



LAPPEENRANTA  
UNIVERSITY OF TECHNOLOGY

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# **FUSION WELD METAL SOLIDIFICATION: Continuum from weld interface to centerline**

*Thesis for the degree of Doctor of Science (Technology) to be presented with due permission for the public examination and criticism in the Auditorium 1383 at Lappeenranta University of Technology, Lappeenranta, Finland on the 7th of March, 2008, at noon*

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# CONTENTS

<b>ABSTRACT</b>	<b>3</b>
<b>FOREWORD</b>	<b>4</b>
<b>CONTENTS</b>	<b>5</b>
<b>LIST OF SYMBOLS</b>	<b>7</b>
<b>ORIGINAL FEATURES OF THIS DISSERTATION</b>	<b>9</b>
<b>INTRODUCTION</b>	<b>11</b>
<b>Chapter 1 GENERAL ASPECTS OF SOLIDIFICATION</b>	<b>14</b>
1.1 Solidification basics	14
1.2 Descriptive classification vs. "Cases"	28
1.3 Growth modes	28
<b>Chapter 2 SOLIDIFICATION RESEARCH IN THE 20<sup>th</sup> CENTURY</b>	<b>29</b>
2.1 Equilibrium solidification; Case 1	29
2.2 Start of modern solidification theory; Gulliver and Case 2	29
2.3 Scheil during WWII	30
2.4 Bell Laboratories; Burton, Primm & Slichter, Pfann's Cases	31
2.5 University of Toronto; ~1950	32
2.6 MIT; Flemings and Mullins & Sekerka	35
2.7 RPI; Savage	36
2.8 Lausanne – EPFL; Kurz	39
2.9 David & Vitek 1989; NEGS to EGS transformation	42
2.10 Tokyo University; Koseki	43
2.11 Osaka University; Nishimoto, Mori	44
2.12 St. Petersburg State Polytechnic University	45
2.13 Inverse modeling of temperature field	45
2.14 Paton institute; Demchenko	46
2.15 Phase-Field simulation	47
2.16 Bimetallic surfaces: Special phase diagrams and anomalous nano-particles	48
<b>Chapter 3 THE FOUR CASES OF SOLIDIFICATION</b>	<b>49</b>
3.1 Case 1: Equilibrium solidification	49
3.2 Case 2: No diffusion in solid, total mixing in liquid	49
3.3 Case 3: No diffusion in solid, partial diffusion in liquid	50
3.4 Case 4: Splat cooling	50
<b>Chapter 4 INTERMEDIATE SUB-CASES</b>	<b>51</b>
4.1 Sub-Cases below Case 3	51
4.2 Sub-Cases above Case 3: Mullins & Sekerka / Lausanne / Solute Trapping	53
<b>Chapter 5 WELD SOLIDIFICATION CONTINUUM AND ITS MODELING</b>	<b>55</b>
5.1 Rate-Gradient analyses	55
5.2 Geometric morphology-model	55
5.3 Solid solute profile-model: One Case	56
5.4 Weld Solidification Continuum Model Frame – a tool for modeling	56
5.5 Discussion of the proposed Model Frame	60
5.6 The melting stage and Melting/ Solidification- (M/S-) model	62
5.7 About the Model Frame, Cases, Sub-Cases, Sub-Case Variables and the Lausanne and RPI approaches	65
<b>Chapter 6 EXPERIMENTS ON PURE AND DOPED Cu</b>	<b>67</b>
6.1 Materials and tests	67
6.2 Metallographic observations	71
6.3 Hot cracking	74
6.4 About the experimental method	75

<b>Chapter 7 DISCUSSION</b>	<b>76</b>
<b>Chapter 8 SUMMARY OF THE DISSERTATION</b>	<b>77</b>
<b>REFERENCES</b>	<b>79</b>
<b>APPENDIXES 84</b>	
Appendixes 1...10: No dope, Cu	85
Appendixes 11...22: Bi-dope	98
Appendixes 23...27: La-dope	110
Appendixes 28...31: Li-dope	115
Appendixes 32...33: P-dope	118
Appendixes 34...35 Pb-dope	121
Appendix 36. Ambiguities in the definitions of some central concepts	125
Appendix 37. The dismissal of the cellular dendritic growth	126
Appendix 38. The Melting/Solidification- (M/S-) model	127
Appendix 39. Pool Shape	139
Appendix 40. Joining Case 2 to Case 1 with added solid diffusion, Sub-Case 2(-)Ds	141
Appendix 41. Visualization of the Cases, Sub-Cases and operation paths of Cases 2 and 3 from solidification start to its end	142
Appendix 42. The Stagnant Layer and the Concentration Gradient Width	144
Appendix 43. The Lausanne- and RPI-approaches at cell centerline	147