the input of the weak parameters, the G_μ scheme is employed: When considering leptonic final state, which are always produced via off-shell EW vector bosons, we use the complex-mass scheme [108] throughout, i.e. we use complex W - and Z -boson masses and define the EW mixing angle as $\cos\theta_W^2 = (m_W^2 - i\Gamma_W m_W)/(m_Z^2 - i\Gamma_Z m_Z)$ and $\alpha = \sqrt{2} G_\mu m_W^2 \sin^2\theta_W/\pi$, using the PDG [105] values $G_F = 1.16639 \times 10^{-5} \text{ GeV}^{-2}$, $m_W = 80.385 \text{ GeV}$, $\Gamma_W = 2.0854 \text{ GeV}$, $m_Z = 91.1876 \text{ GeV}$ and $\Gamma_Z = 2.4952 \text{ GeV}$. Furthermore, we set $m_H = 125 \text{ GeV}$ and $\Gamma_H = 0.00407 \text{ GeV}$. When considering on-shell single-boson production or on-shell production of heavy-boson pairs, the masses of the weak vector bosons and the weak mixing angle are consistently kept real by setting $\Gamma_W = \Gamma_Z = 0$, and we also use a real Higgs boson mass, i.e. $\Gamma_H = 0$. The number of heavy-quark flavours depends on the applied flavour scheme. As outlined in Sect. 5.2.4, all processes involving W^+W^- contributions use the 4FS as default to consistently remove top-quark contamination by dropping the (separately IR finite) partonic processes with real bottom-quark emissions. In the 4FS we use the on-shell bottom mass $m_b = 4.92 \text{ GeV}$. All other processes apply the 5FS with a vanishing bottom mass $m_b = 0$. The top quark is treated as massive and unstable throughout, and we set $m_t = 173.2 \text{ GeV}$ as well as $\Gamma_t = 1.44262 \text{ GeV}$.⁴¹ We use the consistent NNPDF3.0 [109] set of parton distributions (PDFs) with $n_f = 4$ or $n_f = 5$ active quark flavours. N^{th} LO

⁴¹ Massive top-quark contributions are neglected in the virtual two-loop corrections, but are kept anywhere else in the computations. Besides the fact that massive quark contributions in the two-loop amplitudes are not available and at the edge of current technology, their numerical effect can be expected to be negligible in most cases.

($n = 0, 1, 2$) predictions are obtained by using PDFs at the same perturbative order and the evolution of α_S at $(n + 1)$ -loop order, as provided by the corresponding PDF set.⁴² The CKM matrix is set to unity except for the production of a single (on- or off-shell) W^\pm boson. In that case we use the PDG SM values as reported in Ref. [105]:

$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 0.97417 & 0.2248 & 0.00409 \\ 0.22 & 0.995 & 0.0405 \\ 0.0082 & 0.04 & 1.009 \end{pmatrix}. \quad (7)$$

Our reference choice μ_0 for renormalization (μ_R) and factorization (μ_F) scales as well as the set of cuts applied in our default setups depend on the individual process. Both are reported when discussing the results in the upcoming section. Uncertainties from missing higher-order contributions are estimated in the usual way by independently varying μ_R and μ_F in the range $0.5\mu_0 \leq \mu_R, \mu_F \leq 2\mu_0$, with the constraint $0.5 \leq \mu_R/\mu_F \leq 2$. Unless specified otherwise, jets are defined by the anti- k_T clustering algorithm, $R = 0.4$, $p_{T,j} > 25 \text{ GeV}$ and $|\eta_j| < 4.5$.

6.2 Cross-section predictions

Reference LO, NLO and NNLO predictions of the integrated cross sections for all processes that are available in MATRIX are reported in Table 6. Note that the processes under consideration feature cross sections that may differ by several orders of magnitude, starting from a few fb up to several nb.

Two results are reported at NNLO: $\sigma_{\text{NNLO}}^{r_{\text{cut}}}$ denotes the NNLO cross section at a fixed r_{cut} value; the default $r_{\text{cut}} = 0.15\%$ is used throughout for our reference results. Our best prediction is denoted as $\sigma_{\text{NNLO}}^{\text{extrapolated}}$, and it is determined by the $r_{\text{cut}} \rightarrow 0$ extrapolation of the r_{cut} dependence between $r_{\text{cut}} = 0.15\%$ and $r_{\text{cut}} = 1\%$ (see Sect. 7 for details). Both NNLO predictions are provided at the end of every MATRIX run, and for each process the results in Table 6 are taken from the same MATRIX run. The relative uncertainties, automatically computed by the code, refer to scale variations, as defined in Sect. 6.1.⁴³ The numerical uncertainty is reported in round brackets for all our predic-

⁴² More precisely, in the 5FS we use NNPDF30_lo_as_0118, NNPDF30_nlo_as_0118, and NNPDF30_nnlo_as_0118 at LO, NLO, and NNLO, corresponding to $\alpha_S^{(5F)}(m_Z) = 0.1180$ throughout. In the 4FS we use NNPDF30_lo_as_0118_nf_4, Footnote 42 continued

NNPDF30_nlo_as_0118_nf_4, and NNPDF30_nnlo_as_0118_nf_4 at LO, NLO, and NNLO, corresponding to $\alpha_S^{(4F)}(m_Z) = 0.1136, 0.1123, \text{ and } 0.1123$, respectively.

⁴³ The automatic evaluation of PDF uncertainties is not supported in the first release of MATRIX.

tions. For $\sigma_{\text{NNLO}}^{\text{extrapolated}}$ this uncertainty is obtained by combining the statistical uncertainty from Monte Carlo integration with the systematic uncertainty induced by the r_{cut} dependence.

Besides results at LO, NLO and NNLO accuracy, a separate column refers to the absolute (and relative) size of the loop-induced gg component σ_{loop} ($\sigma_{\text{loop}}/\Delta\sigma_{\text{NNLO}}^{\text{ext}}$) of the NNLO corrections, where applicable. The absolute size of the NNLO contributions for the extrapolated result is defined as $\Delta\sigma_{\text{NNLO}}^{\text{ext}} = \sigma_{\text{NNLO}}^{\text{extrapolated}} - \sigma_{\text{NLO}}$, where σ_{NLO} is computed with NLO PDFs. Two additional columns refer to the relative size of the radiative corrections in terms of K factors at NLO and NNLO, defined as

$$K_{\text{NLO}} = \frac{\sigma_{\text{NLO}}}{\sigma_{\text{LO}}} \quad \text{and} \quad K_{\text{NNLO}} = \frac{\sigma_{\text{NNLO}}}{\sigma_{\text{NLO}}}. \quad (8)$$

The latter are computed from our best NNLO predictions, i.e. the extrapolated NNLO results.

For all production processes involving massive on-shell bosons (H , Z , W^\pm , W^+W^- and ZZ production), Table 6 reports fully inclusive cross sections, i. e. no phase-space cuts are applied. For all remaining processes, phase-space cuts are applied on the final-state leptons, neutrinos and photons in order to simulate a realistic selection in a fiducial volume. The respective sets of cuts for each of these processes are discussed below. For detailed studies of phenomenological results we refer to dedicated publications on the respective processes. We restrict ourselves to summarizing basic features of the calculations and the overall effect of the higher-order QCD corrections.

Higgs boson production

Radiative corrections to Higgs boson production are known to be particularly large. The corresponding cross sections in Table 6 have been computed with fixed renormalization and factorization scales set to $\mu_0 = m_H$. The results have been checked to be in perfect agreement within the quoted numerical uncertainty with the analytic code SUSHI [110]. We find $K_{\text{NLO}} = 1.96$ and $K_{\text{NNLO}} = 1.32$ for the NLO and NNLO K factors, respectively. As it is well known [3–5], scale variations significantly decrease upon inclusion of radiative corrections, but at LO and NLO they do not reflect the actual size of missing higher-order contributions.

Drell–Yan production

On-shell Drell–Yan production is another well-studied process, and it was the first hadron-collider process for which NNLO corrections were computed [2, 3]. The results reported in Table 6 are obtained with renormalization and factorization scales set to $\mu_0 = m_Z$ and $\mu_0 = m_W$ for $pp \rightarrow Z$ and $pp \rightarrow W^\pm$, respectively. The same fixed scales are applied to the corresponding off-shell processes. The Drell–Yan cross section is more than three orders of magnitude larger than the

one of Higgs boson production, and the impact of radiative corrections is known to be smaller: NLO corrections increase the LO result by about 25%, and NNLO corrections amount to a further +3% effect. $pp \rightarrow Z$ has been checked numerically against the analytic result of Refs. [2, 3], and we have validated the CKM implementation by finding full agreement at the level of the numerical errors for $pp \rightarrow e^\pm \nu$ with FEWZ [53] and DYNNOLO [12].⁴⁴

The cross sections of the charged-current and neutral-current Drell–Yan processes correspond in a first approximation to the on-shell W or Z production cross sections times the respective leptonic branching ratios. Consequently, they decrease by at least one order of magnitude with respect to the on-shell case.

The following sets of cuts, which are also summarized in Table 7, are applied to these processes: Every final-state lepton is required to have a minimum transverse momentum of $p_{T,\ell} > 25 \text{ GeV}$ and a maximal pseudo-rapidity $|\eta_\ell| < 2.47$. Neutrinos originating from a W -boson decay are restricted by a minimal requirement on the total missing transverse momentum, $p_T^{\text{miss}} > 20 \text{ GeV}$. Additionally, we require $66 \text{ GeV} < m_{\ell-\ell^+} < 116 \text{ GeV}$ for the invariant mass of the two leptons in $pp \rightarrow e^-e^+$. The lower cut separates the leptons to avoid singularities arising from the photon-mediated contributions to this process. The process $pp \rightarrow \nu_e \bar{\nu}_e$, which is only relevant as a technical check, is calculated without any phase-space cuts. We find that, except for the $pp \rightarrow e^-e^+$ process, which is affected by perturbative instabilities as discussed below, the off-shell contributions and additional phase-space cuts hardly have any effect on radiative corrections, which remain $K_{\text{NLO}} \sim 1.25$ and $K_{\text{NNLO}} \sim 1.03$ as in the on-shell case. The ratio of W^- and W^+ cross sections does not significantly differ between on-shell and off-shell W^\pm production: We find roughly $\sigma_{W^-}/\sigma_{W^+} \sim 0.75$, essentially independent of the perturbative order.

We note that the $pp \rightarrow e^-e^+$ process has a peculiarly large r_{cut} dependence at NNLO, similar to the processes involving final-state photons, thereby leading to a rather large systematic uncertainty. The large r_{cut} dependence is due to the choice of symmetric p_T thresholds on the leptons, which causes perturbative instabilities in the integrated cross section, as first observed in Ref. [111] (for a recent discussion of this problem, see Ref. [112]).⁴⁵ However, choosing asym-

⁴⁴ More precisely, FEWZ and MATRIX agree at the permille level (see Sect. 7), and the agreement between DYNNOLO and MATRIX at fixed r_{cut} values is at the same level.

⁴⁵ We note that a finite r_{cut} leads to a smoother behaviour of the NNLO cross section in the delicate region of symmetric cuts (see e.g. Ref. [113]). One should, however, keep in mind that r_{cut} is not to be understood as a tuning parameter. The smoother behaviour is a simple consequence of the fact that a finite r_{cut} resolves the delicate phase-space region in less detail, thus smearing the unphysical behaviour of

Table 6 Integrated cross sections for all available processes in MATRIX using the default setups

Process ($\{\text{process_id}\}$)	σ_{LO}	σ_{NLO}	σ_{loop} ($\sigma_{\text{loop}}/\Delta\sigma_{\text{NNLO}}^{\text{ext}}$)	$\sigma_{\text{NNLO}}^{\text{cut}}$	$\sigma_{\text{NNLO}}^{\text{extrapolated}}$	K_{NLO} (%)	K_{NNLO} (%)
$pp \rightarrow H$ (pph21)	15.42(0) $^{+22\%}_{-17\%}$ pb	30.26(1) $^{+20\%}_{-15\%}$ pb	–	39.93(3) $^{+11\%}_{-10\%}$ pb	39.93(3) $^{+11\%}_{-10\%}$ pb	+ 96.2	+ 32.0
$pp \rightarrow Z$ (ppz01)	43.32(0) $^{+12\%}_{-13\%}$ nb	54.20(1) $^{+3.1\%}_{-4.9\%}$ nb	–	56.01(3) $^{+0.84\%}_{-1.1\%}$ nb	55.99(3) $^{+0.84\%}_{-1.1\%}$ nb	+ 25.1	+ 3.31
$pp \rightarrow W^-$ (ppw01)	60.15(0) $^{+13\%}_{-14\%}$ nb	75.95(2) $^{+3.3\%}_{-5.3\%}$ nb	–	78.36(3) $^{+0.98\%}_{-1.2\%}$ nb	78.33(8) $^{+0.98\%}_{-1.2\%}$ nb	+ 26.3	+ 3.14
$pp \rightarrow W^+$ (ppwx01)	81.28(1) $^{+13\%}_{-14\%}$ nb	102.2(0) $^{+3.4\%}_{-5.3\%}$ nb	–	105.8(1) $^{+0.93\%}_{-1.3\%}$ nb	105.8(1) $^{+0.93\%}_{-1.3\%}$ nb	+ 25.7	+ 3.52
$pp \rightarrow e^-e^+$ (ppeex02)	592.8(1) $^{+14\%}_{-14\%}$ pb	699.7(2) $^{+2.9\%}_{-4.5\%}$ pb	–	728.4(3) $^{+0.48\%}_{-0.72\%}$ pb	732.7(3.4) $^{+0.43\%}_{-0.79\%}$ pb	+ 18.0	+ 4.72
$pp \rightarrow \nu_e\bar{\nu}_e$ (ppnenex02)	2876(0) $^{+12\%}_{-13\%}$ pb	3585(1) $^{+3.0\%}_{-4.9\%}$ pb	–	3705(2) $^{+0.86\%}_{-1.1\%}$ pb	3710(2) $^{+0.85\%}_{-1.1\%}$ pb	+ 24.6	+ 3.48
$pp \rightarrow e^-\bar{\nu}_e$ (ppenex02)	2972(0) $^{+14\%}_{-15\%}$ pb	3674(1) $^{+3.1\%}_{-5.2\%}$ pb	–	3772(2) $^{+0.89\%}_{-0.94\%}$ pb	3768(3) $^{+0.90\%}_{-0.93\%}$ pb	+ 23.6	+ 2.57
$pp \rightarrow e^+\nu_e$ (ppexne02)	3964(0) $^{+14\%}_{-14\%}$ pb	4855(1) $^{+3.0\%}_{-5.1\%}$ pb	–	4986(2) $^{+0.88\%}_{-0.95\%}$ pb	4986(3) $^{+0.88\%}_{-0.95\%}$ pb	+ 22.5	+ 2.70
$pp \rightarrow \gamma\gamma$ (ppaa02)	5.592(1) $^{+10\%}_{-11\%}$ pb	25.75(1) $^{+8.8\%}_{-7.5\%}$ pb	2.534(1) $^{+24\%}_{-17\%}$ pb (17.4%)	40.86(2) $^{+8.7\%}_{-7.2\%}$ pb	40.28(30) $^{+8.7\%}_{-7.0\%}$ pb	+ 361	+ 56.4
$pp \rightarrow e^-e^+\gamma$ (ppeexa03)	1469(0) $^{+12\%}_{-12\%}$ fb	2119(1) $^{+2.9\%}_{-4.6\%}$ fb	16.02(1) $^{+24\%}_{-18\%}$ fb (8.14%)	2326(1) $^{+1.2\%}_{-1.3\%}$ fb	2316(5) $^{+1.1\%}_{-1.2\%}$ fb	+ 44.3	+ 9.29
$pp \rightarrow \nu_e\bar{\nu}_e\gamma$ (ppnenexa03)	63.61(1) $^{+2.7\%}_{-3.5\%}$ fb	98.75(2) $^{+3.3\%}_{-2.7\%}$ fb	2.559(2) $^{+26\%}_{-19\%}$ fb (17.3%)	114.7(1) $^{+3.2\%}_{-2.6\%}$ fb	113.5(6) $^{+2.9\%}_{-2.4\%}$ fb	+ 55.2	+ 15.0
$pp \rightarrow e^-\bar{\nu}_e\gamma$ (ppenexa03)	726.1(1) $^{+11\%}_{-12\%}$ fb	1850(1) $^{+6.6\%}_{-5.3\%}$ fb	–	2286(1) $^{+4.0\%}_{-3.7\%}$ fb	2256(15) $^{+3.7\%}_{-3.5\%}$ fb	+ 155	+ 22.0
$pp \rightarrow e^+\nu_e\gamma$ (ppexnea03)	861.7(1) $^{+10\%}_{-11\%}$ fb	2187(1) $^{+6.6\%}_{-5.3\%}$ fb	–	2707(3) $^{+4.1\%}_{-3.8\%}$ fb	2671(35) $^{+3.8\%}_{-3.6\%}$ fb	+ 154	+ 22.1
$pp \rightarrow ZZ$ (ppzz02)	9.845(1) $^{+5.2\%}_{-6.3\%}$ pb	14.10(0) $^{+2.9\%}_{-2.4\%}$ pb	1.361(1) $^{+25\%}_{-19\%}$ pb (52.9%)	16.68(1) $^{+3.2\%}_{-2.6\%}$ pb	16.67(1) $^{+3.2\%}_{-2.6\%}$ pb	+ 43.3	+ 18.2
$pp \rightarrow W^+W^-$ (ppwxw02)	66.64(1) $^{+5.7\%}_{-6.7\%}$ pb	103.2(0) $^{+3.9\%}_{-3.1\%}$ pb	4.091(3) $^{+27\%}_{-19\%}$ pb (29.5%)	117.1(1) $^{+2.5\%}_{-2.2\%}$ pb	117.1(1) $^{+2.5\%}_{-2.2\%}$ pb	+ 54.9	+ 13.4
$pp \rightarrow e^-\mu^-e^+\mu^+$ (ppemexmx04)	11.34(0) $^{+6.3\%}_{-7.3\%}$ fb	16.87(0) $^{+3.0\%}_{-2.5\%}$ fb	1.971(1) $^{+25\%}_{-18\%}$ fb (57.6%)	20.30(1) $^{+3.5\%}_{-2.9\%}$ fb	20.30(1) $^{+3.5\%}_{-2.9\%}$ fb	+ 48.8	+ 20.3
$pp \rightarrow e^-e^-e^+e^+$ (ppeexex04)	5.781(1) $^{+6.3\%}_{-7.4\%}$ fb	8.623(3) $^{+3.1\%}_{-2.5\%}$ fb	0.9941(4) $^{+25\%}_{-18\%}$ fb (56.9%)	10.37(1) $^{+3.5\%}_{-3.0\%}$ fb	10.37(1) $^{+3.5\%}_{-3.0\%}$ fb	+ 49.2	+ 20.2
$pp \rightarrow e^-e^+\nu_\mu\bar{\nu}_\mu$ (ppeexnmnm04)	22.34(0) $^{+5.3\%}_{-6.4\%}$ fb	33.90(1) $^{+3.3\%}_{-2.7\%}$ fb	3.212(1) $^{+25\%}_{-19\%}$ fb (49.6%)	40.39(2) $^{+3.5\%}_{-2.8\%}$ fb	40.38(2) $^{+3.5\%}_{-2.8\%}$ fb	+ 51.7	+ 19.1
$pp \rightarrow e^-\mu^+\nu_\mu\bar{\nu}_e$ (ppemxnmn04)	232.9(0) $^{+6.6\%}_{-7.6\%}$ fb	236.1(1) $^{+2.8\%}_{-2.4\%}$ fb	26.93(1) $^{+27\%}_{-19\%}$ fb (94.3%)	264.7(1) $^{+2.2\%}_{-1.4\%}$ fb	264.6(2) $^{+2.2\%}_{-1.4\%}$ fb	+ 1.34	+ 12.1
$pp \rightarrow e^-e^+\nu_e\bar{\nu}_e$ (ppeexnen04)	115.0(0) $^{+6.3\%}_{-7.3\%}$ fb	203.4(1) $^{+4.7\%}_{-3.8\%}$ fb	12.62(1) $^{+26\%}_{-19\%}$ fb (33.8%)	240.8(1) $^{+3.4\%}_{-3.0\%}$ fb	240.7(1) $^{+3.4\%}_{-3.0\%}$ fb	+ 76.9	+ 18.4
$pp \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$ (ppemexnm04)	11.50(0) $^{+5.7\%}_{-6.8\%}$ fb	23.55(1) $^{+5.5\%}_{-4.5\%}$ fb	–	26.17(1) $^{+2.2\%}_{-2.1\%}$ fb	26.17(2) $^{+2.2\%}_{-2.1\%}$ fb	+ 105	+ 11.1
$pp \rightarrow e^-e^-e^+\bar{\nu}_e$ (ppeexn04)	11.53(0) $^{+5.7\%}_{-6.8\%}$ fb	23.63(1) $^{+5.5\%}_{-4.5\%}$ fb	–	26.27(1) $^{+2.3\%}_{-2.1\%}$ fb	26.25(2) $^{+2.3\%}_{-2.1\%}$ fb	+ 105	+ 11.1

Table 6 continued

Process ($\{\text{process_id}\}$)	σ_{LO}	σ_{NLO}	σ_{loop} ($\sigma_{\text{loop}}/\Delta\sigma_{\text{NNLO}}^{\text{ext}}$)	$\sigma_{\text{NNLO}}^{r_{\text{cut}}}$	$\sigma_{\text{NNLO}}^{\text{extrapolated}}$	$K_{\text{NLO}} (\%)$	$K_{\text{NNLO}} (\%)$
$pp \rightarrow e^- e^+ \mu^+ \nu_\mu$ (ppeeexmxnm04)	17.33(0) $^{+5.3\%}_{-6.3\%}$ fb	34.14(1) $^{+5.3\%}_{-4.3\%}$ fb	–	37.74(2) $^{+2.2\%}_{-2.0\%}$ fb	37.74(4) $^{+2.2\%}_{-2.0\%}$ fb	+97.0	+10.6
$pp \rightarrow e^- e^+ e^+ \nu_e$ (ppeeexxne04)	17.37(0) $^{+5.3\%}_{-6.3\%}$ fb	34.21(2) $^{+5.3\%}_{-4.3\%}$ fb	–	37.85(2) $^{+2.3\%}_{-2.0\%}$ fb	37.84(3) $^{+2.3\%}_{-2.0\%}$ fb	+96.9	+10.6

Table 7 Default setup of fiducial cuts for Z , W^\pm and $\gamma\gamma$ production processes

	$pp \rightarrow e^- e^+$	$pp \rightarrow e^- \bar{\nu}_e / pp \rightarrow e^+ \nu_e$	$pp \rightarrow \gamma\gamma$
Lepton cuts	$p_{T,\ell} > 25 \text{ GeV}$, $ \eta_\ell < 2.47$ $66 \text{ GeV} < m_{\ell-\ell^+} < 116 \text{ GeV}$	$p_{T,\ell} > 25 \text{ GeV}$, $ \eta_\ell < 2.47$	–
Photon cuts	–	–	$p_{T,\gamma_1} > 40 \text{ GeV}$, $p_{T,\gamma_2} > 25 \text{ GeV}$ $ \eta_\gamma < 2.5$ $20 \text{ GeV} < m_{\gamma\gamma} < 250 \text{ GeV}$
Neutrino cuts	–	$p_T^{\text{miss}} > 20 \text{ GeV}$	–
Photon isolation	–	–	Frixione isolation with $n = 1$, $\varepsilon = 0.5$ and $\delta_0 = 0.4$
Jet definition	Anti- k_T algorithm with $R = 0.4$; $p_{T,j} > 25 \text{ GeV}$, $ \eta_j < 4.5$		

Table 8 Default setup of fiducial cuts for $Z\gamma$ and $W^\pm\gamma$ production processes

	$pp \rightarrow e^- e^+ \gamma$	$pp \rightarrow \nu_e \bar{\nu}_e \gamma$	$pp \rightarrow e^- \bar{\nu}_e \gamma / pp \rightarrow e^+ \nu_e \gamma$
Lepton cuts	$p_{T,\ell} > 25 \text{ GeV}$, $ \eta_\ell < 2.47$ $m_{\ell-\ell^+} > 40 \text{ GeV}$	–	$p_{T,\ell} > 25 \text{ GeV}$, $ \eta_\ell < 2.47$
Photon cuts	$p_{T,\gamma} > 15 \text{ GeV}$, $ \eta_\gamma < 2.37$	$p_{T,\gamma} > 100 \text{ GeV}$, $ \eta_\gamma < 2.37$	$p_{T,\gamma} > 15 \text{ GeV}$, $ \eta_\gamma < 2.37$
Neutrino cuts	–	$p_T^{\text{miss}} > 90 \text{ GeV}$	$p_T^{\text{miss}} > 35 \text{ GeV}$
Separation cuts	$\Delta R_{\ell j} > 0.3$, $\Delta R_{\gamma j} > 0.3$, $\Delta R_{\ell\gamma} > 0.7$	$\Delta R_{\gamma j} > 0.3$	$\Delta R_{\ell j} > 0.3$, $\Delta R_{\gamma j} > 0.3$, $\Delta R_{\ell\gamma} > 0.7$
Photon isolation	Frixione isolation with $n = 1$, $\varepsilon = 0.5$ and $\delta_0 = 0.4$		
Jet definition	Anti- k_T algorithm with $R = 0.4$; $p_{T,j} > 30 \text{ GeV}$, $ \eta_j < 4.4$		

metric p_T cuts on the harder and softer lepton does not reduce this dependence significantly. On the contrary, we find that if the asymmetric cuts are separately applied on the negatively and positively charged leptons (instead of applying them on the harder and softer lepton) the ensuing r_{cut} behaviour is extremely flat and therefore a small $r_{\text{cut}} \rightarrow 0$ extrapolation uncertainty is obtained. The r_{cut} behaviour of the $pp \rightarrow e^- e^+$ process is discussed in Sect. 7, where we also present a comparison of our results with FEWZ. We stress that more accurate results for this process can be obtained through the setting of `switch_qT_accuracy = 1` in

the fixed-order cross section. A reliable perturbative prediction in the region of symmetric cuts can only be obtained through a dedicated resummation procedure.

the file `parameter.dat` by using a minimal value of $r_{\text{cut}} = 0.05\%$ (default is $r_{\text{cut}} = 0.15\%$) for the extrapolation range, see Sect. 5.2.2.3.

Diphoton and vector-boson plus photon production

For diphoton production we choose the invariant mass of the photon pair as the central scale, i.e. $\mu_0 = m_{\gamma\gamma}$, Frixione isolation with $n = 1$, $\varepsilon = 0.5$ and $\delta_0 = 0.4$ (see Eq. (3)), and the following fiducial cuts, which are also summarized in Table 7: The isolated photons are required to have a pseudo-rapidity $|\eta_\gamma| < 2.5$, and the transverse momentum of the (sub)leading photon must fulfil $p_{T,\gamma} > 40(25) \text{ GeV}$. Further, we require $20 \text{ GeV} < m_{\gamma\gamma} < 250 \text{ GeV}$ for the invariant mass of the two photons. Our predictions show the importance of QCD corrections for this process: With $K_{\text{NLO}} = 4.61$ and

$K_{\text{NNLO}} = 1.56$, higher-order effects are enormous [28, 29] and not at all reflected by the estimated scale uncertainties at lower orders. This process entails a loop-induced gg component in the NNLO cross section. With only a 17% contribution to the NNLO correction it has a rather moderate impact though. Our results have been compared to those obtained with the $2\gamma\text{NNLO}$ code at fixed values of r_{cut} , and agreement has been found at the level of 0.5%.

Next, we consider the associated production of an off-shell vector boson with a photon, i.e. the leptonic final states $e^-e^+\gamma/\nu_e\bar{\nu}_e\gamma$ (summarized as $Z\gamma$ production) and $e^+\nu_e\gamma/e^-\bar{\nu}_e\gamma$ (summarized as $W\gamma$ production).⁴⁶ Our setup is adopted from Ref. [31]: The dynamic scale $\mu_0 = \sqrt{m_V^2 + p_{T,\gamma}^2}$ is chosen as central value for both renormalization and factorization scales, where $m_V = m_Z$ for $Z\gamma$ and $m_V = m_W$ for $W\gamma$ production. As for diphoton production, Frixione isolation with $n = 1$, $\varepsilon = 0.5$ and $\delta_0 = 0.4$ (see Eq. (3)) is used to identify photons. The fiducial cuts include standard cuts on leptons, photons and the missing transverse momentum, as well as lepton–photon, lepton–jet and photon–jet separations in R . The numerical values of these cuts are summarized in Table 8. The $Z\gamma$ processes feature large corrections, $K_{\text{NLO}}(K_{\text{NNLO}}) = 1.44(1.09)$ for $pp \rightarrow e^-e^+\gamma$ and $K_{\text{NLO}}(K_{\text{NNLO}}) = 1.55(1.15)$ for $pp \rightarrow \nu_e\bar{\nu}_e\gamma$. For $W\gamma$ production, radiative corrections are known to be huge due to a radiation zero at LO [114]: At NLO the $W^\pm\gamma$ cross section is increased by more than +150%, and the NNLO corrections have a further effect of +22%. The ratio between the $W^-\gamma$ and $W^+\gamma$ cross sections is roughly $\sigma_{W^-\gamma}/\sigma_{W^+\gamma} \sim 0.75$, widely independent of the perturbative order and very similar to the ratio of the charged Drell–Yan processes.

One should bear in mind that all processes with isolated photons in the final state have a relatively large uncertainty at NNLO (~ 0.5 –1%) even after the $r_{\text{cut}} \rightarrow 0$ extrapolation (which in the default setup is based on the r_{cut} dependence between $r_{\text{cut}} = 0.15\%$ and $r_{\text{cut}} = 1\%$). More accurate results can be obtained by setting `switch_qT_accuracy = 1` in the file `parameter.dat`, which uses a minimal value of $r_{\text{cut}} = 0.05\%$ for the extrapolation range, see Sect. 5.2.3. We refer to the discussion in Sect. 7 for details.

Vector-boson pair production

The on-shell ZZ and W^+W^- results in Table 6 correspond to the inclusive cross sections of Ref. [33] and Ref. [36], respectively, with an updated set of input parameters. We have explicitly checked that MATRIX reproduces the results of Refs. [33, 36] when adjusting the setup accordingly. Con-

sistent with these studies, we have used fixed renormalization and factorization scales of $\mu_0 = m_Z$ and $\mu_0 = m_W$ for ZZ and W^+W^- production, respectively. Radiative corrections are large for both processes: The NLO corrections amount to +43% at NLO and still +18% at NNLO in the case of ZZ production, where a bit more than half of the NNLO corrections originates from the loop-induced gg channel, though. The predicted W^+W^- cross section receives NLO corrections of +55%, and NNLO corrections lead to a further increase by +13%, a third of which results from the loop-induced gg contribution. For both processes the corrections exceed by far the perturbative uncertainties estimated by scale variations at lower orders. This is caused, in part, by the additional contribution from the gg component, which is not covered by NLO scale variations. The purely gluon-induced NLO corrections to the gg channel, which are part of a complete N^3LO calculation, have been computed in Refs. [115, 116].

Several leptonic channels originate from off-shell ZZ production. They involve the SF and DF four-lepton channels, 4ℓ and $2\ell 2\ell'$, respectively, which have been studied at NNLO QCD in Ref. [34]. On the other hand, one of the Z bosons may decay to two neutrinos instead. In that case the SF channel is defined as the one where the neutrino flavour matches the lepton flavour ($2\ell 2\nu$), while the DF flavour channel is defined as the one where the lepton and neutrino flavours are different ($2\ell 2\nu'$).⁴⁷ The SF $2\ell 2\nu$ final state is special since it receives contributions from both resonant ZZ and W^+W^- sub-topologies, which mix the two processes. From an experimental viewpoint, in the ZZ or W^+W^- analyses the two production mechanisms are isolated by using suitable cuts that enhance the respective process in its signal region. Since we include all resonant and non-resonant topologies leading to such final states, our computation of $2\ell 2\nu$ is applicable to both ZZ and W^+W^- studies by simply applying the corresponding cuts. NNLO cross sections for the $2\ell 2\nu$ and $2\ell 2\nu'$ channels are reported here for the first time. A detailed study of these processes will be presented elsewhere.

For the off-shell ZZ processes we use the setup of Ref. [34]: The renormalization and factorization scales are fixed to $\mu_0 = m_Z$. The fiducial cuts are summarized in Table 9. They involve standard transverse-momentum and rapidity thresholds for the leptons, and a lepton–lepton separation in R . In the $2\ell 2\ell'$ channel, the invariant mass of OSSF lepton pairs is required to be in a mass window around the Z peak. In the 4ℓ channel, there are two possible combinations of OSSF lepton pairs that can be associated with the par-

⁴⁶ We note again that $Z\gamma$ and $W\gamma$ are only used as shorthand notations here. The full amplitudes for the leptonic final states are used throughout without any approximation, including off-shell effects and spin correlations.

⁴⁷ We note that both final states contain an OSSF lepton pair and (possibly) missing transverse momentum from the two neutrinos that cannot be detected. Our distinction into SF and DF final states is motivated more by the underlying technical calculations than by their phenomenology in this case.

Table 9 Default setup of fiducial cuts for ZZ and ZZ/W⁺W⁻ production processes

	$pp \rightarrow e^- \mu^- e^+ \mu^+ / pp \rightarrow e^- e^- e^+ e^+$	$pp \rightarrow e^- e^+ \nu_e \bar{\nu}_e / pp \rightarrow e^- e^+ \nu_\mu \bar{\nu}_\mu$
Lepton cuts	$p_{T,\ell} > 7 \text{ GeV}, \eta_\ell < 2.7$ $66 \text{ GeV} < m_{\ell-\ell'} < 116 \text{ GeV}$	$p_{T,\ell} > 7 \text{ GeV}, \eta_\ell < 2.7$ $66 \text{ GeV} < m_{\ell-\ell'} < 116 \text{ GeV}$
Neutrino cuts	–	$p_T^{\text{miss}} > 30 \text{ GeV}$
Separation cuts	$\Delta R_{\ell\ell} > 0.2$	–
Jet definition	Anti- k_T algorithm with $R = 0.4$; $p_{T,j} > 25 \text{ GeV}, \eta_j < 4.5$	

Table 10 Default setup of fiducial cuts for W⁺W⁻ and W[±]Z production processes

	$pp \rightarrow e^- \mu^+ \nu_\mu \bar{\nu}_e$	$pp \rightarrow \ell'^{\pm} \nu_{\ell'} \ell^+ \ell^-$, $\ell, \ell' \in \{e, \mu\}$
Lepton cuts	$p_{T,\ell_1} > 25 \text{ GeV}, p_{T,\ell_2} > 20 \text{ GeV}$ $ \eta_\ell < 2.47, \eta_\ell \notin [1.37; 1.52]$ $ \eta_\mu < 2.4, m_{\ell-\ell'} > 10 \text{ GeV}$	$p_{T,\ell_z} > 15 \text{ GeV}, p_{T,\ell_w} > 20 \text{ GeV}$ $ \eta_\ell < 2.5$ $ m_{\ell_z \ell_z} - m_Z < 10 \text{ GeV}$
Neutrino cuts	$p_T^{\text{miss}} > 20 \text{ GeV}, p_T^{\text{miss,rel}} > 15 \text{ GeV}$	$m_{T,W} > 30 \text{ GeV}$
Separation cuts	$\Delta R_{\ell\ell} > 0.1$	$\Delta R_{\ell_z \ell_z} > 0.2, \Delta R_{\ell_z \ell_w} > 0.3$
Jet cuts	$N_{\text{jets}} = 0$	–
Jet definition	Anti- k_T algorithm with $R = 0.4$; $p_{T,j} > 25 \text{ GeV}, \eta_j < 4.5$	

ent Z bosons. We choose the combination which minimizes $|m_{\ell-\ell'} - m_Z| + |m_{\ell-\ell'} - m_Z|$, see Sect. 5.2.4.4 for details, and apply the invariant mass cuts only on the corresponding lepton pairs. Since no dedicated phenomenological studies of the $2\ell 2\nu/2\ell 2\nu'$ signatures at NNLO exist, we simply adopt the $2\ell 2\ell'$ setup, while removing the R separation of the leptons and adding a loose cut on the missing transverse energy of the neutrinos. This choice provides a generic benchmark scenario for these processes.

Comparing the SF 4ℓ process $pp \rightarrow e^- e^- e^+ e^+$ and the DF $2\ell 2\ell'$ process $pp \rightarrow e^- \mu^- e^+ \mu^+$ in Table 6, it is obvious that they give very similar results, taking into account the relative combinatorial factor of one-half in the SF channel (if the two SF channels $pp \rightarrow e^- e^- e^+ e^+$ and $pp \rightarrow \mu^- \mu^- \mu^+ \mu^+$ are added, DF and SF channels would be of the same size again). It is not surprising that the K factors for the $4\ell, 2\ell 2\ell'$ and $2\ell 2\nu'$ channels are very close, given the fact that very similar cuts are applied and that the dominant contribution results from resonant ZZ production in all these processes. The NLO corrections amount to roughly +50%, and the cross sections are increased by further $\sim +20\%$ at NNLO, i.e. radiative corrections in the fiducial regions are even a bit larger than for the inclusive ZZ cross section. For the 4ℓ and $2\ell 2\ell'$ channels, the loop-induced gg component has a slightly bigger impact ($\sim 57\%$ of the NNLO corrections) in the fiducial phase space than in the fully inclusive case ($\sim 53\%$), whereas it contributes a bit less for the $2\ell 2\nu'$ channel ($\sim 50\%$).

The SF $2\ell 2\nu$ channel, on the other hand, shows a rather different behaviour due to the large impact of its W^+W^- topologies, which are expected to dominate by about an order of magnitude due to the involved EW couplings and branching ratios. Under the quite loose cuts, compared to a dedi-

cated $ZZ \rightarrow \ell\ell\nu\nu$ selection, the cross section at LO is still about a factor of five larger than for the $2\ell 2\nu'$ process, due to the dominance of W^+W^- contributions. This cross section receives somewhat larger corrections than the “pure” ZZ processes, namely $K_{\text{NLO}} = 1.77$ and $K_{\text{NNLO}} = 1.18$, where the gg component contributes 33% of the NNLO corrections, comparable to on-shell W^+W^- production.

The off-shell W^+W^- process with DF leptons ($\ell\nu\ell'\nu'$), namely $pp \rightarrow e^- \mu^+ \nu_\mu \bar{\nu}_e$, has been studied at NNLO in Ref. [37]. We adopt the fixed scale choice of $\mu_0 = m_W$ and the fiducial cuts used in that study. The latter are summarized in Table 10: Besides standard cuts like transverse momentum thresholds, rapidity ranges and different isolation criteria, the selection cut with the largest impact on the size of higher-order corrections is a jet veto, which is required in W^+W^- analyses to suppress top-quark backgrounds. As a consequence of the jet veto, and in contrast to the inclusive W^+W^- cross section, the fiducial cross section receives very small radiative corrections, only +1.3% at NLO. The NNLO corrections amount to +12%, but they are almost entirely due to the loop-induced gg component. This component (at its leading order, which in terms of power counting belongs to the NNLO corrections of the complete process) has Born-level kinematics and is thus not affected by the jet veto, whereas real-radiation corrections are significantly suppressed. However, higher-order corrections to the gg contribution are affected by the jet veto, i.e. similar to the radiative corrections to the $q\bar{q}$ channel, they are significantly reduced with respect to an inclusive calculation. Hence, due to the suppression of radiative corrections by the jet veto, and the fact that no further new channels open up beyond NNLO, scale variations should provide a reasonable estimate of the uncertainties due to yet un-calculated higher-order QCD con-

tributions. The purely gluon-induced NLO corrections to the gg channel have been computed in Ref. [116].

With $W^\pm Z$ production [38, 39], the last diboson process has recently been computed at NNLO accuracy. Four different processes with three leptons and one neutrino are associated with $W^\pm Z$ production: $W^- Z$ and $W^+ Z$ production can each be split into a SF and a DF channel. Since these processes have charged final states, no loop-induced gg component contributes at NNLO. Following Ref. [39] we set $\mu_0 = (m_Z + m_W)/2$ for the central value of renormalization and factorization scales and use the fiducial cuts summarized in Table 10: The lepton transverse-momentum thresholds distinguish between leptons associated with the Z - and the W -boson decays. The lepton pair associated with the Z -boson decay is required to have an invariant mass close to the Z -boson mass, and the transverse mass of the W boson, defined through the lepton associated with the W -boson decay and the transverse missing-energy vector (see Appendix A), is restricted from below. Furthermore, leptons are required to be separated in R , where the separation depends on whether the respective leptons are both associated with the Z -boson decay or with the decays of two different heavy bosons. In the SF channel there is an ambiguity how to assign the leptons to the Z - and W -boson decays, and we follow the resonant-shape identification procedure of Ref. [107] (see also Sect. 5.2.4.9 for details). Since Ref. [39] uses the most recent input parameters corresponding to the default MATRIX settings, the 13 TeV results of the fiducial cross sections are exactly (within the numerical uncertainties) reproduced. Radiative corrections in that process are known to be large because of an approximate radiation zero [117] in the Born scattering amplitudes, which is broken beyond LO. We find $K_{\text{NLO}} = 2.05(1.97)$ and $K_{\text{NNLO}} = 1.11(1.11)$ for $W^- Z$ ($W^+ Z$), both for SF and DF channels. The $\sigma_{W^- Z}/\sigma_{W^+ Z}$ ratio is about 0.69, both at NLO and NNLO, i.e. slightly smaller than what is found for the $\sigma_{W^-}/\sigma_{W^+}$ ratio in the charged-current Drell–Yan process.

We conclude this section by discussing the performance of the code. In Table 11 we report the runtimes needed to obtain the LO, NLO and NNLO results of Table 6, converted to the time needed for a serial run on a single CPU core. The runtime estimates for achieving a statistical uncertainty of one permille, stated in the last column, facilitate a direct comparison among the various processes, and we find that the most time-consuming ones are those involving off-shell $V\gamma$ final states. We stress that the numerical uncertainties quoted in Table 11 are purely statistical: For processes featuring a large systematic uncertainty from the r_{cut} extrapolation, the choice of the (purely statistical) target accuracy should be adapted to the size of the systematic uncertainties, where the latter can be reduced by setting `switch_qT_accuracy = 1`.

7 Systematic uncertainties of q_T subtraction

As pointed out before, NLO and NNLO cross sections computed with the q_T -subtraction formalism exhibit a residual dependence on the cut-off r_{cut} in the slicing parameter $r = q_T/M$, where q_T is the transverse momentum and M the mass of the colourless system. This residual dependence is due to power-suppressed terms, which are left after the subtraction of the IR singular contribution at finite values of r_{cut} and vanish only in the limit $r_{\text{cut}} \rightarrow 0$. The r_{cut} dependence of the cross sections computed with the q_T -subtraction method has been discussed in some detail for the $W^\pm\gamma$, off-shell W^+W^- and off-shell $W^\pm Z$ production processes in Refs. [31, 37, 39], to which we refer the reader interested in these specific processes. In the following, we study the systematic uncertainties of our results for a representative set of processes available in MATRIX, using the corresponding default setup of each process.

MATRIX performs an extrapolation $r_{\text{cut}} \rightarrow 0$ for total rates computed by means of the q_T -subtraction procedure, i.e. at NNLO, and possibly at NLO if the q_T -subtraction method is applied. A conservative estimate of the extrapolation uncertainty is included in the numerical error of this extrapolated result, which is considered our best prediction at the corresponding perturbative order and printed on screen at the end of each run. To perform the extrapolation, MATRIX automatically computes the cross section at fixed values of r_{cut} in the interval $[r_{\text{cut}}^{\text{min}}; 1\%]$ using steps of 0.01%. Unless stated otherwise (see the process-specific information in Sect. 5.2), the default value MATRIX uses is $r_{\text{cut}}^{\text{min}} = 0.15\%$. The extrapolation procedure, which is discussed below, has been tested to work extremely well at NLO, where r_{cut} -independent results are available. Note that already the cross section at the lowest calculated value $r_{\text{cut}}^{\text{min}} = 0.15\%$ (actually also for higher r_{cut} values up to at least $r_{\text{cut}} \sim 1\%$) provides a very reasonable prediction in cases where the r_{cut} dependence is small, and thus the result at $r_{\text{cut}}^{\text{min}}$ is also printed on screen at the end of each run. A comparison of the extrapolated cross section and the result at the fixed value $r_{\text{cut}}^{\text{min}}$ indicates at which level of accuracy the fixed- r_{cut} result can be trusted: In case of a significant r_{cut} dependence of the total rate, we recommend to correct the kinematic distributions by the ratio $\sigma_{\text{NNLO}}^{\text{extrapolated}}/\sigma_{\text{NNLO}}^{r_{\text{cut}}}$. In the first release of MATRIX, distributions are indeed always calculated at $r_{\text{cut}} = r_{\text{cut}}^{\text{min}}$. We note that such reweighting should not be applied to distributions that are trivial at LO: For example, the transverse-momentum of the colourless system vanishes at LO, and its high- p_T region is not affected by a finite r_{cut} value. Given that we have not observed any significant r_{cut} dependence of our NNLO results for kinematic distributions in various dedicated studies, where we have performed the extrapolation on a bin-by-bin basis (see, e.g., Ref. [39]), we consider

Table 11 MATRIX runtime for integrated cross-section results in Table 6. The relative uncertainty is entirely due to the numerical phase space integration. The runtimes correspond to the total time required for the production phase (*pre-run* and *main-run*) of the respective MATRIX runs if it was performed on a single CPU core. Automatic scale variations, r_{cut} extrapolation and the computation of distributions has been included in these runs

Process ($\{\text{process_id}\}$)	LO runtime (relative uncertainty)	NLO runtime (relative uncertainty)	NNLO runtime (relative uncertainty)	NNLO runtime estimate for 10^{-3} uncertainty
$pp \rightarrow H$ (pph21)	0d 0h 2min (1.5×10^{-4})	0d 0h 12min (2.7×10^{-4})	35d 23h 23min (7.2×10^{-4})	19d
$pp \rightarrow Z$ (ppz01)	0d 0h 10min (8.2×10^{-5})	0d 0h 16min (2.6×10^{-4})	53d 15h 31min (4.6×10^{-4})	11d
$pp \rightarrow W^-$ (ppw01)	0d 0h 7min (8.1×10^{-5})	0d 0h 22min (2.6×10^{-4})	50d 17h 29min (4.4×10^{-4})	10d
$pp \rightarrow W^+$ (ppwx01)	0d 0h 14min (8.1×10^{-5})	0d 0h 24min (2.6×10^{-4})	47d 7h 46min (4.9×10^{-4})	11d
$pp \rightarrow e^-e^+$ (ppeex02)	0d 0h 48min (1.0×10^{-4})	0d 2h 24min (2.8×10^{-4})	173d 20h 36min (3.6×10^{-4})	22d
$pp \rightarrow \nu_e\bar{\nu}_e$ (ppnenex02)	0d 1h 31min (8.2×10^{-5})	0d 1h 0min (2.5×10^{-4})	89d 18h 17min (4.5×10^{-4})	18d
$pp \rightarrow e^-\bar{\nu}_e$ (ppenex02)	0d 1h 46min (8.7×10^{-5})	0d 5h 21min (2.2×10^{-4})	114d 2h 18min (4.3×10^{-4})	21d
$pp \rightarrow e^+\nu_e$ (ppexne02)	0d 1h 56min (8.5×10^{-5})	0d 3h 43min (2.6×10^{-4})	114d 6h 18min (4.6×10^{-4})	24d
$pp \rightarrow \gamma\gamma$ (ppaa02)	0d 1h 13min (9.8×10^{-5})	0d 4h 11min (2.8×10^{-4})	27d 17h 7min (4.6×10^{-4})	6d
$pp \rightarrow e^-e^+\gamma$ (ppeexa03)	0d 17h 55min (9.2×10^{-5})	1d 19h 48min (2.8×10^{-4})	1276d 12h 47min (3.6×10^{-4})	167d
$pp \rightarrow \nu_e\bar{\nu}_e\gamma$ (ppnenexa03)	0d 2h 50min (8.7×10^{-5})	0d 8h 59min (2.5×10^{-4})	75d 9h 6min (4.7×10^{-4})	17d
$pp \rightarrow e^-\bar{\nu}_e\gamma$ (ppenexa03)	0d 22h 18min (1.0×10^{-4})	3d 16h 59min (3.2×10^{-4})	1484d 16h 50min (4.0×10^{-4})	232d
$pp \rightarrow e^+\nu_e\gamma$ (ppexnea03)	1d 7h 8min (9.6×10^{-5})	6d 8h 7min (3.0×10^{-4})	428d 7h 1min (1.0×10^{-3})	443d
$pp \rightarrow ZZ$ (ppzz02)	0d 1h 44min (8.2×10^{-5})	0d 1h 6min (2.4×10^{-4})	132d 19h 37min (4.4×10^{-4})	25d
$pp \rightarrow W^+W^-$ (ppwxw02)	0d 1h 23min (8.2×10^{-5})	0d 0h 48min (2.5×10^{-4})	69d 20h 49min (4.3×10^{-4})	13d
$pp \rightarrow e^-\mu^-e^+\mu^+$ (ppemexmx04)	0d 5h 43min (8.2×10^{-5})	0d 4h 32min (2.7×10^{-4})	219d 16h 33min (4.5×10^{-4})	45d
$pp \rightarrow e^-e^-e^+e^+$ (ppeexex04)	0d 11h 34min (9.0×10^{-5})	0d 12h 8min (3.4×10^{-4})	742d 13h 37min (5.1×10^{-4})	193d
$pp \rightarrow e^-e^+\nu_\mu\bar{\nu}_\mu$ (ppeexnmnm04)	0d 6h 33min (9.4×10^{-5})	0d 6h 36min (2.7×10^{-4})	158d 13h 40min (4.4×10^{-4})	31d
$pp \rightarrow e^-\mu^+\nu_\mu\bar{\nu}_e$ (ppemxnmn04)	0d 13h 33min (9.2×10^{-5})	1d 22h 9min (2.7×10^{-4})	521d 2h 20min (4.8×10^{-4})	119d
$pp \rightarrow e^-e^+\nu_e\bar{\nu}_e$ (ppeexnenex04)	0d 23h 36min (8.2×10^{-5})	0d 17h 46min (4.8×10^{-4})	270d 6h 59min (4.4×10^{-4})	52d
$pp \rightarrow e^-\mu^-e^+\bar{\nu}_\mu$ (ppemexnm04)	0d 5h 18min (1.0×10^{-4})	0d 5h 15min (2.9×10^{-4})	104d 16h 46min (4.3×10^{-4})	19d

Table 11 continued

Process ($\{\text{process_id}\}$)	LO runtime (relative uncertainty)	NLO runtime (relative uncertainty)	NNLO runtime (relative uncertainty)	NNLO runtime estimate for 10^{-3} uncertainty
$pp \rightarrow e^-e^-e^+\bar{\nu}_e$ (ppeeexnex04)	0d 14h 19min (8.3×10^{-5})	0d 14h 56min (2.7×10^{-4})	179d 14h 6min (4.7×10^{-4})	39d
$pp \rightarrow e^-e^+\mu^+\nu_\mu$ (ppeeexmxnm04)	0d 10h 32min (8.1×10^{-5})	0d 8h 18min (2.6×10^{-4})	104d 17h 58min (4.5×10^{-4})	21d
$pp \rightarrow e^-e^+e^+\nu_e$ (ppeeexexne04)	0d 9h 19min (1.0×10^{-4})	0d 13h 11min (4.6×10^{-4})	167d 6h 49min (5.1×10^{-4})	44d

this reweighting procedure sufficiently accurate⁴⁸, and leave a proper extrapolation procedure of distributions for a future update of MATRIX.

The $r_{\text{cut}} \rightarrow 0$ extrapolation of the cross section is obtained using a simple quadratic least χ^2 fit. Such fit is repeated varying the upper bound of the fit interval, starting from a minimum upper bound of 0.5% (0.25% for dilepton production or processes involving photons with $r_{\text{cut}}^{\text{min}} = 0.15\%$; 0.15% for the same processes with $r_{\text{cut}}^{\text{min}} = 0.05\%$), and the result with the lowest $\chi^2/\text{degrees-of-freedom}$ value is kept as the best fit. The extrapolation uncertainty is determined by comparing the result of the best fit with the results obtained by variations of the upper bound of the fit interval. To be conservative, a lower bound on this uncertainty is introduced, corresponding to half of the difference between the $r_{\text{cut}} \rightarrow 0$ result and the cross section at $r_{\text{cut}}^{\text{min}}$. This extrapolation error is combined quadratically with the numerical error, which is determined by extrapolating also statistical errors at finite r_{cut} values to $r_{\text{cut}} = 0$.

Our results for the r_{cut} dependence of a representative set of processes are shown in Fig. 2. Before commenting the various plots we provide some general explanation. The central values of the green bars represent the NNLO cross section calculated at the respective fixed r_{cut} values, $r_{\text{cut}} \in [0.01\%; 1\%]$ in steps of 0.01%, and their sizes denote the numerical uncertainties. Our reference prediction, computed with the default MATRIX setup, is the $r_{\text{cut}} \rightarrow 0$ extrapolation obtained from the values $r_{\text{cut}} \geq 0.15\%$, shown as a blue solid line. A vertical blue dotted line at $r_{\text{cut}} = 0.15\%$ indicates the lowest value used for this extrapolation. The blue uncertainty band is obtained by combining the numerical and extrapolation uncertainties and corresponds to the on-screen output of MATRIX. When the r_{cut} dependence is strong, we also show the MATRIX result extrapolated from $r_{\text{cut}} \geq 0.05\%$ values as a red solid line with a red band, with its uncertainty

⁴⁸ We note that in the region close to kinematical boundaries the r_{cut} dependence of the NNLO results is expected to be amplified by the presence of perturbative instabilities of Sudakov type [118]. In such regions, however, the predictivity of fixed-order computations is limited, and a resummation of the logarithmically enhanced contributions would be required.

computed analogously to the blue band. Where available, NNLO results obtained either from analytical calculations or from alternative NNLO numerical programs are reported as black lines, while the grey band shows their numerical integration error. All the results are reported as relative deviations from the reference prediction in percent.

We start our discussion from the first two plots in Fig. 2, which refer to the inclusive on-shell production of a Higgs (left) and a Z boson (right), respectively. In both cases the NNLO cross sections turn out to be extremely stable with respect to r_{cut} : Almost all fixed- r_{cut} results deviate by less than one permille from the default $r_{\text{cut}} \rightarrow 0$ prediction, and all fixed- r_{cut} results are compatible with the extrapolated result within their numerical uncertainties. The high stability with respect to r_{cut} in these cases would justify choosing essentially any r_{cut} value in the given range to provide a reasonable prediction for the NNLO cross section. Our default choice to use $r_{\text{cut}} \geq 0.15\%$ to obtain the $r_{\text{cut}} \rightarrow 0$ extrapolation appears to be a sound compromise between a sufficiently low r_{cut} value and a good numerical convergence. The blue band constitutes a reasonable estimate of the remaining extrapolation uncertainty of our reference result. Since no cuts have been applied, our results can be compared with available analytic computations of the inclusive Higgs and Z production cross sections. Such results are obtained with SUSHI [110] for Higgs boson production, and with ZWPROD [2,3] for Z-boson production, and are reported in Fig. 2 by the black solid lines with grey numerical error bands. The agreement is excellent and confirms that with MATRIX we control these computations at the subpermille level.

The next process we consider is $pp \rightarrow e^+\nu_e$ via an off-shell W^+ boson (third plot in Fig. 2). The r_{cut} dependence is similar to the case of on-shell Higgs and Z production with all fixed- r_{cut} results deviating not more than about one permille from the extrapolated result. We therefore conclude that the stability fully justifies our reference prediction and that its blue uncertainty band, which is slightly larger than for the on-shell processes discussed before, gives a reasonable estimate of the uncertainty due to the r_{cut} dependence of the cross

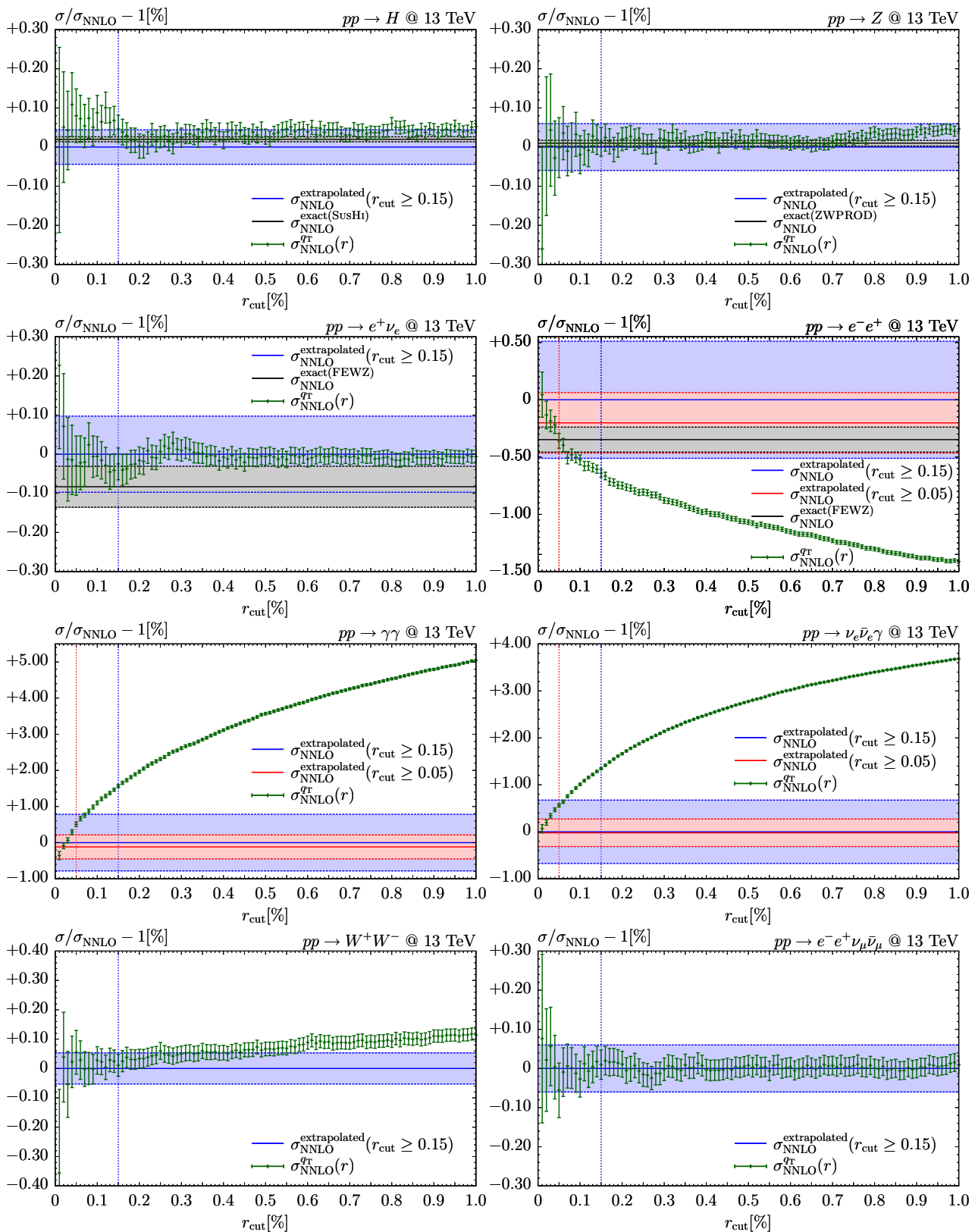


Fig. 2 Dependence of the NNLO cross sections on r_{cut} for various processes. The NNLO results at fixed values of r_{cut} are normalized to the $r_{\text{cut}} \rightarrow 0$ extrapolation obtained by using $r_{\text{cut}} \geq 0.15\%$. The blue band represents the combined numerical and extrapolation uncertainty.

For processes with a large r_{cut} dependence, the extrapolated result and uncertainty obtained by using $r_{\text{cut}} \geq 0.05\%$ is shown in red. Where available, r_{cut} -independent reference results are black

section. In the same plot we also report the result obtained with FEWZ [53], depicted by a solid black line with grey error bands. The MATRIX and FEWZ results are fully consistent within the respective numerical uncertainties. A similar level of agreement is obtained with the program NNLOJET [119].⁴⁹ Since both FEWZ and NNLOJET are based on fully independent subtraction schemes, the above agreement can be considered as an important mutual consistency check of the three NNLO calculations.

Next, we discuss the dilepton production process $pp \rightarrow e^-e^+$, which, in our default setup, exhibits a rather large r_{cut} dependence. This is illustrated in the fourth plot of Fig. 2. As discussed in Sect. 6, the strong r_{cut} dependence can be traced back to the presence of perturbative instabilities [111] affecting the fixed-order computation in the case of symmetric p_T cuts. We have explicitly tested that if we change our default setup from $p_{T,\ell} > 25 \text{ GeV}$ to $p_{T,e^-} > 25 \text{ GeV}$ and $p_{T,e^+} > 24 \text{ GeV}$, we get a stable r_{cut} dependence. If we change this setup by letting the cut on p_{T,e^+} approach 25 GeV , the r_{cut} dependence of the cross section becomes increasingly stronger. We also point out that, if we remove the lepton p_T thresholds completely or choose them as small as $p_{T,\ell} > 5 \text{ GeV}$, we obtain a flat r_{cut} dependence of the cross section. The sizeable r_{cut} dependence implies a larger uncertainty in the $r_{\text{cut}} \rightarrow 0$ extrapolation. We indeed see that by using the default setup the estimated uncertainty, represented by the blue band, is about $\pm 0.5\%$. By reducing the minimum r_{cut} value to 0.05% , we reduce the extrapolation uncertainty by about a factor of 2 (red band) and we obtain a fully consistent result with the one obtained from $r_{\text{cut}} \geq 0.15\%$. This is a strong indication that the extrapolation procedure is robust and provides a reasonable estimate of the ensuing uncertainty. In the same plot we report the result obtained with FEWZ: the agreement with the extrapolated results is excellent. A similar level of agreement is obtained with NNLOJET. As in the previous cases, the agreement of NNLO predictions obtained with fully independent methods confirms the robustness of the results that can be obtained with MATRIX. We remark that this conclusion holds also in a case, like the one of dilepton production with symmetric cuts, in which a fixed-order computation is challenged.

In terms of the r_{cut} dependence of their cross sections, processes with an isolated photon in the final state suffer from large power-suppressed corrections. Since the case of $W\gamma$ production was discussed in Ref. [31], here we consider diphoton and $Z\gamma$ production with the Z boson decaying to a neutrino pair. The corresponding results are shown in the fifth

and sixth plot in Fig. 2, respectively. Looking at our extrapolated reference results for $r_{\text{cut}} \geq 0.15\%$ and $r_{\text{cut}} \geq 0.05\%$, we see that they are nicely consistent with the behaviour of the numerical results below the respective minimal r_{cut} value and that they are in neat mutual agreement. In particular, the result at the lowest r_{cut} value $r_{\text{cut}} = 0.01\%$ is consistent with both the red and blue bands in all cases.

It is clear that, for dilepton, diphoton and $Z\gamma$ production, the extrapolation $r_{\text{cut}} \rightarrow 0$ of runs with $r_{\text{cut}} \geq 0.15\%$ allows us to control the uncertainty of our NNLO predictions at the $0.5\text{--}1\%$ level. If the minimal r_{cut} value is decreased to $r_{\text{cut}}^{\text{min}} = 0.05\%$, the ensuing uncertainty is reduced to few permille. We have explicitly checked that this picture is common to all processes involving photons. We conclude that, taking into account the estimated r_{cut} uncertainties, we obtain consistent predictions for all these processes.

The last two plots in Fig. 2 are representative r_{cut} -dependence plots for on- and off-shell diboson production: The first one shows on-shell W^+W^- production, and the second one off-shell ZZ production in the $2\ell 2\nu'$ decay channel. These plots feature to a large extent the same behaviour as observed for on-shell Higgs and vector-boson production processes: In general, the NNLO cross section is very stable with respect to r_{cut} over two orders of magnitude. The r_{cut} dependence of the W^+W^- cross section seems to have a very slight slope, which, however, is perfectly modelled by the extrapolation. Our default choice of the minimal r_{cut} value leads to a reasonable reference result with the estimated uncertainties being meaningful and in some cases even a bit conservative.

In summary, for most of the processes implemented in the first release of MATRIX, NNLO predictions can generally be controlled at the one permille level (or better). For processes with a large r_{cut} dependence like those involving photons or Drell–Yan dilepton pairs, fiducial cross sections can be computed with uncertainties of few permille by using the setting `switch_qT_accuracy = 1`. This accuracy should be sufficient for all practical purposes.

8 Summary

In this paper we have introduced the new computational framework MATRIX [1], which allows a user to produce NNLO QCD predictions for a wide class of hadron-collider processes. Using the q_T -subtraction formalism, our computations are fully differential in the phase space of the final-state particles and of the associated QCD radiation, thereby enabling the evaluation of arbitrary IR safe observables. Since our implementation is completely general, it is applicable to the computation of NNLO corrections to any process with colourless final states. The list of available processes is therefore limited only by the availability of two-loop ampli-

⁴⁹ Note that we have set the CKM matrix to unity here, see Sect. 5.1.2, in order to be able to compare against the results of NNLOJET. The CKM input does not have any impact on the r_{cut} dependence beyond statistical uncertainties, which is why the discussion above is valid irrespective of the chosen CKM settings.

tudes for the Born-level processes. The first MATRIX release involves $2 \rightarrow 1$ and $2 \rightarrow 2$ hadronic reactions with Higgs and vector bosons in the final state. In particular, we consider final states with two, three and four leptons (plus missing energy) from the decays of the vector bosons, and we account for all resonant and non-resonant diagrams with off-shell effects and spin correlations. This enables the evaluation of cross sections with realistic cuts to define any fiducial volume.

We have presented a detailed description of the first release of the MATRIX code. Besides the theoretical framework and the tools MATRIX is based on, we have focused on the technical aspects relevant for a user to produce fully differential NNLO results. MATRIX features automatic compilation and running through dedicated scripts. The most popular clusters are preconfigured and can be simply selected by the user. Having specified a target precision and a desired runtime per job, the code automatically determines the required parallelization in each run. In combination with the fast numerical multi-channel integration offered by MUNICH, this allows us to obtain accurate NNLO results even for the most complicated of the available processes on a middle-sized cluster in less than a couple of days, simpler processes being significantly faster. With every run MATRIX provides not only the central prediction, but automatically evaluates the effect of independent factorization- and renormalization-scale variations in order to obtain an estimate of the perturbative uncertainties at each order. Furthermore, by simultaneously computing NNLO cross sections at several values of the q_T -subtraction parameter r_{cut} , MATRIX performs an extrapolation $r_{\text{cut}} \rightarrow 0$ of the integrated cross section in order to provide its final prediction that includes an extrapolation uncertainty. Such procedure allows us to offer a robust estimate of the systematic uncertainty due to the q_T -subtraction procedure. Both scale variations and the r_{cut} extrapolation procedure are fully automated within MATRIX without the need of extra computing power.

In particular for processes with a large r_{cut} dependence, such as dilepton production or processes with isolated photons, MATRIX is able to significantly improve over predictions computed at fixed r_{cut} values by performing the $r_{\text{cut}} \rightarrow 0$ extrapolation. Besides an improved accuracy in the central prediction, our procedure includes a conservative estimate of systematic uncertainties, which allows the user to control the precision of these processes at the level of few permille, when using corresponding settings.

We have discussed in detail all relevant MATRIX input cards accessible to the user. Besides standard settings applicable to all processes, information specific to each individual process has been provided, such as suitable dynamic scales which are predefined for certain processes and process-specific cuts. The latter facilitate the restriction of the phase space to fiducial volumes as defined by the LHC experiments.

In combination with a general way to define distributions, this enables the possibility to compute fiducial cross sections and distributions that can be directly compared to unfolded experimental data.

Reference predictions for the integrated cross sections of all processes available in MATRIX have been provided at LO, NLO and NNLO in the default setups. For the NNLO cross section we have quoted predictions for a fixed value $r_{\text{cut}} = 0.15\%$ and the final NNLO result after performing the extrapolation $r_{\text{cut}} \rightarrow 0$. We have studied the impact of radiative corrections for each of these processes as well as the impact of the loop-induced gg component, where applicable. The impact of NLO and NNLO QCD corrections is generally large. While NLO corrections typically range between 30 and 100%, NNLO corrections are still as large as 3–30% for the processes and scenarios we have considered. The size of radiative corrections is typically widely un-affected if only fiducial cuts for particle identification, like transverse-momentum thresholds, geometric (pseudo-)rapidity ranges or isolation cuts are applied (see, e.g., inclusive on-shell ZZ production and off-shell $ZZ \rightarrow 4\ell$ production in a ZZ signal region). This is in general no longer true if the considered cuts modify the dominant resonance structures (e.g. $ZZ \rightarrow 4\ell$ production in the $H \rightarrow ZZ$ background region). If real radiation is restricted, in particular by a veto against jets, the size of higher-order corrections is strongly suppressed, and NLO and NNLO K factors can be very different as compared to the inclusive phase-space (see, e.g., inclusive on-shell W^+W^- production and off-shell $WW \rightarrow 2\ell 2\nu$ production, which requires a jet veto to suppress the top-quark backgrounds).

Scale variations tend to underestimate the uncertainty from missing higher-order contributions at LO, and also widely at NLO. This is due to the fact that vector-boson and vector-boson pair production processes are driven by $q\bar{q}$ initial states at LO (gg initial states in case of Higgs boson production). The gq channel opens up only at NLO, and NNLO is the first order where all partonic channels are contributing. As a consequence, in most of the cases NNLO uncertainties obtained through scale variations should provide the correct order of magnitude of yet un-calculated perturbative QCD contributions. When NNLO corrections are particularly large, as in the case of diphoton production, a more conservative estimate of missing higher-order contributions can be obtained by considering the difference with the previous order.

All the vector-boson pair production processes with an electrically neutral final state include a loop-induced gg contribution at NNLO. Its size strongly depends on the considered process and can range between roughly 10% and 60% of the NNLO corrections. In cases where radiative corrections are suppressed by a jet veto, since the gg component is not affected due to its Born-level kinematics, it may provide the dominant NNLO contribution. As the gg component is

effectively only LO accurate, scale variations might underestimate the actual size of its missing perturbative corrections in some cases.

To conclude, we believe that the numerical tool presented in this paper will be highly valuable for the high-energy community. Several experimental studies have already used the results obtained with MATRIX for data–theory comparison in SM measurements (see, e.g., Refs. [107, 120–138]) and for background estimates in various new-physics searches. MATRIX [1] can be used to produce benchmark predictions for a wide range of processes relevant both for SM measurements and as backgrounds to Higgs and new-physics searches. Extensions of the code to include additional processes, the inclusion of further perturbative contributions (e.g. NLO corrections to the gg channel or EW corrections) as well as the resummation of certain classes of logarithmic contributions are left for future work.

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Appendix A Predefined cuts

In this Appendix the process-dependent cuts introduced in Sect. 5.2 are explained in more detail. It can be used as a dictionary since the respective cuts in Sect. 5.2 contain interactive links to their explanations in Table 12.

Appendix B Modifications of the C++ code (advanced user)

The user is generally advised to contact the authors if he/she is interested in changing any parts of the C++ code in order to define new dynamic scales, fiducial cuts or distributions. Below we provide some general guidance on how such implementations can be realized in the C++ code. Any changes of the C++ code require recompilation of the relevant process. This can be done with the `matrix` script, but in certain cases it might be simpler to use directly the `Makefile` the `matrix` script has created during the initial compilation of a process with ID `process_id`, by typing

```
$ make process_id
```

This enables recompilation without cleaning the whole process and without checking again whether all the relevant libraries are correctly installed.

B.1 General C++ commands

B.1.1 Access to particle groups

In the C++ routines for the user-defined scales and cuts one has access to all particle groups listed in Fig. 3 and the ones defined by the user, see below. As discussed before, the particle groups are ordered in the transverse momentum of the particles and can be accessed via `PARTICLE("particle_group")[index]`, where `particle_group` is one of the particle groups defined in Table 3 or the user-defined ones, and `index` indicates the position in the p_T -ordering of the group starting from the hardest one at `index = 0`.

For example, the hardest lepton can be accessed via

```
particle hardest_lepton = PARTICLE("lep")[0];
```

The particle class itself has various predefined class variables that can be directly used. For example, the p_T or squared invariant mass can be determined as follows:

```
double pT_hardest_lepton = PARTICLE("lep")[0].pT;
double m2_hardest_lepton = PARTICLE("lep")[0].m2;
```

These can also be determined via the full four-vector that has certain predefined functions and can be used as follows:

```
fourvector fourvector_of_hardest_lepton = PARTICLE("lep")
[0].momentum;
double pT_hardest_lepton = fourvector_of_hardest_lepton.
pT();
double m2_hardest_lepton = fourvector_of_hardest_lepton.
m2();
```

or similar functions for other observables, such as rapidity and pseudo-rapidity

```
double y_hardest_lepton = PARTICLE("lep")[0].momentum.
rapidity();
double eta_hardest_lepton = PARTICLE("lep")[0].momentum.
eta();
```


Table 12 Explanations of the pre-defined cuts available in the various MATRIX processes. See Sect. 5.2 for which cuts belong to which process

user_switch user_cut	Description
lepton_identification	Switch to change between different identification procedures of Z and W bosons in the same-flavour channels of ZZ and WZ production. See Sects. 5.2.4.4 and 5.2.4.9 for details.
M_leplep	Switch for cuts on invariant mass $m_{\ell\ell}$ of all possible lepton pairs
min_M_leplep	Minimal requirement $m_{\ell\ell} > \text{min_M_leplep}$ for all lepton pairs
max_M_leplep	Maximal requirement $m_{\ell\ell} < \text{max_M_leplep}$ for all lepton pairs
M_leplep_OSSF	Switch for cuts on invariant mass $m_{\ell-\ell^+}$ of opposite-sign, same-flavour (OSSF) lepton pairs
min_M_leplep_OSSF	Minimal requirement $m_{\ell-\ell^+} > \text{min_M_leplep_OSSF}$ for OSSF pairs
max_M_leplep_OSSF	Maximal requirement $m_{\ell-\ell^+} < \text{max_M_leplep_OSSF}$ for OSSF pairs
min_M_Z1_OSSF	Minimal requirement $m_{\ell-\ell^+} > \text{min_M_Z1_OSSF}$ for OSSF pair closer to m_Z
max_M_Z1_OSSF	Maximal requirement $m_{\ell-\ell^+} < \text{max_M_Z1_OSSF}$ for OSSF pair closer to m_Z
M_Zrec	Switch for cuts on invariant mass $m_{\ell-\ell^+}$ of lepton pairs associated with Z bosons
min_M_Zrec	Minimal requirement $m_{\ell-\ell^+} > \text{min_M_Zrec}$ for (reconstructed) Z bosons
max_M_Zrec	Maximal requirement $m_{\ell-\ell^+} < \text{max_M_Zrec}$ for (reconstructed) Z bosons
delta_M_Zrec_MZ	Switch for cuts on absolute difference between invariant mass $m_{\ell-\ell^+}$ of lepton pairs associated with Z bosons and the Z -boson mass
max_delta_M_Zrec_MZ	Maximal requirement $ m_{\ell-\ell^+} - m_Z < \text{max_delta_M_Zrec_MZ}$ for (reconstructed) Z bosons
delta_M_lepleplep_MZ	Switch for cuts on absolute difference between invariant mass $m_{\ell\ell\ell}$ of 3-lepton system and the Z -boson mass
min_delta_M_lepleplep_MZ	Minimal requirement $ m_{\ell\ell\ell} - m_Z > \text{min_delta_M_lepleplep_MZ}$
M_4lep	Switch for cuts on invariant mass $m_{\ell\ell\ell\ell}$ of 4-lepton system
min_M_4lep	Minimal requirement $m_{\ell\ell\ell\ell} > \text{min_M_4lep}$ for 4-lepton system
max_M_4lep	Maximal requirement $m_{\ell\ell\ell\ell} < \text{max_M_4lep}$ for 4-lepton system
min_delta_M_4lep	Minimal requirement $ m_{\ell\ell\ell\ell} - m_Z > \text{min_delta_M_4lep}$ for 4-lepton system
max_delta_M_4lep	Maximal requirement $ m_{\ell\ell\ell\ell} - m_Z < \text{max_delta_M_4lep}$ for 4-lepton system
M_leplepnunu	Switch for cuts on invariant mass $m_{\ell\ell\nu\nu}$ of 2-lepton–2-neutrino system
min_M_leplepnunu	Minimal requirement $m_{\ell\ell\nu\nu} > \text{min_delta_M_leplepnunu}$ for $2\ell 2\nu$ system
max_M_leplepnunu	Maximal requirement $m_{\ell\ell\nu\nu} < \text{max_delta_M_leplepnunu}$ for $2\ell 2\nu$ system
min_delta_M_leplepnunu	Min. requirement $ m_{\ell\ell\nu\nu} - m_Z > \text{min_delta_M_leplepnunu}$ for $2\ell 2\nu$ system
max_delta_M_leplepnunu	Max. requirement $ m_{\ell\ell\nu\nu} - m_Z < \text{max_delta_M_leplepnunu}$ for $2\ell 2\nu$ system
pT_leplep	Switch for cuts on transverse momentum of lepton pair $p_{T,\ell\ell}$
min_pT_leplep	Minimal requirement $p_{T,\ell\ell} > \text{min_pT_leplep}$ for lepton pair
pT_lep_1st	Switch for cuts on transverse momentum of hardest lepton p_{T,ℓ_1}
min_pT_lep_1st	Minimal requirement $p_{T,\ell_1} > \text{min_pT_lep_1st}$ for hardest lepton
pT_lep_2nd	Switch for cuts on transverse momentum of second-hardest lepton p_{T,ℓ_2}
min_pT_lep_2nd	Minimal requirement $p_{T,\ell_2} > \text{min_pT_lep_2nd}$ for second-hardest lepton

Table 12 continued

user_switch user_cut	Description
lepton_cuts min_pT_lep_1st min_pT_lep_2nd	Switch for cuts on transverse momentum of (second-)hardest lepton $p_{T,\ell_1}(p_{T,\ell_2})$ Minimal requirement $p_{T,\ell_1} > \text{min_pT_lep_1st}$ for hardest lepton Minimal requirement $p_{T,\ell_2} > \text{min_pT_lep_2nd}$ for second-hardest lepton
leading_lepton_cuts min_pT_1st_if_e min_pT_1st_if_mu	Switch for flavour-dependent cuts on hardest-lepton transverse momentum p_{T,ℓ_1} Minimal requirement $p_{T,\ell_1} > \text{min_pT_1st_if_e}$ if hardest lepton is electron Minimal requirement $p_{T,\ell_1} > \text{min_pT_1st_if_mu}$ if hardest lepton is muon
lepZ_cuts min_pT_lepZ_1st min_pT_lepZ_2nd	Switch for cuts on transverse momentum of (second-)hardest lepton associated with Z-boson decay $p_{T,\ell_{Z,1}}(p_{T,\ell_{Z,2}})$ Minimal requirement $p_{T,\ell_{Z,1}} > \text{min_pT_lepZ_1st}$ for hardest lepton of Z Minimal requirement $p_{T,\ell_{Z,2}} > \text{min_pT_lepZ_2nd}$ for second-hardest lepton of Z
lepW_cuts min_pT_lepW max_eta_lepW	Switch for cuts on lepton associated with W-boson decay Minimal requirement $p_{T,\ell_W} > \text{min_pT_lepW}$ for lepton from W-boson decay Minimal requirement $\eta_{\ell_W} < \text{max_eta_lepW}$ for lepton from W-boson decay
R_leplep min_R_leplep	Switch for cuts on lepton separation in $\Delta R_{\ell\ell} = \sqrt{\Delta y_{\ell\ell}^2 + \Delta\phi_{\ell\ell}^2}$ Minimal requirement $\Delta R_{\ell\ell} > \text{min_R_leplep}$ for all lepton pairs
R_lepZlepZ min_R_lepZlepZ	Switch for cuts on separation between leptons associated with Z-boson decay in $\Delta R_{\ell_Z\ell_Z} = \sqrt{\Delta y_{\ell_Z\ell_Z}^2 + \Delta\phi_{\ell_Z\ell_Z}^2}$ Minimal requirement $\Delta R_{\ell_Z\ell_Z} > \text{min_R_lepZlepZ}$ for leptons of Z decay
R_lepZlepW min_R_lepZlepW	Switch for cuts on separation between leptons associated with Z-boson decay and lepton associated with W-boson decay in $\Delta R_{\ell_Z\ell_W} = \sqrt{\Delta y_{\ell_Z\ell_W}^2 + \Delta\phi_{\ell_Z\ell_W}^2}$ Minimal requirement $\Delta R_{\ell_Z\ell_W} > \text{min_R_lepZlepW}$ for leptons of Z and W decay
phi_leplep min_phi_leplep	Switch for cuts on azimuthal separation $\Delta\phi_{\ell\ell}$ between all lepton pairs Minimal requirement $\Delta\phi_{\ell\ell} > \text{min_phi_leplep}$ for all lepton pairs
phi_leplep_nunu min_phi_leplep_nunu	Switch for cuts on azimuthal separation $\Delta\phi_{\ell\ell,\nu\nu}$ between the transverse-momentum vectors of the 2-lepton system $\mathbf{p}_{T,\ell\ell}$ and the missing energy $\mathbf{p}_T^{\text{miss}}$ Minimal requirement $\Delta\phi_{\ell\ell,\nu\nu} > \text{min_phi_leplep_nunu}$
electron_cuts min_pT_e_1st min_pT_e_2nd	Switch for cuts on transverse momentum of (second-)hardest electron $p_{T,e_1}(p_{T,e_2})$ Minimal requirement $p_{T,e_1} > \text{min_pT_e_1st}$ for hardest electron Minimal requirement $p_{T,e_2} > \text{min_pT_e_2nd}$ for second-hardest electron
muon_cuts min_pT_mu_1st min_pT_mu_2nd	Switch for cuts on transverse momentum of (second-)hardest muon $p_{T,\mu_1}(p_{T,\mu_2})$ Minimal requirement $p_{T,\mu_1} > \text{min_pT_mu_1st}$ for hardest muon Minimal requirement $p_{T,\mu_2} > \text{min_pT_mu_2nd}$ for second-hardest muon
gap_eta_e	Switch for detector gap in absolute pseudo-rapidity $ \eta_e $ of electrons

Table 12 continued

user_switch user_cut	Description
gap_min_eta_e gap_max_eta_e	Start of the gap, keeping only events with $ \eta_e < \text{gap_min_eta_e}$ End of the gap, keeping only events with $ \eta_e > \text{gap_max_eta_e}$
M_gamgam min_M_gamgam max_M_gamgam	Switch for cuts on invariant mass $m_{\gamma\gamma}$ of photon pairs Minimal requirement $m_{\gamma\gamma} > \text{min_M_gamgam}$ for photon pairs Maximal requirement $m_{\gamma\gamma} < \text{max_M_gamgam}$ for photon pairs
pT_gam_1st min_pT_gam_1st	Switch for cuts on transverse momentum of hardest photon p_{T,γ_1} Minimal requirement $p_{T,\gamma_1} > \text{min_pT_gam_1st}$ for hardest photon
R_gamgam min_R_gamgam	Switch for cuts on photon separation in $\Delta R_{\gamma\gamma} = \sqrt{\Delta y_{\gamma\gamma}^2 + \Delta\phi_{\gamma\gamma}^2}$ Minimal requirement $\Delta R_{\gamma\gamma} > \text{min_R_gamgam}$ for photon pairs
gap_eta_gam gap_min_eta_gam gap_max_eta_gam	Switch for detector gap in absolute pseudo-rapidity $ \eta_\gamma $ of photons Start of the gap, keeping only events with $ \eta_\gamma < \text{gap_min_eta_gam}$ End of the gap, keeping only events with $ \eta_\gamma > \text{gap_max_eta_gam}$
M_lepgam min_M_lepgam	Switch for cuts on invariant mass $m_{\ell\gamma}$ of lepton–photon pairs Minimal requirement $m_{\ell\gamma} > \text{min_M_lepgam}$ for lepton–photon pairs
R_lepgam min_R_lepgam	Switch for cuts on lepton–photon separation in $\Delta R_{\ell\gamma} = \sqrt{\Delta y_{\ell\gamma}^2 + \Delta\phi_{\ell\gamma}^2}$ Minimal requirement $\Delta R_{\ell\gamma} > \text{min_R_lepgam}$ for lepton–photon pairs
R_lepjet min_R_lepjet	Switch for cuts on lepton–jet separation in $\Delta R_{\ell j} = \sqrt{\Delta y_{\ell j}^2 + \Delta\phi_{\ell j}^2}$ Minimal requirement $\Delta R_{\ell j} > \text{min_R_lepjet}$ for lepton–jet pairs
lep_iso lep_iso_delta_0 lep_iso_epsilon	Switch for special isolation of lepton–lepton and lepton–parton pairs, as used for example in the ZZ Higgs background, see Ref. [139]. For each lepton i we compute the sum of the transverse momenta over all leptons and partons in a certain R cone around i and take the ratio to its transverse momentum. All events are discarded where this ratio is below a certain threshold: $\sum_{\substack{j \in \{\ell, \text{partons}\} \\ \text{with } \Delta R_{ij} < \delta_0}} p_{T,j} / p_{T,i} < \epsilon$ δ_0 in the formula above ϵ in the formula above
R_ejet min_R_ejet	Switch for cuts on electron–jet separation in $\Delta R_{ej} = \sqrt{\Delta y_{ej}^2 + \Delta\phi_{ej}^2}$ Minimal requirement $\Delta R_{ej} > \text{min_R_ejet}$ for electron–jet pairs
R_gamjet min_R_gamjet	Switch for cuts on photon–jet separation in $\Delta R_{\gamma j} = \sqrt{\Delta y_{\gamma j}^2 + \Delta\phi_{\gamma j}^2}$ Minimal requirement $\Delta R_{\gamma j} > \text{min_R_gamjet}$ for photon–jet pairs
mT_CMS min_mT_CMS	Switch for cuts on transverse mass $m_{T,W}$ of W boson as defined by CMS [140] Minimal requirement $m_{T,W} > \text{min_mT_CMS}$ for the W boson

Table 12 continued

user_switch user_cut	Description
pT_W min_pT_W max_pT_W	Switch for cuts on transverse momentum $p_{T,\ell\nu_\ell}$ of (identified) W bosons Minimal requirement $p_{T,\ell\nu_\ell} > \text{min_pT_W}$ for (identified) W bosons Maximal requirement $p_{T,\ell\nu_\ell} < \text{max_pT_W}$ for (identified) W bosons
MT_Wrec min_MT_Wrec	Switch for cuts on transverse mass $m_{T,\ell\nu_\ell}$ of (identified) W bosons, defined by $m_{T,\ell\nu_\ell} = \sqrt{(E_{T,\ell} + E_{T,\nu_\ell})^2 - (p_{T,\ell\nu_\ell})^2}$ with $(E_{T,x})^2 = m_x^2 + (p_{T,x})^2$ Minimal requirement $m_{T,\ell\nu_\ell} > \text{min_mT_Wrec}$ for (identified) W bosons
rel_pT_miss min_rel_pT_miss	Switch for cuts on the relative missing transverse momentum $p_T^{\text{miss,rel}}$, which is defined as $p_T^{\text{miss}} \times \sin \Delta\phi $, where $\Delta\phi$ is the azimuthal separation between $\mathbf{p}_T^{\text{miss}}$ and the momentum of the closest lepton, see Ref. [130] Minimal requirement $p_T^{\text{miss,rel}} > \text{min_rel_pT_miss}$

It is important to note that the four-vectors of the particles can be simply added to define a new four-vector, where the same functions can be used. For example, the transverse mass ($\sqrt{m^2 + p_T^2}$) of the system of the lepton pair (hardest and second-hardest lepton) can be simply computed by

```
fourvector fourvector_of_leplep = PARTICLE("lep")[0].
momentum+PARTICLE("lep")[1].momentum;
double mT_leplep = fourvector_of_leplep.ET();
```

Similarly, one may also directly sum two objects of type `particle` to define a new particle whose momentum corresponds to the sum. Thus, it would be equivalent to compute the transverse mass of the system of the lepton pair by using

```
particle leplep = PARTICLE("lep")[0] + PARTICLE("lep")[1];
double mT_leplep = leplep.ET();
```

Finally, if a certain observable one may want to compute is neither predefined in the `particle` nor the `fourvector` class, one can always access the momenta directly by using

```
fourvector fourvector_of_hardest_lep = PARTICLE("lep")[0].
momentum;
double E_hardest_lep = fourvector_of_hardest_lepton.x0();
double x_hardest_lep = fourvector_of_hardest_lepton.x1();
double y_hardest_lep = fourvector_of_hardest_lepton.x2();
double z_hardest_lep = fourvector_of_hardest_lepton.x3();
```

and compute the desired observable from the explicit momentum components.

B.1.2 Access to user-defined parameters

In the file `parameter.dat` three types of user-defined parameters can be added, which are available in the C++ code and can be directly accessed throughout the process-specific C++ files inside the folder `MATRIX_v1.0.0/prc/$ {process_id}/user`.

- An integer-valued user parameter is added via

```
user_switch my_integer_parameter = 1
```

to the file `parameter.dat` and is accessed in the C++ code by

```
static int my_integer
= USERSWITCH("my_integer_parameter");
```

Such switches are useful in many respects, two already used examples are to turn on and off cuts, or to choose between different identification procedures.

- A real-valued user parameter is added via

```
user_cut my_real_parameter = 1.23
```

to the file `parameter.dat` and is accessed in the C++ code by

```
static double my_real = USERCUT("my_real_parameter");
```

Such real parameters are useful in many respects, the most important example is their use to define and

implement cuts that can be changed later from the file `parameter.dat` without recompilation of the code.

- Finally, a new particle (group) can be defined by adding

```
user_particle my_own_particle = my_own_particle
```

to the file `parameter.dat`. Only if defined this way, it can be filled in the C++ code,

```
USERPARTICLE("my_own_particle").
push_back(PARTICLE("lep")[0] + PARTICLE("lep")[1]);
```

which would add a particle whose momentum is the sum of the hardest and second-hardest lepton to the user-defined particle group `my_own_particle`. If a user-defined particle group is filled with more than one particle, the usual p_T -ordering is done automatically before the respective particle group is used in scales, cuts or distributions. Note that a `USERPARTICLE` may only be filled in a certain position of the code, see below in Appendix B.2, and that it can be accessed later like all other particle groups via the container `PARTICLE`.

B.2 Definition of a new particle group

The predefined particle groups are sufficient for most practical cases. However, the user is allowed to define his own particle group by filling the respective four-vectors. This can be very useful if an intermediate particle cannot be unambiguously reconstructed, like in the case of the SF channel in ZZ (or $W^\pm Z$) production, where an identification procedure is needed for the Z (and the W) bosons. As described in Sects. 5.2.4.4 and 5.2.4.9, such definition of process-specific particle groups is done intrinsically for these two processes following different identification procedures used by ATLAS and CMS. In the following we describe the necessary steps for a user to add his own definition of a particle group to any process.

The relevant C++ file is `MATRIX_v1.0.0/prc/${process_id}/user/specify.particles.cxx` to fill user-defined particles. As described above, one has to add the definition of a new particle group to the file `parameter.dat`. After that the respective particle group exists as an empty array of objects of type `particle` inside the C++ code, which must be filled by appending at least one object of type `particle` to the array.

Let us give a simple example: A new particle group should be filled depending on the value of an integer switch with either the hardest lepton or the second-hardest lepton. The relevant input in the file `parameter.dat` would look like

```
user_particle relevant_lepton = relevant_lepton # lepton, depending on switch_lepton
user_switch switch_lepton = 0 # (0) hardest lepton, (1) second-hardest lepton
```

and the relevant C++ code in the `specify.particles.cxx` would be

```
...
static int switch_lepton = USERSWITCH("switch_lepton");
if (switch_lepton == 0){
    USERPARTICLE("relevant_lepton").push_back
        (PARTICLE("lep")[0]);
}
else if (switch_lepton == 1){
    USERPARTICLE("relevant_lepton").push_back(PARTICLE
        ("lep")[1]);
}
}
```

```
else {
    logger << LOG_ERROR << "ERROR: switch_lepton =
    " << switch_lepton << "; allowed values:
    0, 1" << endl;
    assert(false);
}
...
}
```

Bear in mind that after definition of a `USERPARTICLE`, the respective particle group is automatically filled afterwards. If the user-defined particle group contains more than one particle, the usual p_T -ordering is applied. The new particle group can then be accessed via the standard `PARTICLE` container, e.g.

```
...
particle the_relevant_lepton
    = PARTICLE("relevant_lepton")[0]
...
}
```

At this point the definition of the new particle has no practical effect yet, but one could now use the new particle group in the definition of a cut or for a distribution, and then decide via the switch in the input file whether it uses the hardest lepton or the second-hardest lepton. Such simple example may not appear to be extremely useful, however, this changes drastically if such cut or distribution is done according to a more complicated identification of a particle. In that case the identification procedure can be switched on-the-fly without the need of recompilation and without having to reimplement the same cuts and distributions for every new identification procedure. We refer the interested reader to `MATRIX_v1.0.0/prc/ppeeex04/user/specify.particles.cxx` for a sample implementation.

B.3 Implementation of a new dynamic scale

The relevant C++ file is `MATRIX_v1.0.0/prc/${process_id}/user/specify.scales.cxx` to add a new user-defined dynamic scale. All processes have at least two dynamic scales already implemented, and one can follow these implementations. In principle, one is free to code whatever one desires in that file, without taking care of the existing

structure. One only has to make sure that in the end the variable `temp_mu_central` is set to the correct value. However, we recommend to follow the existing structure of the `if` and `else if` blocks to keep with the functionality of choosing different dynamic scales in the file `parameter.dat`.

Let us give a simple example, for completeness: If we want to add a dynamic scale 123 that computes the sum of the Z -boson mass and the transverse momentum of the hardest lepton, we would set

```
dynamic_scale = 123 # dynamic ren./fac. scale
```

in the file `parameter.dat` and add an `else if` block to the `specify.scales.cxx` file:

```
...
else if (sd == 123){
    // sum of Z-boson mass and pT of hardest lepton
    double m_Z = osi_msi.M_Z;
    double pT_hardest_lepton = PARTICLE("lep")[0].pT;
    temp_mu_central = m_Z + pT_hardest_lepton;
}
...
```

B.4 Implementation of a new user-defined cut

The relevant C++ file is `MATRIX_v1.0.0/prc/${process_id}/user/specify.cuts.cxx` to add a new user-defined cut. Most processes already have several process-specific cuts implemented, and one can in principle follow these implementations. Also in this file the user is essentially free to implement whatever he deserves without taking care of the existing structure. The only relevant information is that under whatever conditions one requires an event to be discarded, one sets

```
...
osi_cut_ps[i_a] = -1;
return;
...
```

in order to cut the current phase-space point. The relevant momenta at each event are accessed via the particle groups as explained above. Nevertheless, we recommend to keep the existing structure by defining cuts via the `user_switch` and `user_cut` parameters that can be interactively changed afterwards in the file `parameter.dat` without recompilation of the C++ code, instead of hard-coding such information in the file `specify.cuts.cxx`.

As a simple example we consider a lower cut on the absolute rapidity difference between the hardest and second-hardest lepton. Such cuts are added to the file `parameter.dat`,

```
user_switch dy_lep1lep2 = 1 # switch to turn on (1) and off (0) cuts on absolute dy of leptons
user_cut min_dy_lep1lep2 = 0.5 # requirement on absolute rapidity difference of leptons (lower cut)
```

and implemented into the C++ code as follows:

```
...
// get settings for cut on absolute rapidity
// difference of leptons
static int switch_dy_lep1lep2
= USERSWITCH("dy_lep1lep2 ");
static double cut_min_dy_lep1lep2
= USERCUT("min_dy_lep1lep2");

// perform cut on absolute rapidity difference
// of leptons according to settings
if (switch_dy_lep1lep2 == 1){
```

```
double y_lep1 = PARTICLE("lep")[0].rapidity;
double y_lep2 = PARTICLE("lep")[1].rapidity;
double dy_lep1lep2 = y_lep1 - y_lep2;
if (abs(dy_lep1lep2) < cut_min_dy_lep1lep2) {
    osi_cut_ps[i_a] = -1; // cut phase-space point
    return;
}
...
}
```

B.5 Implementation of a new observable for distributions

The relevant C++ file is `MATRIX_v1.0.0/src-MUNICH/classes/xdistribution.cpp` to add a new user-defined distribution. Note that this part of the code is not specific to a certain process, and any observable implemented here can in principle be used in all processes. The relevant routine of the `xdistribution` class is

```
void xdistribution::computeObservable(...) {
    ...
}
```

A rather comprehensive description of how to add a new distribution can be found commented inside this routine. We summarize the most important information. As pointed out in Sect. 5.1.3, each observable has a certain type identifier `distributiontype` set in the file `distribution.dat`, which must be specified in every distribution block. Inside the `computeObservable` routine of the `xdistribution.cpp` file, we can add a new distribution-type by extending the `if` and `else if` blocks for `xdistribution_type`, which corresponds to the string set for `distributiontype` in the file `distribution.dat`. The sum of the momenta of particle `i` defined for each distribution in the file `distribution.dat` is saved to an array with entries of type `fourvector` called `reconstructedParticles[i]` inside the C++ code. The distributions can now be defined using these particles, by setting the variable `observable` to the value of the observable that should be binned for the desired `xdistribution_type`.

Let us consider a simple example where we want to plot the distribution of events in the sum of the rapidities of the two

hardest leptons by defining a new `xdistribution_type`. The definition of the distribution in the file `distribution.dat` would look like

```
distributionname = y_lep1_plus_y_lep2
distributiontype = sum_of_y
particle 1 = lep 1
particle 2 = lep 2
startpoint = 0.
endpoint = 10.
binwidth = 0.2
```

where the name and the specific definition of the binning has relevance for this example. The C++ code for the distribution type `sum_of_y` can be implemented in a general way for an arbitrary number of `particle_i` definitions by adding an `else if` block to the `computeObservable` routine in the file `xdistribution.cpp`:

```
...
else if (xdistribution_type == "sum_of_y") {
    double sum_y = 0;
    for (int group = 0; group < particles.size();
        group++) {
        fourvector fourvector_of_current_reconstructed_
            particle = reconstructedParticles[group]
        sum_y = sum_y + fourvector_of_current_
            reconstructed_particle.y();
    }
    observable = sum_y;
}
...

```

Appendix C Troubleshooting

C.1 Compiling on lxplus

There is a problem when compiling OPENLOOPS on the lxplus cluster due to an outdated Fortran version. Furthermore, when using the window manager `screen`, the `compilers/executables` might not be working (including Python). In both cases you need to execute

```
$ source /afs/cern.ch/sw/lcg/hepsoft/
0.9/x86_64-slc6-gcc48-opt/setup.sh
```

before compiling OPENLOOPS.⁵⁰

C.2 Using a window manager on lxplus

Since lxplus grants read/write permissions via kerberos tickets, which are valid only for 24 h, it is not trivial to employ a window manager. In particular, the standard option `screen` does not work properly. We recommend `tmux` on lxplus instead, which can be used as follows:

First, create a session with a kerberos ticket

```
krenew -b -t -- tmux new-session -d -s
my_tmux_session
```

and enter the session with

```
tmux attach
```

Change the directory to a MATRIX process folder and start a run inside the `tmux` session. The session can now be detached (`Ctrl+b` `q`) and the run will continue. However, read/write permission will end after 24 h. In order to maintain

them, the kerberos ticket must be renewed inside the `tmux` session. To do so, enter the `tmux` session again and open a second window inside the same session (`Ctrl+b` `g`). Now, enter

```
kinit
```

and type your CERN password to renew the kerberos ticket. Change between the two `tmux` windows (`Ctrl+b` `n`) and get back to the output of the MATRIX run. Before further 24 h have passed, the kerberos ticket needs to be renewed again. In principle, one could have a script take care of these renewals. However, it is not secure to save the CERN password within a human-readable executable.

C.3 Problems with libquadmath

If you encounter

```
error while loading shared libraries:\
libquadmath.so.0: cannot open shared
object file: No such file or
directory
```

at runtime, implying that dynamic linking to `libquadmath` failed, you can set `path_to_libgfortran` in the file `MATRIX_configuration` to the path where `libquadmath` is installed on your system.

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⁵⁰ In general, it is a good idea to add it to your `.bashrc/.bash_profile` (and/or your `.screenrc`) to avoid having to retype it for each new session/screen.

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