Generic Certificateless Encryption in the Standard Model*

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Abstract. Despite the large number of certificateless encryption schemes recently proposed, many of them have been found to be insecure under a practical attack called *malicious-but-passive* KGC attack, since they all follow the same key generation procedure as that of the one proposed by Al-Riyami and Paterson in ASIACRYPT 2003. The only scheme that remains secure against this attack is due to Libert and Quisquater (PKC 2006). However, the security can only be shown in the random oracle model. In this paper, we first show that a scheme which has a different key generation procedure from that of Al-Riyami and Paterson also suffers from the malicious-but-passive KGC attack. Our attacking techniques are different and may cause greater extent of damage than the previous ones. We also propose a generic construction of certificateless encryption which can be proven secure against this attack in the standard model. This generic scheme not only is the first one proven secure in the standard model, but is also very efficient to instantiate. We also describe how to use short signature and hybrid encryption to construct highly efficient instantiations of this generic scheme.

1 Introduction

In traditional public key cryptography, a user selects a public/private key pair (pk, sk) and publishes pk. A certificate, which essentially is a signature on the user's identity and pk issued by a certification authority (CA), will then be employed for indicating the relationship between the user and pk. This method works under the public key infrastructure (PKI) involves a lot of additional work for managing the certificates that include revocation, storage and distribution.

In 1984, Shamir [19], introduced the notion of identity-based cryptography, aiming to alleviate the existing problems in PKI by getting rid of certificates. A user can use an email address, an IP address or any other information related to his identity, that is publicly known and unique in the whole system, as his public key. There is a trusted party, called Key Generation Center (KGC), which is in charge of the user private key generation. The advantage of an identity-based cryptosystem is that anyone can simply use the user's identity to encrypt messages. This can be done even before the user gets its private key from the KGC. However, the user must also completely trust the KGC, which can impersonate the user and decrypt any of the user's ciphertexts. This issue is generally referred to as key escrow problem in identity-based cryptography.

In 2003, Al-Riyami and Paterson [1] introduced *certificateless cryptography*, which is intended to solve the key escrow problem that is inherent in identity-based cryptography, while at the same time, eliminate the use of certificates as in the traditional PKI. In a certificateless cryptosystem, the KGC is involved to issue a user *partial* key psk_{ID} for a user with identity ID. The user independently generates a user public/private key pair $(upk_{\text{ID}}, usk_{\text{ID}})$, and publishes upk_{ID} . A

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message will then encrypted under both upk_{ID} and the user's identity ID . To decrypt a ciphertext, the user must have the knowledge of both the user partial key psk_{ID} and secret key usk_{ID} . Knowing only one of them does not allow the recovery of the plaintext.

Related Work. Since the introduction of certificateless cryptography [1], there have been many schemes proposed [22,15,17,12,13,2,18]. The original definition of certificateless encryption [1] consists of seven algorithms. It has recently been simplified to five [12,13] and has shown to be more versatile than the original one. In this paper, we also adopt the five-algorithm simplified version for defining a certificateless encryption scheme.

Yum and Lee proposed a generic certificateless encryption scheme in [21] which has later been shown to be insecure under the model of [1] by Libert and Quisquater [17] and Galindo et al. [10] independently. In [17], the authors also proposed a generic certificateless encryption scheme. However, their scheme is only proven secure in the random oracle model, which is a heuristic method for showing the security of cryptographic schemes. The security may not preserve when the random oracle is replaced by a hash function, even if the scheme is reduced to some complexity (or number-theoretic) assumption. Recently, Liu et al. [18] proposed another certificateless encryption scheme which, to the best of our knowledge, is the first one in the standard model. However, as we will show in this paper, their scheme is insecure against malicious-but-passive KGC attack which is introduced as follows.

In [2], Au et al. considered another strong security model for certificateless cryptography, in which the user's trust on the KGC is further relaxed. By using the term introduced in [2], the KGC of a certificateless cryptosystem can be malicious-but-passive. This means the KGC can be malicious so that it may not follow the scheme specification for generating system parameters and master key, while it does not actively replace a user's public key or corrupt the user's secret key. The purpose of such a malicious-but-passive KGC is to compromise a user's secret key without being detected. Since the KGC does not need to replace the user's public key or compromise the user's machine for corrupting the user's secret key, in practice, it is very difficult to find out the occurrence of this attack. Consider a user who is the president of a country or an organization. It may have a great incentive for the KGC to launch the malicious-but-passive attack as ciphertexts for the president may contain some valuable and profitable information. The attack is practical, and the new security model would become much stronger and realistic than the old ones in this aspect if the attack is properly formalized.

Under the *malicious-but-passive* KGC attacking model, certificateless cryptosystems proposed in [1,15,16] have been shown to be insecure, since they all follow the same key generation procedure as that of [1]. The only provably secure certificateless encryption scheme against malicious-but-passive KGC attack currently available is due to Libert and Quisquater [17]. The proof is given in [2]. They showed that the IND-CPA-secure certificateless encryption scheme in [17] is also IND-ID-CPA secure under the malicious-but-passive KGC adversarial model. Then, by applying the transformation technique of [17], any IND-ID-CPA-secure scheme can be converted to an IND-ID-CCA2-secure one. However, the final scheme is only secure in the random oracle model. There is no concrete or generic construction of certificateless encryption which is proven secure against malicious-but-passive KGC attacks in the standard model.

Our Results. As a motivation, we first show that a recently proposed certificateless encryption scheme [18] also suffers from the malicious-but-passive KGC attack. As mentioned above,

schemes in [1,15,16] are vulnerable to the malicious-but-passive KGC attack described in [2] as they all follow the same key generation procedure as that of [1]. However, the attacking technique of [2] does not apply to the scheme in [18] as the key generation procedure is different. We propose two malicious-but-passive KGC attacks against the scheme in [18]. The first attack causes the same extent of damage as the attack described in [2] against [1,15,16]. The second attack may cause greater impact to the system since in this attack, the malicious-but-passive KGC is able to decrypt ciphertexts which are for any user in the system without pre-selecting a target user to attack. Note that our attacks do not refute the security claims made in [18], since in their security model, it is assumed that the KGC can launch attacks only after honestly generating the master public/private key pair (and system parameters).

Then we propose the *first generic* certificateless encryption scheme which is proven secure against malicious-but-passive KGC attacks in the standard model. The idea of our construction is simple. It is constructed based on three well-formalized primitives and can be considered as a sequential encryption as in [22,2], with an additional signature-based mechanism to defend against attacks discussed in [17], but without relying on the assumption of random oracles. The construction is also efficient. We will describe how to use short signature [3] and hybrid encryption to implement highly efficient instantiations of this generic scheme.

It's worthy to note that, similar ideas were used by Dolev *et al.* [8] to construct non-malleable encryption schemes, and by Canetti *et al.* [6,4] to build public key encryption schemes from a weak variant identity-based encryption schemes.

Paper Organization. In Sec. 2, we define the certificateless encryption scheme and its security. In Sec. 3, we show that the certificateless encryption scheme in [18] is vulnerable to some new malicious-but-passive KGC attacks. Our generic construction of secure encryption schemes and its security analysis are provided in Sec. 4. We also describe some instantiations of the generic scheme based on short signature and hybrid encryption. The paper is concluded in Sec. 5.

2 Definition and Adversarial Model

A certificateless encryption scheme [1,2] consists of five (probabilistic) polynomial-time (PPT) algorithms:

- MasterKeyGen: On input 1^k where $k \in \mathbb{N}$ is a security parameter, it generates a master public/private key pair (mpk, msk).
- PartialKeyGen: On input msk and an identity $\mathsf{ID} \in \{0,1\}^*$, it generates a user partial key psk_{ID} .
- UserKeyGen: On input mpk and a user identity ID, it generates a user public/private key pair $(upk_{\rm ID}, usk_{\rm ID})$.
- Enc: On input mpk, a user identity ID, a user public key upk_{ID} and a message m, it returns a ciphertext c.
- Dec: On input a user private key usk_{ID} , a user partial key psk_{ID} , and a ciphertext c, it returns the plaintext m.

In practice, the KGC (Key Generation Center) performs the first two algorithms: MasterKeyGen and PartialKeyGen. The master public key mpk is then published and it is assumed that everyone

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in the system can get a legitimate copy of mpk. It is also assumed that the partial key is issued to the corresponding user via a secure channel so that no one except the intended user can get it. Every user in the system also performs UserKeyGen for generating its own public/private key pair and publishes the public key. The correctness requirement is defined in the conventional way. We skip the details and refer readers to [1,2] for details.

Adversarial Model. There are two types of security for a certificateless encryption scheme, Type-I security and Type-II security, along with two types of adversaries, \mathcal{A}_1 and \mathcal{A}_2 , respectively. Adversary \mathcal{A}_1 models a malicious adversary which compromises the user private key usk_{ID} or replaces the user public key upk_{ID} , however, cannot compromise the master private key msk nor get access to the user partial key psk_{ID} . Adversary \mathcal{A}_2 models the malicious-but-passive KGC which controls the generation of the master public/private key pair, and that of any user partial key psk_{ID} . The following are five oracles which can be accessed by the adversaries.

- CreateUser: On input an identity $ID \in \{0,1\}^*$, if ID has not been created, the oracle runs $psk_{ID} \leftarrow \mathsf{PartialKeyGen}(msk, ID)$ and $(upk_{ID}, usk_{ID}) \leftarrow \mathsf{UserKeyGen}(mpk, ID)$. It then stores $(ID, psk_{ID}, upk_{ID}, usk_{ID})$ into a list List¹. In both cases, upk_{ID} is returned.
- RevealPartialKey: On input an identity ID, the oracle searches List for an entry corresponding to ID. If it is not found, \perp is returned; otherwise, the corresponding psk_{ID} is returned.
- RevealSecretKey: On input an identity ID, the oracle searches List for the entry of ID. If it is not found, \perp is returned; otherwise, the corresponding usk_{ID} is returned.
- ReplaceKey: On input an identity ID along with a user public/private key pair (upk', usk'), the oracle searches List for the entry of ID. If it is not found, nothing will be carried out. If $usk' = \bot$, the oracle sets $usk' = usk_{\text{ID}}$. Then, it updates (ID, psk_{ID} , upk_{ID} , usk_{ID}) to (ID, psk_{ID} , upk', usk').
- Decryption: On input an identity ID and a ciphertext c, the oracle searches List for the entry of ID. If it is not found, \bot is returned. Otherwise, it runs $m \leftarrow \mathsf{Dec}(psk_{\mathsf{ID}}, usk_{\mathsf{ID}}, c)$ and returns m. Note that the original upk_{ID} (which is returned by CreateUser oracle) may have been replaced by the adversary.

Remark 1 (On the Decryption Oracle): In the original adversarial model of certificateless encryption [1,17], it is required that the Decryption oracle should provide correct decryptions even after the user public key has been replaced by the adversary while the corresponding user secret key is not known to the oracle. We believe that the model is hardly realistic. Hence in this paper, we only require the Decryption oracle to perform the decryption task by using the current user keys. This also captures the case that the user public key is replaced by the adversary, but the user secret key remains the same. It is possible that the message m recovered from the ciphertext by using the current usk_{1D} is \bot .

Remark 2 (On the Stronger Decryption Oracle Again): It seems to be somewhat self-contradictory if we require a certificateless encryption scheme to be secure against both the adversaries with access to the stronger Decryption oracle and the malicious-but-passive KGC. Suppose that it is secure against Type-I adversaries with access to the stronger Decryption oracle. The game simulator, which also plays the role of the KGC, has to simulate the Decryption oracle for the adversary. In order to provide correct decryption without the user private key, the

¹ Note that the list List is shared among all these five oralces.

simulator usually needs to play tricks in setting the system parameters. However, in the same way, the *malicious-but-passive* KGC should also be able to compute the correct plaintext with a high probability, without knowing user private keys.

Let \mathcal{C} be the game challenger/simulator, and $k \in \mathbb{N}$ be the security parameter. We denote by \mathcal{A} the Type-I adversary (or the Type-II adversary) in the following game:

Game-I (or, Game-II):

- 1. If this is **Game-I**, \mathcal{C} runs $(mpk, msk) \leftarrow \mathsf{MasterKeyGen}(1^k)$, and then invokes \mathcal{A}_1 on input 1^k and mpk. If this is **Game-II**, \mathcal{C} runs \mathcal{A} on input 1^k , which returns a master public key mpk to \mathcal{C} . Note that \mathcal{A} cannot make any oracle query at this stage².
- 2. In the game, \mathcal{A} can issue CreateUser, RevealPartialKey, RevealSecretKey, ReplaceKey and Decryption queries adaptively. If this is **Game-II**, the oracle RevealPartialKey is no more needed by \mathcal{A} since it has the master secret key, and when \mathcal{A} issues a query to CreateUser oracle, it has to additionally provide the user partial key psk_{ID} .
- 3. \mathcal{A} submits two equal-length messages (m_0, m_1) along with a target identity ID^* . \mathcal{C} then selects a random bit $b \in \{0, 1\}$, computes a challenge ciphertext c^* by running $c^* \leftarrow \mathsf{Enc}(mpk, \mathsf{ID}^*, upk_{\mathsf{ID}^*}, m_b)$, and returns c^* to \mathcal{A} , where upk_{ID^*} is the user public key currently in List for ID^* .
- 4. \mathcal{A} continues to issue queries as in step 2. Finally it outputs a bit b' as its guess for bit b.

 \mathcal{A} is said to win the game if b'=b, and (1) \mathcal{A} did not query RevealPartialKey on ID*, (2) \mathcal{A} did not query Decryption on (ID*, c^*), (3) if this is **Game-II**, \mathcal{A} did not query ReplaceKey on ID*. We denote by $\Pr[\mathcal{A} \text{ Succ}]$ the probability that \mathcal{A} wins the game, and define the *advantage* of \mathcal{A} in **Game-II** (or, **Game-II**) to be $\mathsf{Adv}_{\mathcal{A}} = \left|\Pr[\mathcal{A} \text{ Succ}] - \frac{1}{2}\right|$.

Definition 1. A certificateless encryption scheme CLE is said to be Type-I secure (resp. Type-II secure) if there is no probabilistic polynomial-time adversary \mathcal{A} which wins **Game-I** (resp. **Game-II**) with non-negligible advantage. CLE is said to be IND-ID-CCA2 secure if it is both Type-I secure and Type-II secure.

3 Malicious-but-Passive KGC Attack

We describe two new malicious-but-passive KGC attacking techniques (under **Game-II**) to compromise schemes that follow the key generation procedure described in [18]. The techniques are different from that in [2], which is used to compromise schemes based on another type of key generation procedures [1,15,16].

We briefly describe the certificateless encryption scheme proposed in [18] to a certain extent that our attacking technique can be understood without referring to the complete description of the original scheme. In the MasterKeyGen of [18], the KGC first generates a pairing $e: \mathbb{G}_1 \times \mathbb{G}_1 \to \mathbb{G}_2$ such that each group has order p. Then, a generator g of \mathbb{G}_1 is selected. This is followed by the selection of a set of random elements in \mathbb{G}_1 . The parameters we are going to use in the

² One exception is that if a scheme is analyzed under the random oracle model, \mathcal{A} can query the random oracle. In this paper, we do not consider this exception as the security of our scheme proposed in the subsequent section (Sec. 4) will be shown in the standard model.

attack below are $g_2, g_1', h_1, u' \in_R \mathbb{G}_1$ and $\hat{U} = \{\hat{u}_i\}$ where $\hat{u}_i \in_R \mathbb{G}_1$, for $i = 1, \dots, n$, and some $n \in \mathbb{Z}$. We skip the description of the remaining steps of MasterKeyGen and also the entire PartialKeyGen. In UserKeyGen, the user public key upk_{ID^*} for a user with identity ID^* is denoted by $(\mathsf{pk}^{(1)}, \mathsf{pk}^{(2)}) \in \mathbb{G}_1^2$. We do not need to look into how these two elements are generated. Our first attack is described as follows.

(Attack 1) The malicious-but-passive KGC (that is A_2 in Game-II) arbitrarily selects a target identity ID*. It computes $\mathfrak{u}=H_u(\mathsf{ID}^*)$, where $H_u:\{0,1\}^*\to\{0,1\}^n$ is a collision-resistant hash function pre-defined for this scheme. Let $\mathfrak{u}[i]$ be the i-th bit of \mathfrak{u} . Define $\mathcal{U}\subseteq\{1,\cdots,n\}$ to be the set of indices such that $\mathfrak{u}[i]=1$. The KGC then randomly selects $s\in_R\mathbb{Z}_p$, and sets $g_2=(U^*)^s$, where $U^*=u'\prod_{i\in\mathcal{U}}\hat{u}_i$. Other parameters in the master public/private key pair are generated normally by the KGC. In the challenge phase of Game-II, the KGC submits two distinct equal-length messages, (m_0,m_1) , and ID* as the target identity. The challenger \mathcal{C}_2 randomly selects a bit b, computes the challenge ciphertext $C^*=(\hat{C}^*,\mathsf{com}^*,\mathsf{tag}^*)$ according to the encryption algorithm of [18]. Let the challenge ciphertext $\hat{C}^*=(C_1^*,C_2^*,C_3^*,C_4^*)$. According to the specification of the encryption algorithm in [18], we have

$$C_1^* = e(\mathsf{pk}^{(2)}, g_2)^t M, \quad C_2^* = g^t, \quad C_3^* = (U^*)^t, \quad C_4^* = ((g_1')^{\mathsf{com}^*} h_1)^t$$

where $t \in_R \mathbb{Z}_p$ and $M = m_b \| \text{dec}$ for some binary string dec. The KGC can get the plaintext of \hat{C}^* by computing the following

$$\frac{C_1^*}{e(\operatorname{pk}^{(2)},(C_3^*)^s)} = \frac{e(\operatorname{pk}^{(2)},g_2^t)M}{e(\operatorname{pk}^{(2)},(U^*)^{st})} = \frac{e(\operatorname{pk}^{(2)},g_2^t)M}{e(\operatorname{pk}^{(2)},(g_2)^t)} = M = m_b \| \operatorname{dec}$$

By comparing m_b with m_0 and m_1 , the KGC can easily find out the message corresponding to C^* . This attack causes the same extent of damage as that described in [2] against [1,15,16]. Both attacks require the KGC to *pre-select* a target identity. The KGC is not able to compromise two users in the system under the **Game-II**. Specific to this certificateless encryption scheme described in [18], there is a more powerful malicious-but-passive KGC attacking technique which allows the KGC to decrypt any ciphertext in the system regardless which user is the corresponding decryptor. Therefore, the KGC does not need to pre-select a target identity.

(Attack 2) Note that the message M is 'masked' in C_1^* by $e(\mathsf{pk}^{(2)}, g_2)^t$. Instead of selecting g_2 randomly from \mathbb{G}_1 , suppose the malicious-but-passive KGC randomly picks $\beta \in \mathbb{Z}_p$ and sets $g_2 = g^{\beta}$. We can see that the KGC can remove the mask of any ciphertext by simply computing the mask value as $e(\mathsf{pk}^{(2)}, C_2^*)^{\beta}$.

The certificateless signature scheme of [18] also suffers from the first malicious-but-passive KGC attack described above. We also remark that our attacks do not refute the security claims made in [18] as their security model does not consider/capture the malicious-but-passive KGC attacks.

A Design Philosophy: To design a certificateless scheme, no matter it is an encryption scheme or a signature scheme, for security against malicious-but-passive KGC attacks, we have a great concern on its security if the scheme requires the user to make use of the parameters generated by the KGC when generating its own user public/private key pair (via UserKeyGen). The attacks above illustrate how subtle an attack can be if the malicious-but-passive KGC has certain control

on the parameters used for user key pair generation. In the first attack above, the KGC can simply modify the generation of g_2 which is one of the many parameters generated/controlled by the KGC. The user has no way to tell if g_2 is generated accordingly or maliciously. In fact, there are many other ways for the KGC to break the scheme in [18], as there are many parameters generated by or under control of the KGC. One can easily come up with more attacks against the one in [18] in addition to the two attacks described above. In addition, even if the KGC only generates a set of group parameters, for example, a bilinear pairing operation and its associated groups, we cannot guarantee that any malicious-but-passive KGC attack cannot be launched. The reason is that the groups generated and the bilinear operation chosen by the malicious KGC may not be 'generic' [20]. There may exist some trapdoor such that only the one who generates the group parameters, in our case, it is the malicious KGC, can perform some operations efficiently. Therefore, those schemes which require the user to use group parameters generated by the KGC may either be broken by some newly discovered malicious-but-passive KGC attacking techniques, or have their security left unproven.

In our generic scheme proposed below, we design our scheme such that the user partial key and user secret key are generated and used totally independently, while retaining high efficiency.

4 Our Scheme

In this section, we propose a generic certificateless encryption scheme CLE and show that it is secure under the adversarial model defined in Sec. 2. In particular, this generic scheme is the first one proven secure against the malicious-but-passive KGC attacks in the standard model.

4.1 The Scheme

Let IBE = (KG, Extract, Enc, Dec) be an IND-ID-CCA2 secure identity-based encryption scheme, PKE = (KG, Enc, Dec) an IND-CCA2 secure public key encryption scheme, and S = (KG, Sign, Vrfy) a strong one-time signature scheme. For formal definitions of IBE, PKE and S, please refer to Appendix A. In the following, we propose a generic certificateless encryption scheme CLE, which is based on these three primitives.

- MasterKeyGen: The KGC runs $(mpk, msk) \leftarrow \mathsf{IBE}.\mathsf{KG}(1^k)$, publishes mpk and keeps msk secret.
- PartialKeyGen: On input an identity ID, the KGC runs $psk_{\mathsf{ID}} \leftarrow \mathsf{IBE}.\mathsf{Extract}\ (msk, \mathsf{ID})$ and returns psk_{ID} .
- UserKeyGen: The user (with identity ID) runs $(upk_{\mathsf{ID}}, usk_{\mathsf{ID}}) \leftarrow \mathsf{PKE}.\mathsf{KG}(1^k)$, publishes $(\mathsf{ID}, upk_{\mathsf{ID}})$ and stores usk_{ID} .
- Enc: To encrypt a message m for user ID, the encryptor computes the following and returns $c \stackrel{\text{def}}{=} (c_2, \sigma, vk)$:

$$\begin{aligned} (vk, sk) &\leftarrow \mathsf{S.KG}(1^k) \\ c_1 &\leftarrow \mathsf{IBE.Enc}(mpk, \mathsf{ID}, m \| vk) \\ c_2 &\leftarrow \mathsf{PKE.Enc}(upk_{\mathsf{ID}}, c_1) \\ \sigma &\leftarrow \mathsf{S.Sign}(sk, c_2) \end{aligned}$$

– Dec: On input an identity ID and a ciphertext $c = (c_2, \sigma, vk)$, if $0 \leftarrow \text{S.Vrfy}(vk, \sigma, c_2)$, \perp is returned. Otherwise, the decryptor computes the following:

$$c_1 \leftarrow \mathsf{PK.Dec}(usk_{\mathsf{ID}}, c_2)$$

 $m \| vk' \leftarrow \mathsf{IBE.Dec}(psk_{\mathsf{ID}}, \mathsf{ID}, c_1)$

If $vk' \neq vk$, the decryptor outputs \perp ; otherwise, it outputs m.

Our construction has some similarity with Yum and Lee's [21], both can be considered as sequential combination of public key encryption and identity-based encryption. However, their scheme is insecure under our model. Our construction additionally employs a strong one-time signature which ensures the 'well-formedness' of a ciphertext and can be proven secure under our model. In [7], Dodis and Katz considered the security of multiple encryption and presented a generic construction of it. They applied the parallel encryption technique, used a freshly generated one-time verification key as the tag for each (tag-based) encryption scheme, and signed the ciphertext using the one-time signing key. Our scheme employs the sequential encryption, and uses a simpler idea. We do not need to consider tags in the encryption schemes.

4.2 Security Analysis

Theorem 1. The certificateless encryption scheme CLE is Type-I secure, provided that the underlying identity-based encryption scheme IBE is IND-ID-CCA2 secure, and the one-time signature scheme S is strongly unforgeable.

Proof. Suppose that \mathcal{A}_1 is a PPT adversary that tries to break the Type-I security of CLE. Let the challenge ciphertext that \mathcal{A}_1 receives be $c^* = (c_2^*, \sigma^*, vk^*)$. We say a ciphertext $c = (c_2, \sigma, vk)$ is valid if σ is a valid signature on c_2 with regard to the verification key vk. We denote by Forge_1 the event that vk^* appears in a decryption query $(\mathsf{ID}, c = (c_2, \sigma, vk^*))$ issued by \mathcal{A}_1 such that c is valid and $(c_2, \sigma) \neq (c_2^*, \sigma^*)$. Then we have:

Lemma 1. $Pr[Forge_1]$ is negligible in the security parameter k.

Lemma 2.
$$\left|\Pr[\mathcal{A}_1 \mid \operatorname{Succ} \wedge \overline{\mathsf{Forge}_1}] + \frac{1}{2}\Pr[\mathsf{Forge}_1] - \frac{1}{2}\right|$$
 is negligible (in k).

Please refer to Appendix B for the proofs. Therefore, by these two lemmas, we have

$$\begin{aligned} \mathsf{Adv}_{\mathcal{A}_1} &= \left| \Pr[\mathcal{A}_1 \; \mathsf{Succ}] - \frac{1}{2} \right| \\ &= \left| \Pr[\mathcal{A}_1 \; \mathsf{Succ} \land \mathsf{Forge}_1] - \frac{1}{2} \Pr[\mathsf{Forge}_1] + \frac{1}{2} \Pr[\mathsf{Forge}_1] + \Pr[\mathcal{A}_1 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_1}] - \frac{1}{2} \right| \\ &\leq \left| \Pr[\mathcal{A}_1 \; \mathsf{Succ} \land \mathsf{Forge}_1] - \frac{1}{2} \Pr[\mathsf{Forge}_1] \right| + \left| \Pr[\mathcal{A}_1 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_1}] + \Pr[\mathsf{Forge}_1] \cdot \frac{1}{2} - \frac{1}{2} \right| \\ &\leq \frac{1}{2} \Pr[\mathsf{Forge}_1] + \left| \Pr[\mathcal{A}_1 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_1}] + \frac{1}{2} \Pr[\mathsf{Forge}_1] - \frac{1}{2} \right| \end{aligned}$$

which is also *negligible* in k. This completes the proof of Theorem 1.

Theorem 2. The certificateless encryption scheme CLE is Type-II secure if the underlying public key encryption scheme PKE is IND-CCA2 secure and the one-time signature scheme S is strongly unforgeable.

Proof. Suppose that \mathcal{A}_2 is a PPT adversary that tries to break the Type-II security of CLE. Let $c^* = (c_2^*, \sigma^*, vk^*)$ be the challenge ciphertext that \mathcal{A}_2 receives, and let Forge_2 be the event that vk^* appears in a decryption query ($\mathsf{ID}, c = (c_2, \sigma, vk)$) issued by \mathcal{A}_2 (i.e., $vk^* = vk$) such that c is valid and $(c_2, \sigma) \neq (c_2^*, \sigma^*)$. We have the following two lemmas:

Lemma 3. $Pr[Forge_2]$ is negligible in k.

This proof is similar to that of Lemma 1, and thus is omitted here.

Lemma 4. $\left|\Pr[\mathcal{A}_2 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_2}] + \frac{1}{2}\Pr[\mathsf{Forge}_2] - \frac{1}{2}\right| \; is \; \mathrm{negligible} \; in \; k.$

Proof. We construct a PPT algorithm C_2 to break the IND-CCA2 security of PKE by using A_2 as a subroutine. Given the challenge public key pk and a decryption oracle $\bar{\mathcal{O}}_D$, C_2 runs A_2 on input 1^k , which returns a master public key mpk. Assume that A_2 issues at most q distinct CreateUser queries. Then, C_2 randomly selects $i \in \{1, 2, \dots, q\}$, runs $(vk^*, sk^*) \leftarrow \mathsf{S.KG}(1^k)$, stores (vk^*, sk^*) which will be used in the generation of the challenge ciphertext of A_2 , and simulates all the oracles for A_2 as follows:

- CreateUser: On input an identity ID and the user partial key psk_{ID} , we assume that this is the j-th distinct CreateUser query. If $j \neq i$, \mathcal{C}_2 runs $(upk_{\mathsf{ID}}, usk_{\mathsf{ID}}) \leftarrow \mathsf{PKE}.\mathsf{KG}(1^k)$, stores $(\mathsf{ID}, psk_{\mathsf{ID}}, upk_{\mathsf{ID}}, usk_{\mathsf{ID}}, 0)$ into a list List, and returns upk_{ID} . If j = i, \mathcal{C}_2 simply stores $(\mathsf{ID}, psk_{\mathsf{ID}}, pk, \bot, 0)$ into List and returns pk.
- RevealSecretKey: On input an identity ID, C_2 searches List for the entry of ID. If there is no such an entry, C_2 returns \perp . If $upk_{\mathsf{ID}} = pk$, C_2 outputs a random bit and aborts. Otherwise, it returns the corresponding usk_{ID} .
- ReplaceKey: On input (ID, upk', usk'), C_2 searches List for the entry of ID. If there is no such an entry, C_2 does nothing. If $upk_{\mathsf{ID}} = pk$, C_2 aborts and outputs a random bit. If $usk' = \bot$, C_2 sets $usk' = usk_{\mathsf{ID}}$. Then, it updates (ID, psk_{ID} , upk_{ID} , usk_{ID}) to be (ID, psk_{ID} , upk', usk').
- Decryption: On input (ID, $c = (c_2, \sigma, vk)$), C_2 searches List for the entry of ID. If it is not found, C_2 returns \bot . If ID is not the *i*-th distinct query made by A_2 to CreateUser, C_2 simulates the Decryption oracle using its knowledge of psk_{ID} and usk_{ID} . Otherwise $(upk_{\text{ID}} = pk)$, after the validity check of σ on c_2 with respect to vk, C_2 makes a Decryption query to oracle $\bar{\mathcal{O}}_{\text{D}}$ which returns with c_1 . Then it completes the rest using its knowledge of psk_{ID} . Note that if event Forge₂ occurs during the simulation of Decryption oracle, namely, σ is a valid signature on c_2 with respect to vk and $vk = vk^*$, C_2 outputs a random bit and aborts.

At some point \mathcal{A}_2 submits two equal-length messages (m_0, m_1) along with a target identity ID^* . If $usk_{\mathsf{ID}^*} \neq pk$, \mathcal{C}_2 outputs a random bit and aborts. Otherwise, it computes $(c_1)_0 \leftarrow \mathsf{IBE}.\mathsf{Enc}(mpk,\mathsf{ID}^*,m_0\|vk^*)$ and $(c_1)_1 \leftarrow \mathsf{IBE}.\mathsf{Enc}(mpk,\mathsf{ID}^*,m_1\|vk^*)$, submits $(c_1)_0$ and $(c_1)_1$ to its challenger, and is returned c_2^* which is a ciphertext of $(c_1)_b$, where $b \in \{0,1\}$. It then computes $\sigma^* \leftarrow \mathsf{S}.\mathsf{Sign}(sk^*,c_2^*)$ and returns $c^* = (c_2^*,\sigma^*,vk^*)$ to \mathcal{A}_2 as the challenge ciphertext. \mathcal{C}_2 continues to simulate all the oracles for \mathcal{A}_2 as above. Finally it outputs the bit b' output by \mathcal{A}_2 .

Obviously, the probability that C_2 doesn't abort in simulating ReplaceKey and RevealSecretKey oracles is at least 1/q. If C_2 doesn't abort in simulating the two oracles, the probability that it wins its own game is $\frac{1}{2}\Pr[\mathsf{Forge}_2] + \Pr[\mathcal{A}_2 \; \mathsf{Succ} \wedge \overline{\mathsf{Forge}_2}]$. Thus, we get that the advantage that C_2 wins its game is

$$\begin{aligned} \mathsf{Adv}_{\mathcal{C}_2} &= \left| \Pr[\mathcal{C}_2 \; \mathsf{Succ}] - \frac{1}{2} \right| \\ &\geq \left| \frac{1}{2} \cdot \left(1 - \frac{1}{q} \right) + \left(\Pr[\mathcal{A}_2 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_2}] + \frac{1}{2} \Pr[\mathsf{Forge}_2] \right) \cdot \frac{1}{q} - \frac{1}{2} \right| \\ &= \left| \Pr[\mathcal{A}_2 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_2}] + \frac{1}{2} \Pr[\mathsf{Forge}_2] - \frac{1}{2} \right| \cdot \frac{1}{q} \end{aligned}$$

Guaranteed by the IND-CCA2 security of PKE, we have that $Adv_{\mathcal{C}_2}$ is negligible in k. Thus, $|\Pr[\mathcal{A}_2 | \operatorname{Succ} \wedge \overline{\mathsf{Forge}_2}] + \frac{1}{2} \Pr[\mathsf{Forge}_2] - \frac{1}{2}|$ is negligible as well since 1/q is polynomial in k.

By the two lemmas above, we have

$$\begin{split} \mathsf{Adv}_{\mathcal{A}_2} &= \left| \Pr[\mathcal{A}_2 \; \mathsf{Succ}] - \frac{1}{2} \right| \\ &\leq \left| \Pr[\mathcal{A}_2 \; \mathsf{Succ} \wedge \mathsf{Forge}_2] - \frac{1}{2} \Pr[\mathsf{Forge}_2] \right| + \left| \Pr[\mathcal{A}_2 \; \mathsf{Succ} \wedge \overline{\mathsf{Forge}_2}] + \frac{1}{2} \Pr[\mathsf{Forge}_2] - \frac{1}{2} \right| \\ &\leq \frac{1}{2} \Pr[\mathsf{Forge}_2] + \left| \Pr[\mathcal{A}_2 \; \mathsf{Succ} \wedge \overline{\mathsf{Forge}_2}] + \frac{1}{2} \Pr[\mathsf{Forge}_2] - \frac{1}{2} \right| \end{split}$$

which is negligible as well. This completes the proof of Theorem 2.

The following corollary is obtained immediately from Theorem 1 and Theorem 2.

Corollary 1. The certificateless encryption scheme CLE described above is IND-ID-CCA2 secure.

4.3 Efficiency

In practice, for high performance in the encryption process, we usually use the *hybrid encryption* method which combines a public key encryption and a symmetric encryption to encrypt the message instead of using the public key encryption directly to encrypt bulk data. To apply this to our generic scheme CLE, we first generate a random symmetric key key for a secure symmetric encryption scheme SE, then use SE to encrypt m||vk| under key, and finally encrypt key using CLE. The decryption algorithm is modified accordingly. One of the key advantages of applying the hybrid encryption onto CLE (besides efficiency) is that the message space will not be restricted by the size of the verification key vk. We elaborate more on the size of vk below.

The (strong) one-time signature in our generic scheme CLE provides a certain assurance on that the encryptor did encrypt the message itself (or the 'well-formedness' of a ciphertext). Since most of the one-time signature schemes in the literature follow the 'one-way function paradigm' [9,11], the verification key and the signature are both of large size. An immediate consequence is that the message encrypted (i.e., m||vk|) and the resulting ciphertext (i.e., $c = (c_2, \sigma, vk)$) of our

scheme also suffer from the large size. We describe two methods which can significantly reduce the size in the actual implementation of CLE.

One simple solution is to replace the strong one-time signature scheme with a conventional signature scheme which is strongly unforgeable under adaptive chosen message attack. This does not weaken the security of CLE because any strongly unforgeable signature scheme is also a strong one-time signature scheme. A good candidate is the short signature proposed by Boneh and Boyen [3] as the verification key and the signature of the scheme in [3] are both small in size. The tradeoff is that the resulting scheme requires more computation than that of a strong one-time signature scheme.

Another solution is to first map the one-time verification key into a much shorter string using a collision-resistant hash function H, and then encrypt m||H(vk)| rather than m||vk|. The decryption algorithm is changed accordingly. That is, the user checks if the second part of the plaintext (decrypted from the ciphertext) is the hash of vk. To analyze the security of this modified scheme, we need to show that it is negligible for the adversary to issue a Decryption query on input ID and $c = (c_2, \sigma, vk)$ such that $vk \neq vk^*$ but $H(vk) = H(vk^*)$, where vk^* is the verification key in the challenge ciphertext. It is guaranteed by the collision-resistance property of H. This method reduces the impact on the message size by the size of the verification key while adding only slightly on the computation cost. However, the ciphertext is not much shorter than that of the original scheme.

We also observe that the verification key vk could be removed from the ciphertext without any influence on the security of the resulting encryption scheme. In addition, there is no need to use the asymmetric version of one-time signature. Instead, we can use the symmetric version - a (strong) one-time message authentication code (MAC) [5,4]. The construction of the new scheme CLE' remains the same as CLE , except that the one-time signature is replaced with a MAC. It is readily to see that CLE' enjoys better efficiency and much shorter ciphertext than CLE does.

5 Conclusion

In this paper, we considered the security of certificateless encryption schemes in the presence of a *malicious-but-passive* KGC, and proposed the *first generic* certificateless encryption scheme in *the standard model*. We also described how to use short signature or hybrid encryption to implement efficient instantiations of our generic scheme.

On the study of malicious-but-passive KGC attacks, we showed that although the scheme in [18] does not have the same key generation procedure as that of [1], there are two new attacks which can compromise the Type-II security of their scheme. In particular, our second attack allows the KGC to decrypt any ciphertext without pre-selecting a target user.

It still remains an open problem to determine the exact relationship between strong decryption oracle introduced in [1] and the malicious-but-passive KGC adversarial capability.

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A Definitions Revision

A.1 Identity-Based Encryption

An identity-based encryption scheme consists of four (probabilistic) polynomial-time algorithms, KG, Extract, Enc and Dec, which are for master key generation, user private key extraction, encrypting a message and decrypting a ciphertext, respectively. The standard and strongest notion of security of an ID-based encryption scheme is IND-ID-CCA2, which is defined by the following game between a challenger and a PPT adversary \mathcal{A} :

- 1. The challenger runs $\mathsf{KG}(1^k)$ to obtain a master public/private key pair (mpk, msk), and sends mpk to \mathcal{A} .
- 2. \mathcal{A} can adaptively issue the following two types of queries for polynomially many times:
 - Extraction: \mathcal{A} submits an identity $\mathsf{ID} \in \{0,1\}^*$, and is returned the corresponding private key $sk_{\mathsf{ID}} \leftarrow \mathsf{Extract}(msk, \mathsf{ID})$.
 - Decryption: \mathcal{A} submits an identity ID and a ciphertext c of its choice, and is returned $m \leftarrow \mathsf{Dec}(sk_{\mathsf{ID}},\mathsf{ID},c)$.
- 3. \mathcal{A} submits two equal-length messages, (m_0, m_1) along with an identity ID^* to the challenger, which then selects a bit $b \in \{0, 1\}$ at random, computes $c^* \leftarrow \mathsf{Enc}(mpk, \mathsf{ID}^*, m_b)$, and returns c^* to \mathcal{A} .
- 4. \mathcal{A} continues to issue queries as in Step 2. Finally, It outputs a bit b'.

We say \mathcal{A} wins the game if b' = b, and (1) \mathcal{A} didn't issue an Extraction query on input ID*; (2) \mathcal{A} didn't issue a Decryption query on input (ID*, c^*). We denote by $\Pr[\mathcal{A} \text{ Succ}]$ the probability that \mathcal{A} wins the game, and define \mathcal{A} 's advantage in the game to be $\mathsf{Adv}_{\mathcal{A}} = |\Pr[\mathcal{A} \text{ Succ}] - \frac{1}{2}|$.

A.2 Public Key Encryption

A public key encryption scheme consists of three (probabilistic) polynomial-time algorithms, KG, Enc and Dec, which are for key generation, encrypting a message and decrypting a ciphertext, respectively. The standard notion of security of a public key encryption scheme is IND-CCA2, which is defined by the following game between a challenger and a PPT adversary \mathcal{A} :

- 1. The challenger runs $KG(1^k)$ to obtain a public/private key pair (pk, sk), and sends pk to A.
- 2. \mathcal{A} requests to decrypt a ciphertext c of its choice, under the public key pk, and is returned $m \leftarrow \mathsf{Dec}(sk,c)$. This process can be repeated for polynomially many times.
- 3. \mathcal{A} submits two equal-length messages, (m_0, m_1) to the challenger, which then selects a bit $b \in \{0, 1\}$ at random, computes $c^* \leftarrow \mathsf{Enc}(pk, m_b)$, and returns c^* to \mathcal{A} .
- 4. \mathcal{A} continues to request to decrypt ciphertexts of its choice. Finally, \mathcal{A} outputs a bit b'.

We say \mathcal{A} wins the game if b' = b, and \mathcal{A} didn't request to decrypt c^* . We denote by $\Pr[\mathcal{A} \text{ Succ}]$ the probability that \mathcal{A} wins the game, and define \mathcal{A} 's advantage in the game to be $\mathsf{Adv}_{\mathcal{A}} = |\Pr[\mathcal{A} \text{ Succ}] - \frac{1}{2}|$.

A.3 Strong One-Time Signature

A signature scheme consists of three (probabilistic) polynomial-time algorithms, KG, Sign and Vrfy, which are for key generation, signing a message, and verifying a signature, respectively. The standard notion of the security of a signature scheme is existential unforgeability under a chosen message attack. A strong one-time signature is a signature scheme with strong existential unforgeability under a chosen one message attack, which is a security notion stronger than the standard one, and defined by the following game between a challenger and a PPT forger \mathcal{F} :

- 1. The challenger computes a one-time key pair (vk, sk) by running $(vk, sk) \leftarrow \mathsf{KG}(1^k)$, and then runs \mathcal{F} on input vk.
- 2. \mathcal{F} may issue a signing query on a single message chosen by itself, $m \in \{0,1\}^*$, under the verification key vk, and is returned a valid signature $\sigma \leftarrow \mathsf{Sign}(sk,m)$.
- 3. Finally, \mathcal{F} outputs a message/signature pair, (m^*, σ^*) , and wins the game if $(m^*, \sigma^*) \neq (m, \sigma)$ and $1 \leftarrow \mathsf{Vrfy}(vk, \sigma^*, m^*)$.

We denote by $\Pr[\mathcal{F} | \mathsf{Succ}]$ the probability that \mathcal{F} wins the game. $\mathsf{Adv}_{\mathcal{F}}$ is defined to be $\Pr[\mathcal{F} | \mathsf{Succ}]$.

B Proofs of Lemma 1 and Lemma 2

B.1 Proof of Lemma 1

Proof. We can construct a PPT algorithm \mathcal{F} to break the strong unforgeability of the underlying one-time signature scheme by using \mathcal{A}_1 as a subroutine. Given the target verification key vk^* and a one-time signing oracle \mathcal{O}_{S} , \mathcal{F} works as follows:

- 1. \mathcal{F} randomly generates the master public/private key pair by running $(mpk, msk) \leftarrow \mathsf{IBE.KG}(1^k)$, and runs \mathcal{A}_1 on input mpk.
- 2. \mathcal{F} simulates oracles RevealSecretKey, RevealPartialKey, ReplaceKey and Decryption for \mathcal{A}_1 , by its knowledge of msk. When to answer a Decryption query (ID, $c = (c_2, \sigma, vk)$), \mathcal{F} first checks if the input ciphertext c is valid and $vk = vk^*$. If so, \mathcal{F} outputs (c_2, σ) and halts; otherwise, it then behaves as the real decryptor.
- 3. At some point, \mathcal{A}_1 submits two equal-length messages (m_0, m_1) along with a target identity ID^* . \mathcal{F} randomly chooses a bit b, runs $c_1^* \leftarrow \mathsf{IBE}.\mathsf{Enc}(mpk, \mathsf{ID}^*, m_b \| vk^*)$ and $c_2^* \leftarrow \mathsf{PKE}.\mathsf{Enc}(upk_{\mathsf{ID}^*}, c_1^*)$, and then issues a signing query to \mathcal{O}_{S} to get a one-time signature σ^* on c_2^* . \mathcal{F} returns (c_2^*, σ^*, vk^*) to \mathcal{A}_1 .
- 4. \mathcal{A}_1 continues to issue queries. Again, if a Decryption query (ID, $c = (c_2, \sigma, vk)$) is valid and $vk = vk^*$, \mathcal{F} outputs (c_2, σ) as its forgery for S.
- 5. If event Forge₁ doesn't occur before A_1 produces its final output b', \mathcal{F} aborts and fails.

It is readily to see that \mathcal{F} perfectly simulates all the oracles for \mathcal{A}_1 . So event Forge_1 occurs with the same probability as it would in the real environment. On the other hand, if Forge_1 occurs, \mathcal{F} also succeeds in outputting a valid forgery for the one-time signature scheme S. Therefore, guaranteed by the strong unforgeability of S, we have that $\mathsf{Pr}[\mathsf{Forge}_1]$ is negligible in k.

B.2 Proof of Lemma 2

Proof. We now construct a PPT algorithm C_1 to break the IND-ID-CCA2 security of IBE, using A_1 as a subroutine. Given the master public key mpk, an Extract oracle \mathcal{O}_{E} and a Decryption oracle \mathcal{O}_{D} , \mathcal{C}_1 runs A_1 on input mpk. Since the generation of the verification key (in a ciphertext) is independent of the message, C_1 can randomly generate the one-time key pair, which will be used in the generation of the challenge ciphertext c^* , at the onset of the simulation. Namely, C_1 runs $(vk^*, sk^*) \leftarrow \mathsf{S.KG}(1^k)$, and stores (vk^*, sk^*) . To answer A_1 's oracle queries, C_1 maintains a list List = $\{(\mathsf{ID}, psk_{\mathsf{ID}}, upk_{\mathsf{ID}}, usk_{\mathsf{ID}})\}$ and works as follows:

- CreateUser: On input an identity ID, if ID was queried before, C_1 returns the previous answer; otherwise, it runs $(upk_{\mathsf{ID}}, usk_{\mathsf{ID}}) \leftarrow \mathsf{PKE}.\mathsf{KG}(1^k)$. It stores $(\mathsf{ID}, \bot, upk_{\mathsf{ID}}, usk_{\mathsf{ID}})$ into List and returns upk_{ID} .
- RevealSecretKey: On input an ID, C_1 looks up List for the entry of ID. If there is no such an entry, \perp is returned; otherwise, the corresponding usk_{ID} is returned.
- RevealPartialKey: On input an identity ID, C_1 searches List for the entry of ID. If there is no such an entry, \bot is returned. If $psk_{\mathsf{ID}} = \bot$, it issues a query to oracle \mathcal{O}_{E} on input ID to get the partial private key psk_{ID} and stores it. C_1 returns psk_{ID} to \mathcal{A}_1 .
- ReplaceKey: On input (ID, upk', usk'), C_1 searches List for the entry of ID. If there is no such an entry, C_1 does nothing else. If $usk' = \bot$, it sets $usk' = usk_{\mathsf{ID}}$. Then, it updates (ID, $psk_{\mathsf{ID}}, upk_{\mathsf{ID}}, usk_{\mathsf{ID}}$) to (ID, $psk_{\mathsf{ID}}, upk', usk'$).
- Decryption: On input an identity ID and a ciphertext $c = (c_2, \sigma, vk)$, C_1 first searches List for the entry of ID. If there is no such an entry, \bot is returned. Else, C_1 works as a real Decryption oracle with the only exception that if event Forge₁ occurs, it simply outputs a random bit and aborts.

At some point, \mathcal{A}_1 submits to \mathcal{C}_1 two equal-length messages (m_0, m_1) along with a target identity ID^* . \mathcal{C}_1 submits $(m_0\|vk^*, m_1\|vk^*)$ and ID^* to its own challenger which would then choose a bit b, encrypt m_b with respect to identity ID^* and return the ciphertext c_1^* . \mathcal{C}_1 then computes $c_2^* \leftarrow \mathsf{PKE}.\mathsf{Enc}(upk_{\mathsf{ID}^*}, c_1^*)$ and $\sigma^* \leftarrow \mathsf{S.Sign}(sk^*, c_2^*)$. It returns $c^* = (c_2^*, \sigma^*, vk^*)$ to \mathcal{A}_1 as the challenge ciphertext. \mathcal{A}_1 then continues to issue queries, and \mathcal{C}_1 answers as above. Note that, if \mathcal{A}_1 issues a Decryption query on input $(\mathsf{ID}^*, c = (c_2, \sigma, vk))$ where $c \neq c^*$, since \mathcal{C}_1 doesn't know the partial key psk_{ID^*} , it could not decrypt c by itself. Instead, after the decryption of c_2 , \mathcal{C}_1 issues a Decryption query to its oracle \mathcal{O}_{D} on input c_1 , and is returned $m\|vk'$. If vk = vk', \mathcal{C}_1 returns m. Finally, \mathcal{C}_1 outputs the bit b' output by \mathcal{A}_1 .

It's readily seen that C_1 perfectly simulates all the oracles for A_1 . If A_1 succeeds in guessing the bit b, then C_1 also succeeds in outputting the correct bit. (If c_2^* is a ciphertext of $m_{b'}$ in CLE setting, then $c_1^* \leftarrow \mathsf{PKE.Dec}(usk_{\mathsf{ID}^*}, c_2^*)$ is a ciphertext of $m_{b'}$ in IBE setting.) Therefore, the advantage that C_1 breaks the IND-IN-CCA2 security of IBE is

$$\mathsf{Adv}_{\mathcal{C}_1} = \left| \Pr[\mathcal{C}_1 \; \mathsf{Succ}] - \frac{1}{2} \right| = \left| \Pr[\mathcal{A}_1 \; \mathsf{Succ} \land \overline{\mathsf{Forge}_1}] + \Pr[\mathsf{Forge}_1] \cdot \frac{1}{2} - \frac{1}{2} \right|$$

By the IND-ID-CCA2 security of IBE, we have that Adv_{C_1} is negligible. The lemma is proved. \Box