

## Gating of high-mobility two-dimensional electron gases in GaAs/AlGaAs heterostructures

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**Abstract.** In this work, we investigate high-mobility two-dimensional electron gases in  $\text{Al}_x\text{Ga}_{1-x}\text{As}$  heterostructures by employing Schottky-gate-dependent measurements of the samples' electron density and mobility. Surprisingly, we found that two different sample configurations can be set *in situ* with mobilities differing by a factor of more than two in a wide range of densities. This observation is discussed in the context of charge redistributions between the doping layers and is relevant for the design of future gateable high-mobility electron gases.

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## 1. Introduction

Two-dimensional electron gases (2DEGs) in  $\text{Al}_x\text{Ga}_{1-x}\text{As}$  heterostructures can reach mobilities exceeding  $10^7 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at low temperatures, facilitating the observation of fascinating phenomena like the microwave-induced zero-resistance states, the  $\nu = 5/2$  quantum Hall state and interactions between composite fermions [1]. To study them, clean materials and other growth techniques beyond the standard modulation doping approach are essential [2–4]. However, current growth protocols are apparently in conflict with the *in situ* control of the 2DEG's density via Schottky gates: recent experiments on gated high-mobility structures have reported hysteresis effects and temporal drifts when biasing Schottky gates [5, 6]. In order to investigate the origin of these effects, we fabricate gated Hall bars containing a high-mobility 2DEG.

## 2. Experiment

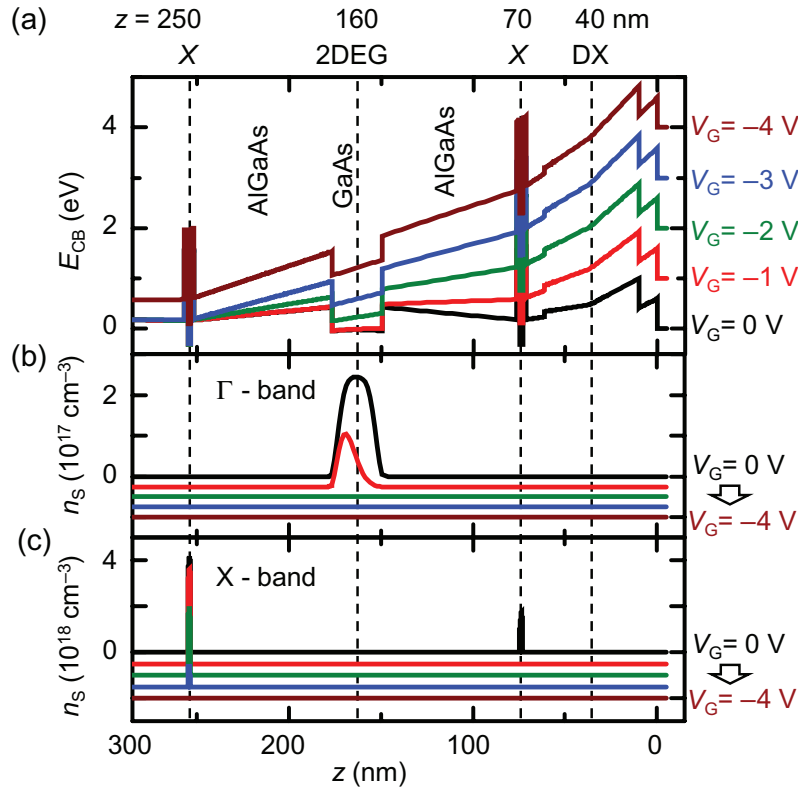
In the investigated samples, the 2DEG resides in a 30 nm wide GaAs quantum well, 160 nm beneath the surface. The overall growth scheme is similar to that reported previously [8]. Two Si donor layers are situated at depths  $z$  of about 40 and 680 nm in order to compensate for surface states and background impurities in the substrate. Since these donors are embedded in  $\text{Al}_{0.33}\text{Ga}_{0.67}\text{As}$ , they are expected to form DX-centres below the  $\Gamma$ -band [7]. Layers of GaAs at  $z \approx 70 \text{ nm}$  and  $z \approx 250 \text{ nm}$  are  $\delta$ -Si doped and enclosed in 2 nm thick layers of AlAs. The ground state in the AlAs wells ( $X$ -minima) is lower than that in the GaAs wells ( $\Gamma$ -minima). Consequently, only a part of the donors' free electrons reside in the high-mobility 2DEG, whereas the rest is expected to populate the  $X$ -band within the AlAs layers embedding the doping planes [2, 8].

The investigated samples stem from different wafers with the same layer structure. Typical transport characteristics of unprocessed samples are a Drude mobility of  $\mu \gtrsim 18 \times 10^6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at an electron density of  $n_S = 3.2 \times 10^{11} \text{ cm}^{-2}$  as measured in van der Pauw geometry at a temperature of  $T = 1.3 \text{ K}$  (data not shown).

The samples are etched 150 nm deep to define a  $1100 \mu\text{m}$  long and  $100 \mu\text{m}$  wide Hall bar. AuGe pads are deposited and annealed to contact the 2DEG. In a final step, 200 nm of Ti/Au are deposited on the Hall bar to form a Schottky top gate.

Figure 1(a) shows the uppermost 300 nm of the heterostructure's  $\Gamma$  conduction band edge, calculated self-consistently for different top gate voltages<sup>4</sup>. The electrochemical potential (defined as  $E_{\text{CB}} = 0 \text{ eV}$ ) is assumed to be pinned mid-gap in the substrate and 0.6 eV below the  $\Gamma$  conduction band at the surface. For the sake of simplicity, dynamic processes are not taken into account and the ionization degree of the DX-dopants is assumed to be independent of gate voltage. The doping concentrations at  $z = 70 \text{ nm}$  and  $z = 250 \text{ nm}$  have been chosen so that both the 2DEG's electron density at  $V_G = 0 \text{ V}$  and the pinch-off voltage are consistent with the experimentally determined values. The chosen value of  $8.0 \times 10^{11} \text{ cm}^{-2}$  is smaller than the density of silicon atoms of  $20 \times 10^{11} \text{ cm}^{-2}$ , suggesting that only part of the donors are electrically active. The gate is situated at the surface ( $z = 0 \text{ nm}$ ) and is set to  $V_G = 0, -1, -2, -3$  and  $-4 \text{ V}$ , respectively (black, red, green, blue and maroon traces). Figure 1(b) shows the calculated free electron density in the  $\Gamma$ -band for these gate voltages. Applying  $V_G = -1 \text{ V}$  reduces the 2DEG's electron density and shifts the wavefunction to the lower boundary of the well

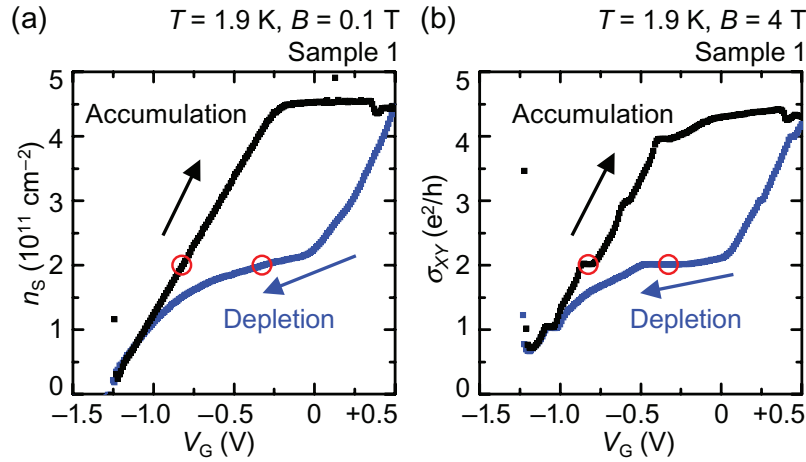
<sup>4</sup> We employ the 3D nanodevice simulator nextnano<sup>3</sup>, available at <http://www.nextnano.de>



**Figure 1.** (a) Calculated conduction band profile of the investigated heterostructure, shown for top gate voltages  $V_G = 0, -1, -2, -3$  and  $-4$  V (black to maroon). The gate is situated at  $z \leq 0$  nm; Si-dopants in AlGaAs at  $z \approx 40$  nm and  $z \approx 680$  nm compensate for surface states and substrate impurities, respectively. Si-dopants in GaAs at  $z \approx 70$  nm and  $z \approx 250$  nm are bordered by AlAs layers with the well state in the X-band (not shown) situated below the Fermi energy (defined as  $E_{CB} = 0$  eV) for  $V_G = 0$  V. The 2DEG resides in a GaAs quantum well at  $z \approx 160$  nm. (b) Calculated free electron density in the  $\Gamma$ -band for  $V_G = 0, -1, -2, -3$  and  $-4$  V, with curves vertically offset for clarity. With increasingly negative gate bias, the 2DEG's density decreases until it is fully depleted at  $V_G = -2$  V (green traces). (c) Electron density in the X-band, calculated for the same set of gate voltages. The upper layer of X-electrons is depleted first and then the lower layer of X-electrons is depleted at  $V_G \lesssim -3$  V.

(red trace). The 2DEG is depleted when applying  $V_G = -2$  V (green trace). Figure 1(c) shows the electron density in the X-band for the same set of gate voltages. At  $V_G = 0$  V (black trace), electrons occupy the AlAs layers at  $z \approx 70$  nm and  $z \approx 250$  nm with the respective electron densities in the X-band being  $n_S = 2.1 \times 10^{-11} \text{ cm}^{-3}$  (upper layer) and  $n_S = 5.5 \times 10^{-11} \text{ cm}^{-3}$  (lower layer). Applying  $V_G = -1$  V (red) depletes the upper layer of X-electrons and applying  $V_G \lesssim -3$  V depletes also the bottom layer of X-electrons.

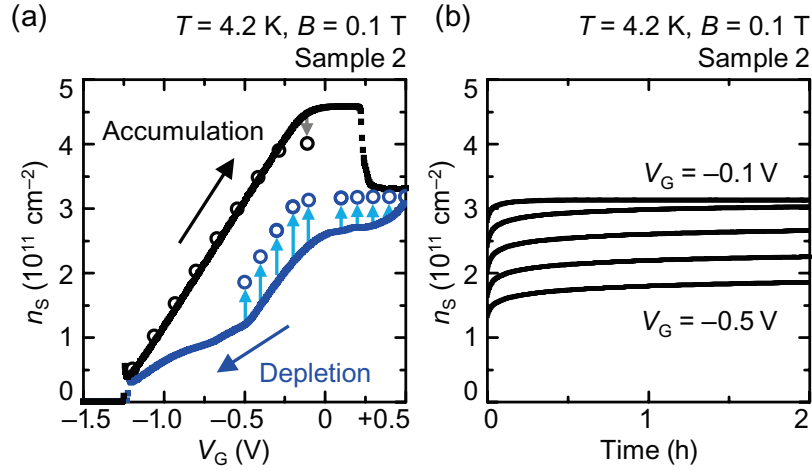
The samples' transport properties are measured at low temperatures  $T \lesssim 4.2$  K employing a standard lock-in technique with a typical modulation frequency of  $f = 72$  Hz and an amplitude of  $\Delta V_{SD} = 40 \mu\text{V}$ . The Hall density  $n_S$  is obtained from the measured source-drain current  $I_{SD}$  and the transversal four-terminal voltage  $U_Y$  via the relationship  $n_S = BI_{SD}/eU_Y$ . Here,



**Figure 2.** (a) Electron density  $n_S$  as a function of gate voltage, measured at a small perpendicular magnetic field  $B = 0.1 \text{ T}$  at  $T = 1.9 \text{ K}$ . Sweeping from  $V_G = +0.5 \text{ V}$  to  $V_G = -3 \text{ V}$  (blue), the density is reduced in a nonlinear manner. In contrast, the density increases linearly as the positive gate bias increases (black). The gate voltages corresponding to a density of  $n_S = 2 \times 10^{11} \text{ cm}^{-2}$  are marked by red circles. (b) Transversal magnetoconductance  $\sigma_{XY} = I_{SD}/U_Y$  in units of  $e^2/h$ , plotted as a function of the applied gate bias at  $B = 4 \text{ T}$ . The two gate voltages with  $\sigma_{XY} = 2 e^2/h$  and, hence, filling factor  $\nu = 2$  are again marked by red circles.

$B$  is the magnetic field strength applied perpendicular to the plane of the 2DEG and  $e$  denotes the elementary charge. Starting from positive gate bias  $V_G = +0.5 \text{ V}$ , the gate voltage is swept with a rate of  $\Delta V_G/\Delta t \approx 10 \text{ m V}^{-1} \text{ s}^{-1}$  to  $V_G = -3 \text{ V}$  and back to  $V_G = +0.5 \text{ V}$ . The upper limit of  $V_G = +0.5 \text{ V}$  is determined by the onset of leakage current, whereas the lower boundary of  $V_G = -3 \text{ V}$  was empirically chosen because larger voltage loops do not change the results described in the following. The calculated electron densities shown in figure 1(c) suggest that this lower border is correlated with the depletion of the lower layer of X-electrons for  $V_G \lesssim -3 \text{ V}$ .

Figure 2(a) shows the measured electron density as a function of gate bias in the magnetic field of  $B = 0.1 \text{ T}$  oriented perpendicular to the plane of the 2DEG. Clearly, there is a strong hysteresis between depletion (blue trace) and accumulation of the 2DEG (black). For comparison, two red circles highlight the gate voltages where  $n_S = 2 \times 10^{11} \text{ cm}^{-2}$ . Figure 2(b) shows a similar measurement repeated at  $B = 4 \text{ T}$ , where the density is expressed as the transversal magnetoconductance  $\sigma_{XY} = I_{SD}/U_Y$  in units of  $e^2/h$ . Having entered the quantum Hall regime, plateaus of  $\sigma_{XY}$  correspond to integer filling factors  $\nu = n_S h/eB$  and hence  $\nu = n_S \times 1.03 \times 10^{-11} \text{ cm}^2$ . Again, gate voltages corresponding to the electron density  $n_S = 2 \times 10^{11} \text{ cm}^{-2}$  are marked by red circles. These voltages match the values from figure 2(a), implying that the classical Hall density matches the quantum Hall density and no populated second subband or other parallel conducting channels contribute to the measured electron densities within experimental accuracy, as confirmed by zero resistance minima in Shubnikov-de Haas data (not shown). For both measurements, as long as the 2DEG density is being reduced,  $n_S$  is not linear with respect to the gate bias. In contrast, the electron density increases linearly



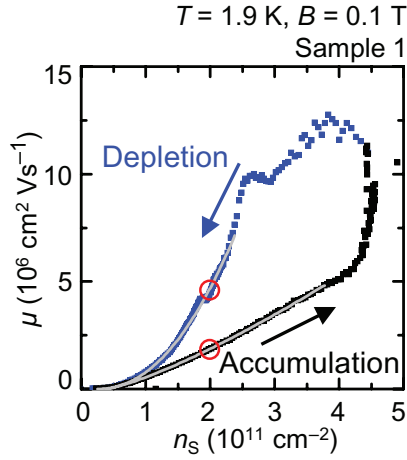
**Figure 3.** (a) Electron density  $n_S$  as a function of gate voltage, measured during the depletion (blue) and accumulation (black) of the 2DEG. When stopping the gate-sweep during depletion, the electron density converges towards the values shown by blue circles. A stop during accumulation and waiting for 1 h results in the densities shown by black circles. During depletion, the sample's electron density drifts towards larger values, whereas during accumulation the sample is stable for densities  $n_S \lesssim 3.5 \times 10^{11} \text{ cm}^{-2}$ . (b) Time dependence of the electron density after the depletion has been interrupted at one of the gate voltages  $V_G = -0.1, -0.2, -0.3, -0.4$  and  $-0.5 \text{ V}$ .

with a slope of  $dn_S/dV_G = 4.2 \times 10^{11} \text{ cm}^{-2} \text{ V}^{-1}$  while accumulating the 2DEG, being in good agreement with the model of a parallel-plate capacitor defined by the gate and the 2DEG<sup>5</sup>. This qualitative difference indicates that charge redistributes in the region between gate and 2DEG during depletion but not during accumulation of the 2DEG.

Figure 3(a) shows the electron density of another sample with the same heterostructure layer sequence, measured at  $B = 0.1 \text{ T}$  and  $T = 4.2 \text{ K}$ . Again, the electron density shows a strong hysteresis between depletion (blue) and accumulation (black) of the 2DEG. Interrupting the gate-sweep during depletion and waiting for 2 h results in an increased electron density (blue circles). In contrast, the same procedure during accumulation shows that the electron density is stable for at least 1 h during accumulation (black circles). This finding implies that the charge redistribution is complete at gate biases  $V_G \lesssim -1.5 \text{ V}$  and is stable in time afterwards. For comparison, the temporal evolution of the electron density during depletion is shown in figure 3(b). Stopping the gate-sweep at one of the gate voltages  $V_G = -0.1, -0.2, -0.3, -0.4$  and  $-0.5 \text{ V}$  results in a slow recovery of the electron density.

A probable reason for the observed charge redistributions is the charging of the  $\delta$ -doping layer at  $z \approx 40 \text{ nm}$  beneath the surface and/or the  $X$ -electrons at  $z \approx 70 \text{ nm}$ . Thus, the observed hysteresis resembles the memory-like behaviour in 2DEG samples with vertically tunnel

<sup>5</sup> Assuming the plates to be formed by the top gate and the 2DEG at a depth of  $d \approx 160 \text{ nm}$ , the expected slope  $dn_S/dV_G$  is given by  $dn_S/dV_G = C/e = \epsilon\epsilon_0/ed \approx 4.2 \times 10^{11} \text{ cm}^{-2} \text{ V}^{-1}$ , where  $C$  is the capacity between the top gate and 2DEG,  $\epsilon \approx 12$  the dielectric constant of  $\text{Al}_{0.33}\text{Ga}_{0.67}\text{As}$  and  $\epsilon_0 = 8.85 \times 10^{-12} \text{ CV}^{-1} \text{ m}^{-1}$  is the electric field constant.



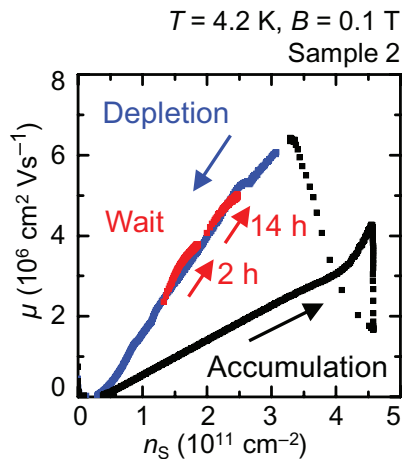
**Figure 4.** Drude mobility  $\mu$  as a function of the 2DEG's electron density  $n_s$  measured at  $B = 0.1$  T,  $T = 1.9$  K. The mobility while depleting (blue) is much higher than that when accumulating (black). For example, at  $n_s = 2 \times 10^{11} \text{ cm}^{-2}$  (red circles), the mobilities are found to be  $\mu = 4.5 \times 10^6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  (depleting) and  $\mu = 1.9 \times 10^6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  (accumulating), respectively. Grey lines are the fits of a power-law dependence  $\mu = c \times (n_s - n_0)^k$  to the data, yielding exponents of  $k = 2.1$  (depleting) and  $k = 1.3$  (accumulating).

coupled self-assembled quantum dots [9, 10]. The layers would build up positive charge during depletion up to full ionization at very negative gate voltages  $V_G \lesssim -1.5$  V. According to the calculation of the band structure in figure 1(a), electrons would not be able to repopulate the layers unless a sufficiently positive gate bias is applied. In the gate-sweeps in figures 2 and 3, such a reset of the 2DEG's density is indeed observed when ramping the gate voltage up to  $V_G \sim 0$  V. The more drastic reset at  $T = 4.2$  K (figure 3) indicates that the time constant of the associated charge redistribution is temperature dependent.

Different charge configurations of the doping layers are expected to have a strong impact on the Drude mobility  $\mu = I_{SD}/(en_s U_X) \times l/w$  of the 2DEG, where  $U_X$  is the longitudinal potential drop and  $l/w = 6$  is the aspect ratio of the Hall bar. Figure 4 shows the mobility plotted as a function of the electron density  $n_s$  at  $B = 0.1$  T and  $T = 1.9$  K during a gate-sweep from  $V_G = +0.5$  V to  $V_G = -3$  V and back to  $V_G = +0.5$  V. The mobility during depletion is clearly larger than that during accumulation at any given density (e.g.  $\mu \approx 4.5 \times 10^6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  as compared to  $\mu \approx 1.9 \times 10^6 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  at  $n_s \approx 2 \times 10^{11} \text{ cm}^{-2}$ , red circles). When accumulating, a recovery of the mobility sets in at electron densities  $n_s \gtrsim 4 \times 10^{11} \text{ cm}^{-2}$ , corresponding to gate voltages  $V_G \gtrsim 0$  V.

For temperatures of  $T \lesssim 2$  K, we find that the mobility is independent of temperature (measurement not shown), indicating that phonon scattering is not relevant for the interpretation of this gate-sweep. The fit of a power-law dependence  $\mu = c \times (n_s - n_0)^k$  to the data yields exponents of  $k = 2.1$  (depleting) and  $k = 1.3$  (accumulating)<sup>6</sup>. Such dependence is commonly associated with remote impurity scattering of ionised donor atoms [11] and is in contrast to the  $k \sim 0.7$  found in background-impurity-limited 2DEGs [3].

<sup>6</sup> The other fitting parameters are  $c = 3.4 \times 10^{-18} \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1} (\text{cm}^2)^k$ ,  $n_0 = 0.2 \times 10^{11} \text{ cm}^{-2}$  during depletion and  $c = 8.4 \times 10^{-9} \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1} (\text{cm}^2)^k$ ,  $n_0 = 0.4 \times 10^{11} \text{ cm}^{-2}$  during accumulation.



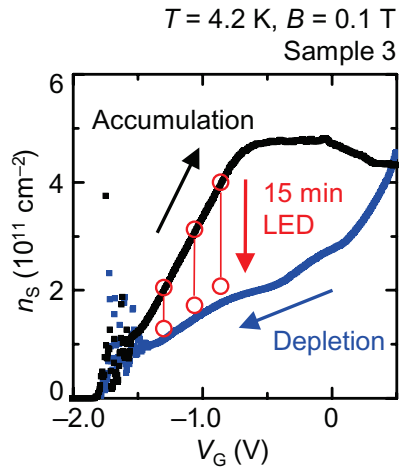
**Figure 5.** Mobility  $\mu$  as a function of the 2DEG's electron density  $n_s$  measured at  $B = 0.1 \text{ T}$  and  $T = 4.2 \text{ K}$ . The mobility during depletion (blue) is much higher than during accumulation (black). Stopping the gate-sweep at  $n_s \approx 1.3 \times 10^{11} \text{ cm}^{-2}$  and waiting for 2 h (lower red trace) results in a gradual increase of the mobility and density along the depletion-trace. The same behaviour is observed when stopping at  $n_s \approx 2 \times 10^{11} \text{ cm}^{-2}$  and waiting for 14 h (upper red trace). If the gate-sweep is stopped during accumulation, the sample's density and mobility do not change over time.

From the strong positive  $n_s$ -dependence of our sample's mobility, it can be concluded that the dominant scatterers are characterized by a potential  $V(r)$  whose Fourier transform  $V(q)$  diminishes strongly when  $q$  is increased. The significantly larger exponent  $k$  and the higher mobility during depletion suggest that during depletion, the disorder potential is steeper in  $q$ -space, corresponding to a smoother (long-range) potential in real space.

The observed decrease of the mobility with decreasing electron density may be due to several effects:

1. Decreasing the electron density increases the Fermi wavelength. This in turn facilitates scattering events that arise from the long-range part of the disorder potential [12].
2.  $X$ -electrons, which screen the dopants' disorder potential at  $V_G = 0 \text{ V}$ , are depleted at sufficiently negative gate bias. The loss of the screening layer might have a strong impact on the 2DEG's mobility.
3. During depletion, dopants between the gate and 2DEG become ionized, which leads to increased remote ionized impurity scattering.
4. At more negative gate biases (and hence lower densities), the confinement potential of the 2DEG is more strongly tilted. In this situation, the weight of the 2DEG's wavefunction is situated closer to the lower AlGaAs barrier, increasing the alloy scattering and interface roughness scattering [13].

The observation of different mobilities at the same density cannot be related to the first effect, because the Fermi wavelength is the same in both the cases. In order to test the impact of ionized donors above the 2DEG onto the mobility, the temporal evolution of the mobility is shown in figure 5. The mobility is measured at a temperature of  $T = 4.2 \text{ K}$  (compared to



**Figure 6.** Electron density  $n_S$  as a function of gate voltage, measured at  $B = 0.1$  T,  $T = 4.2$  K. There is a strong hysteresis between depletion (blue curve) and accumulation of the 2DEG (black curve). The vertical (red) lines show the density change during 15 min of IR-LED illumination with a current of  $I = 0.1$  mA at gate voltages of  $V_G = -1.3$ ,  $-1.06$  and  $-0.86$  V. During illumination, the density converges towards the value observed during depletion.

$T = 1.9$  K in figure 4) in order to speed up the relatively slow process of ionization. As a consequence, the dependence of mobility on density is almost linear due to enhanced phonon scattering [11], but still mobility is higher during depletion than during accumulation. During depletion (blue), the gate-sweep is stopped and the changes of the sample's density and mobility are recorded. Starting from  $n_S \approx 1.3 \times 10^{11} \text{ cm}^{-2}$  (lower red trace) or  $n_S \approx 2.0 \times 10^{11} \text{ cm}^{-2}$  (upper red trace), both density and mobility increase over time. The evolution follows the depletion curve, indicating that the progressing ionization acts primarily as a positive gate bias and does not determine the mobility at a given electron density. This leads us to conclude that the drastic change of the mobility after fully depleting the 2DEG is not due to changes of the charge states of the screening layer at  $z \approx 70$  nm or the doping layer at 40 nm, but rather due to the screening layer at 250 nm. After depleting both the 2DEG and this lower screening layer, more positive charge is present beneath the 2DEG, increasing the interface roughness scattering and alloy scattering due to a more tilted confinement potential. Additionally, the loss of this screening layer should increase the 2DEG's remote ionized impurity scattering with dopants beneath the 2DEG. The latter effect might be weaker than the effect of a tilted potential, because the mobility shown in figure 4 does not show a drastic decrease at the gate voltage corresponding to the expected depletion of the upper screening layer.

This finding implies that the bottom screening layer cannot be refilled laterally (from non-depleted areas of the Hall bar) but requires vertical tunnelling or an additional activation energy to regain its original X-electron density. In order to test this interpretation, the response of the electron density to illumination with an infrared light-emitting diode (IR-LED) is investigated. According to the bandstructure calculation shown in figure 1(a), the conduction band edge of the doping layers between the top gate and 2DEG is above the Fermi energy for gate voltages  $V_G \lesssim -0.5$  V. Hence, we expect an increase of the electron density in the 2DEG if the LED affects these doping layers by facilitating further ionization. In contrast, the band edge of the



screening layer at  $z \approx 250$  nm is situated below the Fermi energy as long as the 2DEG is populated. If the LED resets the positively charged bottom screening layer, the electron density of the 2DEG should decrease. Figure 6 shows the electron density at  $B = 0.1$  T,  $T = 4.2$  K, plotted as a function of gate voltage. Sweeping the gate bias from  $V_G = +0.5$  V to  $V_G = -3$  V (blue curve) and back to  $V_G = +0.5$  V (black) creates again a strong density hysteresis. When the gate-sweep is stopped during accumulation and the IR-LED is switched on by applying a current of  $I = 0.1$  mA, the density decreases over time, implying that indeed a repopulation of the screening layer at  $z \approx 250$  nm is observed. Vertical red lines at voltages  $V_G = -1.3$ ,  $-1.06$  and  $-0.86$  V show that the density decreases almost to the depletion value during 15 min of illumination, rather than approaching the density reached by stopping to deplete and waiting (as shown in figure 3). This suggests that some photo-generated electrons get trapped in the upper screening layer. Indeed, once the LED is switched off, a slow increase of the electron density is observed (data not shown), consistent with the time dependencies shown in figure 3.

### 3. Conclusion

In conclusion, we investigated gating effects in high-mobility 2DEGs. It is found that a gate-induced ionization of the doping layers between the top gate and 2DEG causes a significant hysteresis in the electron density. Surprisingly, this ionization has almost no impact on the 2DEG's mobility at a given electron density. On the other hand, the depletion of the screening layer beneath the 2DEG is found to decrease the mobility by more than a factor of 2. This drastic effect can be explained by a reduced screening of dopants and a shift of the 2DEG's wavefunction towards its lower AlGaAs boundary. Our finding indicates that for gateable high-mobility 2DEGs, it is important to keep the 2DEG wavefunction at the centre of the quantum well, which could for example be achieved through a buried back gate. At the same time, any possible screening from X-electrons needs to be (and can be) sacrificed in order to achieve large density tunability.

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