

GENERALIZED LERAY–SCHAUDER NONLINEAR ALTERNATIVES FOR GENERAL CLASSES OF MAPS

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Abstract. New Leray–Schauder nonlinear alternatives are presented. These coincidence type results are established for set-valued maps.

Key Words and Phrases: Coincidence points, nonlinear alternatives.

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